Identification of boosted, hadronically decaying W bosons and comparisons with ATLAS data taken at $\sqrt{s} = 8$ TeV

ATLAS Collaboration

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Identification of boosted, hadronically decaying $W$ bosons and comparisons with ATLAS data taken at $\sqrt{s} = 8$ TeV

ATLAS Collaboration*
CERN, 1211 Geneva 23, Switzerland

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Abstract This paper reports a detailed study of techniques for identifying boosted, hadronically decaying $W$ bosons using 20.3 fb$^{-1}$ of proton–proton collision data collected by the ATLAS detector at the LHC at a centre-of-mass energy $\sqrt{s} = 8$ TeV. A range of techniques for optimising the signal jet mass resolution are combined with various jet substructure variables. The results of these studies in Monte Carlo simulations show that a simple pairwise combination of groomed jet mass and one substructure variable can provide a 50% efficiency for identifying $W$ bosons with transverse momenta larger than 200 GeV while maintaining multijet background efficiencies of 2–4% for jets with the same transverse momentum. These signal and background efficiencies are confirmed in data for a selection of tagging techniques.

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1 Introduction
The high collision energies at the large hadron collider (LHC) can result in the production of particles with transverse momentum, $p_T$, much larger than their mass. Such particles are boosted: their decay products are highly collimated, and for fully hadronic decays they can be reconstructed as a single hadronic jet ($R \approx M/p_T \sim 2$: the jet mass divided by the $p_T$ is roughly equal to the maximum opening angle of the two decay products). Heavy new particles as predicted in many theories beyond the Standard Model can be a source of highly boosted particles.

The work presented here is the result of a detailed study of a large number of techniques and substructure variables that have, over recent years, been proposed as effective methods for tagging hadronically decaying boosted particles. In 2012, the ATLAS experiment collected 20.3 fb$^{-1}$ of proton–proton collision data at a centre-of-mass energy of $\sqrt{s} = 8$ TeV, providing an opportunity to determine which of the many available techniques are most useful for identifying boosted, hadronically decaying $W$ bosons. In the studies

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* ATLAS uses a right-handed coordinate system with its origin at the nominal interaction point (IP) in the centre of the detector and the $z$-axis along the beam pipe. The $x$-axis points from the IP to the centre of the LHC ring, and the $y$-axis points upwards. Cylindrical coordinates ($r, \phi$) are used in the transverse plane, $\phi$ being the azimuthal angle around the $z$-axis. The pseudorapidity is defined in terms of the polar angle $\theta$ as $\eta = -\ln \tan(\theta/2)$. Angular distance is measured in units of $\Delta R = \sqrt{\Delta \eta^2 + \Delta \phi^2}$.  

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presented here, jets that contain the W boson decay products are referred to as W-jets.

A brief overview of the existing jet grooming and substructure techniques, along with references to more detailed information, are provided in Sect. 2. The ATLAS detector is described in Sect. 3, and details of Monte Carlo simulations (MC) in Sect. 4. The event selection procedure and object definitions are given in Sect. 5.

The body of the work detailing the W-jet tagging performance studies is divided into a broad study using MC (Sect. 6) and a detailed study of selected techniques in data (Sect. 7).

In Sect. 6 a two-stage optimisation procedure has been adopted: firstly more than 500 jet reconstruction and grooming algorithm configurations are investigated at a basic level, studying the groomed jet mass distributions only. Secondly, 27 configurations that are well-behaved and show potential for W-jet tagging are investigated using pairwise combinations of mass and one substructure variable.

In Sect. 7, one of the four most promising jet grooming algorithms and three substructure variables are selected as a benchmark for more detailed studies of the W-jet tagging performance in data. Jet mass and energy calibrations are discussed. Event topologies are compared, and various sources of systematic uncertainty and their effects on the measurements are discussed.

In Sect. 8 the conclusions of all the studies are presented.

2 A brief introduction to jets, grooming, and substructure variables

2.1 Jet grooming algorithms

The jet grooming algorithms studied here fall into three main categories: trimming [2], pruning [3,4] and split-filtering [5]. Within each category there are several tunable configuration parameters, in addition to the chosen initial jet reconstruction algorithm, Cambridge–Aachen [6] (C/A) or anti-kt [7], and jet radius parameter R. The FastJet [8] package is used for jet reconstruction and grooming. Jet grooming algorithms generally have two uses: (i) to remove contributions from pileup (additional pp interactions in the same or adjacent bunch crossings within the detector readout window), and (ii) to reveal hard substructure within jets resulting from massive particle decays by removing the soft component of the radiation.

The three major categories of jet grooming algorithms are described below:

- **Trimming:** Starting with constituents of jets initially reconstructed using the C/A or anti-kt algorithm, smaller ‘subjets’ are reconstructed using the kt algorithm [9] with a radius parameter \( R = R_{\text{sub}} \), and removed if they carry less than a fraction \( f_{\text{cut}} \) of the original, ungroomed, large-R jet \( p_T \). For reference, the recommended trimming configuration from prior ATLAS studies [10] is anti-kt, \( R = 1.0 \), with \( f_{\text{cut}} \geq 5 \% \) and \( R_{\text{sub}} = 0.3 \).

- **Pruning:** The constituents of jets initially reconstructed with the C/A or anti-kt algorithms are re-clustered with the C/A algorithm with two parameters: \( R_{\text{cut}} \) and \( Z_{\text{cut}} \). The \( k_t \) algorithm was used for re-clustering in previous studies [10], but was not found to be as effective. In each pairwise clustering, the secondary constituent is discarded if it is (i) wide-angled: \( \Delta R_{12} > R_{\text{cut}} \times 2M/p_T \), where \( \Delta R_{12} \) is the angular separation of the two subjets; or (ii) soft: \( f_2 < Z_{\text{cut}} \), where \( M \) is the jet mass and \( f_2 \) is the \( p_T \) fraction of the softer constituent with respect to the \( p_T \) of the pair. A configuration of the pruning algorithm is favoured by the CMS experiment for W-jet tagging [11,12], using C/A jets with \( R = 0.8 \) and pruning with \( Z_{\text{cut}} = 10 \% \) and \( R_{\text{cut}} = 0.5 \).

- **Split-filtering:** This algorithm has two stages: the first (splitting) is based on the jet substructure, and the second (filtering) is a grooming stage to remove soft radiation. For the first stage, C/A jets are de-clustered through the clustering history of the jet. This declustering is an exact reversal of the C/A clustering procedure, and can be thought of as splitting the jet into two pieces. The momentum balance, \( \sqrt{12} \), is defined as:

\[
\sqrt{12} = \frac{\min(p_{T1}, p_{T2})}{m_{12}} \Delta R_{12},
\]

where \( p_{T1} (p_{T2}) \) is the piece with the highest (the lowest) \( p_T \), and \( m_{12} \) is the invariant mass of the two pieces. The mass-drop fraction \( \mu_{12} \) is the fraction of mass carried by the piece with the highest mass:

\[
\mu_{12} = \frac{\max(m_1, m_2)}{m_{12}}.
\]

If the requirements on the mass-drop \( \mu_{12} < \mu_{\text{max}} \) and momentum balance \( \sqrt{12} > \sqrt{\text{min}} \) are met then the jet is accepted and can proceed to the filtering stage. Otherwise the de-clustering procedure continues with the highest mass piece: this is now split into two pieces and the \( \mu_{12} \) and \( \sqrt{12} \) requirements are again checked. This process continues iteratively. In the filtering stage, the constituents of the surviving jet are reclustered with a subjet size of \( R_{\text{sub}} = \min(0.3, \Delta R_{12}) \) where \( \Delta R_{12} \) is taken from the splitting stage. Any remaining radiation outside the three hardest subjets is discarded. This algorithm differs somewhat from pruning and trimming in...
2.2 Substructure variables

Substructure variables are a set of jet properties that are designed to uncover hard substructure within jets. An important difference in the substructure variables comes from the choice of distance measure used in their calculation. The various distance measures indicated are used by one or more of the algorithms described in the text. The abbreviation ‘wta’ stands for ‘winner-takes-all’.

Jet shapes use the relative positions and momenta of jet constituents with respect to each other, rather than defining subjects. The jet mass, \( M \), energy correlation ratios \( C_i^{(\beta)} \) [16] and \( D_i^{(\beta)} \) [17,18], the mass-normalised angularity \( a_3 \) [19], and the planar flow, \( P \) [19], all satisfy this description. The calculations of the jet mass and energy correlation ratios are described later in this section.

Splitting scales use the clustering history of the jet to define substructures (‘natural subjects’). The splitting scales studied here are \( \sqrt{D_{12}} \) [20] and its mass-normalised form \( \sqrt{\tau_{12}} \) [21], and the momentum balance and mass-drop variables \( \sqrt{\gamma_{12}} \) and \( \mu_{12} \), defined above in the description of the split-filtering algorithm. The soft-drop level \( L_{SD}(\beta) \) [22] also belongs in this class of variables.

Subjettiness variables [23,24] force the constituents into substructure templates to see how well they fit (‘synthetic subjects’), and are connected to how likely the corresponding jet is composed of \( n \) subjets. The calculations for two forms of 2-subjettiness \( \tau_2, \tau_2^{\text{wta}} \), and the corresponding ratios \( \tau_{21}, \tau_{21}^{\text{wta}} \) are given later in this section. The dipolarity [25], \( D \), uses a related method to define hard substructure.

Centre-of-mass jet shapes transform the constituents and then use them with respect to the jet axis. The variables considered are thrust, \( T_{\text{min}}, T_{\text{maj}} \), sphericity, \( S \), and aplasticity, \( A \), which have been used in a previous ATLAS measurement [26].

Quantum-jet variables The quantum jets (‘Q-jets’) method [27] is unique in its class, using a non-deterministic approach to jet reconstruction. More information on the use of this method by ATLAS can be found in Ref. [28].

The variables found in the following studies to be most interesting in terms of \( W \)-jet tagging are described here in more detail.

Jet mass:

The mass of a jet is given by the difference between the squared sums of the energy \( E_i \) and momenta \( p_i \) of the constituents:

\[
M^2 = \left( \sum_i E_i \right)^2 - \left( \sum_i p_i \right)^2.
\]

For a two-body decay, the jet mass can be approximated as:

\[
M^2 \approx p_{T1} p_{T2} \Delta R_{12}^2.
\]

N-subjettiness:

The “N-subjettiness” [23,24] jet shape variables describe to what degree the substructure of a given jet \( J \) is compatible with being composed of \( N \) or fewer subjets. The 0-, 1- and 2-subjettiness are defined as:

\[
\tau_0(\beta) = \sum_{i \in J} p_{Ti} \Delta R^\beta,
\]

\[
\tau_1(\beta) = \frac{1}{\tau_0(\beta)} \sum_{i \in J} p_{Ti} \Delta R_{a1,i}^\beta,
\]

\[
\tau_2(\beta) = \frac{1}{\tau_0(\beta)} \sum_{i \in J} p_{Ti} \min(\Delta R_{a1,i}^\beta, \Delta R_{a2,i}^\beta),
\]

where the distance \( \Delta R \) refers to the distance between constituent \( i \) and the jet axis, and the parameter \( \beta \) can be used to give a weight to the angular separation of the jet constituents. In the studies presented here, the value of \( \beta = 1 \) is taken. The calculation of \( \tau_N \) requires the definition of \( N \) axes, such that...
the distance between each constituent and any of these axes is $R_{d\phi,i}$. In the above functions, the sum is performed over the constituents $i$ in the jet $J$, such that the normalisation factor $\tau_0$ (Eq. 5a) is equivalent to the magnitude of the jet $p_T$ multiplied by the $\beta$-exponentiated jet radius.

