Measurement of the production cross section for W-bosons in association with jets in p collisions at $\sqrt{s} = 7$ TeV with the ATLAS detector


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**A B S T R A C T**

This Letter reports on a first measurement of the inclusive $W + n$ jets cross section in proton–proton collisions at a centre-of-mass energy of 7 TeV at the LHC, with the ATLAS detector. Cross sections, in both the electron and muon decay modes of the $W$-boson, are presented as a function of jet multiplicity and of the transverse momentum of the leading and next-to-leading jets in the event. Measurements are also presented of the ratio of cross sections $\sigma(W + n)/\sigma(W + n - 1)$ for inclusive jet multiplicities $n = 1-4$. The results, based on an integrated luminosity of 1.3 pb$^{-1}$, have been corrected for all known detector effects and are quoted in a limited and well-defined range of jet and lepton kinematics. The measured cross sections are compared to particle-level predictions based on perturbative QCD. Next-to-leading order calculations, studied here for $n \leq 2$, are found in good agreement with the data. Leading-order multiparton event generators, normalized to the NNLO total cross section, describe the data well for all measured jet multiplicities.

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1. Introduction

The study of massive vector boson ($V$, where $V = W$ or $Z$) production in association with one or more jets ($V + n$ jets) is an important test of quantum chromodynamics (QCD). In addition, $V + n$ jets processes are a significant background to studies of Standard Model processes such as $t\bar{t}$ or single-top production, as well as searches for the Higgs boson and for physics beyond the Standard Model. Measurements of the cross section and kinematic properties of $V + n$ jets processes and comparisons to theoretical predictions are therefore of significant interest. This Letter reports on a first measurement at the Large Hadron Collider (LHC) of the $W + n$ jets cross section in proton–proton ($pp$) collisions at a centre-of-mass energy ($\sqrt{s}$) of 7 TeV, in both electron and muon decay modes of the $W$-boson, with the ATLAS detector. The measurement is based on an integrated luminosity of approximately 1.3 pb$^{-1}$.

The cross section measurements are presented as a function of jet multiplicity and of the transverse momentum ($p_T$) of the leading and next-to-leading jets in each event. Measurements are also presented of the ratio of cross sections $\sigma(W + n)/\sigma(W + n - 1)$ for inclusive jet multiplicities $n = 1-4$. The results have been corrected for all known detector effects and are quoted in a limited and well-defined range of jet and lepton kinematics, fully covered by the detector acceptance, so as to avoid model-dependent extrapolations and to facilitate comparisons with theoretical predictions. Previous measurements of $W + n$ jets production in proton–antiproton collisions at $\sqrt{s} = 1.96$ TeV were published by the CDF Collaboration [1]. Theoretical calculations at next-to-leading-order (NLO) in perturbative QCD (pQCD) have been computed for up to four jets for $W$ production [2,3]. Comparisons are made in this Letter with NLO pQCD calculations for $n \leq 2$; higher jet multiplicities are compared only to leading-order (LO) calculations.

2. The ATLAS detector

The ATLAS detector [4,5] consists of an inner tracking system (inner detector, or ID) surrounded by a thin superconducting solenoid providing a 2T magnetic field, electromagnetic and hadronic calorimeters and a muon spectrometer (MS). The ID consists of pixel and silicon microstrip (SCT) detectors, surrounded by the transition radiation tracker (TRT). The electromagnetic calorimeter is a lead liquid-argon (LAr) detector. Hadron calorimetry is based on two different detector technologies, with scintillators or LAr as active media, and with either steel, copper, or tungsten as the absorber material. The MS is based on three large superconducting toroids arranged with an eight-fold azimuthal coil symmetry around the calorimeters, and a system of three stations of chambers for the trigger and for precise measurements. The nominal $pp$ interaction point at the centre of the detector is defined as the origin of a right-handed coordinate system. The positive $x$-axis is defined by the direction from the interaction point to the centre of the LHC ring, with the positive $y$-axis pointing upwards, while the beam direction defines the $z$-axis. The azimuthal angle $\phi$ is measured around the beam axis and...
the polar angle \( \theta \) is the angle from the z-axis. The pseudorapidity is defined as \( \eta = -\ln \tan(\theta/2) \).

3. Simulated event samples

Simulated event samples were used for most of the background estimates, for the correction of the signal yield for detector effects and for comparisons of the results to theoretical expectations. The detector simulation [6] was performed using GEANT4 [7]. The simulated event samples are summarised in Table 1. The ALPGEN samples were generated with the MLM matching scheme [8] and interfaced to HERWIG v6.510 [9] for parton shower and fragmentation processes and to JIMMY v4.31 [10] for underlying event simulation. Parton density functions (PDF) were: CTEQ6L1 [11] for the ALPGEN and SHERPA samples, MRST 2007 LO [12] for PYTHIA, and MSTW2008 [13] for FELW [14]. For the POWHEG samples, the PDF set was CTEQ6.6M [15] for the NLO matrix element calculations, while CTEQ6L1 was used for the parton showering and underlying event via the POWHEG interface to PYTHIA. The radiation of photons from charged leptons was treated in HERWIG and PYTHIA using PHOTOS v2.15.4 [16]. Tauola v1.0.2 [17] was used for tau decays. The underlying event tune was the ATLAS MC09 tune [18] for the ALPGEN samples, PYTHIA inclusive vector boson production, and PYTHIA QCD samples. The POWHEG sample used the ATLAS MC09 tune with one parameter adjusted.1 The AMBT1 [19] tune was used for the PYTHIA W + jets samples. The samples generated with SHERPA used the default underlying event tune. Samples were generated with minimum bias interactions overlaid on top of the hard-scattering event in order to account for the multiple pp interactions in the same beam crossing (pile-up) experienced in the data. The number of minimum bias interactions followed a Poisson distribution with a mean of two [20]. These samples were then reweighted such that the distribution of the number of primary vertices matched that of the data.

