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Publication date
2024

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Citation for published version (APA):

Levering, N. A. C. (2024). *Modeling and control of congestion phenomena*. [Thesis, fully internal, Universiteit van Amsterdam].

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Nikki Levering

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Printed by: Ipskamp Printing

The research for/publication of this doctoral thesis received financial assistance from the Dutch Research Council (NWO), with the NWO Gravitation project NETWORKS, grant number 024.002.003.

Modeling and control of congestion phenomena

ACADEMISCH PROEFSCHRIFT

ter verkrijging van de graad van doctor
aan de Universiteit van Amsterdam
op gezag van de Rector Magnificus
prof. dr. ir. P.P.C.C. Verbeek

ten overstaan van een door het College voor Promoties ingestelde commissie,
in het openbaar te verdedigen in de Aula der Universiteit
op vrijdag 2 februari 2024, te 14.00 uur

door Nikki Agatha Cornelia Levering
geboren te Limmen

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Faculteit der Natuurwetenschappen, Wiskunde en Informatica

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Acknowledgements

First and foremost, I wish to express my deepest gratitude to my doctoral advisors Sindo Núñez Queija, Michel Mandjes, and Marko Boon. Without their trust, guidance, and everything they have taught me over the past years, this thesis would not have existed. Sindo, your door was always open, your advice helped me to see problems in the right context, and I really enjoyed our discussions in front of the whiteboard. Michel, you continuously inspired me to dig deeper, taught me to ask the right questions, and gave me the confidence to tackle these with an open mind. Marko, you kept me spirited in times things went less smoothly, and not a day goes by that I do not use your training when setting up numerical experiments. I greatly enjoyed all our offline and online meetings; the parts in which we actually tried to do research, as well as the parts in which we discussed other important things in life, such as sports, the cultural differences between the northern and southern part of the Netherlands, and the entertaining stories from your times as starting researchers. It was a true pleasure.

I also want to thank Brendan Patch, Rens Kamphuis, Royi Jacobovic and Onno Boxma, the wonderful colleagues that I have collaborated with over the past years. Brendan, without your and Michel's invitation to work on one of your ideas for my Master thesis, and your excellent guidance during these months, I may have never experienced the joys of research. Rens, I am very happy that we got the opportunity to work together so closely, whereby I've learnt a lot from your ability to always keep the bigger picture in mind. Royi, I am truly grateful that you took me under your wing and introduced me to the world of externalities. Your hard work and dedication are a true inspiration. Onno, it is a privilege to call you a co-author; your help, insights, and feedback have been invaluable.

My time at the KdVI would not have been so pleasant were it not for the amazing colleagues there. Special thanks to my mathematical 'brothers' and 'sisters', and my office mates over the past years. Lucas, Rens, Ben, Bharti, Purva, Patrick, Sven, Madelon, Fabian, Liron, Shreehari, and Roshan, I hold great memories to all our encounters, delightful conversations, and sometimes welcome distractions. I am very glad to have been able to get to know some of you on a more personal level, and especially fond of the memories in Helsinki, Tallinn, and Nancy. Special thanks to Bharti, who always agreed to be my roommate on these trips, and to Purva, who hosted my stays in Eindhoven. The tourist trips the three of us undertook were really enjoyable as well; it was refreshing to see the Netherlands through different eyes. I also want to thank all (former) members of the KdVI PhD Council, for organizing fun activities together that allowed me to get to know the PhD students from the other research areas, and all involved in the NETWORKS

consortium, for expanding my horizons beyond Amsterdam.

Over the past four years, the support from my family and friends has made all the difference. I am grateful to everyone who has been in my life during this period, and want to thank a few specifically. First, my parents, for their continuous warmth and care, and for always encouraging me to follow my dreams; they are my true idols. Lars and Bram, I am blessed for having brothers like you. My grandparents, for their unconditional faith (despite congestion levels in traffic still rising). My parents-in-law, for welcoming me into their family. Nancy, Jonna, Femke, Ayla, Eline, and Debbie, who have been in my life for a long time, but somehow never gave up on me. The shared laughter, dinners, hikes, game nights, and dances gave me the spirit to finish this journey, and I am lucky to call you my friends. And finally, I am forever indebted to my wife Linda. *Meer nog dan ik eigenlijk toegeven wil, maakte zij het verschil*¹.

¹Inspired by the lyrics from ‘Zij maakt het verschil’ (2001) by *De Poema*’s.