Search for Higgs bosons decaying into new spin-0 or spin-1 particles in four-lepton final states with the ATLAS detector with 139 fb$^{-1}$ of pp collision data at $\sqrt{s} = 13$ TeV

The ATLAS Collaboration

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Search for Higgs bosons decaying into new spin-0 or spin-1 particles in four-lepton final states with the ATLAS detector with $139 \text{ fb}^{-1}$ of $pp$ collision data at $\sqrt{s} = 13 \text{ TeV}$

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**ABSTRACT:** Searches are conducted for new spin-0 or spin-1 bosons using events where a Higgs boson with mass 125 GeV decays into four leptons ($\ell = e, \mu$). This decay is presumed to occur via an intermediate state which contains two on-shell, promptly decaying bosons: $H \to XX/ZX \to 4\ell$, where the new boson $X$ has a mass between 1 and 60 GeV. The search uses $pp$ collision data collected with the ATLAS detector at the LHC with an integrated luminosity of $139 \text{ fb}^{-1}$ at a centre-of-mass energy $\sqrt{s} = 13 \text{ TeV}$. The data are found to be consistent with Standard Model expectations. Limits are set on fiducial cross sections and on the branching ratio of the Higgs boson to decay into $XX/ZX$, improving those from previous publications by a factor between two and four. Limits are also set on mixing parameters relevant in extensions of the Standard Model containing a dark sector where $X$ is interpreted to be a dark boson.

**KEYWORDS:** Beyond Standard Model, Hadron-Hadron Scattering, Higgs Physics

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1 Introduction

Although the Higgs boson was discovered at the Large Hadron Collider (LHC) in 2012 [1, 2], there is good reason to believe that the description of the Higgs sector of the Standard Model (SM) is still incomplete. Besides the well-known issues of naturalness and baryon asymmetry, astrophysical observations implying the existence of dark matter motivate extensions to the Higgs sector of the SM, particularly those that propose the existence of a ‘dark’ (i.e., hidden) sector, with its own hidden-sector particles [3, 4].

An attractive way to search for new physics in the Higgs sector is through non-standard (‘exotic’) decays of the Higgs boson. Existing precision measurements of the properties of the Higgs boson still allow a branching ratio of up to about 30% to non-standard decays (assuming that the couplings of the Higgs boson to the W and Z bosons are not larger than their SM values) [5–7]. Further, since the SM predicts a very narrow decay width for the Higgs boson, even a small coupling to a new light state could result in a significant branching ratio to that state. In addition, new hidden-sector particles may preferentially couple to the Higgs boson, making it a ‘portal’ to explore this new physics [8–11]. Such exotic decays of the Higgs boson are predicted by many proposed extensions to the SM, including models with a first-order electroweak phase transition [12, 13], models with neutral naturalness [14–16], and models with a hidden sector [17–27], as well as by several models of dark matter [3, 28–32], including some posited to explain observed excesses of astrophysical positrons [33–35]. They are also predicted by the Next-to-Minimal Supersymmetric Standard Model (NMSSM) [36–41].

This paper reports three related searches, each of which looks for a SM Higgs boson $H$ decaying via a new boson into a final state consisting of four charged leptons ($\ell \equiv e, \mu$). All use the full LHC Run 2 data set of about $139 \text{ fb}^{-1}$ that the ATLAS detector collected from proton-proton collisions at a centre-of-mass energy of $\sqrt{s} = 13 \text{ TeV}$. Following the models motivating these analyses, the new boson could be either a dark-sector vector boson or a scalar boson, denoted by $X$. The three searches considered are:

- **High-mass (HM):** $H \rightarrow XX \rightarrow 4\ell$ (15 GeV $< m_X < 60$ GeV).
- **Low-mass (LM):** $H \rightarrow XX \rightarrow 4\mu$ (1 GeV $< m_X < 15$ GeV).
- **Single Z boson (ZX):** $H \rightarrow ZX \rightarrow 4\ell$ (15 GeV $< m_X < 55$ GeV).

The LM analysis uses only the 4$\mu$ final state because the selection efficiency for isolated muons is significantly larger than that for isolated electrons in this mass range (see section 5.4). These searches are sensitive to any intermediate bosons within the considered mass ranges that are narrow, on-shell, and decay promptly. This paper provides model-independent fiducial cross-section limits, as well as limits based on the specific models described in section 2.

This work extends previous searches performed by ATLAS with $20 \text{ fb}^{-1}$ of data collected at $\sqrt{s} = 8 \text{ TeV}$ [42] and with $36 \text{ fb}^{-1}$ of data collected at $\sqrt{s} = 13 \text{ TeV}$ [43]. In addition to a larger data sample and improved lepton identification, the signal region selection of the HM analysis has been re-optimized. Other similar searches, including searches for pairs of
light bosons decaying into muons, τ-leptons, photons, and/or jets, as well as searches for a single light boson decaying into a pair of muons, using both $\sqrt{s} = 8$ TeV and 13 TeV data, have been performed by ATLAS [44–48], CMS [49–52], and LHCb [53]. Further searches for a SM Higgs boson decaying into undetected particles are reported in refs. [54, 55].

This section is followed by a summary of the theoretical models used in the interpretation of the results (section 2). Next, the detector is described (section 3), followed by discussions of features that are common to all three analyses, including the samples of data and simulated events (section 4), the reconstruction of lepton candidates and of their combinations (sections 5.1 and 5.2), the event selections (section 5.3), and the common systematic uncertainties (section 6). Next, aspects specific to each analysis are described (sections 7 to 9). Finally, the ways the analyses are combined to extract limits, and the interpretations of the results in terms of the theoretical models, are presented in section 10, and a summary is given in section 11.

2 Benchmark models

2.1 Dark bosons

Many theories of dark matter posit a hidden sector [17–26, 56], which does not interact with SM particles except via a mediator or portal interaction (besides gravity). A concrete realization of such a mediator involves adding a field with a U(1)$_d$ dark gauge symmetry [21–26] which mixes kinetically with the SM U(1)$_Y$ hypercharge gauge field with some strength $\epsilon$ [57–59]. The gauge boson of this symmetry is the Z$_d$ vector boson, also called a ‘dark photon’.

The coupling strength of the Z$_d$ boson to SM particles, and hence its lifetime (assuming no significant decays to non-SM particles), is determined by the mixing parameter $\epsilon$. The decays of the Z$_d$ boson, on the other hand, are determined by the gauge couplings, and the decay branching ratios are largely independent of $\epsilon$ for $\epsilon \ll 1$. Over the Z$_d$ mass range 1 GeV $< m_{Z_d} < 60$ GeV, the branching ratio for decays into electron or muon pairs can be 10%–15% [21]. Over the same mass range, the decay is prompt for $\epsilon \gtrsim 10^{-5}$ [21]. For smaller values of $\epsilon$, the decay vertex would be significantly displaced from the interaction point, while for $\epsilon \lesssim 10^{-8}$ the lifetime of the Z$_d$ boson becomes long enough for it to likely escape the detector. Also, the decay width of the Z$_d$ boson is very small ($\ll 1$ GeV) for $\epsilon \ll 1$ and $m_{Z_d} < 60$ GeV. ATLAS and CMS have searched for these long-lifetime signatures in collisions at energies of both 8 TeV [60–63] and 13 TeV [64–68].

If the U(1)$_d$ symmetry is broken by an additional dark Higgs boson $s$, then there could be mixing with strength $\kappa$ between the SM Higgs boson and the dark Higgs boson [21–26]. The observed Higgs boson would be one of the mass eigenstates and could also decay into dark-sector particles, including dark Higgs bosons that subsequentially decay into SM fermions. The dark Higgs boson would inherit the Yukawa couplings from the SM Higgs boson and decay preferentially into high-mass fermion pairs.

A further possibility is mass mixing between the Z$_d$ boson and the SM Z boson [23, 24]. If the mass term for this mixing is written as $\epsilon_Z m_Z^2 Z Z_d$, with $\epsilon_Z = \delta m_{Z_d}/m_Z$, then $\delta$ is the model parameter describing the mixing.
Figure 1. Exotic decays of the Higgs boson into four leptons induced by intermediate dark vector bosons via (a) the hypercharge portal (to which the ZX analysis is sensitive) and (b) the Higgs portal, where $s$ is a dark Higgs boson [21] (to which the HM and LM analyses are sensitive). The $Z_d$ gauge boson decays into SM particles through kinetic mixing with the hypercharge field (with branching ratios that are nearly independent of $\epsilon$). The $HZZ_d$ vertex factor is proportional to $\epsilon$ whereas the $HZ_dZ_d$ vertex factor is proportional to $\kappa$. (c) illustrates the decay of a Higgs boson into dark Higgs scalars $s$ or pseudoscalars $a$ that couple to SM particles through mixing with the SM Higgs field in models with an extended Higgs sector (section 2.2).

The processes probed in this paper that involve a SM Higgs boson decaying into $Z_d$ bosons are depicted in figures 1(a) and 1(b) and are included in the Hidden Abelian Higgs Model (HAHM) [21]. The decay $H \to ZZ_d$ is sensitive to the parameters $\epsilon$ and $m_{Z_d}$, but does not depend on $\kappa$. However, the presence of an irreducible background from the SM $H \to ZZ^*$ process means that this signal can be observed only as a peak in the dilepton mass spectrum over the background. The process $H \to Z_dZ_d$, in contrast, is much more easily separated from SM backgrounds and hence is potentially sensitive to smaller values of the kinetic mixing $\epsilon$, where it is only required that the mixing be large enough for the $Z_d$ boson to decay promptly. However, this process does require mixing between the SM and dark-sector Higgs bosons and thus depends on $\kappa$.

Limits on the kinetic mixing of $\epsilon \lesssim 0.03$ have been set from precision electroweak measurements [21, 69, 70] over the range $1 \text{ GeV} < m_{Z_d} < 200 \text{ GeV}$. Searches for dilepton resonances, $pp \to Z_d \to \ell\ell$, at the LHC for $m_{Z_d} < m_H$ imply that $\epsilon \lesssim 0.005–0.020$ for $20 \text{ GeV} < m_{Z_d} < 80 \text{ GeV}$ [71]. Other searches rule out $\epsilon \gtrsim 10^{-3}$ for $10 \text{ MeV} < m_{Z_d} < 10 \text{ GeV}$ [72–77]. The $H \to XX \to 4\ell$ analyses constrain the Higgs mixing parameter $\kappa$, while the $H \to ZZ_d \to 4\ell$ analysis provides information about the kinetic mixing parameter $\epsilon$.