4. Data and event selection

The data used in this analysis were collected from March to August 2010. Application of beam, detector, and data-quality requirements resulted in a total integrated luminosity of 1.3 pb⁻¹. The uncertainty on the luminosity determination is estimated to be 11% [26]. Criteria for electron and muon identification, as well as for event selection, followed closely those for the W-boson inclusive cross section analysis [27].

In the electron channel, a hardware-based level-one trigger system selected events containing one or more electron candidates, based on the presence of a cluster in the electromagnetic calorimeter with a transverse energy \( E_T \) greater than 14 GeV; this is the only difference in the electron channel with respect to the W inclusive cross section analysis, and was motivated by the fact that, for this larger dataset, this trigger was the lowest-threshold, useful electromagnetic trigger without any additional higher-level trigger requirements. The impact of the trigger efficiency was negligible for electrons with \( E_T > 20 \) GeV. In the offline analysis, electrons were required to pass the standard “tight” electron selection criteria [27] with \( E_T > 20 \) GeV and \( |\eta| < 2.47 \); electrons in the transition region between the barrel and endcap calorimeter \( (1.37 < |\eta| < 1.52) \) were rejected. The “tight” selection was used in order to improve the rejection of the QCD background. No isolation requirement was applied to the electron selection. Events were also rejected if there was a second electron passing the “medium” electron selection criteria [27] and the same kinematic selections as above.

In the muon channel, the hardware-based trigger selected events containing one or more muon candidates, based on hit patterns in the MS, corresponding to \( p_T > 10 \) GeV. Offline, the muons were required to be identified in both ID and MS sub-systems and to have \( p_T > 20 \) GeV and \( |\eta| < 2.4 \). The ID track was required to have \( \geq 2 \) hits in the pixel detector, \( \geq 6 \) hits in the SCT and, for tracks with \( |\eta| < 2.0, \geq 1 \) hit in the TRT. The muon impact parameter with respect to the primary vertex [20] was required to be \( < 0.1 \) mm and \(< 10 \) mm in the \( r-\phi \) and \( r-z \) planes, respectively. The first of these requirements was added to further reduce non-prompt muons from decays of hadrons, and muons from cosmic rays. The difference between the ID and MS \( p_T \), corrected for the mean energy loss in upstream material, was required to satisfy \( p_T^{ID} - p_T^{MS} < 0.5 \times p_T^{ID} \). Compared to the criteria used in Ref. [27], this scaled requirement reduced the background from decays-in-flight of hadrons and improved the signal efficiency at high \( p_T \). As in Ref. [27], the muons were required to be isolated, following a track-based isolation, but the cone size was reduced from \( \Delta R = 0.4 \) to \( \Delta R = 0.2 \) (where \( \Delta R = \sqrt{\Delta \eta^2 + \Delta \phi^2} \) of the muon) and the isolation requirement was changed from \( \Sigma p_T^{ID} / p_T \leq 0.2 \) to \( \Sigma p_T^{ID} < 1.8 \) GeV to improve the QCD background rejection. With these optimised cuts, the QCD background was reduced by a factor of 1.7 for the inclusive 1-jet sample. In addition, a number of requirements were added on the tracks inside the isolation cone: the difference between the \( z \) position of the track extrapolated to the beam line and the \( z \) coordinate of the primary vertex was required to be \( < 1 \) cm, and the total number of hits in the pixel and SCT detectors was required to be \( \geq 4 \). These additional requirements further improved the rejection of QCD background. Events were rejected if there was a second muon passing the same kinematic selections and isolation requirements as above.

The calculation of missing transverse energy (\( E_T^{miss} \)) and transverse mass \( (M_T) \) followed the prescription in Ref. [27]. \( M_T \) was defined by the lepton and neutrino \( p_T \) as \( M_T = \sqrt{2 p_T^{\ell} p_T^{\nu}(1 - \cos(\phi^{\ell} - \phi^{\nu}))} \), where the \( (x, y) \) components of the neutrino momentum were inferred from the corresponding \( E_T^{miss} \) components. \( E_T^{miss} \) was calculated from the energy deposits of calorimeter cells inside three-dimensional clusters [28]. These clusters were then corrected to take into account the different response to hadrons compared to electrons or photons, as well as dead material and out-of-cluster energy losses [29]. In the muon channel, \( E_T^{miss} \) was corrected for the muon momentum. Events were required to have \( E_T^{miss} > 25 \) GeV and \( M_T > 40 \) GeV. After requiring \( \geq 1 \) primary vertex with \( \geq 3 \) associated tracks in the event, the primary vertex was required to be within 150 mm along the beam direction relative to the centre of the detector. In events with multiple vertices along the beam axis, the vertex with the largest \( \Sigma p_T^{ID} \) of associated tracks was taken as the primary event vertex. Starting from approximately \( 9.6 \times 10^6 \) triggered events in each of the electron and muon channels, these selection criteria reduced the sample to 4216 and 4911 events, respectively.