Recent studies [29] have shown that an effective alternative axis definition can increase the discrimination power of these variables. The ‘winner-takes-all’ axis uses the direction of the hardest constituent in the exclusive $k_t$ variables. The ‘winner-takes-all’ axis uses the direction of the hardest constituent in the exclusive $k_t$ variables. The ratio of the $N$-subjettiness functions found with the standard subjett axes, $\tau_{2,1}$, and with the ‘winner-takes-all’ axes, $\tau_{2,1}^{wta}$, can be used to generate the dimensionless variables that have been shown in particle-level MC to be particularly useful in identifying two-body structures within jets:

$$\tau_{2,1} = \frac{\tau_2}{\tau_1}, \quad \tau_{2,1}^{wta} = \frac{\tau_2^{wta}}{\tau_1^{wta}}. \tag{6}$$

### Energy correlation ratios:

The 1-point, 2-point and 3-point energy correlation functions for a jet $J$ are given by:

$$E_{CF0}(\beta) = 1, \tag{7a}$$

$$E_{CF1}(\beta) = \sum_{i \in J} p_{Ti}, \tag{7b}$$

$$E_{CF2}(\beta) = \sum_{i<j \in J} p_{Ti} p_{Tj} (\Delta R_{ij})^\beta, \tag{7c}$$

$$E_{CF3}(\beta) = \sum_{i<j<k \in J} p_{Ti} p_{Tj} p_{Tk} (\Delta R_{ij} \Delta R_{jk} \Delta R_{kj})^\beta, \tag{7d}$$

where the parameter $\beta$ is used to give weight to the angular separation of the jet constituents. In the above functions, the sum is over the constituents $i$ in the jet $J$, such that the 1-point correlation function Eq. (7b) is approximately the jet $p_T$. Likewise, if one takes $\beta = 2$, it is noted that the 2-point correlation functions are equivalent to the mass of a particle undergoing a two-body decay in collider coordinates.

An abbreviated form of these definitions can be written as:

$$e_2^{(\beta)} = \frac{E_{CF2}(\beta)}{E_{CF1}(\beta)^2}, \tag{8a}$$

$$e_3^{(\beta)} = \frac{E_{CF3}(\beta)}{E_{CF1}(\beta)^3}. \tag{8b}$$

These ratios of the energy correlation functions can be used to generate the dimensionless variable $C_2^{(\beta)}$ [16], and its more recently modified version $D_2^{(\beta)}$ [17,18], that have been shown in particle-level MC to be particularly useful in identifying two-body structures within jets:

$$C_2^{(\beta)} = \frac{e_3^{(\beta)}}{(e_2^{(\beta)})^2}, \tag{9a}$$

$$D_2^{(\beta)} = \frac{e_3^{(\beta)}}{(e_2^{(\beta)})^3}. \tag{9b}$$

Values of $\beta = 1$ and 2 are studied here.

### 3 The ATLAS detector

The ATLAS detector [30] at the LHC covers nearly the entire solid angle around the collision point. It consists of an inner tracking detector surrounded by a thin superconducting solenoid, electromagnetic and hadronic calorimeters, and a muon spectrometer incorporating three large superconducting toroid magnets.

The inner-detector system (ID) is immersed in a 2 T axial magnetic field and provides charged particle tracking in the range $|\eta| < 2.5$. A high-granularity silicon pixel detector covers the vertex region and typically provides three measurements per track. It is followed by a silicon microstrip tracker, which usually provides four two-dimensional measurement points per track. These silicon detectors are complemented by a transition radiation tracker, which enables radially extended track reconstruction up to $|\eta| = 2.0$. The transition radiation tracker also provides electron identification information based on the fraction of hits (typically 30 in total) above a higher energy-deposit threshold corresponding to transition radiation.

The calorimeter system covers the pseudorapidity range $|\eta| < 4.9$. Within the region $|\eta| < 3.2$, electromagnetic calorimetry is provided by barrel and endcap high-granularity lead/liquid-argon (LAr) electromagnetic calorimeters, with an additional thin LAr presampler covering $|\eta| < 1.8$, to correct for energy loss in material upstream of the calorimeters. For the jets measured here, the transverse granularity ranges from 0.003 × 0.1 to 0.1 × 0.1 in $\Delta \eta \times \Delta \phi$, depending on depth segment and pseudorapidity. Hadronic calorimetry is provided by a steel/scintillator-tile calorimeter, segmented into three barrel structures within $|\eta| < 1.7$, and two copper/LAr hadronic endcap calorimeters. This system enables measurements of the shower energy deposition in three depth segments at a transverse granularity of typically 0.1 × 0.1. The solid angle coverage is extended with forward copper/LAr and tungsten/LAr calorimeter modules optimised for electromagnetic and hadronic measurements respectively.

A muon spectrometer (MS) comprises separate trigger and high-precision tracking chambers measuring the deflection of muons in a magnetic field generated by superconducting air-core toroids. The precision chamber system covers the region $|\eta| < 2.7$ with three layers of monitored drift tubes, com-
plemented by cathode strip chambers in the forward region, where the background is highest. The muon trigger system covers the range $|\eta| < 2.4$ with resistive-plate chambers in the barrel, and thin-gap chambers in the endcap regions.

A three-level trigger system is used to select interesting events [31]. The Level-1 trigger is implemented in hardware and uses a subset of detector information to reduce the event rate to a design value of at most 75 kHz. This is followed by two software-based trigger levels which together reduce the event rate to about 400 Hz.

4 Data and Monte Carlo simulations

The data used for this analysis were collected during the $pp$ collision data-taking period in 2012, and correspond to an integrated luminosity of 20.3 fb$^{-1}$ with a mean number of $pp$ interactions per bunch crossing, $\langle \mu \rangle$, of about 20. The uncertainty on the integrated luminosity, 2.8 %, is derived following the same methodology as that detailed in Ref. [32] using beam-separation scans. Data quality and event selection requirements are given in Sect. 5.

Events from Monte Carlo generator are passed through a GEANT4-based [33] simulation of the ATLAS detector [34], and reconstructed using the same algorithm used as for data. All MC samples are produced with the addition of pileup, using hits from minimum-bias events that are produced with PYTHIA (8.160) [35] using the A2M set of tunable parameters (tune) [36] and the MSTW2008LO [37] PDF set. This simulated pileup does not exactly match the distribution of $\langle \mu \rangle$ measured in data. As such, event weights are derived as a function of $\langle \mu \rangle$ for the MC samples used in the data/MC comparisons, making the differences between the data and MC $\langle \mu \rangle$ distributions negligible.

4.1 Monte Carlo samples for the $W$ signal

Samples of the hypothetical process $W' \rightarrow WZ \rightarrow q\bar{q}\ell\ell$ are produced as a source of signal high-$p_T$ $W$-jets, with the boost in $p_T$ coming from the high mass of the parent $W'$. These samples are produced using PYTHIA (8.165) with the AU2 [36] tune and the MSTW2008LO [37] PDF set. Nine separate signal samples are produced with $W'$ masses ranging from 400 to 2000 GeV in steps of 200 GeV. This ensures good coverage over a wide range of $W$-jet $p_T$. The nine samples are combined and the events are given weights such that when the event weights are applied, the $p_T$ distribution of the combined signal $W$-jets sample matches that of the multijet background sample described in Sect. 4.2. These are used as the signal samples in the preliminary optimisation studies presented in Sect. 6.

The $W$ boson tagging efficiency from top quark decays in data, detailed in Sect. 7, is measured using $t\bar{t}$ samples simulated with the POWHEG-BOX (version 1, r2330) NLO generator [38] interfaced with PYTHIA (6.427). A cross-check is performed with MC@NLO [39] (4.03), with parton showers provided by HERWIG (6.520) [40]+JIMMY (4.31) [41]. In both cases, the next-to-leading order CT10 [42] PDF set is used, and the top quark mass is set to 172.5 GeV. Single-top-quark events in the $s$-, $t$- and $Wt$-channels are simulated with POWHEG-BOX interfaced with PYTHIA (6.426), with the Perugia 2011c [43] tune. The $t$-channel is also generated with POWHEG-BOX in the four-flavour scheme. Background $W$-jet and $Z$-jet events are simulated using ALPGEN [44] (2.14) in the four-flavour scheme ($b$-quarks are treated as massive) followed by PYTHIA (6.426) for the parton shower. Up to five extra partons are considered in the matrix element. The CTEQ6L1 [45] PDF set and the Perugia 2011c tune are used. For diboson events, the SHERPA [46] (1.4.3) generator is used with up to three extra partons in the matrix element and the masses of the $b$- and $c$-quarks are taken into account.

The effects of differences between the $W' \rightarrow WZ$ process used for $W$-jets in the preliminary optimisation studies and the $t\bar{t}$ process used in the detailed comparisons with data are discussed in Sect. 7.2.

4.2 Monte Carlo samples for the multijet background

The background sample used in Sect. 6 is made up of several high-$p_T$ multijets event samples produced using PYTHIA [35] with the AU2 [36] tune and the CT10 [42] PDF set. Eight samples in total are produced according to the leading jet’s $p_T$, four of which are used in this analysis to cover the $p_T$ range 200–2000 GeV. These samples are combined with event weights determined by their relative cross-sections to produce the smoothly falling $p_T$ distribution predicted by PYTHIA. The MC optimisation studies use the leading jets from these events. The jets in these background samples are initiated by light quarks and gluons, the interactions of which are described by Quantum Chromodynamics, QCD.

The $W$-tagging efficiency in multijet background events is studied on the same multijet samples as used for the optimisation studies, using PYTHIA (8.165) with the AU2 tune and the CT10 PDF set, and also a HERWIG++ (2.6.3) sample with the EE3 tune [47] and CTEQ6L1 [45] PDF set. It is these samples that are used for the comparisons with data in Sect. 7.

The effects of differences between these samples due to using the leading jets (for the MC-based optimisation) or both leading and sub-leading jets (for the multijet background efficiency measurement in data) are discussed in Sect. 7.2.
5 Object reconstruction and event selection

In the studies presented here, calorimeter jets are reconstructed from three-dimensional topological clusters (topoclusters) [48] which have been calibrated using the local cluster weighting (LCW) scheme [49]. In MC simulated events, truth jets are built from generator-level particles that have a lifetime longer than 10 ps, excluding muons and neutrinos. Jets are reconstructed using one of the iterative recombination jet reconstruction algorithms [50,51] C/A or anti-kt. The kt algorithm is also used by the jet trimming algorithm to reconstruct subjets.

In all following discussions, the term constituents means particles in the case of truth jets and LCW topoclusters in the case of calorimeter jets.

For the MC-based optimisation studies discussed in Sect. 6, events are characterised using the leading jet, reconstructed from generator-level particles with the C/A, R = 1.2 algorithm.

Objects used to select tt̄ events in data and MC for the studies in Sect. 7 include reconstructed leptons (electrons and muons), missing transverse momentum (E_T^miss), small-R jets (reconstructed with the anti-kt algorithm with radius parameter R = 0.4), trimmed anti-kt, R = 1.0 jets and b-tagged jets, defined below.

- **Electrons:** Electron candidates are reconstructed from energy deposits in the EM calorimeter matched to reconstructed tracks in the ID. Candidates are required to be within |η| < 2.47, excluding the barrel/endcap transition region, 1.37 < |η| < 1.52, of the EM calorimeter, and must have a transverse energy E_T > 25 GeV. They are required to satisfy tight identification criteria [52] and to fulfil isolation [53] requirements; excluding its own track, the scalar sum of the p_T of charged tracks within a cone of size ΔR = min(10 GeV/E_T, 0.4) around the electron candidate must be less than 5% of the p_T of the electron.

- **Muons:** Muons are reconstructed by matching MS to ID tracks. Muons are required to be within |η| < 2.5 and have p_T > 25 GeV. In order to reject non-prompt muons from hadron decays, the significance of their transverse impact parameter must be |d_0|/σ_d_0 < 3, the longitudinal impact parameter must be |z_0| < 2 mm, and the scalar sum of p_T of the charged tracks within a cone of size ΔR = min(10 GeV/p_T, 0.4) around the muon candidate, excluding its own track, must be less than 5% of the p_T of muon.

- **Trigger leptons:** Events are selected by requiring an unprescaled single-lepton trigger for the electron and muon channels. Two single-electron triggers, with transverse energy thresholds of E_T > 24 GeV for isolated electrons and E_T > 60 GeV without isolation criteria, are used in combination with two single-muon triggers, with transverse momentum of p_T > 24 GeV for isolated muons and p_T > 36 GeV without isolation criteria. The selected muon (electron) must be matched to a trigger and is required to fulfil p_T > 25(20) GeV and |η| < 2.5. Events are rejected if any other electron or muon satisfying the identification criteria is found in the event.

