UNIVERSITY OF AMSTERDAM

UvA-DARE (Digital Academic Repository)

CP-violating axion interactions II: axions as dark matter

Plakkot, V.; Dekens, W.; de Vries, J.; Shain Poruvelil, S.

DOI
10.1007/JHEP11(2023)012

Publication date
2023

Document Version
Final published version

Published in
The Journal of High Energy Physics

License
CC BY

Link to publication

Citation for published version (APA):
Plakkot, V., Dekens, W., de Vries, J., & Shain Poruvelil, S. (2023). CP-violating axion interactions II: axions as dark matter. *The Journal of High Energy Physics*, *2023*(11), Article 012. https://doi.org/10.1007/JHEP11(2023)012

General rights
It is not permitted to download or to forward/distribute the text or part of it without the consent of the author(s) and/or copyright holder(s), other than for strictly personal, individual use, unless the work is under an open content license (like Creative Commons).

Disclaimer/Complaints regulations
If you believe that digital publication of certain material infringes any of your rights or (privacy) interests, please let the Library know, stating your reasons. In case of a legitimate complaint, the Library will make the material inaccessible and/or remove it from the website. Please Ask the Library: https://uba.uva.nl/en/contact, or a letter to: Library of the University of Amsterdam, Secretariat, P.O. Box 19185, 1000 GD Amsterdam, The Netherlands. You will be contacted as soon as possible.

UvA-DARE is a service provided by the library of the University of Amsterdam (https://dare.uva.nl)

Download date:18 Nov 2026

Published for SISSA by Springer

Received: July 4, 2023
Revised: September 14, 2023
Accepted: October 19, 2023
Published: November 2, 2023

CP-violating axion interactions II: axions as dark matter

V. Plakkot,[a,b] **W. Dekens,**[c] **J. de Vries**[a,b] **and S. Shain**[a,b]

[a] *Institute for Theoretical Physics Amsterdam and Delta Institute for Theoretical Physics, University of Amsterdam, Science Park 904, 1098 XH Amsterdam, The Netherlands*
[b] *Theory Group, Nikhef, Science Park 105, 1098 XG, Amsterdam, The Netherlands*
[c] *Institute for Nuclear Theory, University of Washington, Seattle WA 91195-1550, U.S.A.*

E-mail: v.plakkot@uva.nl, wdekens@uw.edu, j.devries4@uva.nl, sshain@nikhef.nl

Abstract: Axions provide a solution to the strong CP problem and are excellent dark matter candidates. The presence of additional sources of CP violation, for example to account for the matter/antimatter asymmetry of the universe, can lead to CP-violating interactions between axions and Standard Model fields. In case axions form a coherent dark matter background, this leads to time-oscillating fundamental constants such as the fine-structure constant and particle masses. In this work we compare the sensitivity of various searches for CP-odd axion interactions. These include fifth-force experiments, searches for time-oscillating constants induced by axion dark matter, and direct limits from electric dipole moment experiments. We show that searches for oscillating constants can outperform fifth-force experiments in the regime of small axion masses, but, in general, do not reach the sensitivity of electric dipole moment experiments.

Keywords: Axions and ALPs, CP Violation, Effective Field Theories, Specific BSM Phenomenology

ArXiv ePrint: 2306.07065

Open Access, © The Authors.
Article funded by SCOAP[3].

https://doi.org/10.1007/JHEP11(2023)012

JHEP11(2023)012

Contents

1 Introduction **1**

2 Theoretical framework and motivation **3**
2.1 CP-violating axion interactions in LEFT 3

3 Time-varying effects **7**
3.1 Axion-nucleon couplings and time-varying nucleon masses 8
3.2 Axion-photon coupling and a time-varying fine-structure constant 8
3.3 Magnetic axion couplings and the time-varying magnetic moments 9

4 Constraining the CPV axion interactions **10**
4.1 Atomic clocks and interferometers 10
4.2 Fifth-force experiments 11
4.3 Dipole interaction searches 12
4.4 Limits on CPV axion couplings 12

5 The bigger picture **16**
5.1 A leptoquark scenario 17
5.2 Left-right symmetric model 19
5.3 Chromo-electric dipole moments 22

6 Conclusions and discussion **22**

A Contributions of LEFT operators **24**

B Contributions to EDMs **26**
B.1 EDMs of polar molecules 26
B.2 EDMs of nucleons, nuclei, and atoms 27

JHEP11(2023)012

1 Introduction

The lack of CP violation in the strong sector via $\mathcal{L} \supset \bar{\theta} G\widetilde{G}$ (with G being the gluonic field strength tensor, and $\widetilde{G}$ its dual) [1–4], dubbed the strong CP problem, can be solved by allowing the parameter $\bar{\theta}$ to be a dynamical variable that settles to zero at the minimum of its potential. This is achieved by introducing a global U(1) Peccei-Quinn (PQ) symmetry, $\mathrm{U}(1)_{\mathrm{PQ}}$, broken at a high energy scale f_a, called the axion decay constant [5, 6]. The (pseudo-)Goldstone boson of this broken symmetry is the QCD axion, $a(x)$, and is an excellent dark matter (DM) candidate [7–11]. The so-called *invisible* axion models offer attractive UV-complete mechanisms to introduce axions [12–15]. The model space for axions

is however not limited to these two benchmark models; several extensions and alternative models provide ways to extend the viable parameter space of QCD axions [16–23]. Experimental efforts are yet to yield conclusive evidence for the existence of axions, although huge chunks of the available parameter space are yet to be probed [24, 25].

The PQ mechanism efficiently removes the single source of CP violation in the strong sector. However, even within the Standard Model (SM) this is not sufficient to remove all CP violation. In addition, it is not unlikely that additional sources of CP violation exist in a beyond-the-SM theory that addresses some of the SM shortcomings (such as the universal matter-antimatter asymmetry). The presence of CP-violating interactions beyond the QCD $\bar{\theta}$ term leads to CP-violating interactions between axions and SM fields. In recent work, we derived the CP-odd interactions between axions and leptons, hadrons, and nuclei in the framework of the Standard Model effective field theory (SM-EFT) [26]. The CP-odd interactions lead to an axion-mediated scalar-scalar (monopole) and scalar-pseudoscalar (monopole-dipole) potential between, for example, atoms [27] that can be potentially detected in dedicated experiments, see e.g. ref. [28] for an overview. We concluded however that at least at the level of dimension-six SM-EFT interactions, it will be extremely difficult to detect axion CP-odd interactions because limits from electric dipole moments (EDMs) on the CP-odd dimension-six couplings are too stringent.

In this work, we will investigate whether we can detect CP-odd axion interactions under the assumption that axions form the dark matter (DM) in our universe. If we assume axions to form a coherent wave-like DM field new phenomenological implications arise. The axion DM field becomes locally coherent, with only a time-varying component, such that the equation of motion is solved by $a(t) \simeq a_0 \cos(m_a t)$, with m_a the axion mass which thus sets the oscillation frequency of the axion DM wave. a_0 is related to the local axion density, $\rho_a \simeq \frac{1}{2} m_a^2 a_0^2$, which implies $a_0 = \sqrt{2\rho_a}/m_a$ [29]. Assuming then that axions account for all the DM, the axion density can be set to the local DM density, $\rho_a = \rho_{\rm DM} \simeq 0.3\,{\rm GeV/cm}^3$. Such a scenario can be tested by a range of axion experiments; see, for example ref. [24] for an overview. In the presence of CP-violating axion interactions, the effects of the oscillating axion background field leads to time-varying fundamental constants such as the fine-structure constant as well as the masses of elementary particles and composite systems such as hadrons, and nuclei [30, 31]. In this work, we extend the analysis of ref. [26] to include the additional experimental signatures that arise for axionic DM. We will see that probes of variation in fundamental constants can be more sensitive than limits from fifth-force experiments, especially at small axion masses, but, unfortunately, in general still fall short of EDM experiments.

This work is organized as follows. In section 2 we introduce the general setup, sources of CP violation, and effective CP-odd axion interactions and their renormalization. In section 4 we discuss experiments that are sensitive to axionic CP violation and compare constraints on different couplings from a broad range of experiments. We discuss specific beyond-the-Standard-Model scenarios in section 5 and conclude in section 6.

JHEP11(2023)012

2 Theoretical framework and motivation

Axions are interesting and well-motivated BSM particles that can account for several SM problems: the lack of a DM candidate, and a SM peculiarity, the CP-conserving nature of QCD. It must be said that within the SM small values of $\bar{\theta}$ are technically natural; once a small value of $\bar{\theta} \ll 1$ is selected it remains small. Only minuscule radiative corrections to $\bar{\theta}$ are induced [32] which cannot be detected in present-day EDM experiments.

In generic BSM extensions this is no longer the case. While one can still set $\bar{\theta} \ll 1$ at some energy scale, in general large corrections are induced at lower scales. For example, in supersymmetric models soft phases induce sizable threshold corrections [33] to $\bar{\theta}$. While models can be constructed that avoid tree- and one-loop level corrections to $\bar{\theta}$ [34], higher loop corrections are still problematic [35, 36]. Similar conclusions can be drawn from a model-independent analysis within the SM-EFT framework [37]. The existence of dimension-six sources of CP violation imply large threshold corrections to $\bar{\theta}$ at the scale where the UV-complete theory is matched to the SM-EFT. This then strongly motivates an infrared mechanism to relax the value of $\bar{\theta}$ to zero, and the PQ mechanism is the only game in town. In essence, axions are even *better* motivated in BSM scenarios than in the SM itself. We illustrate this in figure 1.

In general, one may use the term "axion" to refer to a whole class of axion-like particles (ALPs) that arise similarly to the QCD axion, but need not solve the strong CP problem. Here, we restrict ourselves mainly to QCD axions, and the use of "axion" will mean QCD axion unless explicitly stated otherwise.

2.1 CP-violating axion interactions in LEFT

The Lagrangian describing the axion framework generally consists of the SM piece, the effective axion Lagrangian, and additional CP-violating sources,

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \mathcal{L}_{\text{axion}} + \mathcal{L}_{\text{LEFT}} \,. \tag{2.1}$$

The terms that depend on the axion are given by

$$\begin{aligned} \mathcal{L}_{\text{axion}} = & \frac{1}{2}(\partial_\mu a)^2 - \frac{\alpha_s}{8\pi}\frac{a}{f_a}\widetilde{G}^A_{\mu\nu}G^{A\,\mu\nu} - \frac{1}{4}g^{(0)}_{a\gamma}\frac{a}{f_a}\widetilde{F}_{\mu\nu}F^{\mu\nu} \\ & + \sum_{f=\nu,e,q}\frac{\partial_\mu a}{2f_a}\left[\bar{f}_L c^f_L \gamma^\mu f_L + \bar{f}_R c^f_R \gamma^\mu f_R\right], \end{aligned} \tag{2.2}$$

where f_a is the axion decay constant, $G_{\mu\nu}$ and $F_{\mu\nu}$ are the gluon and electromagnetic field strength tensors, α_s is the strong fine-structure constant, and $g^{(0)}_{a\gamma}$, c^f_L, and c^f_L are coupling constants that are determined by the UV completion of the effective theory. The axion mass comes from low-energy non-perturbative QCD effects, and is related to the axion decay constant as [20]

$$m_a \approx 6\,\mu\text{eV}\left(\frac{10^{12}\,\text{GeV}}{f_a}\right). \tag{2.3}$$

JHEP11(2023)012

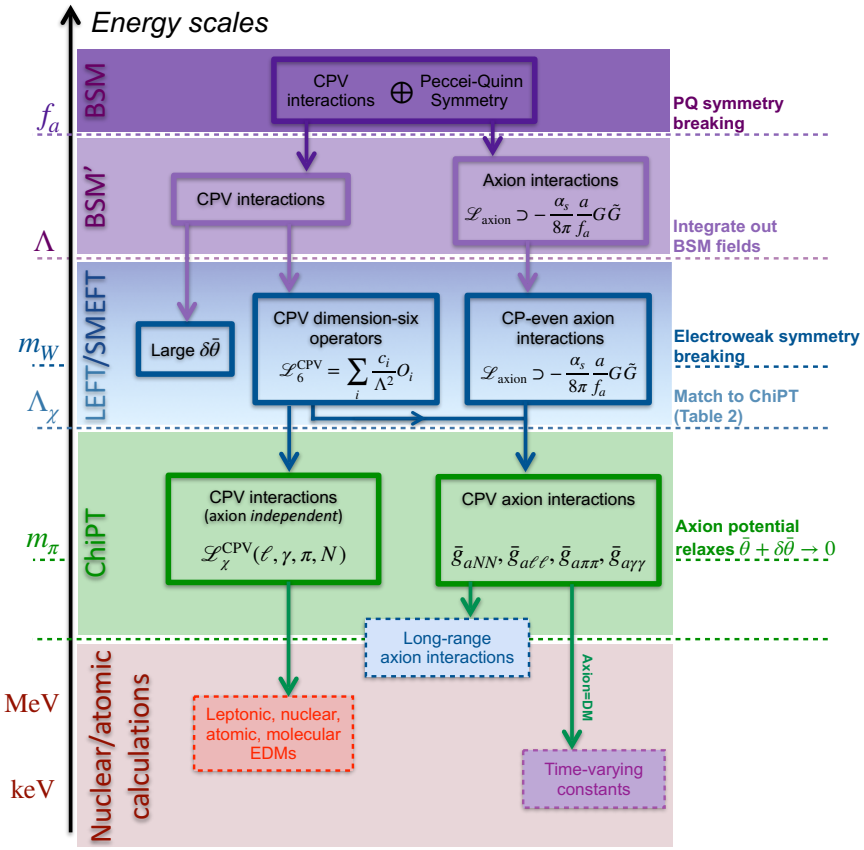

Figure 1. A schematic overview of the scales related to the PQ symmetry and CPV interactions that appear within the scenarios we consider in this work. The figure also shows how the new CPV interactions give rise to EDMs, while the interplay of these CPV sources with the PQ mechanism leads to CPV couplings of the axion to SM particles. These axion interactions can in turn be probed in fifth force experiments and, assuming the axion forms the DM abundance, searches for time-varying fundamental constants.

The couplings of axions to SM particles are inversely proportional to f_a and thus scale as $\propto m_a$. Nevertheless, the exact value of the couplings depend on the UV-complete model in question. Note however that this relation fails to hold for ALPs, where the couplings can be completely independent of m_a.

The Lagrangian (2.2) can be extended with SM-EFT operators, which would be matched to the low-energy effective field theory (LEFT) at energies below electroweak scale. The contributions of such terms can be written as $\mathcal{L}_{\rm LEFT} = \sum_i L_i \mathcal{O}_i$. Although the complete set of LEFT operators up to dimension six has been derived [38], we are only interested in the operators that induce CPV interactions. All such operators were considered in ref. [26] and are listed in appendix A, but we will only need a subset of operators here. All operators are suppressed by powers of the high-energy scale Λ, assumed to lie far above the electroweak scale, but well below the PQ scale $\sim f_a$.