2.2 Extended Higgs sectors

Models containing two Higgs doublets and an additional scalar field (2HDM+S) [22, 78] are also relevant for the search for $H \to XX \to 4\mu$. Two-Higgs-doublet models (2HDMs) generically contain two neutral scalars $H_{1,2}$, two charged scalars $H^\pm$, and one neutral pseudoscalar $A$. The lighter of the neutral scalars $H_1$ is identified as the observed Higgs boson $H$, while the other states are constrained to be heavy by existing data [79, 80]. Adding a complex scalar singlet that mixes weakly with $H_{1,2}$ gives two additional states, a scalar $s$ and a pseudoscalar $a$. If these are lighter than $m_H/2$, then $H \to aa$ and $H \to ss$
decays are allowed (figure 1(c)). This paper probes the process \( H \rightarrow aa \rightarrow 4\mu \), but limits on \( H \rightarrow aa \rightarrow 4\mu \) also apply to \( H \rightarrow ss \rightarrow 4\mu \).

The decays of the scalar and pseudoscalar into fermions are determined by their Yukawa couplings [22], implying that the branching ratio to electrons is very small, and that the branching ratio to muons is smaller than that of the \( Z_d \) vector bosons described previously. Branching ratios for \( H \rightarrow aa \) and \( a \rightarrow \mu \mu \) can be significant in the range \( 2m_\mu < m_a < 2m_\tau \), ranging from \( 10^{-2} \) to \( 10^{-1} \) in some regions of parameter space [22]. In 2HDMs, there are several possible ways for the Higgs sector to couple to fermions. Of these, type-III models (in which leptons and quarks couple to different Higgs doublets) at large \( \tan \beta \) (where \( \tan \beta \) is the ratio of the vacuum expectation values of the two Higgs doublets) are particularly interesting for these analyses. A light pseudoscalar can correspond to the \( R \)-symmetry limit of the NMSSM [81, 82], which reduces the need for fine-tuning and addresses the \( \mu \)-problem [83]. Searches for exotic decays of the Higgs boson into new light scalars or pseudoscalars have been carried out for a variety of mass ranges and final states with both LHC [42, 43, 45–50, 68, 84–89] and Tevatron [90] data.

3 ATLAS detector

The ATLAS detector [91] at the LHC covers nearly the entire solid angle around the collision point.\(^1\) It consists of an inner tracking detector surrounded by a thin superconducting solenoid, electromagnetic and hadron calorimeters, and a muon spectrometer incorporating three large superconducting air-core toroidal magnets.

The inner-detector system (ID) is immersed in a 2 T axial magnetic field and provides charged-particle tracking in the range \(|\eta| < 2.5\). The high-granularity silicon pixel detector covers the vertex region and typically provides four measurements per track, the first hit normally being in the insertable B-layer (IBL) installed before Run 2 [92, 93]. It is followed by the silicon microstrip tracker, which usually provides eight measurements per track. These silicon detectors are complemented by the transition radiation tracker (TRT), which enables radially extended track reconstruction up to \(|\eta| = 2.0\). The TRT also provides electron identification information based on the fraction of hits (typically 30 in total) above a higher energy-deposit threshold corresponding to transition radiation.

The calorimeter system covers the pseudorapidity range \(|\eta| < 4.9\). Within the region \(|\eta| < 3.2\), electromagnetic calorimetry is provided by barrel and endcap high-granularity lead/liquid-argon (LAr) calorimeters, with an additional thin LAr presampler covering \(|\eta| < 1.8\) to correct for energy loss in material upstream of the calorimeters. Hadron calorimetry is provided by the steel/scintillator-tile calorimeter, segmented into three barrel structures within \(|\eta| < 1.7\), and two copper/LAr hadron endcap calorimeters. The

\(^1\)ATLAS uses a right-handed coordinate system with its origin at the nominal interaction point (IP) in the centre of the detector and the \( z \)-axis along the beam pipe. The \( x \)-axis points from the IP to the centre of the LHC ring, and the \( y \)-axis points upwards. Cylindrical coordinates \((r, \phi)\) are used in the transverse plane, \( \phi \) being the azimuthal angle around the \( z \)-axis. The pseudorapidity is defined in terms of the polar angle \( \theta \) as \( \eta = -\ln \tan(\theta/2) \), and the rapidity is defined in terms of energy \( E \) and momentum \( p \) as \( y = (1/2)\ln((E + p_z)/(E - p_z)) \). Angular distance is measured in units of \( \Delta R \equiv \sqrt{(\Delta \eta)^2 + (\Delta \phi)^2} \).
solid angle coverage is completed with forward copper/LAr and tungsten/LAr calorimeter modules optimized for electromagnetic and hadronic energy measurements respectively.

The muon spectrometer (MS) comprises separate trigger and high-precision tracking chambers measuring the deflection of muons in a magnetic field generated by the superconducting air-core toroidal magnets. The field integral of the toroids ranges between 2.0 and 6.0 T m across most of the detector. A set of precision chambers covers the region $|\eta| < 2.7$ with three layers of monitored drift tubes, complemented by cathode-strip chambers in the forward region, where the background is highest. The muon trigger system covers the range $|\eta| < 2.4$ with resistive-plate chambers in the barrel, and thin-gap chambers in the endcap regions.

Interesting events are selected by the first-level trigger system implemented in custom hardware, followed by selections made by algorithms implemented in software in the high-level trigger [94]. The first-level trigger accepts events from the 40 MHz bunch crossings at a rate below 100 kHz, which the high-level trigger reduces in order to record events to disk at about 1 kHz.

An extensive software suite [95] is used in the reconstruction and analysis of real and simulated data, in detector operations, and in the trigger and data acquisition systems of the experiment.

4 Data and simulated event samples

The results in this paper are based on 139 fb$^{-1}$ of $\sqrt{s} = 13$ TeV proton-proton ($pp$) collision data collected with the ATLAS detector over the period 2015–2018.

Monte Carlo (MC) simulation is used to determine expected contributions from both the signal processes and most background processes. For most samples, detector effects were included using a Geant4 [96] simulation of the ATLAS detector [97]. The $H \rightarrow aa$, $H \rightarrow ZZ_d$, and $H \rightarrow Za$ signal samples, as well as a portion of the $gg \rightarrow ZZ^*$ and triboson background samples, instead used a fast simulation [97] which relies on a parameterization of the calorimeter response [98]. The effects of pile-up (additional $pp$ collisions in the same or a neighbouring bunch crossing) are included in the simulation. Weights are applied to the simulated events to correct for small differences between data and simulation in the reconstruction, identification, isolation, and impact parameter efficiencies for electrons and muons [99–101]. Further, the lepton momentum scales and resolutions in the simulation are adjusted to match the data [99, 101, 102]. Table 1 summarizes the samples and generators used, which include MadGraph5_aMC@NLO version 2.2.2 [103], Powheg Box v2 [104–108], Pythia 8.186 [109] (along with EvtGen 1.2.0 [110] to decay heavy-flavour hadrons), and Sherpa 2.2.0, 2.2.1, and 2.2.2 [111].

Signal samples involving a $Z_d$ vector boson were generated according to the HAHM [21, 22, 25, 26] implementation in MadGraph5_aMC@NLO, with the Higgs bosons being produced via gluon-gluon fusion (ggF) and the Higgs boson mass set to $m_H = 125$ GeV. For the $H \rightarrow Z_dZ_d$ process, $\epsilon$ and $\kappa$ were both set to $10^{-4}$ and samples were generated with $m_{Z_d} = 0.5$ GeV, 1 GeV, 2 GeV, and every 5 GeV in the range $5 \text{ GeV} \leq m_{Z_d} \leq 60$ GeV. For the $H \rightarrow ZZ$ process, $\kappa$ was changed to $10^{-10}$, and samples were generated every 5 GeV.
Table 1. Overview of the event generators used for the simulated signal and background samples. For each process, the table lists the matrix element (ME) generator used along with the parton distribution function (PDF), the model used to implement parton showering (PS), the underlying event (UE), and the decay of heavy-flavour hadrons (HF), as well as the set of tuned parameters used to model the UE. The text gives the full version numbers of the generators.

<table>
<thead>
<tr>
<th>Process</th>
<th>ME generator</th>
<th>ME PDF</th>
<th>PS/UE/HF model</th>
<th>UE tune</th>
</tr>
</thead>
<tbody>
<tr>
<td>$H \rightarrow Z_{a}Z_{a} / ZZ_{a}$</td>
<td>MadGraph5_aMC@NLO</td>
<td>NNPDF2.3lo [112]</td>
<td>Pythia/EvtGen</td>
<td>A14 [113]</td>
</tr>
<tr>
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<td>Pythia/EvtGen</td>
<td>AZNLO [114]</td>
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<tr>
<td>$H \rightarrow Za$</td>
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<td>AZNLO</td>
</tr>
<tr>
<td>$ggF$</td>
<td>Powheg Box</td>
<td>PDF4LHC15NNLO</td>
<td>Pythia/EvtGen</td>
<td>AZNLO</td>
</tr>
<tr>
<td>$VBF$</td>
<td>Powheg Box</td>
<td>CT10nlo [116]</td>
<td>Pythia/EvtGen</td>
<td>AZNLO</td>
</tr>
<tr>
<td>$VV$</td>
<td>Powheg Box</td>
<td>NNPDF2.3lo [112]</td>
<td>Pythia/EvtGen</td>
<td>A14</td>
</tr>
<tr>
<td>$ggZH$</td>
<td>Powheg Box</td>
<td>NNPDF3.0nlo</td>
<td>Pythia/EvtGen</td>
<td>AZNLO</td>
</tr>
<tr>
<td>$bbH$</td>
<td>MadGraph5_aMC@NLO</td>
<td>NNPDF2.3lo</td>
<td>Pythia/EvtGen</td>
<td>A14</td>
</tr>
<tr>
<td>$t\bar{t}H$</td>
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<tr>
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<td>NNPDF3.0nlo</td>
<td>Pythia/EvtGen</td>
<td>A14</td>
</tr>
</tbody>
</table>

in the range $15 \text{ GeV} \leq m_{Z_{a}} \leq 55 \text{ GeV}$. Final states with $\tau$-leptons were not included; the change in signal region yield due to the omission of these decays was below 1% and thus neglected. The much smaller production of signal events by vector-boson fusion (VBF), $VH$, and $t\bar{t}H$ was also omitted.