- **Missing transverse momentum, E_T^miss and transverse mass, m_W:** The missing transverse momentum is calculated from the vector sum of the transverse energy of topological clusters in the calorimeter [54]. The clusters associated with the reconstructed electrons and small-R jets are replaced by the calibrated energies of these objects. Muon p_T determined from the ID and the muon spectrometer are also included in the calculation. The E_T^miss is required to exceed 20 GeV. The sum of the E_T^miss and the transverse mass, m_W = \sqrt{2p_T E_T^miss(1 - \cos Δφ)}, reconstructed from the E_T^miss and the transverse momentum of the lepton, must be E_T^miss + m_W > 60 GeV.

- **Small-R Jets (anti-kt, R = 0.4):** Using locally calibrated topological clusters as input, small-R jets are formed using the anti-kt algorithm with a radius parameter R = 0.4. Small-R jets are required to be within |η| < 2.5 and to have p_T > 25 GeV. To reject jets with significant pileup contributions, the jet vertex fraction [55], defined as the scalar sum of the p_T of tracks associated with the jet that are assigned to the primary vertex divided by the scalar sum of the p_T of all tracks associated to the jet, is required to be greater than 0.5 for jets with p_T < 50 GeV. At least one small-R jet must be found. In addition, at least one small-R jet must lie within ΔR = 1.5 of the lepton. The leading small-R jet within ΔR = 1.5 of the lepton is defined as the “leptonic-top jet” and denoted j_1. Jets have to satisfy specific cleaning requirements [56] to remove calorimeter signals coming from non-collision sources or calorimeter noise. Events containing any jets that fail these requirements are rejected.

- **b-jets (anti-kt, R = 0.4):** The output of the MV1 [57] algorithm is used to identify small-R jets containing b-hadrons. Small-R jets are tagged as b-jets if the MV1 weight is larger than the value corresponding to the 70% b-tagging efficiency working point of the algorithm. At least one small-R jet must be tagged as a b-jet. Loose b-jets are defined as having an MV1 weight larger than the value corresponding to the 80% working point. All loose b-jets must be separated by ΔR > 1.0 from the W-jet candidate.

- **Trimmed R = 1.0 Jets:** Using locally calibrated topological clusters as inputs, anti-kt, R = 1.0 jets are groomed using the trimming algorithm with parameters fcut = 5% and R_sub = 0.2. The pseudorapidity, energy and mass of these jets are calibrated using a simulation-based calibration scheme as mentioned in Sect. 6.4. At least one trimmed anti-kt, R = 1.0 jet with p_T > 200 GeV and
|η| < 1.2 is required. If more than one jet satisfies these criteria, the leading jet is used to reconstruct the W boson candidate, JW. This candidate, JW, has to be well separated from the leptonic-top jet, ΔR(JW, Jt) > 1.2.

- Overlapping jets and leptons: An overlap removal procedure is applied to avoid double-counting of leptons and anti-kt, R = 0.4 jets, along with an electron-in-jet subtraction procedure to recover prompt electrons that are used as constituents of a jet. If an electron lies ΔR < 0.4 from the nearest jet, the electron four-momentum is subtracted from that of the jet. If the subtracted jet fails to meet the small-R jet selection criteria outlined above, the jet is marked for removal. If the subtracted jet satisfies the jet selection criteria, the electron is removed and its four-momentum is added back into the jet. Next, muons are removed if ΔR(meson, jet) < 0.04 + 10 GeV/Pt,muon using jets that are not marked for removal after the electron subtraction process.

For the measurement of the multijet background efficiency, a different selection is used to ensure a multijet-enriched sample. The multijet sample is selected using a single, un-prescaled, R = 1.0 jet trigger that is 80% efficient for jets with pT > 450 GeV. No grooming is applied to jets at the trigger level. For events with a leading jet above the trigger threshold, both the leading and the sub-leading jets are used for this performance study, making it applicable for jets with pT down to 200 GeV. At least one anti-kt, R = 1.0 jet, trimmed with fc = 5% and Rsh = 0.2, is required to have pT > 200 GeV and |η| < 1.2. Events containing fake jets from noise in the calorimeter or non-collision backgrounds, according to Refs. [58, 59], are rejected.

For the t¯t and multijet background selection, good data quality is required for events in data, meaning that all the detectors of ATLAS as well as the trigger and data acquisition system are required to be fully operational. Events are required to have at least one reconstructed primary vertex with at least five associated tracks, and this vertex must be consistent with the LHC beam spot.

6 A comprehensive comparison of techniques in Monte Carlo simulations

The initial phase of this study evaluates the performance of a large number of grooming and tagging algorithms in MC simulated events.

To account for correlations between the W boson pT and the resulting jet substructure features, events are categorised by the pT of the leading (highest pT) jet reconstructed with the C/A [6] algorithm with radius parameter R = 1.2, using stable particles as inputs. These ranges in the ungroomed truth jet pT, pTtruth, are: [200, 350] GeV, [350, 500] GeV, [500, 1000] GeV. This large, ungroomed jet is considered a rough proxy for the W boson, and this choice does not introduce a bias towards any particular grooming configuration for the pTtruth ranges in question. Only events with a C/A, R = 1.2 truth jet within |η| < 1.2 are considered, ensuring that jets are within the acceptance of the tracking detector, which is necessary for the derivation of the systematic uncertainties.

First, in Sect. 6.1, more than 500 jet reconstruction and grooming algorithm configurations are selected based on prior studies [10, 11, 60–63]. The leading-groomed-jet mass distributions for W-jet signal and multijet background in MC are examined. An ordered list is built rating each configuration based on the background efficiency. The notation for the background efficiency at this grooming stage is ϵG&T, and this is measured within a mass window that provides a signal efficiency of 68%, denoted ϵW = 68%. The best performers for each category described in Sect. 2.1 (trimming, pruning, split-filtering) are retained for the next stage: a total of 27 jet collections.

Observations about pileup-dependence are summarised in Sect. 6.2. Jet grooming reduces the pileup-dependence of the jet mass and helps distinguish W-jets from those initiated by light quarks and gluons by improving the mass resolution, but does not provide strong background rejection. Further information coming from the distribution of energy deposits within a jet can be used to improve the ratio of signal to background.

In the second stage, 26 substructure variables are studied for all 27 selected jet collections. These studies are detailed in Sect. 6.3. Substructure variables can be calculated using jet constituents before or after grooming; in these studies all variables are calculated from the groomed jet’s constituents, such that the potential sensitivity to pileup conditions is reduced.

The aim of these studies is to find an effective combination of groomed jet mass and one substructure variable. The background efficiency ϵG&T/QCD (where G&T indicates grooming plus tagging) versus the signal efficiency ϵW/G&T is calculated for all variables in each configuration, and background efficiencies for ‘medium’ (50%) and ‘tight’ (25%) signal efficiency working points are determined. Four grooming algorithms and three tagging variables are identified as having a particularly low background efficiency at the medium signal efficiency working point, ϵW/G&T = 50%.

In Sect. 6.4 the conclusions of these preliminary studies of combined groomed mass and substructure taggers are presented.

6.1 Performance of grooming algorithms

A set of more than 500 jet reconstruction and grooming algorithm configurations (introduced in Sect. 2.1) are explored within the parameter space summarised in Table 1.
Table 1  Details of the different trimming, pruning and split-filtering configurations that were tried in order to define the best grooming algorithms. All combinations of the grooming parameters are explored in these studies.

Trimming configurations
Input jet algorithms | $R$ | $R_{\text{sub}}$ | $f_{\text{cut}}$ ($\%$) |
<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>C/A, anti-$k_t$</td>
<td>0.6, 0.8, 1.0, 1.2</td>
<td>0.1, 0.2, 0.3</td>
<td>1, 2, 3, 4, 5, 7, 9, 11, 13, 15</td>
</tr>
</tbody>
</table>

Pruning configurations
Input jet algorithm | $R$ | Reclust. alg. | $Z_{\text{cut}}$ ($\%$) | $R_{\text{cut}}$ |
<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>C/A, anti-$k_t$</td>
<td>0.8, 1.0, 1.2</td>
<td>C/A</td>
<td>10, 15, 20, 25, 30</td>
<td>$\frac{1}{2}$, $\frac{3}{4}$, 1, 1.0</td>
</tr>
</tbody>
</table>

Split-filtering configurations
Input jet algorithm | $R$ | $R_{\text{sub}}$ | $\mu_{\text{max}}$ | $y_{\text{cut}}$ |
<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>C/A</td>
<td>0.8, 1.0, 1.2</td>
<td>0.3, min(0.3, $\Delta R/2$)</td>
<td>67, 78, 89, 100</td>
<td>0.06, 0.07, ..., 0.20</td>
</tr>
</tbody>
</table>

Fig. 2  Uncalibrated mass distributions for various selected grooming configurations: a trimmed with $R_{\text{sub}} = 0.2$, b trimmed with $R_{\text{sub}} = 0.3$, c pruned, and d split-filtered. The transverse momentum range $p_{\text{T}}^{\text{truth}} = [200, 350] \text{ GeV}$ is shown for $W$ signal (solid blue line) and multijet background (dashed red line). The (black) Gaussian fit uses an initial-condition mass set to 80.4 GeV. The dotted vertical lines indicate the $1\sigma$ fit interval. The dashed lines contain 68% of the signal and define the mass window. These are examples of grooming algorithms leading to satisfactory mass distributions. Uncertainty bands are statistical only.
The signal and background mass distributions for a selection of grooming configurations in the range $200 < p_T^{\text{Truth}} < 350$ GeV are shown in Fig. 2. A Gaussian fit to the $W$ boson mass peak (with the $W$ mass set as the initial condition) is shown. Two alternative signal mass window definitions are considered:

1. The $\sigma$ boundaries of the Gaussian fit.
2. The smallest interval that contains 68% of the integral.

Comparing the extent of these two mass windows allows an estimation of how closely the signal mass peak resembles a Gaussian distribution. The $W$-jet mass is required to be within the boundaries defined by this latter definition of the signal window; this leads, by definition, to a baseline signal efficiency of $\epsilon_W^G = 68\%$ for all algorithms.

The groomed jet mass distributions for leading jets are examined for all combinations of grooming configurations for $W$-jet signal and multijet background. The background efficiency, $\epsilon_{\text{QCD}}^G$ is defined as follows:

- The denominator is the total number of pre-selected events from the multijet background sample, where the pre-selection requires an ungroomed $C/A, R = 1.2$ truth jet with $p_T^{\text{Truth}} > 200\text{ GeV}$ and $|\eta^{\text{Truth}}| < 1.2$.
- The numerator is the number of pre-selected events where the groomed jet mass falls in the window that contains 68% of the $W$-jet signal, $\epsilon_W^G = 68\%$.

The minimisation of $\epsilon_{\text{QCD}}^G$ is the primary criterion for ordering the algorithms according to their performance. In addition, there are a number of possible pathologies revealed in the mass distributions: features that show obviously unsuitable configurations, or make it impossible to derive a jet mass calibration, or indicate the need for additional pileup removal techniques. These are:

(i) The $\epsilon_W^G = 68\%$ window does not contain the $W$ boson mass [64]. An example of this is shown in Fig. 3a.
(ii) The signal mass distribution is strongly non-Gaussian. An example of this is shown in Fig. 3b.
(iii) The background mass distribution has an irregular shape (e.g. it has local maxima) in the region of the signal peak. An example of this is also shown in Fig. 3b.
(iv) The jet mass after grooming is strongly affected by pileup. Configurations where the average jet mass increases by $>1$ GeV times the number of primary vertices, NPV, are rejected. This issue is discussed in Sect. 6.2.

Algorithms that are susceptible to any of these pathologies are removed from the list of well-behaved algorithm configurations.

The $W$ boson tagging efficiency performance is studied independently for three different ranges in the $p_T$ of the ungroomed truth jet reconstructed with the $C/A, R = 1.2$ algorithm: $[200, 350], [350, 500], [500, 1000]$ GeV. The results for the three grooming categories share some common features:
The jets reconstructed with $R = 0.6$ and $R = 0.8$ are too small to contain all the decay products of a $W$-jet for $p_T < 500$ GeV and $p_T < 350$ GeV, respectively. The reconstructed jet mass is often much smaller than 80 GeV, indicating that some of the $W$ boson decay products are not clustered, and the 68% signal mass window is wider, resulting in a higher background efficiency. Small radii jets can, however, have good performance at high $p_T$.

- In the highest $p_T$ bin, 500–1000 GeV, the various configurations result in a similar performance.