Jets were reconstructed using the anti-\( k_t \) algorithm [30] with a radius parameter \( R = 0.4 \) [31]. The efficiency for reconstructing jets was found to be approximately 98% in simulation for jet \( p_T \) of 20 GeV, rising to close to 100% efficiency for 30 GeV jets. Jets arising from detector noise or cosmic rays were rejected [32]. To take into account the differences in calorimeter response to electrons and hadrons, a \( p_T \) - and \( \eta \)-dependent factor, derived from simulated events, was applied to each jet to provide an average energy scale correction [31] back to particle-level. Jets were required to have \( |\eta| < 2.8 \) and \( p_T > 20 \) GeV. All jets within \( \Delta R < 0.5 \) of an

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1 The cutoff for multiple parton interactions, PARP(32), was adjusted from 2.3 to 2.1 GeV, suitable for the CTEQ6L1 PDF.
electron or muon (that passed the lepton identification requirements) were removed, regardless of the jet pt or η.

Jets from pile-up interactions were removed by a cut on the jet-vertex fraction (JVF) which was computed for each jet in the event. After associating tracks to jets with a simple matching in ΔR(track, jet), requiring ΔR < 0.4, the JVF was computed for each jet as the scalar sum pT of all matched tracks from the primary vertex divided by the total jet-matched track pT from all vertices. Jets which fell outside of the fiducial tracking region (|η| < 2.5) or which had no matching tracks were not considered for the JVF cut. Jets for which JVF < 0.75 were rejected; this requirement was chosen to optimise the Kolmogorov distance between the jet multiplicity (in data) with and without pile-up interactions. The application of the JVF cut reduced the sensitivity of the measured jet multiplicity distribution to additional jets from pile-up. The rejection rate of pile-up jets was found to be linear as a function of the number of pile-up interactions. The bias of the JVF cut on the jet multiplicity was found to be negligible for events with ≤ 4 jets.

5. Signal and background yields

The major background processes in the electron channel are QCD and leptonic backgrounds. The latter consist of

\[ W \rightarrow τν \rightarrow ℓν \ell'ν \]

where the tau decays to an electron, and semileptonic tt decays (\( tt \rightarrow b\bar{b}qq'ℓν \)). The QCD background in the electron channel has two components, one where a hadronic jet passes the electron selection and additional energy mismeasurement in the event results in large E_{miss}^γ, and the other where a bottom- or charm-hadron decays to an electron. For the muon channel, the main backgrounds arise from semileptonic heavy flavour decays in multijet events and from the leptonic background from the following sources: W → τν where the tau decays to a muon, Z → μμ where one muon is not identified, and semileptonic tt decays in the muon channel. The contributions of single-top and diboson production to the measured cross section have been estimated to be slightly smaller than the W → τν background, and are not subtracted from the data.

The number of leptonic background events surviving the above selection cuts was estimated with simulated event samples: ALPGEN for vector boson samples (PYTHIA was used for W → τν+jets) and POWHEG for tt background. The simulated leptonic background samples were normalised to the integrated luminosity of the data using the predicted NNLO or NLO+NNLL cross sections. The number of QCD background events was estimated by fitting, in each jet multiplicity bin, the E_{miss}^γ distribution in the data (without the E_{miss}^γ and M_{T} cuts) to a sum of two templates: one for the QCD background and another which included signal and the leptonic backgrounds. In both muon and electron channels, the shapes for the second template were obtained from simulation. In the electron channel, the template for the QCD background was obtained from the data because the mechanisms by which a jet fakes an electron are difficult to simulate. This template was derived from a data sample where looser electron identification criteria were applied on the shower shapes and the track-cluster matching requirements were inverted. In the muon channel, the QCD template was obtained from simulations. The QCD background was computed from the results of the template fit. In the electron channel, the fit was performed in the region E_{miss}^γ > 10 GeV due to the poor understanding of the background below 10 GeV. The fit to the E_{miss}^γ distribution was used only to determine the QCD background normalisation, taking into account contributions from leptonic background and signal in the low E_{miss} region. The W + jet signal yield for the cross section calculation was derived as the difference between the observed number of events in the signal region and the sum of background components. Fig. 1 shows the E_{miss}^γ distribution for events with one jet, with the fitted contributions from all background sources in the electron and muon channels respectively, after all the other selection requirements (except for the M_{T} and E_{miss} requirements) have been applied. The residual difference in E_{miss}^γ between the data and the QCD template in the control region is covered by the systematic uncertainties. The number of observed events and the estimated number of background events are summarised in Table 2.

The yield of signal events was corrected back to the particle level, taking into account detector and reconstruction efficiency. The dominant corrections in the electron channel come from electron reconstruction efficiency (≈ 20%) and from the lepton identification requirements. In the muon channel, the dominant corrections come from trigger and reconstruction efficiency (corrections of ≈ 10–20% and ≈ 10% respectively). The corrections were computed using the ALPGEN W + jets event generator plus full detector simulation, restricting the events to the same phase space as the data analysis. The phase space requirements were applied to generated quantities. In this analysis, particle-level jets were constructed in simulated events by applying the jet finder to all final state particles (excluding muons and neutrinos) with a lifetime longer than 10 ps, whether produced directly in the pp collision or from the decay of particles with shorter lifetimes. Correction factors were computed as one-dimensional functions of jet multiplicity and pT of the leading and next-to-leading jets, and were treated as independent. Migration of events across bins of jet pT was made small compared to the