JHEP11(2023)012

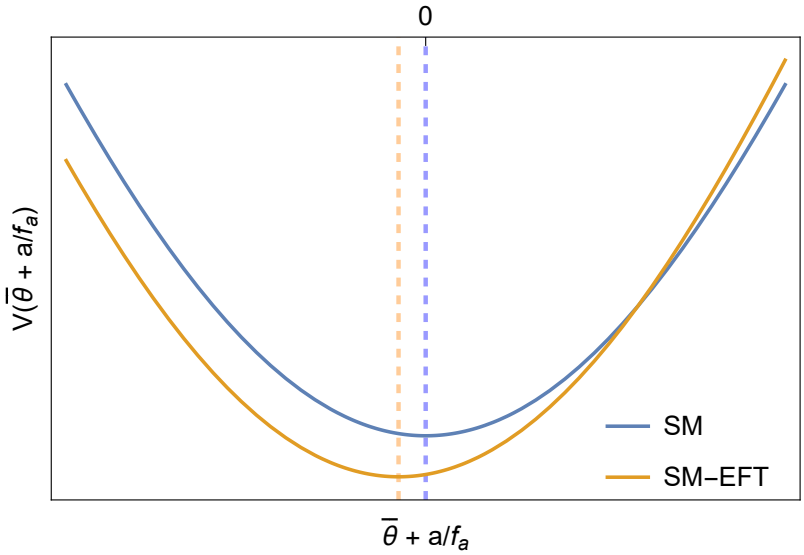

Figure 2. An (exaggerated) schematic representation of the shift in effective axion potential in the presence of higher-dimensional operators. The dashed lines represent the value of $\bar{\theta} + a/f_a$ at its potential minimum when SM-EFT operators are absent (in blue, coinciding with zero), and when they are present (in orange). The blue line corresponds to a scenario with just the $\bar{\theta}$ term and ignores CP violation in the electroweak interactions.

The PQ mechanism protects the naturalness of a small $\bar{\theta}$ by driving the axion potential to its minimum, which lies at $\bar{\theta} + \langle a \rangle / f_a = 0$. That is, the vacuum expectation value of the axion field (up to f_a) is such that it cancels out $\bar{\theta}$. In the presence of LEFT operators mentioned above, however, the minimum of the potential shifts such that $\bar{\theta} + \langle a \rangle / f_a \neq 0$. This is shown schematically in figure 2, where the blue (orange) line represents the potential without (with) LEFT operators. The field values at the minima are shown using dotted lines of the same color.

The effective $\bar{\theta}$ no longer vanishes and some CP violation is left behind. However, the remnant CP violation, characterised by the shift in the minimum, is at least suppressed by Λ_χ^2/Λ^2 with $\Lambda_\chi \sim 1\,\text{GeV}$, which (partially) explains its smallness.

Because not all CP violation is removed we are led to consider CP-violating interactions between axions and SM fields. For experimental purposes we are mainly interested in CP-odd interactions of axions with leptons and hadrons. We derived these in detail in ref. [26] and here we present the most relevant couplings for the present work. In particular, we consider

$$\begin{aligned}\mathcal{L}_{\text{axion, CPV}} = {} & \bar{g}^{(0)}_{a\ell\ell}\, a\, \bar{\ell}\ell + \bar{g}^{(0)}_{a\pi\pi}\, a\, \vec{\pi}\cdot\vec{\pi} + \bar{g}^{(0)}_{a\pi_0\pi_0}\, a\, \pi_0\pi_0 + \bar{g}^{(0)}_{aNN}\, a\, \bar{N}N \\ & + \bar{g}^{(0)}_{a\ell\gamma}\, a\, \bar{\ell}\sigma^{\mu\nu}\ell F_{\mu\nu} + \bar{g}^{(0)}_{an\gamma}\, a\, \bar{n}\sigma^{\mu\nu}nF_{\mu\nu} + \bar{g}^{(0)}_{ap\gamma}\, a\, \bar{p}\sigma^{\mu\nu}pF_{\mu\nu} \\ & + \frac{\bar{g}^{(0)}_{a\gamma\gamma}}{4}\, a\, F_{\mu\nu}F^{\mu\nu} + \dots\,, \end{aligned} \tag{2.4}$$

in terms of leptons $\ell = \{e, \mu, \tau\}$, the pion triplet π^a, the nucleon doublet $N = (p,\, n)^T$, and the photon field strength $F_{\mu\nu}$. The terms in the first line describe, respectively, CP-violating axion-lepton, isospin-conserving and -breaking axion-pion, and axion-nucleon interactions

JHEP11(2023)012

(we have omitted here a possible isospin-breaking axion-nucleon term as it only plays a small role in our analysis). The second line describes axion couplings to lepton and nucleon magnetic moments, while the last line describes the CP-odd counterpart of the usual axion-photon-photon interaction. We use a bar notation on the coupling constants to indicate that the coupling breaks CP and the (0) superscript indicates that these are bare couplings in the Lagrangian which are renormalized at the loop level. We discuss how these couplings are generated as well as their renormalization in more detail below.

Standard Model contributions. Although small, the SM does provide a source of CP violation beyond the $\bar{\theta}$ term in the form of the phase in the CKM matrix. The basis-independent quantity that induces CP violation is the Jarlskog invariant, $J = \mathrm{Im}(V_{ud}^* V_{us} V_{td} V_{ts}^*) \simeq 3 \cdot 10^{-5}$, which can induce the couplings of eq. (2.4). The generated CP-odd axion couplings are expected to be proportional to $G_F^2 J$, as at least two exchanges of the W boson are required to obtain the combination of CKM elements in J. To estimate the contributions to eq. (2.4), we start from an effective Lagrangian at a scale of $\mu \simeq 2\,\mathrm{GeV}$, where all heavy SM fields have been integrated out. The relevant sources of CP violation at this scale are then captured by dimension-six operators, which arise from diagrams involving the W boson.

For the couplings to nucleons [39, 40] and leptons [26] we use the estimates in the literature

$$\bar{g}_{a\ell\ell} \sim \frac{m_\ell}{f_a} \left(\frac{\alpha}{4\pi}\right)^2 \left(G_F F_\pi^2\right)^2 J \simeq \frac{m_\ell}{m_e} \frac{1}{2} \frac{10^{-25}\,\mathrm{MeV}}{f_a}\,, \tag{2.5}$$

$$\bar{g}_{aNN} \sim \frac{m_*}{f_a} \left(G_F F_\pi^2\right)^2 J \simeq \frac{1}{2} \frac{10^{-18}\,\mathrm{MeV}}{f_a}\,. \tag{2.6}$$

To estimate the coupling to pions we consider the contribution coming from a tree-level weak operator $\sim V_{ud} V_{us}^* G_F (\bar{u}_L \gamma_\mu d_L)(\bar{s}_L \gamma^\mu u_L)$, combined with an electroweak penguin operator $\sim \frac{\alpha}{4\pi} V_{td} V_{ts}^* G_F (\bar{q}_R \gamma_\mu Q q_R)(\bar{s}_L \gamma^\mu d_L)$, where Q denotes the quark charge matrix.[1] Using Naive Dimensional Analysis (NDA) [41, 42], we obtain

$$\bar{g}_{a\pi\pi} \sim \frac{F_\pi^2}{f_a} \left(G_F F_\pi^2\right)^2 J \simeq 3 F_\pi \frac{10^{-17}\,\mathrm{MeV}}{f_a}\,. \tag{2.7}$$

Finally, we consider contributions to $\bar{g}_{a\gamma\gamma}$ arising from $a - K$ mixing, induced by a tree-level weak operator, combined with a $K\gamma\gamma$ vertex induced by another tree-level weak operator and two insertions of the QED current. The corresponding NDA estimate is

$$\bar{g}_{a\gamma\gamma} \sim \frac{\alpha}{4\pi} \frac{1}{f_a} \left(G_F F_\pi^2\right)^2 J \simeq 2 \cdot 10^{-22} \frac{1}{f_a}\,. \tag{2.8}$$

When discussing the sensitivity of current and future experiments in section 4, we will use the above estimates to indicate the expected SM effect, although in most cases they are too small to be shown.

[1] One could in principle consider contributions from other tree-level interactions instead of an EW penguin operator. However, the chiral properties of the tree-level interactions only allow them to contribute to chirally suppressed operators involving additional derivatives in the chiral Lagrangian. The chiral suppression is expected to be similar to the loop suppression encountered when employing the EW penguin operators.

JHEP11(2023)012

Higher-dimensional contributions. The contributions to the couplings in the chiral Lagrangian of eq. (2.4) in terms of the quark-level LEFT operators is determined by hadronic matrix elements, parameterized by so-called low-energy constants (LECs). The values of $\bar{g}^{(0)}_{a\ell\ell}$, $\bar{g}^{(0)}_{a\pi\pi}$, and $\bar{g}^{(0)}_{aNN}$ in terms of CP-violating dimension-six LEFT operators have been discussed in great detail in ref. [26], while our discussion of $\bar{g}_{a\gamma\gamma}$ and the coupling of the axion to the magnetic moments go beyond that work. Here we will not perform a detailed construction of the chiral Lagrangian that leads to the couplings in eq. (2.4). Instead, we summarize both the LEFT operators as well as the NDA estimates of their contributions to eq. (2.4) in appendix A. These estimates will be of use when we consider several specific BSM scenarios in section 5.

The interactions in eq. (2.4) have a different form to those in the usual CP-conserving axion Lagrangian in which the axion couples derivatively to electrons (see eq. (2.2)), nucleons, and pions [20]. As we discuss in more detail in the next section, this feature will lead to new, time-varying, effects.

3 Time-varying effects

In this section, we will consider the possible signals that arise when we assume that the axion explains the DM abundance. This assumption leads to a coherent background axion field. In the presence of such a field, the CPV couplings effectively introduce a time-oscillating component to the lepton, pion, and nucleon masses [30]. For example, the effective electron mass becomes

$$m_e(t) \simeq m_e \left[1 - \frac{\bar{g}_{aee}}{m_e} a(t)\right], \tag{3.1}$$

where m_e denotes the time-independent electron mass term that originates in the SM. Similarly, the second and third line of eq. (2.4) lead to time-varying lepton and nucleon magnetic moments and a time-varying fine-structure constant.

Without knowing the mechanism of CP violation it is not possible to address the relative sizes of the couplings in eq. (2.4). However, all terms are expected to be suppressed as $\bar{g}_i \propto \kappa^{d_i} \frac{\kappa^3}{f_a \Lambda}$, where d_i is the dimension of the coupling $\bar{g}_i$ and κ is a hadronic scale, $\kappa \lesssim \Lambda_\chi$. We will discuss more specific scenarios where this question can be answered in section 5. Before doing so, we will first discuss loop corrections that relate the various couplings in eq. (2.4) as well as experimental constraints, irrespective of the origin of the couplings. This is important because the experimental constraints on the various terms in eq. (2.4) are quite different. Roughly, the strongest direct limits are set on the axion-photon-photon coupling, while weaker constraints are set on the axion-nucleon-nucleon, magnetic axion-nucleon-nucleon, and axion-electron-electron interactions. Essentially no direct constraints are set on the axion-pion-pion terms but because they renormalize other interactions, they will still play an important role.

We stress that the kind of interactions discussed here are not unique to axions, and are usually studied in the context of ultralight scalar DM (ULDM) (see, e.g., ref. [30] where the protagonist is a dilaton). As a result, the constraints discussed in the next section, in

JHEP11(2023)012

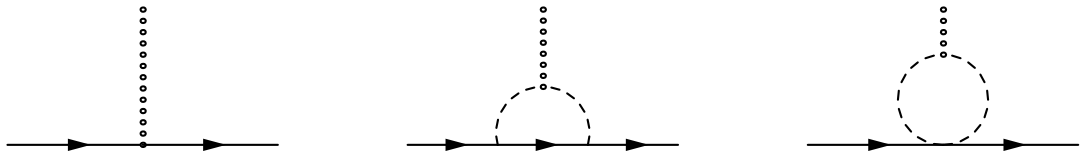

Figure 3. Contributions to the axion-nucleon coupling. The solid, dashed, and dotted lines represent nucleons, pions, and axions, respectively.

the context of an effective field theory framework, apply equally well to ULDM. Although we will refer only to axions in the upcoming sections, the axionic nature of DM is employed only in section 5 where we discuss specific BSM models.

3.1 Axion-nucleon couplings and time-varying nucleon masses

The CP-odd axion-nucleon interaction arises from the diagrams in figure 3. In principle there appear additional diagrams from electromagnetic corrections but these are not relevant for our analysis. The total effective interaction becomes

$$\bar{g}_{aNN} = \bar{g}^{(0)}_{aNN} + \frac{9\pi}{2}\frac{m_\pi g_A^2}{(4\pi F_\pi)^2}\left(\bar{g}_{a\pi\pi} + \frac{1}{3}\bar{g}^{(0)}_{a\pi_0\pi_0}\right), \tag{3.2}$$

in terms of the nucleon axial charge, $g_A \simeq 1.27$, the pion decay constant, $F_\pi \simeq 92.2\,\text{MeV}$, and the pion mass, m_π. In the presence of an axion DM background, this terms lead to an oscillating nucleon mass

$$m_N(t) = m_N\left[1 - \frac{\bar{g}_{aNN}}{m_N}a(t)\right]. \tag{3.3}$$

3.2 Axion-photon coupling and a time-varying fine-structure constant

Conventional axion models lead to CP-even axion-photon interaction of the form

$$\mathcal{L}^{\text{CP}}_{a\gamma} \supset g_{a\gamma\gamma} a F_{\mu\nu}\widetilde{F}^{\mu\nu}, \tag{3.4}$$

where the axion-photon coupling $g_{a\gamma\gamma}$ dictates the probability of axion-photon conversion in the presence of magnetic fields, as is probed in several axion detection experiments such as haloscopes and helioscopes (see, e.g., refs. [43–45]). CPV axion interactions can induce an additional effective axion-photon term to the Lagrangian,

$$\mathcal{L}^{\text{CPV}}_{a\gamma} = \frac{\bar{g}_{a\gamma\gamma}}{4} a F_{\mu\nu}F^{\mu\nu}, \tag{3.5}$$

which causes an interaction $\propto a(\vec{E}^2 - \vec{B}^2)$ in terms of electric and magnetic fields $\vec{E}$ and $\vec{B}$, as opposed to the conventional CP-even coupling $\propto a(\vec{E}\cdot\vec{B})$.

In addition to the direct pieces the CPV coupling gets contributions from the loop diagrams in figure 4 involving virtual mesons and leptons.[2] The total coupling then becomes

$$\bar{g}_{a\gamma\gamma} = \bar{g}^{(0)}_{a\gamma\gamma} - \frac{\alpha_{\text{em}}}{12\pi}\frac{\bar{g}_{a\pi\pi}}{m_\pi^2} - \sum_{e,\mu,\tau}\frac{2\alpha_{\text{em}}}{3\pi}\frac{\bar{g}_{a\ell\ell}}{m_\ell}, \tag{3.6}$$

[2]One could in principle think about diagrams with virtual protons appearing in the loop. However, these do not appear within a heavy-baryon χEFT framework where anti-nucleons are integrated out at low energies. In this language, such contributions are already contained in the direct piece $\bar{g}^{(0)}_{a\gamma\gamma}$.

JHEP11(2023)012

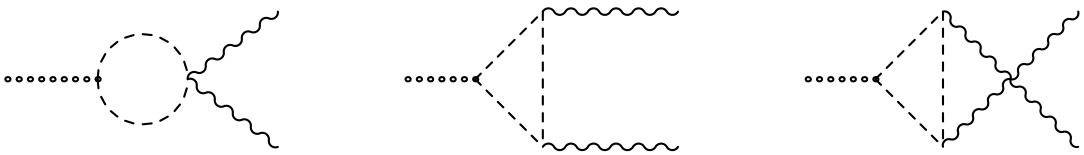

Figure 4. One-loop contributions to the $a\gamma\gamma$ vertex. The dashed lines represent pions or leptons, while dotted and wavy lines denote axions and photons, respectively.

where $\alpha_{\rm em}$ is the fine-structure constant. The constants $\alpha_{\rm em}$, m_π, and m_ℓ in the above expressions can be taken as time-independent as any time-varying component will appear at higher order in the already suppressed CPV axion couplings, and can be neglected.

