Niobium diselenide has long served as a prototype of two-dimensional charge ordering, believed to arise from an instability of the electronic structure analogous to the one-dimensional Peierls mechanism. Despite this, various anomalous properties have recently been identified experimentally, which cannot be explained by Peierls-like weak-coupling theories. Here, we consider instead a model with strong electron-phonon coupling, taking into account both the full momentum and orbital dependence of the coupling matrix elements. We show that both are necessary for a consistent description of the full range of experimental observations. We argue that NbSe$_2$ is typical in this sense, and that any charge-ordered material in more than one dimension will generically be shaped by the momentum and orbital dependence of its electron-phonon coupling as well as its electronic structure. The consequences will be observable in many charge-ordered materials, including cuprate superconductors.
The charge density wave (CDW) order in 2H-NbSe$_2$ has been surrounded by controversy since its first observation nearly 40 years ago. The most basic unresolved question concerns the driving mechanism of the ordering transition. In quasi-one-dimensional (1D) materials, it is well known that charge order arises from a Peierls instability: any interaction between states at the Fermi energy ($E_F$) results in a periodic modulation of both the electronic charge density and the atomic lattice positions, which lowers the free energy through the corresponding opening of a band gap. Such a mechanism is termed weak coupling since an arbitrarily small interaction will drive the system to order at low enough temperatures. In higher-dimensional systems, a nesting of the Fermi surface is typically required for such an instability to be effective. In NbSe$_2$, however, Fermi surface nesting does not occur. The lack of a lock-in transition and the coexistence of CDW order with superconductivity below 7.2 K nonetheless seem to suggest a weak-coupling origin of the charge order. As a result, a number of alternative weak-coupling mechanisms have been proposed, based on nested saddle-points in the electronic dispersion, local field effects or a combination of weak coupling and momentum-dependent electron–phonon coupling.

There are a number of experimental observations, however, that are hard to reconcile with weak-coupling approaches in NbSe$_2$. The first concerns the size of the electronic gap in the charge-ordered state. Kinks in the density of states (DOS) observed by planar tunnelling experiments have been interpreted to arise from a gap of $\Delta = 35$ meV, while only much smaller gaps between 2 and 5 meV were seen by high-precision angle-resolved photoemission spectroscopy (ARPES) experiments, and older studies even reported no gap at all in ARPES and resistivity measurements. Assuming a weakly coupled driving mechanism for the charge order, the size of the gap is expected to be proportional to the transition temperature, $\Delta \approx 1.76k_BT_C$ in direct analogy to the BCS theory of superconductivity. A gap size of 35 meV would then be far too large to explain the observed $T_C$ of 33 K. The 5 meV gap consistent with ARPES data is of the expected size, but it occurs only in isolated points on the Fermi surface, raising the question of how the correspondingly small gain in electronic energy can overcome the cost of introducing the periodic lattice distortions associated with CDW order. In addition, while the gaps seen in ARPES measurements are connected by the CDW wave vector, other equally well-connected points support either a much smaller gap or no gap at all. It was recently suggested, based on scanning tunnelling spectroscopy (STS) measurements, that a particle–hole asymmetric gap of 12 meV, centred above $E_F$, exists in NbSe$_2$. The offset in energy explains why ARPES only sees a smaller gap size, while the value of 12 meV is consistent with the order of magnitude expected for a strongly coupled CDW, which may have $\Delta \approx 4k_BT_C$ in analogy to strong-coupling superconductors.

The idea that the CDW order in NbSe$_2$ is of the strong coupling variety, in which a sizable electron–phonon coupling is essential in causing an instability of the electronic structure, is also consistent with two further recent experimental observations. First, it was observed in X-ray scattering experiments that at the transition temperature a broad momentum-range of phonons simultaneously softens towards zero energy. This in stark contrast to the sharp Kohn anomaly expected in a Peierls-like transition and may be understood to be an effect of the importance of the entropy carried by phonon fluctuations in the strongly coupled scenario. These phonon fluctuations are localized in real space and therefore necessarily involve a broad range of momenta. In an electronically nested system, on the other hand, the nesting vector localizes any fluctuations to a single point in momentum space. The second experimental result arguing for a strongly coupled transition is the observation of a reduction of the density of states persisting well above the transition temperature, in what has been termed a pseudogap regime. In strongly coupled CDW materials, a pseudogap typically appears through the presence of locally fluctuating charge order without long-range coherence. These same charge fluctuations have recently been suggested to play a central role in the description of the pseudogap phase of cuprate superconductors. The precise nature of the pseudogap in these materials, however, is difficult to establish owing to the presence of various nearby competing orders. NbSe$_2$, being free of such complications, provides a test bed on which the formation and characteristics of a pseudogap phase due to charge fluctuations can be studied directly.

