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A search for new physics in dijet mass and angular distributions in $pp$ collisions at $\sqrt{s} = 7$ TeV measured with the ATLAS detector

The ATLAS Collaboration

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**Abstract.** A search for new interactions and resonances produced in LHC proton–proton ($pp$) collisions at a centre-of-mass energy $\sqrt{s} = 7$ TeV was performed with the ATLAS detector. Using a dataset with an integrated luminosity of 36 pb$^{-1}$, dijet mass and angular distributions were measured up to dijet masses of $\sim 3.5$ TeV and were found to be in good agreement with Standard Model predictions. This analysis sets limits at 95% CL on various models for new physics: an excited quark is excluded for mass between 0.60 and 2.64 TeV, an axigluon hypothesis is excluded for axigluon masses between 0.60 and 2.10 TeV and quantum black holes are excluded in models with six extra space–time dimensions for quantum gravity scales between 0.75 and 3.67 TeV. Production cross section limits as a function of dijet mass are set using a simplified Gaussian signal model to facilitate comparisons with other hypotheses. Analysis of the dijet angular distribution using a novel technique simultaneously employing the dijet mass excludes quark contact interactions with a compositeness scale $\Lambda$ below 9.5 TeV.
The search for new phenomena in particle interactions is perhaps most exciting when new
vistas are opened up by significant increases in experimental sensitivity, either by collecting
larger samples of data or by entering kinematic regimes never before explored. Searches are
particularly compelling when one can do both, as has recently become the case in the first
studies of proton–proton (pp) collisions at a centre-of-mass (CM) energy of 7 TeV produced
at the CERN Large Hadron Collider (LHC). We report on a search for massive objects and
new interactions using a sample of 36 pb\(^{-1}\) of integrated luminosity observed by the ATLAS
detector.

This analysis focuses on those final states where two very energetic jets of particles are
produced with large transverse momentum ($p_T$) transfer. These $2 \rightarrow 2$ scattering processes are
well described within the Standard Model (SM) by perturbative quantum chromodynamics
(QCD), the quantum field theory of strong interactions. However, there could be additional...
contributions from the production of a new massive particle that then decays into a dijet final state, or the rate could be enhanced through a new force that only manifests itself at very large CM energies.

One can perform sensitive searches for new phenomena by studying both the dijet invariant mass, \( m_{jj} \), and the angular distributions of energetic jets relative to the beam axis, usually described by the polar scattering angle in the two-parton CM frame, \( \theta^* \). QCD calculations predict that high-\( p_T \) dijet production is dominated by \( t \)-channel gluon exchange, leading to rapidly falling \( m_{jj} \) distributions and angular distributions that are peaked at \( |\cos \theta^*| \) close to 1. By contrast, models of new processes characteristically predict angular distributions that would be more isotropic than those of QCD. Discrepancies from the predicted QCD behaviour would be evidence for new physics. This analysis focuses on a study of dijet mass and angular distributions, which have been shown by previous studies \([1–9]\) to be sensitive to new processes. These dijet variables are well suited for searches employing early LHC data. The dijet mass analyses can be performed using data-driven background estimates, while the angular analyses can be designed to have reduced sensitivity to the systematic uncertainties associated with the jet energy scale (JES) and integrated luminosity.

Following the first ATLAS studies of massive dijet events with 0.3 pb\(^{-1}\) \([5]\) and 3.1 pb\(^{-1}\) \([6]\), the full 2010 data set has increased statistical power by more than an order of magnitude, and we have made several improvements to the analysis. A variety of models of new physics have been tested and the angular distributions have been analysed using a new technique that finely bins the data in dijet mass to maximize the sensitivity of the search to both resonant and non-resonant phenomena. We set limits on a number of models and provide cross section limits using a simplified Gaussian signal model to facilitate tests of other hypotheses that we have not considered.

Section 2 describes the kinematic variables we used in this search. Section 3 describes the detector and the data sample, as well as the common event selection criteria used in the studies reported here. Section 4 describes the theoretical models employed, including the procedures used to account for detector effects. Section 5 describes the search for resonance and threshold phenomena using the dijet invariant mass. Section 6 describes the studies employing the angular distributions as a function of the invariant mass of the dijet system. Section 7 summarizes our results.

2. Kinematics and angular distributions

This analysis is focused on those \( pp \) collisions that produce two high-energy jets recoiling back-to-back in the partonic CM frame to conserve momentum relative to the beamline. The dijet invariant mass, \( m_{jj} \), is defined as the mass of the two highest \( p_T \) jets in the event. The scattering angle \( \theta^* \) distribution for \( 2 \rightarrow 2 \) parton scattering is predicted by QCD in the parton CM frame, which is in practice moving along the beamline due to the different momentum fractions (Bjorken \( x \)) of one incoming parton relative to the other. The rapidity of each jet is therefore a natural variable for the study of these systems, \( y \equiv \frac{1}{2} \ln \left( \frac{E+p_z}{E-p_z} \right) \), where \( E \) is the jet energy and \( p_z \) is the \( z \)-component of the jet’s momentum\(^1\). The variable \( y \) transforms under a

\(^1\) The ATLAS coordinate system is a right-handed Cartesian system with the \( x \)-axis pointing to the centre of the LHC ring, the \( z \)-axis following the counter-clockwise beam direction and the \( y \)-axis directed upwards. The polar angle \( \theta \) refers to the \( z \)-axis, and \( \phi \) is the azimuthal angle about the \( z \)-axis. Pseudo-rapidity is defined as \( \eta \equiv -\ln \tan(\theta/2) \) and is a good approximation to rapidity as the particle mass approaches zero.

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Lorentz boost along the z-direction as $y \rightarrow y - y_B = y - \tanh^{-1}(\beta_B)$, where $\beta_B$ is the velocity of the boosted frame, and $y_B$ is its rapidity boost.

We use the $m_{jj}$ spectrum as a primary tool to search for new particles that would be observed as resonances. The $m_{jj}$ spectrum is also sensitive to other phenomena, such as threshold enhancements or the onset of new interactions at multi-TeV mass scales in our current data sample. We bin the data in $m_{jj}$ choosing bin-widths that are consistent with the detector resolution as a function of mass so that binning effects do not limit our search sensitivity.

We employ the dijet angular variable $\chi$ derived from the rapidities of the two highest $p_T$ jets, $y_1$ and $y_2$. For a given scattering angle $\theta^*$, the corresponding rapidity in the parton CM frame (in the massless particle limit) is $y^* = \frac{1}{2} \ln(\frac{1+\cos\theta^*}{1-\cos\theta^*})$. We determine $y^*$ and $y_B$ from the rapidities of the two jets using $y^* = \frac{1}{2}(y_1 - y_2)$ and $y_B = \frac{1}{2}(y_1 + y_2)$. The variable $y^*$ is used to determine the partonic CM angle $\theta^*$ and to define $\chi \equiv \exp(|y_1 - y_2|) = \exp(2|y^*|)$. As noted in previous studies, the utility of the $\chi$ variable arises because the $\chi$ distributions associated with final states produced via QCD interactions are relatively flat compared with the distributions associated with new particles or interactions that typically peak at low values of $\chi$.