Table 1

<table>
<thead>
<tr>
<th>Physics process</th>
<th>Generator</th>
<th>σ (BR (nb))</th>
</tr>
</thead>
<tbody>
<tr>
<td>W → ℓν inclusive (ℓ = e, μ, τ)</td>
<td>PYTHIA 6.4.21 [21]</td>
<td>10.46 NNLO [14]</td>
</tr>
<tr>
<td>W → ℓν</td>
<td>PYTHIA 6.4.21 [21]</td>
<td>6.16 NNLO [14]</td>
</tr>
<tr>
<td>W → ℓν</td>
<td>PYTHIA 6.4.21 [21]</td>
<td>4.30 NNLO [14]</td>
</tr>
<tr>
<td>W → ℓν+jets (ℓ = e, μ, τ)</td>
<td>ALPGEN 2.13 [22]</td>
<td>1.07 NNLO [14]</td>
</tr>
<tr>
<td>W → ℓν+jets (ℓ = e, μ, τ)</td>
<td>SHERPA 1.13 [23]</td>
<td></td>
</tr>
<tr>
<td>Z → ℓν+jets (M_{T} ≥ 40 GeV, 0 ≤ N_{parton} &lt; 5)</td>
<td>ALPGEN 2.13 [22]</td>
<td>0.16 NLO + NNLL [25]</td>
</tr>
<tr>
<td>Z → ℓν+jets (M_{T} ≥ 40 GeV, 0 ≤ N_{parton} &lt; 5)</td>
<td>POWHEG-HVQ v1.01 patch 4 [24]</td>
<td></td>
</tr>
<tr>
<td>Dijet (e channel, p_{T} &gt; 15 GeV)</td>
<td>PYTHIA 6.4.21 [21]</td>
<td>1.2 × 10^{6} LO [21]</td>
</tr>
<tr>
<td>Dijet (μ channel, p_{T} &gt; 8 GeV, p_{T}^{miss} &gt; 8 GeV)</td>
<td>PYTHIA 6.4.21 [21]</td>
<td>10.6 × 10^{6} LO [21]</td>
</tr>
</tbody>
</table>
lated photons within QED radiation, the energy of the generated lepton was defined as recover particle-level distributions. To treat the effect of final state calculated data showed that these correction factors were sufficient to directly from the data as follows. In the electron channel, events were triggered either by an independent \( \sqrt{s} \) trigger or a loose electron trigger with an approximately 5 GeV threshold. The full \( W + \text{jets} \) selection was carried out in essentially the same way as described above in order to isolate a pure electron sample. The main difference was in the QCD background estimation, which was done with templates for the shape of the electron isolation distribution, where the isolation variable was defined as the sum of transverse energy in a cone of \( \Delta R = 0.4 \) around the electron divided by the transverse energy of the electron. These templates were obtained by inverting one or more of the electron shower shape requirements. The electron trigger efficiency was found to be close to 100% in both data and simulation. In the muon channel, the trigger efficiency was computed with a sample of unbiased offline reconstructed muons from \( Z \rightarrow \mu \mu \) decays. Average trigger efficiencies of 82.0 ± 1.4% and 86.9 ± 0.1% were obtained in data and simulation, respectively; the difference between data and simulation comes from a mismodelling of both the efficiency of the forward muon chambers and of the programming of the muon trigger electronics. The trigger efficiency (and its uncertainty) from the data was used for the correction factor.

### Table 2

<table>
<thead>
<tr>
<th>Background Source</th>
<th>( N_{\text{jet} \geq 0} )</th>
<th>( N_{\text{jet} \geq 1} )</th>
<th>( N_{\text{jet} \geq 2} )</th>
<th>( N_{\text{jet} \geq 3} )</th>
<th>( N_{\text{jet} \geq 4} )</th>
</tr>
</thead>
<tbody>
<tr>
<td>QCD</td>
<td>130 ± 20</td>
<td>100 ± 40</td>
<td>45 ± 20</td>
<td>18 ± 8</td>
<td>–</td>
</tr>
<tr>
<td>( W \rightarrow \tau \nu )</td>
<td>113 ± 11</td>
<td>28 ± 5</td>
<td>4 ± 2</td>
<td>0.5 ± 0.4</td>
<td>–</td>
</tr>
<tr>
<td>( Z \rightarrow ee )</td>
<td>17 ± 2</td>
<td>7 ± 6</td>
<td>3 ± 2</td>
<td>1 ± 1</td>
<td>–</td>
</tr>
<tr>
<td>Observed in data</td>
<td>4216</td>
<td>987</td>
<td>276</td>
<td>83</td>
<td>–</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Background Source</th>
<th>( N_{\text{jet} \geq 0} )</th>
<th>( N_{\text{jet} \geq 1} )</th>
<th>( N_{\text{jet} \geq 2} )</th>
<th>( N_{\text{jet} \geq 3} )</th>
<th>( N_{\text{jet} \geq 4} )</th>
</tr>
</thead>
<tbody>
<tr>
<td>QCD</td>
<td>30 ± 20</td>
<td>20 ± 13</td>
<td>4 ± 2</td>
<td>2 ± 2</td>
<td>1 ± 1</td>
</tr>
<tr>
<td>( W \rightarrow \tau \nu )</td>
<td>133 ± 12</td>
<td>24 ± 6</td>
<td>5 ± 2</td>
<td>0.9 ± 0.5</td>
<td>0.4 ± 0.3</td>
</tr>
<tr>
<td>( Z \rightarrow \mu \mu )</td>
<td>170 ± 14</td>
<td>30 ± 4</td>
<td>8 ± 1</td>
<td>2 ± 0.5</td>
<td>0.6 ± 0.2</td>
</tr>
<tr>
<td>( Z \rightarrow \tau \nu )</td>
<td>18 ± 2</td>
<td>18 ± 2</td>
<td>18 ± 2</td>
<td>16 ± 2</td>
<td>11 ± 1</td>
</tr>
<tr>
<td>Observed in data</td>
<td>4911</td>
<td>1049</td>
<td>292</td>
<td>95</td>
<td>36</td>
</tr>
</tbody>
</table>

The primary sources of systematic uncertainty in the cross section for both electron and muon channels are uncertainties in the integrated luminosity and in the jet energy scale [31]. In the electron channel, the uncertainty due to the QCD background shape is also important. Both electron and muon channels are affected by uncertainties in the lepton reconstruction efficiency. The luminosity uncertainty enters primarily through the signal normalisation but also has an effect on the estimation of the leptonic backgrounds; the luminosity uncertainty is therefore larger in the muon channel.

