Gamma-ray observations of MAXI J1820+070 during the 2018 outburst

Abe, H.; The MAGIC collaboration; Abdalla, H.; Berge, D.; Prokhorov, D.A.; Prokoph, H.; Vink, J.; The H.E.S.S. collaboration; Acharyya, A.; The VERITAS Collaboration; Bosch-Ramon, V.; Celma, C.; Linares, M.; Russell, D.M.; Sala, G.

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H. Abe,1 S. Abe,1 V. A. Acciari,2 T. Aili,2 3 S. Ansoldi,4* L. A. Antonelli,3 A. Arbet Engels,5
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* E-mail: contact.magic@mpp.mpg.de (JH, EM); contact.hess@hess-experiment.eu (SLS, DM); nahee.park@queensu.ca (NP)
† Now at: University of Innsbruck, Institute for Astro and Particle Physics.
‡ Now at: Universitat de Barcelona (UPF), Alan Turing Institute (ATi), Spain.
§ Now at: University of Innsbruck, Institute for Astro and Particle Physics.
|| Now at: University of Innsbruck, Institute for Astro and Particle Physics.
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Affiliations are listed at the end of the paper

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ABSTRACT

MAXI J1820+070 is a low-mass X-ray binary with a black hole (BH) as a compact object. This binary underwent an exceptionally bright X-ray outburst from 2018 March to October, showing evidence of a non-thermal particle population through its radio emission during this whole period. The combined results of 59.5 h of observations of the MAXI J1820+070 outburst with the H.E.S.S., MAGIC and VERITAS experiments at energies above 200 GeV are presented, together with Fermi-LAT data between 0.1 and 500 GeV, and multiwavelength observations from radio to X-rays. Gamma-ray emission is not detected from MAXI J1820+070, but the obtained upper limits and the multiwavelength data allow us to put meaningful constraints on the source properties under reasonable assumptions regarding the non-thermal particle population and the jet synchrotron spectrum. In particular, it is possible to show that, if a high-energy (HE) gamma-ray emitting region is present during the hard state of the source, its predicted flux should be at most a factor of 20 below the obtained Fermi-LAT upper limits, and closer to them for
magnetic fields significantly below equipartition. During the state transitions, under the plausible assumption that electrons are accelerated up to \( \sim 500 \) GeV, the multiwavelength data and the gamma-ray upper limits lead consistently to the conclusion that a potential HE and very-HE gamma-ray emitting region should be located at a distance from the BH ranging between \( 10^{11} \) and \( 10^{13} \) cm. Similar outbursts from low-mass X-ray binaries might be detectable in the near future with upcoming instruments such as CTA.

**Key words:** stars: individual: MAXI J1820+070 – gamma rays: general – stars: black holes – X-rays: binaries.

1 INTRODUCTION

X-ray binaries are systems in which a compact object – either a black hole (BH) or a neutron star – accretes matter from a companion star. In low-mass X-ray binaries, the companion mass is below \( \sim 1 \) M\(_{\odot}\), and accretion on to the compact object normally takes place through accretion disc generated by the Roche lobe overflow mechanism (e.g. Remillard & McClintock 2006). Typically, low-mass X-ray binaries with a BH (BH-LMXBs) also feature transient jets launched from the BH, which are powered by the accretion process, the magnetic field, the BH rotation, or a combination of them (see Romero et al. 2017, and references therein). These jets can efficiently accelerate charged particles, potentially up to GeV or TeV energies, and emit non-thermal radiation from radio to gamma rays as a result of the radiative cooling of the accelerated particles (see e.g. Mirabel & Rodríguez 1999; Fender & Muñoz-Darias 2016, for a review on jets in X-ray binaries).

Most of the time, BH-LMXBs are in a quiescent state until they undergo periodic outbursts likely triggered by variations in the properties of the accretion disc that result in a change of the mass accretion rate on to the BH (e.g. Fender & Belloni 2012). During one of these outbursts, which may last for several months, the luminosity of a BH-LMXB increases by several orders of magnitude. A BH-LMXB can be detected in a soft state (SS) or a hard state (HS) based on the hardness of its X-ray spectrum during one of these outbursts. At the beginning of the outburst, a BH-LMXB is typically in the HS, in which the X-rays exhibit a hard-spectrum component. This emission likely originates in a hot corona around the BH, where inverse Compton (IC) scattering of low-energy photons coming from the accretion disc takes place. The HS also features jet synchrotron emission, which is mostly seen at radio and infrared wavelengths, although it may also be responsible for a significant contribution to the X-ray output of the system (e.g. Fender & Muñoz-Darias 2016). As the outburst continues, the source will transition to the SS. In this state, most of the X-rays are of thermal origin, emitted by the hot inner regions of the accretion disc. Also, radio emission fades away, indicating a lack of jet activity (although weak jets may still be present and remain undetected). In a typical outburst, a BH-LMXB normally completes the HS–SS–HS cycle, going through short-lived intermediate states during the HS–SS and SS–HS transitions. As happened with the triggering of the outburst, the changes in the spectral states of BH-LMXBs are probably produced by variations in the accretion disc properties. During the state transitions, especially the HS–SS one, discrete blobs of plasma moving away from the BH can sometimes be resolved in radio, rather than the continuous jets typical of the HS (see Fender & Belloni 2012, and references therein for a more detailed description of the states of BH-LMXBs).

With one possible exception, no high-energy (HE, above 100 MeV) or very-high-energy (VHE, above 100 GeV) gamma-ray emission is detected from BH-LMXBs (Ahnen et al. 2017a; H.E.S.S. Collaboration et al. 2018b). The possible exception to this is the \( \sim 4\sigma \) excess reported by a recent reanalysis of the Fermi-LAT data; Harvey, Rulten & Chadwick 2021. A firm detection of BH-LMXBs at HE or VHE would enable a better physical characterization of these systems in terms of their magnetic field, particle acceleration mechanisms and maximum particle energy, or gamma-ray absorption processes, among others. We note that LMXBs hosting a neutron star have been detected at HE (see e.g. Harvey, Rulten & Chadwick 2022). In these systems, the gamma-ray emission likely originates in processes involving the neutron star, which are therefore not applicable in a BH scenario (e.g. Strader et al. 2016, and references therein).

For high-mass X-ray binaries, there is already evidence for gamma-ray emission. HE gamma rays are detected from systems like Cygnus X-1 and Cygnus X-3, likely originating from the jets in both cases (see Fermi LAT Collaboration et al. 2009; Tavani et al. 2009; Zanin et al. 2016; Zdziarski et al. 2018). HE emission is also detected from regions of SS433 far from the central binary, where the jets terminate interacting with the supernova remnant around the source (Fang, Charles & Blandford 2020; Li et al. 2020). On the other hand, the VHE detection of high-mass X-ray binaries is still elusive (Aleksić et al. 2010, 2015; Archambault et al. 2013; Archer et al. 2016; Ahnen et al. 2017b), with the exception of SS433 (and excluding gamma-ray binaries from this source class). For this source, the HAWC Collaboration detected photons with energies of \( \sim 20 \) TeV originating in regions very far from the binary system, although not spatially coincident with the HE-emitting sites. The post-trial detection significance ranged from 4.0 to 4.6\( \sigma \) depending on the analysed region, and reached 5.4\( \sigma \) for a joint fit of the interaction regions (Abeyesekara et al. 2018). MAXI J1820+070 (RA = 18h29m21.9s, Dec. = +07°11’07”; Galactic coordinates \( l = 35°85′36″, b = +10°15′92″ \)) is a BH-LMXB discovered in the optical band on 2018 March 6 (MJD 58184.1) by the All-Sky Automated System for Supernovae (ASAS-SN; Tucker et al. 2018), and on March 11 (MJD 58188.5) was also detected in X-rays by the Monitor of All-sky X-Ray Image (MAXI; Kamiwaku et al. 2018). Soon after its discovery, MAXI J1820+070 showed an exceptionally high X-ray flux peaking at \( \sim 4 \) times that of the Crab Nebula (e.g. Del Santo & Segreto 2018; Shidatsu et al. 2019). A distance to the source of \( d = 2.96 \pm 0.33 \) kpc was determined from radio parallax (Atri et al. 2020), which is consistent with the distance of \( 3.28^{+0.65}_{-0.60} \) kpc obtained from Gaia DR3 data (Bailer-Jones et al. 2021). Jet activity was detected from MAXI J1820+070 in the form of radio and infrared emission, which classifies the source as a microquasar (e.g. Bright et al. 2020; Ridi et al. 2021). The Lorentz factor of the jet during the HS was estimated to be \( \Gamma = 1.7–4.1 \) from radio-to-optical data, the upper and lower limits of this range being determined from constraints on the jet power and the pair production rate, respectively (Zdziarski, Tetarenko & Sikora 2022). For discrete ejections taking place in the HS–SS transition, a Lorentz factor of \( \Gamma = 2.2^{+2.3}_{-0.7} \) was obtained (using a distance to the source of \( 2.96 \) kpc; Atri et al. 2020). The jet inclination was measured to be \( \theta = 64° \pm 5° \) from radio observations (Wood et al. 2021), and its half-opening angle in the HS was found to be \( 1.3° \pm 0.7° \) (Zdziarski et al. 2022). Using optical polarization observations, the jet misalignment with...
Table 1. Starting and ending times used for each X-ray state of MAXI J1820+070, based on the results of Shidatsu et al. (2019). Hard State I and II refer, respectively, to the initial and final states of the source, as depicted in Fig. 1.

