Measurement of the polarisation of single top quarks and antiquarks produced in the t-channel at $\sqrt{s} = 13$ TeV and bounds on the tWb dipole operator from the ATLAS experiment

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Measurement of the polarisation of single top quarks and antiquarks produced in the $t$-channel at $\sqrt{s} = 13$ TeV and bounds on the $tWb$ dipole operator from the ATLAS experiment

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ABSTRACT: A simultaneous measurement of the three components of the top-quark and top-antiquark polarisation vectors in $t$-channel single-top-quark production is presented. This analysis is based on data from proton–proton collisions at a centre-of-mass energy of 13 TeV corresponding to an integrated luminosity of 139 fb$^{-1}$, collected with the ATLAS detector at the LHC. Selected events contain exactly one isolated electron or muon, large missing transverse momentum and exactly two jets, one being $b$-tagged. Stringent selection requirements are applied to discriminate $t$-channel single-top-quark events from the background contributions. The top-quark and top-antiquark polarisation vectors are measured from the distributions of the direction cosines of the charged-lepton momentum in the top-quark rest frame. The three components of the polarisation vector for the selected top-quark event sample are $P_{x'} = 0.01 \pm 0.18$, $P_{y'} = -0.029 \pm 0.027$, $P_{z'} = 0.91 \pm 0.10$ and for the top-antiquark event sample they are $P_{x'} = -0.02 \pm 0.20$, $P_{y'} = -0.007 \pm 0.051$, $P_{z'} = -0.79 \pm 0.16$. Normalised differential cross-sections corrected to a fiducial region at the stable-particle level are presented as a function of the charged-lepton angles for top-quark and top-antiquark events inclusively and separately. These measurements are in agreement with Standard Model predictions. The angular differential cross-sections are used to derive bounds on the complex Wilson coefficient of the dimension-six $\mathcal{O}_{tW}$ operator in the framework of an effective field theory. The obtained bounds are $C_{tW} \in [-0.9, 1.4]$ and $C_{itW} \in [-0.8, 0.2]$, both at 95% confidence level.

KEYWORDS: Hadron-Hadron Scattering, Top Physics

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1 Introduction

Single-top-quark production through the electroweak (EW) charged current at hadron colliders proceeds mostly, according to the Standard Model (SM) prediction, via three modes that can be defined at leading order (LO) in quantum chromodynamics (QCD): the exchange of a virtual $W$ boson in either the $t$- or $s$-channel, and the associated production of a top quark and a $W$ boson (named $tW$). At the LHC, in proton–proton ($pp$) collision data, the $t$-channel is the dominant process and the subject of the measurements presented in this paper. In the $t$-channel process, a light-flavour quark $q$ from one of the colliding protons interacts with a $b$-quark, which can be considered as being emitted directly from the other
Figure 1. Feynman diagrams for the processes contributing to $t$-channel single-top-quark production at LO, in the five-flavour scheme. In the dominant subprocess, an up- or down-type quark from one of the colliding protons interacts with a bottom quark or antiquark from the other proton by exchanging a virtual $W$ boson to produce a (a) top quark or (d) top antiquark. In the subdominant subprocess, a down- or up-type antiquark from one of the colliding protons interacts with a bottom quark or antiquark from another proton by exchanging a virtual $W$ boson to produce a (b) top quark or (c) top antiquark.

colliding proton (five-flavour scheme or 5FS) or as originating from gluon splitting (four-flavour scheme or 4FS). The incoming light-flavour quark exchanges a space-like virtual $W$ boson, producing a top quark $t$ and a recoiling light-flavour quark $q'$, called the spectator quark. Two subprocesses contribute to the $t$-channel process in the production of either single top quarks ($t$) or single top antiquarks ($\bar{t}$) at LO. The dominant subprocess is the scattering of the incoming up-type (down-type) quark from a bottom quark (antiquark), to produce a down-type (up-type) spectator quark and a top quark (antiquark), as illustrated in figures 1(a) and 1(d). The subdominant subprocess is the scattering of a down-type (up-type) antiquark from a bottom quark (antiquark), to produce an up-type (down-type) spectator antiquark and a top quark (antiquark), as illustrated in figures 1(b) and 1(c). The production cross-section of single top quarks is about twice as large as that of single top antiquarks.

The QCD $pp \rightarrow t\bar{t}$ process produces unpolarised top quarks because of parity conservation in QCD [1–4], while single-top-quark production yields a large sample of highly polarised top quarks and top antiquarks. In the $t$-channel at LO, as a consequence of the vector minus axial-vector $(V - A)$ form of the $tWb$ vertex, single top quarks are produced with their spin completely aligned along the direction of the down-type quarks [5, 6]. For single top quarks produced by the dominant subprocess, this direction is the spectator-quark direction, while for the subdominant subprocess it is the direction of the incoming down-type antiquark. For single top-antiquark production, the spin aligns in the direction opposite to that of the incoming down-type quark in the dominant subprocess, and op-
posite to that of the spectator antiquark in the subdominant process. Thus, the degree of polarisation for a sample of single-top-quark or single-top-antiquark events depends on the mix of dominant and subdominant production processes and the relative alignment between the beam line and spectator-quark directions, averaged over the sample selected. The orientation of the polarisation vector is in the production plane. In all cases the direction is relative to the rest frame of the top quark or antiquark.

In the $t$-channel production process, the spectator-quark direction lies close to the beam direction. The predominant $ub \rightarrow dt$ process (or $ug \rightarrow dtb$ in the 4FS), as well as the similarity of the two aforementioned directions, produces very high (though not 100%) top-quark polarisation along the direction of the spectator quark when both the dominant and subdominant processes are considered. For top antiquarks, the two subprocesses contribute to different degrees, but also lead to nearly 100% polarisation, this time in the direction opposite to that of the spectator quark. At LO in the SM, the expected values of the polarisations of top quarks and top antiquarks along the direction of the spectator quark are 0.90 and $-0.86$, respectively, computed in the 4FS as detailed in ref. [7]. However, effects beyond LO as well as acceptance requirements, which have a large effect on the polarisation, are not accounted for in that calculation. A calculation at next-to-next-to-leading order (NNLO), based on ref. [8], predicts top-quark polarisation along the direction of the spectator quark of $0.965 \pm 0.003$ (scale)$^{+0.003}_{-0.004}$ (PDF + $\alpha_s$) for top quarks and $-0.957^{+0.003}_{-0.012}$ (scale)$^{+0.004}_{-0.002}$ (PDF + $\alpha_s$) for top antiquarks. These values are obtained from a parton-level calculation at fixed order using the CT18nnlo [9] set of parton distribution functions (PDFs) with the renormalisation ($\mu_r$) and factorisation ($\mu_f$) scales set to half of the top-quark mass ($m_t$). This calculation considers stable single top quarks produced in the $t$-channel from $pp$ collisions at $\sqrt{s} = 13$ TeV, in a region with exactly one light-flavour jet, where jets are clustered with the anti-$k_t$ algorithm [10] with a radius parameter of 0.4, and they are required to have $p_T > 30$ GeV and $|\eta| < 4.5$. Additional acceptance criteria for the light-flavour jet, implementing the acceptance requirement defined in eq. (4.2) and described in section 4, were also applied in calculating the prediction. The effect of the scale uncertainty is calculated by varying the renormalisation and factorisation scales by factors of 2.0 and 0.5 from their central value. The effect of the $\alpha_s$ uncertainty is calculated by varying $\alpha_s(m_Z)$ by 0.001 from its central value. The PDF uncertainty is calculated from the 68% confidence level (CL) eigenvectors in the CT18nnlo PDF sets at the most similar $\alpha_s$ value. The effects of the $\alpha_s$ and PDF uncertainties are summed in quadrature. Similar calculations were previously carried out for $pp$ collisions at LO at $\sqrt{s} = 14$ TeV [6], at next-to-leading order (NLO) at $\sqrt{s} = 7$ TeV [11], and in proton–antiproton collisions at LO at Tevatron energies [5]. A general trend is that typical acceptance requirements increase the top-quark polarisation, while effects beyond LO reduce it. NLO EW corrections to the $tWb$ vertex are calculated in refs. [12–16], and ref. [15] explicitly calculates the effect on top-quark polarisation. While that calculation is done for the full phase space of single-top-quark production, rather than the restricted space of the calculation described in this paper, the EW corrections are smaller than those from QCD.

This paper reports a direct measurement of the top-quark and top-antiquark polarisation vectors from a template fit to the joint distributions of the direction cosines of the
charged-lepton momentum in the top-quark rest frame. Each component of the polarisation vector is thereby measured without any assumption about the other two components. In addition, normalised differential cross-sections corrected to a fiducial region at particle level are presented as a function of the charged-lepton angles for top-quark and top-antiquark events separately and inclusively, so that they can be combined with other experimental inputs, to derive bounds on complex Wilson coefficients in the framework of an effective field theory (EFT). In this paper, the inclusive measurements are used to derive bounds on the complex Wilson coefficient of the dimension-six $O_{tW}$ operator.

1.1 Decay angles from polarised top quarks and top antiquarks

This analysis exploits the $t \to Wb \to bl^+\nu$ decay mode of the top quark, as well as the charge-conjugate decay mode of the top antiquark. The lepton $l^\pm$ can be either an electron or a muon. In the decay, three orthogonal directions may be defined \cite{7}. These serve to express the spin vector of the top quark. As illustrated in figure 2, the $\hat{z}'$ direction is the direction of the momentum of the spectator quark, $\vec{p}_q'$, in the top-quark reference frame. The $\hat{y}'$ direction is taken along $\hat{z}' \times \vec{p}_q$, where $\vec{p}_q$ is the direction of the incoming light-flavour quark, in the top-quark reference frame. Then, the $\hat{x}'$ direction lies in the production plane, orthogonal to $\hat{y}'$ and $\hat{z}'$, such that \{x', y', z'\} form a right-handed coordinate system: $\hat{z}' = \vec{p}_q' / |\vec{p}_q'|$, $\hat{y}' = (\hat{z}' \times \vec{p}_q) / |\hat{z}' \times \vec{p}_q|$, and $\hat{x}' = \hat{y}' \times \hat{z}'$.

The polarisation vector $\vec{P}$ is defined in this coordinate system; it satisfies $|\vec{P}| \leq 1$, equality holding if and only if the top quarks are produced in a pure quantum mechanical ensemble with respect to spin. Information about the spin of the top quark is transferred to the decay products, and therefore can be extracted from their angular distributions. This was already exploited in previous analyses \cite{17–21} which measure spin observables in single-top-quark and/or $tt$ events using LHC data. Previous measurement of $t$-channel
single-top-quark polarisation at $\sqrt{s} = 8$ TeV from ATLAS [20] set a limit $|P_z'| > 0.72$ (at 95\% CL) at parton level, where an average is taken over top quarks and top antiquarks. The spin asymmetry $A_\ell = (P_z'\alpha_\ell)/2$, where $\alpha_\ell$ is the analysing power of the charged lepton ($\ell$) in the top-quark decay, was determined to be $0.49 \pm 0.06$ by ATLAS [19] and $0.26 \pm 0.11$ by CMS [22] at $\sqrt{s} = 8$ TeV and measured to be $0.440 \pm 0.070$ by CMS at $\sqrt{s} = 13$ TeV [21]. In all these cases, this was done at parton level, and an average over top quarks and antiquarks was also taken.

As shown in refs. [1–4], the charged lepton is the most sensitive probe of the top-quark spin, with analysing power close to 1; for that reason the analysis is based upon angular distributions of the charged lepton from the top-quark decay. Angular distributions of single top quarks are discussed in ref. [23], where the four-dimensional fully differential decay distribution for the top-(anti)quark decays with polarisation $\vec{P}$ is presented. Equation (11) in that reference is used as the basis for a custom decay model, valid at LO, which is interfaced with the LO PROTON [24] event generator, in order to generate simulated event samples containing pure ensembles of events fully polarised along the $x'$, $y'$, or $z'$ direction. Calculations of top-quark angular decay distributions at NLO and NNLO [25, 26] indicate that higher-order effects are small compared to the precision of this analysis. A fitting function describing angular distributions of event samples with arbitrary polarisation is constructed by taking linear combinations of templates derived from simulated pure ensembles with $x'$, $y'$, or $z'$ polarisation at reconstruction level. The fitting function is then used in a template fit to data, in which the three components of polarisation, $\{P_{x'}, P_{y'}, P_{z'}\}$ are allowed to float without imposing the $|\vec{P}| \leq 1$ constraint. This is the strategy followed in this analysis to measure all components of the polarisation vector $\vec{P}$ for top-quark and top-antiquark events separately. Details of the fit model are given in section 9.