In a previous dijet angular distributions analysis \[2\], a single measure of isotropy based on $y^*$ intervals was introduced. This measure, $F_\chi$, is the fraction of dijets produced centrally versus the total number of observed dijets for a specified dijet mass range. We extend this to a measure that is finely binned in dijet mass intervals:

$$F_\chi \left( \left[m_{jj}^{\min} + m_{jj}^{\max} \right]/2 \right) = \frac{N_{\text{events}}(|y^*| < 0.6, m_{jj}^{\min}, m_{jj}^{\max})}{N_{\text{events}}(|y^*| < 1.7, m_{jj}^{\min}, m_{jj}^{\max})},$$

(1)

where $N_{\text{events}}$ is the number of candidate events within the $y^*$ interval and in the specified $m_{jj}$ range. The interval $|y^*| < 0.6$ defines the central region where we expect to be most sensitive to new physics and corresponds to the angular region $\chi < 3.32$, while $|y^*| < 1.7$ extends the angular range to $\chi < 30.0$, where QCD processes dominate. This new observable, $F_\chi(m_{jj})$, is defined using the same fine $m_{jj}$ binning used in analysis of the $m_{jj}$ spectrum. We also employ the variable $F_\chi$ to denote the ratio in equation (1) for dijet masses above 2 TeV. Our studies have shown that the $F_\chi(m_{jj})$ distribution is sensitive to mass-dependent changes in the rate of centrally produced dijets.

Jets are reconstructed using the infrared-safe anti-$k_t$ jet clustering algorithm \[9, 10\] with the distance parameter $R = 0.6$. The inputs to this algorithm are clusters of calorimeter cells defined by energy depositions significantly above the measured noise. Jet four-momenta are constructed by the vectorial addition of cell clusters, treating each cluster as an $(E, \vec{p})$ four-vector with zero mass. The jet four-momenta are then corrected as a function of $\eta$ and $p_T$ for various effects, the largest of which are the hadronic shower response and detector material distributions. This is done using a calibration scheme based on Monte Carlo (MC) studies including full detector simulation and validated with extensive test-beam studies \[12\] and collision data \[13–15\].

The measured distributions include corrections for the JES but are not unfolded to account for resolution effects. These distributions are compared to theoretical predictions processed through a full detector simulation software.
3. The ATLAS detector and event selection

3.1. The detector and trigger requirements

The ATLAS detector [16] is instrumented over almost the entire solid angle around the $pp$ collision point with layers of tracking detectors, calorimeters and muon chambers. Jet measurements are made using a finely segmented calorimeter system designed to efficiently detect the high-energy jets that are the focus of the study.

The electromagnetic (EM) calorimeter consists of an accordion-shaped lead absorber over the region $|\eta| < 3.2$, using liquid argon (LAr) as the active medium to measure the energy and geometry of the showers arising from jets. The measurement of hadronic energy flow in the range $|\eta| < 1.7$ is complemented by a sampling calorimeter made of steel and scintillating tiles. In the end-cap region $1.5 < |\eta| < 3.2$, hadronic calorimeters consisting of a steel absorber and a LAr active medium match the outer $|\eta|$ limits of the EM calorimeters. To complete the $\eta$ coverage to $|\eta| < 4.9$, the LAr forward calorimeters provide both EM and hadronic energy measurements. The calorimeter ($\eta, \phi$) granularities are $\sim 0.1 \times 0.1$ for the hadronic calorimeters up to $|\eta| < 2.5$ and then $0.2 \times 0.2$ up to $|\eta| < 4.9$. The EM calorimeters feature a finer readout granularity varying by layer, with cells as small as $0.025 \times 0.025$ extending over $|\eta| < 2.5$.

The inner tracking detector (ID) covers the range $|\eta| < 2.5$, and consists of a silicon pixel detector, a silicon microstrip detector (SCT) and, at $|\eta| < 2.0$, a transition radiation tracker (TRT). The ID is surrounded by a thin superconducting solenoid providing a 2T magnetic field. ATLAS has a three-level trigger system, with the first level trigger (L1) being custom-built hardware and the two higher level triggers (HLT) being realized in software. The triggers employed in this study selected events that had at least one large transverse energy deposition, with the transverse energy threshold varying over the period of the data-taking as the instantaneous luminosity of the LHC $pp$ collisions rose.

The primary first-level jet trigger used in the resonance analysis had an efficiency of $> 99\%$ for events with dijet masses $m_{jj} > 500$ GeV. This is illustrated in figure 1 where we show the measured trigger efficiency as a function of $m_{jj}$. After applying the full event selection from the resonance analysis (except the $m_{jj}$ cut) we compute the fraction of events passing a reference trigger which also pass our analysis trigger. The reference trigger is an inclusive jet trigger that was fully efficient for $p_T > 80$ GeV, while our event selection already requires $p_T > 150$ GeV to guarantee full efficiency of the reference trigger. Thus, we efficiently identify events for the dijet resonance analysis at $m_{jj} > 500$ GeV.

In order to have uniform acceptance for the angular distribution analysis, additional lower-$p_T$ triggers were used for different angular and mass regions. We verified that these triggers provided uniform acceptance as a function of $\chi$ for the dijet mass intervals in which they were employed. Because these lower threshold triggers sampled only a subset of the $pp$ collisions at higher instantaneous luminosity, the effective integrated luminosity collected for dijet masses between 500 and 800 GeV was $2.2 \, \text{pb}^{-1}$ and that between 800 and 1200 GeV was $9.6 \, \text{pb}^{-1}$ in the dijet angular distribution analysis. Above 1200 GeV, the same trigger is used for the resonance and angular analyses, and the full $36 \, \text{pb}^{-1}$ are used for both analyses.

3.2. Common event selection

Events are required to have at least one primary collision vertex defined by more than four charged-particle tracks. Events with at least two jets are retained if the highest $p_T$ jet (the
Figure 1. The efficiency of passing the primary first-level trigger as a function of the dijet invariant mass, $m_{jj}$. The uncertainties are statistical.

‘leading’ jet) satisfies $p_T^{j_1} > 60$ GeV and the next-to-leading jet satisfies $p_T^{j_2} > 30$ GeV. The asymmetric thresholds avoid suppression of events where a third jet has been radiated, while the 30 GeV threshold ensures that reconstruction is fully efficient for both leading jets. Events containing a poorly measured jet [17] with $p_T > 15$ GeV are vetoed to avoid cases where such a jet would cause incorrect identification of the two leading jets. This criterion rejects less than 0.6% of the events. The two leading jets are required to satisfy quality criteria that ensure that they arise from in-time energy deposition.