In the presence of a coherent DM axion background field, a CPV axion-photon term may be interpreted as an effective time variation in the fine structure constant. Combined with the kinetic term for the photons,

$$\mathcal{L} \supset -\frac{1}{4}F^{\mu\nu}F_{\mu\nu} + \frac{\bar{g}_{a\gamma\gamma}}{4}aF^{\mu\nu}F_{\mu\nu}. \tag{3.7}$$

Following ref. [30], a field redefinition $A_\mu \to A_\mu/e$ ensures that the factors of e (and thus the fine structure constant) appear only in the terms given in eq. (3.7). The two terms can then be combined by defining an effective fine-structure constant,

$$\mathcal{L} \supset -\frac{1}{4e^2}(1-\bar{g}_{a\gamma\gamma})F^{\mu\nu}F_{\mu\nu} \equiv -\frac{1}{16\pi\alpha_{\rm eff}}F^{\mu\nu}F_{\mu\nu}, \tag{3.8}$$

which can be physically interpreted as a time-oscillation in the fine-structure constant,

$$\alpha_{\rm em}(t) \simeq \alpha_{\rm em}\left[1+\bar{g}_{a\gamma\gamma}\,a(t)\right]. \tag{3.9}$$

3.3 Magnetic axion couplings and the time-varying magnetic moments

The pionic terms in eq. (2.4) induce axion-nucleon magnetic couplings at the one-loop level. The only non-vanishing diagrams are depicted in figure 5, and they induce

$$\begin{aligned}
\bar{g}_{ap\gamma} &= \bar{g}^{(0)}_{ap\gamma} - \frac{e\pi\bar{g}_{a\pi\pi}}{2m_\pi}\frac{g_A^2}{(4\pi F_\pi)^2}\,,\\
\bar{g}_{an\gamma} &= \bar{g}^{(0)}_{an\gamma} + \frac{e\pi\bar{g}_{a\pi\pi}}{2m_\pi}\frac{g_A^2}{(4\pi F_\pi)^2}\,.
\end{aligned} \tag{3.10}$$

Together, these terms can be interpreted as time-varying nucleon magnetic moments

$$\begin{aligned}
\mu_p(t) &\simeq \mu_p\left[1+\left(\bar{g}^{(0)}_{ap\gamma} - \frac{e\pi\bar{g}_{a\pi\pi}}{2m_\pi}\frac{g_A^2}{(4\pi F_\pi)^2}\right)\frac{a(t)}{\mu_p}\right],\\
\mu_n(t) &\simeq \mu_n\left[1+\left(\bar{g}^{(0)}_{an\gamma} + \frac{e\pi\bar{g}_{a\pi\pi}}{2m_\pi}\frac{g_A^2}{(4\pi F_\pi)^2}\right)\frac{a(t)}{\mu_n}\right],
\end{aligned} \tag{3.11}$$

in terms of the proton $\mu_p \simeq 2.79\,\mu_N$ and neutron $\mu_n \simeq -1.93\,\mu_N$ magnetic moments in units of nuclear magnetons. While a nuclear magneton $\mu_N = e/(2m_p)$, the explicit dependence on the proton mass is conventional and there is no direct link between the oscillating nucleon

JHEP11(2023)012

Figure 5. Corrections to nucleon magnetic moments via the axion-pion portal. The solid, dashed, dotted, and wavy lines represents nucleons, pions, axions, and photons, respectively.

mass and the oscillating nucleon magnetic moment. Any such dependence is hidden in the direct pieces which cannot be computed in a model-independent way. Nevertheless, we expect that the two matrix elements are connected and one may estimate the time-dependence in the direct piece to come from the proportionality $g^{(0)}_{aN\gamma} \propto 1/m_N(t)$ given in eq. (3.3). In this way we can estimate the sensitivity of time-varying nucleon masses through their impact on the time-varying nucleon magnetic moment.

For elementary particles such as leptons the link between masses and magnetic moments is cleaner. In this case, the leptonic magnetic moments obtain time-dependence through the $a\bar{\ell}\ell$ couplings and we obtain

$$\mu_\ell(t) \simeq \mu_\ell \left[1 + 2\left(\bar{g}^{(0)}_{a\ell\gamma} + \bar{g}_{a\ell\ell}\frac{\mu_\ell}{m_\ell}\right)\frac{a(t)}{\mu_\ell}\right] , \tag{3.12}$$

where $\mu_\ell = e/2m_\ell$.

4 Constraining the CPV axion interactions

4.1 Atomic clocks and interferometers

The discussion in section 2.1 shows that a coherent light axion DM field with CPV interactions can have effects similar to ULDM [30], which include a time-variation in fundamental constants such as particle masses, the fine-structure constant, and magnetic moment of nucleons. Several of these effects can be probed with precision experiments using atomic clocks [46]. Atomic transition frequencies depend on the nuclear magnetic moment μ_A, the fine-structure constant, and electron mass through

$$f_A(t) \propto \left[\frac{\mu_A(t)}{\mu_e(t)}\right]^{\zeta_A} [\alpha_{\rm em}(t)]^{\xi_A+2} [m_e(t)] , \tag{4.1}$$

where $\mu_e(t)$ is the electron magnetic moment, ζ_A is either 1 or 0 depending on whether the transition is hyperfine or optical. ξ_A depends on the atomic properties and is an effect of relativistic and many-body corrections which are independent of m_e [47]; see, e.g., ref. [46] for ξ_A values of some relevant systems. We consider atoms with a single valence nucleon in the core implying that the nuclear magnetic moment can be written as $\mu_A(t) \simeq \mu_N(t)+\Delta(t)$, where μ_N is the magnetic moment of the valence nucleon (see eq. (3.11)) and $\Delta(t)$ denotes nuclear contributions. The latter are hard to compute from first principles. We expect that the dominant time-dependence arises from the axion-pion interactions which modifies

JHEP11(2023)012

the pion mass and thus the nucleon-nucleon potential. Barring an exact understanding of these contributions, we will focus on the contributions from $\mu_N(t)$ instead.

Under these assumptions, we obtain[3]

$$\left(\frac{\mu_A(t)}{\mu_e(t)}\right) \simeq \left(\frac{\mu_A}{\mu_e}\right)\left[1+\left(\frac{\bar{g}_{aN\gamma}}{\mu_A}-\frac{\bar{g}^{(0)}_{ae\gamma}}{\mu_e}-\frac{\bar{g}_{aee}}{m_e}\right)a(t)\right]. \tag{4.2}$$

Consequently, for the ratio of transition frequencies of two atoms A and B, we get a fractional change

$$\frac{\delta(f_A/f_B)}{(f_A/f_B)} \approx \left[\left(\frac{\zeta_A}{\mu_A}-\frac{\zeta_B}{\mu_B}\right)\bar{g}_{aN\gamma}-\zeta_{AB}\left(\frac{\bar{g}^{(0)}_{ae\gamma}}{\mu_e}+\frac{\bar{g}_{aee}}{m_e}\right)+\xi_{AB}\,\bar{g}_{a\gamma\gamma}\right]a(t), \tag{4.3}$$

where $\zeta_{AB}=\zeta_A-\zeta_B$ and $\xi_{AB}=\xi_A-\xi_B$. Factors of $[\alpha_{\rm em}(t)]^2$ and the direct dependence on $m_e(t)$ cancel in the ratio. With this expression we can relate frequency stability of a system of atomic clocks to the strengths of different CPV axion interactions. Take, for example, a model where only the last term in the square brackets contributes. Knowing ξ_{AB} and ρ_a (which enters through a_0), a non-observation of oscillation in the frequency ratio lets us draw (m_a-dependent) limits on $\bar{g}_{a\gamma\gamma}$, up to the inherent frequency stability of the systems A and B which appears on the left-hand side of eq. (4.3).

Atom interferometry-based gravitational wave detectors have also been proposed as candidates for ULDM detection [49]. The proposed setup relies on differential phase accumulation between spatially separated atom interferometers, of the same type of atoms in this case, using controlled laser pulses. Since only one atomic system is used, it is clear from eq. (4.1) that the dependence of variation in transition frequency on $m_e(t)$ is explicit and the Rydberg factor of 2 in the exponent of $\alpha_{\rm em}(t)$ also comes into play. For electronic transitions (i.e., with $\zeta_A=0$), the transition frequency then varies as

$$\frac{\delta f_A}{f_A} \simeq \left[(\xi_A+2)\,\bar{g}_{a\gamma\gamma}+\frac{\bar{g}_{aee}}{m_e}\right]a(t), \tag{4.4}$$

and thus is sensitive to CPV axion-photon and axion-electron interactions. Although such systems have not been realised yet, we use the predicted reach of the proposals to draw projected limits on various CPV axion couplings [49–51].

4.2 Fifth-force experiments

In the presence of above-mentioned CPV axion interactions, long-distance axion exchange may lead to a new gravitation-like effective force, dubbed the "fifth force", thereby violating Newton's inverse-square law (ISL) and the weak equivalence principle (WEP). Experiments looking for such fifth forces are powerful tools to constrain CPV axion-nucleon and axion-lepton couplings [52–55]. Moreover, given the Coulombic contribution to the nucleon binding energy, the constraints also help us draw conservative limits on $\bar{g}_{a\gamma\gamma}$ as well [30]. In what follows, we will be heavily using the fifth-force search results to interpret bounds on different CPV axion interactions; we refer the reader to ref. [26] for more details.

[3]The dependence on $\bar{g}_{aN\gamma}/\mu_A$ is somewhat different with respect to ref. [48], which instead finds $\bar{g}_{an\gamma}/\mu_n$ for a system with a valence neutron and thus neglects nuclear contributions to the magnetic moments which are not negligible.

JHEP11(2023)012

4.3 Dipole interaction searches

CPV interactions in the effective theory, involving axions or otherwise, can induce EDMs in various systems such as nuclei, atoms, and molecules. Similarly, the presence of both CP-odd and CP-even operators involving axions can lead to spin-dependent monopole-dipole interactions. For the CP-even couplings, we use the DFSZ model and set the vacuum expectation values of the two scalar doublets to be equal. Without going into the details (once again, the interested reader is directed to ref. [26]), we would just like to point out that EDM measurements [1, 2, 56–59] set very stringent bounds on specific BSM scenarios, while proposed monopole-dipole searches such as ARIADNE and QUAX [60–63] can be competitive with EDM searches for specific axion mass ranges. We do not show the resulting constraints in the general framework discussed in this section, but rather employ them in section 5.

4.4 Limits on CPV axion couplings

The CP-violating axion-photon coupling. The effect of axion DM on $\alpha_{\rm em}$ can be isolated by focusing on optical transitions only, so that $\zeta_A = \zeta_B = 0$. In this way, we can focus on $\bar{g}_{a\gamma\gamma}$ exclusively. Assuming a coherent wave-like background axion field, a suitable approximation for cold and feebly-interacting axion DM with small m_a and homogeneous local distribution, the experimental sensitivity depends on the fractional stability of the atomic clocks, the (axion) DM density ($\rho_{\rm DM}$), the axion mass, as well as the coherence time of the DM field. The scaling of sensitivity with axion mass however implies that they remain competitive only for tiny m_a. For higher masses, the sensitivity decreases rapidly making such probes unviable at large axion masses. In this regime individual (averaged) measurements are not able to record the variation in $\alpha_{\rm em}$ given the high frequency of oscillation (recall that the frequency of a coherent axion DM field is given by m_a, and $1\,\text{eV} \simeq 1.52 \times 10^{15}\,\text{Hz}$) and the limits to which individual measurement times can be discretised, and we rely on alternative methods to limit $\bar{g}_{a\gamma\gamma}$.

For very light axions, roughly $m_a \leq 10^{-10}\,\text{eV}$, limits on the time-oscillation in $\alpha_{\rm em}$ provide very stringent upper bounds on $\bar{g}_{a\gamma\gamma}$. Given the rapid progress in this field, more stringent bounds are expected in the future as clocks with even better frequency stability are designed. Atom interferometry can also become very sensitive for ultralight DM axion in the future [49–51]. For larger axion masses, fifth-force experiments probing long-range axion-mediated forces, effectively violating the weak equivalence principle (WEP), provide upper bounds on $\bar{g}_{a\gamma\gamma}$ [52, 54, 55]. Laser-interferometric methods [64–66], as well as the gravitational wave detector AURIGA [67], have recently also been shown to be competitive with these bounds near $m_a = 10^{-12}\,\text{eV}$. Above $\sim 10\,\mu\text{eV}$, the constraints instead arise from the bounds on axion-to-photon conversion given by various conventional axion experiments and astrophysical bounds on $g_{a\gamma\gamma}$, since the axion-to-photon conversion does not discriminate between the two operators in eqs. (3.4) and (3.5). In general, we can expect $\bar{g}_{a\gamma\gamma}$ to be smaller than its CP-conserving counterpart and that the effect of $\bar{g}_{a\gamma\gamma}$ on such experiments be unnoticeable compared to a possibly larger $g_{a\gamma\gamma}$. However, this is a model-dependent statement and here we just show the bounds on $\bar{g}_{a\gamma\gamma}$.

JHEP11(2023)012

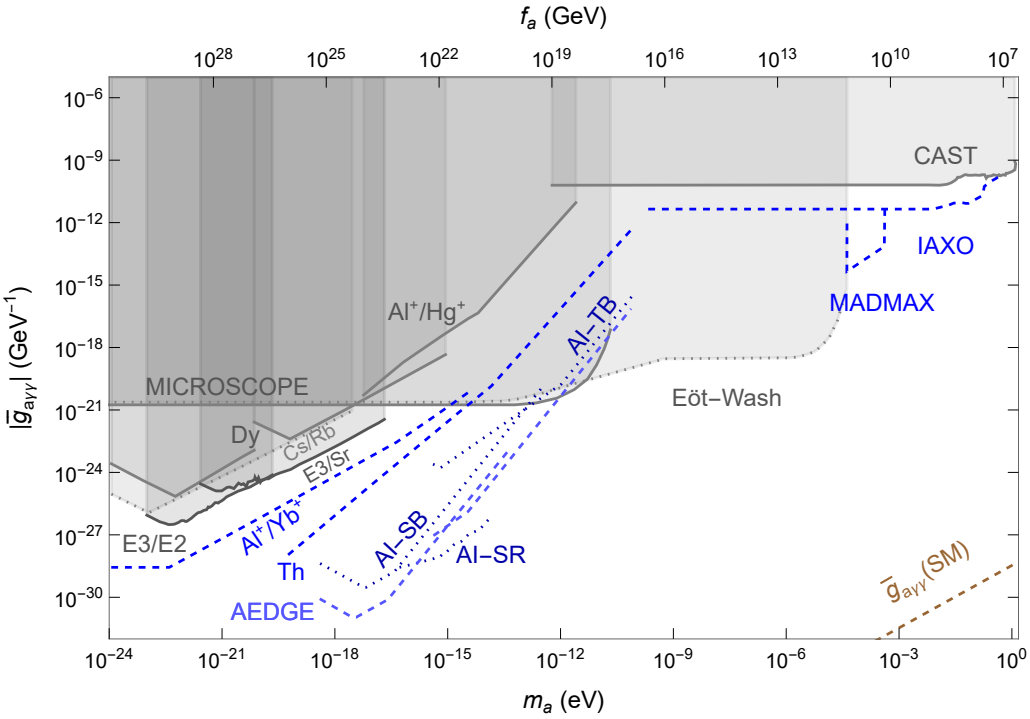

Figure 6. Upper bounds on the CPV axion-photon coupling $\bar{g}_{a\gamma\gamma}$. The existing (projected) bounds are given in gray (blue). Atomic clock (labeled Dy, Cs/Rb, Al^+/Hg^+, Al^+/Yb^+, E3/E2, E3/Sr), nuclear clock (Th), and atom interferometer (AI-TB, AI-SR, AI-SB, AEDGE, AION-km) bounds rely on the CPV structure of the axion-photon coupling to produce a time-oscillating $\alpha_{\rm em}$ [46, 49–51, 68–72]. CAST, MADMAX, IAXO are conventional axion experiments that look for axion-photon conversion in the presence of magnetic fields [45, 73–76]. MICROSCOPE and Eöt-Wash probe look for WEP violation through axion-mediated long-range forces [52–55]. Several other (weaker) bounds are not shown here to avoid clutter. The SM contribution via eq. (2.8) ($\bar{g}_{a\gamma\gamma}$(SM)) is shown in brown.