Here we present a theoretical analysis of the charge order in NbSe$_2$ based on a model of strong electron–phonon coupling. Although the transition is phonon driven, we find that a full knowledge of the electronic states scattered from and to, including both wave vector and orbital dependence, is crucial in explaining the experimental data. Despite a lack of nesting, the limited matching of states at $E_F$ acts in unison with the momentum dependence of the electron–phonon coupling to select out the CDW-ordering vector, while the orbital characters of the bands naturally explain why a CDW gap appears primarily in only one of the Fermi surface pockets. The resulting momentum dependence of the gap itself agrees with ARPES experiments as well as with the observed particle–hole asymmetry in the DOS. Finally, we find that the phonon modes are softened over a broad range of wave vectors, and that including the presence of strong phonon fluctuations leads to a suppression of the transition temperature, implying a range of intermediate temperatures dominated by incoherent, fluctuating, charge order and a corresponding pseudogap. In light of these findings, and the generic nature of the electronic structure of NbSe$_2$, we argue that the momentum and orbital dependence of the electron–phonon coupling may be expected to play a similarly central part in the description of other charge-ordered materials, especially in the presence of relatively strong coupling as in the case of the layered high-$T_C$ superconductors.

Results

The extent of electronic nesting. NbSe$_2$ is a layered material, in which hexagonal layers of niobium atoms are sandwiched between similar layers of selenium atoms, displaced so that they lie above and below half of the Nb interstitial locations, as shown in the inset of Fig. 1. Consecutive sandwich layers are displaced to have the complementary half of the interstices occupied, giving two formula units per unit cell. The Fermi surface consists of two concentric barrel-shaped pockets centred around both the $\Gamma$ and the $K$ points, as well as a very small pancake-shaped pocket surrounding $\Gamma$, which we ignore in the analysis below. The inner pockets at $K$ are seen in ARPES to develop the largest CDW gaps. The CDW itself is of the 3Q type, with three equivalent superposed modulations at 120° with respect to one another.

To describe the electronic states, we employ a Slater–Koster tight-binding fit to the band structure using a basis of Se-4p and Nb-4d orbitals. For the two main bands crossing $E_F$ that give rise to the barrel-shaped pockets (which we will refer to as inner, developing the CDW instability, and outer), the fit is constrained by data from ARPES measurements, while the remaining 20 bands are fit to recent LDA calculations. In agreement with earlier reports, we find that both the inner and outer bands at $E_F$ are primarily composed of the $d_{3x^2-r^2}$ and $d_{5x^2}$ orbitals centred on the Nb atoms within a unit cell, in the form of bonding (inner) and antibonding (outer) combinations (as shown in Fig. 1).
bonding and antibonding combinations of the two niobium resulting from the two bands crossing negative parts of the orbital wave functions. (within a unit cell, as indicated (with red and blue signifying postive and negative parts of the orbital wave functions). (Figure 1 | Model band structure of NbSe2. (a) The band structure of NbSe2 modelled by a tight-binding fit to both ARPES data and first-principles band structure calculations. The two bands crossing \( E_F \) (thick lines) are the ones involved in the formation of charge order. They consist of bonding and antibonding combinations of the two niobium \( d_{xy} \) orbitals within a unit cell, as indicated (with red and blue signifying positive and negative parts of the orbital wave functions). (b) The Fermi surface resulting from the two bands crossing \( E_F \). (c) The layered atomic structure of NbSe2, with Nb in red and Se in blue. The unit cell, containing two formula units across consecutive sandwich layers, is indicated.