In the coordinate system previously defined, and considering $\theta_{\ell i}$ as the polar angle of the charged-lepton momentum with respect to the $i$th axis ($i = x', y', z'$), one can obtain the differential angular distributions associated with the three different polarisation components $\{P_{x'}, P_{y'}, P_{z'}\}$. These differential angular distributions are distorted by the inefficiencies and acceptance of the detector, smeared by the reconstruction procedures, and sculpted by the event selection criteria. In this paper, the detector effects are unfolded and the measured normalised differential angular distributions are compared directly with theoretical predictions within a fiducial region as detailed in section 10.

1.2 Sensitivity of polarised top-quark decay angles to effective field theory operators

Measurements of polarisation observables in $t$-channel single-top-quark production are sensitive to new physics phenomena affecting the $tWb$ vertex. In the framework of SM EFT [27], the SM Lagrangian ($\mathcal{L}_{\text{SM}}$) is augmented with higher-dimensional operators invariant under the SM gauge symmetry. Since dimension-five operators do not contribute to top-quark production or decay [28], the leading contributions from higher-dimensional operators are from dimension-six operators ($\mathcal{O}_k^{[6]}$). This analysis is therefore limited to those terms, with corresponding Wilson coefficients ($C_k$) scaled by $1/\Lambda^2$:

$$\mathcal{L}_{\text{EFT}} = \mathcal{L}_{\text{SM}} + \sum_k \frac{C_k}{\Lambda^2} \mathcal{O}_k^{[6]} + \ldots,$$
where \( \mathcal{L}_{\text{EFT}} \) is the effective Lagrangian, \( \Lambda \) is the scale of new physics chosen such that higher-dimensional operators are sufficiently suppressed by higher powers of \( \Lambda \), and where \( k \) runs over all dimension-six operators. There are only three dimension-six effective operators that contribute at order \( 1/\Lambda^2 \) at tree level in the \( t \)-channel production of the single top quark as presented in ref. [29]. In the so-called ‘Warsaw’ basis, the three operators are \( \mathcal{O}_{\bar{q}q}, \mathcal{O}_{qq} \) and \( \mathcal{O}_{tW} \) as described in ref. [30], where \( \varphi \) stands for the Higgs field. Other effective operators such as \( \mathcal{O}_{bW} \) and \( \mathcal{O}_{\varphi t\bar{b}} \) contribute but are suppressed by a factor \( 1/\Lambda^4 \) or by the small value of the bottom-quark mass relative to that of the top quark. Within the present limits set on these other operators \([20, 31–36]\), their effect on the polarisation of the top quark is expected to be insignificant compared to the current precision of the measurement.

The operator \( \mathcal{O}_{\varphi q} \) affects the signal production cross-section and has no effect on normalised distributions. The four-fermion operator, \( \mathcal{O}_{qq} \), has a negligible effect on angular distributions [29] and can be ignored. Only the \( \mathcal{O}_{tW} \) operator with its complex coefficient has an effect on the polarisation of the top quark. The real and imaginary parts of its coefficient are indicated in this work by \( C_{tW} \) and \( C_{itW} \), respectively. The coefficient \( C_{tW} \) mostly affects \( P_{x'} \), whereas \( C_{itW} \) affects \( P_{y'} \). Since the SM prediction for \( P_x \) is already near the maximum allowed value, it is less sensitive to changes in \( C_{tW} \) or \( C_{itW} \). A non-zero value for \( C_{itW} \) could be a hint of non-SM CP violation in the \( tWb \) vertex, making it especially interesting with regard to the matter–antimatter asymmetry present in nature.

This formalism is used to perform an interpretation of the unfolded normalised differential angular distributions presented in section 1.1 in an EFT context, providing limits on the real and imaginary parts of the \( \mathcal{O}_{tW} \) dipole operator.

This paper is organised as follows. Section 2 describes the data samples as well as the simulated event samples used to predict properties of the \( t \)-channel signal and the background processes. Section 3 describes the object and event reconstruction for the identification of signal events, while section 4 presents the criteria used to define the signal region and the control regions. The procedures for modelling background processes are described in section 6. The event yields comparing the predictions and the observed data are also shown in this section. Section 8 quantifies the systematic uncertainties in this measurement. Section 9 describes the measurement of the polarisation vector of an ensemble of top quarks or antiquarks. The particle-level differential measurement of the normalised angular distributions is described in section 10, while the way these angular differential cross-section distributions are used to set limits on some EFT coefficients is presented in section 11. The conclusions are given in section 12.

2 Data and simulated event samples

The ATLAS detector\(^1\) [37] at the LHC covers nearly the entire solid angle around the collision point. It consists of an inner tracking detector surrounded by a thin superconducting
solenoid producing a 2 T axial magnetic field, electromagnetic and hadronic calorimeters, and an external muon spectrometer incorporating three large toroidal magnet assemblies. The analysis is performed using pp collision data collected at a centre-of-mass energy of 13 TeV from 2015 to 2018. Stringent detector and data quality requirements were applied [38], resulting in a data sample corresponding to a total integrated luminosity of 139 fb$^{-1}$ [39, 40]. The events were selected by single-lepton\textsuperscript{2} triggers [41, 42], imposing low thresholds on the transverse energy ($E_T$) of electrons and the transverse momentum ($p_T$) of muons, in addition to isolation requirements, or imposing a looser identification criterion and higher thresholds with no isolation requirement. The lowest thresholds varied from 20 to 26 GeV depending on the lepton flavour and the data-taking period.

Samples of simulated events were produced using different Monte Carlo (MC) event generators including parton shower (PS) and hadronisation models. The effect of multiple interactions in the same and neighbouring bunch crossings (pile-up) was modelled by overlaying the hard-scattering event with simulated minimum-bias events generated with PYTHIA8.186 [43, 44] using the NNPDF2.3lo [45] PDF set and the A3 set of tuned parameters [46]. Events were reweighted such that the distribution of the average number of interactions per bunch crossing matches that observed in data.

Single-top-quark $t$-channel events were generated with the NLO POWHEG BOX [47–50] v2 generator, which provides matrix elements (MEs) at NLO in the strong coupling constant $\alpha_s$ using the 4FS with the NNPDF3.0nlo nf4 [51] PDF set. The scales were set to $\mu_T^2 = \mu_F^2 = 16(m_b^2 + p_T^2)$, where $m_b$ and $p_T$ are the mass and $p_T$ of the $b$-quark from the initial gluon splitting.

Additional samples of simulated $t$-channel signal events were produced within the 4FS with the LO PROTOS 2.3 generator [24] using the CTEQ6L1 PDF set [52]. The scales were set to $\mu_T^2 = -p_T^2$ for the light-flavour quark distribution function and $\mu_T^2 = p_T^2 + m_b^2$ for the gluon distribution function, where $p_T$ and $p_T$ are the momentum of the exchanged $W$ boson and the $p_T$ of the $b$-antiquark originating from the gluon splitting, respectively [24, 53]. In addition to a SM signal sample, six samples with $tWb$ anomalous couplings [54, 55], $V_{L,R}$ and $g_{L,R}$, enabled in both the production and decay vertices were produced with the PROTOS event generator. The ranges chosen for the anomalous coupling event samples were based on previous established limits [20]: $Re[g_R]/V_L = \pm 0.18; \quad Im[g_R]/V_L = \pm 0.07; \quad V_R/V_L = \pm 0.4$ and $g_R/V_L = \pm 0.32$. For $V_L = 1$ and $\Lambda = 1$ TeV, following ref. [56], these correspond to $C_{tW} = \pm 2$, $C_{ttW} = \pm 0.8$, and $C_{tWb} = \pm 1$. The PROTOS generator was also modified with a special decay model allowing it to generate event samples with top quarks fully polarised along, or opposite to, the $x'$, $y'$, or $z'$ axes as defined in section 1.1, resulting in six simulated samples in total. These samples are used to produce templates for the determination of top-quark and top-antiquark polarisations.

Furthermore, five samples of simulated signal events with non-zero Wilson coefficients related to dimension-six effective operators were also produced. These simulation samples were generated at NLO, using the same set-up as in ref. [29], with the MADGRAPH5\_AMC@NLO 2.6.2 [57] generator using the NNPDF3.0nlo PDF set. The val-

\textsuperscript{2}Henceforth, ‘lepton’ indicates an electron or muon.
ues of the non-zero Wilson coefficients in the different simulated event samples were set to: $C_{tW} = 2.0$; $C_{tW} = 1.75$; $C_{tW} = -0.4$; $C_{tW} = -2.0$ and $C_{tW} = -0.4$; and $C_{tW} = 2.0$ and $C_{tW} = -1.75$. The EFT operators were allowed to enter in the production vertex as well as the decay vertex, consistently including possible effects on the width of the top quark. The implementation of the NLO effective operators [58] makes use of the 5FS, indicating that the $b$-quark is treated as being massless and thus part of the proton. The two scales were set to $\mu_T = \mu_F = m_t$ in the MC generation.

The $t$-channel signal production cross-section was calculated at NLO [59] in perturbative QCD using HATHOR 2.1 [60, 61]. For pp collisions at $\sqrt{s} = 13$ TeV, this cross-section corresponds to $136 \pm 5$ pb and $81 \pm 4$ pb for top-quark and top-antiquark production, respectively. The cross-section uncertainties connected with the PDFs and $\alpha_s$ were calculated using the PDF4LHC prescription [62] with the MSTW2008nlo 68% CL [63, 64], CT10nnlo [65] and NNPDF2.3nlo PDF sets, and were added in quadrature to the effect of the scale uncertainty.

The production of $tt$ events, as well as single-top-quark events in the $tW$ process and in the $s$-channel, were modelled using the POWHEG Box v2 generator, which provides MEs at NLO, with the NNPDF3.0nlo PDF set. In $tt$ events, the POWHEG Box $h_{\text{damp}}$ parameter\(^3\) was set to $1.5 m_t$ [66]. For the $tt$ process, the scales were set to $\mu_T^2 = \mu_F^2 = m_t^2 + p_{T,t}^2$, where $p_{T,t}$ is the $p_T$ of the top quark, while for the $tW$ and $s$-channel processes these scales were set to $m_t$. In the case of $tW$ associated production, the diagram-removal scheme [67] was employed to handle the interference with $tt$ production [66]. The $tt$ cross-section was calculated at NNLO in QCD including resummation of next-to-next-to-leading logarithmic (NNLL) soft-gluon terms with Top++ 2.0 [68–73]. This cross-section is $832 \pm 35$ (PDF + $\alpha_s$) $\pm 29$ (scale) pb. The cross-section uncertainties due to the PDF and $\alpha_s$ were calculated using the PDF4LHC prescription with the MSTW2008nnlo 68% CL, CT10nnlo [74] and NNPDF2.3nnlo PDF sets, and were added in quadrature to the effect of the scale uncertainty. The $tW$ events are normalised to the predicted production cross-section of $72 \pm 4$ pb calculated at NLO in QCD including NLL soft-gluon corrections [75]. The uncertainty in the cross-section corresponds to the sum in quadrature of the uncertainty derived from the MSTW2008nnlo 90% CL PDF set and the effect of the scale uncertainties. For the $s$-channel process, the inclusive cross-section is corrected to the theory prediction calculated at NLO in QCD with HATHOR. This cross-section is $10.3 \pm 0.4$ pb. The uncertainties in the cross-section due to the PDF and $\alpha_s$ were calculated using the PDF4LHC prescription, similarly to the $t$-channel.

Vector-boson production in association with jets (generally named $V$+jets, or $W/Z$+jets) was simulated with the multi-leg SHERPA 2.2.1 [76] generator. The NNPDF3.0nnlo set [51] of PDFs as well as the dedicated set of tuned PS parameters developed by the SHERPA authors for this version were used. The events were filtered according to their $b$-hadron and $c$-hadron content at the particle level. The ME+PS matching [77] was employed for different jet multiplicities, which were then merged into an

\[^3\]The POWHEG $h_{\text{damp}}$ parameter controls the $p_T$ of the first additional emission beyond the LO Feynman diagram in the PS and therefore regulates the high-$p_T$ emission against which the $tt$ system recoils.
inclusive sample using an improved CKKW matching procedure [78, 79] which is extended to NLO accuracy using the MEPS@NLO prescription [80]. These particular simulations are accurate to NLO for up to two additional partons and accurate to LO for up to four additional partons. The virtual QCD corrections for MEs at NLO accuracy are provided by the OpenLoops library [81, 82]. Fully leptonically and semileptonically decaying diboson (VV) samples were simulated with the SHERPA 2.2.1 ME+PS generator. The ME+PS matching is the same as for the single-boson processes. These particular simulations are accurate to NLO for up to one additional parton and accurate to LO for up to three additional parton emissions using factorised on-shell decays. The inclusive cross-sections for V+jets production were calculated to NNLO accuracy [83] with FEWZ program [84]. For W+ jets production, the overall theoretical uncertainty is 34%. This is the result of adding in quadrature the overall cross-section normalisation uncertainty and 24% per additional jet, according to the Berends–Giele scaling [85].