<table>
<thead>
<tr>
<th>Source state</th>
<th>Start (MJD)</th>
<th>End (MJD)</th>
<th>Start (Gregorian)</th>
<th>End (Gregorian)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Hard State I</td>
<td>58189.0</td>
<td>58303.5</td>
<td>12 Mar. 2018</td>
<td>4 Jul. 2018</td>
</tr>
<tr>
<td>HS → SS</td>
<td>58303.5</td>
<td>58310.7</td>
<td>4 Jul. 2018</td>
<td>11 Jul. 2018</td>
</tr>
<tr>
<td>Soft State</td>
<td>58310.7</td>
<td>58380.0</td>
<td>11 Jul. 2018</td>
<td>19 Sep. 2018</td>
</tr>
<tr>
<td>SS → HS</td>
<td>58380.0</td>
<td>58393.0</td>
<td>19 Sep. 2018</td>
<td>2 Oct. 2018</td>
</tr>
<tr>
<td>Hard State II</td>
<td>58393.0</td>
<td>58420.0</td>
<td>2 Oct. 2018</td>
<td>29 Oct. 2018</td>
</tr>
</tbody>
</table>

respect to the perpendicular to the orbital plane was measured to be at least 40° with a 68 per cent confidence level (CL); Poutanen et al. 2022]. An orbital period of 16.4518 ± 0.0002 h was determined from optical spectroscopic observations (Torres et al. 2019). The BH and stellar masses were constrained through further spectroscopy measurements to a 95 per cent confidence interval of 5.7–8.3 and 0.28–0.77 M⊙, respectively, for orbital inclinations between 66° and 81° (Torres et al. 2020). The parameters above yield an orbital semimajor axis of ~4.5 × 10¹⁴ cm. An estimate of the donor star parameters is discussed in Mikolajewska et al. (2022).

MAXI J1820+070 remained in the HS from the beginning of the outburst in March until early July 2018, when it began its transition to the SS. This source state lasted until late September, when MAXI J1820+070 started transitioning back to the HS shortly before becoming quiescent and putting an end to the outburst, which lasted a total of ~7 months. During its outburst, MAXI J1820+070 was observed with a wide variety of instruments at radio (e.g. Atri et al. 2020; Bright et al. 2020), near-infrared (e.g. Sánchez-Sierra & Muñoz-Darias 2020), optical (e.g. Shidatsu et al. 2019; Torres et al. 2019; Veledina et al. 2019), and X-ray (e.g. Buisson et al. 2019; Roques & Jourdain 2019; Shidatsu et al. 2019; Chakraborty et al. 2020; Fabian et al. 2020; Zdziarski et al. 2021) frequencies. We make use of the results of Shidatsu et al. (2019) to define the exact dates of the beginning and end of each source state, based on the MAXI Gas Slit Camera (MAXI/GSC) hardness ratio (i.e. the flux ratio of HE to low-energy X-rays) between the 6–20 and 2–6 keV photon fluxes. These dates are shown in Table 1. The evolution of the X-ray state of MAXI J1820+070 can be seen in the bottom panel of Fig. 1, which shows its hardness ratio from MAXI/GSC data.

In this work, we present the results of combined observations, by the H.E.S.S., MAGIC, and VERITAS collaborations, of VHE gamma rays from MAXI J1820+070, the brightest BH-LMXB in X-rays ever observed. In order to give a more complete picture of the source, Fermi-LAT data in HE gamma rays are also included, as well as mult wavel e ngth observations from radio to X-rays. This work is structured as follows: Section 2 describes the HE and VHE observations and data analysis for each telescope. Section 3 presents the results of this work, for which a discussion is given in Section 4. Finally, we conclude with a summary in Section 5.

2 OBSERVATIONS AND DATA ANALYSIS

2.1 H.E.S.S., MAGIC, and VERITAS data

MAXI J1820+070 was observed during its 2018 outburst with the H.E.S.S., MAGIC, and VERITAS Imaging Atmospheric Cherenkov Telescope (IACT) arrays. H.E.S.S. is an array of five IACTs located in the Khomas Highland, Namibia (23° S, 16° E, 1800-m above sea level). It comprises four telescopes with a 12-m diameter dish and a field of view (FoV) of 5° (for a description, see Aharonian et al. 2006a), and one telescope with a 28-m diameter dish and a 3:2 FoV (Bolmont et al. 2014). H.E.S.S. investigates gamma rays in the energy range from ~20 GeV (H.E.S.S. Collaboration et al. 2018a) to ~100 TeV (Abdalla et al. 2021). MAGIC (Aleksic et al. 2016a) is a stereoscopic system of two IACTs located at the Roque de los Muchachos Observatory in La Palma, Spain (29°N, 18°W, 2200 m above sea level). The telescopes have a 3:5 FoV, and are equipped with a primary dish with a diameter of 17 m. MAGIC can detect gamma rays from ~15 GeV (MAGIC Collaboration et al. 2020b) to ~100 TeV (MAGIC Collaboration et al. 2020a). VERITAS is an array of four IACTs located at the Fred Lawrence Whipple Observatory in southern Arizona, USA (32°N, 111°W, 1270 m above sea level; Weekes et al. 2002). Each telescope covers a FoV of 3:5, collecting light from a 12-m diameter reflector. VERITAS is sensitive to gamma-ray photons ranging from ~85 GeV to ~30 TeV. The performance of VERITAS is described in Park et al. (2015).

The MAGIC and H.E.S.S. observations were performed from 2018 March to October, covering the initial HS of the source, the beginning of the SS, and the state transitions. The VERITAS data were collected from March to June, when the source was in the HS. After data quality cuts, 26.3, 22.5, and 10.7 h of effective observation time (defined as the exposure time corrected for dead-time losses) remains for H.E.S.S., MAGIC, and VERITAS, respectively, for a combined total of 59.5 h. The data sample was divided according to the X-ray state (or transition) of the source as defined in Section 1. A summary of the observations, including their zenith angle, is shown in Table 2.

The observation dates of each telescope are shown in Table A1, and they are also represented in Fig. 1 superimposed on the hard X-ray light curve (LC) of the source.