Figure 6 shows the current (in grey) and projected (in blue) bounds on $\bar{g}_{a\gamma\gamma}$. For $m_a \lesssim 10^{-17}\,$eV, current atomic clock experiments (labeled by Dy, Cs/Rb, E3/E2 and E3/Sr) [68, 69, 72]) already set constraints on $\bar{g}_{a\gamma\gamma}$ that are up to six orders of magnitude more stringent than fifth-force searches (MICROSCOPE). A recent analysis of the Sr/Cs system [77] also improves on the WEP bounds but is weaker than the limits from E3/E2 and E3/Sr, and the limits are not shown here to avoid clutter. Bounds from laser interferometry and AURIGA around $m_a = 10^{-12}\,$eV [64–67] are also not shown for the same reason.

Future atomic clocks (labeled by Al^+/Yb^+) can become more sensitive by several orders of magnitude and increase the axion mass range [46]. Nuclear clocks, labeled by Th, are very promising as well [71]. AI-SB, AI-SR, AI-TB refer to atom interferometry projections for terrestrial and space-based gravitational wave detectors, and AEDGE, AION-km label the projected reach for cold Strontium atom interferometers [49–51]. Such experiments can improve the constraints by many orders of magnitude.

JHEP11(2023)012

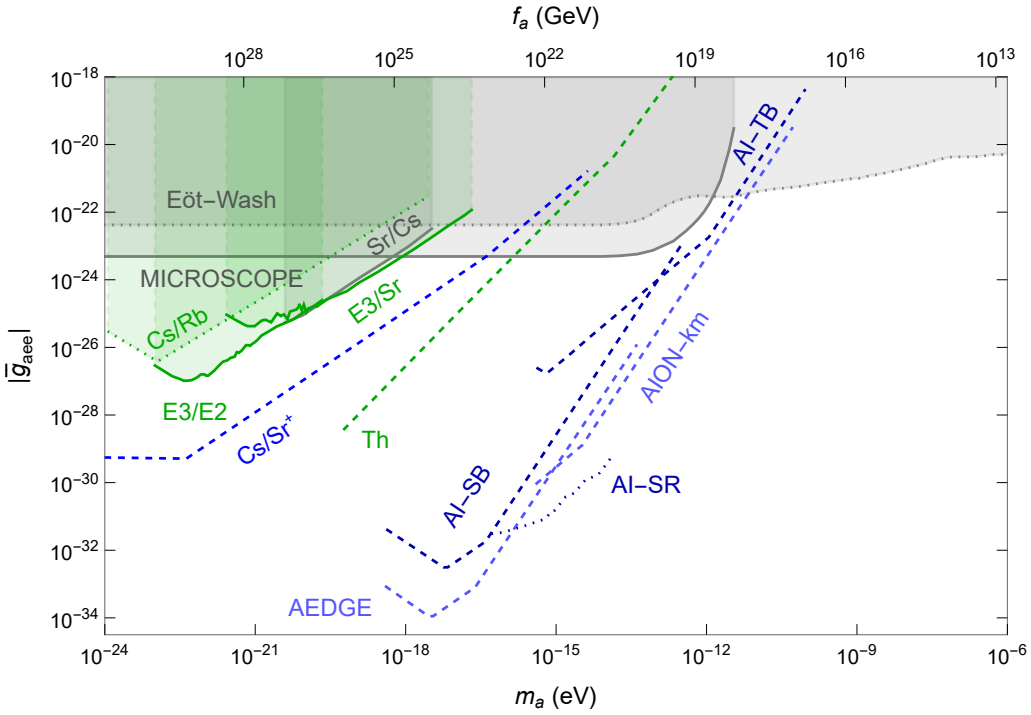

Figure 7. Direct limits (in grey, shaded) and projections (in blue) on $\bar{g}_{aee}$. The WEP bounds are from ref. [78], and Sr/Cs is from ref. [77]. Cs/Sr$^+$ is from ref. [46]; see figure 6 for the rest of the projections. In green are indirect bounds on $\bar{g}_{aee}$ obtained using eq. (3.6), where shading implies existing limits [69, 72]. The SM effect discussed previously is too small ($\sim 10^{-41}$ at $m_a = 10^{-6}$ eV) to enter the frame.

The CP-violating axion-electron coupling. Atomic clock systems involving hyperfine transitions (e.g., with microwave clocks) are sensitive to small variations in μ_A/μ_e, and thus to $\bar{g}_{aN\gamma}$, $\bar{g}^{(0)}_{a\ell\gamma}$, and $\bar{g}_{aee}$ through eq. (4.3). The limits and projections on $\bar{g}_{aee}$ from microwave clock measurements as well as other experiments are shown in figure 7.

The gray lines labelled by MICROSCOPE and Eöt-Wash indicate again current constraints from fifth-force experiments. The only limit on $\bar{g}_{aee}$ from microwave clock systems which improve upon these WEP limits come from a recent analysis of Sr/Cs clocks [77] which is also depicted in gray (and labeled with Sr/Cs). It is also possible to extract upper limits on axion-lepton couplings (as well as $\bar{g}_{a\pi\pi}$) with the use of only optical systems through eq. (3.6), assuming there are no large cancellations against the others terms appearing in that equation. Despite the loop suppression, because of the superior sensitivity of optical clocks to a time-varying fine-structure constant, the resulting indirect limits on $\bar{g}_{aee}$ are similar to the more direct limits from hyperfine transitions. These indirect bounds are in shown in green in figure 7. Once again, we do not show the recent constraints close to $m_a = 10^{-12}$ eV [64–67] that are competitive with fifth-force probes to avoid clutter.

Looking ahead, atom interferometers are sensitive to variations in the electron mass and $\alpha_{\rm em}$ and promise a direct reach in $\bar{g}_{aee}$ (see eq. (4.4)) that is about two orders of magnitude more sensitive than the translated bounds from $\bar{g}_{a\gamma\gamma}$ (using eq. (3.6)) [49–51].

JHEP11(2023)012

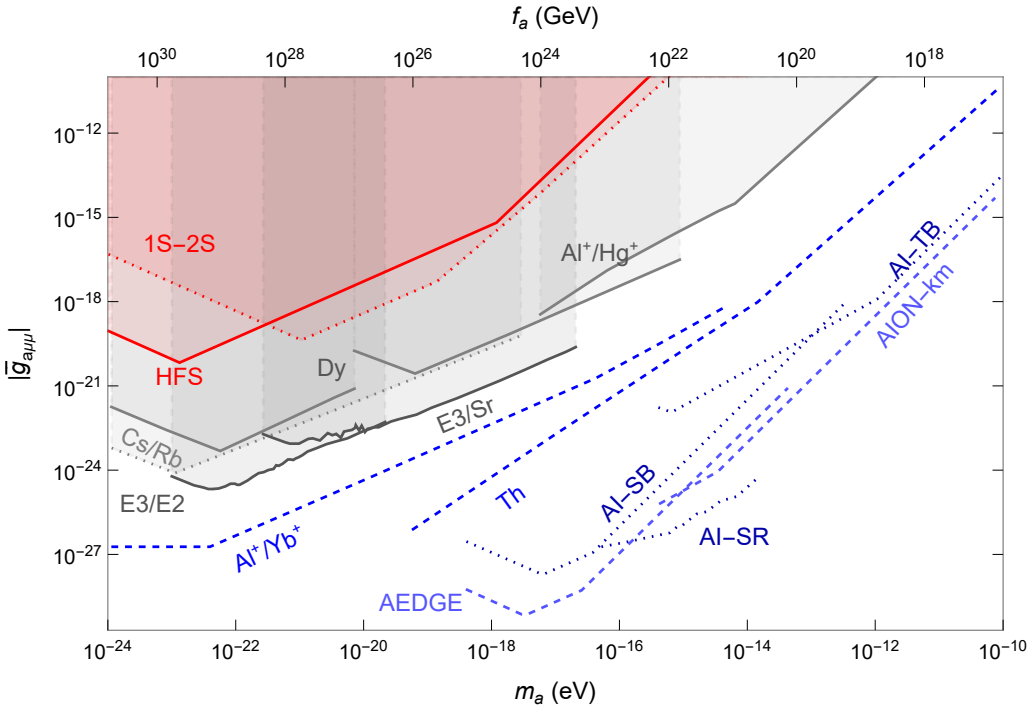

Figure 8. Bounds on the CPV axion-muon coupling. The bounds in red are from a recent study on muonium and muonic atoms, probing the variation in muon mass with hyperfine splitting (HFS) and 1S-2S transitions [79]. In gray and blue are the current and projected upper bounds coming from the loop-induced axion-photon coupling, given in figure 6. The WEP bounds (not shown here) become stronger than the best projection at $m_a \sim 10^{-12}$ eV (similar to figure 6). The SM effect is $\sim 10^{-43}$ at $m_a = 10^{-10}$ eV.

The CP-violating axion-muon coupling. We now briefly discuss the constraints on a coupling that does not enter eq. (4.3) explicitly, namely $\bar{g}_{a\mu\mu}$. A recent study pointed out that $\bar{g}_{a\mu\mu}$ can be studied by its effect on the spectra of muonium and muonic atoms [79] which would provide direct bounds. However, as shown in figure 8, these direct bounds pale in comparison to the upper bounds put on $\bar{g}_{a\mu\mu}$ by indirect constraints through eq. (3.6), as is confirmed in ref. [80]. There are in principle other limits, e.g., through muon precession experiments [81], that are weaker than the muonium limits and are thus not shown in figure 8.

The CP-violating axion-nucleon coupling. The axion-nucleon coupling $\bar{g}_{aNN}$ plays a role through its effects on $\bar{g}_{aN\gamma}$ due to variation in nucleon mass over time, see the discussion below eq. (3.11). In principle, there could be similar effects on $\bar{g}_{a\gamma\gamma}$. However, there are no closed nucleon loops in heavy-baryon χEFT, such that $\bar{g}_{aNN}$ cannot contribute through the first diagram in figure 4. Instead, such high-energy effects are captured in the LEC $\bar{g}_{a\gamma\gamma}$ itself, implying that knowledge of the quark-level theory is needed in order to relate $\bar{g}_{a\gamma\gamma}$ and $\bar{g}_{aNN}$. Keeping this in mind, we close our eyes and estimate the effects of $\bar{g}_{aNN}$ on $\bar{g}_{a\gamma\gamma}$ by using eq. (3.6) as we did for $\bar{g}_{a\ell\ell}$. The resulting contributions are m_N-suppressed and give weaker bounds, which are shown in figure 9. As mentioned before, if the direct

JHEP11(2023)012

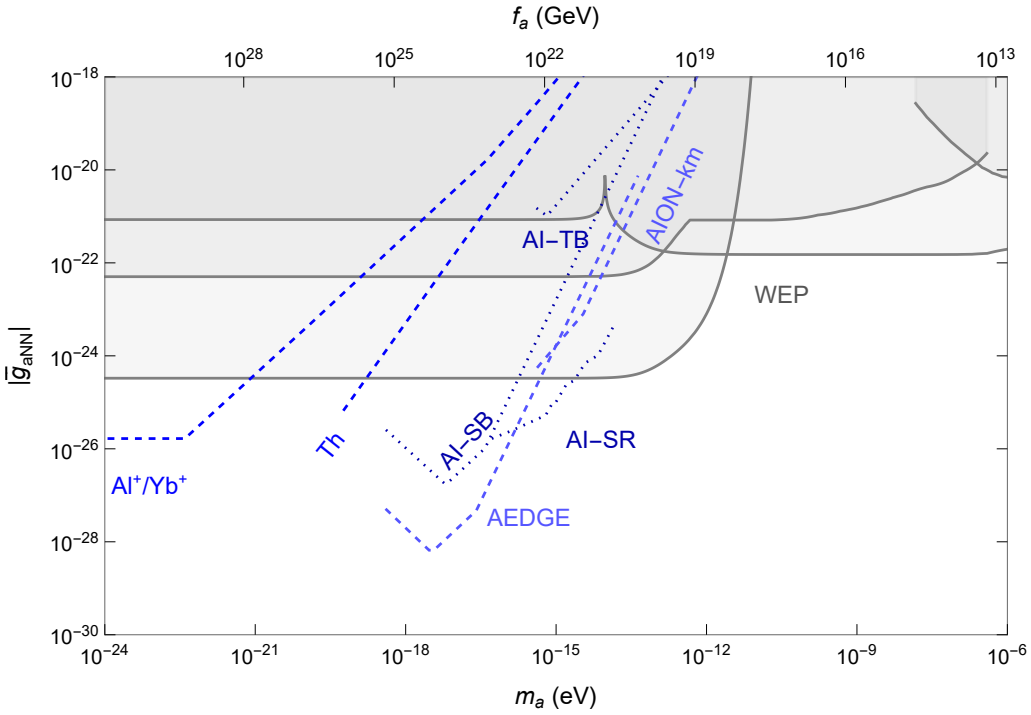

Figure 9. Limits and projections on $\bar{g}_{aNN}$. See figure 6 for details on the projections, and refs. [26, 28] for the WEP bounds. The SM effect is once again small, $\sim 10^{-34}$ at $m_a = 10^{-6}$ eV.

contribution of axion DM to nucleon magnetic moments is assumed to scale as $1/m_N(t)$, we can also estimate the resulting limits on the axion-nucleon coupling coming from hyperfine transitions. The best estimated projection from a Cs/Sr$^+$ system [46] lies close to the Al$^+$/Yb$^+$ line and is not shown here. Unlike the previously discussed interactions, no existing data can improve the WEP bounds (and are thus not shown in figure 9), and only proposed experiments do better. Again we stress, that the limits are not computed in a consistent way and we will provide more accurate computations in specific high-energy scenarios in the section below.

Axion-pion coupling. Pion loops play a part in all of the above-mentioned observables, and thus $\bar{g}_{a\pi\pi}$ is in principle detectable from several terms in eq. (4.3). Nevertheless, one can expect the contribution to $\bar{g}_{a\gamma\gamma}$ to dominate in terms of constraining power due to larger scale suppressions in other terms, as well as better frequency stability of optical clocks. In the absence of other direct measurements in the variation of pion mass, we rely completely on the bounds arising from eq. (3.6). The resulting constraints would look similar to figure 6 with the vertical axis rescaled by about one order of magnitude. As we will see below in various BSM scenarios, the pion couplings play an important role.