The production of t\bar{t}Z, t\bar{t}W, tZq, tHq, and tWZ events was modelled by the MadGraph5_AMC@NLO 2.3.3 generator, which provides MEs at NLO in \alpha_s, with the NNPDF3.0nlo PDF set. The production of tH events was modelled using the Powheg Box generator at NLO with the NNPDF3.0nlo PDF set.

All the signal and background processes involving one or more top quarks were simulated assuming a top-quark mass of 172.5 GeV, and the top quark was assumed to decay only into a W boson and a b-quark. In these samples, top quarks and W and Z bosons were decayed at LO using MadSpin [86, 87] to preserve all spin correlations. Moreover, the PS, hadronisation and underlying-event (UE) modelling was simulated with PYTHIA 8.230 or 8.212, using the A14 set of tuned parameters (A14 tune) [88] and the NNPDF2.3lo PDF set. The decays of bottom and charm hadrons were simulated using the EvtGen 1.6.0 or 1.2.0 program [89].

Alternative samples of simulated single-top-quark and t\bar{t} events were also produced, using either different generators or different values of parameters in Powheg+Pythia8 (further details are given in section 8) to estimate the generator modelling uncertainties. For studies of the NLO matching method, MadGraph5_AMC@NLO 2.6.2 or 2.6.0 using either the NNPDF3.0nlo nf4 PDF set for the t-channel process or the NNPDF3.0nlo PDF set for the t\bar{t}, tW and s-channel processes, was used. In these cases, the ME generator was interfaced to Pythia 8.230 or 8.212. To study the PS, the hadronisation and the UE modelling, the Powheg Box v2 generator interfaced to HERWIG 7.04 [90, 91] using the H7UE set of tuned parameters [91] and the MMHT2014lo PDF set [92] was used. In the case of tW associated production, a simulated event sample using the diagram-subtraction scheme [67] is employed to estimate the uncertainty associated with the scheme used to handle the interference with t\bar{t} production.

Dijet events were simulated using Pythia 8.186 with the A14 tune and the NNPDF2.3nlo PDF set, and the decays of bottom and charm hadrons were simulated using the EvtGen 1.2.0 program. Here, 2 \to 2 QCD processes were generated, including multijet, q\bar{q} \to q\gamma, q\bar{q} \to g\gamma, EW (W/Z) and t\bar{t} production processes. This simulated sample was filtered at generator level to enrich the event sample with jets that are likely to resemble electrons with detector signatures. Events were kept if particles in the event (ex-
cluding neutrinos and muons) deposit >17 GeV of energy into a square area $\eta \times \phi = 0.1 \times 0.1$ of the electromagnetic calorimeter, mimicking the highly localised energy deposits characteristic of electrons.

All baseline simulated event samples were passed through the full simulation of the ATLAS detector [93] based on the GEANT4 [94] framework. Simulated samples of fully polarised single top quarks and top antiquarks, used to estimate the impact of anomalous couplings or EFT on the differential measurements, and samples used to evaluate most of the systematic effects were processed with a fast simulation [93] which relies on a parameterisation of the calorimeter response [95].

An extensive software suite [96] is used in the reconstruction and analysis of real and simulated data, in detector operations, and in the trigger and data acquisition systems of the experiment.

3 Object definitions

Electron candidates are reconstructed from clusters of energy deposits in the electromagnetic calorimeter that are matched to a track in the inner-detector tracking system. They are required to satisfy $p_T > 7$ GeV, $|\eta_{\text{cluster}}| < 2.47$ and a ‘tight’ likelihood-based identification requirement [97]. Electron candidates are excluded if their calorimeter clusters lie within the transition region between the barrel and endcap sections of the electromagnetic calorimeter, $1.37 < |\eta_{\text{cluster}}| < 1.52$. The track associated with the electron must pass the requirements $|z_0 \sin \theta| < 0.5$ mm and $|d_0/\sigma(d_0)| < 5$, where $z_0$ is the longitudinal impact parameter with respect to the reconstructed primary vertex, $d_0$ denotes the transverse impact parameter relative to the beam-line axis and $\sigma(d_0)$ is the uncertainty in $d_0$.

Muon candidates are reconstructed from tracks measured in the muon spectrometer matched to tracks measured in the inner-detector tracker in the pseudorapidity range of $|\eta| < 2.5$. They must satisfy $p_T > 7$ GeV along with the ‘medium’ identification requirements defined in ref. [98]. These include requirements on the number of hits in the different inner-detector and muon spectrometer subsystems and on the significance of the charge-to-momentum ratio $q/p$. In addition, the track associated with the muon candidate must have $|z_0 \sin \theta| < 0.5$ mm and $|d_0/\sigma(d_0)| < 3$.

Isolation criteria are applied to the selected electrons and muons. For electrons, the scalar sum of the $p_T$ of tracks within a variable-size cone around the electron, excluding tracks originating from the electron itself, must be less than 6% of the electron $p_T$. The track isolation cone size $\Delta R = \sqrt{(\Delta \eta)^2 + (\Delta \phi)^2}$ is given by the smaller of $\Delta R = 10$ GeV/$p_T$ and $\Delta R = 0.2$. In addition, the sum of the transverse energy of the calorimeter topoclusters in a cone of $\Delta R = 0.2$ around the electron is required to be less than 6% of the electron $p_T$, excluding clusters originating from the electron itself. For muons, the scalar sum of the $p_T$ of tracks within a variable-size cone around the muon (excluding its own track) must be less than 6% of the muon $p_T$, with the track isolation cone size being given by the smaller of $\Delta R = 10$ GeV/$p_T$ and $\Delta R = 0.3$.

Jets are reconstructed from topological clusters of energy deposited in the calorimeter [99] using the anti-$k_t$ algorithm with a radius parameter of 0.4. They are calibrated
through the application of a jet energy scale derived from data and simulation [100]. These jets are required to have $p_T > 30 \text{ GeV}$ and $|\eta| < 4.5$. To suppress jets from additional $pp$ interactions within a bunch crossing, the so-called jet-vertex tagger (JVT) [101] is applied to jets with $p_T < 120 \text{ GeV}$ and $|\eta| < 2.5$. Jets containing $b$-hadrons (named $b$-tagged jets) are identified (tagged) by the MV2c10 $b$-tagging algorithm [102, 103]. The algorithm calculates a multivariate discriminant from information about the impact parameters of associated charged-particle tracks, the properties of reconstructed secondary vertices, and the topology of $b$- and $c$-hadron decays inside the jets. The $b$-tagging efficiency is measured for jets in the pseudorapidity range $|\eta| < 2.5$ and with $p_T > 20 \text{ GeV}$ in simulated $tt$ events. The chosen working point for this analysis corresponds to a $b$-tagging efficiency of 60% [104]. The corresponding mistagging rates for $c$-quark and light-flavour jets are approximately 2.9% and 0.065%, respectively, as predicted in simulated $tt$ events and calibrated in data [105, 106].

The missing transverse momentum in the event, whose magnitude is denoted in the following by $E_{miss}^T$, is defined as the negative vector sum of the $p_T$ of the reconstructed and calibrated objects in the event [107, 108]. This sum also includes a ‘soft term’ consisting of the transverse momenta of inner-detector tracks that are associated with the primary vertex but not with any other objects.

Objects can satisfy both the jet and lepton selection criteria and therefore a procedure called ‘overlap removal’ is applied to ensure that objects are matched to a unique hypothesis. If any electron shares a track with a muon, the electron is removed since it is very likely to correspond to the reconstructed muon. Similarly, if any jet is close to an electron (within $\Delta R < 0.2$), the closest jet is removed. Electrons close to jets (within $\Delta R < 0.4$) are also removed to reduce the impact of non-prompt leptons. To reduce contributions from muons which stem from heavy-flavour decays inside a jet, muons are removed if they are separated from the nearest jet by $\Delta R < 0.4$. Additionally, jets with fewer than three tracks and separated from a muon by $\Delta R < 0.4$ are removed to reduce the number of fake jets from muons depositing a large fraction of their energy in the calorimeters.

4 Event selection in the signal and control regions

Events are required to have at least one vertex reconstructed from at least two inner-detector tracks with transverse momenta of $p_T > 0.5 \text{ GeV}$. The primary vertex for each event is defined as the vertex with the highest sum of $p_T^2$ over all associated inner-detector tracks [109]. The analysis considers only $W$-boson decay modes to an electron or a muon. Events in which the $W$ boson decays to a $\tau$-lepton are thus included if the $\tau$-lepton subsequently decays to an electron or a muon. The signal event candidates are selected by requiring a single isolated lepton, significant $E_{miss}^T$ and exactly two jets. Each muon (electron) is required to have $p_T > 30 \text{ GeV}$ and $|\eta| < 2.5 \ (|\eta| < 2.47$, excluding the region $1.37 < |\eta| < 1.52$), and to satisfy the identification and isolation criteria discussed in section 3. To remove background events from $tt$, $Z +$ jets and diboson production, the event is vetoed if an additional ‘loose’ lepton candidate with $p_T > 10 \text{ GeV}$ is found when applying less stringent lepton identification criteria and no isolation requirements [97, 110, 111].
value of $E_{\text{T}}^{\text{miss}}$ is required to be larger than 35 GeV. Jets in the endcap–forward transition region of the calorimeters, $2.75 < |\eta| < 3.5$, are required to satisfy the more stringent requirement $p_T > 35$ GeV. Exactly one of the jets is required to be $b$-tagged and have $|\eta| < 2.5$. The other, non-$b$-tagged, jet is referred to as the ‘spectator jet’.

Two additional multijet background rejection criteria are applied. The transverse mass of the lepton–$E_{\text{T}}^{\text{miss}}$ system,

$$m_T(\ell, E_{\text{T}}^{\text{miss}}) = \sqrt{2p_T(\ell)E_{\text{T}}^{\text{miss}}(1 - \cos \Delta\phi(p_T(\ell), E_{\text{T}}^{\text{miss}}))},$$

is required to be larger than 60 GeV, and $\Delta\phi(p_T(\ell), E_{\text{T}}^{\text{miss}})$ is the azimuthal angle between the lepton momentum and the $E_{\text{T}}^{\text{miss}}$ direction. Further reduction of this background is achieved by imposing an additional requirement on events where the lepton and the leading jet in $p_T$ have opposite directions in the transverse plane,

$$p_T(\ell) > 50 \left(1 - \frac{\pi - |\Delta\phi(p_T(j_1), p_T(\ell))|}{\pi - 1}\right) \text{ GeV},$$

where $\Delta\phi(p_T(j_1), p_T(\ell))$ is the azimuthal angle between the lepton $p_T$ and the leading jet in $p_T$. This requirement provides significant rejection of background originating from multijet events where two jets are produced back-to-back in the azimuthal plane and one of those is misreconstructed as a lepton. This set of requirements defines the preselection region.

The on-shell $W$ boson originating from the decay of the top quark is reconstructed from the momenta of the lepton and the neutrino by imposing four-momentum conservation. Since the neutrino escapes undetected, the $x$ and $y$ components of the reconstructed $E_{\text{T}}^{\text{miss}}$ are assumed to correspond to the $p_T$ of the neutrino. The unmeasured longitudinal component of the neutrino momentum, $p^\nu_z$, is computed by imposing a $W$-boson mass constraint on the lepton–neutrino system. A quadratic expression is found for $p^\nu_z$, and the solution closer to zero is taken. If the solutions are complex, the reconstructed $E_{\text{T}}^{\text{miss}}$ is rescaled, preserving its direction, in order to have a unique real solution for $p^\nu_z$. The top-quark candidate is then reconstructed by combining the four-momenta of the reconstructed $W$ boson and the selected $b$-tagged jet. Finally, the lepton momentum is boosted into the top-quark rest frame and the angles $\theta_{\ell i}$ ($i = x', y', z'$) are derived by its projection along the axes defined in section 1.1. In doing so, the ambiguity in the direction of the incoming light quark in the laboratory frame is resolved by accepting the direction which is closer to that of the spectator quark, also in the laboratory frame.