Samples for $H \rightarrow aa$ were simulated using Powheg Box at next-to-next-to-leading order (NNLO) for arbitrary inclusive $gg \rightarrow H$ observables by reweighting the Higgs boson rapidity to that of HNNLO [104, 117–120]. Again, only the ggF production process was considered. Higgs boson decays into two scalars and thence into muons were simulated at leading order (LO) using Pythia. Samples were generated for $m_{a} = 0.5, 1, 2, 2.5, 4, 6, 8, 10, 15, 30, 45,$ and $60 \text{ GeV}$. Samples for $H \rightarrow Za$ were generated similarly, for $m_{a} = 1, 2, 4, 6, 8, 10, 15, 20, 25,$ and $30 \text{ GeV}$. Prompt-lepton backgrounds are estimated directly from MC simulations. They arise primarily from the SM $H \rightarrow ZZ^{*} \rightarrow 4\ell$ process along with the non-resonant $ZZ^{*} \rightarrow 4\ell$ process. Smaller leptonic backgrounds arise from triboson production as well as $t\bar{t} + Z$ decays. Decays involving $Z \rightarrow \tau\tau$ were found to contribute negligibly to the background yields and are thus not included in the simulation. Backgrounds with jets misidentified as leptons are estimated with data-driven methods, detailed below in the individual analysis sections.

The $H \rightarrow ZZ^{*} \rightarrow 4\ell$ background process comprises various Higgs boson production modes. The ggF process $gg \rightarrow H$ [104–108, 121] was simulated in the same way as the
$H \to aa$ signal sample described above. The prediction was normalized to the next-to-next-to-leading-order (N^3LO) cross section in QCD with next-to-leading-order (NLO) electroweak corrections \cite{122–133}. The VBF process \cite{106–108, 134} was simulated using Powheg Box at NLO. The prediction was normalized to an approximate-NNLO cross section in QCD with NLO electroweak corrections \cite{135–137}. Associated production with a vector boson ($VH$) \cite{138–145} was simulated at LO, while $t\bar{t}$ and $b\bar{b}$ associated production ($t\bar{t}H$, $b\bar{b}H$) \cite{103, 146}, as well as loop-induced Higgs and $Z$ boson production ($ggZH$) \cite{147}, were simulated at NLO.

The non-resonant $q\bar{q} \to ZZ^* \to 4\ell$ background process \cite{148} was simulated using Sherpa 2.2.2 at NLO for up to one additional parton and at LO for up to three additional partons. Matrix element calculations were matched and merged with the Sherpa parton shower based on the Catani-Seymour dipole factorization \cite{149, 150} using the MEPS@NLO prescription \cite{151–154}. The virtual QCD corrections are provided by the OpenLOOPS library \cite{155–157}. The gluon-initiated process ($gg \to ZZ^* \to 4\ell$) was simulated in the same manner, except that it was at LO, and the s-channel $H$ diagrams were omitted to avoid double-counting. The gluon-initiated process has a large QCD correction at NLO, so the cross section was scaled by a NLO/LO $K$-factor of $1.70 \pm 0.15$ \cite{158}. Interference between the $gg \to ZZ^* \to 4\ell$ and $gg \to H \to ZZ^* \to 4\ell$ processes is neglected.

Higher-order electroweak processes include triboson production ($VVV$) and vector-boson scattering (VBS). These processes can yield final states with four leptons along with two additional particles. They were generated with Sherpa 2.2.2 at NLO for the inclusive processes and at LO for up to two additional partons, with the same treatment as for $q\bar{q} \to ZZ^* \to 4\ell$. Higgs boson production via VBF was subtracted from these samples in order to avoid double-counting.

The process $t\bar{t} + (Z \to \ell\ell)$ was generated with Sherpa 2.2.0 at LO with up to one additional parton emission.

Other, reducible, backgrounds have fewer than four prompt leptons in the final state, but can be accepted by the signal selection if there are additional leptons from heavy-flavour decay or jets misidentified as leptons. The $Z +$ jets process was generated with Sherpa 2.2.1 using NLO matrix elements for up to two partons and LO matrix elements for up to four partons. The $t\bar{t}$ process was generated with Powheg Box at NLO with the $h_{\text{damp}}$ parameter, which regulates the high-$p_T$ radiation against which the $t\bar{t}$ system recoils, set to $1.5m_{\text{top}} = 258$ GeV \cite{159}. The $WZ$ process was also generated with Powheg Box at NLO with the CT10NLO PDF.

5 Event reconstruction and selection

5.1 Lepton reconstruction

For the analyses considered in this paper, the final-state objects of interest are electrons and muons.

Electrons are reconstructed and identified from charged-particle tracks in the ID that match energy deposits in the calorimeters \cite{99}. The identification algorithm, based on a likelihood analysis, corresponds to the ‘Loose’ selection described in ref. \cite{99}. The
reconstruction and identification efficiency for electrons from $Z \rightarrow ee$ decays is about 90\% per electron [99].

Muon reconstruction [101] begins by independently finding tracks in both the ID and MS. These track candidates are combined in a second step along with information from the calorimeters to form muon candidates of different types. Combined muons have matching tracks in both the MS and ID. Segment-tagged muons have an ID track but only a single-chamber track segment in the MS. Calorimeter-tagged (CT) muons have no MS track but have a pattern of energy deposition in the calorimeters consistent with a muon; this is used only in regions where the MS is not fully instrumented ($|\eta| < 0.1$). Finally, stand-alone (SA) muons have an MS track but no ID track, and are used in regions beyond the coverage of the ID, $2.5 < |\eta| < 2.7$. Due to the reduced performance of the latter two types, no more than one CT or SA muon may be used in an event. Muons are then identified by imposing quality requirements, corresponding to the ‘Loose’ selection in ref. [101]. The reconstruction and identification efficiency for muons from $W \rightarrow \mu\nu$ decays is greater than 98\% [101].

To avoid identifying the same detector signature as multiple particles, an electron candidate that has the same ID track as a muon candidate is ignored, unless the muon is only calorimeter-tagged, in which case the muon is ignored instead. Electrons that have the same track or cluster as a higher-$p_T$ electron are also ignored.

5.2 Invariant kinematic mass variables

All three analyses considered in this paper involve looking for mass resonances in final states consisting of a quadruplet of two same-flavour opposite-sign (SFOS) lepton pairs: $(e^+e^- + e^+e^-)$, $(e^+e^- + \mu^+\mu^-)$, or $(\mu^+\mu^- + \mu^+\mu^-)$. The invariant masses of the two pairs are denoted by $m_{12}$ and $m_{34}$, where $m_{12}$ is taken to be the one closer in mass to the $Z$ boson, $|m_{12} - m_Z| < |m_{34} - m_Z|$.

If all four leptons have the same flavour, then for a given $m_{12}$ and $m_{34}$ labelling, alternative SFOS pairings can also be defined. An invariant mass $m_{14}$ is constructed from the positively charged lepton of the $m_{12}$ pair and the negatively charged lepton of the $m_{34}$ pair. The other alternative pairing $m_{23}$ is constructed analogously.

5.3 Common event selection

The analyses all involve a Higgs boson decaying into a pair of new bosons $X$, or into a new boson $X$ along with a $Z$ boson, which in turn decay into pairs of leptons. The $X$ bosons are presumed to be on-shell, so the strategy is to search for resonances in the relevant dilepton mass distributions. Each analysis defines a signal region (SR) via a series of selections on measured quantities which maximizes the sensitivity to the signal.

All three analyses share a common preselection, but differ in the subsequent steps of selecting the candidate final-state leptons, forming them into quadruplets, selecting one of those quadruplets, and applying further requirements to the selected quadruplet. Table 2 shows the event selections of the different analyses.

The common preselection requires that events were recorded with the detector in good operating condition [161] and without excess calorimeter noise [162]. Each event must have an identified primary vertex with at least two tracks [163] and at least four lepton
candidates. Events were triggered by requiring either one or two lepton candidates, where the candidates could be either electrons or muons [164–166]. The lepton candidates identified offline must match candidates identified by the trigger. The trigger $p_T$ requirements range from $p_T > 7 \text{ GeV}$ to $p_T > 60 \text{ GeV}$, depending on lepton multiplicity and flavour. In either case, the trigger efficiency is above 95% (relative to signal region events surviving all other event selections).

Electron and muon candidates are reconstructed as described in section 5.1. Electrons must be within the central region of the detector ($|\eta| < 2.47$), have $p_T > 7 \text{ GeV}$, have a longitudinal impact parameter $z_0$ that satisfies $|z_0 \sin \theta| < 0.5 \text{ mm}$ with respect to the primary vertex, and have an additional associated hit in the insertable B-layer. Muons must be within the acceptance of the muon spectrometer, $|\eta| < 2.7$. All muons must have
$p_T > 5$ GeV, while CT muons must pass the stronger requirement $p_T > 15$ GeV. Lastly, all muon candidates that are associated with a vertex, i.e. all except SA muons, must have a longitudinal impact parameter with respect to the reconstructed primary vertex satisfying $|z_0 \sin \theta| < 0.5$ mm and a transverse impact parameter with respect to the position of the beam satisfying $d_0 < 1$ mm.

All possible quadruplets (section 5.2) are formed from the selected leptons. A quadruplet may contain no more than one SA or CT muon, and at least one lepton in the quadruplet must correspond to a lepton found by one of the triggers satisfied by the event. The three highest-$p_T$ leptons must satisfy, respectively, $p_T > 20$ GeV, $p_T > 15$ GeV, and $p_T > 10$ GeV. Except for the LM analysis, for which the angular separation between leptons can be very small, all pairs of same-flavour leptons in the quadruplet must satisfy $\Delta R(\ell, \ell') > 0.1$, while different-flavour pairs must satisfy $\Delta R(\ell, \ell') > 0.2$. At least one quadruplet per event is required. For the HM and LM analyses, if there is more than one quadruplet passing these requirements, the one with the smallest mass difference between the two pairs, $\Delta m_{\ell\ell} = |m_{12} - m_{34}|$, is chosen. The analogous procedure for the ZX analysis is described in section 5.6.