5 The bigger picture

So far our analysis has been performed at the level of eq. (2.4) without specifying the sources of CP violation beyond the $\bar{\theta}$ term. As such, the results in figures 6–9 do not depend on the axionic nature of Dark Matter, making them equally valid for ULDM. In the rest of

JHEP11(2023)012

this work, we will consider several BSM scenarios and study how the CP-violating terms in eq. (2.4) are generated. We subsequently discuss the sensitivity of searches for oscillating constants due to axionic DM and compare them to EDM searches that constrain additional sources of CP violation directly. We again borrow heavily from our older work [26] where we have provided the necessary EDM computations and here we focus on the results. We will study three different scenarios:

1. An explicit BSM scenario involving scalar leptoquarks.
2. A minimal left-right symmetric scenario.
3. A scenario where BSM CP violation is dominated by the chromo-electric dipole moments of down-type quarks.

In each scenario we will compare the reach of searches for EDMs, axionic forces, and axion-induced oscillations of fundamental constants.

5.1 A leptoquark scenario

We now consider a BSM model with a $S_1 \in (\bar{3}, 1, 1/3)$ leptoquark (LQ). This scenario induces CP-violating SM-EFT operators which generate both EDMs and oscillations of fundamental constants, allowing us to compare the resulting bounds. The renormalizable couplings of the model are

$$\mathcal{L}_{LQ} = S_1^{\gamma} \left[\bar{Q}_{\gamma}^{c,I} y_{LL} \epsilon_{IJ} L^J + \overline{u^c}_R y_{RR} e_R \right] + \text{h.c.}\,, \tag{5.1}$$

where Q and L are the quark and lepton doublets respectively, and γ is a color index. We focus on couplings to first-generation quarks and leptons. We have not considered operators without quarks that in principle are also induced in the model as they are less interesting from the present point of view, and we also switch off LQ couplings with two quarks. We assume the leptoquarks to be heavy in order to avoid LHC constraints, which probe masses between 1 and 2 TeV [82, 83] for LQs that mainly couple to the first generation, and integrate them out at their threshold scale.

At $\mu \simeq m_{S_1}$, this leads first of all to a large correction to $\bar{\theta}$ [26, 84]

$$|\delta\bar{\theta}| \simeq \frac{1}{(4\pi)^2} \frac{m_e}{m_u} \text{Im}\left(y_{LL}^* y_{RR}\right)\,. \tag{5.2}$$

Unless we tune the phase of the Yukawa couplings to very small values by hand, the correction to $\bar{\theta}$ is unacceptably large. Apart from fine-tuning the tree-level contribution to $\bar{\theta}$ to cancel the $\delta\bar{\theta}$, the only other solution is to relax $\bar{\theta}$ to small values in the infrared through the axion mechanism.

In addition to renormalizing $\bar{\theta}$, integrating out LQs leads to several dimension-six SM-EFT operators. Here we are mainly interested in dimension-six electron-quark interactions which, once mapped to LEFT, take the form

$$\mathcal{L}_{eu} = L^{\text{S,RR}}_{\substack{eu \\ eeuu}} (\bar{e}_L e_R)(\bar{u}_L u_R)\,, \qquad L^{\text{S,RR}}_{\substack{eu \\ eeuu}} = -\frac{1}{2} \frac{y_{LL}^* y_{RR}}{m_{S_1}^2}\,. \tag{5.3}$$

JHEP11(2023)012

If $L^{\mathrm{S,RR}}_{\substack{eu\\eeuu}}$ has a nonzero imaginary part, then the electron-quark interaction violates CP symmetry and contributes to the EDMs of polar molecules such as ThO and HfF [57, 58, 85]. The contributions of the above interaction to EDMs are summarized in appendix B. In addition, as worked out in ref. [26], the PQ mechanism results in the CP-odd axion-electron coupling

$$\bar{g}_{aee} = \frac{m_*}{2f_a}\frac{m_\pi^2 F_\pi^2}{m_u + m_d}\frac{1}{m_u}\mathrm{Im}\left(L^{\mathrm{S,RR}}_{\substack{eu\\eeuu}}\right) , \tag{5.4}$$

and we stress that this interaction depends on the same combination of couplings that enters the correction to $\bar{\theta}$ in eq. (5.2). The LQ extension thus nicely illustrates the schematic picture in figure 1. In what follows, we will set $\mathrm{Im}\,(y^*_{LL}y_{RR}) = 1$ for the couplings to up-quark and electrons in order to illustrate the constraints. Other choices of couplings can simply be obtained by rescaling the value of m_{S_1}.

The upper bounds on $\bar{g}_{aee}$ shown in figure 7 can now be understood in terms of the LQ parameters and can be seen to constrain the combination $\mathrm{Im}(y^*_{LL}y_{RR})/(f_a m^2_{S_1})$. The bounds on the leptoquark mass, as a function of m_a (or f_a) are depicted in figure 10. The projected bounds from the oscillating α_{em} probes are several orders of magnitude better than the WEP constraints for small axion masses. The EDM constraints from HfF and $\mathrm{d_{Hg}}$ measurements are shown as horizontal lines in the plot, while the bound from ThO is slightly weaker than the HfF limit and is thus not shown. These limits are far more stringent than any other bounds across the whole axion mass range.

Coupling to muons. If we instead allow the LQ to couple to different generations, the bounds on m_{S_1} can change dramatically. Consider a scenario where the axion couples to muons and up quarks with $\mathcal{O}(1)$ Yukawa couplings and sizable phases, while the other elements of y_{LL} and y_{RR} are set to zero. Again a large threshold correction to $\bar{\theta}$ is induced which requires an axion solution which leads to a nonzero CP-odd coupling $\bar{g}_{a\mu\mu}$.

However, in this case the EDM limits are far weaker. The muon EDM is induced when evolving the quark-muon four-fermion interaction to lower energies and we obtain

$$\left|\frac{d_\mu}{e}\right| \approx \frac{1}{m^2_{S_1}}\frac{m_u}{(4\pi)^2}\left[4\log\left(\frac{m_{S_1}}{\Lambda_\chi}\right) + \frac{7}{2}\right] + \ldots \tag{5.5}$$

where $\Lambda_\chi = 2\,\mathrm{GeV}$ is a low-energy scale where perturbative QCD should be matched to chiral EFT. In addition there is a non-perturbative contribution arising from this matching to chiral EFT, which comes with a poorly known QCD matrix element [86]. As the nonperturbative contribution is expected to be of the same size as the perturbative term, we use the latter to estimate the total contribution. The best muon EDM limit arises from considering its contributions to the EDMs of polar molecules [58, 59] which gives approximately

$$|d_\mu| < 7 \times 10^{-21}\, e\,\mathrm{cm}\,, \tag{5.6}$$

which is more stringent than the direct limit [87].

JHEP11(2023)012

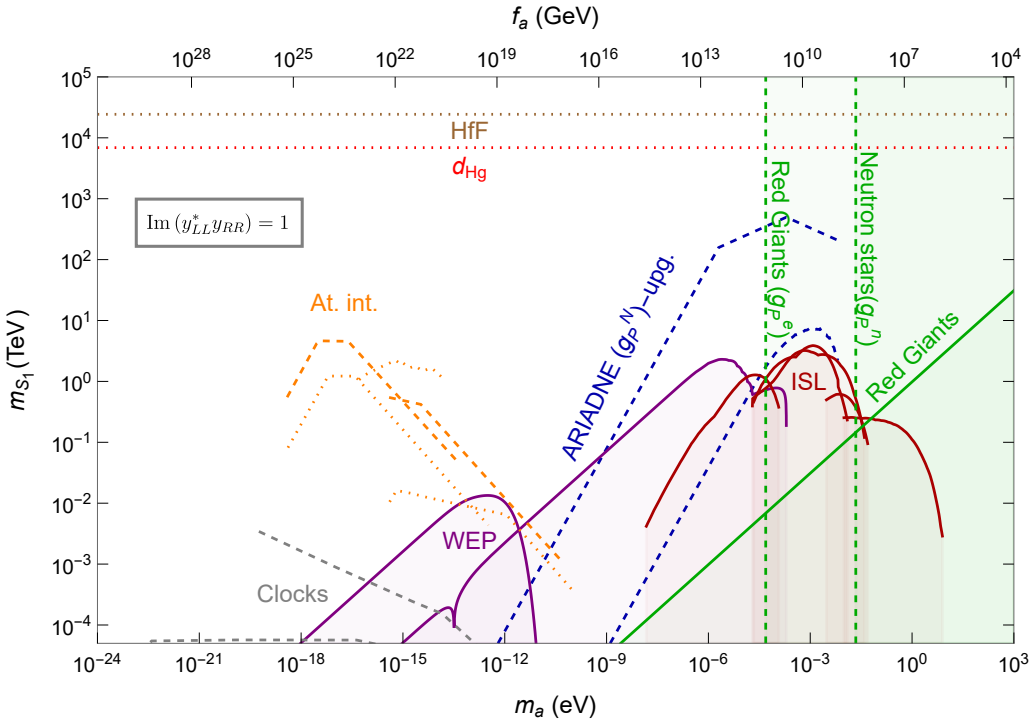

Figure 10. Constraints on the leptoquark mass as a function of axion mass (or decay constant) as discussed in section 5.1, for a scenario with mixing between up-quark and electron. The LQ Yukawa couplings are fixed to 1 as indicated in the figure. The atomic and nuclear clock bounds are shown in grey, and the prospects for atom interferometry experiments are shown orange (see figure 6 for details); note that the existing bounds are too weak to enter the picture. The reader is referred to ref. [26] for an explanation of the bounds not discussed here.

We collect the various limits in figure 11. The EDM limits are now less stringent compared to the electron case but still outperform the present-day searches for fifth forces and time-varying fundamental constants (mainly $\alpha_{\rm em}(t)$ in this case). Future interferometers could become competitive with the EDM limits in a small window of axion masses, assuming the EDM experiments do not improve. However, we must keep in mind that all bounds for muonic couplings are fairly weak and only probe rather light LQ masses that can already be probed by the LHC experiments. We do not explicitly show the collider constraints, but note that these reach scales of 1−2 TeV for couplings to muons [82], beyond the mass scales considered in the figure.

5.2 Left-right symmetric model

Left-right symmetric models (LRSM) introduce a new gauge symmetry $\mathrm{SU}(2)_R \times \mathrm{U}(1)_{B-L}$ in addition to the $\mathrm{SU}(3)_C$ and $\mathrm{SU}(2)_L$ symmetries of the SM. This gauge group is broken to $\mathrm{U}(1)_Y$ at an energy scale higher than the electroweak scale, characterised by the vev of a right-handed scalar triplet field, v_R, which is related to the mass of the right-handed W-boson, m_{W_R} [88]. In specific variants of the model with exact parity symmetry, the bare QCD theta term is forbidden seemingly resolving the strong CP problem. However, once

JHEP11(2023)012

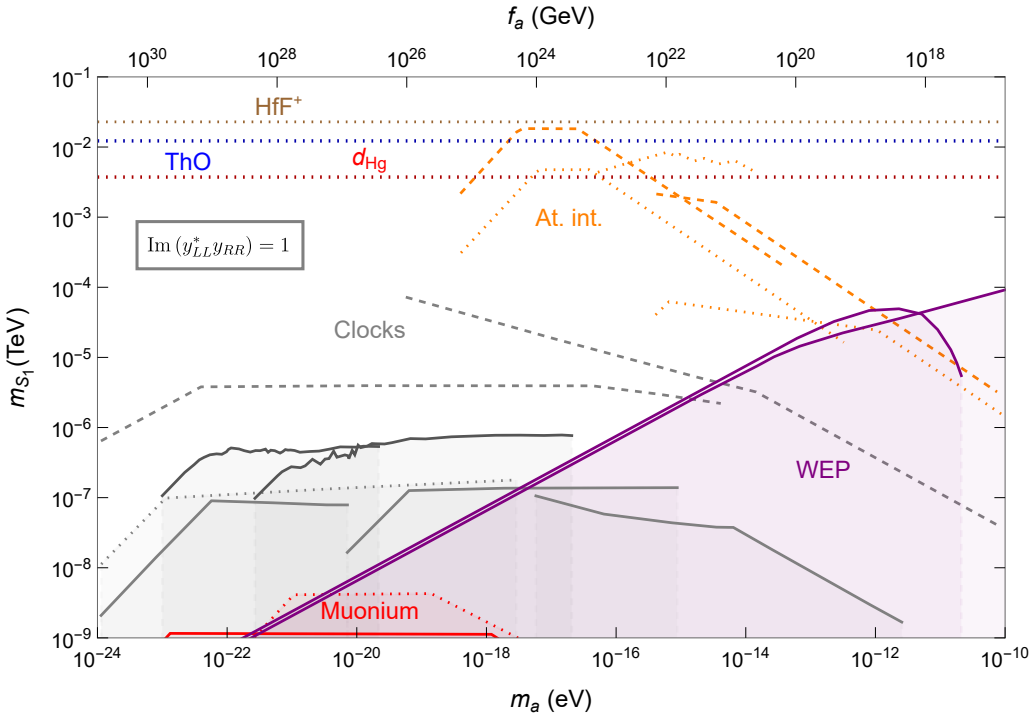

Figure 11. Constraints on the leptoquark mass as a function of axion mass (or decay constant) as discussed in section 5.1, for a scenario with mixing between up-quark and muon. Once again, the Yukawa couplings are set to 1 as shown in the figure. Unlike figure 10, the current bounds from clocks do improve the WEP limits for small m_a. The lower EDM bounds are from ref. [59], while the HfF$^+$ bound uses the same prescription but with more recent data [58]. Rest of the limits and projections can be inferred from figures 8 and 10.

parity is spontaneously broken at lower energy scales new contributions to $\bar{\theta}$ are induced, which are significant [89]. These corrections again point towards a PQ mechanism as an attractive solution.

Within the mLRSM, additional dimension-six operators are induced that violate CP. In particular, the exchange of a W_R leads to a CP-odd four-quark operator that couples left- and right-handed quarks and is sometimes called the four-quark left-right (FQLR) operator [90]:

$$\mathcal{L}_{6,\,\mathrm{FQLR}} = iC_{\mathrm{FQLR}}\left(\bar{u}_L\gamma^\mu d_L\,\bar{d}_R\gamma_\mu u_R - \bar{d}_L\gamma^\mu u_L\,\bar{u}_R\gamma_\mu d_R\right)\,, \tag{5.7}$$

where

$$C_{\mathrm{FQLR}} = |V_{ud}|^2\frac{g_R^2}{m_{W_R}^2}\frac{\xi\sin\alpha}{1+\xi^2}\,, \tag{5.8}$$

in terms of the SU(2)$_R$ gauge coupling, $g_R = g$, a ratio of vacuum expectation values, ξ, which determines the amount of W_L-W_R mixing, and a spontaneous CP-violating phase, α. The FQLR operator leads to a very rich EDM phenomenology of nucleons, nuclei, and diamagnetic atoms which has been worked out in detail in the literature [90–92]. In particular, the operator contributes to the nucleon EDMs, as well as pion-nucleon couplings which can induce nuclear EDMs, see appendix B for details.