Uncertainties in the jet energy scale (JES) and jet energy resolution (JER) were determined primarily from simulations [31]. The JES uncertainty varies as a function of jet \( p_T \) and \( \eta \), and ranges from around 10% at 20 GeV to about 8% at 100 GeV. The JER uncertainty is 14% of the jet energy resolution. To take into account the differences in calorimeter response to quark- and gluon-initiated jets, an additional uncertainty of 5% was added in quadrature to the JES uncertainty, based on the average difference in simulation of the calorimeter response between jets in the \( W + \text{jets} \) sample compared to those in the dijet samples (on which the JES...
calibration is based). Uncertainties in the JES due to nearby jets in \( W + \) jets events were also studied but found to be small. To estimate the impact of the JES uncertainty, jet energies in the simulated events were shifted by the JES uncertainty, and the \( E_{T}^{\text{miss}} \) vector was recomputed. In addition, calorimeter clusters not associated to a jet or electron, such as those coming from the underlying event, were scaled using a \( p_{T} \)-dependent uncertainty [27], ranging from \( \pm 20\% \) for \( p_{T} \approx 500 \text{ MeV} \) to \( \pm 5\% \) at high \( p_{T} \). Similarly, the jet energies were smeared with a Gaussian representing the JER uncertainty and the \( E_{T}^{\text{miss}} \) vector was recomputed. The full analysis was repeated with these variations, and the cross sections were recomputed; the change in the cross section was taken as the systematic uncertainty. The impact of the JES and \( E_{T}^{\text{miss}} \) uncertainties on the cross section uncertainty was approximately 10%.

A significant source of uncertainty in the electron channel is the potential bias in the sample selection for building the template shape of the QCD background; with the current selection requirements, the contribution from semileptonic heavy flavour decays is underestimated. The size of the effect was determined with simulated events by comparing the background estimates from two templates: one based on the electron selection used for this cross section measurement and the other based on the selection used for the QCD background estimation in the electron channel. The resulting uncertainty on the QCD background estimate, including significant contributions from the limited statistics of the simulated event samples, was as high as 50%, but the effect on the cross section for the inclusive 1-jet bin was about 5%. The fit region for the QCD background was varied by \( \pm 5 \text{ GeV} \) to account for shape differences in the low \( E_{T}^{\text{miss}} \) region; the resulting uncertainty on the cross section was 1–2%.

The uncertainty in the electron identification efficiency was taken from the inclusive cross section measurement [27]. By examining the reconstruction efficiency in simulated events as a function of the \( \Delta R \) separation between the jet and the electron, the reconstruction efficiency was found to be consistent with the value in Ref. [27]. Furthermore, in the region \( \Delta R > 0.5 \), the efficiency was found to be constant as a function of \( \Delta R \) and as a function of jet multiplicity. The uncertainty in the muon reconstruction efficiency was estimated by comparing the efficiency measured with simulated events to that measured in the data with muons from \( Z \rightarrow \mu\mu \) decays, following a method similar to that described in Ref. [27]. The resulting uncertainties in the cross section were approximately 5.5% in both electron and muon channels.

Other uncertainties which were considered include the trigger efficiency, jet reconstruction efficiency, lepton momentum scale and resolution, pile-up, and biases in the procedure for correcting for detector effects (for example, by comparing correction factors obtained with ALPGEN to those obtained with SHERPA). Their effect on the cross section was found to be smaller than the uncertainties described above. For example, the uncertainty on the electron energy resolution was based on extrapolations from test-beam measurements [27] and had a \(< 0.1\% \) effect on the cross section. All of the above systematic uncertainties (except for the bias in the template shape for the QCD background in the electron channel) were also applied to the estimates of the QCD and lepton backgrounds in both electron and muon channels. In addition, for the leptonic backgrounds the uncertainty in the NNLO cross sections was taken to be 5% for \( W/Z \) production as in Ref. [27]. The \( R \) cross section uncertainty was taken to be approximately 7%, amounting to the sum in quadrature of PDF uncertainties (3%) and uncertainties estimated by varying renormalisation and factorisation scales (6%) [33]. The resulting uncertainty on the \( W + \) jets cross section ranged from 0.1 to 2%, depending on the jet multiplicity, and was small compared to other systematic uncertainties.

The systematic uncertainties in the cross section measurement are summarised in Table 3 for \( N_{\text{jet}} \geq 1 \); most of the uncertainties are approximately independent of jet multiplicity, except for the uncertainty due to the jet energy scale and resolution, and the QCD background in the electron channel. The dominant systematic uncertainties are shown as a function of jet multiplicity and leading jet \( p_{T} \) in Fig. 2. Both distributions are similar for electron and muon channels; the uncertainty is therefore shown as a function of jet multiplicity for the electron channel and as a function of leading jet \( p_{T} \) for the muon channel. The main contribution to the other uncertainties in the electron channel comes from the QCD background (especially at high jet multiplicities), the electron identification efficiency and the electron energy scale. For the muon channel, the main contribution is from the muon reconstruction efficiency.

