Multi-scale simulations with complex automata: In-stent restenosis and suspension flow

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### Bibliography

### Samenvatting

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### Publications