JHEP11(2023)012

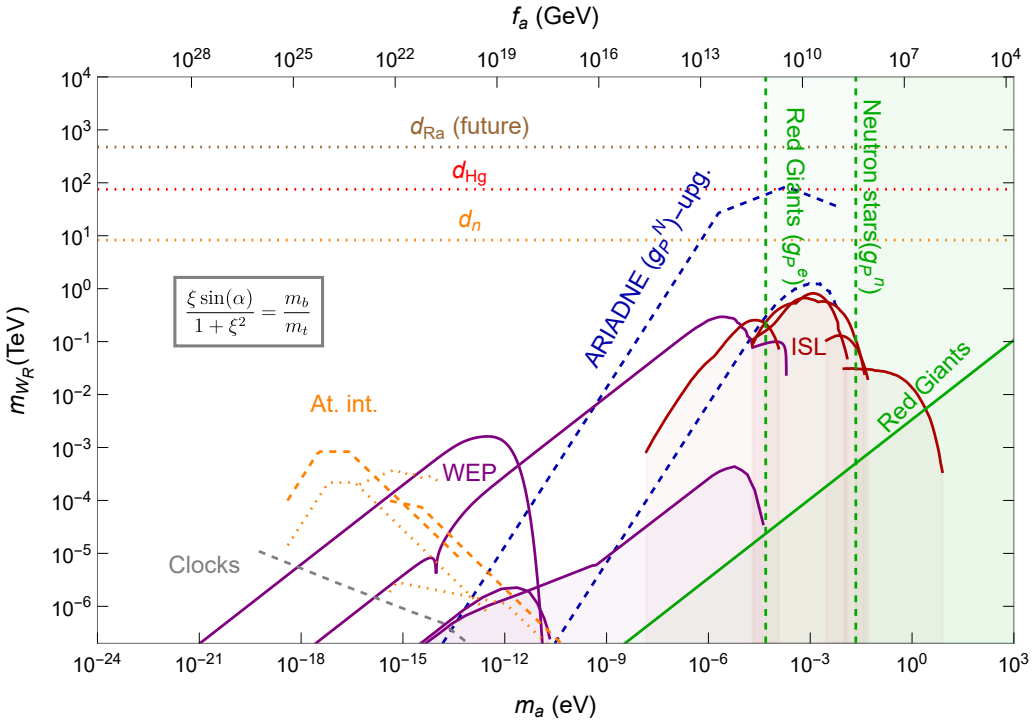

Figure 12. Constraints on the right-handed W-boson mass as discussed in section 5.2, with the parameters related to $W_L - W_R$ mixing fixed as indicated in the figure. The atomic clock and interferometer bounds are derived essentially from $\bar{g}_{a\gamma\gamma}$ limits in figure 6. Once again, the current clock bounds are too weak to be shown.

The combination of the FQLR operator with the PQ mechanism leads to CP-odd axion interactions with hadrons. In particular, it gives rise to the following axion-nucleon coupling [26]

$$\bar{g}^{(0)}_{aNN} \simeq \left(0.11\,\text{GeV}^2\right) \frac{F_\pi}{f_a}\, C_{\text{FQLR}}\,, \tag{5.9}$$

in agreement with the NDA expectations in table 2 for the L_{qq} operators. Within the model, this coupling dominates axionic fifth forces. In addition, in the presence of axion DM it leads to time-varying nucleon masses which can be probed through their impact on hyperfine transitions. However, somewhat more stringent constraints can be set through the induced axion-pion interactions

$$\bar{g}^{(0)}_{a\pi\pi} \simeq -(0.45\,\text{GeV})^2 \frac{F_\pi^2}{f_a}\, C_{\text{FQLR}}\,. \tag{5.10}$$

This result again agrees with the NDA estimate which estimated $|\bar{g}^{(0)}_{a\pi\pi}| = \mathcal{O}(F_\pi^2 \Lambda_\chi^2 / f_a\, C_{\text{FQLR}})$. These couplings lead to changes in the fine-structure constant through eq. (3.6) with a scaling $\bar{g}_{a\gamma\gamma} = (\alpha/(4\pi))(\bar{g}^{(0)}_{a\pi\pi}/m_\pi^2)$ and are thus enhanced by two powers in the chiral power counting, Λ_χ^2/m_π^2, over the direct contributions given in table 2.

We collect all relevant limits in figure 12 where we present the constraints on m_{W_R} as a function of the axion mass. To generate these plots we have set $\xi/(1+\xi^2) = m_b/m_t$ [92, 93]

JHEP11(2023)012

and $\sin\alpha = 1$. We observe that EDM limits are much more stringent than current searches for fifth-forces and oscillating fundamental constants. Collider searches also provide constraints up to $m_{W_R} \gtrsim 5\,\text{TeV}$ (not shown in figure 12) for W_R bosons decaying to di-jets [94, 95], top and bottom quarks [96–98], or heavy neutrinos [99, 100]. Projected atomic clock experiments are competitive with fifth force experiments for $m_a \simeq 10^{-18}\,\text{eV}$, but are very far away from EDM limits. Future interferometer experiments could significantly improve on existing axion searches in the same axion mass range, but would still be many orders of magnitude away from EDM limits. Somewhat more promising is the proposed ARIADNE experiment, which does not rely on axions providing the DM abundance, but looks for axion-induced monopole-dipole interactions. The projected constraints could overtake EDM limits for axion masses around $10^{-4}\,\text{eV}$ as already pointed out in refs. [26, 101].

5.3 Chromo-electric dipole moments

As the final example, we consider a model where the CP-violation is dominated by chromo-electric dipole moments (CEDMs). Employing only CEDM terms for the first generation of quarks, the Lagrangian is

$$\mathcal{L}_{\text{CEDM}} = L_5^u \bar{u}_L T^A G^A_{\mu\nu} \sigma^{\mu\nu} u_R + L_5^d \bar{d}_L T^A G^A_{\mu\nu} \sigma^{\mu\nu} d_R + \text{h.c.}\,, \tag{5.11}$$

where T^A are the $\text{SU}(3)_C$ generators and we will assume that the Wilson coefficients scale as $L_5^q \sim m_q/\Lambda^2$. For concreteness, we turn on only the down-quark CEDM. Similar to the FQLR operator, this interaction induces the nucleon EDMs and pion-nucleon couplings which can generate nuclear EDMs, see appendix B for details. In addition, the PQ mechanism then results in an axion-nucleon coupling [26]

$$\bar{g}^{(0)}_{aNN} \simeq \left(\frac{0.0054\,\text{GeV}^2}{m_d}\right) \frac{1}{f_a} \text{Im}\left(L_5^d\right), \tag{5.12}$$

where we show the m_d dependence explicitly as it cancels out with the m_d scaling in L_5^d when extracting the limits on Λ. Unlike for the FQLR, for the CEDMs no axion-pion-pion interaction is induced at this order.

The bounds on the BSM scale Λ in this case are shown in figure 13. Like the previous example, the atomic clock and interferometer bounds are rather weak although they do better than WEP bounds for tiny m_a in this case as well. The EDM limits completely dominate across all mass scales and only the future ARIADNE experiment has any hope of competing with these constraints.

6 Conclusions and discussion

Axions can provide a simultaneous explanation of two problems in the SM: the lack of a DM candidate and the absence of strong CP violation. Already within the SM there exist more sources of CP violation and there are good reasons to believe that BSM theories contain additional sources, for instance to account for the universal matter/antimatter

JHEP11(2023)012

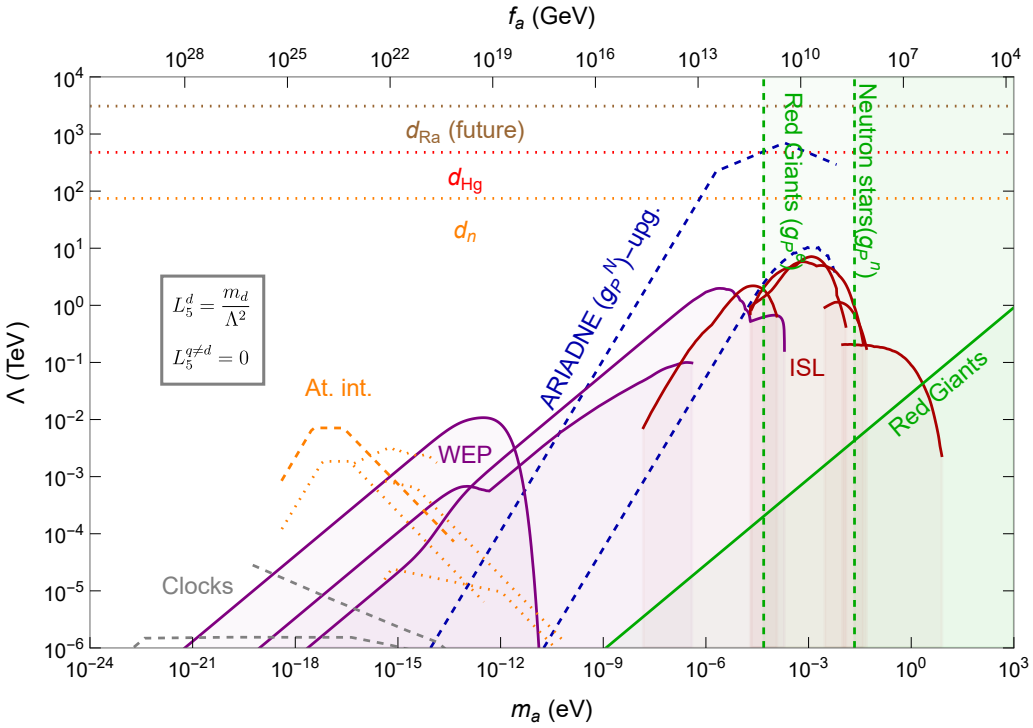

Figure 13. Constraints on the BSM scale Λ for the CEDM scenario discussed in section 5.3, where only the down-quark CEDM contribution is considered.

asymmetry. In presence of non-$\bar{\theta}$ sources of CP violation, the Peccei-Quinn mechanism leads to CP-violating interactions between axions and SM fields, and, at lower energies, to CP-violating interactions between axions and hadrons. These interactions were constructed in the framework of the Standard Model EFT in ref. [26], which provides a direct connection between the strength and form of CP-odd axion interactions with hadrons and leptons and general underlying sources of CP violation at the quark level.

In this work we go one step further and assume that axions are light and form the DM of our universe. In this case, the CP-odd axion couplings can effectively be interpreted as time-oscillating fundamental constants. For example, the fine-structure constant $\alpha_{\rm em}$ and SM particle masses will now oscillate with a frequency set by the axion mass and an amplitude that depends on the strength of the CP-violating sources. The resulting phenomenology is very similar to that of ultralight scalar DM. The oscillations can be probed by precision experiments that, for example, look for variations in atomic transition frequencies. In the first part of this paper, we work out how a variety of CP-violating axion couplings are connected to searches for oscillating fundamental constants. In particular, we demonstrate that loop corrections can be relevant because the different experimental searches have very different sensitivities so that loop suppressions can be overcome. This part of our work is independent of the axionic nature of DM and equally applies to scalar DM.

We subsequently compared fifth-force experiments, test of the weak equivalence principle (WEP), to searches for time-varying fundamental constants. In general we find that for

JHEP11(2023)012

very light axions, the latter probes have the potential to significantly improve the limits on CP-odd axion-photon, -electron, -muon, and -nucleon couplings from fifth-force and WEP experiments. At higher masses, however, the bounds set by clock experiments are weaker as the oscillation frequency becomes too large to be detected with considerable precision. This could be partially overcome by future interferometer experiments. We find that the most sensitive searches are related to measurements of optical transitions which can constrain a time-varying fine-structure constant. For example, CPV axion-muon couplings lead to oscillating muon masses and, through loop corrections, to oscillating $\alpha_{\rm em}$. In this case, searches for the latter outperform more direct limits by 5 orders of magnitude. Similarly, searches for CPV axion-electron interactions through hyperfine transitions in microwave clocks cannot compete with the indirect limits obtained from optical transitions.

In the second part of the paper, we focus on the specific case of axion DM. In this case, the CP-violating axion-SM interactions are sourced by non-$\bar{\theta}$ sources of CP violation and can therefore be related to axion-independent CP-violating effects. We consider several scenarios involving such sources of CP violation, both within the Standard Model and beyond. The CPV axion couplings can be expressed in terms of the model parameters in these scenarios, allowing us to see how the constraints from (a lack of) variation in fundamental constants compare to direct limits on extra sources of CP violation from electric dipole moment experiments. While future searches for time-varying fundamental constants can greatly improve limits obtained from fifth-force experiments, we find that, in general, they fall short of EDM sensitivities. That is, mechanisms that would predict, for example, a detectable axion-induced time-varying fine-structure constant within axion models, should have led already to a detection in any of the recent electric dipole moment experiments. This conclusion can be avoided when the axion does not couple to first-generation particles, for example, the EDM limits are significantly less stringent in the case of couplings to muons. Furthermore, EDM limits do not apply for ultralight scalar DM so that the search for time-varying constants remains well motivated. Finally, future prospects, for instance through nuclear clocks and/or quantum sensing [102], have the potential to greatly enhance the search for time-varying constants and it might very well be that such searches provide the best chance to measure CP-violating axion interactions in the future.

Acknowledgments

We thank Arghavan Safavi Naini for useful discussions and encouragement. JdV acknowledges support from the Dutch Research Council (NWO) in the form of a VIDI grant. WD acknowledges support by the U.S. DOE under Grant No. DE-FG02-00ER41132.

A Contributions of LEFT operators

Here we discuss the contributions of LEFT operators to eq. (2.4). The operators that are expected to give the leading contributions, those unsuppressed by derivatives in χPT, are listed in table 1 [26]. Here we only consider the operators that give rise to unsuppressed operators in the chiral Lagrangian. The relevant four-quark operators arise from

JHEP11(2023)012

$(\bar{L}R)X + \text{H.c.}$	
$\mathcal{O}_{u\gamma}$	$\bar{u}_{Lp}\sigma^{\mu\nu}u_{Rr}\,F_{\mu\nu}$
$\mathcal{O}_{d\gamma}$	$\bar{d}_{Lp}\sigma^{\mu\nu}d_{Rr}\,F_{\mu\nu}$
$\mathcal{O}_{uG}$	$\bar{u}_{Lp}\sigma^{\mu\nu}T^A u_{Rr}\,G^A_{\mu\nu}$
$\mathcal{O}_{dG}$	$\bar{d}_{Lp}\sigma^{\mu\nu}T^A d_{Rr}\,G^A_{\mu\nu}$

X^3	
$\mathcal{O}_{\widetilde{G}}$	$f^{ABC}\widetilde{G}^{A\nu}_{\mu}G^{B\rho}_{\nu}G^{C\mu}_{\rho}$

$(\bar{L}L)(\bar{L}L)$	
$\mathcal{O}^{V,LL}_{\nu u}$	$(\bar{\nu}_{Lp}\gamma^\mu\nu_{Lr})(\bar{u}_{Ls}\gamma_\mu u_{Lt})$
$\mathcal{O}^{V,LL}_{\nu d}$	$(\bar{\nu}_{Lp}\gamma^\mu\nu_{Lr})(\bar{d}_{Ls}\gamma_\mu d_{Lt})$
$\mathcal{O}^{V,LL}_{eu}$	$(\bar{e}_{Lp}\gamma^\mu e_{Lr})(\bar{u}_{Ls}\gamma_\mu u_{Lt})$
$\mathcal{O}^{V,LL}_{ed}$	$(\bar{e}_{Lp}\gamma^\mu e_{Lr})(\bar{d}_{Ls}\gamma_\mu d_{Lt})$
$\mathcal{O}^{V,LL}_{\nu edu}$	$(\bar{\nu}_{Lp}\gamma^\mu e_{Lr})(\bar{d}_{Ls}\gamma_\mu u_{Lt}) + \text{H.c.}$