Focussing on the two non-interacting bands at \( E_F \), we introduce the interaction between electrons \( \psi \) and phonons \( \varphi \):

\[
\hat{H}_{\text{int}} = \sum_{m,n} \sum_{k,q} \delta_{k,k}^{m,n} \psi_k^{m} \varphi_k^{n} \psi_{k+q}^{n} + \text{h.c.}
\]

(1)

The bare phonon dispersion can be described by a Brillouin function tending to a maximum of 11.2 meV at the zone boundary. The electron–phonon coupling \( g \) depends on the momenta, as well as the band indices \( m \) and \( n \), of the ingoing and outgoing electron states. Following Varma et al., we model both of these dependencies using knowledge purely of the electronic structure, which has been shown to work well for a range of transition metals and their compounds. In terms of the matrices of tight-binding overlap integrals \( S_k \) and generalized eigenvectors \( A_k \), the electron–phonon coupling matrix elements are given by:

\[
\delta_{k,k}^{m,n} = \nu_k^m [A_k^S S_k A_k]^{mn} - [A_k^S S_k A_k]^{mn} \nu_k^n.
\]

(2)

where a constant prefactor has been omitted, and the band velocity \( \nu_k^m \) for electrons in band \( n \) is defined in terms of the band energy \( \varepsilon_k^m \) as \( \nu_k^m = \partial \varepsilon_k^m / \partial k \). In the interaction of equation (1) we restrict attention to the longitudinal component of \( g \), since only the longitudinal acoustic phonons are observed to soften in inelastic neutron and X-ray scattering experiments.

Inserting the tight-binding results into equation (2), we find that the interband electron–phonon coupling is strictly zero, while the intraband coupling is about a factor of three stronger for the inner band than for the outer. This result immediately explains why the experimentally observed CDW gap is so much more pronounced in the inner band, indicative of a negligible role of the electronic structure. Black solid curve: the evolution of the susceptibility to be entirely independent. This means that the lower value of the intraband coupling in the outer band leads to an order of magnitude suppression of its contribution to \( \chi_0 \) and therefore to a correspondingly reduced gap in its Fermi surface pocket. It is thus the orbital character of the electronic bands, and consequently the orbital dependence of the electron–phonon coupling, that causes a relative size difference between the CDW gaps in the pockets around the K-point, even if they are equally well nested.

The expression for the susceptibility in equation (3) can further be used to quantify both the amount of nesting present in NbSe2, and to evaluate the relative contribution of the electron–phonon coupling matrix elements in selecting the observed value of the (incommensurate) ordering wave vector \( \mathbf{Q}_{\text{CDW}} = (1 - \delta \frac{1}{2}) \Gamma M \), with \( \delta \approx 0.02 \). In the left panel of Fig. 2, three susceptibilities are compared. The dotted blue line shows the susceptibility for a perfectly nested model with a single 1D band of cosine dispersion. The sharp peak characteristic of a nested Fermi surface is apparent. The dashed red line is the bare susceptibility in NbSe2, obtained by setting \( g = 1 \) in equation (3). This does not include any of the momentum and orbital dependence of the electron–phonon coupling and is the form that has been widely used in previous studies. It is almost completely flat except for a very broad and low maximum far from \( \mathbf{Q}_{\text{CDW}} \), and can therefore not explain the observed ordering vector. The solid black line, on the other hand, displays the susceptibility of just the inner band. A broad but distinct maximum develops at the experimentally observed CDW vector. The selection of the ordering vector is thus shown to arise from the combined influence of both the electronic structure and the orbital and momentum-dependent electron–phonon coupling, with neither contribution being negligible.

Here \( f(\xi) \) is the Fermi–Dirac distribution function, and the static Lindhard function is given by \( \chi_0 \) when \( g = 1 \). The absence of interband coupling causes the contributions of the two bands to