Fig. 4: Mass windows and background efficiencies for various configurations of trimming ($R = 1.0$ shown). The baseline systematic uncertainty on the background efficiency for the $p_T$ bin in question (the range $350 < p_T < 500$ GeV is shown here) is calculated by varying the jet mass scale (JMS) and jet energy scale (JES) by $\pm 1\sigma$ for a representative jet collection. For trimming, this representative configuration is $R_{sub} = 0.2$ and $f_{cut} = 5\%$. The stars indicate the favoured trimming configurations for $W$-tagging, as detailed in Sect. 6.4.

Table 2: The best trimming configurations for $W$-tagging with each $R$ based on the first stage of the MC-based optimisation studies.

<table>
<thead>
<tr>
<th>Initial algorithm</th>
<th>$R$</th>
<th>$f_{cut}$ (%)</th>
<th>$R_{sub}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>anti-$k_t$</td>
<td>1.2</td>
<td>5</td>
<td>0.2</td>
</tr>
<tr>
<td>C/A</td>
<td>1.2</td>
<td>5</td>
<td>0.2</td>
</tr>
<tr>
<td>anti-$k_t$</td>
<td>1.0</td>
<td>5</td>
<td>0.2</td>
</tr>
<tr>
<td>C/A</td>
<td>1.0</td>
<td>5</td>
<td>0.2</td>
</tr>
<tr>
<td>anti-$k_t$</td>
<td>1.0</td>
<td>5</td>
<td>0.3</td>
</tr>
<tr>
<td>anti-$k_t$</td>
<td>0.8</td>
<td>5</td>
<td>0.2</td>
</tr>
<tr>
<td>C/A</td>
<td>0.8</td>
<td>5</td>
<td>0.2</td>
</tr>
<tr>
<td>C/A</td>
<td>0.6</td>
<td>5</td>
<td>0.2</td>
</tr>
</tbody>
</table>

- C/A and anti-$k_t$ jets have a similar performance under the same configurations.
- The larger values of $f_{cut}$ can lead to significantly lower background efficiency.
- The dependence of the performance on $R_{sub}$ is less significant, but the background efficiency does decrease somewhat for smaller $R_{sub}$ values.

Based on the performance of these algorithms, the trimming implementations considered for further investigation are given in Table 2. Although promising, configurations with $R_{sub} = 0.1$ are not pursued further in these studies, as this size is approaching the limiting granularity of the hadronic...
Pruning:
The performance of pruning is studied using both C/A and anti-$k_t$ algorithms for the initial large-$R$ ($R = 0.6$–$1.2$) jet finding, and C/A for the reclustering procedure. The background efficiencies and 68% signal mass windows obtained with a subset of pruning configurations for the range $350 < p_T < 500$ GeV are shown in Fig. 5.

Several observations can be made:

• Using the C/A algorithm as the re-clustering algorithm for pruning is consistently better than using the $k_t$ algorithm, for the same values of the $R_{\text{cut}}$ and $Z_{\text{cut}}$ parameters.

• Pruning with smaller $R_{\text{cut}}$ and/or higher $Z_{\text{cut}}$ can be overly harsh, resulting in $W$-jet mass peaks at values lower than 80 GeV.

• The background efficiency does not have strong dependence on $R_{\text{cut}}$ or on $Z_{\text{cut}}$, but there is evidence for a $p_T$ dependence of the optimal $Z_{\text{cut}}$, with $Z_{\text{cut}} = 0.15$ being preferable for the ranges $200 < p_T < 350$ GeV and $350 < p_T < 500$ GeV, and $Z_{\text{cut}} = 0.10$ being preferred for $p_T > 500$ GeV.

• For all pruning configurations, the performance is significantly worse in the lowest $p_T$ bin.

Based on the performance of all the algorithms, the eight combinations retained for further studies are given in Table 3.

### Table 3
The best pruning configurations for $W$-tagging with each $R$ based on the first stage of the MC-based optimisation studies

<table>
<thead>
<tr>
<th>Initial algorithm</th>
<th>$R$</th>
<th>$Z_{\text{cut}}$ (%)</th>
<th>$R_{\text{cut}}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>C/A</td>
<td>1.2</td>
<td>10</td>
<td>0.5</td>
</tr>
<tr>
<td>C/A</td>
<td>1.2</td>
<td>15</td>
<td>0.5</td>
</tr>
<tr>
<td>C/A</td>
<td>1.0</td>
<td>10</td>
<td>0.5</td>
</tr>
<tr>
<td>C/A</td>
<td>1.0</td>
<td>15</td>
<td>0.5</td>
</tr>
<tr>
<td>C/A</td>
<td>0.8</td>
<td>10</td>
<td>0.5</td>
</tr>
<tr>
<td>C/A</td>
<td>0.8</td>
<td>15</td>
<td>0.5</td>
</tr>
<tr>
<td>C/A</td>
<td>0.6</td>
<td>10</td>
<td>0.5</td>
</tr>
<tr>
<td>C/A</td>
<td>0.6</td>
<td>15</td>
<td>0.5</td>
</tr>
</tbody>
</table>

### Split-filtering:
Split-filtering is studied with C/A jets with $R = 1.2$ and $1.0$, and various values of the parameters $\sqrt{\Delta y_{\text{min}}}$, $R_{\text{sub}}$ and $\mu_{\text{max}}$. The background efficiencies and 68% signal mass windows obtained with a subset of split-filtering configurations for the range $350 < p_T < 500$ GeV are shown in Figs. 6 and 7.

Observations from the results of these studies include the following:

• Larger $\sqrt{\Delta y_{\text{min}}}$ values tend to result in lower background efficiencies.

• The performance has a dependence on $\sqrt{\Delta y_{\text{min}}}$ and the optimal requirement varies with jet $p_T$. For $\chi_{\text{cut}} \geq 0.09$, the background efficiency is relatively stable.
ATLAS
Pythia8 simulation
\( \sqrt{s} = 8 \text{ TeV} \)

Split-filtered jets, \( R=1.2 \)
\( 350 < p_T^{\text{Truth}} < 500 \text{ GeV} \)
\( |\eta^{\text{Truth}}| < 1.2 \)
\( \mu_{\text{max}} = 1 \)
\( \mu_{\text{max}} = 2/3 \)
\( R_{\text{sub}} = 0.3 \)
\( y_{\text{cut}} = 15\% \)

Shaded bands indicate extent of 68\% mass windows

W mass

Bars indicate stat. + baseline syst. uncertainty from JMS+JES

\( \varepsilon_{\text{GCB}} \)

10\% background efficiency

\( M \) [GeV]

40
60
80
100
120

\( \mu_{\text{max}} = \frac{1}{2} \)

\( \mu_{\text{max}} = 3 \)

\( y_{\text{cut}} = \text{var} \)

\( y_{\text{cut}} = 20\% \)

Fig. 6 Mass windows and background efficiencies for various additional configurations of split-filtering (\( R = 1.2 \) shown). The baseline systematic uncertainty on the background efficiency for the \( p_T \) bin in question (the range \( 350 < p_T < 500 \text{ GeV} \) is shown here) is calculated by varying the jet mass scale (JMS) and jet energy scale (JES) by \( \pm 1\sigma \) for a representative jet collection. For split-filtering, this representative configuration is \( \mu_{\text{max}} = 1, R_{\text{sub}} = 0.3 \) and \( y_{\text{cut}} = 15\% \).

Split-filtered jets, \( R=1.2 \)
\( 350 < p_T^{\text{Truth}} < 500 \text{ GeV} \)
\( |\eta^{\text{Truth}}| < 1.2 \)
\( \mu_{\text{max}} = 1 \)
\( \mu_{\text{max}} = 2/3 \)
\( R_{\text{sub}} = 0.3 \)

ATLAS
Pythia8 simulation
\( \sqrt{s} = 8 \text{ TeV} \)

Shaded bands indicate extent of 68\% mass windows

W mass

Bars indicate stat. + baseline syst. uncertainty from JMS+JES

\( \varepsilon_{\text{GCB}} \)

10\% background efficiency

\( M \) [GeV]

40
60
80
100
120

\( \mu_{\text{max}} = \frac{1}{2} \)

\( \mu_{\text{max}} = 3 \)

\( y_{\text{cut}} = \text{var} \)

\( y_{\text{cut}} = 20\% \)

Fig. 7 Mass windows and background efficiencies for various configurations of split-filtering (\( R = 1.2 \) shown). The baseline systematic uncertainty on the background efficiency for the \( p_T \) bin in question (the range \( 350 < p_T < 500 \text{ GeV} \) is shown here) is calculated by varying the jet mass scale (JMS) and jet energy scale (JES) by \( \pm 1\sigma \) for a representative jet collection. For split-filtering, this representative configuration is \( \mu_{\text{max}} = 1, R_{\text{sub}} = 0.3 \) and \( y_{\text{cut}} = 15\% \). The star indicates the favoured split-filtering configuration for \( W \)-tagging, as detailed in Sect. 6.4.

- For a \( \sqrt{y_{\text{min}}} > 0.09 \), there is not a strong dependence of the performance on \( R_{\text{sub}} \) or \( \mu_{\text{max}} \).

A total of 11 split-filtering jet collections are considered for further study, all with \( \mu_{\text{max}} = 100\% \) and \( R_{\text{sub}} = 0.3 \). These are given in Table 4.
6.2 Pileup dependence

The influence of pileup on the reconstructed groomed jets is examined during the first stage of algorithm optimisation, and configurations that show large susceptibility to pileup after grooming are discarded. There are a number of methods [61,65–71] available for reducing the effects of pileup, either on their own or combined with grooming; these techniques are not considered in this study. Most grooming configurations almost completely remove the effects of pileup from the mean jet mass as illustrated in Fig. 8 in which the correlation between average jet mass $\langle M \rangle$ and number of reconstructed primary vertices is shown. The significant correlation between the average ungroomed jet mass and the number of reconstructed primary vertices is absent for trimmed jets in both signal and background.

The pileup dependence of the mean jet mass obtained with all 27 of the grooming configurations selected for stage two of the optimisation studies is shown in terms of the fitted slope of $\delta \langle M \rangle/\delta \text{NPV}$ in Fig. 9 for the $p_T$ range 350–500 GeV. In general, the average masses of jets with larger radii have a more pronounced pileup dependence, and the trimmed jet mass has a weaker pileup dependence than that obtained with the pruning and split-filtering algorithms. For all jet algorithms, the pileup dependence is much reduced with respect to that of ungroomed jets.

6.3 Performance of substructure variables

Substructure variables are introduced in Sect. 2.2. A brief description of the variables studied in this analysis are listed below:

- The energy correlation ratios $C_2^{(β)}$ and $D_2^{(β)}$, described in detail in Sect. 2.2.
- The N-subjettiness ratios $τ_2$, $τ_2^{\text{wa}}$, $τ_{21}$, and $τ_{21}^{\text{wa}}$ are also described in detail in Sect. 2.2.
- Planar flow [19], $P$, is a measure of how uniformly distributed the energy of a jet is, perpendicular to its axis.
- The angularity, $a_3$, distribution is expected to peak sharply at values close to zero for a balanced two-body decay, such as that of a $W$ boson, while a broader tail is expected for jets initiated by quarks and gluons. The general formula for the mass-normalised angularity can be found in Ref. [19].
- Splitting scales [20] are calculated, within the jet clustering algorithm, and can be calculated for any jet using its constituents. The splitting scale $\sqrt{d_{12}}$, is calculated for a jet (re)clustered with the $k_t$-clustering algorithm, and is the $k_t$ distance between the two proto-jets of the final clustering step.
- The variable $\sqrt{z_{12}}$ [21] is a variant on the original splitting scale $\sqrt{d_{12}}$ which uses the jet mass.
- The momentum balance [5], $\sqrt{R_{12}}$, and mass-drop fraction $μ_{12}$, are defined at the first de-clustering step that satisfies a minimum mass-drop and momentum balance requirement, and are only available for those jets that are groomed with the split-filtering algorithm.
- The soft-drop algorithm [22] declusters the jet, following the path of highest $p_T$ through the clustering history. A condition is defined:

### Table 4 The best split-filtering configurations for $W$-tagging with each $R$ based on the first stage of the MC-based optimisation studies