Further requirements are made on the jets in order to optimize the analysis of the dijet mass spectrum and angular distributions, as described in sections 5 and 6.

4. Theoretical models and Monte Carlo (MC) simulations

The MC signal samples used for the analysis have been produced with a variety of event generators. We have employed several of the most recent parton distribution functions (PDFs) so that we consistently match the orders of the matrix element calculations implemented in the different MC generators when we calculate QCD predictions, and to be conservative in the calculation of expected new physics signals (all new physics signals are calculated only to leading order (LO)).

4.1. Quantum chromodynamics (QCD) production

The angular distribution analyses required a prediction for the angular distribution arising from QCD production. MC samples modelling QCD dijet production were created with the *Pythia* 6.4.21 event generator [18] and the ATLAS MC09 parameter tune [19], using the [URL](http://www.njp.org/)
modified leading-order MRST2007 [20] PDF (MRST2007LO*). The generated events were passed through the detailed simulation of the ATLAS detector [21], which uses the Geant4 package [22] for the simulation of particle transport, interactions, and decays, to incorporate detector effects. The simulated events were then reconstructed in the same way as the data to produce predicted dijet mass and angular distributions that can be compared with the observed distributions.

Bin-by-bin correction factors ($K$-factors) have been applied to the angular distributions derived from MC calculations to account for next-to-leading order (NLO) contributions. These $K$-factors were derived from dedicated MC samples and are defined as the ratio $\text{NLO}_\text{ME}/\text{PYT}_\text{SHOW}$. The $\text{NLO}_\text{ME}$ sample was produced using matrix elements in NLOJET++ [23–25] with the NLO PDF from CTEQ6.6 [26]. The $\text{PYT}_\text{SHOW}$ sample was produced with the Pythia generator restricted to LO matrix elements and parton showering using the MRST2007LO* PDF.

The angular distributions generated with the full Pythia calculation include various non-perturbative effects such as multiple parton interactions and hadronization. The $K$-factors defined above were designed to retain these effects while adjusting for differences in the treatment of perturbative effects. We multiplied the full Pythia predictions of angular distributions by these binwise $K$-factors to obtain a reshaped spectrum that includes corrections originating from NLO matrix elements. Over the full range of $\chi$, the $K$-factors change the normalized angular distributions by up to 6%, with little variability from one mass bin to the other.

The QCD predictions used for comparison with the measured angular distributions in this paper are the product of the two-step procedure described above.

4.2. Models for new physics phenomena

MC signal events for a benchmark beyond-the-SM resonant process were generated using the excited-quark ($qg \rightarrow q^*$) production model [27, 28]. The excited quark $q^*$ was assumed to have spin-1/2 and quark-like couplings, relative to those of the SM $SU(2)$, $U(1)$ and $SU(3)$ gauge groups, of $f = f' = f_s = 1$, respectively. The compositeness scale ($\Lambda$) was set to the $q^*$ mass. Signal events were produced using the Pythia event generator with the MRST2007LO* PDF and with the renormalization and factorization scales set to the mean $p_T$ of the two leading jets. We also used the Pythia MC generator to decay the excited quarks to all possible SM final states, which are dominantly $qg$ but also $qW$, $qZ$ and $q\gamma$. The MC samples were produced using the ATLAS MC09 parameter tune.

We also considered two other models of new physics that generate resonant signatures: axigluons and Randall–Sundrum (RS) gravitons. The axigluon interaction [29–31] is described by the Lagrangian

$$\mathcal{L}_{\text{Aqq}} = g_{\text{QCD}} \bar{q} A^\mu_\alpha \frac{\lambda^\alpha}{2} \gamma^\mu \gamma_5 q.$$  \hspace{1cm} (2)

The parton-level events were generated using the CalcHEP MC package [32] with MRST2007LO* PDF. We used a Pythia MC calculation to model the production and decays of an RS graviton [33, 34] of a given mass. We performed this calculation with the dimensionless coupling $\kappa/M_{\text{Pl}} = 0.1$, where $M_{\text{Pl}}$ is the reduced Planck mass, to set limits comparable to other searches [7, 35].
For non-resonant new phenomena, we used a benchmark quark contact interaction (CI) as the beyond-the-SM process. This models the onset of kinematic properties that characterize quark compositeness: the hypothesis that quarks are composed of more fundamental particles. The model Lagrangian is a four-fermion contact interaction [36–38] whose effect appears below or near a characteristic energy scale $\Lambda$. While a number of contact terms are possible, the Lagrangian in standard use since 1984 [36] is the single (isoscalar) term:

$$\mathcal{L}_{qqqq}(\Lambda) = \frac{\xi g^2}{2\Lambda^2} \bar{\Psi}_q^L \gamma^\mu \Psi_q^L \bar{\Psi}_q^L \gamma^\mu \Psi_q^L,$$

where $g^2/4\pi = 1$ and the quark fields $\Psi_q^L$ are left-handed. The full Lagrangian used for hypothesis testing is then the sum of $\mathcal{L}_{qqqq}(\Lambda)$ and the QCD Lagrangian. The relative phase of these terms is controlled by the interference parameter, $\xi$, which is set for destructive interference ($\xi = +1$) in the current analysis. Previous analyses [3] showed that the choice of constructive ($\xi = -1$) or destructive ($\xi = +1$) interference changed exclusion limits by $\sim 1\%$.

MC samples were created by a Pythia 6.4.21 calculation using this Lagrangian, with each sample corresponding to a distinct value of $\Lambda$. As another example of non-resonant new physics phenomena, we considered quantum black holes (QBH) [39, 40], by which we mean any quantum gravitational effect that produces events containing dijets. We used the BlackMax black hole event generator [41] to simulate the simplest two-body final state scenario describing the production and decay of a QBH for a given fundamental quantum gravity scale $M_D$. These would appear as a threshold effect that also depends on the number of extra space–time dimensions.

Previous ATLAS jet studies [42] have shown that the use of different event generators and models for non-perturbative behaviour has a negligible effect on the observables in the kinematic region we are studying. All of the MC signal events were modelled with the full ATLAS detector simulation.

5. Search for dijet resonances

We make a number of additional selection requirements on the candidate events to optimize the search for effects in the dijet mass distribution. Each event is required to have its two highest-$p_T$ jets satisfy $|\eta_j| < 2.5$ with $|\Delta\eta_{jj}| < 1.3$. In addition, the leading jet must satisfy $p_T^1 > 150$ GeV and $m_{jj}$ must be greater than 500 GeV. These criteria have been shown, based on studies of expected signals and QCD background, to efficiently optimize the signal-to-background in the sample. There are 98 651 events meeting these criteria.