In the cross section ratio measurement, the uncertainty due to the jet energy scale uncertainty remains the dominant effect, amounting to approximately 10% on the ratio. The luminosity uncertainty does not completely cancel in the ratio because the background estimates are affected by the luminosity uncertainty and the background levels vary as a function of jet multiplicity.

7. Results and conclusions

The measured \( W + \) jets cross section (multiplied by the leptonic branching ratio) and the cross section ratios are shown as a function of corrected jet multiplicity in Tables 4 and 5 respectively, as well as in Figs. 3 and 4. The measurement was not performed in the inclusive 4-jet bin in the electron channel because of the poor signal-to-background ratio. The cross sections are quoted in the limited kinematic region: \( E_{T}^{\mu} > 20 \text{ GeV} \), \( |\eta^{\mu}| < 2.8 \), \( E_{T}^{\ell} > 20 \text{ GeV} \), \( |\eta^{\ell}| < 2.47 \) (excluding \( 1.37 < |\eta^{\ell}| < 1.52 \), \( |\eta^{\mu}| < 2.4 \), \( p_{T}^{\ell} > 25 \text{ GeV} \), \( M_{T} > 40 \text{ GeV} \), \( \Delta R^{\ell\mu} > 0.5 \), where \( \ell, j \) and \( \nu \) denote lepton, jet and neutrino, respectively. The quantities \( p_{T}^{\ell} \), \( |\eta^{\ell}| \), and \( M_{T} \) include the energy of all radiated photons within \( \Delta R = 0.1 \) around the lepton. The \( W + \) jets cross section (times leptonic branching ratio) is shown as a function of \( p_{T} \) of the leading and next-to-leading jets in the event in Fig. 5; the leading jet is shown for \( N_{\text{jet}} \geq 1 \) and the next-to-leading jet is shown for \( N_{\text{jet}} \geq 2 \).

Also shown in Figs. 3, 4, and 5 are particle-level expectations from PYTHIA, ALPGEN and SHERPA simulations as well as a calculation using MCFM v5.8 [35]. PYTHIA is LO, while ALPGEN and SHERPA match higher-multiplicity matrix elements to a leading-logarithmic parton shower; these predictions have been normalised to the NNLO inclusive \( W \) production cross section. The version of MCFM used here provides NLO predictions at parton level for \( W \)-boson production with \( N_{\text{jet}} \leq 2 \); only leading-order predictions are available for \( W + \) three jets. No additional normalisation was applied to the MCFM predictions.

The MCFM results were obtained with the same jet algorithm and same kinematic selection requirements as applied to the data. Renormalisation and factorisation scales were set to \( H_{T}/2 \), where \( H_{T} \) is the scalar sum of the \( p_{T} \) of the unclustered partons and of the lepton and neutrino from the \( W \) decay. The PDFs were CTEQ6L1 [11] and CTEQ6.6M [15] for the LO and NLO calculations, respectively. Corrections for hadronisation and underlying event were computed with PYTHIA as a function of leading and next-to-leading jet \( p_{T} \). Hadronisation and underlying event corrections ranged from \(-10\% \) to \(-4\% \) and \(+10\% \) to \(+4\% \), respectively, for jet \( p_{T} \approx 20 \text{ GeV} \) to \( p_{T} > 80 \text{ GeV} \). The partial cancellation of hadronisation and underlying event corrections [5] results in an overall correction of approximately 4%. The effect of final state QED radi-
summing up the photons within acceptance before radiation with the acceptance after radiation, but ALPGEN (both using PHOTOS) and with SHERPA, comparing the ac-

Table 3
Summary of the systematic uncertainties in the cross section. The uncertainties are shown only for $N_{\text{jet}} \geq 1$. The sign convention for the JES and lepton energy scale uncertainties is such that a positive change in the energy scale results in an increase in the jet or lepton energy observed in the data.

<table>
<thead>
<tr>
<th>Effect</th>
<th>Range</th>
<th>Cross section uncertainty (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Jet energy scale and $E_{\text{T}}^{\text{miss}}$</td>
<td>$\pm 10%$ (dependent on jet $\eta$ and $p_T$)</td>
<td>$\pm 5%$</td>
</tr>
<tr>
<td>Jet energy resolution</td>
<td>$\pm 14%$ on each jet</td>
<td>$\pm 1.0$</td>
</tr>
<tr>
<td>Electron triggers</td>
<td>$\pm 0.5%$</td>
<td>$\pm 0.7$</td>
</tr>
<tr>
<td>Electron identification</td>
<td>$\pm 0.2%$</td>
<td>$\pm 5.5$</td>
</tr>
<tr>
<td>Electron energy scale</td>
<td>$\pm 3%$</td>
<td>$\pm 3.9$, $-4.7$</td>
</tr>
<tr>
<td>Pile-up removal cut</td>
<td>4–7% in lowest jet $p_T$ bin</td>
<td>$\pm 1.9$</td>
</tr>
<tr>
<td>Residual pile-up effects</td>
<td>from simulation</td>
<td>$\pm 2.2$</td>
</tr>
<tr>
<td>QCD background shape</td>
<td>from template variation</td>
<td>$-1.5$, $+5.2$</td>
</tr>
<tr>
<td>Luminosity</td>
<td>$\pm 11%$</td>
<td>$-10$, $+13$</td>
</tr>
</tbody>
</table>