<table>
<thead>
<tr>
<th>Initial algorithm</th>
<th>$R$</th>
<th>$\sqrt{\text{min}}$ (%)</th>
<th>$μ_{\text{max}}$ (%)</th>
<th>$R_{\text{sub}}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>C/A</td>
<td>1.2</td>
<td>0</td>
<td>100</td>
<td>0.3</td>
</tr>
<tr>
<td>C/A</td>
<td>1.2</td>
<td>4</td>
<td>100</td>
<td>0.3</td>
</tr>
<tr>
<td>C/A</td>
<td>1.2</td>
<td>9</td>
<td>100</td>
<td>0.3</td>
</tr>
<tr>
<td>C/A</td>
<td>1.2</td>
<td>12</td>
<td>100</td>
<td>0.3</td>
</tr>
<tr>
<td>C/A</td>
<td>1.2</td>
<td>15</td>
<td>100</td>
<td>0.3</td>
</tr>
<tr>
<td>C/A</td>
<td>0.8</td>
<td>0</td>
<td>100</td>
<td>0.3</td>
</tr>
<tr>
<td>C/A</td>
<td>0.8</td>
<td>4</td>
<td>100</td>
<td>0.3</td>
</tr>
<tr>
<td>C/A</td>
<td>0.8</td>
<td>9</td>
<td>100</td>
<td>0.3</td>
</tr>
<tr>
<td>C/A</td>
<td>0.6</td>
<td>0</td>
<td>100</td>
<td>0.3</td>
</tr>
<tr>
<td>C/A</td>
<td>0.6</td>
<td>4</td>
<td>100</td>
<td>0.3</td>
</tr>
<tr>
<td>C/A</td>
<td>0.6</td>
<td>9</td>
<td>100</td>
<td>0.3</td>
</tr>
</tbody>
</table>

![Fig. 8](image-url) The average jet mass $\langle M \rangle$ as a function of the number of reconstructed primary vertices for $W$-jet signal and multijet background, before and after grooming using anti-$k_t$, $R = 1.0$ trimmed with $f_{\text{cut}} = 0.05$ and $R_{\text{sub}} = 0.2$. The slopes of straight line fits are provided in each case: for ungroomed jets this is $\sim 2$ GeV per vertex, while for trimmed jets it is flat.
The soft-drop levels

\[ L_{SD}(\beta) \] are defined as the highest level of balance in the jet history

\[ z_g > z_{cut} \times r_g^\beta, \]  

(10)

where the fractional momentum of the softest of the two branches is \( z_g = \frac{\min(p_{T1}, p_{T2})}{p_{T1} + p_{T2}} \), and the fractional angular separation of the two branches (with respect to the \( R \) parameter of the initial jet algorithm, \( R_0 \)) is \( r_g = \frac{\Delta R_1}{R_0} \). Nine values of the \( z_{cut} \) parameter between 4 and 20% are explored here, given in Table 5. The \( \beta \) values chosen here are \(-1.0, -0.75, \) and \(-0.5\). The starting condition of Eq. 10 with \( z_{cut} = 4 \% \) is applied to the first step in the declustering. If this condition is not satisfied, the algorithm continues to the next step in the jet’s clustering history, and so on, checking if the condition is satisfied at any point. If it is not, the ‘soft-drop-level’, \( L_{SD}(\beta) \) is zero. If this condition is satisfied, \( L_{SD}(\beta) = 1 \). The algorithm then remains at this point in the clustering history and asks for the same condition with the harder momentum condition, \( z_{cut} = 6 \% \). If this condition is not satisfied, the algorithm continues to the next step in the jet’s clustering history, and so on.

- The dipolarity [25], \( D \), is a measure of the colour flow between two hard centres within a jet.
- Jet shape variables are computed in the centre-of-mass frame of a jet, which can increase the separation power between \( W \)-jets and jets in multijet events. Sphericity, \( S \), aplanarity, \( A \), and thrust minor and major, \( T_{\text{min}}, T_{\text{maj}} \), already used in a previous ATLAS measurement [26], as well as the ratio of the second to zeroth order Fox–Wolfram moments, \( R_2^{FW} \) [72] are considered.
- For a jet clustered with a given recombination jet clustering algorithm, the Q-jets technique [27] reclusters the jet many times for each step in the clustering. Following this, any jet observable, such as the mass, will have a distribution for a given jet. The Q-jets configuration optimised in Ref. [28] is adopted in this study. The high mass in \( W \)-jets tends to persist during the re-clustering while the mass of QCD jets fluctuates. A sensitive observable to this trend is the coefficient of variation of the mass distribution for a single jet, called the volatility [27,28], \( \nu^g \). The superscript \( g \) denotes the rigidity, which controls the sensitivity of the pair selection to the random number generation used in the clustering.

For all 27 jet collections and grooming algorithms described in Sect. 6.1, the full list of substructure variables described above are computed. The distributions of the three variables \( \tau_{\text{21}}^{\text{wta}}, C_2^{(\beta=1)} \) and \( D_1^{(\beta=1)} \) are shown in Figs. 10, 11, 12 for anti-\( k_t \), \( R = 1.0 \) jets trimmed with \( f_{\text{cut}} = 0.05 \) and \( R_{\text{sub}} = 0.2 \), after applying the 68% signal efficiency mass window requirement. This grooming algorithm is referred to in the remainder of this paper as ‘R2-trimming’. At this stage no jet mass calibrations have been applied for any of the grooming configurations. Also shown are the correlations between the

<table>
<thead>
<tr>
<th>( L_{SD}(\beta) )</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>6</th>
<th>7</th>
<th>8</th>
<th>9</th>
</tr>
</thead>
<tbody>
<tr>
<td>( z_{cut} )</td>
<td>4%</td>
<td>6%</td>
<td>8%</td>
<td>10%</td>
<td>12%</td>
<td>14%</td>
<td>16%</td>
<td>18%</td>
<td>20%</td>
</tr>
</tbody>
</table>

Table 5 The soft-drop levels \( L_{SD}(\beta) \) are defined as the highest level of balance in the jet history.
Fig. 10 The $C_2^{(\beta=1)}$ variable, for R2-trimmed jets: a distributions in signal (blue solid line) and background (red dashed) in MC in the range $350 < p_T < 500$ GeV, obtained after applying the 68% signal efficiency mass window requirement (discussed in Sect. 6.1); b correlation with the leading jet’s mass in (left) multijet background and (right) W-jet signal events. No truth-matching requirements are made, so the signal events can contain background jets as well as W-jets. The vertical line corresponds to the value of the cut providing a combined 50% efficiency for grooming and tagging (corresponding to a tagging-only efficiency of 50%/68% = 73.5%).
the jet mass to be within the mass window defined by the grooming.

6.4 Summary of grooming and substructure in MC

Four grooming configurations, given in Table 6, show consistently high performance in all \( p_T \) bins. The jet \( \eta \), mass and energy calibrations are derived for these four using a simulation-based calibration scheme, used as the standard one by ATLAS in previous studies [10]. The mass window sizes for calibrated jets, the background efficiencies for \( \epsilon_W = 68 \% \) and the \( \delta(M)/\delta\text{NPV} \) in the range \( 200 < p_T < 350 \text{ GeV} \) are also given in Table 6.

Since the first algorithm in Table 6 is the only one of the four with negligible pileup dependence across all \( p_T \) ranges (the central \( p_T \) range only is shown in Fig. 9), it is adopted for all successive studies.

The best substructure variables for use with R2-trimmed jets at the \( \epsilon_{G&T}^{W} = 50 \% \) working point, providing background efficiencies \( \epsilon_{\text{QCD}}^{G&T} \sim 2 \% \) (background rejection power \( \sim 50 \), in terms of Fig. 13) for jets with \( p_T > 350 \text{ GeV} \), are given in Table 7. Studies of the R2-trimmed grooming configuration and the three preferred substructure variables are described in the next section, where the results obtained from Monte Carlo simulations are compared to data.
7 Detailed studies of selected techniques in data

This section describes a comparison of the $W$-jet and multijet tagging efficiencies measured using three tagging variables $C_{2}^{β=1}$, $D_{2}^{β=1}$ and $τ_{wta}^{21}$ computed for the leading R2-trimmed jet in data and MC.

In data, a relatively pure sample of boosted, hadronically decaying $W$ bosons can be obtained from decays of top quark pairs in the lepton-plus-jets decay channel: $t\bar{t} \rightarrow W^+ b W^- \bar{b} \rightarrow ℓνq\bar{q}bb$. The selection requirements detailed in Sect. 5 are applied to events in data and MC, where relevant. The composition of the data and MC samples introduced in Sect. 4 is discussed in Sect. 7.1. Details of the event topology differences between the $t\bar{t}$ final state examined in this section and the $W'$ final state used in the preliminary optimisation studies are given in Sect. 7.2. The systematic uncertainties are discussed in Sect. 7.3, and the distributions of mass and substructure variables in data and MC are presented in Sect. 7.4. The signal and background efficiency estimation procedures and their uncertainties are detailed in Sect. 7.5. A summary of the signal and background tagging efficiencies measured in data and compared to MC is given in Sect. 7.6.

In all the following studies, events are categorised according to the leading, reconstructed R2-trimmed jet $p_T$ in three ranges: [200, 250], [250, 350], and [350, 500] GeV. This
For jets with \( P_T > 500 \) GeV, the background rejection rate is shown for all possible pairings of the 27 grooming configurations and 26 substructure variables. The error shown is obtained from the tail of the background distribution.

The optimised substructure variable for jet algorithm \( \tau = 50 \) events in data and in the MC sample details in Sect. 4. The \( \tau \) production cross-section differs from that used in the first stage of the optimisation in Sect. 6, which uses ungrouped C/A, range \( R = 2 \). The selection is extended to \( P_T > 500 \) GeV and different ranges; there are insufficient data above 500 GeV in the 2012 dataset. The low-

<table>
<thead>
<tr>
<th>( A )</th>
<th>( B )</th>
<th>( C )</th>
<th>( D )</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.1</td>
<td>0.2</td>
<td>0.3</td>
<td>0.4</td>
</tr>
<tr>
<td>0.5</td>
<td>0.6</td>
<td>0.7</td>
<td>0.8</td>
</tr>
<tr>
<td>0.9</td>
<td>1.0</td>
<td>1.1</td>
<td>1.2</td>
</tr>
</tbody>
</table>

**Background rejection \( @ e, \phi, T = 50\% \)**

- Trimmed
- Pruned
- Split-Filtered
Fig. 14 For jets with $350 < p_T < 500 \text{GeV}$, the signal efficiency versus background rejection power “ROC” curve for selected tagging variables (combined with the uncalibrated groomed mass window) on a subset of high-performance algorithms is shown. The endpoint at 68% signal efficiency is a result of the 68% mass window. The inset enlarges the high-efficiency region.

Table 6 The four favoured grooming configurations along with their mass windows (derived using calibrated jets), background efficiencies, and pileup dependence for $\epsilon_W = 68\%$ in the range $200 < p_T < 350 \text{GeV}$.

<table>
<thead>
<tr>
<th>Grooming configuration</th>
<th>$\epsilon_W = 68%$ mass range (GeV)</th>
<th>$\epsilon_{QCD}$ (%)</th>
<th>$\delta(M)/\delta \text{NPV}$ (GeV)</th>
</tr>
</thead>
<tbody>
<tr>
<td>anti-$k_t$, $R = 1.0$ trimmed $f_{cut} = 0.05$, $R_{sub} = 0.2$</td>
<td>61–93</td>
<td>11</td>
<td>0.1–0.2</td>
</tr>
<tr>
<td>anti-$k_t$, $R = 1.0$ trimmed $f_{cut} = 0.05$, $R_{sub} = 0.3$</td>
<td>65–99</td>
<td>16</td>
<td>0.5–0.6</td>
</tr>
<tr>
<td>C/A, $R = 1.0$ pruned $Z_{cut} = 0.15$, $R_{cut} = 0.5$</td>
<td>59–111</td>
<td>16</td>
<td>0.9–1.1</td>
</tr>
<tr>
<td>C/A, $R = 1.2$ split-filt $\sqrt{y_2} = 0.15$, $R_{sub} = 0.3$</td>
<td>63–103</td>
<td>13</td>
<td>0.1–0.3</td>
</tr>
</tbody>
</table>

Table 7 The mass windows for calibrated R2-trimmed jets that provide $\epsilon_W = 68\%$, and the requirements on the three substructure variables that result in the lowest background efficiencies $\epsilon_{G&T}^{\mu}$ when combined with the mass windows to provide $\epsilon_{G&T} = 50\%$.