The low-level data analyses of H.E.S.S., MAGIC, and VERITAS were performed using standard collaboration procedures, each of them including an independent cross-check (i.e. an independent analysis, performed with a different software pipeline, that yielded compatible results with the main analysis). These low-level analyses comprise, among others, calibration, and image cleaning procedures, methods to separate atmospheric showers triggered by gamma rays from those triggered by hadrons, and gamma-ray energy and direction reconstruction (see de Naurois & Rolland 2009; Holler et al. 2015 for the H.E.S.S. main analysis; Parsons & Hinton 2014 for the H.E.S.S. cross-check; Aleksic et al. 2016b for MAGIC; Daniel et al. 2008 for the VERITAS main analysis; and Maier & Holder 2017 for the VERITAS cross-check). The VHE emission was assumed point like (since it is expected to come from regions close to the binary system, with angular sizes smaller than the instruments’ resolutions), and the signal region was defined by a radius of 0.12, 0.14 or 0.10 around the source position for H.E.S.S., MAGIC, and VERITAS, respectively. In order to maximize the source effective observation time, and thus the probability of detection, a joint analysis of the data from the three experiments was also done (see Appendix B). No significant signal was detected from the individual or combined data sets, regardless of the energy range considered. The gamma-ray upper limits (ULs) in different energy bins were computed following a maximum-likelihood ratio test as described in Appendix B, both for the individual and combined data sets. We also refer the reader to MAGIC Collaboration et al. (2018) for a similar method. A CL of 0.95 was used, and a global flux systematic uncertainty of 30 per cent was taken for each experiment, which accounts for the systematic error in both the flux normalization and the energy scale (see e.g. Aleksic et al. 2012). The choice of a common value of the systematic uncertainty for the three experiments is motivated by the similar values of the systematic errors among them (see Aharonian et al.)
2006a; Aleksić et al. 2016b; Adams et al. 2022, for the estimation of systematic errors in H.E.S.S., MAGIC, and VERITAS, respectively). The VHE gamma-ray spectrum was assumed to follow a power law with spectral index $\alpha = 2.5$, i.e. $dN/d\varepsilon \propto \varepsilon^{-\alpha}$, where $N$ is the number of gamma-ray photons and $\varepsilon$ is their energy. This spectral shape is chosen as it resembles what has been observed for other binary systems detected at VHE (e.g. Albert et al. 2006; Aharonian et al. 2006b; Adams et al. 2021), since similar particle acceleration mechanisms and non-thermal emission processes of VHE gamma rays are expected to occur in MAXI J1820+070.

### 2.2 Fermi-LAT data

The Large Area Telescope (LAT) (Atwood et al. 2009) is a pair-conversion detector on the Fermi Gamma-Ray Space Telescope. It consists of a tracker and a calorimeter, each of them made of a 4 × 4 array of modules, an anticoincidence detector that covers the tracker array, and a data acquisition system with a programmable trigger. The Fermi-LAT is located at a low-Earth orbit with 90-min period and normally operates in survey mode, with a 2.4 sr FoV. Such an observational strategy allows the instrument to cover the whole sky in ~3 h. The data selected for the analysis presented in this paper cover the period MJD 58189–58420. The 0.1–500 GeV data were analysed with the latest available fermi_tools v. 2.0.8 with P8R3_V3 response functions (SOURCE photon class; maximum zenith angle of 90°).

A standard binned likelihood analysis (Mattox et al. 1996) of the data taken from a 14'-radius region of interest (ROI) around the MAXI J1820+070 position was performed. The analysis is based on the fitting of a spatial and spectral model of the sky region around the source of interest to the data. The model of the region included all sources from the 4FGL DR3 catalogue (Abdollahi et al. 2020) as well as components for isotropic and galactic diffuse emissions given by the standard spatial and spectral templates iso_P8R3_SOURCE_V3_v1.txt and gll_iem_v07.fit.

The spectral template for each 4FGL source in the region was selected according to the catalogue model. The normalizations of the spectra of these sources, as well as the normalizations of the Galactic diffuse and isotropic backgrounds, were assumed to be free parameters during the fit. MAXI J1820+070 was modelled as a point-like source with a power-law spectrum. Following the recommendation of the Fermi-LAT collaboration, our analysis is performed with the energy dispersion handling enabled. To minimize the potential effects from the sources present beyond the considered ROI, we additionally included into the model all the 4FGL sources up to $10^7$ beyond the ROI, with all the spectral parameters fixed to the catalogue values. The parameters used for the Fermi-LAT analysis are summarized in Table 3.

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### Table 2

Summary of the observations of MAXI J1820+070 by the H.E.S.S., MAGIC, and VERITAS collaborations, after data quality cuts. The effective observation time, the zenith angle range, and its median are shown for each source state and experiment.

<table>
<thead>
<tr>
<th>Source state</th>
<th>Experiment</th>
<th>Time (h)</th>
<th>Zenith angle (median) (°)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Hard State</td>
<td>H.E.S.S.</td>
<td>17.9</td>
<td>30–61 (33)</td>
</tr>
<tr>
<td></td>
<td>MAGIC</td>
<td>14.2</td>
<td>21–58 (34)</td>
</tr>
<tr>
<td></td>
<td>VERITAS</td>
<td>10.7</td>
<td>20–39 (28)</td>
</tr>
<tr>
<td>HS → SS</td>
<td>H.E.S.S.</td>
<td>4.0</td>
<td>30–38 (32)</td>
</tr>
<tr>
<td></td>
<td>MAGIC</td>
<td>4.9</td>
<td>21–48 (27)</td>
</tr>
<tr>
<td>Soft State</td>
<td>H.E.S.S.</td>
<td>2.6</td>
<td>30–34 (31)</td>
</tr>
<tr>
<td>SS → HS</td>
<td>H.E.S.S.</td>
<td>1.8</td>
<td>37–53 (43)</td>
</tr>
<tr>
<td></td>
<td>MAGIC</td>
<td>3.4</td>
<td>28–56 (41)</td>
</tr>
<tr>
<td>TOTAL</td>
<td>H.E.S.S.</td>
<td>26.3</td>
<td>30–61 (33)</td>
</tr>
<tr>
<td></td>
<td>MAGIC</td>
<td>22.5</td>
<td>21–58 (32)</td>
</tr>
<tr>
<td></td>
<td>VERITAS</td>
<td>10.7</td>
<td>20–39 (28)</td>
</tr>
</tbody>
</table>

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1 See e.g. https://fermi.gsfc.nasa.gov/ssc/data/analysis/scitools/binnedisp_tutorial.html.
Table 3. Details of Fermi-LAT data analysis. From top to bottom, the parameters of the analysis are type of response functions; event class and type; maximum zenith angle; spatial and energy bins widths for the likelihood analysis; number of energy dispersion bins; energy range used for the analysis; radius of the region of interest up to which the sources were included with free normalization [ROI (free)]; radii range in which the sources were included with all parameters fixed to 4FGL-DR3 values [ROI(fixed)]; used catalogue; Galactic diffuse and isotropic diffuse background templates; and time range (in Fermi seconds) used for the analysis.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Response functions</td>
<td>P8R3_V3</td>
</tr>
<tr>
<td>evclass</td>
<td>128</td>
</tr>
<tr>
<td>evtype</td>
<td>3</td>
</tr>
<tr>
<td>zmax</td>
<td>90°</td>
</tr>
<tr>
<td>Spatial bin width</td>
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</tr>
<tr>
<td>Energy bins per decade</td>
<td>5</td>
</tr>
<tr>
<td>edisp_bins</td>
<td>−3</td>
</tr>
<tr>
<td>Energy range</td>
<td>0.1–500 GeV</td>
</tr>
<tr>
<td>ROI (free)</td>
<td>14°</td>
</tr>
<tr>
<td>ROI (fixed)</td>
<td>14°–24°</td>
</tr>
<tr>
<td>Catalogue</td>
<td>4FGL-DR3</td>
</tr>
<tr>
<td>Background (galactic)</td>
<td>glLem_v07.fits</td>
</tr>
<tr>
<td>Likelihood analysis optimizer</td>
<td>iso_P8R3_SOURCE_V3_v1.txt</td>
</tr>
<tr>
<td>Time ranges</td>
<td>NEWMINUUT</td>
</tr>
<tr>
<td></td>
<td>542505605–56246005 (TOTAL)</td>
</tr>
<tr>
<td></td>
<td>542505605–552398405 (HS I)</td>
</tr>
<tr>
<td></td>
<td>552398405–553020485 (HS–SS)</td>
</tr>
<tr>
<td></td>
<td>553020485–559008005 (SS)</td>
</tr>
<tr>
<td></td>
<td>559008005–560131205 (SS–HS)</td>
</tr>
<tr>
<td></td>
<td>560131205–562464005 (HS II)</td>
</tr>
</tbody>
</table>