The leptons in the quadruplet must be isolated from other deposits in the calorimeter or ID tracks [100, 101]. This rejects backgrounds in which leptons arise from the decay of heavy-flavour jets, or in which hadronic jets are misidentified as leptons. For each lepton, the sum of the transverse energies of topological clusters [167] within a cone of $\Delta R = 0.2$ around it (excluding energy attributed to the lepton itself) must be less than 20% of its $p_T$ for electrons, and less than 30% of its $p_T$ for muons. The transverse momenta of tracks in a cone around the lepton are also summed, and must be less than 15% of its $p_T$. The $\eta-\phi$ radius of the cone depends on the momentum of the lepton. For electrons, the radius is $\Delta R = \min(0.2, 10$ GeV$/p_T)$, while for muons, it is $\Delta R = \min(0.3, 10$ GeV$/p_T)$. In both cases, tracks and energy clusters attributed to other leptons in the quadruplet are also excluded from the sums. This is particularly important for the LM analysis (section 5.5), where the angular separation between leptons may be very small.

In addition to the impact parameter requirements discussed earlier, each lepton in the quadruplet must have transverse impact parameter significance $d_0/\sigma_{d_0} < 5$ for electrons and $d_0/\sigma_{d_0} < 3$ for muons (with the exception of SA muons, which do not have an ID track), where $\sigma_{d_0}$ is the estimated error in the reconstructed transverse impact parameter $d_0$.

5.4 HM event selection

The high-mass analysis applies a set of kinematic requirements to select events consistent with $H \rightarrow XX \rightarrow 4\ell$ decays. The invariant mass of the four-lepton system must be consistent with the SM Higgs boson: 115 GeV < $m_{4\ell}$ < 130 GeV. Also, the lepton pairs must not be consistent with the decays of $Z$ bosons (Z-veto): 10 GeV < $m_{12,34}$ < 64 GeV. For the $4e$ and $4\mu$ channels, it is possible that the leptons from a single $X$ or $Z$ decay are not paired together, but rather a lepton from one $Z/X$ decay may be paired with a lepton from the other $Z/X$ decay. Therefore, there are also requirements on the alternative lepton pairings, 5 GeV < $m_{14,23}$ < 75 GeV, in order to suppress $ZZ^*$ background events in
which the leptons are mispaired. Events with pairs consistent with $J/\psi$ or $\Upsilon$ decay are also rejected with requirements on the lepton pair masses (see table 2).

The final requirement enforces consistency between $m_{12}$ and $m_{34}$: $m_{34}/m_{12} > 0.85 - 0.1125 f(m_{12})$, where the function $f(m_{12})$ is defined in the appendix. Together with the relation $|m_{12} - m_Z| < |m_{34} - m_Z|$, this defines a wedge-shaped region in the $m_{12}$–$m_{34}$ plane, as shown in figure 3(b).

5.5 LM event selection

The LM analysis is designed to be sensitive to the mass range $1 \text{ GeV} < m_X < 15 \text{ GeV}$. For these low masses, the angular separation between the two leptons in the $X \to \ell\ell$ decay can become very small ($\Delta R(\ell, \ell) < 0.1$ for $m_X = 1 \text{ GeV}$). In this case, the efficiency to select isolated electrons is significantly smaller than that for muons, so this analysis uses only the $4\mu$ final state. Otherwise, the event selection is very similar to that of the HM analysis (section 5.4), except that a few kinematic criteria differ. The $\Delta R$ requirements between final-state leptons are removed, and the $Z$-veto requirement is not relevant. In addition to the HM heavy-flavour veto, the two lepton pair masses $m_{12}$ and $m_{34}$ must not be in the ranges $2$–$4.4 \text{ GeV}$ or $8$–$12 \text{ GeV}$. The $m_{4\ell}$ requirement is narrowed to $120 \text{ GeV} < m_{4\ell} < 130 \text{ GeV}$, because muons have smaller radiative losses than electrons, and both lepton pairs must satisfy $1.2 \text{ GeV} < m_{12,34} < 20 \text{ GeV}$. Also, the final requirement for the signal region is simplified to $m_{34}/m_{12} > 0.85$.

5.6 ZX event selection

The selection for the ZX analysis differs from those of the HM and LM analyses as it is selecting a $Z$ boson along with a new $X$ boson. It is, however, very similar to the selection used for the ATLAS SM $H \to ZZ^* \to 4\ell$ analysis [168]. In addition to the common criteria described in section 5.3, each quadruplet must satisfy $50 \text{ GeV} < m_{12} < 106 \text{ GeV}$, $12 \text{ GeV} < m_{34} < 115 \text{ GeV}$, and, for the $4e$ and $4\mu$ channels, the alternative pairings must satisfy $m_{14,23} > 5 \text{ GeV}$.

Backgrounds from $\Upsilon$ decays were found to be negligible after all selections. If there is more than one such quadruplet, quadruplets are ranked by the following criteria, applied in sequence:

- Rank by the flavours of the two lepton pairs according to the reconstruction efficiencies of the leptons. The reconstruction efficiency for muons is higher than that for electrons, especially at lower lepton momenta. Therefore, the final state lepton pairs in order of decreasing reconstruction efficiency are $4\mu$, $2e2\mu$, $2\mu2e$, and $4e$.

- Choose the quadruplet with the smallest $|m_Z - m_{12}|$.

- Choose the quadruplet with the smallest $|m_Z - m_{34}|$.

This is strictly applied to all quadruplets, even same-flavour ones, and thus differs slightly from the prescription used in the analysis of ref. [168], where the lower-ranked alternative pairing of a same-flavour quadruplet is prevented from being considered in the quadruplet
selection. For this analysis, the alternative pairing is treated as a separate quadruplet and participates in the ranking and quadruplet selection.

Following the selection of the quadruplet, the tracks associated with all four leptons are required to be consistent with originating from a common vertex: $\chi^2/N_{\text{dof}} < 9$ (tightened to $< 6$ for the $4\mu$ channel), where these upper bounds were chosen to give an efficiency of 99.5%. This removes additional reducible backgrounds, mainly $Z + \text{jets}$ and $t\bar{t}$. (These backgrounds are already very small for the HM and LM analyses, so this requirement is not applied in those cases.) Finally, the total invariant mass is required to be consistent with the decay of a Higgs boson, in the same manner as in the HM analysis: $115 \text{GeV} < m_{4\ell} < 130 \text{GeV}$. None of the other requirements of the HM analysis ($Z$ boson/heavy-flavour veto and signal region requirements) are applied here.

6 Systematic uncertainties

Many systematic uncertainties are common to all the analyses considered here. The dominant ones include:

- **Luminosity and pile-up.** The uncertainty in the integrated luminosity is 1.7% [169], obtained using the LUCID-2 detector [170] for the primary luminosity measurements. Uncertainty due to pile-up arises from differences between the predicted and measured inelastic cross sections, as well as from the reweighting procedure described in section 4. This uncertainty is approximately 1%.

- **Lepton-related uncertainties.** The efficiency for events to pass the selection depends on the reconstruction and identification efficiencies for leptons, as well as the determination of their momentum scale. Tag-and-probe techniques are applied to the dilepton resonances $Z \rightarrow \ell^+\ell^-, J/\psi \rightarrow \ell^+\ell^-$, and $\Upsilon \rightarrow \mu^+\mu^-$ in order to measure the efficiencies and momentum scales and resolutions for electrons and muons. This leads to corrections, usually of the order of up to a percent, to account for differences observed between data and simulation, as well as an estimate of the residual uncertainty [99, 101]. As there are four leptons in the final state, small single-lepton uncertainties can result in larger uncertainties in the final yields, which range up to 15%, dominated by the uncertainty in the electron reconstruction and identification efficiency.

- **Theoretical uncertainties.** Uncertainties in the modelling of the simulated signal and background processes are estimated by varying the parton distribution functions, the factorization, renormalization, and QCD scales, and the modelling of hadronization and the underlying event. The total uncertainty in the acceptance of the signal is around 3%, and the uncertainty in the background yield is 3%–9% for the $H \rightarrow ZZ* \rightarrow 4\ell$ process [171] and about 5% for $ZZ^* \rightarrow 4\ell$ [148–150, 152, 156, 158].

Uncertainties related to data-driven background estimates are discussed in the analysis-specific sections below.
Each source of systematic uncertainty is considered to be uncorrelated with others: in the statistical description of the data, each source of systematic uncertainty is parameterized by several nuisance parameters that are constrained by Gaussian probability density distributions. The luminosity and lepton-related uncertainties are completely correlated among all Monte Carlo samples.

7 HM analysis: $H \rightarrow XX \rightarrow 4\ell \ (15 \text{ GeV} < m_X < 60 \text{ GeV})$

The high-mass analysis searches for decays of a SM Higgs boson into a pair of new bosons $X$, where $X$ could be $Z_d$, $a$, or $s$, which in turn decay into pairs of electrons or muons (see figure 1). The event selection (detailed in section 5.4) seeks two same-flavour opposite-sign pairs of leptons of similar invariant mass that are consistent with the decay of a SM Higgs boson and inconsistent with the subsequent decay of $Z$ bosons.

7.1 Background estimate

Backgrounds with four prompt leptons are estimated from simulation (see section 4) and validated using data from background-dominated control samples. The dominant backgrounds are $H \rightarrow ZZ^* \rightarrow 4\ell$ (about 72% of the total background) and $ZZ^* \rightarrow 4\ell$ (about 24% of the total background). Other such processes include $t\bar{t}Z \rightarrow 4\ell$ and processes with three gauge bosons. These are found to be negligible.