<table>
<thead>
<tr>
<th>Variable</th>
<th>Tagging criteria in $p_T$ range</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\epsilon_W = 68%$ mass range</td>
<td>61–93 GeV</td>
</tr>
<tr>
<td>$\epsilon_{G&amp;T}^{\mu} = 50% C_2^{(\beta=1)}$</td>
<td>&lt;0.18</td>
</tr>
<tr>
<td>$\epsilon_{G&amp;T}^{\mu} = 50% D_2^{(\beta=1)}$</td>
<td>&lt;1.14</td>
</tr>
<tr>
<td>$\epsilon_{G&amp;T}^{\mu} = 50% \tau_2^{21}$</td>
<td>&lt;0.32</td>
</tr>
</tbody>
</table>

section is scaled to match the value obtained from NNLO calculations [73]. An additional reweighting is then applied to the $t\bar{t}$ MC using the generator-level $p_T$ of the top quark and the $p_T$ of the $t\bar{t}$ system to reproduce the $p_T$-dependence of the measured cross-section [74].

The leading backgrounds to the $t\bar{t}$ event topology come from $t\bar{t}$ production where there is only partial reconstruction of the $W$ boson decay, with or without contamination from radiation outside of the top quark decay (such as hard gluon emission, non-tagged $b$-jets). Generator-level information from the $t\bar{t}$ and $Wt$ samples is used to distinguish the cases where the $W$ candidate jet is matched to a genuine $W$ boson or to other jets (referred to as top quark background events). An event is categorised as belonging to the $W$ signal when both partons from the $W$ boson decay are within $\Delta R = 1.0$ of the jet axis; otherwise, the event is labelled as non-$W$ background.

The leading non-top background process is production of $W$ bosons in association with jets. The $W$+jets contribution is estimated using a data-driven charge asymmetry method [75]. ALPGEN + PYTHIA MC samples provide the event kinematics, and the relative flavour contributions and overall normalisation are determined from data. The flavour fractions are found using a control region in which there is no $b$-tagged jet requirement and instead of requiring a large-$R$ jet, events are required to have exactly two small-$R$ jets. The
relative contributions from each jet flavour are found using the charge asymmetry and the flavour fractions are fixed for W+jets events in the signal region before the b-tagged jet requirement is applied. Finally, an overall normalisation is obtained by scaling the simulated W+jets charge asymmetry to match the charge asymmetry in data, after other charge-asymmetric backgrounds are accounted for using MC.

The contribution from multijet events to the sample composition is estimated by using loose lepton identification criteria and deriving the contribution of non-prompt leptons using the matrix method [76,77]. This method relies on the fact that the tight lepton identification criteria selects primarily prompt leptons, while loose leptons that do not satisfy the tight criteria are primarily from backgrounds. The probabilities for a non-prompt lepton from multijet production which satisfies the loose/tight identification criteria are measured from data in control regions dominated by multijet events, with prompt-lepton contributions subtracted based on MC. The corresponding probabilities for a lepton from prompt sources (such as W bosons) which satisfies the loose/tight identification criteria are derived from MC samples, corrected using data-to-MC correction factors derived from Z → ℓℓ events. Once the fraction of events satisfying the different identification criteria is known, an event weight is calculated and applied to data events with the loosened lepton identification criteria to provide an estimate of the multijet contribution.

7.2 Event topology effects in Monte Carlo simulations

The preliminary MC-based optimisation studies in Sect. 6 use a signal composed of well-isolated W-jets from the hypothetical process W′ → WZ → qqℓℓ provided by PYTHIA and a background sample of jets initiated by light quarks or gluons, also provided by PYTHIA. In the following sections, efficiencies are measured in data, so the ℓℓ final state is used as a source of W-jets. As described in Sect. 4, the main ℓℓ signal processes are provided by either POWHEG-BOX + PYTHIA or MC@NLO + HERWIG and the multijet background is provided by PYTHIA or by HERWIG++.

Despite the backgrounds in both event topologies being PYTHIA multijets, they are different in that the background efficiencies obtained in data include a leading-jet minimum pT requirement of 450 GeV in order to ensure full efficiency with respect to the trigger used. With this selection, the lower pT ranges, [200, 250] and [250, 350] GeV, are composed entirely of sub-leading jets, and the highest pT bin, [350, 500] GeV, is a mixture of leading and sub-leading jets. Jets softer than the sub-leading jet are not considered. In the background sample used for the studies in Sect. 6 there is no comparison with data, thus there are no trigger requirements and the leading jet is always shown. A higher average jet mass is observed in the leading + sub-leading jet selection than with the leading-jet selection. This in turn leads to a higher background efficiency for the studies summarised in Sect. 7 than for those in Sect. 6.4. These differences are relevant in that leading and sub-leading jets have different flavour compositions (light-quark versus gluon). Gluon-initiated jets have higher average mass than quark-initiated jets [78].

The signal event topologies are more obviously different, with the W′ process producing potentially more isolated W-jets than those found in the ℓℓ final state. The W bosons produced in the W′ decay are also generally longitudinally polarised, making them potentially easier to distinguish from multijet background than W-jets from top decays, which are produced in both the longitudinal and transverse modes [11, 63].

The signal efficiency versus background rejection curves in the two different event topologies, including the differences in both signal and background, are shown in Fig. 15. The curves for tagging W-jets from the W′ against a leading-jet background indicate better performance in this event topology, with the magnitude of the difference depending on the substructure variable used for tagging. Figure Fig. 16 shows the curves again, but this time the leading jet from the PYTHIA multijet background is used in both cases, thus removing the differences in background efficiencies, and isolating the differences resulting from the different signal event topologies. With identical background compositions, the performance is generally slightly better in the POWHEG-BOX ℓℓ sample.
The systematic uncertainty on the JSS is needed in order to derive the full systematic uncertainties on the signal and background efficiencies. Uncertainties are derived using in situ methods by comparing the measured calorimeter jet energy, mass and substructure variables to the same quantities measured by well-calibrated and completely independent detectors in both data and MC, using the double ratio:

\[
\langle X^{\text{jet}} / X^{\text{ref}} \rangle_{\text{data}} / \langle X^{\text{jet}} / X^{\text{ref}} \rangle_{\text{MC}}
\]

where \(X\) denotes a jet variable. In this case, track-jets are used as reference objects, since tracks from charged hadrons are well-measured and are independent of the calorimeter. In addition, the use of track-jets, where tracks are required to come from the hard scattering vertex, suppresses pileup effects. A geometrical matching in the \(\eta-\phi\) plane is applied to associate track-jets with calorimeter-jets. This approach was widely used in the measurement of the jet mass and substructure properties of jets in the 2011 data [10]. Performance studies have also shown that there is excellent agreement between the measured positions of clusters and tracks in data, indicating no systematic misalignment between the calorimeter and the inner detector. This technique achieves a precision of around 3–7 % in the central detector region, which is dominated by systematic uncertainties arising from the inner-detector tracking efficiency and MC modelling uncertainties of the charged and neutral components of jets.

The double ratio of Eq. (11) is computed for two different MC generators, PYTHIA and HERWIG++, and the largest disagreement between data and each of the MC generators is taken as a modelling uncertainty. The total uncertainty is then obtained by adding in quadrature this modelling uncertainty to the tracking efficiency uncertainty. Specific uncertainties for tracks inside the core of dense jets are not needed here, because only jets with \(p_T < 1\) TeV are considered. The scale uncertainties for the jet energy, mass and substructure variables are derived in ranges of the \(p_T, \eta, M/p_T\) of the reconstructed calorimeter jet.

Figure 18 shows a set of six representative distributions for \(c_2^{(b=1)}, D_2^{(b=1)}\) and \(t_{21}^{\text{eta}}\) in the range \(350 < p_T < 500\) GeV. The mean values of the single-ratio \(X^{\text{jet}} / X^{\text{ref}}\) distributions are shown as a function of the jet mass, along with the distributions of \(X^{\text{jet}} / X^{\text{ref}}\) themselves within the relevant \(\epsilon_W^G \sim 68\%\) mass window.

Large discrepancies between data and MC are observed for low-mass jets, while for masses around 80 GeV the data/MC agreement is within 5 %. In the distributions of \(X^{\text{jet}} / X^{\text{ref}}\) it is noticed that while the tails of the ratio distributions show discrepancies between data and the MC, the agreement is good for values of the ratio close to one, which represents the large majority of events. In summary, the scale uncertainty of the three jet substructure variables ranges between 1 and 5 % in the different kinematic regions.
from MC sources listed in Table 9 and described in Sect. 7.5. The R2-trimmed jet mass distributions for signal candidates in the range.

Fig. 17 The R2-trimmed jet mass distributions for signal W-jet candidates in the range. a 200 < pt < 250 GeV, and b 350 < pt < 500 GeV, and multijet background candidates (c, d) in the same ranges. The W-jets are taken from the processes W → W, Z (solid black), and t¯t events provided by POWHEG-BOX (dotted red). Two kinds of PYTHA multijets are shown: the solid black line is for the leading jets and the dotted red line is for the leading and sub-leading jets. The ratios between the models is shown at the bottom. The inclusion of sub-leading jets, which are more likely to be initiated by gluons, results in higher-mass jets. The vertical lines represent the signal mass window.

Additional, sub-dominant systematic uncertainties come from MC sources listed in Table 9 and described in Sect. 7.5 in terms of the uncertainty on the final measured signal and background efficiencies. The full systematic uncertainty on the mass and substructure variables are obtained by adding each of the scale, resolution, statistical and MC uncertainties in quadrature.

7.4 Mass and substructure distributions in t¯t events

The jet mass distribution for the leading R2-trimmed jets in events satisfying the pre-selection criteria in Sect. 5 are shown in Fig. 19. The data and events in POWHEG-BOX + PYTHA and MC@NLO + HERWIG simulations agree within the uncertainties detailed in Sect. 7.3. Distributions of the three tagging variables C2(β=1), D2(β=1) and τw are shown for the same pre-selection criteria, before and after making the relevant requirements for the pt range in question, in Fig. 20. These variables are used to define medium and tight tagging criteria, where the medium working point provides a signal efficiency of εG&T = 50% and the tight working point provides εG&T = 25%.

The jet mass distributions of the W boson candidates satisfying or failing to satisfy the medium signal efficiency requirement for each of the three substructure variables are...
shown in Fig. 21. The mass distribution for jets failing the \( C^{(β=1)}_2 \) tagger (Fig. 21a) is notably different from the mass distributions for jets that fail the \( D^{(β=1)}_2 \) and/or \( \tau^{\text{wta}}_{21} \) taggers, with a significantly higher mass peak and a low-mass tail that is conspicuous in its absence. This effect can be understood by referring back to Fig. 10b: the correlation between
the mass and $C_2^{(\beta=1)}$ is strong for background jets with low masses, while there is no clear correlation in the signal mass region. This means that the $C_2^{(\beta=1)}$ variable performs well when combined with a mass window, but is not very effective without the mass constraint.

7.5 Signal and background efficiencies and uncertainties

Background efficiencies are measured in a multijet-enriched sample of data, using the large-$R$ trigger and event selection described in Sect. 5.

The systematic uncertainties on the background efficiency measurements in multijet events are summarised in Table 8. The uncertainties are propagated coherently through to the measurement and then added together in quadrature. The background efficiency uncertainty due the JSS uncertainty can be as large as ~25% for jets with $p_T > 500$ GeV and is about 15–20% in the lower $p_T$ ranges for the scale uncertainty on $D_2^{(\beta=1)}$. The background efficiency uncertainties from the JMS are, in general, larger than those from the JES and are of the order of 6–10 and 2–9%, respectively. The impact of JER and JMR uncertainties is much smaller than that of the scale uncertainties.

Signal efficiencies are extracted from data by performing a template fit to the mass distributions of jets that satisfy or fail to satisfy the requirement on the given tagging variable. The signal template is constructed using the POWHEG-BOX + PYTHIA $t\bar{t}$ events, requiring that both partons from the W boson decay in the event record are within $\Delta R = 1.0$ of the jet axis. The mass templates for the background are composed of decays of $W$ bosons from top quarks, where not all the decay products fall inside the jet cone, and the other non-$W$ backgrounds are also estimated using POWHEG-BOX + PYTHIA. The normalisations of both templates are allowed to float.

