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DOI
10.1103/PhysRevLett.110.034501

Publication date
2013

Document Version
Final published version

Published in
Physical Review Letters

Citation for published version (APA):
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(Received 19 June 2012; revised manuscript received 17 October 2012; published 14 January 2013)

We study the pinch-off dynamics of droplets of yield stress and shear thinning fluids. To separate the two non-Newtonian effects, we use a yield stress material for which the yield stress can be tuned without changing the shear thinning behavior, and a shear thinning system (without a yield stress) for which the shear thinning can be controlled over a large range, without introducing too much elasticity into the system. We find that the pinch-off remains very similar to that of constant viscosity Newtonian liquids, and consequently thinning in shear flow does not imply a thinning in elongational flow.

The evolution of the minimum neck radius (cf. Fig. 2) was obtained from sequences of rapid camera images; each experiment was repeated at least 5 times. The thinning of the neck is usually fitted to a power-law dependence; here we do the same and fit

$$R_{\text{min}} = A |t_0 - t|^\alpha,$$

(1)
where \( t_0 \) is the breakup time and \( \alpha \) is the power-law exponent. For Newtonian fluids, \( \alpha \) is either \( \frac{2}{3} \) or 1, depending on which forces are balanced. If the elongational viscosity is rate dependent, the expectation is that \( \alpha = n \) \([5,7,8,12]\). However, in our filament thinning experiments (cf. Fig. 2), we find \( \alpha \approx 0.67 \) for low yield stress emulsions, and unity for very elastic emulsions (Fig. 3). Here the somewhat gradual transition is the result of fitting over a limited scaling range. This suggests that the emulsion behaves very similarly to Newtonian fluids, where for low viscosities one finds an exponent of \( \frac{2}{3} \) (inertia-capillary regime), while for high viscosities a power of unity is observed (capillary-inertial-viscous or capillary-viscous regime) \([1]\). This picture is confirmed by the fact that at the crossover, a typical Reynolds number \( Re \) is of order unity, as shown in the inset of Fig. 3.

In addition, the main visual difference between viscous and inertial regimes is that for the former the breakup exhibits up-down symmetry around the breakup point, whereas the symmetry is broken if inertia is important. Indeed, the asymmetry coefficient defined in \([20]\), which is plotted in Fig. 3, demonstrates a transition from asymmetric to symmetric, as the power-law exponent changes from \( \frac{2}{3} \) to 1.

Thus, the yield stress appears to be irrelevant and the breakup exponent is unrelated to the rheology altogether. To assess what the effective viscosity for the thinning is in the experiment, we can use the fact that for Newtonian fluids the rate of thinning in the viscous regime is given by the capillary speed \( \frac{\gamma}{\eta} \), where \( \gamma \) is the surface tension. However, determining the latter is in fact a difficult problem, since most if not all of the usual methods for determining surface tensions of liquids fail when the material has a yield stress.

We therefore developed a new method that makes use of the breakup images. Once the drop is formed, the conical shape of the interface (see the pictures in Fig. 4, inset) relaxes under the influence of the surface tension. This process stops as soon as the capillary pressure can no
longer overcome the yield stress of the material and so from measuring the radius of curvature, as indicated in the figure, the surface tension should follow from the force balance $\gamma / R = \tau_y$. We thus measure the curvature of the interface a long time after breakup when it no longer moves, and plot the curvature as a function of the yield stress. We find roughly a straight line, the slope of which should be the surface tension, as seen in Fig. 4.

We find a surface tension $\gamma = 17 \pm 4$ mN/m, close to the expected value, since both the oil phase and the surfactant rich water phase have a surface tension $\gamma = 20$ mN/m. Then, knowing the surface tension, we can obtain the effective viscosity from the filament thinning rate in the viscous regime. For instance from the data shown in Fig. 2, we conclude that the capillary velocity is on the order of 0.025 m/s for the 74% sample, corresponding to a viscosity of 0.032 Pa·s. Comparing to the rheology, this suggests that the value of the viscosity deduced from the breakup experiment corresponds to a typical shear viscosity at high shear rates.

Therefore, to study the relationship between pinch-off and shear-thinning rheology in more detail and more quantitatively, we will consider a simpler system. We use aqueous xanthan solutions and solutions of xanthan in glycerol-water mixtures (the glycerol was obtained from Sigma) to be able to control the shear thinning rate in the viscous regime. For instance from the data shown in Fig. 2, we conclude that the capillary velocity is on the order of 0.025 m/s for the 74% sample, corresponding to a viscosity of 0.032 Pa·s. Comparing to the rheology, this suggests that the value of the viscosity deduced from the breakup experiment corresponds to a typical shear viscosity at high shear rates.