Further discrimination between $t$-channel signal events and background events is achieved by applying additional criteria that optimise the signal-to-background ratio (S/B), and thereby determine the signal region. Thus, the following criteria are applied:

- The invariant mass of the lepton–$b$-tagged jet system, $m_{\ell b}$, is required to be lower than 153 GeV.
- The mass of the reconstructed top quark, $m_{\ell \nu b}$, is required to be within 120.6–234.6 GeV.
- The mass of the spectator-jet–top-quark system, $m_{j\ell \nu b}$, is required to be larger than 320 GeV.
A trapezoidal requirement is imposed in order to reject background events from the two-dimensional correlation among the pseudorapidities of the spectator jet, $\eta_j$, and the reconstructed top quark, $\eta_{\ell\nu b}$. This requirement is:

$$
\begin{align*}
\eta_j &< (4 \eta_{\ell\nu b} + a) \quad \& \quad \eta_j > (4 \eta_{\ell\nu b} - a) \\
(\eta_j > (0.44 \eta_{\ell\nu b} + b) \quad \text{or} \quad \eta_j < (0.44 \eta_{\ell\nu b} - b)),
\end{align*}
$$

(4.2)

where the intercept parameters $a$ and $b$ of the lines defining the trapezoid were optimised to be 10 and 2, respectively.

The scalar sum of the $p_T$ of all final-state objects, $H_T$, must be larger than 190 GeV, since the $H_T$ distributions of the backgrounds peak at lower values than the $t$-channel signature.

Additionally, two specific background-enriched control regions, orthogonal to the signal region, are defined in order to estimate the contributions of the most important background processes in the $t$-channel signal region, coming from $t\bar{t}$ and $W^+\text{jets}$ events, by computing scale factors for the overall normalisations. These two specific background-enriched regions are:

- A control region enriched in $t\bar{t}$ events is defined by applying all the preselection requirements, except for the requirement of exactly one $b$-tagged jet; instead, exactly two $b$-tagged jets are required.
- A control region enriched in $W^+\text{jets}$ events is defined by selecting events satisfying the preselection requirements and at least one of the reversed requisites for $m_{\ell b}$, $m_{\ell\nu b}$, $m_{j\ell\nu b}$ or trapezoidal requirement, all from the selection criteria. This control region has a $W^+$ jets flavour composition similar to that in the signal region (in terms of $W^+$ light-jets and $W^+$ heavy-jets contributions).

Table 1 summarises the selection criteria defining the preselection, the signal region and the two control regions used in this analysis. For the separate measurements of top-quark and top-antiquark events, the selected events in each region are further divided into two different regions according to the lepton charge.

5 Particle-level object definition and fiducial region selection

In order to reduce the dependency on phenomenological models which describe colour reconnection, initial- and final-state radiation, and fragmentation, the measured differential angular distributions are unfolded to particle level.

5.1 Particle-level objects

The definitions of the particle-level objects are the same as the ones detailed in ref. [112]. They are constructed from stable particles in the MC event record with a lifetime larger than 30 ps, within the observable pseudorapidity range.
Common event selection criteria

- Exactly one electron or muon
- Veto secondary low-\(p_T\) charged loose leptons
- Exactly two jets
  - \(E_T^{\text{miss}} > 35\) GeV
  - \(m_T(\ell, E_T^{\text{miss}}) > 60\) GeV
  - \(p_T(\ell) > 50\left(1 - \frac{\Delta R(\ell, j)}{2}\right)\) GeV

<table>
<thead>
<tr>
<th>Preselection region</th>
<th>Signal region</th>
<th>tf control region</th>
<th>W+ jets control region</th>
</tr>
</thead>
<tbody>
<tr>
<td>Exactly one b-tagged jet</td>
<td>Exactly one b-tagged jet</td>
<td>Exactly two b-tagged jet</td>
<td>Exactly one b-tagged jet</td>
</tr>
<tr>
<td>(m_b &lt; 153) GeV</td>
<td>(m_b &gt; 153) GeV</td>
<td>(m_{j,b} &lt; 320) GeV</td>
<td>(m_{j,b} &gt; 320) GeV</td>
</tr>
<tr>
<td>(m_{j,b} &gt; 320) GeV</td>
<td></td>
<td>Veto trapezoidal requirement</td>
<td></td>
</tr>
<tr>
<td>Trapezoidal requirement</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>(H_T &gt; 190) GeV</td>
<td></td>
<td>(H_T &lt; 190) GeV</td>
<td></td>
</tr>
</tbody>
</table>

| Table 1. Summary of the selection criteria defining the preselection, the signal region and the two control regions. |

Particle-level leptons are defined as electrons, muons or neutrinos that do not originate from hadron decays, either directly or via a \(\tau\)-lepton decay. Thus, leptons from either a \(W\)- or \(Z\)-boson decay are considered, including those emerging from a subsequent \(\tau\)-lepton decay. In \(t\)-channel single-top-quark events, exactly one such electron or muon is present. No isolation requirement is imposed on the selected charged lepton and the calculation of its four-momentum includes photons within a surrounding cone of size \(\Delta R = 0.1\). The \(E_T^{\text{miss}}\) is calculated from the vector sum of all the selected neutrinos.

Particle-level jets are reconstructed using the anti-\(k_t\) algorithm with a radius parameter of 0.4. All stable particles are used to reconstruct the jets, excluding electrons, muons, neutrinos, and photons used in the definition of the selected charged leptons. A particle-level jet is identified as a \(b\)-tagged jet if the jet is within \(|\eta| < 2.5\) and an associated \(b\)-hadron is found with a ghost-matching technique [113]; the hadron must have \(p_T > 5\) GeV. All particle-level charged leptons identified within a cone of size \(\Delta R = 0.4\) around a selected particle-level jet are removed.

5.2 Fiducial region definition

The differential angular distributions are unfolded to particle level in a fiducial region. This fiducial region is defined so as to be close to the measured phase space, using the particle-level objects defined in section 3. Exactly one particle-level electron or muon with \(p_T > 30\) GeV and \(|\eta| < 2.5\) (excluding the region \(1.37 < |\eta| < 1.52\) for the case of electrons) is required. There must be two particle-level jets with \(p_T > 30\) GeV; exactly one of these jets must be identified as a \(b\)-tagged jet with \(|\eta| < 2.5\) while the other jet must satisfy \(|\eta| < 4.5\). The particle-level \(E_T^{\text{miss}}\) is required to be larger than 35 GeV. The two additional multijet background rejection criteria, i.e. \(m_T(\ell, E_T^{\text{miss}})\) larger than 60 GeV and the requirement in eq. (4.1), and the remaining signal region requirements are also applied to the particle-level objects. The signal region criteria require the reconstruction of the top
Table 2. Summary of the signal selection criteria, applied to particle-level objects, for defining the fiducial region.

<table>
<thead>
<tr>
<th>Fiducial region</th>
</tr>
</thead>
<tbody>
<tr>
<td>Exactly one electron or muon</td>
</tr>
<tr>
<td>Exactly two jets</td>
</tr>
<tr>
<td>Exactly one $b$-tagged jet</td>
</tr>
<tr>
<td>$E_T^{\text{miss}} &gt; 35$ GeV</td>
</tr>
<tr>
<td>$m_T(t, E_T^{\text{miss}}) &gt; 60$ GeV</td>
</tr>
<tr>
<td>$p_T(t) &gt; 50 \left(1 - \frac{\pi -</td>
</tr>
<tr>
<td>$m_{tb} &lt; 153$ GeV</td>
</tr>
<tr>
<td>$m_{\ell\nu b} \in [120.6, 234.6]$ GeV</td>
</tr>
<tr>
<td>$m_{j\ell\nu b} &gt; 320$ GeV</td>
</tr>
<tr>
<td>Trapezoidal requirement</td>
</tr>
<tr>
<td>$H_T &gt; 190$ GeV</td>
</tr>
</tbody>
</table>

quark. In this case, a top-quark proxy, called a pseudo top quark [112], is defined by using the particle-level objects and following exactly the same method described in section 4.

Table 2 summarises the signal selection criteria, applied to particle-level objects, for defining the fiducial region used in this analysis.

6 Background estimation

The largest background contributions to the fiducial region arise from $t\bar{t}$ and $W+$jets production. The former is difficult to distinguish from the $t$-channel single-top-quark signal since $t\bar{t}$ events contain real top quarks in the final state. The $W+$jets production process contributes to the background if there is a $b$-quark in the final state or if a $c$-jet or light-flavour jet is mistagged. Other minor backgrounds originate from $tW$, $s$-channel single-top-quark, $Z+$jets, diboson, $t\bar{t}Z$, $t\bar{t}W$, $tZq$, $tHq$, and $tWZ$ production. Multijet events produced via the strong interaction can also contribute if, in addition to having two reconstructed jets, an extra jet is misidentified as an isolated lepton, or if a non-prompt lepton appears to be isolated.

For all processes except multijet production, the normalisations are initially estimated by using the simulated samples scaled to the theoretical cross-section predictions for $pp$ collisions at $\sqrt{s} = 13$ TeV, discussed in section 2. In the template fit and in the measurement of the angular differential cross-sections, described in section 9 and section 10, respectively, the MC predicted yields for the two major background processes ($t\bar{t}$ and $W+$jets) are normalised to the numbers of data events using the dedicated control regions defined in section 4. The shape of the event distributions is taken from simulation.

The prediction for the normalisation and shape of any multijet distribution is obtained by using the purely data-driven anti-muon model for events containing a muon, and the mixed data–simulation jet-electron model for events containing an electron [114, 115]. In these methods, event distribution templates are derived from data (for the anti-muon method) or from dijet simulation (for the jet-electron method). For the jet-lepton model,
Table 3. Pre-fit event yields in the preselection and signal regions and in the $t\bar{t}$ and $W$+jets control regions for the combined electron and muon channels. The predictions are derived from simulated event samples normalised to the theoretical cross-sections. For multijet production the normalisation is estimated using a data-driven likelihood fit. The label ‘Others’ represents $t\bar{t}Z$, $t\bar{t}W$, $tZq$, $tHq$, and $tWZ$ production. The data-driven scale factors obtained for the top-quark and $W$+jets background processes are not considered when computing these event yields. The uncertainties shown account for systematic effects and the uncertainty due to limited MC sample size. The expected S/B ratio and the ratio of the observed number to the expected number of events are also given.

<table>
<thead>
<tr>
<th>Process</th>
<th>Preselection region</th>
<th>Signal region</th>
<th>$t\bar{t}$ control region</th>
<th>$W$+jets control region</th>
</tr>
</thead>
<tbody>
<tr>
<td>$t$-channel</td>
<td>219 000 ± 11 000</td>
<td>70 600 ± 35 000</td>
<td>13 480 ± 68 000</td>
<td>148 200 ± 7 400</td>
</tr>
<tr>
<td>$t\bar{t}$, $tW$, $s$-channel</td>
<td>736 000 ± 39 000</td>
<td>43 200 ± 2 400</td>
<td>147 800 ± 8 400</td>
<td>693 000 ± 37 000</td>
</tr>
<tr>
<td>$W$+jets</td>
<td>590 000 ± 200 000</td>
<td>26 200 ± 8 900</td>
<td>16 100 ± 5 500</td>
<td>560 000 ± 190 000</td>
</tr>
<tr>
<td>$Z$+jets, diboson</td>
<td>52 900 ± 51 000</td>
<td>21 200 ± 3 500</td>
<td>26 200 ± 3 600</td>
<td>50 800 ± 4 900</td>
</tr>
<tr>
<td>Others</td>
<td>494 ± 38</td>
<td>30 ± 4</td>
<td>79 ± 6</td>
<td>464 ± 36</td>
</tr>
<tr>
<td>Multijet</td>
<td>52 000 ± 10 000</td>
<td>3500 ± 640</td>
<td>5500 ± 1800</td>
<td>48 500 ± 9 400</td>
</tr>
<tr>
<td>Total expected</td>
<td>1 650 000 ± 216 000</td>
<td>145 600 ± 99 000</td>
<td>186 000 ± 10 000</td>
<td>1 510 000 ± 200 000</td>
</tr>
<tr>
<td>Data</td>
<td>1 750 918</td>
<td>154 361</td>
<td>188 326</td>
<td>1 596 557</td>
</tr>
<tr>
<td>S/B</td>
<td>0.15 ± 0.02</td>
<td>0.94 ± 0.13</td>
<td>0.08 ± 0.01</td>
<td>0.11 ± 0.02</td>
</tr>
<tr>
<td>Data/Prediction</td>
<td>1.06 ± 0.13</td>
<td>1.06 ± 0.07</td>
<td>1.02 ± 0.06</td>
<td>1.06 ± 0.14</td>
</tr>
</tbody>
</table>

7 Signal and background event yields

Table 3 provides the predicted signal and background event yields for the combined electron and muon channels in the preselection, signal and control regions. The multijet background is normalised as explained in section 6. Observed data yields are also shown. In addition, the S/B ratio and the ratio of the observed number to the expected number of events (Data/Prediction) are shown for each region.

8 Sources of systematic uncertainty

Various sources of systematic uncertainty affect the signal and background rates and the shape of the kinematic and angular distributions.