The statistical uncertainty on the efficiency measurement in data includes the statistical uncertainty of the templates. For most sources of systematic uncertainty, a variation of the fit is performed with templates modified by $\pm 1\sigma$. In the case of the JMS, this variation is between $\pm 0.5\sigma$ and $\pm 1.0\sigma$; this reduction in the uncertainty with respect to that obtained with the standard double-ratio technique is made possible by fitting the mass distributions in data to a number of different templates. The templates are obtained by shifting the jet mass up and down by fractions (0.25–1.0) of $\sigma$. The $\chi^2/ndf$ fit quality of each template is calculated, and a parabolic fit performed to the $\chi^2/ndf$ as a function of the fraction of $\sigma$. The fraction of $\sigma$ that results in a one unit shift from that which minimises $\chi^2/ndf$ is used as the uncertainty on the JMS for the signal efficiency calculation.

The full set of contributions to the systematic uncertainty on the signal efficiency is summarised in Table 9, after applying the mass and $D_2^{(\beta=1)}$ medium tagging requirements. As in the background efficiency uncertainty estimate, the JSS contributes the largest uncertainty on this efficiency, varying between 3 and 5% for the $D_2^{(\beta=1)}$ scale. The contribution from the JMR is $\sim 3\%$. The contribution from JER is less significant than JMR, being negligible in the lowest $p_T$ bin and $\sim 1\%$ for jets with $250 < p_T < 500$ GeV. The contribution from JMS variations is also $\sim 1\%$ (symmetrised as a result of the profiling technique) and increases to $\sim 10\%$ in the highest $p_T$ range (350 < $p_T$ < 500 GeV). The uncertainty from the JES is around 2–4%.

In addition to the scale and resolution uncertainties, two other types of uncertainty are considered for the signal efficiency measurement: (a) $t\bar{t}$ modelling—initial-state radiation (ISR), final-state radiation (FSR), and generator uncertainty; (b) the normalisation of the main background sources—multijet, $W$+jets, partial-$W$ and non-$W$ in single top and $t\bar{t}$.

The generator uncertainty is taken into account as the difference between the signal efficiency measurement using the MC@NLO + HERWIG mass templates for the signal instead of the default POWHEG-BOX + PYTHIA ones. These uncertainties are between 1 and 3%. The modelling uncertainty of the QCD radiation is estimated using ACERMC [80] v3.8 plus PYTHIA v6.426 MC samples by varying the parame-
Fig. 20 Distributions of the $W$ candidate jet substructure variables before (left) and after (right) the $C^G_W = 68\%$ mass window for selected lepton+jets $t\bar{t}$ events in data and POWHEG-BOX + PYTHIA MC for the combined electron and muon channel. a, b $C_2^{(\beta = 1)}$, c, d $D_2^{(\beta = 1)}$ and e, f $\tau_{21}^{WTA}$. Data points are shown with statistical uncertainties, and the combined MC is shown with full systematic and statistical uncertainties. The lower panels show the data/MC ratios, with the statistical uncertainty on the MC given in black forward-slashed bands, and the full systematic uncertainty given in the blue, back-slashed bands.
Fig. 21 The distribution of the $W$ candidate mass for R2-trimmed jets failing (left) and passing (right) the selection corresponding to $\epsilon_{G&T} = 50\%$ for the combined electron and muon channel in the $p_T$ range 200–250 GeV, without application of the mass cut. In a, b, the variable used for selection is $C_2^{(\beta=1)}$, in c and d it is $D_2^{(\beta=1)}$, and in e, f it is $\tau_{21}^{\text{NS}}$. Data points are shown with statistical uncertainties, and the combined MC is shown with full systematic and statistical uncertainties. The lower panels show the data/MC ratios, with the statistical uncertainty on the MC given in black forward-slashed bands, and the full systematic uncertainty given in the blue, back-slashed bands.
ters controlling the ISR and FSR in a range consistent with a previous ATLAS measurement [81]. The resulting uncertainties on the signal efficiency increase with jet $p_T$ and are 2–6%. The normalisation uncertainties for the main background sources are evaluated using a $\pm 1\sigma$ variation of the cross-section. The normalisation uncertainties are negligible with respect to the scale and resolution uncertainties, and for the $t\bar{t}$ signal and W+jets background they are <1%.

7.6 Summary of W boson tagging efficiencies in data and MC

The $W$-jet tagging efficiency in $t\bar{t}$ events using the R2-trimmed jet mass window and the medium and tight $C_2^{\beta=1}$ selections is measured in top-enriched data and in MC provided by POWHEG-BOX + PYTHIA and MC@NLO + HERWIG. The background efficiency with the same selection is measured in multijet-enriched data and in PYTHIA and HERWIG++ simulations. The results of these measurements are shown in Fig. 22. In both the signal and background efficiency distributions, the ratio of data to each of the two MC models is shown in the lower panels. The corresponding signal and background efficiency distributions for $D_2^{\beta=1}$ and $\tau_{21}^{\text{G&T}}$ are shown in Figs. 23 and 24 respectively. Systematic errors from background modeling are added for the signal data points, while no background modeling is involved in the derivation of background efficiencies, whose points only show statistical error. Good agreement is observed between data and predictions.

The signal efficiency at the medium working point is not exactly 50% because the selection requirements for the $e_W^{G&T} = 50\%$ working point are calculated using $W$-jets from $W' \rightarrow WZ \rightarrow qq\ell\ell$ events, and are applied here to W-jets in $t\bar{t}$ events.

The data points are the result of fits using templates extracted from POWHEG-BOX + PYTHIA; the difference with respect to the results that would be obtained using templates from MC@NLO + HERWIG is added in quadrature as an additional source of systematic uncertainty.

The $D_2^{\beta=1}$ tagger has the smallest background efficiency for the medium and tight working points in all $p_T$ ranges except for the lowest, $200 < p_T < 250\text{ GeV}$. The background efficiencies decrease with increasing $p_T$, with the exception of the $C_2^{\beta=1}$ tagger, for which the background efficiency increases for jets in the range $250 < p_T < 350\text{ GeV}$. This behaviour can be explained by the stronger uncertainties on scales (JMS, JES and JSS indicate the mass, energy and substructure scale uncertainties) can be in both directions, and so result in pairs of efficiency uncertainties. The mass and energy resolution uncertainties are denoted JMR and JER respectively. The contributions from each source are added in quadrature to get the total uncertainty on $e_W^{G&T}$.
Fig. 22  W boson tagging efficiencies in ranges of jet $p_T$ for (left) signal $W$-jets in $t\bar{t}$ events and (right) multijet background. The $\epsilon_{W}^{\text{G&T}} \sim 50\%$ working points obtained with the combined mass window and $C_2^{(\beta=1)}$ requirements are shown in (a) and (b), and the $\sim 25\%$ working points are shown in (c), (d). The deviations from 50 and 25\% in (a) and (c) respectively are due to the optimisations being based on $W$-jets in a different $W'$ → $WZ$ topology, as discussed in the text. The lower panels show ratios of the efficiency measured in data to the efficiency in two different MC simulations.
Fig. 23 $W$ boson tagging efficiencies in ranges of jet $p_T$ for (left) signal $W$-jets in $t\bar{t}$ events and (right) multijet background. The $\epsilon_{G&T}^{W} \sim 50$% working points obtained with the combined mass window and $D_2^{(β=1)}$ requirements are shown in a and b, and the $\sim 25$% working points are shown in c, d. The deviations from 50 and 25 in a and c respectively are due to the optimisations being based on $W$-jets in a different $W' \rightarrow WZ$ topology, as discussed in the text. The lower panels show ratios of the efficiency measured in data to the efficiency in two different MC simulations.
Fig. 24  W boson tagging efficiencies in ranges of jet $p_T$ for (left) signal $W$-jets in $t\bar{t}$ events and (right) multijet background. The $\epsilon_{G&T}^{W} \sim 50\%$ working points obtained with the combined mass window and $t_{\tau_1}^{\text{sub}}$ requirements are shown in a and b, and the $\sim 25\%$ working points are shown in c, d. The deviations from 50 and 25% in a and c respectively are due to the optimisations being based on $W$-jets in a different $W' \to WZ$ topology, as discussed in the text. The lower panels show ratios of the efficiency measured in data to the efficiency in two different MC simulations.
Fig. 25 Signal efficiency versus background rejection power (1/background efficiency) curves derived using POWHEG-BOX + PYTHIA signal efficiencies and PYTHIA background efficiencies compared with points from data. Three $p_T$ ranges are shown: a 200–250 GeV, b 250–350 GeV, and c 350–500 GeV. The data points include systematic uncertainties on the signal efficiency measurement in $t\bar{t}$ events and the uncertainties on the PYTHIA background efficiency predictions.

The $p_T$ dependence of the $C_2^{(\beta=1)}$ tagger compared to the $D_2^{(\beta=1)}$ and $r_{21}^\text{G\&T}$ taggers.

For the signal efficiencies, the uncertainty bands of the ratios account for the correlations in the systematic uncertainties between data and MC. In general, data and POWHEG-BOX + PYTHIA agree better than data and MC@NLO + HERWIG. For the medium working point, there is agreement between the two MC models within 1σ except in the range $200 < p_T < 250$ GeV, while for the tight working point ($C_2^{G\&T}$ ~ 25%) the efficiency of MC@NLO + HERWIG is 1.5σ to 2σ higher than both the efficiency predicted by POWHEG-BOX + PYTHIA and the measurements in data. There is a potential bias towards POWHEG-BOX + PYTHIA, as this generator provides the signal template used in determining the background subtraction that is necessary to define the signal efficiency in data. However, even when using MC@NLO + HERWIG for the templates in the subtraction, POWHEG + PYTHIA gives a better description of the signal efficiency measured in data. The differences in the MC signal efficiencies stem from the differences in the signal mass distributions between models; the mass peak has a different width, so the fraction of signal in the mass window (which is the same for both Monte Carlo samples) is already significantly different after the requirement on the groomed jet mass is applied (see for example Fig. 17).

Figure 25 shows the $t\bar{t}$ MC efficiency versus rejection curves with data measurements at the medium and tight working points, including systematic uncertainties on the sig-
nal and background efficiencies. Generally good agreement between data and MC simulation is observed in all $p_T$ ranges for these measurements.

8 Conclusions

Several combinations of jet grooming algorithms and tagging variables have been studied to find an optimal $W$-jet tagger in terms of (a) maximising multijet background rejection power for given values of $W$-jet signal efficiency; (b) minimising systematic uncertainties and the effects of pileup; and (c) the modelling of the jet mass and substructure variables in Monte Carlo simulations.

The signal efficiency working point $\epsilon_G^{W} = 68\%$ is chosen as a suitable baseline for the comparison of grooming algorithms. The performances of the best few configurations of trimming, pruning and split-filtering are similar at this working point, and the anti-$k_T$, $R = 1.0$ jet trimmed with $f_{cut} = 5\%$ and $R_{sub} = 0.2$ (‘R2-trimming’) does particularly well in terms of removing pileup-dependence. Cambridge-Aachen pruning also provides significant discrimination for $W$-jet tagging, as does split-filtering without the mass-drop requirement. The irrelevance of the mass-drop requirement was shown previously in phenomenological studies [82], and is verified here in MC samples with a full ATLAS detector simulation. Trimming with $R_{sub} = 0.1$ shows promise in terms of the jet mass; it is not pursued further in these studies because it is challenging in terms of systematic uncertainties, as one is entering the arena of single-cluster jet, but it may well be considered in future extensions of these studies (for example in tagging $W$ bosons with $p_T > 1$ TeV).

The energy correlation ratios $D_2^{(\beta=1)}$, $C_2^{(\beta=1)}$ are found to be particularly good variables for tagging $W$-jets, as shown for the first time here in data. However, there is some evidence of the $C_2^{(\beta=1)}$ variable having a higher background efficiency for low-$p_T$ jets. Similarly good is the N-subjettiness ratio $\tau_{21}^{wta}$, which performs better than its predecessor $\tau_{21}$.

The signal and background efficiencies obtained using pairwise combinations of the R2-trimmed mass and three different substructure variables are measured in $t\bar{t}$ and multijet events from 20.3 fb$^{-1}$ of 8 TeV $pp$ collisions recorded by ATLAS at the LHC. These are compared to various MC predictions which show in general good agreement within the uncertainties with the data measurements of signal efficiencies around 50% for background efficiencies around 2%.