In order to check the quality of the considered model of the region at the initial step of the analysis, we built a test-statistics (TS) map showing the TS value of a point-like source not present in the model located in a given pixel of the map. The TS map obtained is shown in the left-hand panel of Fig. 2. The map illustrates that the selected model describes the region well in the energy and time-ranges considered. We note the presence of a TS ~10 residual at RA = 275.88°, Dec. = 5.84° (with a positional uncertainty of 0.15°), marked as n1 on the map. This residual is positionally coincident with PSR J1823+0550 (PSR B1821 + 05). We modelled this source as a point-like source with a power-law spectrum, dN/dE = K E^{−α}, with K being the flux normalization. The best-fitting parameters in the selected time range and in the 0.1–500 GeV energy band are K = (1.3 ± 0.4) × 10^{−12} ph cm^{−2} s^{−1} MeV^{−1} at 1 GeV, and α = 2.2 ± 0.2. We included this source to the considered model of the region with a free normalization and the index fixed to the best-fitting value. After all these steps, MAXI J1820+070 was not detected with the binned-likelihood analysis for the time period considered (assuming a power-law spectrum model with a free spectral index), and is therefore not present at the TS map of Fig. 2.

In what follows, the Fermi-LAT flux upper limits for MAXI J1820+070 were calculated at a 0.95 CL with the help of the IntegralUppLimit module provided as a part of standard Fermi-LAT data analysis software for a power-law index fixed to α = 2.5, as for the VHE data analysis (and also similar to what is observed for high-mass microquasars in the Fermi-LAT energy range, see e.g. Zanin et al. 2016; Zdziarski et al. 2018).

In order to search for a possible short time-scale variability observed in several microquasars detected up to GeV energies, we computed the LC of the source with variable (adaptive) time binning (e.g. Lott et al. 2012). Namely, we selected a time bin duration such that each bin receives 16 photons in the 0.1–500 GeV energy range and in a radius of 1° around the MAXI J1820+070 position. This resulted in 55 time bins in the total time range considered with an average duration of 4.2 d (minimum: 1 d, maximum: 27 d). Such time bin selection allows us to identify the shortest possible periods during which the source potentially could be detected with up to a ∼4σ significance. A similar approach was found to be effective for a search of short flares during the periods of strong GeV variability of PSR B1259-63 in the analysis of Chernyakova et al. (2020, Chernyakova et al. 2021). The performed analysis did not result in the detection of MAXI J1820+070 in any of the time bins, and the resulting ULs are shown in the right-hand panel of Fig. 2.

2.3 Additional multiwavelength data

Data from several radio telescopes at different frequencies are taken from Bright et al. (2020). Optical data are taken from Celma (2019), in which observations performed with the Joan Oró Telescope (TJO; Colomé et al. 2010) and Swift Ultraviolet/Optical Telescope (Swift/UVOT; Roming et al. 2005) are reported. The optical fluxes are obtained from images taken with the five Johnson–Cousins filters (with central wavelengths around 366, 435, 548, 635, and 880 nm, respectively from the U to I filters), and they are already corrected for interstellar extinction with values ranging from 0.2 to 0.6 mag (see Fitzpatrick 1999; Celma 2019, and references therein). Public LCs from MAXI/GSC (Matsuoka et al. 2009) and Swift Burst Alert Telescope (Swift/BAT Krimm et al. 2013) are also included.

For the spectral energy distributions (SEDs) of MAXI J1820+070, International Gamma-Ray Astrophysics Laboratory (INTEGRAL; Winkler et al. 2003) data are added to that of the previously mentioned instruments, based on results by Roques & Jourdain (2019) from MJD 58206 to 58246, during the first half of the HS. Data from the Neutron star Interior Composition Explorer (NICER, Gendreau, Arzoumanian & Okajima 2012) are also used. NICER is designed to study neutron stars via soft X-ray timing spectroscopy and has been operating from the International Space Station since 2017. It observed for 109, 21.8, and 4.56 h during the HS, the HS–SS transition, and SS–HS transition, respectively. Preprocessed event files were retrieved through the HEASARC data base. Reprocessing and filtering were done using standard criteria with the nicer12 task from the NICERDAS software available in the HEASoft distribution2 (v6.26). Spectra were extracted using the extractor function from the tools package. Error bars account only for the statistical uncertainty on detector counts, namely ±1 standard deviation of a Poisson distribution. Energy and gain calibrations were performed using the HEASARC Calibration Database version XTI(20200722). To avoid telemetry saturation, the fraction of active modules had to be adjusted. This was taken into account considering that each module contributes equally to the effective area. The fluxes were corrected for interstellar extinction using a hydrogen column density of N_H = 1.4 × 10^{21} cm^{−2} (Dzielak, De Marco & Zdziarski 2021).

3 RESULTS

The observations of MAXI J1820+070 reported in this work do not show any significant emission in either HE or VHE gamma rays, regardless of the source state. The computed integral flux ULs for Fermi-LAT data and the combined data set of H.E.S.S., MAGIC, and

2https://heasarc.gsfc.nasa.gov/docs/software/heasoft/
Figure 2. Left-hand panel: Test-statistics map in Galactic coordinates of a $5' \times 5'$ region around MAXI J1820+070 (cyan circle at the centre) in the 0.1–500-GeV energy range, with a 0.1-pixel size. Green symbols show the 4FGL Fermi-LAT sources present in the region. The cyan circle marked as $n$ shows a TS $\sim 10$ point-like residual positionally coincident with PSR J1823 + 0550. Right-hand panel: Fermi-LAT LC of MAXI J1820+070 in the 0.1–500-GeV energy band with an adaptive time binning. The bin widths correspond to 16 photons arrived in a 1'-radius around MAXI J1820+070. Source states are represented with light red (HS), light blue (SS), and light yellow (HS–SS / SS–HS) background colours.

Table 4. Integral flux upper limits with a 0.95 C.L. during different source states, between 0.1 and 500 GeV from Fermi-LAT data, and above 200 GeV from the combined H.E.S.S., MAGIC, and VERITAS data. For the SS $\rightarrow$ HS transition, the UL above 300 GeV is shown instead.

<table>
<thead>
<tr>
<th>Source state</th>
<th>Fermi-LAT UL (0.1–500 GeV)</th>
<th>IACT UL (&gt;200/3000 GeV)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>(ph cm$^{-2}$ s$^{-1}$)</td>
<td>(ph cm$^{-2}$ s$^{-1}$)</td>
</tr>
<tr>
<td>Hard State I</td>
<td>$3.1 \times 10^{-8}$</td>
<td>$9.5 \times 10^{-13}$</td>
</tr>
<tr>
<td>HS $\rightarrow$ SS</td>
<td>$1.6 \times 10^{-7}$</td>
<td>$9.5 \times 10^{-13}$</td>
</tr>
<tr>
<td>Soft State</td>
<td>$2.5 \times 10^{-8}$</td>
<td>$1.6 \times 10^{-12}$</td>
</tr>
<tr>
<td>SS $\rightarrow$ HS</td>
<td>$5.2 \times 10^{-8}$</td>
<td>$2.2 \times 10^{-12}$</td>
</tr>
<tr>
<td>Hard State II</td>
<td>$6.0 \times 10^{-8}$</td>
<td>$-$</td>
</tr>
<tr>
<td>TOTAL</td>
<td>$1.8 \times 10^{-8}$</td>
<td>$7.2 \times 10^{-13}$</td>
</tr>
</tbody>
</table>

VERITAS are shown in Table 4 for each X-ray state. The former are calculated for photon energies $\varepsilon > 100$ MeV, while the latter are computed at $\varepsilon > 200$ GeV for the HS, the HS–SS transition, the SS and the whole sample, and at $\varepsilon > 300$ GeV for the SS–HS transition. The increase in energy threshold of the last data set is due to a higher average zenith angle of the observations, which does not allow electromagnetic showers triggered by lower energy gamma rays to be detected. We note that the VHE UL for the SS, shown here for completeness, may not be representative of the whole source state, since it only covers the very first days of the SS (see the top panel of Fig. 1).