5.1. The dijet mass distribution

In order to develop a data-driven model of the QCD background shape, a smooth functional form

$$f(x) = p_1(1 - x)^{p_2}x^{p_3+p_4\ln x},$$

5.3. In the resulting mass spectrum and fitted background, indicating that the observed spectrum is consistent with a rapidly falling, smooth distribution. The bin widths have been chosen to be consistent with the dijet mass resolution,
Figure 2. The observed (D) dijet mass distribution (filled points) fitted using a binned QCD background (B) distribution described by equation (4) (histogram). The predicted $q^*$ signals normalized to 36 pb$^{-1}$ for excited-quark masses of 1000, 1700 and 2500 GeV are overlaid. The bin-by-bin significance of the data–background difference is shown in the lower panel.

Increasing from $\sim 50$ to $\sim 200$ GeV for dijet masses from 600 to 3500 GeV, respectively. The $p$-value of the fit to the data, calculated using the chi-squared test determined from pseudo-experiments as a goodness-of-fit statistic, is 0.88. Although this $p$-value suggests that there is no significant overall disagreement, we use a more sensitive statistical test, the BumpHunter algorithm [43, 44], to establish the presence or absence of a resonance.

In its implementation in this analysis, the BumpHunter algorithm searches for the signal window with the most significant excess of events above the background, requiring insignificant discrepancy (Poisson counting $p$-value > $10^{-3}$) in both the adjacent sidebands. Starting with a two-bin window, the algorithm increases the signal window and shifts its location until all possible bin ranges, up to half the mass range spanned by the data, have been tested. The most significant departure from the smooth spectrum, defined by the set of bins that have the smallest probability of arising from a background fluctuation assuming Poisson statistics, is therefore identified. The algorithm accounts for the ‘trials factor’ to assess the significance (i.e., $p$-value) of its finding. It does this by performing a series of pseudo-experiments to determine the probability that random fluctuations in the background-only hypothesis would create an excess as significant as the observed one anywhere in the spectrum. The background to which the data are compared is obtained from the aforementioned fit, excluding the region with the biggest local excess of data in cases where the $\chi^2$ test yields a $p$-value less than 0.01. Although this is not the case for the actual data, it can happen in some of the pseudo-experiments that are used to determine the $p$-value. The reason for this exclusion is to prevent potential new physics signal from biasing the background.
The most significant discrepancy identified by the BumpHunter algorithm is a three-bin excess in the dijet mass interval 995–1253 GeV. The $p$-value, of observing an excess at least as large as this assuming a background-only hypothesis, is 0.39. We therefore conclude that there is no evidence for a resonance signal in the $m_{jj}$ spectrum and proceed to set limits on various models.

5.2. Exclusion limits using the dijet mass

We set Bayesian credibility intervals by defining a posterior probability density from the likelihood function for the observed mass spectrum, obtained by a fit to the background functional form and a signal shape derived from MC calculations. A prior constant in the possible signal strength is assumed. The posterior probability is then integrated to determine the 95% credibility level (CL) for a given range of models, usually parameterized by the mass of the resonance. A Bayesian approach is employed for setting limits using the dijet mass distribution as it simplifies the treatment of systematic uncertainties.

The systematic uncertainties affecting this analysis arise from instrumental effects, such as the JES and resolution (JER) uncertainties, the uncertainty on the integrated luminosity and the uncertainties arising from the background parameterization. Extensive studies of the performance of the detector using both data and MC modelling have resulted in a JES uncertainty ranging from 3.2 to 5.7% in the current data sample [15]. The systematic uncertainty in the integrated luminosity is 11% [45]. The uncertainties in the background parameterization are taken from the fit results discussed earlier and range from 3% at 600 GeV to ~40% at 3500 GeV. These uncertainties are incorporated into the analysis by varying all the sources according to Gaussian probability distributions and convolving these with the Bayesian posterior probability distribution. Credibility intervals are then calculated numerically from the resulting convolutions.

Uncertainties in the signal models come primarily from our choice of PDFs and the tune for the Pythia MC, which provides the best match of observed data with the predictions with that choice of PDF. Our default choice of PDFs for the dijet mass analysis is MRST2007LO* [20] with the MC09 tune [19]. Limits are quoted also using CTEQ6L1 and CTEQ5L PDF sets, which provide an alternative PDF parameterization and allow comparisons with previous results [3], respectively. For the $q^*$ limit analysis, we also vary the renormalization and factorization scales in the Pythia calculation by factors of one-half and two and find that the observed limit varies by ~0.1 TeV.

5.3. Limits on excited quark production

The particular signal hypothesis used to set limits on excited quarks ($q^*$) has been implemented using the Pythia MC generator, with fixed parameters to specify the excited quark mass, $m_{q^*}$, and its decay modes, as discussed in section 4. Each choice of mass constitutes a specific signal template, and a high-statistics set of MC events was created and fully simulated for each choice of $m_{q^*}$. The acceptance, $A$, of our selection requirements ranges from 49 to 58% for $m_{q^*}$ from 600 to 3000 GeV, respectively. The loss of acceptance comes mainly from the pseudorapidity requirements, which ensure that the candidate events have a high signal-to-background ratio.

In figure 3 the resulting 95% CL limits on $\sigma \cdot A$ for excited quark production are shown as a function of the excited quark mass, where $\sigma$ is the cross section for production of resonance.
Table 1. The 95% CL lower limits on the allowed \( q^* \) mass obtained using different tunes and PDF sets. The MC09' tune is identical to MC09 except for the PYTHIA parameter PARP(82) = 2.1 and the use of the CTEQ6L1 PDF set.

<table>
<thead>
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<th>Expected limit (TeV)</th>
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<td>2.27</td>
</tr>
<tr>
<td>MC09'</td>
<td>CTEQ6L1 [46]</td>
<td>2.06</td>
<td>2.19</td>
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<tr>
<td>Perugia0</td>
<td>CTEQ5L [48]</td>
<td>2.14</td>
<td>2.26</td>
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Figure 3. The 95% CL upper limits on the cross section times acceptance for a resonance decaying to dijets taking into account both statistical and systematic uncertainties (points and solid line) compared to an axigluon model and to a \( q^* \) model with three alternative MC tunes. We also show the expected limit (dotted line) and the 68 and 95% contours of the expected limit (bands).

The sensitivity of the resulting limit to the choice of PDFs was modest, as shown in table 1 where the observed and expected mass limits are compared for several other models. In all cases, the mass limits vary by less than 0.1 TeV. The inclusion of systematic uncertainties results in modest reductions in the limit, illustrating that the limit setting is dominated by statistical uncertainties.