Reducible backgrounds include those from processes with leptons originating from the decay of heavy-flavour jets, or with jets misidentified as leptons. The background from the $Z +$ jets process is estimated using data. Control regions enriched in misidentified leptons are defined by selecting quadruplets with one or two of its subleading leptons satisfying ‘inverted’ criteria but otherwise passing the signal region selection. ‘Inverted’ electrons fail either the Loose electron selection or the isolation requirement, but not both. ‘Inverted’ muons fail either the isolation requirement or the transverse impact parameter significance requirement ($d_0/\sigma_{d_0} < 3$), or both. Two samples are defined, both requiring two leptons consistent with the decay of a $Z$ boson. The ‘good’ sample requires at least one extra lepton passing the nominal selection, while the ‘inverted’ sample requires at least one extra lepton passing the ‘inverted’ selection. Since both samples are highly enriched in $Z \rightarrow \ell\ell$ decays, the extra leptons originate mostly from jets misidentified as leptons. Transfer factors are defined as the ratio of the number of extra leptons passing the ‘good’ selection to the number passing the ‘inverted’ selection. These transfer factors are applied to events in the ‘inverted’ control regions in order to extrapolate to the signal region. The systematic uncertainties in this procedure are estimated by propagating the statistical uncertainties in the transfer factors as well as comparing the results from several different definitions of ‘good’ and ‘inverted’ leptons. This yields an estimate of the background due to the $Z +$ jets process in the signal region compatible with zero.

Other reducible backgrounds are estimated from simulation. The dominant contribution is from $t\bar{t}$, with about 3% of the total background. Other such backgrounds, including those from diboson production and heavy-flavour processes, are found to be negligible.
7.2 Background validation

The background estimates are validated using four dedicated background-enriched validation regions, defined so that they do not overlap with the HM signal region:

- **VR1**: the $Z$-veto requirement on the alternative pairings is inverted, requiring $m_{14,23} \geq 75$ GeV, and the compatibility requirement on $m_{34}/m_{12}$ is removed. This produces a sample enriched in the $H \to ZZ^* \to 4\ell$ process as well as the non-resonant $ZZ^* \to 4\ell$ process. Only the $4e$ and $4\mu$ final states contribute to this region.

- **VR2**: the requirements on the four invariant mass pairings are removed and replaced with $m_{12} \geq 64$ GeV, and the compatibility requirement on $m_{34}/m_{12}$ is removed. This sample is also enriched in both the $H \to ZZ^* \to 4\ell$ and $ZZ^* \to 4\ell$ processes. All final states contribute to this region.

- **VR3**: both the Higgs boson mass window requirement ($115$ GeV < $m_{4\ell}$ < $130$ GeV) and the final $m_{34}/m_{12}$ compatibility requirement are inverted, producing a sample dominated by $ZZ^* \to 4\ell$.

- **VR4**: the final $m_{34}/m_{12}$ compatibility requirement is inverted, and all four dilepton mass requirements are changed to $m_{\ell\ell} < 55$ GeV. This sample mainly consists of $H \to ZZ^* \to 4\ell$, but has a significant contribution from $ZZ^* \to 4\ell$.

Although these validation regions are constructed so that they do not overlap with the signal region for the HM analysis, there is some overlap of VR1 and VR2 with the signal region of the ZX analysis. However, given the cross-section limits found for the $H \to ZZ_{d} \to 4\ell$ process (figure 17(a)), the contribution of ZX signal events to either of these regions is less than 5% of the SM background expectation.

Figure 2 compares the predicted backgrounds in these regions with the data for the variable $\langle m_{\ell\ell} \rangle = \frac{1}{2}(m_{12} + m_{34})$. Good agreement is found in all cases. In these validation regions, the $Z +$ jets background is estimated from MC simulations, while for the signal region it is estimated from data.

7.3 Results

The resulting $\langle m_{\ell\ell} \rangle$ distribution for this analysis is shown in figure 3(a), while table 3 summarizes the final yields and uncertainties in the signal region as defined in table 2. A total of 20 events are observed, with a total predicted background of $15.6 \pm 1.3$ events. The $p$-values for the background-only hypothesis as a function of $m_X$ are shown in figure 4. The profile-likelihood ratio $(-2 \log[L(\mu = 0, \hat{\theta})/L(\hat{\mu}, \hat{\theta})])$ is used as the test statistic, and the likelihood used is described in section 10. Different final states are not distinguished in the fit; distributions used are summed over all channels. The largest deviation from SM expectations occurs around $m_{Z_d} = 28$ GeV, corresponding to the two events with $\langle m_{\ell\ell} \rangle \approx 28$ GeV, with a local significance of $2.5\sigma$. Following procedures fixed before the data in the signal region were examined, the one event with $\langle m_{\ell\ell} \rangle < 15$ GeV and the two with $\langle m_{\ell\ell} \rangle > 60$ GeV are not considered when setting limits and do not affect figure 4. The distribution of $m_{34}$ versus $m_{12}$ for the selected events is shown in figure 3(b).
Figure 2. Distributions of $\langle m_{\ell\ell} \rangle = \frac{1}{2}(m_{12}+m_{34})$ in the validation regions for the HM $H \to XX \to 4\ell$ ($15 \text{ GeV} < m_X < 60 \text{ GeV}$) analysis: for (a) VR1, (b) VR2, (c) VR3, and (d) VR4 (see text for definitions). The signal contribution to these regions is negligible. The shaded band represents the total uncertainty of the prediction. The lower panels show the ratio of the observed data to the (pre-fit) MC predictions; the arrows at the upper edge indicate data points that fall outside of the $y$-axis range. The uncertainties of the plotted data are asymmetric and are calculated using eqs. (40.76) of ref. [160].
Figure 3. Distribution of (a) $\langle m_{\ell\ell} \rangle$ and (b) $m_{34}$ vs $m_{12}$, for events selected in the HM $H \to XX \to 4\ell$ ($15 \text{ GeV} < m_X < 60 \text{ GeV}$) analysis. In the $\langle m_{\ell\ell} \rangle$ distribution (a), the (pre-fit) background expectations are also shown; the hatched band contains the statistical and systematic uncertainties. The expectations for the signal are also shown, for several masses. The signal histograms are stacked on top of the background histograms, and expected yields are normalized with $\sigma(pp \to H \to ZZ^* \to 4\ell) = 10 \sigma_{\text{SM}}(pp \to H \to ZZ^* \to 4\ell) = 0.60 \text{ fb}$ (ggF process only). The uncertainties of the plotted data are asymmetric and are calculated using eqs. (40.76) of ref. [160]. For the $m_{34}$ vs $m_{12}$ distribution (b), each marker corresponds to an event that passed the Higgs boson window requirement and $Z$ boson veto. The markers (differentiated by channel) that fall inside the green shaded area correspond to the events of the signal region.

Table 3. Expected event yields of the SM background processes and data yield for the HM $H \to XX \to 4\ell$ ($15 \text{ GeV} < m_X < 60 \text{ GeV}$) selection. Three of the 20 observed events are outside the range $15 \text{ GeV} < \langle m_{\ell\ell} \rangle < 60 \text{ GeV}$ and are thus not considered when setting limits. The systematic uncertainties of the background estimates are highly correlated between the different sources of background (see section 6).
Figure 4. Observed local $p$-values under the background-only hypothesis for the process $H \rightarrow XX \rightarrow 4\ell$ in the high-mass range. For the limit determination, the distributions of $\langle m_{\ell\ell} \rangle$ in the signal region are binned with a width of 1 GeV. The $p$-values are plotted in steps of 0.25 GeV in the vicinity of observed data and 1 GeV elsewhere. The most significant excess corresponds to a local significance of 2.5$\sigma$ at $m_{Z_d} = 28$ GeV.

8 LM analysis: $H \rightarrow XX \rightarrow 4\mu$ (1 GeV < $m_X$ < 15 GeV)

The LM analysis extends the HM analysis to the region 1 GeV < $m_X$ < 15 GeV, where $X = Z_d$, $a$, or $s$. Only the $4\mu$ final state is considered for this analysis. The event selection is detailed in section 5.5 and is similar to that of the HM analysis, with some adjustments for the different kinematic region.

8.1 Background estimate

Backgrounds involving four prompt leptons are estimated directly from MC simulations (see section 4). The $H \rightarrow ZZ^* \rightarrow 4\mu$ and $ZZ^* \rightarrow 4\mu$ processes together comprise about two thirds of the total background estimate. Higher-order electroweak processes, including triboson production and vector-boson scattering, are found to be negligible.

The remaining backgrounds involve non-prompt leptons, primarily from decays of heavy-flavour hadrons in events with multiple $b$-quarks such as $bb$. A leading part of this contribution comes from double semileptonic decays, where a $b$-hadron decays into a muon and a $c$-hadron, which further decays into another muon and light hadrons. Resonances produced in the $b$-hadron decay chain (i.e., $\omega$, $\rho$, $\phi$, $J/\psi$) are also an important background but are almost completely suppressed by the heavy-flavour vetoes on dilepton masses required as part of the LM event selection. There is also a small contribution from $b\bar{b}b\bar{b}$, where each muon originates from an independent $b$-quark. As the muons selected here are all isolated, $b$-jet tagging is not useful for reducing these backgrounds. The backgrounds from these processes are estimated together using a data-driven method [43, 49].
The first step is to find the shape of the background in the $m_{12}$–$m_{34}$ plane. The invariant mass distribution of each muon pair is modelled separately to account for the different kinematic selections imposed on the leading, subleading, and remaining muons. Two distinct control samples are used, each of which contains an opposite-sign muon pair plus a third muon. The first sample, used to model $m_{12}$, requires a muon pair with $p_T^1 > 20$ GeV and $p_T^2 > 10$ GeV satisfying a dimuon trigger, and a third muon with $p_T^3 > 5$ GeV. The second sample, used to model $m_{34}$, requires a muon pair with $p_T^{1,2} > 5$ GeV and a third muon with $p_T^3 > 27$ GeV, satisfying a single-muon trigger. In both cases, the muons must pass the same isolation and quality requirements as for the signal region. Ninety-seven percent of signal events pass both these selections, with the $m_{12}$ and $m_{34}$ pairs passing the requirements of the muon pair in the first and second samples, respectively. The invariant masses of the muon pairs are taken from the two control samples and used to form a 2D template in the $m_{12}$–$m_{34}$ plane as the direct product of the two distributions.