Fig. 3 presents the ULs on the VHE differential flux obtained for five different energy bins and each source state for which observations were performed (excluding the poorly covered SS). Both individual and combined ULs are shown in each case. For the SS–HS transition, the lowest energy bin is not computed due to the increased energy threshold of the corresponding observations. The differences between individual ULs in the same energy bin originate from the different instrument sensitivities and observation times, as well as from statistical fluctuations (see Appendix B). Except in the case of significant differences between the individual ULs, the combined ULs are tighter than any of the individual ones.

Fig. 4 shows the LCs of MAXI J1820+070 at different frequencies, with the gamma-ray LC corresponding to the ULs in Table 4. The radio fluxes in the top panel include both the core emission from the jet regions close to the binary system, and the radiation emitted by discrete ejections launched during the HS–SS transition. Core emission is dominant during the source HS, while the ejections dominate throughout the SS, during which no core emission is detected (see Bright et al. 2020, for the details). The optical fluxes in the second panel are obtained from a total set of 16457 images distributed over 113 different nights between 2018 March and November (Celma et al. 2019). The X-ray LCs in the third panel are obtained from the daily fluxes of MAXI J1820+070 from MAXI/GSC (for $2 \leq \varepsilon \leq 20$ keV) and Swift-BAT (for $15 \leq \varepsilon \leq 50$ keV). The gaps represent the periods when the source was not observed with these instruments.

The SEDs of MAXI J1820+070, averaged for those source states well represented by the VHE data, are shown in Fig. 5. We note that the jump between NICER and INTEGRAL data in the top panel is just an effect of the different time coverage of the observations. While NICER data are averaged over the whole duration of the HS, INTEGRAL data only cover roughly the first half of it (see Section 2.3), when the average X-ray flux was higher.

4 DISCUSSION

In this section, we provide a short description of multiwavelength measurements of MAXI J1820+070 from radio to X-rays. Based on some assumptions regarding the extrapolation of the jet synchrotron spectrum and the distribution (energy dependence and maximum energy) of the non-thermal particles, we estimate the expected jet emission in HE and VHE gamma rays analytically. This expected emission is then compared to the measured ULs, and used to constrain the properties of a potential gamma-ray emission region in MAXI J1820+070.

4.1 Multiwavelength overview of the source

Radio emission from MAXI J1820+070 provides evidence for jet activity during the whole 2018 outburst. This emission is dominated by a steady jet in the HS, a discrete blob in the HS–SS transition (the emission of which is also dominant throughout the SS as the blob moves away from the binary system), and a jet rebrightening during the SS–HS transition (Bright et al. 2020). Without accounting for blob emission during the SS, the radio and hard X-ray fluxes have
similar behaviours: they decrease slowly through the HS, have a steep decrease in the HS–SS transition, are practically undetectable during the SS, and increase again in the SS–HS transition. This is expected from the standard picture of BH-LMXBs, where steady radio jets in the HS coexist with a hard X-ray emitting corona, both of them disappearing in the SS. During the HS, synchrotron emission from the jet is likely the dominant contribution to the SED up to infrared frequencies, beyond which the spectrum becomes dominated by disc and coronal emission (Rodi et al. 2021; Tetarenko et al. 2021; Zdziarski et al. 2021b). We note the less note that the jets in LMXBs may still contribute significantly up to hard X-rays through their synchrotron emission (e.g. Markoff, Nowak & Wilms 2005).

Regarding the contribution from the star to the overall SED, MAXI J1820+070 had a magnitude of 17.4 in the $G$ filter – with a central wavelength around 460 nm – before the outburst (Wenger et al. 2000; Gaia Collaboration 2018), which is at least three magnitudes above the $B$ magnitude during the flare (from the filters shown in the second panel of Fig. 4, the $B$ filter is the closest one to the $G$ filter). This means that the optical flux of MAXI J1820+070 during the flare was at least about 15 times larger than before the outburst. Nonetheless, this increase in flux cannot be exclusively associated to the brightening of the accretion disc, since the stellar luminosity can also increase during the outburst owing to the heating of the stellar surface produced by the X-ray emission close to the BH (e.g. de Jong, van Paradijs & Augusteijn 1996). Assuming a stellar radius of $\sim 10^{11}$ cm equal to that of the Roche lobe, the solid angle of the star as seen by the BH is $\sim 0.01$ sr. This means that the optical luminosity of the X-rays reprocessed in the stellar surface should be about two orders of magnitude below the X-ray luminosity. This optical luminosity is comparable to what is observed from the whole system (see Fig. 5), so we can conclude that the stellar contribution to the optical flux of MAXI J1820+070 may be significant.

### 4.2 Analytical estimates

For the estimates performed in this section, the particles responsible for the non-thermal emission are assumed to be only electrons (and positrons), although we note that hadrons might contribute to the overall emission of the system (see e.g. Bosch-Ramon & Khangulyan 2009, for typical electron and proton cooling timescales in microquasar environments). These electrons are likely accelerated up to relativistic energies close to the BH, and different acceleration mechanisms may play a role (see e.g. Bosch-Ramon & Rieger 2012, for a description of different processes that can contribute to particle acceleration). The non-thermal emission of the electrons is assumed to come from their synchrotron and IC cooling. The derived jet inclination and speed in MAXI J1820+070 make the counter-jet emission significantly more deboosted than that from the jet. The discussion can therefore be focused on the jet emission, and the counter-jet contribution can be neglected. In the following, primed quantities refer to the reference frame moving with the jet flow, while

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**Figure 3.** Differential flux upper limits of MAXI J1820+070 for different energy bins and source states (indicated in the legend). Coloured markers represent the results for the individual experiments, while black lines show the combined upper limits.
unprimed ones refer to quantities in the laboratory frame or as seen by the observer.

4.2.1 A steady jet in the HS

Some jet properties during the initial HS of the source were constrained by Zdziarski et al. (2022) based on the radio to optical emission. In particular, the synchrotron break frequency (above which the emission becomes optically thin) is measured to be $\nu_0 \approx 2 \times 10^9$ GHz. They also find that for a jet Lorentz factor of $\Gamma \approx 3$, the onset of the jet synchrotron emission comes from a distance to the BH of $r \approx 3.8 \times 10^{15}$ cm, where the magnetic field is $B' \approx 10^4$ G. If equipartition between the magnetic and particle energy densities is assumed (the equipartition condition approximately corresponds to the minimum energy requirement for synchrotron radiation, which happens for a magnetic energy of $\sim 0.75$ times the particle one; e.g. Longair 1981).

To estimate the gamma-ray emission of the source, we assume that gamma rays are produced by IC scattering of photons coming from the accretion disc or the corona by jet electrons. This means that the target photons reach the jet mainly from behind, which is very likely the case for X-rays in MAXI J1820+070, and is also approximately the case for optical photons. Given the conditions in the source, the estimates can be done in the context of the Thompson regime, which is approximately valid at the adopted energies ($\gamma \epsilon \lesssim m_e c^2$, see below), and simplifies the calculations (e.g. Longair 1981). In this regime, IC is more efficient and the energy gain of the scattered photons is proportional to the square of the electron Lorentz factor $\gamma$.