In the following, the procedures used to evaluate the systematic uncertainties are described. The systematic uncertainties are grouped into two main categories: experi-
mental uncertainties and theoretical modelling uncertainties. The effect due to the limited size of the simulated event samples is also taken into account when evaluating the total uncertainty.

**Experimental uncertainties:** The uncertainty in the combined 2015–2018 integrated luminosity is 1.7% [39], obtained using the LUCID-2 detector [40] for the primary luminosity measurements. To account for the difference between the pile-up distributions in data and MC simulations, an uncertainty related to the scale factors used to adjust the MC pile-up to the data pile-up profile is applied.

For electrons and muons, the reconstruction, identification, isolation, and trigger performance can differ slightly between data and MC simulation. Scale factors are applied to simulated events to correct for these differences. These scale factors, estimated using the tag-and-probe method [97, 98], as well as the lepton momentum scale and resolution, are assessed using leptonic decays of $Z$ bosons and $J/\psi$ mesons. Corrections to the lepton momentum scale and resolution are applied to data. The associated systematic uncertainties are then propagated to the distributions used in this analysis.

To determine the jet energy scale (JES) uncertainty, information from test-beam data, LHC collision data, and simulation was used, as described in ref. [100]. The JES uncertainty is decomposed into a set of 29 uncorrelated components, with contributions from pile-up, jet flavour composition, single-particle response, and effects of jets not contained within the calorimeter. The jet energy resolution (JER) is measured separately for data and MC simulation, using in situ techniques [100]. The measured relative JER ranges from 22% at 30 GeV to 6% at 300 GeV. Its uncertainty is represented by eight components accounting for jet-$p_T$ and $\eta$-dependent differences between simulation and data. In the measurement of the three components of the polarisation vector, an additional uncertainty is considered in order to take into account the kinematic and sample dependence of the JER uncertainty model. Further details are given in section 9. The systematic uncertainty associated with the JVT is obtained by increasing and decreasing the scale factor used to correct the JVT efficiency in simulation within its uncertainties [101].

The $b$-tagging efficiency and mistagging rates are measured in data using the methods as described in refs. [103, 105, 106], with the systematic uncertainties due to the $b$-tagging efficiency and the mistagging rates calculated separately. The impact of the uncertainties on the $b$-tagging calibration is evaluated separately for $b$-jets, $c$-jets and light-flavour jets.

The systematic uncertainties related to the modelling of the $E_T^{miss}$ in the simulation are estimated by propagating the uncertainties in the energy and momentum scales of electrons, muons and jets, as well as the uncertainties in the resolution and scale of the soft term [107].

**Theoretical modelling uncertainties:** Systematic uncertainties associated with the signal and background MC modelling are estimated by comparing event samples from different generators and by varying parameter values in the event generation.

To assess the uncertainty due to the choice of matching scheme in the $t$-channel single-top-quark signal and single-top-quark background ME generation, sam-
samples from the nominal MC generator POWHEG BOX are compared with those from MADGRAPH5_AMC@NLO, both interfaced to PYTHIA8.

The uncertainty in the PS is estimated for all top-quark processes by comparing samples from POWHEG BOX interfaced to PYTHIA8 with samples from POWHEG BOX interfaced to HERWIG7.

The uncertainty due to missing higher-order QCD corrections in the ME computation is estimated for all top-quark processes by independently varying the renormalisation and factorisation scales by factors of 0.5 and 2.0 from their central value. Additionally, uncertainties due to initial-state radiation from the PS are assessed by varying the corresponding parameter of the A14 parton shower tune \texttt{Var3c} \cite{88}. For the $t\bar{t}$ process and just in the case of the upward variation, the $h_{\text{damp}}$ parameter is also changed and set to $3m_t$ \cite{116}. The uncertainties due to final-state radiation from the PS are assessed by varying the corresponding parameter of the A14 parton shower tune \texttt{Var2} \cite{88} and by varying the renormalisation scale for QCD emission by factors of 0.5 and 2.0.

An additional uncertainty arising from the method used to handle the interference between $tW$ and $t\bar{t}$ production is determined by comparing the $tW$ simulated sample that uses the diagram-subtraction method with the nominal one based on the diagram-removal technique.

In the template fit, described in section 9, an additional uncertainty due to $t$-channel modelling arises from the use of a LO generator (i.e. PROTOs) for the construction of templates in the signal region as detailed in section 9, a choice which was motivated by the possibility of varying the polarisation in a straightforward way. This is determined by comparing the LO PROTOs prediction with the NLO POWHEG BOX prediction.

PDF uncertainties are evaluated using the PDF4LHC15 uncertainty set which consists of 30 eigenvector variations from multiple NLO PDF sets \cite{62}.

The event yields associated with the simulated signal and background processes are estimated using the selection acceptances and the theoretically predicted cross-sections as reported in section 2. The uncertainties in these cross-sections are taken into account. However, for those processes whose normalisation is extracted from the data-driven fits, described in sections 9 and 10, the effect is negligible. The multijet background is normalised through a data-driven analysis based on the techniques described in section 6. A relative systematic uncertainty of 20% (40%) is assigned to this data-driven overall normalisation in the signal and $W+$ jets-dominated ($t\bar{t}$-dominated) regions. It is estimated from fits, as described in section 6, using alternative kinematic variables ($H_T$ and $\Delta\phi(p_T(j_1), p_T(\ell))$ in the electron channel and $\Delta\phi(p_T(\ell), E_T^{\text{miss}})$ in the muon channel) and including modelling uncertainties for the main background processes.

To evaluate the impact of the systematic uncertainty in the shape of the $W+$ jets simulated templates, an upward and downward variation of 30% is applied independently to the $W+b$-jets and $W+c$-jets samples \cite{117}. No variation is considered for $W+$ light-flavour jets production since its contribution is negligible. To evaluate the systematic uncertainty in the shape of the multijet templates, additional MC simulation and data-driven samples were produced, varying the fraction of the jet’s energy that is deposited in the EM calorimeter (jet-electron model) and the ratio of the sum of the transverse
momenta of tracks within a cone of maximum size $\Delta R = 0.4$ to the $p_T$ of the muon (antimuon model). These alternative multijet templates are normalised to the nominal yields and compared with the nominal multijet templates.

**Statistical uncertainties:** statistical fluctuations in the MC simulated event samples contribute to the overall systematic uncertainty. These uncertainties arise from the finite number of simulated background and signal events. This uncertainty is discussed further in sections 9 and 10.

9 Measurement of top-quark and top-antiquark polarisation vectors

The method used to measure the polarisation vector of an ensemble of top quarks or antiquarks that pass the event selection is discussed in this section. The unit vector of the reconstructed lepton momentum in the top-(anti)quark reference frame is first determined in the coordinate system described in section 1.1. The variable $Q$ (also called the *octant variable*) is constructed by slicing the tridimensional phase space into eight octants, in terms of the signs of three variables $\cos \theta_{lx'}$, $\cos \theta_{ly'}$, $\cos \theta_{lz'}$ of this unit vector as illustrated in figure 3. An analysis of the coarsely-binned fully differential top-quark decay distribution described in ref. [23] is afforded by the variable $Q$. Mathematically, it is assigned a value zero through seven according to the equation

$$Q = 4 \cdot \Theta(\cos \theta_{lz'}) + 2 \cdot \Theta(\cos \theta_{lx'}) + \Theta(\cos \theta_{ly'})$$

where $\Theta(\xi)$ is the Heaviside, or unit, step function of the variable $\xi$. The signal region is further divided by lepton charge for a total of 16 bins indexed by $Q_+ = 0, ..., 7$ for bins of positive lepton charge and $Q_- = 0, ..., 7$ for bins of negative lepton charge. Four bins of control data consisting of events with positive and negative leptons in the $W$+jets and the $t\bar{t}$ control regions, as described in section 4, are also considered. These bins, related to the background control region, are indexed by $R \in \{W$+jets, $t\bar{t}\}$ where the sign corresponds to the sign of the charged lepton’s charge. This allows better control of these important backgrounds in the $t$-channel signal region. The event count in these 20 bins constitutes the twenty-bin input data distribution to a binned profile-likelihood fit which is designed to extract the polarisation vector of the top-quark and top-antiquark event sample.

A parameterised fitting function is constructed to describe the distribution in the variable $Q_{\pm}$ of the input data. Adjustable parameters of the function include $\vec{P} = \{P_{x'}, P_{y'}, P_{z'}\}$, separately for top quarks and top antiquarks (i.e. six parameters in total). Nuisance parameters (NPs) include the overall normalisation factors $\beta_k$ for the production of the process $k \in \{t$-channel, $t\bar{t}$, $W$+jets), as well as other NPs, collectively denoted by $\vec{\theta}$, corresponding to the systematic uncertainties described in section 8. The fitting function in the variable $Q_{\pm}$ is determined by the projection of the joint probability density of the four-dimensional fully differential angular decay distribution for the top-(anti)quark decays [23] onto the octant variable $Q_{\pm}$. It is obtained from templates derived from histograms of quantities in events produced using a LO generator (i.e. PROTON). These templates $T_i(Q_{\pm})$, with $i \in \{z_{\pm}' , x', y'\}$, are produced using samples of fully simulated events in which the polarisation of the top (anti)quarks is manipulated to lie fully along the positive or negative $x'$, $y'$, or $z'$ directions. The events are subjected to the same reconstruction procedures and event selection as the data.
Figure 3. Representation of the octant variable $Q$ constructed by slicing the tridimensional phase space into eight octants, according to the signs of the three variables $\cos \theta_{\ell x'}, \cos \theta_{\ell y'}, \cos \theta_{\ell z'}$.

The fitting function $\mu(Q_{\pm})$ for the data is built from these templates plus an additional contribution from background events, also estimated from reconstructed quantities. It describes the expected number of signal events falling within a bin $Q_{\pm}$ and is written as

$$\mu(Q_{\pm}; P, \beta, \theta) = \beta_{t \text{-channel}} \cdot \left\{ \frac{1 + P_{\ell z'}}{2} T_{\ell z'}(Q_{\pm}) + \frac{1 - P_{\ell z'}}{2} T_{\ell z'}(Q_{\pm}) + \frac{P_{\ell x'}}{2} T_{\ell x'}(Q_{\pm}) + \frac{P_{\ell y'}}{2} T_{\ell y'}(Q_{\pm}) \right\} + T_{bkg}(Q_{\pm}; \beta_{W + \text{jets}}, \beta_{t \bar{t}}).$$

Here, $T_{bkg}(Q_{\pm}; \beta_{W + \text{jets}}, \beta_{t \bar{t}})$ is the template for the background, consisting of a sum over all sources of background. Likewise, the number of events in each of the four bins of control data is described by the function $\nu(R_{\pm}; \beta, \theta)$, also derived either from simulation or data-driven methods.

The fitting function is used to construct a likelihood function

$$L(\vec{P}, \vec{\beta}, \vec{\theta}) = \prod_{Q_{+} = 0}^{7} P(N_{Q_{+}}; \mu(Q_{+}; \vec{P}, \vec{\beta}, \vec{\theta})) \prod_{Q_{-} = 0}^{7} P(N_{Q_{-}}; \mu(Q_{-}; \vec{P}, \vec{\beta}, \vec{\theta})) \times \prod_{R_{+} \in \{W + \text{jets}, tt\}} P(N_{R_{+}}; \nu(R_{+}; \vec{\beta}, \vec{\theta})) \prod_{R_{-} \in \{W + \text{jets}, tt\}} P(N_{R_{-}}; \nu(R_{-}; \vec{\beta}, \vec{\theta})) \times \prod_{l} G(\theta_{l}; 0, 1),$$

in which the first line refers to the octants, the second line refers to the control regions, and the third line refers to Gaussian constraints on the NPs $\vec{\theta}$, where $P(N; \lambda)$ indicates a Poisson distribution for $N$ events given expectation $\lambda$, and where $G(m; m_{0}, \sigma)$ indicates a normal distribution in the variable $m$ with mean $m_{0}$ and standard deviation $\sigma$. The full likelihood including all NPs is maximised to extract the six components of $\vec{P}' = \{P_{\ell x}', P_{\ell y}', P_{\ell z}'\}$.
and $\vec{P}^t = \{P^t_{x'}, P^t_{y'}, P^t_{z'}\}$ for top quarks and antiquarks, respectively. Nuisance parameters accounting for systematic uncertainties are not considered in the fit if they have an impact on either normalisation or shape which is below 0.5%.

The angular distributions studied in this paper are sensitive to the JER. The corrections and uncertainties in jet energy are $p_T$ and $\eta$ dependent and were determined with in situ techniques using dijet events. Poorer JER was observed in simulated single-top-quark $t$-channel events than in simulated dijet events. This increase in JER value, which may be attributed to different event kinematics, is also observed in the template fit.