$\mu$ channel

<table>
<thead>
<tr>
<th>Effect</th>
<th>Range</th>
<th>Cross section uncertainty (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Jet energy scale and $E_{\text{T}}^{\text{miss}}$</td>
<td>$\pm 10%$ (dependent on jet $\eta$ and $p_T$)</td>
<td>$\pm 5%$</td>
</tr>
<tr>
<td>Jet energy resolution</td>
<td>$\pm 14%$ on each jet</td>
<td>$\pm 1.8$</td>
</tr>
<tr>
<td>Muon trigger</td>
<td>$\pm 2.5%$ in barrel, $\pm 2.0%$ in endcap</td>
<td>$\pm 1.6$</td>
</tr>
<tr>
<td>Muon reconstruction</td>
<td>$\pm 5.6%$</td>
<td>$-5.4$, $+5.9$</td>
</tr>
<tr>
<td>Muon momentum scale</td>
<td>$\pm 1.3%$</td>
<td>$+2$, $-0.9$</td>
</tr>
<tr>
<td>Muon momentum resolution</td>
<td>$\pm 5%$ in barrel, $\pm 5%$ in endcap</td>
<td>$\pm 1.4$</td>
</tr>
<tr>
<td>Pile-up removal cut</td>
<td>4–7% in lowest jet $p_T$ bin</td>
<td>$\pm 1.7$</td>
</tr>
<tr>
<td>Residual pile-up effects</td>
<td>from simulation</td>
<td>$\pm 1.4$</td>
</tr>
<tr>
<td>Luminosity</td>
<td>$\pm 11%$</td>
<td>$-11$, $+13$</td>
</tr>
</tbody>
</table>

Fig. 2. Summary of the systematic uncertainties on the cross section measurement shown as a function of jet multiplicity in the electron channel (left) and leading-jet $p_T$ in the muon channel (right). The jet energy scale uncertainty includes the uncertainty on $E_{\text{T}}^{\text{miss}}$. The main contribution to the “sum of other uncertainties” in the electron channel comes from the QCD background (especially at high jet multiplicities), the electron identification efficiency and the electron energy scale. For the muon channel, the main contribution is from the muon reconstruction efficiency.

Table 4
The measured cross section times leptonic branching ratio for $W + \text{jets}$ in the electron and muon channels as a function of corrected jet multiplicity with (in order) statistical, systematic, and luminosity uncertainties. The cross sections are quoted in a limited and well-defined kinematic region, described in the text. The measurement was not performed in the inclusive 4-jet bin in the electron channel because of the poor signal-to-background ratio. Theoretical predictions from MCFM are also shown, with all uncertainties combined. MCFM provides NLO predictions for $N_{\text{jet}} \leq 2$ and a LO prediction for $N_{\text{jet}} = 3$.

<table>
<thead>
<tr>
<th>Jet multiplicity</th>
<th>$W \rightarrow e\nu + \text{jets}$ (nb)</th>
<th>MCFM $W \rightarrow e\nu$ (nb)</th>
<th>$W \rightarrow \mu\nu + \text{jets}$ (nb)</th>
<th>MCFM $W \rightarrow \mu\nu$ (nb)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\geq 0$</td>
<td>$4.53 \pm 0.07^{+0.15}<em>{-0.16}^{+0.18}</em>{-0.10} - 0.47$</td>
<td>$5.08 \pm 0.11$</td>
<td>$4.58 \pm 0.07^{+0.18}<em>{-0.16}^{+0.21}</em>{-0.32} - 0.49$</td>
<td>$5.27 \pm 0.11$</td>
</tr>
<tr>
<td>$\geq 1$</td>
<td>$0.84 \pm 0.03^{+0.13}<em>{-0.10}^{+0.11}</em>{-0.09} - 0.04$</td>
<td>$0.81 \pm 0.04$</td>
<td>$0.84 \pm 0.03^{+0.11}<em>{-0.09}^{+0.04}</em>{-0.09} - 0.09$</td>
<td>$0.84 \pm 0.04$</td>
</tr>
<tr>
<td>$\geq 2$</td>
<td>$0.21 \pm 0.01^{+0.02}<em>{-0.01}^{+0.03}</em>{-0.02}$</td>
<td>$0.21 \pm 0.03$</td>
<td>$0.23 \pm 0.04^{+0.05}<em>{-0.03}^{+0.06}</em>{-0.04} - 0.02$</td>
<td>$0.21 \pm 0.02$</td>
</tr>
<tr>
<td>$\geq 3$</td>
<td>$0.047 \pm 0.007^{+0.005}<em>{-0.006}^{+0.008}</em>{-0.011} - 0.006$</td>
<td>$0.05 \pm 0.02$</td>
<td>$0.064 \pm 0.008^{+0.010}<em>{-0.006}^{+0.009}</em>{-0.008} - 0.006$</td>
<td>$0.05 \pm 0.02$</td>
</tr>
<tr>
<td>$\geq 4$</td>
<td>--</td>
<td>--</td>
<td>$0.019 \pm 0.005^{+0.004}_{-0.003}$</td>
<td>--</td>
</tr>
</tbody>
</table>

The systematic uncertainty in the MCFM cross sections due to fragmentation was estimated by comparing PYTHIA with HERWIG. Underlying event uncertainties were estimated by comparing the AMBT1 [19] event generator tune with the tune from JIMMY [10] as well as by varying the AMBT1 tune to increase the underlying event activity by approximately 10%. Renormalisation and factori-
Table 5
The measured cross section ratio for \( W + \text{jets} \) in the electron and muon channels as a function of corrected jet multiplicity with (in order) statistical and systematic uncertainties. The cross section ratios are quoted in a limited and well-defined kinematic region, described in the text. The measurement was not performed in the inclusive 4-jet bin in the electron channel because of the poor signal-to-background ratio. Theoretical predictions from MCFM are also shown, with all uncertainties combined. MCFM provides NLO predictions for \( N_{\text{jet}} \leq 2 \) and a LO prediction for \( N_{\text{jet}} = 3 \).