For HE gamma rays, a characteristic energy of $\epsilon = 100$ MeV is taken, which would be the result of the IC scattering towards the observer of target X-ray photons with typical energies of $\sim 1$ keV by $E_{\text{HE}}' \sim 250$ MeV electrons ($\gamma' \sim 500$). These are reference values for which data at the target photon energy are available, although target photons with energies similar to the chosen ones would also contribute to the IC emission around $\epsilon = 100$ MeV. The electrons with energy $E_{\text{HE}}'$ emit synchrotron photons with an observed frequency of $\nu_{\text{syn}} \approx 1.5 \times 10^{16}$ GHz. The observed flux density at this frequency (extrapolated from the infrared data in Zdziarski et al. 2022) is $F_{\nu,\text{syn}}^{\text{obs}} \sim 30$ mJy. The observed IC flux of the electrons with energy $E_{\text{HE}}'$ can then be estimated as

$$\epsilon \frac{dN}{d\epsilon} \bigg|_{\text{IC}} = \nu_{\text{IC}} F_{\nu}^\text{IC} \approx \nu_{\text{syn}} F_{\nu}^\text{syn} \frac{E_{\text{IC}}}{E_{\text{syn}}},$$  \hspace{0.5cm} (1)
where $E_{IC}^s = -0.039 \alpha E^2$ and $E_{\text{syn}}^s = -1.6 \times 10^{-3} B^2 E^2$ are the IC and synchrotron cooling rates in cgs units, respectively. The energy density of the target photon field with luminosity $L_{\text{tot}} \approx 2 \times 10^{37} \text{erg s}^{-1}$ is $u' \approx u' l^2 = L_{\text{tot}}/4\pi^2 r^2 c^2$ (valid as long as the target photons reach the jet from behind; Dermer & Schlickeiser 1994). Equation (1) yields a predicted IC energy flux at 100 MeV of $\sim 6 \times 10^{-13} \text{erg cm}^{-2} \text{s}^{-1}$, about a factor of 20 smaller than the obtained ULs at this energy (see upper panel of Fig. 5). We note that the predicted energy flux increases with the ratio $\eta$ of particle-to-magnetic energy density as $v_{\text{syn}} F_{\text{ext}}^s \propto \eta^{0.35}$, as long as the corresponding $v_{\text{syn}}$ is in the optically thin regime (see the dependency of $B$ with the energy density fraction in Zdziarski et al. 2022, and how this changes the values of $v_{\text{syn}}$ and $F_{\text{ext}}^s$). For example, taking a value of $\eta = 100$ raises the expected energy flux to $\sim 3 \times 10^{-12} \text{erg cm}^{-2} \text{s}^{-1}$, a factor of five higher than in equipartition and only four times smaller than the ULs.

Regarding the VHE emission, an extrapolated power-law electron distribution is assumed, i.e. $N(E') \propto E'^{-p}$, with $N(E')$ being the number of electrons per energy unit. This distribution is taken up $E_{\text{VHE}} \approx 500$ GeV, which is the energy required to emit VHE gamma rays with $\epsilon \sim 200$ GeV through IC with optical target photons. In order not to contradict the observations, a soft injection index of $p \geq 3$ is required for the high-energy electrons (with energies above those responsible for the infrared emission reported in Zdziarski et al. 2022). Otherwise, the observed MeV fluxes would be violated by the synchrotron emission of the electrons with hundreds of GeV, and the VHE ULs would be violated by the expected IC emission of these electrons. On the other hand, using $p \geq 3$ yields an expected VHE emission that falls at least two orders of magnitude below the obtained UL for the lowest VHE bin in Fig. 5. Therefore, the obtained VHE ULs are not so constraining as the HE ones in the source HS.

### 4.2.2 Discrete events during the state transitions

For the HS–SS transition, Bright et al. (2020) determined that the radio emission was dominated by a discrete blob of plasma. The estimates in this section assume, for both state transitions,\(^3\) a one-zone spherical radio emitter in the flow frame with the Lorentz factor and inclination values reported in Section 1. The non-thermal electrons responsible for this synchrotron radio emission are taken as reference to obtain the expected IC emission in the source. We use the spectral shape derived from the two radio points in Fig. 5, which indicates a self-absorbed synchrotron emission at the observed frequencies. Therefore, the break frequency should be located at a frequency higher than 15.5 GHz. On the other hand, for the HS–SS transition this frequency has to be lower than $\sim 700$ GHz if $p \approx 2$, since otherwise the optical fluxes would be violated by the blob synchrotron emission. For simplicity, a break frequency of $v_0 = 100$ GHz is used in both state transitions: if $v_0$ were lower, the limits derived below would be less restrictive, and more restrictive otherwise. With the Doppler boosting factor of the blob being $\delta = [\Gamma(1 - \beta \cos \theta)]^{-1}$, the break frequency value in the flow frame is $v_{0}^* = v_0 / \delta$, and the extrapolated flux density at $v_{0}^*$ is $F_{0}^* = F_0 / \delta^4$. The distance to the source $d$ can be used to constrain the magnetic field $B$ and radius $R$ of the radio-emitting blob through the following relation

\[ v_0^* \approx 10^{12} F_0^{2/5} B^{-1/5} R^{-4/5} d^{1/5}. \]

We note that, due to the high inclination of the system, $R$ is approximately equal to $R$ measured in the direction of the observer. The magnetic field is parametrized through the fraction $\eta$ of magnetic to particle energy density:

\[ \frac{B^2}{8\pi} = \eta \frac{E_{\text{NT}}' \gamma}{V'}, \]

where $V = 4\pi R^2/3$ is the proper volume of the emitting region, and $E_{\text{NT}}'$ is the energy budget of the non-thermal electrons in the blob. Taking an electron distribution $N'(E') = Q E'^{-p}$ with $p = 2$ between $E_{\text{min}}' \sim 50$ MeV and $E_{\text{max}}' \sim$ GeV yields

\[ E_{\text{NT}}' = Q \ln\left(\frac{E_{\text{max}}'}{E_{\text{min}}'}\right) \sim 3 Q, \]

with $Q$ being a normalization constant. The values of $p$, $E_{\text{min}}'$ and $E_{\text{max}}'$ are not strongly constrained by the observations, but equation (4) is not very sensitive to the exact values of $E_{\text{max}}'$ and $E_{\text{min}}'$ as long as $p \approx 2$. Additionally, the optically thin synchrotron spectral luminosity can be related to the particle distribution as

\[ L_c' \approx N'(E') E_{\text{syn}}' \frac{dE'}{dE}. \]

Taking an equipartition magnetic field with $\eta = 1$, equations (2) to (5) provide the following results for the radio emitter in the HS–SS (SS–HS) transition: a radius of $R \approx 2.0 \times 10^{11}$ cm ($1.1 \times 10^{11}$ cm), a non-thermal energy budget of $E_{\text{NT}}' \approx 2.8 \times 10^{39}$ erg ($6.5 \times 10^{39}$ erg), and a magnetic field of $B' \approx 47$ G ($55$ G).

The same reference energy as in the HS is taken for the HE emission through IC, i.e. $\epsilon = 100$ MeV, which results from the scattering of $\sim 1$ keV photons by $E_{\text{HE}}' \sim 200$ MeV electrons. For the VHE emission, a characteristic energy of $\epsilon = 200$ GeV (400 GeV) is chosen for the HS–SS (SS–HS) transition. These gamma-ray photons are the result of the scattering of disc target photons with typical energies of $\sim 0.5$ eV by $E_{\text{VHE}}' \approx 400$ GeV (600 GeV) electrons. Observational evidence of non-thermal electrons is available only for energies below 10 MeV in the flow frame, since the electrons in this energy range are responsible for the emission up to 15.5 GHz. Therefore, an extension of the electron distribution up to the required $E_{\text{HE}}'$ and $E_{\text{VHE}}'$ is assumed with a power-law shape with index $p = 2$. Reaching such particle energies is not unreasonable for the equipartition magnetic field obtained above, since high acceleration efficiencies are not required to reach those energies. The most constraining efficiency needed is $\eta_{\text{acc}} \approx 200$ for $E = 600$ GeV, with $v_{\text{acc}} = \eta_{\text{acc}} E'/\epsilon c B'$ being the acceleration timescale.

To estimate the expected IC emission, a similar method to the one developed for the HS is used, following equation (1), where $v_{\text{syn}}$ and $F_{\text{ext}}^s$ are now the characteristic synchrotron frequency of the electrons with each of the aforementioned energies, $E_{\text{HE}}'$ and $E_{\text{VHE}}'$, and the corresponding extrapolated flux at $v_{\text{syn}}$, respectively. This sets a minimum distance of the potential gamma-ray emitter to the BH through the dependence of the target photon energy density $u'$ with this distance. If the emitter were closer to the BH (and the accretion disc), $u'$ would be so high that the gamma-ray ULs would be violated by the IC emission of the blob. For the HS–SS (SS–HS) transition, the derived distances of the potential HE and VHE emitters to the BH are $r_{\text{HE}} \gtrsim 2.8 \times 10^{10}$ cm ($1.0 \times 10^{10}$ cm) and $r_{\text{VHE}} \gtrsim 1.1 \times 10^{12}$ cm ($2.3 \times 10^{11}$ cm). The radio emitter size constraints impose that $r_{\text{HE}}$ is likely larger, at least a few times $10^{11}$ cm. Conversely, both $r_{\text{HE}}$ and $r_{\text{VHE}}$ cannot be more than several times the radio emitter size, the exact value depending on the blob expansion velocity, since that

\(^3\)We note that the blob model may not hold for the SS–HS transition, although it is still used for the sake of simplicity and due to the lack of much information for this source state.
would increase the emitter size to the point that the synchrotron radio emission would become optically thin below $v_0$.