In order to account for the difference, two JER uncertainty models are compared. The nominal fit model is used to obtain the central values for the polarisation. In this model, the JER is allowed to vary independently for each bin of the octant variable and for each control region. With this approach, the role of the single-top-quark $t$-channel events in constraining the JER is reduced. In the second model, $t$-channel events are allowed to have a larger impact on the JER. This is achieved by allowing each uncertainty affecting the JER to vary in a correlated way across all bins, leading to the larger JER value mentioned above. The polarisation is measured again in this second fit. The difference between the polarisations obtained with the two fit models is added in quadrature to the uncertainty obtained from the nominal model in order to get the overall uncertainty for the measurement. This additional uncertainty is more pronounced for $P_{x'}$, while $P_{x'}$ and $P_{y'}$ are much less affected. Figure 4 shows the observed and fitted numbers of events per octant $Q$ for top quarks and top antiquarks, separately, after the nominal fit to data. In this figure, neighboring bins refer to pairs of quadrants lying on opposite sides of the production plane, i.e. differing by the sign of $\cos \theta_{\ell y'}$. The first four bins indicate leptons emitted opposite to the spectator-quark direction in the top-quark reference frame, while the last four bins refer to leptons emitted along the spectator-quark direction, i.e. differing by the sign of $\cos \theta_{\ell z'}$.

The extracted polarisations together with the normalisation factors of the $t$-channel, $tt$ and $W^+\text{jets}$ processes are shown in table 4. The column labelled ‘extracted value’ lists the result for the three normalisations and the six polarisation components, and the total uncertainty for each. In the column labelled ‘(stat.)’ the statistical uncertainty is presented separately. These may be compared with parton-level predictions calculated at NNLO, based on ref. [8], where stable single top quarks produced in the $t$-channel from $pp$ collisions at $\sqrt{s} = 13$ TeV are considered. These predictions are $P_{x'}^t = -0.024 \pm 0.001$ (scale)$^{+0.004}_{-0.007}$ (PDF $+\alpha_s$) and $P_{y'}^t = 0.965 \pm 0.003$ (scale)$^{+0.003}_{-0.004}$ (PDF $+\alpha_s$) for top quarks and $P_{x'}^{\bar{t}} = -0.073 \pm 0.008$ (scale)$^{+0.004}_{-0.004}$ (PDF $+\alpha_s$) and $P_{y'}^{\bar{t}} = -0.957^{+0.003}_{-0.012}$ (scale)$^{+0.004}_{-0.002}$ (PDF $+\alpha_s$) for top antiquarks. Because of CP symmetry in top-quark production, $P_{y'}^t$ and $P_{y'}^{\bar{t}}$ are expected to be zero [7]; equivalently, the polarisation vector is expected to lie in the plane of production, as described in section 1. The only non-zero SM contributions to $P_{y'}^t$ and $P_{y'}^{\bar{t}}$ come from absorptive parts of EW NLO diagrams, which are much smaller than the expected uncertainty of this measurement. These theoretical predictions and their uncertainties are calculated as detailed in section 1.

A summary of the impact of the systematic uncertainties on the value of each polarisation parameter is shown in table 5. The larger cross-section for top-quark versus
top-antiquark production leads to smaller uncertainties for the measured polarisation for top quarks. Systematic effects tend to have symmetric impacts for either side of the production plane, leading to reduced impact on $P_{\ell'}$ versus the other directions. The uncertainties with the largest impact are those due to the JES and JER. This is because the polarisation depends on kinematic angles determined in the top-quark reference frame, and since jet energy and $E_{T}^{\text{miss}}$ are used to reconstruct that frame, uncertainties in the measurement of the jet energy are expected to contribute significantly to the total systematic uncertainty. The finite number of simulated events as well as the $t\bar{t}$ modelling are also important sources of uncertainty. The normalisation factor extracted for the $t$-channel signal contribution is compatible with results obtained in ref. [118].

Figure 5 shows the observed best-fit polarisation measurements of $P_{\ell}$ and $P_{\ell'}$ in the two-dimensional polarisation parameter space. Contours for top quarks and top antiquarks are shown separately at 68% CL, including statistical and systematic uncertainties.

From the present analysis one can conclude that a very high degree of polarisation is observed in $t$-channel production, primarily along the direction of the spectator quark (for top-quark events), or opposite to that direction (for top-antiquark events), in agreement with NNLO QCD predictions.
the sum in quadrature of the individual grouped sources. The total systematic uncertainty is calculated as
the squared uncertainty from the nominal fit, and then taking the square root. An additional
of the resulting uncertainty in the parameter of interest (i.e. for each polarisation component) from
performing a fit where the NPs in the group are fixed to their best-fit values, subtracting the square

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Extracted value (stat.)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$t$-channel norm.</td>
<td>$+1.045 \pm 0.022 \ (\pm 0.006)$</td>
</tr>
<tr>
<td>$W+$ jets norm.</td>
<td>$+1.148 \pm 0.027 \ (\pm 0.005)$</td>
</tr>
<tr>
<td>$t\bar{t}$ norm.</td>
<td>$+1.005 \pm 0.016 \ (\pm 0.004)$</td>
</tr>
<tr>
<td>$P_{x',0}^\ell$</td>
<td>$+0.01 \pm 0.18 \ (\pm 0.02)$</td>
</tr>
<tr>
<td>$P_{y',0}^\ell$</td>
<td>$-0.02 \pm 0.20 \ (\pm 0.03)$</td>
</tr>
<tr>
<td>$P_{y',1}^\ell$</td>
<td>$-0.029 \pm 0.027 \ (\pm 0.011)$</td>
</tr>
<tr>
<td>$P_{y',0}^\ell$</td>
<td>$-0.007 \pm 0.051 \ (\pm 0.017)$</td>
</tr>
<tr>
<td>$P_{y',1}^\ell$</td>
<td>$+0.91 \pm 0.10 \ (\pm 0.02)$</td>
</tr>
<tr>
<td>$P_{y',0}^\ell$</td>
<td>$-0.79 \pm 0.16 \ (\pm 0.03)$</td>
</tr>
</tbody>
</table>

Table 4. Normalisation factors of the $t$-channel, $W+$ jets and $t\bar{t}$ processes together with the
polarisation values as extracted from data, including total and statistical-only uncertainties in
the fit.

<table>
<thead>
<tr>
<th>Uncertainty source</th>
<th>$\Delta P_{x',0}^\ell$</th>
<th>$\Delta P_{x',1}^\ell$</th>
<th>$\Delta P_{y',0}^\ell$</th>
<th>$\Delta P_{y',1}^\ell$</th>
<th>$\Delta P_{y',0}^\ell$</th>
<th>$\Delta P_{y',1}^\ell$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Modelling</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Modelling ($t$-channel)</td>
<td>$\pm 0.037$</td>
<td>$\pm 0.051$</td>
<td>$\pm 0.010$</td>
<td>$\pm 0.015$</td>
<td>$\pm 0.061$</td>
<td>$\pm 0.061$</td>
</tr>
<tr>
<td>Modelling ($t\bar{t}$)</td>
<td>$\pm 0.016$</td>
<td>$\pm 0.021$</td>
<td>$\pm 0.004$</td>
<td>$\pm 0.016$</td>
<td>$\pm 0.003$</td>
<td>$\pm 0.016$</td>
</tr>
<tr>
<td>Modelling (other)</td>
<td>$\pm 0.013$</td>
<td>$\pm 0.031$</td>
<td>$\pm 0.003$</td>
<td>$\pm 0.006$</td>
<td>$\pm 0.026$</td>
<td>$\pm 0.043$</td>
</tr>
<tr>
<td>Jet energy scale</td>
<td>$\pm 0.045$</td>
<td>$\pm 0.048$</td>
<td>$\pm 0.005$</td>
<td>$\pm 0.007$</td>
<td>$\pm 0.033$</td>
<td>$\pm 0.025$</td>
</tr>
<tr>
<td>Jet energy resolution</td>
<td>$\pm 0.166$</td>
<td>$\pm 0.185$</td>
<td>$\pm 0.021$</td>
<td>$\pm 0.040$</td>
<td>$\pm 0.070$</td>
<td>$\pm 0.130$</td>
</tr>
<tr>
<td>Jet flavour tagging</td>
<td>$\pm 0.004$</td>
<td>$\pm 0.002$</td>
<td>$&lt;0.001$</td>
<td>$\pm 0.001$</td>
<td>$\pm 0.007$</td>
<td>$\pm 0.009$</td>
</tr>
<tr>
<td>Other experimental uncertainties</td>
<td>$\pm 0.015$</td>
<td>$\pm 0.029$</td>
<td>$\pm 0.002$</td>
<td>$\pm 0.007$</td>
<td>$\pm 0.014$</td>
<td>$\pm 0.026$</td>
</tr>
<tr>
<td>Multijet estimation</td>
<td>$\pm 0.008$</td>
<td>$\pm 0.021$</td>
<td>$&lt;0.001$</td>
<td>$\pm 0.001$</td>
<td>$\pm 0.008$</td>
<td>$\pm 0.013$</td>
</tr>
<tr>
<td>Luminosity</td>
<td>$\pm 0.001$</td>
<td>$\pm 0.001$</td>
<td>$&lt;0.001$</td>
<td>$&lt;0.001$</td>
<td>$&lt;0.001$</td>
<td>$&lt;0.001$</td>
</tr>
<tr>
<td>Simulation statistics</td>
<td>$\pm 0.020$</td>
<td>$\pm 0.024$</td>
<td>$\pm 0.008$</td>
<td>$\pm 0.015$</td>
<td>$\pm 0.017$</td>
<td>$\pm 0.031$</td>
</tr>
<tr>
<td><strong>Total systematic uncertainty</strong></td>
<td>$\pm 0.174$</td>
<td>$\pm 0.199$</td>
<td>$\pm 0.025$</td>
<td>$\pm 0.048$</td>
<td>$\pm 0.096$</td>
<td>$\pm 0.153$</td>
</tr>
<tr>
<td><strong>Total statistical uncertainty</strong></td>
<td>$\pm 0.017$</td>
<td>$\pm 0.025$</td>
<td>$\pm 0.011$</td>
<td>$\pm 0.017$</td>
<td>$\pm 0.022$</td>
<td>$\pm 0.034$</td>
</tr>
</tbody>
</table>

Table 5. Systematic and statistical uncertainties in the measurement of the polarisation vector $\vec{P}$ for top quarks and top antiquarks. The impact of each group of uncertainties is obtained by
performing a fit where the NPs in the group are fixed to their best-fit values, subtracting the square
of the resulting uncertainty in the parameter of interest (i.e. for each polarisation component) from
the squared uncertainty from the nominal fit, and then taking the square root. An additional
uncertainty from the JER is included, consisting of the difference between the central values of the
nominal fit model and the alternative fit model in which JER variations are implemented coherently
across all bins of the octant variable distribution. The total systematic uncertainty is calculated as
the sum in quadrature of the individual grouped sources.
Figure 5. Summary of the observed best-fit polarisation measurements with their statistical-only (green) and statistical+systematic (yellow) contours at 68% CL, plotted on the two-dimensional polarisation parameter space ($P_{x'}$, $P_{z'}$). The interior of the black circle represents the physically allowed region of the parameter space, and the red point indicates the parton-level prediction at NNLO from a calculation based on ref. [8]. The uncertainty in the theoretical prediction includes scale, $\alpha_s$ and PDF uncertainties. Correlations between the predictions of the polarisation parameters are not provided.

10 Angular differential cross-sections for top-quark production

Three angular differential cross-sections are obtained from the distribution of the charged-lepton momentum with respect to the $i^{th}$ axis ($i = x', y', z'$), as defined in section 1.1. These three distributions are associated with the three top-quark polarisation components ($\{P_{x'}, P_{y'}, P_{z'}\}$). The selection criteria for reconstructed events, defined in section 4, are the same as the used for the measurement of top-quark and top-antiquark polarisation vectors in section 9. These differential angular distributions are distorted by finite resolution of the detector and the trigger, reconstruction, and sculpted by the event selection criteria. The detector effects are corrected using an unfolding technique.

In the measurement of the angular differential cross-sections, the normalisation of the $W+\text{jets}$ and top-quark background (i.e. $t\bar{t}$, $tW$, and $s$-channel) contributions is estimated through a simultaneous maximum-likelihood fit to the numbers of data events observed in the signal region and the two control regions. All other backgrounds are fixed to their theoretical or data-driven predictions. The overall normalisation of the $t$-channel signal is treated as another free parameter in the fit. The likelihood function [119] is given by the product of Poisson probability terms associated with the three regions (signal region and $t\bar{t}$ and $W+\text{jets}$ control regions). The fit is performed separately for the signal and control regions defined with positively (negatively) charged leptons for the measurement
of top-quark (top-antiquark) events, as well as for the inclusive regions containing both lepton charges. These normalisation factors are compatible with those extracted in the template fit described in section 9 and with the theoretical predictions.