Figure 2 | Quantifying the extent of nesting in NbSe2. (a) Electronic susceptibility as a function of momentum transfer along \( \Gamma M \). Here \( \mathbf{q} \) is defined through \( \mathbf{q} = q \mathbf{Q}_{\text{CDW}} \), with \( q \in [0,1] \). Blue dotted line: in a perfectly nested 1D band structure, the susceptibility is sharply peaked at \( \mathbf{q} = \mathbf{Q}_{\text{CDW}} \). Red dashed curve: the result for the two bands in NbSe2 crossing \( E_F \), and an orbital-independent electron-phonon coupling. The susceptibility is nearly flat, without any peaks. Black solid curve: the susceptibility of just the inner band, in which a CDW gap is observed. Although a clear maximum can be seen at \( \mathbf{Q}_{\text{CDW}} \) it is not a sharp divergence indicative of perfect nesting. (b) The model electron-phonon coupling \( g = -\delta q^2 - \frac{q^2}{2} + \Delta_{\text{max}} \) as \( \mathbf{q} \) is varied along \( \Gamma M \). (c) Evolution of the CDW vector \( \mathbf{Q}_{\text{CDW}} \) with varying peak position \( q_0 \) of the model electron-phonon coupling. Blue dotted line: in a perfectly nested 1D band structure, the electronic structure determines the CDW formation and \( \mathbf{Q}_{\text{CDW}} \) is independent of \( q_0 \). Red dashed curve: the result for an orbital-independent electron-phonon coupling and the two bands crossing \( E_F \), which is close to a straight line at 45°, indicative of a negligible role of the electronic structure. Black solid curve: the evolution relevant for NbSe2, given by just the inner band as imposed by the orbital-dependent electron-phonon coupling. This curve interpolates between the flat plateau of a perfectly nested structure, and the 45° line dominated by just the structure of the electron-phonon coupling.
Restricting attention to the inner band, we can quantify the extent to which nesting contributes to the selection of \( \mathbf{Q}_{\text{CDW}} \). For this purpose we temporarily switch to a simplified form of \( g \), which is a function only of the momentum transfer: 
\[
g = -a(q_i - Q_i)^2 + g_{\text{max}}
\]
Even though in general the shape of the susceptibility is determined by both the incoming momentum and the momentum transfer, modelling the electron–phonon coupling in this simplified form allows us to directly quantify the effect of varying the position of its peak, and thus its influence on the position of the peak in \( g_0 \). The values of the parameters \( a, q_0 \) and \( g_{\text{max}} \) can be estimated by fitting the experimentally observed phonon softening to the expression for the renormalized phonon energy in the random phase approximation (RPA), \( \Omega_{\text{RPA}}^2 = \Omega_0(\Omega_0 - 2g_0) \), where we take \( \Omega_0 \) to be the high-temperature (unrenormalized) dispersion. In the right panel of Fig. 2 we plot the variation of the maximum in the susceptibility (that is, the expected \( \mathbf{Q}_{\text{CDW}} \)) as \( q_i \) is varied along \( \Gamma M \). Again, the blue dotted line represents the situation of a perfectly nested band structure, in which the electron–phonon coupling never overcomes the peak in the susceptibility, and thus has no effect on \( \mathbf{Q}_{\text{CDW}} \). The red dashed line has the same form of \( g \) for all bands, and is close to a straight line at 45° (grey dashed line). A true 45° line would indicate that \( \mathbf{Q}_{\text{CDW}} = q_i \), implying that the CDW vector is completely determined by the electron–phonon coupling, with the electronic structure having no influence at all. The solid black line, which shows the behaviour of just the inner band, interpolates between these two extremes. There is no plateau, but there is an indication of some flattening, suggesting that while it is mainly the momentum dependence of the electron–phonon coupling that determines the value of CDW-ordering vector, the role of the electronic structure cannot be neglected entirely.

The CDW gap. Having identified the importance of both electron–phonon coupling and electronic structure, we now revert to using the full expression of equation (2). To compare the size and shape of the CDW gap resulting from the orbital- and momentum-dependent \( g \) to the experimentally observed behaviour, the RPA gap equations shown diagrammatically in Fig. 3 are solved self-consistently. We simplify the calculation by using the 9 × 9 gap matrix which includes all higher harmonics appropriate for a commensurate CDW wave vector at \( \mathbf{Q} = \frac{1}{2} \Gamma M \), as an approximation for the gap matrix of the incommensurate CDW in NbSe₂ with \( \mathbf{Q}_{\text{CDW}} \simeq 0.98 \frac{1}{2} \Gamma M \). We further fix the values of the electronic self-energies to 7 meV, approximating the self-consistent result across \( k \) in the high-temperature phase, and constrain the momentum dependence of the gap function to a five parameter tight-binding fit consistent with the symmetries of the lattice. A self-consistent solution for the gap function to all orders in RPA can then be found by searching for a fixed point in the flow of consecutive iterations of the gap equation.