Both the potential HE and VHE emitter distances derived above are sufficiently large for the blob gamma-ray emission to be unaffected by gamma-gamma absorption with the external photons from the disc and the corona (this also applies to the HS emitter studied in Section 4.2.1). Also, for the values of $R'$ and $B'$ obtained, the energy density of the synchrotron soft X-ray photons (emitted as long as the electrons reach high-enough energies) should be comparable to that of the X-rays coming from the corona and/or the disc. Moreover, the energy density of the synchrotron optical photons should also be comparable to that of the disc optical photons. Therefore, synchrotron self-Compton should be responsible for a significant fraction of any HE and VHE emission of MAXI J1820+070.

5 SUMMARY AND CONCLUSIONS

Observations of the exceptionally bright X-ray source MAXI J1820+070 have been performed with the H.E.S.S., MAGIC and VERITAS experiments in VHE gamma rays. These data complement Fermi-LAT observations of HE gamma rays, as well as additional multiwavelength data from radio to X-rays. The latter show the expected behaviour for a typical BH-LMXB, indicating a source following the usual HS–SS–HS cycle during an outburst.

Radio emission throughout the whole outburst provides evidence for the presence of jets with a population of non-thermal particles (electrons and possibly positrons) emitting via the synchrotron mechanism. Based on the study performed by Zdziarski et al. (2022), the estimated HE emission during the HS could be not far below the obtained ULs if the magnetic field is well below equipartition. Additionally, for a spherical blob-like radio emitter during the state transitions, significant constraints to a potential gamma-ray emitter in the source can be set using reasonable assumptions for the synchrotron transition frequency and the spectrum of the emitting electrons. For an equipartition magnetic field, the potential HE emitter should be located at a distance from the BH between a few $10^{11}$ and a few $10^{13}$ cm. If electrons are efficiently accelerated up to energies of $\sim 500$ GeV in the flow frame, a putative VHE emitter should also be located in a similar region, between $\sim 10^{11}$ and $10^{13}$ cm. Having the emitter closer than the region defined by these limits would violate the gamma-ray observations. Conversely, if the emitter is farther than this region, its emission would not be consistent with the observed optically thick radio spectrum. The relatively narrow range of allowed distances during the transitions, and the inferred gamma-ray fluxes in the HS, indicate that the HE and VHE gamma-ray flux of MAXI J1820+070 (and possibly other BH-LMXBs showing evidence for non-thermal emission) might not be too far from being detectable with the current instrument sensitivities, (as the strong hint for V404 Cygni at HE may exemplify) and might be detectable for especially bright outbursts, or with future gamma-ray telescopes like the Cherenkov Telescope Array (Paredes et al. 2013; Cherenkov Telescope Array Consortium et al. 2019).

It should be noted that observations in the 100–1000 GHz band during the state transitions would be very useful to constrain the non-thermal emitter properties by means of establishing the transition frequency between the optically thin and optically thick synchrotron regimes, as well as determining whether non-thermal particles are accelerated up to at least a few hundred MeV or not. Upcoming MeV missions, like the All-sky Medium Energy Gamma-ray Observatory (McEnery et al. 2019) or e-ASTROGRAM (de Angelis et al. 2017), will also be useful to bridge the 1–100 MeV gap in observations of outbursts in X-ray binaries.

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AUTHOR CONTRIBUTION STATEMENT

All authors have read and approved the manuscript and contributed in one or several of the following ways: design, construction, maintenance and operation of the instruments used to acquire the data; preparation and/or evaluation of the observation proposals; data acquisition, processing, calibration and/or reduction; production of analysis tools and/or related Monte Carlo simulations. Notable individual contributions in alphabetical order from MAGIC collaboration members include: J. Hoang - MAGIC analysis cross-check; E. Molina - project leadership, coordination of the MAGIC observations, MAGIC data analysis, theoretical interpretation, paper drafting and editing; M. Ribó - triggering and initial coordination of the MAGIC observations, establishment of the agreement to work with the other collaborations and contact with the multiwavelength community. Contributions from authors outside of the MAGIC, H.E.S.S. and VERITAS collaborations include: V. Bosch-Ramon - theoretical interpretation; C. C. Elma - TJO data analysis, Swift/UVOT data analysis; M. Linares - TJO data analysis, Swift/UVOT data analysis; D.M. Russell - TJO data analysis, Swift/UVOT data analysis; G. Sala - TJO data analysis.

Given the wide array of contributions from many individuals over decades to bring H.E.S.S. and VERITAS to fruition – including to design the instruments, to build them, to maintain them, to operate them, and to develop analysis software – in addition to the efforts needed to obtain, analyse, and interpret the data for a particular scientific study, it is the policy of both the H.E.S.S. and the VERITAS Collaborations not to attempt to summarize the contributions of individual members.

DATA AVAILABILITY

Part of the data underlying this article are available in the article and in its online supplementary material. In particular, MAXI/GSC data were obtained from http://maxi.riken.jp/star_data/J11820+071J11820 +071.html; Swift/BAT data were downloaded from https://swift.gsfc.nasa.gov/results/transients/weak/MAXI J11820 +070T; NICER data were retrieved from https://heasarc.gsfc.nasa.gov/docs/archive.html, and the corresponding calibration data were downloaded from https://heasarc.gsfc.nasa.gov/docs/heasarc/caldb/data/nicer/xti/index/cif_nicer_xti_20200722.html; and Fermi-LAT data were downloaded from https://fermi.gsfc.nasa.gov/ssc/LAT/LATDataQuery.cgi. The rest of the data will be shared on reasonable request to the corresponding authors.

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MNRS 517, 4736–4751 (2022)
SUPPORTING INFORMATION

Supplementary data are available at MNRAS online.

**Figure 4.** From top to bottom panels: radio, optical, X-ray, and gamma-ray LCs of MAXI J1820+070 during its 2018 outburst (MJD S189:0–S1420.0).

**Figure 5.** From top to bottom panels: spectral energy distributions of MAXI J1820+070 averaged over the HS, the HS–SS transition, and the SS–HS transition. Fermi–LAT points include the contribution from the two HSs of the source.

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**APPENDIX A: OBSERVATION DATES**
Table A1. Dates when H.E.S.S., MAGIC, and/or VERITAS observations of MAXI J1820+070 were performed. Only dates with surviving data after quality cuts are shown. These are also depicted in Fig. 1.