The angular distributions observed at reconstruction level are shown in figure 6 for the inclusive signal region. They are compared with the predicted signal and background distributions, normalised to the results of the maximum-likelihood fit. The selection requirements have a significant impact on the shapes of these distributions.

Figure 6. Post-fit distributions of (a) \(\cos \theta_{lx'}\), (b) \(\cos \theta_{ly'}\) and (c) \(\cos \theta_{lz'}\) in the signal region. The data, shown as the black points with statistical uncertainties, are compared with SM signal and background predictions. The multijet background is estimated using MC and data-driven techniques, while contributions from simulated \(W+\) jets and top-quark background and \(t\)-channel signal event samples are normalised to the results of a maximum-likelihood fit to event yields in the signal and control regions. The label ‘others’ represents \(t\bar{t}Z\), \(t\bar{t}W\), \(tZq\), \(tHq\), and \(tWZ\) production. The uncertainty bands include both the statistical and systematic uncertainties. The lower panels show the ratio of data to prediction in each bin.
The measured angular distributions are unfolded to the particle level within the fiducial region. The particle-level selection criteria are discussed in section 5. The unfolding corrections account for distortions due to detector resolution and efficiencies so as to allow direct comparison with theoretical predictions. In this analysis the same unfolding technique as in ref. [120] is used. D’Agostini’s iterative Bayesian approach [121] as implemented in RooUnfold [122] is used to unfold the distributions. The measured expectation value for the number of signal events at particle level in each bin \( k \) of the fiducial volume, \( \nu_{k}^{\text{particle}} \), is obtained from the observed number of events in each bin \( j \) of the reconstructed distribution \( N_{j}^{\text{data}} \), after subtracting the sum of all background contributions \( B_{j} \), according to

\[
\nu_{k}^{\text{particle}} = C_{k}^{\text{particle}\rightarrow\text{reco}} \sum_{j} M_{jk}^{-1} C_{j}^{\text{reco}\rightarrow\text{particle}} (N_{j}^{\text{data}} - B_{j}),
\]

where \( M_{jk} \) is the migration matrix which relates the particle-level and reconstructed values, and \( C_{k}^{\text{reco}\rightarrow\text{particle}} \) is a correction factor that accounts for events that pass reconstruction selection but not particle-level selection. It is defined as

\[
C_{j}^{\text{reco}\rightarrow\text{particle}} = \frac{S_{j}^{\text{reco}} - S_{j}^{\text{reco}\rightarrow\text{particle}}}{S_{j}^{\text{reco}}},
\]

where \( S_{j}^{\text{reco}} \) is the number of reconstructed signal events in bin \( j \) and \( S_{j}^{\text{reco}\rightarrow\text{particle}} \) is the number of events that pass the reconstruction-level selection but not the particle-level selection. Another correction factor, \( C_{k}^{\text{particle}\rightarrow\text{reco}} \), accounts for signal events that pass the particle-level selection but not the reconstruction-level selection:

\[
C_{k}^{\text{particle}\rightarrow\text{reco}} = \frac{1}{\epsilon_{k}} = \frac{S_{k}^{\text{particle}}}{S_{k}^{\text{particle}} - S_{k}^{\text{particle}\rightarrow\text{reco}}},
\]

where \( S_{k}^{\text{particle}} \) is the number of signal events at particle level and \( S_{k}^{\text{particle}\rightarrow\text{reco}} \) is the number of events that pass the particle-level selection but not the reconstruction-level selection. The factor \( C_{k}^{\text{particle}\rightarrow\text{reco}} \) is the inverse of the efficiency \( \epsilon_{k} \) for signal events at particle level in bin \( k \) to pass the reconstruction-level requirements.

Each normalised differential cross-section is determined by dividing the obtained \( \nu_{k}^{\text{particle}} \) value in each bin by the integral over all bins.

The migration matrix and the selection efficiency are computed using samples of \( t \)-channel signal events simulated with the POWHEG BOX+PYTHIA8 generator described in section 2. They are calculated for the signal region defined with positively (negatively) charged leptons for the measurement of top-quark (top-antiquark) events, as well as for the inclusive signal region containing both lepton charges. The obtained \( C_{k}^{\text{reco}\rightarrow\text{particle}} \) correction factors are around 50\% and the efficiencies \( \epsilon_{k} \) around 20\% for all bins.

The number of bins was chosen in order to have a stable unfolding response with at least 70\% of the events in the diagonal elements of the migration matrix. This criterion results in eight bins for the \( \cos \theta_{\ell x'} \) and \( \cos \theta_{\ell y'} \) distributions and four bins for the \( \cos \theta_{\ell z'} \) distribution for which larger migrations are observed. The number of iterations is chosen such that the absolute change between two successive steps becomes negligible (the difference must be
smaller than 0.1% of the integral of the associated distribution) and when a convergent state is reached the difference between the results obtained with the chosen number of iterations and with 15 more iterations should not exceed 0.15% of the integral of the associated distribution for all bins. This stability criterion results in five iterations for the $\cos\theta_{\ell x}'$ distribution and three for both the $\cos\theta_{\ell y}'$ and $\cos\theta_{\ell z}'$ distributions.

The stability of the unfolding procedure was validated through convergence and closure tests performed by using template distributions constructed from the $t$-channel Powheg Box + Pythia8, Protos+Pythia8 and MadGraph5_aMC@NLO+Pythia8 samples. The closure tests showed that the residual bias induced by the unfolding method is negligible. By using template distributions given by the Protos+Pythia8 and MadGraph5_aMC@NLO+Pythia8 samples, generated including effects on the $tWb$ vertex from anomalous couplings or additional EFT operators, it is shown that the unfolding method recovers the generated distributions at particle level within the fiducial region.

The statistical uncertainty of the data unfolded result is determined by running over an ensemble of 100 000 pseudo-experiments, varying the content of each bin according to its expected statistical uncertainty through Poisson fluctuations. For each pseudo-experiment a new background normalisation is extracted using the procedure described above. After background subtraction, each pseudo-experiment is unfolded and normalised. The spread (RMS) of the result in each bin is taken as the measure of the statistical uncertainty.

The uncertainty associated with the finite size of the simulated samples is evaluated using 100 000 pseudo-experiments, varying for each process (excluding the data-driven multijet background) the total prediction in each bin according to the statistical uncertainty through Gaussian fluctuations. The same procedure as for the data statistical uncertainty is then used.

The impact of each source of systematic uncertainty is evaluated by unfolding template distributions resulting from simulated pseudo-data modified to reflect the effect of the given uncertainty source. In each case a new background normalisation estimation is performed before its subtraction from the pseudo-data, using the fitting procedure described above. For all sources of systematic uncertainty the nominal unfolding corrections are considered. Except for the signal modelling uncertainties affecting the unfolding corrections, the systematic uncertainty is evaluated as the difference between the nominal angular distribution values and the ones measured using the varied normalisations and shapes. For the signal modelling uncertainties, the unfolded varied distribution is compared with the corresponding particle-level spectra.

The resulting normalised angular differential cross-sections at particle level within the fiducial region are displayed in figures 7 and 9 for the inclusive, top-quark and top-antiquark measurements. The measured cross-sections include both the statistical and systematic uncertainties, and are compared with the predictions given by the different generators. Among the different uncertainty sources, those related to JER and JES are dominant. The measured distributions are consistent with those obtained from a Protos simulation sample with the polarisations given by the template fit described in section 9.

A global covariance matrix of size 20×20, corresponding to the 20 measured bins in figures 7 and 9 and including the effects of all uncertainties and the correlations among
Figure 7. Particle-level normalised differential cross-sections as a function of (a) $\cos \theta_{lx'}$, (b) $\cos \theta_{ly'}$, and (c) $\cos \theta_{lz'}$, along with various SM MC predictions of the $t$-channel signal for both top quarks and top antiquarks. The data, shown as the black points with statistical uncertainties, are compared with predictions (lines) obtained by using the POWHEG BOX+PYTHIA8 (solid red), PROTONS+PYTHIA8 (dashed blue), MADGRAPH5_AMC@NLO+PYTHIA8 (long-dashed green) and POWHEG BOX+HERWIG7 (dot-dashed violet) generators. The uncertainty bands include both the statistical and systematic uncertainties. The data statistical uncertainty is too small to be visible. The lower panels show the ratio of prediction to data in each bin.
Figure 8. Particle-level normalised differential cross-sections as a function of (a) $\cos \theta_{lx'}$, (b) $\cos \theta_{ly'}$, and (c) $\cos \theta_{lz'}$, along with various SM MC predictions of the $t$-channel signal for top quarks. The data, shown as the black points with statistical uncertainties, are compared with predictions (lines) obtained by using the Powheg Box+Pythia8 (solid red), Protos+Pythia8 (dashed blue), MadGraph5_AMC@NLO+Pythia8 (long-dashed green) and Powheg Box+Herwig7 (dot-dashed violet) generators. The uncertainty bands include both the statistical and systematic uncertainties. The data statistical uncertainty is too small to be visible. The lower panels show the ratio of prediction to data in each bin.
Figure 9. Particle-level normalised differential cross-sections as a function of (a) $\cos \theta_{lx'}$, (b) $\cos \theta_{ly'}$, and (c) $\cos \theta_{lz'}$, along with various SM MC predictions of the $t$-channel signal for top antiquarks. The data, shown as the black points with statistical uncertainties, are compared with predictions (lines) obtained by using the \textsc{Powheg Box}+\textsc{Pythia}8 (solid red), \textsc{Protos}+\textsc{Pythia}8 (dashed blue), \textsc{MadGraph5}_\textsc{amc@nlo}+\textsc{Pythia}8 (long-dashed green) and \textsc{Powheg Box}+\textsc{Herwig7} (dot-dashed violet) generators. The uncertainty bands include both the statistical and systematic uncertainties. The data statistical uncertainty is too small to be visible. The lower panels show the ratio of prediction to data in each bin.
the three angular distributions, is computed in order to perform quantitative comparisons with theoretical predictions.

An initial ensemble of 50000 pseudo-experiments is used to compute the covariance matrix with the systematic uncertainties and the uncertainty associated with the limited size of the simulated samples. In each pseudo-experiment, Gaussian-distributed shifts are applied coherently for each detector-modelling systematic uncertainty by scaling each bin of the data distribution by the expected relative variation from the associated systematic uncertainty effect. For the uncertainty due to the limited size of the simulated samples the Gaussian-distributed shifts are computed independently for each bin. The varied distribution is unfolded with the nominal corrections after subtracting the backgrounds with the normalisation factors derived following the procedure described in section 6. Additional Gaussian-distributed shifts are then applied coherently for each signal- and background-modelling systematic uncertainty. The modelling shifts are derived by using the expected relative variations from the associated systematic uncertainty to scale each bin of the data distribution unfolded with the nominal corrections. The resulting modified unfolded distributions are used to compute an initial matrix.

The statistical correlations between the three different angular distributions are evaluated using the bootstrap method [123], using a set of 1000 bootstrap samples. The global statistical matrix is calculated using the statistical error of each bin of the angular distributions and the correlation coefficients. This matrix is then added to the previous one to compute an unnormalised global covariance matrix.

Finally, a set of 100000 additional pseudo-experiments is used to normalise the covariance matrix. For each additional pseudo-experiment, each element of the three angular distributions is fluctuated using a multivariate Gaussian distribution with the unnormalised global covariance matrix. The resulting pseudo-experiments are normalised and are used to calculate the normalised global covariance matrix.

To quantify the level of agreement between each of the measured normalised differential cross-sections and the theoretical predictions, $\chi^2$ values are calculated according to the relation $\chi^2 = V_{N_b-1}^T \cdot \text{Cov}_{N_b-1}^{-1} \cdot V_{N_b-1}$. Here $N_b$ is the number of bins in the spectrum under consideration, $V_{N_b-1}$ is a vector with the differences between the measured and the predicted cross-sections obtained by discarding one of the $N_b$ elements, and $\text{Cov}_{N_b-1}$ is the $(N_b-1) \times (N_b-1)$ sub-matrix derived from the relevant $N_b \times N_b$ part of the global covariance matrix by discarding the corresponding row and column. A global $\chi^2$ value is also obtained using the full vector of differences for the three angular distributions and the full global covariance matrix. In this case, three elements of the vector and their corresponding rows and columns in the covariance matrix are discarded.