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This allows us to compare to a constitutive equation for xanthan, which behaves like a suspension of rigid rods [21]. The measured elongational viscosity, found from the slope of $R_{\text{min}}$ in the viscous-capillary regime (taking $\eta_s = 3\eta = 0.213\gamma / |R_{\text{min}}|$ [1]), is reported in Fig. 7. A rigid rod will align in the direction of the extensional flow, increasing the viscosity, since the elongational stress is supported by the tension in the rods. Aligned rods are in a stable equilibrium position, so even moderate rates of

The data for the thinning of the neck is shown in Fig. 5, which is again fitted by (1), the scaling exponent being reported in Fig. 6. We find that the power remains constant around 1, and does so both for aqueous xanthan solutions and for xanthan in glycerol-water mixtures; again, each experiment was done at least 5 times to ensure the reproducibility of the results. The check with glycerol was done to make sure inertia could not influence the results. From the data, we show that again the rheology does not influence the breakup dynamics, although the shear-thinning exponent varies over a large range.

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\begin{align*}
\text{FIG. 4.} & \quad \text{Inverse radius of curvature vs yield stress for different volume fractions of castor oil. The inset shows the rounding of the interface after drop detachment.}
\end{align*}

\begin{align*}
\text{FIG. 5 (color online).} & \quad \text{Evolution of the diameter } 2R_{\text{min}} \text{ for low and high concentrations of xanthan in water [1000 ppm (slope } dR_{\text{min}}/dt = 0.0395 \text{ m/s; } \eta = 0.128 \text{ Pa·s) and 3000 ppm (} dR_{\text{min}}/dt = 0.0265 \text{ m/s; } \eta = 0.192 \text{ Pa·s)]. Error bars are smaller than the symbols.}
\end{align*}

\begin{align*}
\text{FIG. 6.} & \quad \text{Left scale: power-law exponent } \alpha \text{ from fit to } R_{\text{min}} \text{ (cf. Fig. 5), vs concentration of xanthan in water as well as in glycerol-water mixtures. Right scale: power-law exponent } n \text{ from the power-law variation of the viscosity (Fig. 8) for aqueous xanthan solutions.}
\end{align*}
extension will lead to almost complete alignment, and the elongational viscosity reaches the constant value [21]:

\[ \eta_{el} = 3\eta_s + 6Nk_B T\lambda. \]  

(2)

Here \( \eta_s \) is the solvent viscosity (10^{-3} Pa s), \( N \) the number density of the polymers in the suspension, \( T \) the temperature, and \( \lambda \) the relaxation time of the polymer solutions, which we determine from shear measurements. As seen in Fig. 7, measured and theoretical values for the extensional viscosity are in reasonable agreement, so we have obtained a quantitative picture of the relation between shear and elongation viscosity in a strongly shear thinning system.

The predicted shear viscosity of the same rigid dumbbell model, on the other hand, shows a behavior that is opposite to the extensional behavior in every aspect. Increasing alignment in the shear direction leads to a decreasing viscosity with shear rate, as particles become better oriented in the direction of shear, offering less and less resistance to the flow. However, the aligned state is unstable in shear flow, so the rod flips continuously between two equilibria, the transient time decreasing gradually with \( \gamma \), leading to the power-law dependence [21]:

\[ \eta(\gamma) = \eta_s + 0.678Nk_B T\lambda^{2/3}\gamma^{-1/3}. \]  

(3)

In Fig. 8 we fit (3) to the high-shear end of our shear measurements, treating \( \lambda \) as an adjustable parameter, used in (2) to calculate the shear viscosity.

In conclusion, we have studied the breakup of non-Newtonian fluids for the cases of shear thinning and yield stress materials; we conclude that both the emulsion and the polymer solution behave very similarly to Newtonian fluids: neither the yield stress nor the shear thinning come into play. Both the shear and the elongational viscosity are modeled quite well by the rigid dumbbell model for high shear rates. During drop formation, the elongational viscosity is always saturated at its high deformation rate value.

Our physical picture does not take into account the possible formation of complex structures created by highly interacting particles. Measurements of a liquid crystalline fluid in the smectic phase have found an extensional rheology in line with shear measurements [10]. However, other liquid crystalline phases showed a strong discrepancy between shear rheology and breakup measurements [11]. A correspondence between shear and elongation rheology was also reported in the case of even more complex (and less well characterized) fluids like ketchup, shaving foam, and hair gel [22,23]. We have to conclude that there may be liquids forming complex networks, whose rheology is beyond our current understanding.