Figure 4 shows energy and momentum cuts through the electronic spectral functions resulting from the solution to the gap equations, as well as their corresponding DOS. A good match with the shape of the experimentally determined DOS in STS experiments can be achieved by introducing a 4 meV shift in the chemical potential, which falls well within the range of experimental uncertainty. The overall strength of the electron–phonon coupling, the constant of proportionality omitted in equation (2) and the only free parameter in the theory, is set to give a maximum CDW gap magnitude of \( \sim 12 \text{ meV} \). The Fermi surface on the right of Fig. 4 then shows a CDW gap opening on the inner band only, and Fermi arcs forming at the same locations as observed in ARPES measurements. The extent of the gap on the Fermi surface, its size (apparent from the dispersion’s back-folding in the centre of Fig. 4) and its restriction to one band are all in agreement with experimental findings. The plot of the DOS on the left indicates that these results, which were previously interpreted to imply a gap size of \( \sim 5 \text{ meV} \), are in fact consistent with the STS results indicating a particle–hole asymmetric gap of \( \sim 12 \text{ meV} \).

The asymmetry hides most of the gap structure above \( E_F \), where photoemission intensity is suppressed by the Fermi–Dirac distribution. The comparison between the experimental STS data and the calculated RPA results shows that the particle–hole asymmetry arises naturally from the interplay between the electronic structure and the momentum-dependent electron–phonon coupling.

The pseudogap. The central role of the orbital- and momentum-dependent electron–phonon coupling in determining both the CDW propagation vector and the structure of the gap suggests that the charge order in NbSe₂ falls in the strong-coupling regime, in which the electronic structure alone is not sufficient to characterize the emergent charge order. In the presence of strong electron–phonon coupling, it is well known that the entropy associated with localized lattice vibrations plays an essential part in the system’s thermal evolution. To understand the properties of NbSe₂ above its CDW transition temperature, it is therefore necessary to consider the influence of phonon fluctuations beyond RPA. The so-called mode–mode coupling approximation (MMA) includes the lowest order terms of this type and has been shown to successfully describe the influence of phonon fluctuations in some of the electronic properties of related dichalcogenide materials like TaSe₂ and TiSe₂. The additional terms included in the MMA fall into two categories: a vertex correction, which we neglect by appeal to Migdal’s theorem because of the large momentum transfer associated with \( \mathbf{Q}_{\text{CDW}} \), and self-energy corrections to the internal electron lines (indicated diagrammatically in Fig. 5), which we include. In agreement with recent X-ray scattering observations on NbSe₂, the MMA-renormalized phonon spectrum shown in Fig. 5b shows a broad range of phonon modes softening near the

Figure 3 | The RPA gap equation. Diagrammatic form of the self-consistent RPA gap equations. As indicated in the legend, the single arrows indicate bare electronic Green’s functions \( G_0 \), and the double arrows the renormalized Green’s functions \( G \) and \( \mathcal{F} \). The anomalous functions \( \mathcal{F}(\mathbf{k}, \mathbf{k} + \mathbf{Q}_i) = \langle \phi_i \bar{\psi}_{\mathbf{k}+\mathbf{Q}_i} \rangle \) do not conserve crystal momentum, and correspond to the CDW order parameter. Notice that the momentum labels for the Green’s functions include Matsubara frequencies, and the final diagram includes a summation over the anomalous momentum \( Q_i \) of the internal electronic propagator.
Figure 4 | Comparison to experimental results. (a) The calculated density of states for the bare dispersion (black line) and renormalized dispersion (red line) compared with experimental results from STS measurements (blue points)\(^4,24\). The opening of the CDW gap leads to an asymmetric suppression of the density of states, centred above \(E_F\). (b) The dispersion of the calculated spectral functions along MK, with the colour scale indicating intensity in arbitrary units. The back-bending induced by the gap at \(E_F\) is apparent in the band corresponding to the inner pocket about \(K\). (c) Fermi energy cut of the spectral function resulting from the self-consistent gap equations, showing the formation of Fermi arcs as a result of gaps opening along MK. Again the colour scale indicates intensity in arbitrary units. Below the dashed line the bare bands are shown for comparison. Note that the outer band develops no discernible gap; this can be compared directly with the results of recent ARPES measurements\(^6,10\).