The $p$-values, relative to the Powheg Box+Pythia8 SM predictions, are then evaluated from the $\chi^2$ values and the number of degrees of freedom (NDF) of each angular distribution, as shown in table 6. Since these are normalised cross-sections, the NDF corresponds to the number of bins in each angular distribution minus one. The obtained values show good agreement of the SM prediction with the measured data. The high $p$-values for $\cos \theta_{\ell x'}$ distribution may indicate that the evaluation of systematics uncertainties is overly conservative.
Table 6. The $\chi^2$ and $p$-value of the three unfolded angular distributions for the top-quark, for the top-antiquark and for both the top-quark and top-antiquark measurements. The numbers are computed by comparing the observed data with the Powheg Box+Pythia8 SM predictions. The NDF corresponds to the number of bins of each angular distribution minus one. A global $\chi^2$ and $p$-value for the three angular distributions are also included.

<table>
<thead>
<tr>
<th>Angular variable</th>
<th>Top quark $\chi^2$/NDF $p$-value</th>
<th>Top antiquark $\chi^2$/NDF $p$-value</th>
<th>Top quark and antiquark $\chi^2$/NDF $p$-value</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\cos \theta_{t'x'}$</td>
<td>1.35/7 0.99</td>
<td>0.94/7 1.00</td>
<td>1.32/7 0.99</td>
</tr>
<tr>
<td>$\cos \theta_{t'y'}$</td>
<td>4.57/7 0.71</td>
<td>2.92/7 0.89</td>
<td>3.78/7 0.81</td>
</tr>
<tr>
<td>$\cos \theta_{t'z'}$</td>
<td>1.55/3 0.67</td>
<td>2.04/3 0.56</td>
<td>2.26/3 0.52</td>
</tr>
<tr>
<td>Global</td>
<td>13.55/17 0.70</td>
<td>6.86/17 0.99</td>
<td>9.25/17 0.93</td>
</tr>
</tbody>
</table>

11 Bounds on EFT coefficients $C_{tW}$ and $C_{itW}$

The unfolded and normalised distributions of $\cos \theta_{t'x'}$ and $\cos \theta_{t'y'}$ are used to set bounds on the complex Wilson coefficient of the dimension-six operator $O_{tW}$. The operator $O_{tW}$ has only a small effect on the $\cos \theta_{t'z'}$ distribution, which in contrast to the $\cos \theta_{t'x'}$ and $\cos \theta_{t'y'}$ distributions is sensitive to many additional EFT operators [124]. The $\cos \theta_{t'z'}$ distribution is therefore ignored in this work. The data are compared with the effects of this dipole operator in a likelihood fit which requires a theoretical prediction in a parametric form. To describe the angular distributions as a function of $C_{tW}$ and $C_{itW}$, a morphing technique [125, 126] is employed to interpolate from a set of 15 MC templates generated as described in section 2. The $O_{tW}$ operator contributes to the production and decay of the top quark. All orders of the EFT expansion parameter $\Lambda$ are included in the parametric description, allowing studies of the effects from high-dimensional (up to $1/\Lambda^8$) terms, which are usually assumed negligible.

The EFT operator can contribute to both the production and decay of the top quark, which leads to 15 terms in the weight function:

$$\sigma(C_{tW}, C_{itW}) = \sigma_1 + \left( C_{tW}^1 \cdot \sigma_2 + C_{itW}^1 \cdot \sigma_3 \right)/\Lambda^2 + \left( C_{tW}^2 \cdot \sigma_4 + C_{itW}^2 \cdot \sigma_5 + C_{tW}^3 \cdot C_{itW}^1 \cdot \sigma_6 \right)/\Lambda^4 + \left( C_{tW}^3 \cdot \sigma_7 + C_{itW}^3 \cdot \sigma_8 + C_{tW}^2 \cdot C_{itW}^1 \cdot \sigma_9 + C_{tW}^1 \cdot C_{itW}^2 \cdot \sigma_{10} \right)/\Lambda^6 + \left( C_{tW}^4 \cdot \sigma_{11} + C_{itW}^4 \cdot \sigma_{12} + C_{tW}^2 \cdot C_{itW}^1 \cdot \sigma_{13} + C_{tW}^3 \cdot C_{itW}^3 \cdot \sigma_{14} + C_{tW}^2 \cdot C_{itW}^2 \cdot \sigma_{15} \right)/\Lambda^8.$$ 

This expression includes all orders of the EFT expansion ($\Lambda$) with the numerical factors originating from the squaring absorbed in the $\sigma_n$ terms, with $n = 1, ..., 15$. The positions in $C_{tW}$ and $C_{itW}$ of 15 simulated event samples was chosen such that the uncertainty in the weight function is a small contribution to the total uncertainty over the parameter-space.
The obtained limits for the coefficients at 68% CL and 95% CL are given in Table 7. The best-fit values for the coefficients are \( C_{tW} \) and \( C_{tW} \) simultaneously is shown in figure 10, where good agreement between the model and the data is observed. Good agreement with the SM prediction from the measured angular differential cross-section. The likelihood contains the uncertainties of the 15 \( \sigma_n \) terms, due to the limited size of the MC samples used to produce the templates, together with the uncertainty of the unfolded measurement contained in a covariance matrix.

The 16×16 covariance matrix for the 16 bins of the measured normalised \( \cos \theta_{t'W} \) and \( \cos \theta_{t'b} \) distributions is the corresponding sub-matrix of the global matrix described in section 10. This matrix has two redundant dimensions caused by the fact that the angular distributions \( \cos \theta_{t'W} \) and \( \cos \theta_{t'b} \) are both normalised and are obtained from the same dataset. In the implementation of the fitting procedure, the covariance matrix is first diagonalised and the data is projected onto the eigenvectors with non-zero eigenvalues.

The robustness of the fit is tested in three ways. It was checked that the unfolding procedure which uses SM-derived corrections can correctly recover non-zero EFT coefficients over a range that spans the current bounds. Secondly, the effect of non-zero EFT coefficients on the background subtraction was proven to be smaller than the measurement uncertainties. Lastly, when applied to MC samples produced by the MadGraph5_AMC@NLO+Pythia8 generator with non-zero values for other EFT operator coefficients \( (C_{tb}, C_{tW}, C_{tb'}, C_{tb}) \), the stability of the fit for \( C_{tW} \) and \( C_{tW} \) was found to be well within the current experimental precision.

The result of fitting \( C_{tW} \) and \( C_{tW} \) simultaneously is shown in figure 10, where good agreement between the model and the data is observed. Good agreement with the SM prediction from the NLO MadGraph5_AMC@NLO+Pythia8 generator is also seen. The best-fit values for the coefficients are \( C_{tW} = 0.3 \pm 0.6 \) (1.1) and \( C_{tW} = -0.3 \pm 0.2 \) (0.5) at 68% CL (95% CL), which is consistent with the SM prediction, as shown in figure 11. The obtained limits for the coefficients at 68% CL and 95% CL are given in table 7. The individual fit result for each coefficient is also obtained by fixing the other coefficient to zero, which results in \( C_{tW} = 0.1 \pm 0.5 \) (1.1) and \( C_{tW} = -0.3 \pm 0.2 \) (0.5) respectively, where the results are quoted for 68% CL (95% CL).

Among previous constraints on \( C_{tW} \), the strongest come from measurements of the values of the \( W \)-boson helicity fractions in top-quark pair decays by ATLAS [127] and CMS [128], with the combined result [36] providing bounds of \([-0.48, 0.29]\) at 95% CL when only \( C_{tW} \) is allowed to vary. Comparable limits were also derived from EFT fits of

<table>
<thead>
<tr>
<th>( C_{tW} )</th>
<th>( C_{tW} )</th>
</tr>
</thead>
<tbody>
<tr>
<td>( 68% ) CL</td>
<td>( 95% ) CL</td>
</tr>
<tr>
<td>All terms</td>
<td>([-0.3, 0.8])</td>
</tr>
<tr>
<td>Order 1/( \Lambda^4 )</td>
<td>([-0.3, 0.8])</td>
</tr>
<tr>
<td>Order 1/( \Lambda^2 )</td>
<td>([-0.3, 0.8])</td>
</tr>
</tbody>
</table>

Table 7. Obtained limits on the real \( (C_{tW}) \) and imaginary \( (C_{tW}) \) coefficient of the \( \mathcal{O}_{tW} \) operator. Also shown are the limits when only the terms up to a specific order in \( \Lambda \) are taken into account.
Figure 10. Comparison of data and the result of the EFT fit for the polarisation angles (a) \( \cos \theta_{lx'} \) and (b) \( \cos \theta_{ly'} \). The solid points show the data, unfolded to particle level. The solid red line corresponds to the EFT prediction using the best-fit values for the Wilson coefficients \( C_{tW} = 0.3 \) and \( C_{itW} = -0.3 \). The blue dashed line represents the SM prediction obtained with the MadGraph5_AMC@NLO+Pythia8 generator. The brown dotted (green dash-dotted) line shows the model at its upper (lower) 95% CL bounds for (a) \( C_{tW} = 1.4 \) \( (C_{itW} = -0.9) \) and (b) \( C_{itW} = 0.2 \) \( (C_{itW} = -0.8) \) also obtained with the MadGraph5_AMC@NLO+Pythia8 generator. The uncertainty bands include both the statistical and systematic uncertainties. The lower panel gives the ratio of the model to the data.

Figure 11. The observed best-fit value (dot) for the Wilson coefficients \( C_{tW} \) and \( C_{itW} \) with the uncertainty contours at 68% CL (dashed) and 95% CL (solid). The CLs are obtained in a simultaneous fit of the two parameters using the prediction obtained with the MadGraph5_AMC@NLO+Pythia8 generator. The red star indicates the SM prediction.
the top-quark sector [31–34] that include those measurements. However, the constraints obtained in those analyses assume $C_{tW} = 0$, which is not assumed in the result presented here. Very stringent individual limits on $C_{tW}$ were obtained from electric dipole moment analyses [129] when only $C_{tW}$ is allowed to be non-zero, but these become much weaker when multiple EFT coefficients are allowed to vary simultaneously. In that case, the previous limits on $C_{tW}$ were dominated by the input from ATLAS [18], which provides bounds on $C_{tW}$ of $[-2.3, 3.0]$ at 95% CL. A global fit including real and imaginary parts of all $tWb$ operators [35] gives $C_{tW} \in [-0.8, 0.7]$ and $C_{itW} \in [-2.3, 1.6]$, where the bound on $C_{itW}$ was dominated by the ATLAS result [19]. Also given in table 7 are the limits when a certain cut-off on the order of $\Lambda$ is applied.

It is observed that including terms up to $1/\Lambda^4$, which corresponds to the squared terms of a dimension-six coefficient, yields identical limits to retaining all 15 terms. The relatively small change in the result obtained with only $1/\Lambda^2$ terms indicates that there is only a modest dependence on $1/\Lambda^4$ terms. The usual assumption that terms beyond $1/\Lambda^4$ can be excluded is also validated.

12 Conclusions

The polarisation of single top quarks and antiquarks produced in the $t$-channel has been measured in 139 fb$^{-1}$ of 13 TeV $pp$ collision data collected with the ATLAS detector at the LHC. An analysis of the full polarisation vector of the top quarks (antiquarks) finds very high polarisation along (against) the direction of the spectator quark in the top-quark (top-antiquark) reference frame. The three components of polarisation are measured to be $P_x' = 0.01 \pm 0.18$, $P_y' = -0.029 \pm 0.027$, $P_z' = 0.91 \pm 0.10$ for top quarks and $P_x' = -0.02 \pm 0.20$, $P_y' = -0.007 \pm 0.051$, $P_z' = -0.79 \pm 0.16$ for top antiquarks. The results are consistent with NNLO QCD predictions and expectation of $P_t = P_{\bar{t}} = 0$ from the hypothesis of CP symmetry in the top-quark and top-antiquark decay.

Normalised differential cross-sections for top-quark production are measured at particle level as a function of the emission angle of the charged lepton resulting from the $t \to Wb \to \ell\nu b$ decay. They are provided for top quarks and antiquarks, both inclusively and separately. Such distributions are associated with the top-quark polarisation components. The measurements are consistent with SM predictions provided by various MC generators at LO and NLO in QCD.

An EFT prediction is fitted to the measured differential cross-sections to obtain exclusion limits simultaneously for the real and imaginary parts of the $\mathcal{O}_{tW}$ operator. Using a morphing technique, 95% CL intervals for these operators are found to be $C_{tW} \in [-0.9, 1.4]$ and $C_{itW} \in [-0.8, 0.2]$, compatible with the SM predictions obtained with the NLO MadGraph5_aMC@NLO+Pythia8 generator. The bounds on $C_{tW}$ presented in this paper improve on previous results from ATLAS.
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