<table>
<thead>
<tr>
<th>Jet multiplicity</th>
<th>( W \rightarrow e\nu )</th>
<th>MCFM ( W \rightarrow e\nu )</th>
<th>( W \rightarrow \mu\nu )</th>
<th>MCFM ( W \rightarrow \mu\nu )</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \geq 1/\geq 0 )</td>
<td>( 0.185 \pm 0.007 \pm 0.005 )</td>
<td>( 0.250 \pm 0.019 \pm 0.000 )</td>
<td>( 0.224 \pm 0.037 \pm 0.022 )</td>
<td>( 0.241 \pm 0.037 \pm 0.061 )</td>
</tr>
<tr>
<td>( \geq 2/\geq 1 )</td>
<td>( 0.185 \pm 0.007 \pm 0.005 )</td>
<td>( 0.250 \pm 0.019 \pm 0.000 )</td>
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<tr>
<td>( \geq 4/\geq 3 )</td>
<td>( 0.185 \pm 0.007 \pm 0.005 )</td>
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</tr>
</tbody>
</table>

Fig. 3. \( W + \text{jets} \) cross section results as a function of corrected jet multiplicity. Left: electron channel. Right: muon channel. The cross sections are quoted in a limited and well-defined kinematic region, described in the text. For the data, the statistical uncertainties are shown by the vertical bars, and the combined statistical and systematic uncertainties are shown by the hashed regions. Also shown are predictions from PYTHIA, ALPGEN, SHERPA and MCFM, and the ratio of theoretical predictions to data (PYTHIA is not shown in the ratio). The theoretical uncertainties are shown only for MCFM, which provides NLO predictions for \( N_{\text{jet}} \leq 2 \) and a LO prediction for \( N_{\text{jet}} = 3 \).

Fig. 4. \( W + \text{jets} \) cross section ratio results as a function of corrected jet multiplicity. Left: electron channel. Right: muon channel. The cross sections are quoted in a limited and well-defined kinematic region, described in the text. For the data, the statistical uncertainties are shown by the vertical bars, and the combined statistical and systematic uncertainties are shown by the hashed regions. Also shown are theoretical predictions from PYTHIA, ALPGEN, SHERPA, and MCFM. The theoretical uncertainties are shown only for MCFM, which provides NLO predictions for \( N_{\text{jet}} \leq 2 \) and a LO prediction for \( N_{\text{jet}} = 3 \).

sation scale uncertainties were estimated by varying the scales, in all combinations, up and down, by factors of two. PDF uncertainties were computed by summing in quadrature the dependence on each of the 22 eigenvectors characterising the CTEQ6.6 PDF set; the uncertainty in \( \alpha_s \) was also taken into account. An alternative PDF set, MSTW2008 [13], with its set of 68% C.L. eigenvectors was also examined, and the envelope of the uncertainties from CTEQ6.6 and MSTW2008 was taken as the final PDF uncertainty. The total resulting uncertainties are given in Tables 4 and 5.

In conclusion, this Letter presents a measurement of the \( W + \text{jets} \) cross section as a function of jet multiplicity in \( pp \) collisions at \( \sqrt{s} = 7 \) TeV in both electron and muon decay modes of the
Fig. 5. $W + \text{jets}$ cross section as a function of the $p_T$ of the two leading jets in the event. The $p_T$ of the leading jet is shown for events with $\geq 1$ jet while the $p_T$ of the next-to-leading jet is shown for events with $\geq 2$ jets. Left: electron channel. Right: muon channel. The cross sections are quoted in a limited and well-defined kinematic region, described in the text. For the data, the statistical uncertainties are shown by the vertical bars, and the combined statistical and systematic uncertainties are shown by the hashed regions. Also shown are theoretical predictions from PYTHIA, ALPGEN, SHERPA and MCFM, and the ratio of theoretical predictions to data (PYTHIA is not shown in the ratio). The theoretical uncertainties are shown only for MCFM, which provides NLO predictions for $N_{\text{jet}} \leq 2$ and a LO prediction for $N_{\text{jet}} = 3$.

$W$-boson, based on an integrated luminosity of 1.3 pb$^{-1}$ recorded with the ATLAS detector. Measurements are also presented of the ratio of cross sections $\sigma(W + \geq n)/\sigma(W + \geq n - 1)$ for inclusive jet multiplicities $n = 1$–4, and of the $p_T$ distribution of the leading and next-to-leading jets in the event. The results have been corrected for all known detector effects and are quoted in a limited and well-defined range of jet and lepton kinematics. This range is fully covered by the detector acceptance, so as to avoid model-dependent extrapolations and to facilitate comparisons with theoretical predictions. As expected, the PYTHIA samples considered, which contain a $2 \rightarrow 1$ matrix element merged with a $2 \rightarrow 2$ matrix element and a leading-logarithmic parton shower, does not provide a good description of the data for jet multiplicities greater than one. Good agreement is observed with the predictions of the multi-parton matrix element generators ALPGEN and SHERPA. Calculations based on $O(\alpha_s^2)$ matrix elements in MCFM (available for jet multiplicities $n \leq 2$) are also in good agreement with the data.

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References

ATLAS Collaboration