A correction to the $m_{12}$–$m_{34}$ template is made to account for a correlation between the kinematics of the two muon pairs, which is introduced by the Higgs boson mass requirement. Another control sample is defined by inverting the isolation and vertex requirements on the muons in the signal event selection, defining a sample enriched in events with muons from heavy-flavour quark decays. Comparing the distributions of muon pair invariant masses before and after the Higgs boson mass requirement yields the correction to the background shape as a function of $m_{12}$ and $m_{34}$.

Finally, the overall normalization for the background from non-prompt leptons is determined from data in regions defined by inverting several selection criteria. As shown in figure 5, region B is defined by inverting the compatibility requirement $m_{34}/m_{12} > 0.85$. In order to improve the statistical precision of the background prediction, additional regions are defined by inverting the Higgs boson mass requirement (region C in figure 5) and also the isolation and vertex requirements (regions D and E in figure 5). The regions with $81 \text{ GeV} < m_{4\ell} < 101 \text{ GeV}$ are excluded in order to reduce contributions from $Z$ bosons. The contribution with prompt muons, mostly $ZZ^*$ in regions B and C, is subtracted from the data. The background with non-prompt leptons in region B is then estimated using $B = C \cdot D/E$. The 2D template is then used to scale from the estimate in region B to the signal region satisfying the compatibility requirement, region A.

The uncertainty in the heavy-flavour background estimate is found by varying each parameter of the background shape model up and down by $2\sigma$ and taking the largest change in yield for each bin, giving an uncertainty of 38%. Statistical uncertainties in the normalization of the signal region are also propagated to the heavy-flavour background yield, giving an uncertainty of 33%. Adding these uncertainties in quadrature gives a total systematic uncertainty of 50% in the heavy-flavour background yield.

### 8.2 Results

The $\langle m_{4\ell} \rangle$ distribution in the LM signal region is shown in figure 6(a). The distribution of $m_{12}$ vs $m_{34}$ is shown in figure 6(b), while table 4 summarizes the final yields and uncertainties. No events are observed, with a total background prediction of $0.89 \pm 0.15$ events.
Figure 5. Definition of regions used in the normalization of the heavy-flavour background in the LM analysis. (a) Region A is the signal region. The $m_{34}/m_{12} > 0.85$ compatibility requirement is inverted in region B, and the Higgs boson mass requirement is inverted in region C. The isolation and impact parameter requirements are inverted in regions D and E shown in (b).

Figure 6. Distribution of (a) $\langle m_{\ell\ell} \rangle$ and (b) $m_{34}$ vs $m_{12}$, for events selected in the LM $H \to XX \to 4\mu$ ($1\text{GeV} < m_X < 15\text{GeV}$) analysis. No data events pass this selection. The expectation for a $H \to aa \to 4\mu$ signal is also shown, for several masses. The signal histograms are stacked on top of the (pre-fit) background histograms, and expected yields are normalized with $\sigma(pp \to H \to aa \to 4\mu) = \frac{1}{17}\sigma_{\text{SM}}(pp \to H \to ZZ^* \to 4\mu) = 0.15\text{fb}$ (ggF process only). The shaded band represents the total uncertainty of the prediction. The crossed-through points in (b) correspond to the 50 events that are outside the $m_{4\ell}$ mass window of $120\text{GeV} < m_{4\ell} < 130\text{GeV}$. The events outside the green signal region are events that fail the $m_{34}/m_{12} > 0.85$ requirement and include one event within the $m_{4\ell}$ mass window.
9 ZX analysis: $H \to ZX \to 4\ell$ ($15 \text{ GeV} < m_X < 55 \text{ GeV}$)

The ZX analysis searches for decays of a SM Higgs boson into a $Z$ boson along with a new boson $X$, where both bosons in turn decay into pairs of electrons or muons. The event selection is detailed in section 5.6. Like the previous analyses, it involves finding two same-flavour opposite-sign lepton pairs with an overall invariant mass consistent with the decay of a SM Higgs boson. Unlike the other analyses, the leading pair must be broadly consistent with the decay of a $Z$ boson, and the analysis then searches for a peak in the invariant mass distribution of the other pair. For $m_{Zd} > 55 \text{ GeV}$, the invariant mass distribution for $Z_d \to \ell\ell$ starts to overlap significantly with that for $Z \to \ell\ell$. Since this analysis accepts events with the leading lepton pair consistent with the decay of a $Z$ boson, it relies much more on the invariant mass distribution of the other lepton pair to reject the $ZZ \to 4\ell$ background than does the HM analysis. Therefore, the upper search range for this analysis is limited to 55 GeV, rather than 60 GeV as for the HM analysis.

9.1 Background estimate

The dominant backgrounds in this analysis are $H \to ZZ^* \to 4\mu$ (about 65% of the total) and non-resonant $ZZ^* \to 4\ell$ (about 33% of the total). Additional prompt backgrounds include the triboson processes $ZZZ$, $WZZ$, and $WWZ$. These are estimated from simulation (see section 4), but the $ZZ^* \to 4\ell$ background estimate is checked using background-enriched validation samples.

Other, reducible, backgrounds, such as those from $Z$+jets, $t\bar{t}$, and $WZ$ processes, contain either additional non-isolated leptons from heavy-flavour decay or objects misidentified as leptons and constitute only a few percent of the background. The procedure used to estimate the total yield of these backgrounds is identical to that of the ATLAS SM $H \to ZZ^* \to 4\ell$ analysis [168, 172].

The reducible background is estimated separately for the cases where the second lepton pair ($m_{34}$) decays into muons ($\ell\ell\mu\mu$) and those where it decays into electrons ($\ell\ell\ell\ell$). For the $\ell\ell\mu\mu$ case, a number of mutually exclusive control regions are defined by inverting or relaxing
some of the lepton identification requirements, including the isolation and impact parameter requirements for the subleading muon pair. A fit to the $m_{12}$ distribution is then performed to estimate the amount of background due to each of $t\bar{t}$, $Z +$ heavy-flavour (having $b$- or $c$-quark content), and $Z +$ light-flavour. Transfer factors derived from simulation are then used to extrapolate the fitted yield of each background in the control regions to the signal region. The contribution from $WZ$ production is estimated using simulation.

The $\ell\ell ee$ background from $Z +$ jets, $t\bar{t}$, and $WZ$ production is classified into processes with jets being misidentified as electrons ($f$), electrons from photon conversions ($\gamma$), and electrons from semileptonic decay of heavy-flavour hadrons ($q$). The $q$ component is estimated from simulation. The other two components are estimated from a control region in which the identification requirements of the lowest-$p_T$ electron are relaxed. Further, to suppress the $ZZ^*$ contribution, the two subleading electrons must have the same sign. The expectations for the $f$ and $\gamma$ components are obtained by fitting to the distribution of the number of inner pixel detector hits associated with the track of the lowest-$p_T$ electron. The estimated yields of all three components are then extrapolated to the signal region using transfer factors derived from simulation.

Finally, the shape of the $m_{34}$ distribution for the reducible background is taken from simulation. An additional 10% systematic uncertainty is assigned to the reducible background estimate to account for differences in the lepton isolation requirements between this analysis and that of refs. [168, 172].

9.2 Background validation

The estimate of the non-resonant $ZZ^* \to 4\ell$ background is further validated in control samples that are enriched in this process. Two validation regions are defined by replacing the requirement $115 \text{ GeV} < m_{4\ell} < 130 \text{ GeV}$ with either $m_{4\ell} < 115 \text{ GeV}$ (VR5) or $130 \text{ GeV} < m_{4\ell} < 170 \text{ GeV}$ (VR6). The latter validation region also requires $|m_{12} - m_Z| < 6 \text{ GeV}$. For consistency with the ATLAS SM $H \to ZZ^* \to 4\ell$ analysis [168, 172], the requirement on $m_{34}$ is also changed for both validation regions:

- $m_{34} > 5 \text{ GeV}$ for $m_{4\ell} < 100 \text{ GeV}$;
- $m_{34} > 1.4(m_{4\ell} - 100 \text{ GeV}) + 5 \text{ GeV}$ for $100 \text{ GeV} < m_{4\ell} < 105 \text{ GeV}$;
- $m_{34} > 12 \text{ GeV}$ for $105 \text{ GeV} < m_{4\ell} < 140 \text{ GeV}$;
- $m_{34} > 0.76(m_{4\ell} - 140 \text{ GeV}) + 12 \text{ GeV}$ for $140 \text{ GeV} < m_{4\ell} < 170 \text{ GeV}$.

These requirements are illustrated in figure 7. Distributions of $m_{34}$ for the two validation regions are shown in figure 8. Good agreement is found with background expectations.

9.3 Results

The final $m_{34}$ distribution for this analysis is shown in figure 9, while table 5 summarizes the final yields and uncertainties. The dominant systematic uncertainty in final states that contain electrons arises from the modelling of the electron identification efficiency. For the $4\mu$ channel, the dominant systematic uncertainty arises from the modelling of muon isolation.
Figure 7. Illustration of the validation region definitions for the $H \rightarrow ZX \rightarrow 4\ell$ analysis. Shown are the selections in the (a) $m_{12}$ vs $m_{4\ell}$ and (b) $m_{34}$ vs $m_{4\ell}$ planes for the two validation regions as well as the signal region. Details of the selections are given in the text.

Figure 8. Distributions of $m_{34}$ in the two validation regions for the $H \rightarrow ZX \rightarrow 4\ell$ analysis. (a) VR5: $m_{4\ell} < 115$ GeV; (b) VR6: $130$ GeV $< m_{4\ell} < 170$ GeV. The shaded band represents the total uncertainty of the (pre-fit) prediction. The lower panels show the ratio of the observed data to the MC predictions. The uncertainties of the plotted data are asymmetric and are calculated using eqs. (40.76) of ref. [160].
A total of 356 events are observed with an expected background of $320 \pm 17$. Figure 10 shows the observed local $p$-values for the background-only hypothesis. The profile-likelihood ratio is again used as the test statistic. Different final states are not distinguished in the fit; distributions used are summed over all channels. The normalization of the $H \to ZZ^*$ background is allowed to float (as an unconstrained nuisance parameter, see section 10.1.2), with a resulting normalization of $1.2 \pm 0.16$. The largest excess, with a local significance of around $2\sigma$, is at about $m_X = 39$ GeV.