$(\bar{R}R)(\bar{R}R)$	
$\mathcal{O}^{V,RR}_{eu}$	$(\bar{e}_{Rp}\gamma^\mu e_{Rr})(\bar{u}_{Rs}\gamma_\mu u_{Rt})$
$\mathcal{O}^{V,RR}_{ed}$	$(\bar{e}_{Rp}\gamma^\mu e_{Rr})(\bar{d}_{Rs}\gamma_\mu d_{Rt})$

$(\bar{L}L)(\bar{R}R)$	
$\mathcal{O}^{V,LR}_{\nu u}$	$(\bar{\nu}_{Lp}\gamma^\mu\nu_{Lr})(\bar{u}_{Rs}\gamma_\mu u_{Rt})$
$\mathcal{O}^{V,LR}_{\nu d}$	$(\bar{\nu}_{Lp}\gamma^\mu\nu_{Lr})(\bar{d}_{Rs}\gamma_\mu d_{Rt})$
$\mathcal{O}^{V,LR}_{eu}$	$(\bar{e}_{Lp}\gamma^\mu e_{Lr})(\bar{u}_{Rs}\gamma_\mu u_{Rt})$
$\mathcal{O}^{V,LR}_{ed}$	$(\bar{e}_{Lp}\gamma^\mu e_{Lr})(\bar{d}_{Rs}\gamma_\mu d_{Rt})$
$\mathcal{O}^{V,LR}_{ue}$	$(\bar{u}_{Lp}\gamma^\mu u_{Lr})(\bar{e}_{Rs}\gamma_\mu e_{Rt})$
$\mathcal{O}^{V,LR}_{de}$	$(\bar{d}_{Lp}\gamma^\mu d_{Lr})(\bar{e}_{Rs}\gamma_\mu e_{Rt})$
$\mathcal{O}^{V,LR}_{\nu edu}$	$(\bar{\nu}_{Lp}\gamma^\mu e_{Lr})(\bar{d}_{Rs}\gamma_\mu u_{Rt}) + \text{H.c.}$
$\mathcal{O}^{V1,LR}_{uu}$	$(\bar{u}_{Lp}\gamma^\mu u_{Lr})(\bar{u}_{Rs}\gamma_\mu u_{Rt})$
$\mathcal{O}^{V8,LR}_{uu}$	$(\bar{u}_{Lp}\gamma^\mu T^A u_{Lr})(\bar{u}_{Rs}\gamma_\mu T^A u_{Rt})$
$\mathcal{O}^{V1,LR}_{ud}$	$(\bar{u}_{Lp}\gamma^\mu u_{Lr})(\bar{d}_{Rs}\gamma_\mu d_{Rt})$
$\mathcal{O}^{V8,LR}_{ud}$	$(\bar{u}_{Lp}\gamma^\mu T^A u_{Lr})(\bar{d}_{Rs}\gamma_\mu T^A d_{Rt})$
$\mathcal{O}^{V1,LR}_{du}$	$(\bar{d}_{Lp}\gamma^\mu d_{Lr})(\bar{u}_{Rs}\gamma_\mu u_{Rt})$
$\mathcal{O}^{V8,LR}_{du}$	$(\bar{d}_{Lp}\gamma^\mu T^A d_{Lr})(\bar{u}_{Rs}\gamma_\mu T^A u_{Rt})$
$\mathcal{O}^{V1,LR}_{dd}$	$(\bar{d}_{Lp}\gamma^\mu d_{Lr})(\bar{d}_{Rs}\gamma_\mu d_{Rt})$
$\mathcal{O}^{V8,LR}_{dd}$	$(\bar{d}_{Lp}\gamma^\mu T^A d_{Lr})(\bar{d}_{Rs}\gamma_\mu T^A d_{Rt})$
$\mathcal{O}^{V1,LR}_{uddu}$	$(\bar{u}_{Lp}\gamma^\mu d_{Lr})(\bar{d}_{Rs}\gamma_\mu u_{Rt}) + \text{H.c.}$
$\mathcal{O}^{V8,LR}_{uddu}$	$(\bar{u}_{Lp}\gamma^\mu T^A d_{Lr})(\bar{d}_{Rs}\gamma_\mu T^A u_{Rt}) + \text{H.c.}$

$(\bar{L}R)(\bar{L}R) + \text{H.c.}$	
$\mathcal{O}^{S,RR}_{eu}$	$(\bar{e}_{Lp}e_{Rr})(\bar{u}_{Ls}u_{Rt})$
$\mathcal{O}^{T,RR}_{eu}$	$(\bar{e}_{Lp}\sigma^{\mu\nu}e_{Rr})(\bar{u}_{Ls}\sigma_{\mu\nu}u_{Rt})$
$\mathcal{O}^{S,RR}_{ed}$	$(\bar{e}_{Lp}e_{Rr})(\bar{d}_{Ls}d_{Rt})$
$\mathcal{O}^{T,RR}_{ed}$	$(\bar{e}_{Lp}\sigma^{\mu\nu}e_{Rr})(\bar{d}_{Ls}\sigma_{\mu\nu}d_{Rt})$
$\mathcal{O}^{S,RR}_{\nu edu}$	$(\bar{\nu}_{Lp}e_{Rr})(\bar{d}_{Ls}u_{Rt})$
$\mathcal{O}^{T,RR}_{\nu edu}$	$(\bar{\nu}_{Lp}\sigma^{\mu\nu}e_{Rr})(\bar{d}_{Ls}\sigma_{\mu\nu}u_{Rt})$
$\mathcal{O}^{S1,RR}_{uu}$	$(\bar{u}_{Lp}u_{Rr})(\bar{u}_{Ls}u_{Rt})$
$\mathcal{O}^{S8,RR}_{uu}$	$(\bar{u}_{Lp}T^A u_{Rr})(\bar{u}_{Ls}T^A u_{Rt})$
$\mathcal{O}^{S1,RR}_{ud}$	$(\bar{u}_{Lp}u_{Rr})(\bar{d}_{Ls}d_{Rt})$
$\mathcal{O}^{S8,RR}_{ud}$	$(\bar{u}_{Lp}T^A u_{Rr})(\bar{d}_{Ls}T^A d_{Rt})$
$\mathcal{O}^{S1,RR}_{dd}$	$(\bar{d}_{Lp}d_{Rr})(\bar{d}_{Ls}d_{Rt})$
$\mathcal{O}^{S8,RR}_{dd}$	$(\bar{d}_{Lp}T^A d_{Rr})(\bar{d}_{Ls}T^A d_{Rt})$
$\mathcal{O}^{S1,RR}_{uddu}$	$(\bar{u}_{Lp}d_{Rr})(\bar{d}_{Ls}u_{Rt})$
$\mathcal{O}^{S8,RR}_{uddu}$	$(\bar{u}_{Lp}T^A d_{Rr})(\bar{d}_{Ls}T^A u_{Rt})$

$(\bar{L}R)(\bar{R}L) + \text{H.c.}$	
$\mathcal{O}^{S,RL}_{eu}$	$(\bar{e}_{Lp}e_{Rr})(\bar{u}_{Rs}u_{Lt})$
$\mathcal{O}^{S,RL}_{ed}$	$(\bar{e}_{Lp}e_{Rr})(\bar{d}_{Rs}d_{Lt})$
$\mathcal{O}^{S,RL}_{\nu edu}$	$(\bar{\nu}_{Lp}e_{Rr})(\bar{d}_{Rs}u_{Lt})$

Table 1. The B- and L-conserving operators of the LEFT of dimension five and six that contribute to CP-violating effects in the meson sector at leading order. Only the hadronic operators that contribute to the non-derivative meson interactions and the semi-leptonic operators that can be written as external sources (shown in blue) are listed.

the $(\bar{L}L)(\bar{R}R)$, $(\bar{L}R)(\bar{L}R)$, and $(\bar{L}R)(\bar{R}L)$ classes. The unsuppressed semi-leptonic operators are generated by the $(\bar{L}R)(\bar{L}R)$ class, while the dipole and Weinberg operators arise from the $(\bar{L}R)X$ and X^3 classes.

We employ NDA to estimate the contributions of these interactions to the axion couplings in eq. (2.4) and list the results in table 2. All estimates are based on NDA, with the exception of the contribution to $\bar{g}^{(0)}_{a\pi\pi}$ from the quark CEDMs, shown in blue. This con-

JHEP11(2023)012

	$L_{q\gamma}$	L_{qG}	$L_{\tilde{G}}$	L_{qq}	$L_{q\ell}$
$\bar{g}^{(0)}_{aNN}$	$eF_\pi \frac{F_\pi}{f_a}$	$\Lambda_\chi \frac{F_\pi}{f_a}$	$\Lambda_\chi^2 \frac{F_\pi}{f_a}$	$F_\pi \Lambda_\chi \frac{F_\pi}{f_a}$	–
$\bar{g}^{(0)}_{a\ell\ell}$	–	–	–	–	$F_\pi \Lambda_\chi \frac{F_\pi}{f_a}$
$\bar{g}^{(0)}_{a\pi\pi}$	$eF_\pi \Lambda_\chi \frac{F_\pi}{f_a}$	$\Lambda_\chi^2 \frac{F_\pi}{f_a} \left(\frac{m_q}{\Lambda_\chi}\right)$	$\Lambda_\chi^2 m_q \frac{F_\pi}{f_a}$	$F_\pi \Lambda_\chi^2 \frac{F_\pi}{f_a}$	–
$\bar{g}^{(0)}_{a\gamma\gamma}$	$\frac{e}{4\pi} \frac{F_\pi}{f_a}$	$\frac{\alpha}{4\pi} \frac{F_\pi}{f_a}$	$\alpha F_\pi \frac{F_\pi}{f_a}$	$\frac{\alpha}{4\pi} F_\pi \frac{F_\pi}{f_a}$	$\frac{\alpha}{4\pi} \frac{m_\ell}{\Lambda_\chi} F_\pi \frac{F_\pi}{f_a}$

Table 2. NDA estimates of the direct contributions from LEFT operators to the axion couplings in eq. (2.4). Here q denotes $q = \{u, d\}$ in the Wilson coefficients $L_{q\gamma}$ and L_{qG}. L_{qq} and $L_{q\ell}$ denote flavor-diagonal hadronic and semi-leptonic four-fermion operators in table 1 that give rise to chirally unsuppressed interactions in the chiral Lagrangian, see the text for details. The contribution of L_{qG} to $\bar{g}^{(0)}_{a\pi\pi}$, indicated in blue, is smaller than its naive NDA estimate as explained in the text.

tribution would be estimated by $\Lambda_\chi^2 \frac{F_\pi}{f_a}$ if one would simply apply NDA. However, explicit calculation shows [26] that these leading terms vanish after aligning the vacuum, so that the first contributions are suppressed by a factor of m_q/Λ_χ as shown in the table.

B Contributions to EDMs

The CP-odd electron-nucleon and pion-nucleon interactions discussed in section 5 contribute to the EDMs of nucleons, nuclei, atoms, and molecules. Here we summarize the relevant input needed to estimate these effects.

B.1 EDMs of polar molecules

The semi-leptonic operators considered in section 5.1, contribute to CP-odd scalar and pseudoscalar interactions between nucleons and electrons [85],

$$C_S^{(0)} = -v_H^2 \frac{\sigma_{\pi N}}{m_u + m_d} \mathrm{Im}\left[L^{\mathrm{S,RR}}_{\substack{eu \\ eeuu}}\right], \qquad C_S^{(1)} = -v_H^2 \frac{1}{2} \frac{\delta m_N}{m_d - m_u} \mathrm{Im}\left[L^{\mathrm{S,RR}}_{\substack{eu \\ eeuu}}\right],$$
$$C_P^{(0)} = v_H^2 \frac{m_N B(D-3F)}{3m_\eta^2} \mathrm{Im}\left[L^{\mathrm{S,RR}}_{\substack{eu \\ eeuu}}\right], \qquad C_P^{(1)} = -v_H^2 \frac{m_N B g_A}{m_\pi^2} \mathrm{Im}\left[L^{\mathrm{S,RR}}_{\substack{eu \\ eeuu}}\right], \tag{B.1}$$

where v_H is the vev of the Higgs field, at tree level $v_H^2 = \sqrt{2} G_F \simeq (246\,\mathrm{GeV})^2$. Furthermore, $g_A = D + F$ is the axial charge of the nucleon, $\delta m_N = (m_n - m_p)_{QCD}$ is the strong nucleon mass splitting, while the nucleon sigma terms are given by $\sigma_q = m_q \frac{\partial \Delta m_N}{\partial m_q}$, where $\Delta m_N = \frac{m_n + m_p}{2}$, and $\sigma_{\pi N} = \sigma_u + \sigma_d$. The input for these hadronic matrix elements can be summarized as [103–107]

$$\sigma_{\pi N} = (59.1 \pm 3.5)\,\mathrm{MeV}, \qquad \delta m_N = (2.32 \pm 0.17)\,\mathrm{MeV},$$
$$\delta m_N = (2.32 \pm 0.17)\,\mathrm{MeV}, \qquad g_A = 1.27 \pm 0.002\,. \tag{B.2}$$

JHEP11(2023)012

The scalar nucleon-electron couplings, $C_S^{(0,1)}$, contribute to CP-odd effects in polar molecules [108–110]

$$\omega_{\rm HfF} = +(32.0 \pm 1.3)(\text{mrad/s}) \left(\frac{C_S}{10^{-7}}\right) , \tag{B.3}$$

$$\omega_{\rm ThO} = +(181.6 \pm 7.3)(\text{mrad/s}) \left(\frac{C_S}{10^{-7}}\right) , \tag{B.4}$$

in terms of $C_S = C_S^{(0)} + \frac{Z-N}{Z+N} C_S^{(1)}$ where Z and N correspond to the number of protons and neutrons, respectively, of the heaviest atom of the molecule.

B.2 EDMs of nucleons, nuclei, and atoms

In addition to the effects in polar molecules, the semileptonic interactions and the isoscalar and isovector pion-nucleon couplings, $\bar{g}_{0,1}$, induce EDMs of nucleons, nuclei, and diamagnetic atoms. For the FQLR and CEDM operators discussed in sections 5.2 and 5.3, the relevant pion-nucleon couplings are given by [26],

$$\begin{aligned} \bar{g}_0 &= -\frac{\bar{B}}{2F_\pi B} \frac{\delta m_N}{\bar{m}\epsilon} \text{Im}\left(L_5^d\right) , \\ \bar{g}_1 &= \frac{\bar{B}}{F_\pi B} \frac{\Delta m_N}{\bar{m}} \text{Im}\left(L_5^d\right) - 0.62\,\text{GeV}^2\, C_{\rm FQLR} , \end{aligned} \tag{B.5}$$

where $\bar{m} = \frac{m_u+m_d}{2}$, $\bar{m}\epsilon = \frac{m_d-m_u}{2}$, and $\bar{B}/B$ is a ratio of matrix elements of the chromomagnetic operator and the quark condensate. This ratio has been estimated using QCD sum rules [111] as well as through a relation to deep inelastic scattering [112]. Here we follow ref. [112] and use $\bar{B}/B \simeq 0.4\,\text{GeV}^2/g_s(2\,\text{GeV})$ [112, 113] with $g_s(2\,\text{GeV}) \simeq 1.85$. In the above expressions for $\bar{g}_{0,1}$ we neglected possible 'direct' contributions to the pion-nucleon couplings, see ref. [26] for details.