Figure 5 | Phonon dispersion in NbSe\(_2\). (a) The solid black line indicates the bare phonon dispersion as a function of momentum along \(\Gamma M\), based on high-temperature X-ray scattering results\(^19\). Here \(q\) is defined through \(q = qfM\), with \(q\in[0,1]\). The blue dotted curve shows the dispersion resulting from the (mean field) RPA calculation at \(T_RPA = 303.5\) K, while the red dashed curve represents the MMA prediction at the same temperature (including the phonon fluctuations as shown in the diagrammatic representation of the renormalized phonon propagator). Both calculations are based on the same tight-binding band structure. The fluctuations of the phonon field can be seen to suppress the onset of charge order predicted by the RPA theory. (b) The MMA dispersion at \(T_{MMA} = 33.5\) K, which represents the true transition temperature. It can be seen that the momentum of the softest phonon mode corresponds to the experimentally observed CDW propagation vector.

transition temperature, rather than the sharp Kohn anomaly indicative of well-nested materials. The momentum of the softest phonon mode at the transition temperature coincides with the experimentally observed CDW propagation vector.

The softening of phonon modes, as the charge-ordered state is approached from high temperatures, is suppressed by the fluctuations beyond RPA. Since the temperature at which the first phonon mode reaches zero energy defines the transition temperature \(T_{CDW}\), this means that the charge-ordering transition temperature in MMA, \(T_{MMA}\), is suppressed with respect to the corresponding value in RPA, \(T_{RPA}\). Choosing the overall strength of the electron–phonon coupling such that \(T_{MMA}\) matches the experimentally observed value of \(T_{CDW} = 33.5\) K, Fig. 5 shows that the corresponding RPA transition occurs already at \(T_{RPA} \approx 300\) K. Physically, this suppression of the transition temperature can be ascribed to the presence of fluctuations in the phonon field. In the temperature range \(T_{MMA} < T < T_{RPA}\), the phonon fluctuations are strong enough to destroy the long-range order predicted by (mean field) RPA theory. In that regime, the amplitude of the static order parameter vanishes, \(\langle \phi_Q \rangle = 0\), but dynamic fluctuations of the order parameter persist, \(\langle |\phi_Q| \rangle > 0\)\(^22\). The result is a locally fluctuating short-range ordered state, characterized by the presence of a non-zero order parameter amplitude, without any long-range phase coherence\(^23\). Due to the non-zero amplitude, the gap in the electronic structure will survive even above the transition temperature \(T_{CDW} = T_{MMA}\), in the form of a pseudogap phase\(^4,23\). The dynamical fluctuations in this regime may become locally pinned in the presence of defects, creating islands of order up to \(T = T_{RPA} \approx 300\) K, in agreement with recent STM and X-ray scattering experiments\(^23,24\). The properties of this regime are reminiscent of the features that characterize the pseudogap phase of cuprate high-temperature superconductors\(^35\), which have recently been shown typically to contain charge-ordered phases of their own\(^28–30\). Specific similarities are the presence of a pseudogap, Fermi surface arcs, dynamical fluctuations and a corresponding sensitivity to the timescales employed by experimental probes, as well as the existence of the crossover to the normal state at \(T \approx T_{RPA}\). Note that the existence of a crossover temperature \(T \approx 300\) K, between the pseudogap and disordered regimes predicted here, falls outside of the temperature range that has been probed in NbSe\(_2\) to date\(^4,24\).

Discussion

Although various theories for the formation of charge order in NbSe\(_2\) have been able to explain many parts of its diverse experimental signatures, the material has so far evaded the simultaneous description of all of its properties by a single consistent theoretical account. The main features, which remain difficult to reconcile with the weak-coupling theories considered so far, include the emergence of CDW order in spite of a lack of nesting in the electronic structure, and an anomalously flat electronic susceptibility, the softening of a broad range of phonon modes rather than a sharp Kohn anomaly, a discrepancy in the sizes of the CDW gap observed in different electron pockets in spite of them being similarly nested, disagreement about the existence, size and particle–hole symmetry of the CDW gap as seen by different experimental probes and the presence of a pseudogap phase characterized by locally fluctuating charge order above the CDW transition temperature. We have shown here that all of these observations can be consistently understood, within a single theory, to result from the simultaneous influence of the presence of a strong electron–phonon coupling, its orbital dependence and its dependence on both incoming and outgoing...
electron momentum. We have shown that none of these ingredients can be neglected in the full description of NbSe$_2$, suggesting possible importance in other dichalcogenide materials as well.

The combination of both the momentum-dependent coupling and the particular electronic structure of NbSe$_2$ is found to be crucial in the selection of the charge-ordering vector, while the orbital dependence naturally explains the different behaviours of different Fermi surface pockets. The same dependencies on orbital dependence naturally explains the different behaviours of...