These results are slightly different from the corresponding results from the ATLAS SM $H \to ZZ^* \to 4\ell$ analysis [173], which observed 310 events and found a signal strength of $\sigma_{\text{ fid}}/\sigma_{\text{ SM}} = 0.96 \pm 0.11$. The difference is largely due to the differences in quadruplet handling mentioned in section 5.6, and also due to differences in the definitions of the isolation and impact parameter selections. When this analysis is repeated using the quadruplet definition of ref. [173], the resulting normalization of the $H \to ZZ^*$ background is $1.12 \pm 0.15$. 
Process Yield ($\pm$stat. $\pm$syst.)

<table>
<thead>
<tr>
<th>Process</th>
<th>$2\ell2\mu$</th>
<th>$2\ell2e$</th>
<th>Total</th>
</tr>
</thead>
<tbody>
<tr>
<td>$H \rightarrow ZZ^* \rightarrow 4\ell$</td>
<td>127.9 $\pm$ 0.1 $\pm$ 3.6</td>
<td>76 $\pm$ 0.1 $\pm$ 10</td>
<td>204 $\pm$ 0.2 $\pm$ 12</td>
</tr>
<tr>
<td>$ZZ^* \rightarrow 4\ell$</td>
<td>70.2 $\pm$ 0.2 $\pm$ 1.9</td>
<td>33.0 $\pm$ 0.2 $\pm$ 3.6</td>
<td>103.3 $\pm$ 0.3 $\pm$ 4.6</td>
</tr>
<tr>
<td>Reducible</td>
<td>4.9 $\pm$ 0.1 $\pm$ 0.3</td>
<td>5.8 $\pm$ 0.3 $\pm$ 0.6</td>
<td>10.7 $\pm$ 0.3 $\pm$ 1.0</td>
</tr>
<tr>
<td>$VVV, tl + Z$</td>
<td>1.1 $\pm$ 0.1 $\pm$ 0.04</td>
<td>0.7 $\pm$ 0.1 $\pm$ 0.1</td>
<td>1.8 $\pm$ 0.1 $\pm$ 0.1</td>
</tr>
<tr>
<td>Total</td>
<td>204.1 $\pm$ 0.3 $\pm$ 5.5</td>
<td>116 $\pm$ 0.5 $\pm$ 14</td>
<td>320 $\pm$ 0.5 $\pm$ 17</td>
</tr>
<tr>
<td>Data</td>
<td>237</td>
<td>119</td>
<td>356</td>
</tr>
</tbody>
</table>

Table 5. Expected and observed numbers of events in each channel after the $H \rightarrow ZX \rightarrow 4\ell$ event selection defined by the mass range $115\text{ GeV} < m_{4\ell} < 130\text{ GeV}$. The background normalization is prior to the fit (see text). The systematic uncertainties of the background estimates are highly correlated between the different sources of background (see section 6).

Figure 10. Observed local $p$-values under the background-only hypothesis for the process $H \rightarrow ZX \rightarrow 4\ell$.

10 Limits and interpretation

No significant excess is observed above SM background predictions for any of the analyses considered. Therefore, the results are interpreted in terms of exclusion limits. Firstly, model-independent limits are placed on fiducial cross sections. Model-dependent exclusion limits are then set for the benchmark models described in section 2.

For the HM and LM $H \rightarrow XX \rightarrow 4\ell$ analyses, evaluating the limits entails parameterizing the signal distribution as a function of both $\langle m_{4\ell} \rangle$ and $m_X$, while the $H \rightarrow ZX \rightarrow 4\ell$ analysis requires the parameterization to be a function of $m_{34}$ and $m_X$. Since simulated events are generated only at discrete values of $m_X$, the signal templates are interpolated between $m_X$ values. For the HM and ZX analyses, this is done using moment morphing [174]. The distributions at the generated values of $m_X$ are used as templates, and the normalization is determined from interpolation of the simulated signal yields. For the LM analysis, Gaussian distributions are fit to the $\langle m_{4\ell} \rangle$ distributions at each generated $m_X$, and the fit parameters are interpolated in $m_X$.
**Table 6.** Summary of the fiducial phase-space definitions, appropriate for $H \rightarrow XX \rightarrow 4\ell$ or $H \rightarrow ZX \rightarrow 4\ell$, where $X$ is a promptly decaying, on-shell, narrow resonance.

The data are described statistically by a likelihood function consisting of a Poisson factor for each histogram bin, summed over each channel, along with a Gaussian constraint for each nuisance parameter [175]:

$$
\mathcal{L}(N, \alpha) = \prod_i \text{Pois} \left( \sum_j N_{ij}; \sum_j \mu S_{ij}(\alpha) + B_{ij}(\alpha) \right) \prod_k \text{Gaus}(\alpha_k; s_k, \sigma_k),
$$

where $N_{ij}$ is the number of observed events observed in bin $i$ for channel $j$, $\alpha$ is the set of nuisance parameters, $S_{ij}(\alpha)$ and $B_{ij}(\alpha)$ are the predicted numbers of signal and background events for each bin and channel, $\mu$ is the signal strength, and $s_k$ and $\sigma_k$ are mean and width of the Gaussian constraint for nuisance parameter $\alpha_k$. Systematic uncertainties are modelled via nuisance parameters which are profiled in the calculation of the test statistic; the effect of systematic uncertainties on the limits is small.

### 10.1 Limits on fiducial and total cross sections

Model-independent cross-section limits for the HM, LM, and ZX analyses are derived in fiducial regions defined using generator-level quantities. These fiducial selections, shown in table 6, are designed to mimic the signal region selection requirements. In order to account for the effects of quasi-collinear electromagnetic radiation from the leptons within the detector resolution, the four-momenta of prompt photons close to a lepton ($\Delta R < 0.1$) are added to the four-momentum of that lepton [176].

The fiducial selections are used to factorize the effects of the event selection into a largely model-independent ‘efficiency’ and a model-dependent ‘acceptance’. The efficiency...
for a given channel is defined as the fraction of events passing the fiducial selection (using generator-level quantities) that also pass the full event selection (using reconstructed quantities). This mostly depends on the lepton reconstruction, but not on the model used. Systematic uncertainties relevant to the reconstruction of leptons are propagated to the efficiency. For a given theoretical signal model, the acceptance for a channel $c$ is defined as

$$\alpha_c = \frac{N_{c,\text{fid}}}{N_{c,\text{tot}}},$$

where $N_{c,\text{fid}}$ is the yield for channel $c$ within the fiducial region (at generator level) and $N_{c,\text{tot}}$ is the total yield for channel $c$ (simply the total generator-level yield for the channel). The efficiency may thus be used to find a model-independent fiducial cross-section limit, which may then be converted to a model-dependent total cross-section limit using the acceptance.

### 10.1.1 HM and LM limits

The efficiencies within the fiducial regions for the HM and LM analyses are shown in figure 11(a). These were calculated using the benchmark $H \rightarrow ZZ_d$ model, but the efficiencies are mostly model-independent: for $H \rightarrow aa \rightarrow 4\mu$ over the range $1 \text{ GeV} < m_a < 15 \text{ GeV}$ the efficiencies are the same as for $H \rightarrow ZZ_d \rightarrow 4\mu$ to within a relative difference of 3%. The difference in efficiency between different final states is mainly due to the fact that the efficiencies for reconstruction, identification, and selection are lower for electrons than for muons. These efficiencies are used to compute 95% confidence level (CL) upper limits on the cross section within the fiducial region, using the CL$_s$ frequentist formalism [177] with the profile-likelihood-ratio test statistic [178]. The resulting limits are shown in figure 12. These limits should be applicable to any models of the SM Higgs boson decaying into four leptons via two intermediate bosons that are narrow, on-shell, and that decay promptly. The model-dependent acceptances for the HM and LM analyses are shown in figure 11(b) for the $H \rightarrow ZZ_d$ and $H \rightarrow aa \rightarrow 4\mu$ models. The resulting upper limit on the product of the total cross section and decay branching ratio for the benchmark model, $\sigma(gg \rightarrow H \rightarrow ZZ_d \rightarrow 4\ell)$, for the HM analysis is shown in figure 13, while figure 14 shows upper limits on $\sigma(gg \rightarrow H \rightarrow ZZ_d \rightarrow 4\mu)$ and $\sigma(gg \rightarrow H \rightarrow aa \rightarrow 4\mu)$ for both the HM and LM analyses. These results are independent of assumptions about the decay branching ratios of the $Z_d$ and $a$ bosons. In particular, figure 14(b) also applies to the scalar case $\sigma(gg \rightarrow H \rightarrow ss \rightarrow 4\mu).

### 10.1.2 ZX limits

For limits involving ZX processes, the normalization of the non-resonant $ZZ^* \rightarrow 4\ell$ background is validated using control samples, but the normalization of the remaining significant background, $H \rightarrow ZZ^* \rightarrow 4\ell$, is allowed to float in the limit determination as an unconstrained nuisance parameter. The model-independent efficiency within the fiducial region is shown in figure 15(a), and the resulting 95% CL upper limit on the fiducial region cross section is shown in figure 16. The fiducial region acceptance for the $H \rightarrow ZZ_d \rightarrow 4\ell$ process is shown in figure 15(b), and the upper limits on the product of the total cross section and decay branching ratio for the benchmark models, $\sigma(gg \rightarrow H \rightarrow ZZ_d \rightarrow 4\ell)$ and $\sigma(gg \rightarrow H \rightarrow Za \rightarrow 2\ell2\mu)$, are shown in figure 17.
Figure 11. (a) Model-independent per-channel efficiencies $\epsilon_c$ calculated in the fiducial volumes described in the $1 \, \text{GeV} < m_X < 15 \, \text{GeV}$ and $15 \, \text{GeV} < m_X < 60 \, \text{GeV}$ columns of Table 6 (i.e. separate phase spaces are defined for $m_X$ above and below 15 GeV). (b) Model-dependent per-channel fiducial region acceptances for the $H \rightarrow ZZ \rightarrow 4\ell$ and $H \rightarrow aa \rightarrow 4\mu$ processes. The shaded areas are the quarkonia veto regions.