\( \mathcal{A} \) is the acceptance for the dijet final state. The expected limit is also shown, based on the statistics of the sample and assuming a background-only hypothesis. We see that the observed and expected limits are in reasonable agreement with each other, strengthening our earlier conclusion that there is no evidence of a signal above the smooth background. Comparing the observed limit with the predicted \( q^* \) cross section times acceptance, we exclude at 95% CL \( q^* \) masses in the interval 0.60 < \( m_{q^*} \) < 2.15 TeV. The expected limit excludes \( m_{q^*} < 2.07 \) TeV.
Table 2. The 95% CL lower limits on the allowed quantum gravity scale for various numbers of extra dimensions.

<table>
<thead>
<tr>
<th>Number of extra dimensions</th>
<th>Observed $M_D$ limit (TeV)</th>
<th>Expected $M_D$ limit (TeV)</th>
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</table>

5.4. Limits on axigluon production

We set limits on axigluon production using the same procedure followed for the $q^*$ analysis, creating templates for the signal using the axigluon model described in section 4 and full detector simulation. There are large non-resonant contributions to the cross section at low dijet mass, so we require at the parton-level that the axigluon invariant mass be between 0.7 and 1.3 times the nominal mass of the resonance. Having made this requirement, we note that the axigluon and $q^*$ signal templates result in very similar limits. So for convenience we use the $q^*$ templates in setting cross section limits on axigluon production.

The resulting limits are shown in figure 3. Using the MRST2007LO* PDFs, we exclude at 95% CL axigluon masses in the interval $0.60 < m < 2.10$ TeV. The expected limit is $m < 2.01$ TeV. If only statistical uncertainties are included, the limit rises by $\sim 0.2$ TeV, indicating that the systematic uncertainties are not dominant.

5.5. Limits on quantum black hole (QBH) production

We search for the production of QBHs as these are expected to produce low multiplicity decays with a significant contribution to dijet final states. Several scenarios are examined, with quantum gravity scales $M_D$ ranging from 0.75 TeV to 4.0 TeV and with the number of extra dimensions, $n$, ranging from two to seven. The fully simulated MC events are used to create templates similar to the $q^*$ analysis. These QBH models produce threshold effects in $m_{jj}$ with long tails to higher $m_{jj}$ that compete with the QCD background. However, the cross section is very large just above the threshold and so it is possible to extract limits given the resulting resonance-like signal shape.

The resulting limits are illustrated in figure 4, showing the observed and expected limits, as well as the predictions for QBH production assuming two, four and six extra dimensions. The observed lower limits on the quantum gravity scale, $M_D$, with and without systematic uncertainty, and the expected limit with and without systematic uncertainty, at 95% CL are summarized in table 2. Using CTEQ6.6 PDFs, we exclude at 95% CL quantum gravity scales in the interval $0.75 < M_D < 3.67$ TeV for the low-multiplicity QBHs with six extra dimensions. The expected limit is $M_D < 3.64$ TeV.

5.6. Limits on Randall–Sundrum (RS) graviton production

We search for the production of RS gravitons by creating dijet mass templates using the MC calculation described in section 4. In this case, the sensitivity of the search is reduced by the
The 95% CL upper limits on the cross section $\times$ acceptance versus the quantum gravity mass scale $M_D$ for a QBH model, taking into account both statistical and systematic uncertainties. The cross section $\times$ acceptance for QBH models with two, four and six extra dimensions is shown. The 68 and 95% CL contours of the expected limit are shown as the band.

The limits obtained for this hypothesis are illustrated in figure 5, showing the observed and expected limits, as well as the predictions for RS graviton production. It is not possible to exclude any RS graviton mass hypothesis, given the small expected signal rates and the relatively large QCD backgrounds. A limit on RS graviton models could be established with increased statistics, although more sophisticated strategies to improve signal-to-background may be necessary.

5.7. Simplified Gaussian model limits

We have used these data to set limits in a more model-independent way by employing as our signal template a Gaussian profile with means ranging from 600 GeV to 4000 GeV and with the width, $\sigma$, varying from 3 to 15% of the mean.

Systematic uncertainties are treated in the same manner as described previously, using pseudo-experiments to marginalize the posterior probabilities that depend on parameters that suffer from systematic uncertainty. However, given that the decay of the dijet final state has not been modelled, assuming only that the resulting dijet width is Gaussian in shape, we adjusted the treatment of the JES by modelling it as an uncertainty in the central value of the Gaussian signal.

The 95% CL limits are shown in table 3, expressed in terms of the number of events observed after all event selection criteria have been applied. We stress that these event limits...
are determined by assuming a Gaussian signal shape. Their variation as a function of mass and width reflects the statistical fluctuations of data in the binned $m_{jj}$ distribution used to set them.

These limits can be employed by computing for a given model the acceptance $A$ using a standard MC calculation. The jet $p_T$ and $\eta$ requirements should first be applied to determine the expected signal shape in $m_{jj}$. Since a Gaussian signal shape has been assumed in determining the limits, we recommend removing any long tails in $m_{jj}$ (a $\pm 20\%$ mass window is recommended). The fraction of MC events surviving these requirements is an estimate of the acceptance, and can be used to calculate the expected event yield given a cross section for the process and assuming a sample size of $36 \text{ pb}^{-1}$. This event yield can then be compared with the limit in table 3, matching the expected signal mean and width to the appropriate entry in the table.

6. Angular distribution analyses

For all angular distribution analyses, the common event selection criteria described in section 3 are applied, including the transverse momentum requirements on the two leading jets: $p_{T1} > 60 \text{ GeV}$ and $p_{T2} > 30 \text{ GeV}$. Additionally, $\chi$ distributions are accumulated only for events that satisfy $|y_B| < 1.10$ and $|y^*| < 1.70$. The $|y^*|$ criterion determines the maximum $\chi$ of 30 for this analysis. These two criteria limit the rapidity range of both jets to $|y_1, 2| < 2.8$ and define a region within the space of accessible $y_1$ and $y_2$ with full and uniform acceptance in $\chi$ at $m_{jj} > 500 \text{ GeV}$. These kinematic cuts have been optimized by MC studies of QCD and new physics signal samples to ensure high acceptance for all dijet masses.

Detector resolution effects smear the $\chi$ distributions, causing events to migrate between neighbouring bins. This effect is reduced by choosing the $\chi$ bins to match the natural segmentation of the calorimeter, making them intervals of constant $\Delta y$ for these high-$p_T$ dijet

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**Figure 5.** The 95% CL upper limits on the cross section $\times$ acceptance for an RS graviton, taking into account both statistical and systematic uncertainties. The 68 and 95% CL contours of the expected limit are shown as the band.
Table 3. The 95% CL upper limits on the number of observed signal events for Gaussian reconstructed $m_{jj}$ distributions. The effects of systematic uncertainties due to the luminosity, the background fit and the JES have been included. We present the signal widths as $\sigma/m$.

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events. The $F_\chi$ and $F_{\chi}(m_{jj})$ variables are even less sensitive to migration effects, given that they depend on separation of the data sample into only two $\chi$ intervals.