In some configurations, significant differences are observed in both the signal and background efficiencies from different Monte Carlo predictions. This can provide important information to improve the Monte Carlo simulations for searches for physics beyond the Standard Model. It further highlights the potential for data measurements such as these to be utilised for tuning Monte Carlo simulations.

These studies are necessarily limited in scope to comparing simple two-variable taggers, made up of a groomed mass window and a substructure variable requirement, both of which are sensitive to $p_T$ and therefore optimised for three different $p_T$ ranges. Extensions to these studies could include combining three or more variables and using multivariate techniques to further boost the signal efficiency and/or reduce the background; investigating how these conclusions change if dedicated pileup-removal techniques are used alongside grooming; and varying the $\epsilon_G^{W}$ baseline at which the grooming algorithms are compared.

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26 (a) Transilvania University of Brasov, National Institute of Physics and Nuclear Engineering, Brasov, Romania; (b) National Institute of Physics and Nuclear Engineering, Bucharest, Romania; (c) Physics Department, National Institute for Research and Development of Isotopic and Molecular Technologies, Cluj Napoca, Romania; (d) University Politehnica Bucharest, Bucharest, Romania; (e) West University in Timisoara, Timisoara, Romania
27 Departamento de Física, Universidad de Buenos Aires, Buenos Aires, Argentina
28 Cavendish Laboratory, University of Cambridge, Cambridge, UK
29 Department of Physics, Carleton University, Ottawa, ON, Canada
30 CERN, Geneva, Switzerland
31 Enrico Fermi Institute, University of Chicago, Chicago, IL, USA
32 (a) Departamento de Física, Pontificia Universidad Católica de Chile, Santiago, Chile; (b) Departamento de Física, Universidad Técnica Federico Santa María, Valparaíso, Chile
33 (a) Institute of High Energy Physics, Chinese Academy of Sciences, Beijing, China; (b) Department of Modern Physics, University of Science and Technology of China, Hefei, Anhui, China; (c) Department of Physics, Nanjing University, Nanjing, Jiangsu, China; (d) School of Physics, Shandong University, Jinan, Shandong, China; (e) Shanghai Key Laboratory for Particle Physics and Cosmology, Department of Physics and Astronomy, Shanghai Jiao Tong University, Shanghai, China; (f) Physics Department, Tsinghua University, Beijing 100084, China
34 Laboratoire de Physique Corpusculaire, Clermont Université et Université Blaise Pascal and CNRS/IN2P3, Clermont-Ferrand, France
35 Nevis Laboratory, Columbia University, Irvington, NY, USA
36 Niels Bohr Institute, University of Copenhagen, Copenhagen, Denmark
37 (a) INFN Gruppo Collegato di Cosenza, Laboratori Nazionali di Frascati, Frascati, Italy; (b) Dipartimento di Fisica, Università della Calabria, Rende, Italy
38 (a) Faculty of Physics and Applied Computer Science, AGH University of Science and Technology, Kraków, Poland; (b) Marian Smoluchowski Institute of Physics, Jagiellonian University, Kraków, Poland
39 Institute of Nuclear Physics, Polish Academy of Sciences, Kraków, Poland
40 Physics Department, Southern Methodist University, Dallas, TX, USA
41 Physics Department, University of Texas at Dallas, Richardson, TX, USA
42 DESY, Hamburg and Zeuthen, Germany
43 Institut für Experimentelle Physik IV, Technische Universität Dortmund, Dortmund, Germany
44 Institut für Kern- und Teilchenphysik, Technische Universität Dresden, Dresden, Germany
45 Department of Physics, Duke University, Durham, NC, USA
46 SUPA-School of Physics and Astronomy, University of Edinburgh, Edinburgh, UK
47 INFN Laboratori Nazionali di Frascati, Frascati, Italy
48 Fakultät für Mathematik und Physik, Albert-Ludwigs-Universität, Freiburg, Germany
49 Section de Physique, Université de Genève, Geneva, Switzerland
50 (a) INFN Sezione di Genova, Genoa, Italy; (b) Dipartimento di Fisica, Università di Genova, Genoa, Italy
51 (a) E. Andronikashvili Institute of Physics, Iv. Javakhishvili Tbilisi State University, Tbilisi, Georgia; (b) High Energy Physics Institute, Tbilisi State University, Tbilisi, Georgia
52 II Physikalisches Institut, Justus-Liebig-Universität Giessen, Giessen, Germany
53 SUPA-School of Physics and Astronomy, University of Glasgow, Glasgow, UK
54 II Physikalisches Institut, Georg-August-Universität, Göttingen, Germany
55 Laboratoire de Physique Subatomique et de Cosmologie, Université Grenoble-Alpes, CNRS/IN2P3, Grenoble, France
56 Department of Physics, Hampton University, Hampton, VA, USA
57 Laboratory for Particle Physics and Cosmology, Harvard University, Cambridge, MA, USA
58 (a) Kirchhoff-Institut für Physik, Ruprecht-Karls-Universität Heidelberg, Heidelberg, Germany; (b) Physikalisches Institut, Ruprecht-Karls-Universität Heidelberg, Heidelberg, Germany; (c) ZITI Institut für technische Informatik, Ruprecht-Karls-Universität Heidelberg, Mannheim, Germany
59 Faculty of Applied Information Science, Hiroshima Institute of Technology, Hiroshima, Japan
60 (a) Department of Physics, The Chinese University of Hong Kong, Shatin, NT, Hong Kong; (b) Department of Physics, The University of Hong Kong, Pokfulam, Hong Kong; (c) Department of Physics, The Hong Kong University of Science and Technology, Clear Water Bay, Kowloon, Hong Kong, China
61 Department of Physics, Indiana University, Bloomington, IN, USA
62 Institut für Astro- und Teilchenphysik, Leopold-Franzens-Universität, Innsbruck, Austria
114 Department of Physics, Oklahoma State University, Stillwater, OK, USA  
115 Palacký University, RCPITM, Olomouc, Czech Republic  
116 Center for High Energy Physics, University of Oregon, Eugene, OR, USA  
117 LAL, Université Paris-Sud and CNRS/IN2P3, Orsay, France  
118 Graduate School of Science, Osaka University, Osaka, Japan  
119 Department of Physics, University of Oslo, Oslo, Norway  
120 Department of Physics, Oxford University, Oxford, UK  
121 (a) INFN Sezione di Pavia, Pavia, Italy; (b) Dipartimento di Fisica, Università di Pavia, Pavia, Italy  
122 Department of Physics, University of Pennsylvania, Philadelphia, PA, USA  
123 National Research Centre “Kurchatov Institute” B.P.Konstantinov Petersburg Nuclear Physics Institute, St. Petersburg, Russia  
124 (a) INFN Sezione di Pisa, Pisa, Italy; (b) Dipartimento di Fisica E. Fermi, Università di Pisa, Pisa, Italy  
125 Department of Physics and Astronomy, University of Pittsburgh, Pittsburgh, PA, USA  
126 (a) Laboratório de Instrumentação e Física Experimental de Partículas-LIP, Lisbon, Portugal; (b) Faculdade de Ciências, Universidade de Lisboa, Lisbon, Portugal; (c) Department of Physics, University of Coimbra, Coimbra, Portugal; (d) Centro de Física Nuclear da Universidade de Lisboa, Lisbon, Portugal; (e) Dipartimento di Fisica, Università di Roma, Braga, Portugal; (f) Departamento de Fisica Teorica y del Cosmos and CAFPE, Universidad de Granada, Granada, Spain; (g) Dep Física and CEFITEC of Faculdade de Ciencias e Tecnologia, Universidade Nova de Lisboa, Caparica, Portugal  
127 Institute of Physics, Academy of Sciences of the Czech Republic, Prague, Czech Republic  
128 Czech Technical University in Prague, Prague, Czech Republic  
129 Faculty of Mathematics and Physics, Charles University in Prague, Prague, Czech Republic  
130 State Research Center Institute for High Energy Physics, Protvino, Russia  
131 Particle Physics Department, Rutherford Appleton Laboratory, Didcot, UK  
132 (a) INFN Sezione di Roma, Rome, Italy; (b) Dipartimento di Fisica, Sapienza Università di Roma, Rome, Italy  
133 (a) INFN Sezione di Roma Tor Vergata, Rome, Italy; (b) Dipartimento di Fisica, Università di Roma Tor Vergata, Rome, Italy  
134 (a) INFN Sezione di Roma Tre, Rome, Italy; (b) Dipartimento di Matematica e Fisica, Università Roma Tre, Rome, Italy  
135 (a) Faculté des Sciences Ain Chock, Réseau Universitaire de Physique des Hautes Energies-Université Hassan II, Casablanca, Morocco; (b) Centre National de l’Energie des Sciences Techniques Nucleaires, Rabat, Morocco; (c) Faculté des Sciences Semlalia, Université Cadi Ayyad, LPHEA-Marrakech, Marrakech, Morocco; (d) Faculté des Sciences, Université Mohamed Premier and LPTPM, Oujda, Morocco; (e) Faculté des Sciences, Université Mohammed V, Rabat, Morocco  
136 DSM/IRFU (Institut de Recherches sur les Lois Fondamentales de l’Univers), CEA Saclay (Commissariat à l’Energie Atomique et aux Energies Alternatives), Gif-sur-Yvette, France  
137 Santa Cruz Institute for Particle Physics, University of California Santa Cruz, Santa Cruz, CA, USA  
138 Department of Physics, University of Washington, Seattle, WA, USA  
139 Department of Physics and Astronomy, University of Sheffield, Sheffield, UK  
140 Department of Physics, Shinshu University, Nagano, Japan  
141 Fachbereich Physik, Universität Siegen, Siegen, Germany  
142 Department of Physics, Simon Fraser University, Burnaby, BC, Canada  
143 SLAC National Accelerator Laboratory, Stanford, CA, USA  
144 (a) Faculty of Mathematics, Physics and Informatics, Comenius University, Bratislava, Slovak Republic; (b) Department of Subnuclear Physics, Institute of Experimental Physics of the Slovak Academy of Sciences, Kosice, Slovak Republic  
145 (a) Department of Physics, University of Cape Town, Cape Town, South Africa; (b) Department of Physics, University of Johannesburg, Johannesburg, South Africa; (c) School of Physics, University of the Witwatersrand, Johannesburg, South Africa  
146 (a) Department of Physics, Stockholm University, Stockholm, Sweden; (b) The Oskar Klein Centre, Stockholm, Sweden  
147 Physics Department, Royal Institute of Technology, Stockholm, Sweden  
148 Departments of Physics and Astronomy and Chemistry, Stony Brook University, Stony Brook, NY, USA  
149 Department of Physics and Astronomy, University of Sussex, Brighton, UK  
150 School of Physics, University of Sydney, Sydney, Australia  
151 Institute of Physics, Academia Sinica, Taipei, Taiwan  
152 Department of Physics, Technion: Israel Institute of Technology, Haifa, Israel
x Also at Hellenic Open University, Patras, Greece
y Also at Institute of Physics, Academia Sinica, Taipei, Taiwan
z Also at LAL, Université Paris-Sud and CNRS/IN2P3, Orsay, France
aa Also at Academia Sinica Grid Computing, Institute of Physics, Academia Sinica, Taipei, Taiwan
ab Also at School of Physics, Shandong University, Shandong, China
ac Also at Moscow Institute of Physics and Technology State University, Dolgoprudny, Russia
ad Also at Section de Physique, Université de Genève, Geneva, Switzerland
ae Also at International School for Advanced Studies (SISSA), Trieste, Italy
af Also at Department of Physics and Astronomy, University of South Carolina, Columbia, SC, USA
ag Also at School of Physics and Engineering, Sun Yat-sen University, Guangzhou, China
ah Also at Faculty of Physics, M.V. Lomonosov Moscow State University, Moscow, Russia
ai Also at National Research Nuclear University MEPhI, Moscow, Russia
aj Also at Department of Physics, Stanford University, Stanford CA, USA
ak Also at Institute for Particle and Nuclear Physics, Wigner Research Centre for Physics, Budapest, Hungary
al Also at University of Malaya, Department of Physics, Kuala Lumpur, Malaysia

* Deceased