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APPENDIX B: THE GAMMA-RAY FLUX COMPUTATION

For each experiment and energy bin, the low-level data analysis yields the number of gamma-ray events recorded in the direction of the source (ON region) and in control regions with only background events (OFF regions), $N_{\text{on}}$ and $N_{\text{off}}$, respectively; the exposure ratio of the OFF to ON regions, $\tau$; the effective observation time of the source after data quality cuts, $t_{\text{eff}}$; and the effective collection area averaged over the considered energy interval, $A_{\text{eff}}$. We assume a power-law distribution for the gamma rays coming from the source, i.e. $dN/d\varepsilon = K\frac{\varepsilon^{-\alpha}}{\Gamma(\alpha+1)}$, where $N$ is the number of gamma-ray photons, $K$ is the flux normalization constant, $\varepsilon$ is the gamma-ray energy, and $\alpha$ is the spectral index. With this, the expected number of gamma rays coming from the source in the energy interval $[\varepsilon_{\text{min}}, \varepsilon_{\text{max}}]$ can be expressed as

$$\mu = t_{\text{eff}} \int_{\varepsilon_{\text{min}}}^{\varepsilon_{\text{max}}} A_{\text{eff}}(\varepsilon) \frac{dN}{d\varepsilon} = K < A_{\text{eff}} > t_{\text{eff}} \frac{\varepsilon_{\text{max}}^{-\alpha} - \varepsilon_{\text{min}}^{-\alpha}}{\alpha - 1}. \quad (B1)$$

In order to obtain the range of values of $K$ compatible with the observed quantities, the value of $\alpha$ is fixed, and a maximum likelihood method is performed as described by Rolke, López & Conrad (2005). We define a Poissonian likelihood function as

$$L = \frac{(\varepsilon \mu + b)^{N_{\text{on}}}}{N_{\text{on}}!} \times \frac{\tau b^{N_{\text{off}}}}{N_{\text{off}}!} \times \frac{1}{\sigma_\varepsilon \sqrt{2\pi}} \exp \left[ -\frac{1}{2} \frac{(\varepsilon - \hat{\varepsilon})^2}{\sigma_\varepsilon^2} \right]. \quad (B2)$$

where the terms correspond, from left to right, to the statistical distributions of a Poissonian signal, a Poissonian background, and a detection efficiency with a Gaussian uncertainty. The parameters $b$ and $\varepsilon$ are treated as nuisance parameters, are the expected number of background events in the signal region, and the expected detector efficiency, respectively. The parameters $\hat{\varepsilon}$ and $\sigma_\varepsilon$ are the estimates for the efficiency and its standard deviation, respectively. Fixing $\varepsilon_0 = 1$ allows us to account for the relative systematic uncertainty of the instrument by equating it to the value of $\sigma_\varepsilon$.

With the likelihood function defined, we find the values $\hat{K}$, $\hat{b}$, and $\hat{\varepsilon}$ that maximize $L$, which can be obtained analytically for the likelihood function expressed in equation (B2). The null hypothesis $K = K_0$ is then tested versus the alternative hypothesis $K \neq K_0$ through a likelihood ratio test statistic:

$$\lambda = \frac{L(K_0, \hat{b}(K_0), \hat{\varepsilon}(K_0))}{L(K, b, \varepsilon)} \quad (B3)$$

where $\hat{b}(K_0)$ and $\hat{\varepsilon}(K_0)$ are the values that maximize $L$ for a given $K_0$. According to the Wilks theorem (Wilks 1938), under the null hypothesis the distribution of the quantity $-2\ln \lambda$ converges to a $\chi^2$ distribution with 1 degree of freedom for large enough statistics. This allows us to find the range of $K_0$ compatible with the observations in the energy bin $[\varepsilon_{\text{min}}, \varepsilon_{\text{max}}]$, i.e. being $n = -2\ln \lambda$, the null hypothesis is excluded at a $n\sigma$ level. Finally, the upper end of this range of $K_0$ is translated to an upper limit in flux (with a $n\sigma$ CL) through the assumed spectral shape.

The method explained above works for the flux computation of each individual experiment. In order to merge H.E.S.S., MAGIC and VERITAS data into a single flux measurement, a joint likelihood function is defined as the product of the individual likelihoods defined in equation (B2):

$$L_{\text{tot}} = \prod_{i=1}^{3} L_i(N_{\text{on},i}, N_{\text{off},i}, \tau_i, t_{\text{eff},i}, A_{\text{eff},i}) \quad (B4)$$

Given that the data of each experiment are independent from each other, the maximization procedure can be done individually for each instrument. Therefore, with the joint likelihood defined in equation (B4), we have

$$-2\ln \lambda_{\text{tot}} = \sum_{i=1}^{3} -2\ln \lambda_i \quad (B5)$$

for each value of $K_0$, and the null hypothesis is rejected or not according to the same criteria as in the individual case.  

$^1$Japanese MAGIC Group: Institute for Cosmic Ray Research (ICRR), The University of Tokyo, Kashiwa, 277-8582 Chiba, Japan  
$^2$Instituto de Astrofísica de Canarias and Dpto. de Astrofísica, Universidad de La Laguna, E-38200, La Laguna, Tenerife, Spain
78 Department of Physics, Konan University, 8-9-1 Okamoto, Higashinada, Kobe, Hyogo 658-8501, Japan
79 Kavli Institute for the Physics and Mathematics of the Universe (WPI), The University of Tokyo Institutes for Advanced Study (UTIAS), The University of Tokyo, 5-1-5 Kashiwa-no-Ha, Kashiwa, Chiba 277-8583, Japan
80 RIKEN, 2-1 Hirosawa, Wako, Saitama 351-0198, Japan
81 Department of Physics, Rikkyo University, 3-34-1 Nishi-Ikebukuro, Toshima-ku, Tokyo 171-8501, Japan
82 Department of Physics, University of the Free State, PO Box 339, Bloemfontein 9300, South Africa
83 Kapteyn Astronomical Institute, University of Groningen, Landleven 12, NL-9747 AD Groningen, the Netherlands
84 Department of Physics and Astronomy, University of Alabama, Tuscaloosa, AL 35487, USA
85 Physics Department, Columbia University, New York, NY 10027, USA
86 DESY, Platanenallee 6, D-15738 Zeuthen, Germany
87 Center for Astrophysics | Harvard & Smithsonian, Cambridge, MA 02138, USA
88 Department of Physics and Astronomy, Barnard College, Columbia University, NY 10027, USA
89 Physics Department, California Polytechnic State University, San Luis Obispo, CA 93407, USA
90 Department of Physics and Astronomy, Iowa State University, Ames, IA 50011, USA
91 Department of Physics, Washington University, St. Louis, MO 63130, USA
92 Department of Astronomy and Astrophysics, 525 Davey Lab, Pennsylvania State University, University Park, PA 16802, USA
93 Department of Physics and Astronomy, Purdue University, West Lafayette, IN 47907, USA
94 Department of Physics and Astronomy and the Bartol Research Institute, University of Delaware, Newark, DE 19716, USA
95 School of Physics and Astronomy, University of Minnesota, Minneapolis, MN 55455, USA
96 Department of Physics, California State University - East Bay, Hayward, CA 94542, USA
97 School of Physics and Center for Relativistic Astrophysics, Georgia Institute of Technology, 837 State Street NW, Atlanta, GA 30332-0430, USA
98 Santa Cruz Institute for Particle Physics and Department of Physics, University of California, Santa Cruz, CA 95064, USA
99 Department of Physics and Astronomy, University of Utah, Salt Lake City, UT 84112, USA
100 Department of Physics and Astronomy, University of Iowa, Van Allen Hall, Iowa City, IA 52242, USA
101 Department of Physics and Astronomy, DePauw University, Greencastle, IN 46135-0037, USA
102 Physics Department, McGill University, Montreal, QC H3A 2T8, Canada
103 School of Physics, National University of Ireland Galway, University Road, H91 TK33 Galway, Ireland
104 School of Physics, University College Dublin, Belfield, Dublin 4, Ireland
105 Department of Physics and Astronomy, Ball State University, Muncie, IN 47306, USA
106 Department of Physics, Anderson University, 1100 East 5th Street, Anderson, IN 46012, USA
107 Department of Physics and Astronomy, University of California, Los Angeles, CA 90095, USA
108 Department of Physics, Queen’s University, Kingston, ON K7L 3N6, Canada
109 Institute of Physics and Astronomy, University of Potsdam, D-14476 Potsdam-Golm, Germany
110 Department of Physical Sciences, Munster Technological University, Bishopstown, Cork T12 P928, Ireland
111 Department of Physics, Indiana University-Purdue University Indianapolis, Indianapolis, IN 46202, USA
112 Departament de Física, Universitat Politècnica de Catalunya (UPC), E-08019 Barcelona, Spain
113 Institutt for Fysikk, Norwegian University of Science and Technology, 7491 Trondheim, Norway
114 Center for Astro, Particle and Planetary Physics, New York University Abu Dhabi, PO Box 129188, Abu Dhabi, UAE
115 Institut d’Estudis Espacials de Catalunya (IEEC), E-08034 Barcelona, Spain

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