6.1. Systematic and statistical uncertainties

Dijet angular distribution analyses have a reduced sensitivity to the JES and JER uncertainties compared to other dijet measurements because data and theoretical distributions are normalized to unit area for each mass bin in all cases. Nevertheless, the JES still represents the dominant systematic uncertainty in the current studies.

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As described in a previous publication [6], our dijet angular analyses use pseudo-experiments to convolve statistical, systematic and theoretical uncertainties. The primary sources of theoretical uncertainty are NLO QCD renormalization ($\mu_R$) and factorization scales ($\mu_F$) and PDF uncertainties. The former are varied by a factor of two, independently, while the PDF errors are sampled from a Gaussian distribution determined using CTEQ6.6 (NLO) PDF error sets. The resulting bin-wise uncertainties for normalized $\chi$ distributions are typically up to 3% for the combined NLO QCD scales and 1% for the PDF uncertainties. These convolved experimental and theoretical uncertainties are calculated for all MC angular distributions (both QCD and new physics samples). These statistical ensembles are used for estimating $p$-values when comparing QCD predictions to data and for parameter determination when setting limits.

6.2. Observed $\chi$ and $F_\chi(m_{jj})$ distributions

The analysis method used in the first ATLAS publication on this topic [6] is revisited here for the full 2010 data sample. The $\chi$ distributions are shown in figure 6 for several relatively large $m_{jj}$ bins, defined by the bin boundaries of 520, 800, 1200, 1600 and 2000 GeV. There are 71 402 events in the sample, ranging from 42 116 events in the lowest mass bin to 212 events with $m_{jj} > 2000$ GeV. These bins were chosen to ensure sufficient statistics in each mass bin. This is most critical for the highest mass bin—the focal point for new physics searches. The $\chi$ distributions are compared in the figure to the predictions from QCD MC models and the
signal that would be seen in one particular new physics model, a QBH scenario with a quantum gravity mass scale of 3 TeV and six extra dimensions.

The data appear to be consistent with the QCD predictions, which include systematic uncertainties. To verify this, a binned likelihood is calculated for each distribution assuming that the sample consists only of QCD dijet production. The expected distribution of this likelihood is then calculated using pseudo-experiments drawn from the QCD MC sample and convolved with the systematic uncertainties as discussed above. The $p$-values for the observed likelihood values, from the lowest to highest mass bins, are 0.44, 0.33, 0.64, 0.89 and 0.44, respectively, confirming that the SM QCD hypothesis is consistent with the data.

We compute the $F\chi(m_{jj})$ observable, introduced in section 2, using the same mass binning employed in the dijet resonance searches. The observed $F\chi(m_{jj})$ data are shown in figure 7 and are compared to the QCD predictions, which include systematic uncertainties. We also show the expected behaviour of $F\chi(m_{jj})$ if a contact interaction with the compositeness scale $\Lambda = 5.0$ TeV were present. Statistical analyses using $F\chi(m_{jj})$ use mass bins starting at 1253 GeV to be most sensitive to the high dijet mass region. Assuming only QCD processes and including systematic uncertainties, the $p$-value for the observed binned likelihood is 0.28, indicating that these data are consistent with QCD predictions.

In the absence of any evidence for signals associated with new physics phenomena, these distributions are used to set 95% CL exclusion limits on a number of new physics hypotheses.

6.3. Exclusion limits from likelihood ratios

Most of the dijet angular distribution analyses described below use likelihood ratios to compare different hypotheses and parameter estimation. Confidence level limits are set using the
frequentist CL$_{s+b}$ approach [49]. As an example, for the $F_x(m_{jj})$ distributions the variable $Q$ is defined as follows:

$$Q = -2[\ln L(F_x(m_{jj})|H0) - \ln L(F_x(m_{jj})|H1)],$$

where $H0$ is the null hypothesis (QCD only), $H1$ is a specific hypothesis for new physics with fixed parameters and $L(F_x(m_{jj})|H)$ is the binned likelihood for the $F_x(m_{jj})$ distribution assuming $H$ as the hypothesis. Pseudo-experiments are used to determine the expected distribution for $Q$ for specific hypotheses. The new physics hypothesis is then varied to calculate a Neyman confidence level.

6.4. Limits on quark contact interactions

The $F_x(m_{jj})$ variable is used for the first time in this paper to set limits on quark contact interactions (CI), as described in section 4. MC samples of QCD production modified by a CI are created for values of $\Lambda$ ranging from 0.50 to 8.0 TeV.

For the pure QCD sample (corresponding to $\Lambda = \infty$), the $F_x(m_{jj})$ distribution is fitted to a second order polynomial. For MC samples with finite $\Lambda$, the distributions are fitted, as a function of $m_{jj}$, to the second order polynomial plus a Fermi function, which is a good representation of the onset curve for CIs. QCD $K$-factors from section 4 are applied to the QCD-only component of the spectra before calculating $F_x(m_{jj})$. This is done through an approximation that neglects possible NLO corrections in the interference term between the QCD matrix element and the CI term. The issue of NLO corrections to contact terms has been independently identified elsewhere [50].

The $F_x(m_{jj})$ event sample is fitted in each $m_{jj}$ bin of the distribution as a function of $1/\Lambda^2$, creating a predicted $F_x(m_{jj})$ surface as a function of $m_{jj}$ and $\Lambda$. This surface enables integration in $m_{jj}$ versus $\Lambda$ for continuous values of $\Lambda$. Using this surface, the 95% CL limit on $\Lambda$ is determined using the log-likelihood ratio defined in equation (5). The resulting 95% CL quantile is shown in figure 8.

Figure 8 also shows the expected value of $Q$ for various choices of $\Lambda$ as well as the expected 95% CL limit and its 68% contour interval.

The observed exclusion limit is found from the point where the 95% quantile (dotted line) crosses the median value of the distribution of $Q$ values for the QCD prediction (dashed line). This occurs at $\Lambda = 9.5$ TeV. The expected limit is $\Lambda = 5.7$ TeV. The observed result is significantly above the expected limit because the data have fewer centrally produced, high mass dijet events than expected from QCD alone, as can be seen in figure 7 where the observed values of $F_x(m_{jj})$ fall below the QCD prediction for dijet masses around 1.6 TeV and above 2.2 TeV. These data are statistically compatible with QCD, as evidenced by the $p$-value of the binned likelihood. The expected probability that a limit at least as strong as this would be observed is $\sim 8\%$.

As a cross-check, a Bayesian analysis of $F_x(m_{jj})$ has been performed, assuming a prior that is constant in $1/\Lambda^2$. This analysis sets a 95% credibility level of $\Lambda > 6.7$ TeV. The expected limit from this Bayesian analysis is 5.7 TeV, comparable to the CL$_{s+b}$ expected limit. While the observed limit from CL$_{s+b}$ analysis is significantly higher than the Bayesian results, we have no basis on which to exclude the CL$_{s+b}$ result a posteriori.

