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### Modelling with cellular automata: problem solving environments and multidimensional applications

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