10.2 Limits on branching ratios

A (model-dependent) cross-section limit may be converted to a branching ratio limit using the relations:

$$B(H \rightarrow XX \rightarrow 4\ell) = \frac{\sigma_{H \rightarrow XX \rightarrow 4\ell}}{\sigma_H},$$

$$B(H \rightarrow XX) = \frac{B(H \rightarrow XX \rightarrow 4\ell)}{\sum_{\ell_1=e,\mu} \sum_{\ell_2=e,\mu} [B(X \rightarrow 2\ell_1) B(X \rightarrow 2\ell_2)]},$$

where $\sigma_{H \rightarrow XX \rightarrow 4\ell}$ is the model-dependent total cross section, $\sigma_H$ is the SM Higgs boson production cross section for the $ggF$ process (48.58 pb for $m_H = 125$ GeV [123]), and $B(X \rightarrow 2\ell)$ is the model-dependent branching ratio for each decay to one lepton flavour. The branching ratios for $Z_d \rightarrow \ell \ell$ and $a \rightarrow \mu \mu$ are taken from the benchmark models [21, 22], where for the $Z_d \rightarrow \ell \ell$ case, the branching ratios for the two lepton flavours are taken to be equal. For the $a \rightarrow \mu \mu$ case, the branching ratio varies considerably in a model-dependent way over the range of $m_a$ considered here. The resulting branching ratio limits are shown in figure 18.

10.3 Limits on Higgs mixing

The branching ratio limit can also be interpreted as a limit on the effective Higgs mixing parameter $\kappa'$, defined as

$$\kappa' = \kappa \frac{m_H^2}{|m_H^2 - m_S^2|},$$

where $\kappa$ is the Higgs portal coupling and $m_S$ is the mass of the dark Higgs boson. Using $\kappa'$ rather than $\kappa$ combines the dependencies on $\kappa$ and $m_S$ into a single parameter. Then,
Figure 12. Per-channel upper limits at 95% CL on fiducial cross sections for the $H \rightarrow XX \rightarrow 4\ell$ process, for the (a) $4\mu$, (b) $4e$, and (c) $2e2\mu$ final states. The step change in the $4\mu$ channel at $m_X = 15$ GeV is due to the change in efficiency caused by the change in fiducial phase-space definition. The shaded areas are the quarkonia veto regions.

According to eq. (2.33) of ref. [21] and assuming $m_S > m_H/2$:

$$\kappa'^2 = \frac{\Gamma_{SM}}{f(m_{Z_a})} \frac{B(H \rightarrow Z_aZ_a)}{1 - B(H \rightarrow Z_aZ_a)}$$

where $\Gamma_{SM}$ is the SM width of the 125 GeV Higgs boson,

$$f(m_{Z_a}) = \frac{v^2}{32\pi m_H} \sqrt{1 - \frac{4m_{Z_a}^2}{m_H^2} \left( m_H^2 + 2m_{Z_a}^2 \right)^2 - 8 \left( m_H^2 - m_{Z_a}^2 \right) m_{Z_a}^2},$$

and $v \approx 246$ GeV is the vacuum expectation value of the Higgs field. The resulting limit is shown in figure 19.

The $H \rightarrow ZZ_a$ analysis can also be used to set limits on the $Z_a$ mixing parameter $\epsilon$ and on the $Z-Z_a$ mass mixing parameter $\delta$, as described in refs. [21, 42]. These are shown in figure 20, assuming the SM Higgs boson production cross section.
Figure 13. Observed and expected upper limits at 95% CL for the cross section of the $H \rightarrow Z_d Z_d \rightarrow 4\ell$ process, assuming SM Higgs boson production via the gluon-gluon fusion process. All final states are combined. HAHM parameters were set to $\kappa = \epsilon = 10^{-4}$.

Figure 14. Observed and expected upper limits at 95% CL for the cross sections of the (a) $H \rightarrow Z_d Z_d \rightarrow 4\mu$ and (b) $H \rightarrow aa \rightarrow 4\mu$ processes, assuming SM Higgs boson production via the gluon-gluon fusion process. The shaded areas are the quarkonia veto regions. HAHM parameters were set to $\kappa = \epsilon = 10^{-4}$. The step changes at $m_{Z_d} = 15\text{ GeV}$ are due to the change in selection from the LM to the HM analysis.
Figure 15. (a) Model-independent efficiencies $\epsilon_c$ for the $H \to ZX$ process for different combinations of the final states calculated in the fiducial volumes described in table 6. (b) Model-dependent per-channel fiducial region acceptances for the $H \to ZZ_d \to 4\ell$ process for different combinations of the final states.

Figure 16. Per-channel upper limit at 95% CL on the fiducial cross section for the $H \to ZX \to 4\ell$ process.
Figure 17. Observed and expected upper limits at 95% CL for the cross sections of the 
(a) $H \rightarrow ZZ_d \rightarrow 4\ell$ and (b) $H \rightarrow Za \rightarrow 2\ell 2\mu$ processes, assuming SM Higgs boson production 
via the gluon-gluon fusion process. All final states are combined. HAHM parameters were set to 
$\epsilon = 10^{-4}$ and $\kappa = 10^{-10}$.

Figure 18. 95% CL upper limits on the cross section times the model-dependent branching ratio 
divided by the SM Higgs boson production cross section for (a) the $H \rightarrow ZZ_d$ process for the 
benchmark HAHM with $\kappa = \epsilon = 10^{-4}$ and (b) the $H \rightarrow aa$ process for the benchmark 2HDM+S 
model. The shaded areas are the quarkonia veto regions. The step changes at $m_{Z_d} = 15$ GeV are 
due to the change in selection from the LM to the HM analysis.
Figure 19. Upper limit at 95% CL on the effective Higgs mixing parameter \( \kappa' = \kappa m_H^2/(m_H^2 - m_Z^2) \), with \( \epsilon \) set to \( 10^{-4} \). The step change at \( m_{Z_d} = 15 \text{ GeV} \) is due to the change in selection from the LM to the HM analysis. The shaded areas are the quarkonia veto regions.

Figure 20. Upper limit at 95% CL on (a) the \( Z_d \) mixing parameter \( \epsilon \), with \( \kappa \) set to \( 10^{-10} \), and (b) the \( Z-Z_d \) mass mixing parameter \( \delta^2 \times B(Z_d \rightarrow \ell\ell) \), assuming the SM Higgs boson production cross section.
11 Conclusion

Searches have been conducted for exotic decays of the Standard Model Higgs boson into two new spin-1 particles $H \to Z_d Z_d$, two new spin-0 particles $H \to aa$, or a $Z$ boson along with a single $Z_d$ or $a$. The searches used 139 fb$^{-1}$ of proton-proton collision data at $\sqrt{s} = 13$ TeV recorded by the ATLAS experiment at the LHC during the period 2015–2018. The first search is for the process $H \to XX \to 4\ell$, where $X$ is either $Z_d$ or $a$, with $15 \text{ GeV} < m_X < 60 \text{ GeV}$. The second search is for the process $H \to XX \to 4\mu$, with $1 \text{ GeV} < m_X < 15 \text{ GeV}$. The third search is for the process $H \to ZX \to 4\ell$, with $15 \text{ GeV} < m_X < 55 \text{ GeV}$. The data are found to be consistent with the predicted backgrounds in the three aforementioned searches, and limits on fiducial and total cross sections are set.

Specializing to the benchmark models, upper limits are set on the branching ratio of the Higgs boson to $Z_d Z_d$ and $aa$ as a function of intermediate boson mass, assuming gluon-gluon fusion Standard Model Higgs production and prompt decay of the $Z_d$/$a$ bosons. Furthermore, assuming the Hidden Abelian Higgs Model introduced at the Higgs portal level with very weak kinetic mixing, limits are set on the mixing parameters $\kappa'$, $\epsilon$, and $\delta$.

The limits presented in this paper improve on those from the previous ATLAS search by factors between two and four due to a larger data sample, improved lepton reconstruction and identification, and a better optimized event selection. In addition to the improvements on the results from the previous search, this paper also presents limits on total cross sections and on the dark Higgs boson mixing parameters.

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A HM signal region optimization

The signal region for the HM analysis in ref. [43] was defined by \( \frac{m_{34}}{m_{12}} > 0.85 \). This was the result of an optimization that assumes the \( Z_d \) width is narrow, as expected in the HAHM, so that the observed width will be dominated by the detector performance. A \( \pm 2\sigma \) change in the energy measurement gives about a 15% change in the lepton-pair invariant mass, motivating the coefficient of 0.85 in the selection. However, the background is low, especially in the lower mass region, so it is possible to widen the signal region somewhat relative to the background without significant loss of sensitivity. This is further motivated by models such as the one discussed in chapter 7 of ref. [180]. Accordingly, the signal region selection was re-optimized to allow for a larger \( Z_d \) width.

The selection widens up to \( 3.5\sigma \) at the low end of the dilepton mass spectrum, where the background is the lowest, but narrows to the previous value of \( 2\sigma \) for higher masses. So the form of the selection is

\[
\frac{m_{34}}{m_{12}} > 0.85 - 0.1125 f(m_{12}),
\]

where \( f(m_{12}) \) is a modulating function that is 1 at the lowest mass and goes to 0 at higher masses.

The form of the modulating function is taken from the shape of the average dilepton mass spectrum in the background. The function fit to this shape consists of an exponential tail matched with half of a Gaussian:

\[
F(x) = \begin{cases} 
B_1 + B_2(x - X) + h e^{-\frac{(x-X)^2}{2\sigma^2}}, & x > X - T \\
B_1 + B_2(x - X) + h e^{\frac{-(2x-2X-T)^2}{2\sigma^2}}, & x < X - T 
\end{cases}
\]

The fit parameters, with \( x \) given in GeV, are \( h = 3.73, \ X = 51.6, \ \sigma = 16.6, \ B_1 = -2.62, \ B_2 = -0.0266, \ \text{and} \ T = 6.39, \) with the maximum of \( F(x) \) occurring at \( x_{\text{max}} = 49.64 \) GeV. The modulating function is then defined by

\[
f(m_{12}) = \begin{cases} 
1 - \frac{F(m_{12}) - F(10)}{F(x_{\text{max}}) - F(10)}, & m_{12} < x_{\text{max}} \\
0, & m_{12} > x_{\text{max}} 
\end{cases}
\]

The final shape of the re-optimized signal region is shown in figure 3(b).
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