As an additional cross-check, the earlier $F_x$ analysis of the $dN/d\chi$ distributions, coarsely binned in $m_{jj}$ [6], has been repeated. With the larger data sample and higher threshold on the...
Figure 8. The log-likelihood ratio defined by the $F_{\chi}(m_{jj})$ distribution versus the strength of the contact interaction, $\Lambda$. The contact interaction limit is set by comparing the measured log-likelihood ratio to that expected for a given value of $\Lambda$.

highest $m_{jj}$ bin (2 TeV), the observed and expected limits are $\Lambda > 6.8$ TeV and $\Lambda > 5.2$ TeV, respectively. As anticipated, these limits are not as strong as those arising from the $F_{\chi}(m_{jj})$ analysis because of the coarser $m_{jj}$ binning.

Finally, an analysis was performed to see whether a more sensitive measure could be created by setting limits based on all 11 bins of the highest mass ($m_{jj} > 2$ TeV) $\chi$ distribution, instead of the two intervals used in the $F_{\chi}$ analysis. In this method, for each bin the same interpolating function used in the $F_{\chi}(m_{jj})$ analysis is fitted to the bin contents resulting from all QCD + CI MC samples, yielding the CI onset curve. Limits are set using the same log-likelihood ratio and pseudo-experiment methods employed in the $F_{\chi}(m_{jj})$ analysis. The observed 95% CL limit is $\Lambda > 6.6$ TeV. For the current data sample, the expected limit is 5.4 TeV. Since the expected limit exceeds that from the $F_{\chi}$ analysis, this method shows promise for future analyses.

6.5. Limits on excited quark production

The $F_{\chi}(m_{jj})$ distributions are also used to set limits on excited quark production. As described earlier, the $q^*$ model depends only on the single parameter, $m_{q^*}$. Twelve simulated $q^*$ mass ($m_{q^*}$) samples in the range of 1.5–5.0 TeV are used for the analysis. Based on the assumption that interference of QCD with excited quark resonances is negligible, $q^*$ MC samples are scaled by their cross sections and added to the NLO QCD sample (which has been corrected using bin-wise $K$-factors). By analogy with the CI analysis above, a likelihood is constructed by comparing the expected and observed $F_{\chi}(m_{jj})$ distributions for each value of $m_{q^*}$. We then form a likelihood ratio with respect to the QCD-only hypothesis and use this to set confidence intervals on the production of a $q^*$.

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Figure 9. The 95% CL limits on the excited quark model using the logarithm of the likelihood ratios obtained from the $F_\chi(m_{jj})$ distribution. The expected 68% interval for the expected limits are shown by the band.

Figure 9 illustrates the limit setting procedure for the $q^*$ model. The observed exclusion limit is found from the point where the 95% quantile (dotted line) crosses the measured value of $Q$ (dashed line). This occurs for $m_{q^*} = 2.64$ TeV. The expected limit, determined from the point where the QCD prediction (solid line) crosses the 95% quantile, is 2.12 TeV. The observed limit falls near the 68% ($\pm 1\sigma$) interval of the expected limit. The difference between observed and expected limits arises from the lower observed $F_\chi(m_{jj})$ values at dijet masses above 2.2 TeV.

This result can be compared to the limits obtained from the dijet resonance analysis, which sets observed exclusion limits on $q^*$ masses of 2.15 TeV.

6.6. Limits on new physics for additive signals

For new physics signals that do not interfere significantly with QCD, limit setting may be done in a more model-independent way. MC signal samples are simulated independently from QCD samples and, for a given choice of new physics model parameters, the two samples are added to create a combined MC sample for comparison with data. This is implemented by introducing a variable $\theta_{np}$ defined as

$$\theta_{np} = \frac{\sigma_{np} \times A_{np}}{\sigma_{QCD} \times A_{QCD}},$$

where $\sigma$ and $A$ are the cross section and acceptance for the given process, and ‘np’ refers to the new physics process. This variable represents the contribution of signal events in terms of cross section times acceptance relative to the QCD background. The acceptance factors are determined by MC calculations.
6.7. Limits on QBH production

The model of QBH production [39, 40], introduced in section 4 and used to set limits on these phenomena in the dijet resonance analysis, is again employed here to search for QBH production using the dijet angular distributions. The $\theta_{np}$-parameter limit-setting method, sensitive to $\sigma_{\text{QBH}} \times A_{\text{QBH}}$, is used in this analysis since the QBH production model does not include interference with QCD.

MC samples are created corresponding to discrete values of the QBH quantum gravity mass scale $M_D$ ranging from 2.0 to 4.0 TeV and for two to seven extra dimensions ($n$), and are used to determine the acceptance $A_{\text{QBH}}$. The acceptance is found to vary from 58 to 89% as $M_D$ is varied from 2.0 to 4.0 TeV, for the case of six extra dimensions. These studies have shown that the signal acceptance for the model considered here varies only slightly with the model parameter $n$. Thus, $A_{\text{QBH}}$ determined from a full simulation of the sample with $n = 6$ is applied to a limit analysis for other choices of $n$, which have different cross sections.

The MC events with dijet masses greater than 2.0 TeV are binned in $\chi$ with the same bin boundaries as those used in figure 6. Pseudo-experiments are used to incorporate the JES uncertainty into the predicted $\chi$ distributions. In each $\chi$ bin, a linear fit is made for $dN/d\chi$ versus $\theta_{np}$, creating a family of lines that define a $dN/d\chi$ surface in $\theta_{np}$ versus $\chi$. Scale and PDF uncertainties, and the uncertainty in the JES correlation between the two jets, are incorporated into this surface using pseudo-experiments, and a value of $F_\chi$ is calculated from each distribution. The expected distributions of $F_\chi$ values are obtained for a range of QBH hypotheses and QCD processes alone. Additional pseudo-experiments are used to model the finite statistics of the high-$m_{jj}$ event sample. The 95% CL exclusion limit on $F_\chi$, as a function of $\theta_{np}$, is derived from the resulting likelihood distributions of $F_\chi$.

Figure 10 illustrates the $\theta_{np}$ parameter limit-setting procedure for the case $n = 6$. The observed exclusion limit is found from the point where the 95% CL contour (dotted line) crosses...
Figure 11. The cross section × acceptance for QBHs as a function of $M_D$ for two, four and six extra dimensions. The measured and expected limits are shown in the solid and dashed lines.

The measured value of $F_\chi = 0.052$ (dashed line), which occurs at $\theta_{np} = 0.020$. The expected limit, determined from the point where the QCD prediction, 0.071 (solid line), crosses the 95% CL contour, is at 0.075. The observed limit falls just outside the 68% (±1σ) interval of the expected limit. These limits on $\theta_{np}$ are translated into limits on $\sigma \times A$ using the QCD cross section and the acceptance for fully simulated dijets, $\sigma_{QCD} \times A_{QCD} = 7.21$ pb, resulting in an observed 95% CL upper limit $\sigma_{QBH} \times A_{QBH} < 0.15$ pb.

Figure 11 shows the $\sigma_{QBH} \times A_{QBH}$ versus $M_D$ curves for two, four and six extra dimensions. The measured and expected limits for $\sigma_{QBH} \times A_{QBH}$ are plotted as horizontal lines. The crossing points of these lines with the $n$ versus $M_D$ curve yield expected and observed exclusion limits for the QBH model studied here. The 95% CL lower limit on the quantum gravity mass scale is 3.69 TeV for six extra dimensions. The expected limit is 3.37 TeV. The limits for all extra dimensions studied here, $n = 2–7$, are listed in table 4.

The limit for $\sigma_{QBH} \times A_{QBH}$ may also be applied to any new physics model that satisfies the following criteria: (1) the $F_\chi$ of $np$ signal-only event samples should be roughly independent of $m_{jj}$, as is the case for $q^*\bar{q}$, QBH and CIs; and (2) this $F_\chi$ should be close to the value of $F_\chi$ for the current QBH study [0.58]. It is not necessary that the $m_{jj}$ spectrum be similar or that the QCD + $np$ sample have the same $F_\chi$.

It should also be noted that the results from this $\theta_{np}$ parameter analysis are in agreement with the expected and observed limits obtained for the same QBH model in the dijet resonance analysis. These two analyses are focusing on complementary variables in the two-dimensional space of $m_{jj}$ and $\chi$ yet arrive at similar limits.

A cross-check of these results is made by extracting a QBH limit using the $F_\chi(m_{jj})$ distribution for the case of six extra dimensions. Signal and background samples are created by combining the QBH signals for various $M_D$’s with the QCD background sample corrected.
Table 4. The 95% CL exclusion limits on $M_D$ for various choices of extra dimensions for the QBH model determined by the $\theta_{np}$ parameter analysis for at $m_{jj} > 2.0$ TeV.

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by $K$-factors. The $F_\chi(m_{jj})$ distribution is then fitted in each $m_{jj}$ bin as a function of $1/M_D^2$ using the same interpolating function employed in $F_\chi(m_{jj})$ CI analysis. The likelihood ratio construction and limit setting procedures used in the CI analysis are also applied in this study, resulting in observed and expected 95% CL limits for $M_D$ of 3.78 and 3.49 TeV, respectively. A further cross-check is performed using the 11-bin $\chi$ analysis to set limits on a QBH for the case of six extra dimensions. This study yields an observed 95% CL limit of $M_D > 3.49$ TeV and an expected limit of $M_D > 3.36$ TeV.

The expected and observed limits resulting from these four studies are summarized with the results of other analyses in table 5. The strongest expected limits on QBH production come from the dijet resonance analysis, but the angular analyses are in close agreement, yielding limits within 0.3 TeV of each other for the QBH hypothesis under study.

7. Conclusion

Dijet mass and angular distributions have been measured by the ATLAS experiment over a large angular range and spanning dijet masses up to $\approx 3.5$ TeV using 36 pb$^{-1}$ of 7 TeV $pp$ collision data. The angular distributions are in good agreement with QCD predictions and we find no evidence for new phenomena. Our analysis, employing both the dijet mass and the dijet angular distributions, places the most stringent limits on contact interactions, resonances and threshold phenomena to date.

In table 5, the constraints on specific models of new physics that would contribute to dijet final states are summarized.

We quote as the primary results the limits using the technique with the most stringent expected limit. Therefore, we exclude at 95% CL excited quarks with masses in the interval $0.60 < m_q^* < 2.64$ TeV, axigluons with masses between 0.60 TeV and 2.10 TeV, and QBHs with $0.75 < M_D < 3.67$ TeV assuming six extra dimensions.

We also exclude at 95% CL quark contact interactions with a scale $\Lambda < 9.5$ TeV. As noted earlier, the observed limit is significantly above the expected limit of 5.7 TeV for this data sample, and above the limits from an alternative calculation using Bayesian statistics. However, we quote this result since the statistical approach is a standard procedure that was chosen a priori.
Table 5. The 95% CL lower limits on the masses and energy scales of the models examined in this study. We have included systematic uncertainties in the upper limits using the techniques described in the text. The result with the highest expected limit is shown in boldface and is our quoted result.

<table>
<thead>
<tr>
<th>Model and analysis strategy</th>
<th>Expected</th>
<th>Observed</th>
</tr>
</thead>
<tbody>
<tr>
<td>Excited quark $q^*$</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Resonance in $m_{jj}$</td>
<td>2.07</td>
<td>2.15</td>
</tr>
<tr>
<td>$F_\gamma(m_{jj})$</td>
<td><strong>2.12</strong></td>
<td><strong>2.64</strong></td>
</tr>
<tr>
<td>QBH for $n = 6$</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Resonance in $m_{jj}$</td>
<td><strong>3.64</strong></td>
<td><strong>3.67</strong></td>
</tr>
<tr>
<td>$F_\gamma(m_{jj})$</td>
<td>3.49</td>
<td>3.78</td>
</tr>
<tr>
<td>$\theta_{np}$ parameter for $m_{jj} &gt; 2$TeV</td>
<td>3.37</td>
<td>3.69</td>
</tr>
<tr>
<td>11-bin $\chi$ distribution for $m_{jj} &gt; 2$TeV</td>
<td>3.36</td>
<td>3.49</td>
</tr>
<tr>
<td>Axigluon</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Resonance in $m_{jj}$</td>
<td><strong>2.01</strong></td>
<td><strong>2.10</strong></td>
</tr>
<tr>
<td>Contact interaction $\Lambda$</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$F_\gamma(m_{jj})$</td>
<td>5.7</td>
<td>9.5</td>
</tr>
<tr>
<td>$F_\gamma$ for $m_{jj} &gt; 2$TeV</td>
<td>5.2</td>
<td>6.8</td>
</tr>
<tr>
<td>11-bin $\chi$ distribution for $m_{jj} &gt; 2$TeV</td>
<td>5.4</td>
<td>6.6</td>
</tr>
</tbody>
</table>

In a number of cases, searches for the same phenomenon have been performed using dijet mass distributions, dijet angular distributions or both. We are able to set comparable limits using these complementary techniques, while at the same time searching for evidence of narrow resonances, threshold effects and enhancements in angular distributions that depend on the dijet invariant mass.

This combined analysis is a sensitive probe into new physics that is expected to emerge at the TeV scale. With increased integrated luminosity and continued improvements to analysis techniques and models, we expect to increase the ATLAS discovery reach for new phenomena that affect dijet final states.

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