The nucleon EDMs can now be estimated in terms of the nucleon-pion couplings through [114],

$$d_n = -\frac{e g_A}{8\pi^2 F_\pi}\left[\bar{g}_0\left(\log\frac{m_\pi^2}{m_N^2} - \frac{\pi m_\pi}{2m_N}\right) + \frac{\bar{g}_1}{4}(\kappa_1-\kappa_0)\frac{m_\pi^2}{m_N^2}\log\frac{m_\pi^2}{m_N^2}\right] , \tag{B.6}$$

$$d_p = \frac{e g_A}{8\pi^2 F_\pi}\left[\bar{g}_0\left(\log\frac{m_\pi^2}{m_N^2} - \frac{2\pi m_\pi}{m_N}\right) - \frac{\bar{g}_1}{4}\left(\frac{2\pi m_\pi}{m_N} + (5/2+\kappa_1+\kappa_0)\frac{m_\pi^2}{m_N^2}\log\frac{m_\pi^2}{m_N^2}\right)\right] ,$$

where $\kappa_1 = 3.7$ and $\kappa_0 = -0.12$ are related to the nucleon magnetic moments. Here we set the renormalization scale to the nucleon mass m_N in order to estimate the EDMs as function of pion-nucleon couplings, but note that these EDMs in principle also receive direct contributions from the FQLR and CEDM operators. Such contributions depend on poorly controlled matrix elements and we neglect them here, see the discussion in e.g. ref. [26] for more details.

JHEP11(2023)012

neutron and atoms (e cm)			Molecules (mrad/s)	
d_n	$d_{\rm Hg}$	$d_{\rm Ra}$	$\omega_{\rm HfF}$	$\omega_{\rm ThO}$
$1.8 \cdot 10^{-26}$	$6.3 \cdot 10^{-30}$	$1.2 \cdot 10^{-23}$	0.14	1.3

Table 3. Current experimental limits (at 90% C.L.) from measurements on the neutron [1], ^{199}Hg [115], ^{225}Ra [56], YbF [116], HfF [58], and ThO [57].

The Hg EDM can now be written as [117–122],

$$\begin{aligned} d_{\rm Hg} = & -(2.1 \pm 0.5) \cdot 10^{-4} \Big[(1.9 \pm 0.1) d_n + (0.20 \pm 0.06) d_p \\ & + \left(0.13^{+0.5}_{-0.07}\, \bar{g}_0 + 0.25^{+0.89}_{-0.63}\, \bar{g}_1 \right) e\,\text{fm} \Big] \\ & - \left[(0.028 \pm 0.006) C_S - \frac{1}{3} (3.6 \pm 0.4) \left(\frac{Z\alpha}{5 m_N R} C_P \right) \right] \cdot 10^{-20}\, e\,\text{cm}\,, \end{aligned} \tag{B.7}$$

in terms of the nuclear radius $R \simeq 1.2\, A^{1/3}\,\text{fm}$, and $C_P = (C_P^{(n)} \langle \vec{\sigma}_n \rangle + C_P^{(p)} \langle \vec{\sigma}_p \rangle)/(\langle \vec{\sigma}_n \rangle + \langle \vec{\sigma}_p \rangle)$. Here we defined the neutron and proton couplings as $C_P^{(n,p)} = C_P^{(0)} \mp C_P^{(1)}$. For ^{199}Hg we use the values [123]

$$\langle \vec{\sigma}_n \rangle = -0.3249 \pm 0.0515\,, \qquad \langle \vec{\sigma}_p \rangle = 0.0031 \pm 0.0118\,. \tag{B.8}$$

The atomic EDM of Ra is dominated by nuclear CP violation due to octopole-deformation of the nucleus, which somewhat simplifies the relevant expression [117, 124]

$$d_{\rm Ra} = (7.7 \cdot 10^{-4}) \cdot [(2.5 \pm 7.5)\, \bar{g}_0 - (65 \pm 40)\, \bar{g}_1]\, e\,\text{fm}\,. \tag{B.9}$$

The pion-nucleon couplings give the largest contributions to the Ra and Hg EDMs as long as $\bar{g}_{0,1}$ receive contributions at leading order, which is the case for the FQLR and CEDM operators under consideration here. The current best limits are collected in table 3.

Open Access. This article is distributed under the terms of the Creative Commons Attribution License (CC-BY 4.0), which permits any use, distribution and reproduction in any medium, provided the original author(s) and source are credited.

References

[1] C. Abel et al., *Measurement of the Permanent Electric Dipole Moment of the Neutron*, *Phys. Rev. Lett.* **124** (2020) 081803 [arXiv:2001.11966] [INSPIRE].

[2] B. Graner, Y. Chen, E.G. Lindahl and B.R. Heckel, *Reduced Limit on the Permanent Electric Dipole Moment of* ^{199}Hg, *Phys. Rev. Lett.* **116** (2016) 161601 [arXiv:1601.04339] [*Erratum ibid.* **119** (2017) 119901] [INSPIRE].

[3] J. Dragos, T. Luu, A. Shindler, J. de Vries and A. Yousif, *Confirming the Existence of the strong CP Problem in Lattice QCD with the Gradient Flow*, *Phys. Rev. C* **103** (2021) 015202 [arXiv:1902.03254] [INSPIRE].

JHEP11(2023)012

[4] J. Liang et al., *Nucleon Electric Dipole Moment from the θ Term with Lattice Chiral Fermions*, arXiv:2301.04331 [INSPIRE].

[5] R.D. Peccei and H.R. Quinn, *CP Conservation in the Presence of Instantons*, *Phys. Rev. Lett.* **38** (1977) 1440 [INSPIRE].

[6] R.D. Peccei and H.R. Quinn, *Constraints Imposed by CP Conservation in the Presence of Instantons*, *Phys. Rev. D* **16** (1977) 1791 [INSPIRE].

[7] S. Weinberg, *A New Light Boson?*, *Phys. Rev. Lett.* **40** (1978) 223 [INSPIRE].

[8] F. Wilczek, *Problem of Strong P and T Invariance in the Presence of Instantons*, *Phys. Rev. Lett.* **40** (1978) 279 [INSPIRE].

[9] J. Preskill, M.B. Wise and F. Wilczek, *Cosmology of the Invisible Axion*, *Phys. Lett. B* **120** (1983) 127 [INSPIRE].

[10] L.F. Abbott and P. Sikivie, *A Cosmological Bound on the Invisible Axion*, *Phys. Lett. B* **120** (1983) 133 [INSPIRE].

[11] M. Dine and W. Fischler, *The Not So Harmless Axion*, *Phys. Lett. B* **120** (1983) 137 [INSPIRE].

[12] J.E. Kim, *Weak Interaction Singlet and Strong CP Invariance*, *Phys. Rev. Lett.* **43** (1979) 103 [INSPIRE].

[13] M.A. Shifman, A.I. Vainshtein and V.I. Zakharov, *Can Confinement Ensure Natural CP Invariance of Strong Interactions?*, *Nucl. Phys. B* **166** (1980) 493 [INSPIRE].

[14] A.R. Zhitnitsky, *On Possible Suppression of the Axion Hadron Interactions* (in Russian), *Sov. J. Nucl. Phys.* **31** (1980) 260 [INSPIRE].

[15] M. Dine, W. Fischler and M. Srednicki, *A Simple Solution to the Strong CP Problem with a Harmless Axion*, *Phys. Lett. B* **104** (1981) 199 [INSPIRE].

[16] D.E. Kaplan and R. Rattazzi, *Large field excursions and approximate discrete symmetries from a clockwork axion*, *Phys. Rev. D* **93** (2016) 085007 [arXiv:1511.01827] [INSPIRE].

[17] L. Di Luzio, F. Mescia and E. Nardi, *Redefining the Axion Window*, *Phys. Rev. Lett.* **118** (2017) 031801 [arXiv:1610.07593] [INSPIRE].

[18] G. Ballesteros, J. Redondo, A. Ringwald and C. Tamarit, *Standard Model-axion-seesaw-Higgs portal inflation. Five problems of particle physics and cosmology solved in one stroke*, *JCAP* **08** (2017) 001 [arXiv:1610.01639] [INSPIRE].

[19] L. Di Luzio, F. Mescia and E. Nardi, *Window for preferred axion models*, *Phys. Rev. D* **96** (2017) 075003 [arXiv:1705.05370] [INSPIRE].

[20] L. Di Luzio, M. Giannotti, E. Nardi and L. Visinelli, *The landscape of QCD axion models*, *Phys. Rept.* **870** (2020) 1 [arXiv:2003.01100] [INSPIRE].

[21] V. Plakkot and S. Hoof, *Anomaly ratio distributions of hadronic axion models with multiple heavy quarks*, *Phys. Rev. D* **104** (2021) 075017 [arXiv:2107.12378] [INSPIRE].

[22] M. Berbig, *S.M.A.S.H.E.D.: Standard Model Axion Seesaw Higgs inflation Extended for Dirac neutrinos*, *JCAP* **11** (2022) 042 [arXiv:2207.08142] [INSPIRE].

[23] J. Diehl and E. Koutsangelas, *Dine-Fischler-Srednicki-Zhitnitsky-type axions and where to find them*, *Phys. Rev. D* **107** (2023) 095020 [arXiv:2302.04667] [INSPIRE].

JHEP11(2023)012

[24] I.G. Irastorza and J. Redondo, *New experimental approaches in the search for axion-like particles*, *Prog. Part. Nucl. Phys.* **102** (2018) 89 [arXiv:1801.08127] [INSPIRE].

[25] P. Sikivie, *Invisible Axion Search Methods*, *Rev. Mod. Phys.* **93** (2021) 015004 [arXiv:2003.02206] [INSPIRE].

[26] W. Dekens, J. de Vries and S. Shain, *CP-violating axion interactions in effective field theory*, *JHEP* **07** (2022) 014 [arXiv:2203.11230] [INSPIRE].

[27] J.E. Moody and F. Wilczek, *New macroscopic forces?*, *Phys. Rev. D* **30** (1984) 130 [INSPIRE].

[28] C.A.J. O'Hare and E. Vitagliano, *Cornering the axion with CP-violating interactions*, *Phys. Rev. D* **102** (2020) 115026 [arXiv:2010.03889] [INSPIRE].

[29] D.J.E. Marsh, *Axion Cosmology*, *Phys. Rept.* **643** (2016) 1 [arXiv:1510.07633] [INSPIRE].

[30] T. Damour and J.F. Donoghue, *Equivalence Principle Violations and Couplings of a Light Dilaton*, *Phys. Rev. D* **82** (2010) 084033 [arXiv:1007.2792] [INSPIRE].

[31] P.W. Graham and S. Rajendran, *Axion Dark Matter Detection with Cold Molecules*, *Phys. Rev. D* **84** (2011) 055013 [arXiv:1101.2691] [INSPIRE].

[32] J.R. Ellis and M.K. Gaillard, *Strong and Weak CP Violation*, *Nucl. Phys. B* **150** (1979) 141 [INSPIRE].

[33] M. Dine and P. Draper, *Challenges for the Nelson-Barr Mechanism*, *JHEP* **08** (2015) 132 [arXiv:1506.05433] [INSPIRE].

[34] K.S. Babu and R.N. Mohapatra, *A Solution to the Strong CP Problem Without an Axion*, *Phys. Rev. D* **41** (1990) 1286 [INSPIRE].

[35] J. de Vries, P. Draper and H.H. Patel, *Do Minimal Parity Solutions to the Strong CP Problem Work?*, arXiv:2109.01630 [INSPIRE].

[36] J. Hisano, T. Kitahara, N. Osamura and A. Yamada, *Novel loop-diagrammatic approach to QCD θ parameter and application to the left-right model*, *JHEP* **03** (2023) 150 [arXiv:2301.13405] [INSPIRE].

[37] J. de Vries, P. Draper, K. Fuyuto, J. Kozaczuk and D. Sutherland, *Indirect Signs of the Peccei-Quinn Mechanism*, *Phys. Rev. D* **99** (2019) 015042 [arXiv:1809.10143] [INSPIRE].

[38] E.E. Jenkins, A.V. Manohar and P. Stoffer, *Low-Energy Effective Field Theory below the Electroweak Scale: Operators and Matching*, *JHEP* **03** (2018) 016 [arXiv:1709.04486] [INSPIRE].

[39] H. Georgi and L. Randall, *Flavor Conserving CP Violation in Invisible Axion Models*, *Nucl. Phys. B* **276** (1986) 241 [INSPIRE].

[40] S. Okawa, M. Pospelov and A. Ritz, *Long-range axion forces and hadronic CP violation*, *Phys. Rev. D* **105** (2022) 075003 [arXiv:2111.08040] [INSPIRE].

[41] A. Manohar and H. Georgi, *Chiral Quarks and the Nonrelativistic Quark Model*, *Nucl. Phys. B* **234** (1984) 189 [INSPIRE].

[42] B.M. Gavela, E.E. Jenkins, A.V. Manohar and L. Merlo, *Analysis of General Power Counting Rules in Effective Field Theory*, *Eur. Phys. J. C* **76** (2016) 485 [arXiv:1601.07551] [INSPIRE].

JHEP11(2023)012

[43] P. Sikivie, *Experimental tests of the "invisible" axion*, *Phys. Rev. Lett.* **51** (1983) 1415 [*Erratum ibid.* **52** (1984) 695] [INSPIRE].

[44] ADMX collaboration, *A Search for Invisible Axion Dark Matter with the Axion Dark Matter Experiment*, *Phys. Rev. Lett.* **120** (2018) 151301 [arXiv:1804.05750] [INSPIRE].

[45] CAST collaboration, *Search for Solar Axions by the CERN Axion Solar Telescope with ^{3}He Buffer Gas: Closing the Hot Dark Matter Gap*, *Phys. Rev. Lett.* **112** (2014) 091302 [arXiv:1307.1985] [INSPIRE].

[46] A. Arvanitaki, J. Huang and K. Van Tilburg, *Searching for dilaton dark matter with atomic clocks*, *Phys. Rev. D* **91** (2015) 015015 [arXiv:1405.2925] [INSPIRE].

[47] V.A. Dzuba, V.V. Flambaum and J.K. Webb, *Calculations of the relativistic effects in many electron atoms and space-time variation of fundamental constants*, *Phys. Rev. A* **59** (1999) 230 [physics/9808021] [INSPIRE].

[48] V.V. Flambaum, D.B. Leinweber, A.W. Thomas and R.D. Young, *Limits on the temporal variation of the fine structure constant, quark masses and strong interaction from quasar absorption spectra and atomic clock experiments*, *Phys. Rev. D* **69** (2004) 115006 [hep-ph/0402098] [INSPIRE].

[49] A. Arvanitaki, P.W. Graham, J.M. Hogan, S. Rajendran and K. Van Tilburg, *Search for light scalar dark matter with atomic gravitational wave detectors*, *Phys. Rev. D* **97** (2018) 075020 [arXiv:1606.04541] [INSPIRE].

[50] AEDGE collaboration, *AEDGE: Atomic Experiment for Dark Matter and Gravity Exploration in Space*, *EPJ Quant. Technol.* **7** (2020) 6 [arXiv:1908.00802] [INSPIRE].

[51] L. Badurina et al., *AION: An Atom Interferometer Observatory and Network*, *JCAP* **05** (2020) 011 [arXiv:1911.11755] [INSPIRE].

[52] J. Bergé, P. Brax, G. Métris, M. Pernot-Borràs, P. Touboul and J.-P. Uzan, *MICROSCOPE Mission: First Constraints on the Violation of the Weak Equivalence Principle by a Light Scalar Dilaton*, *Phys. Rev. Lett.* **120** (2018) 141101 [arXiv:1712.00483] [INSPIRE].

[53] P. Touboul et al., *MICROSCOPE Mission: First Results of a Space Test of the Equivalence Principle*, *Phys. Rev. Lett.* **119** (2017) 231101 [arXiv:1712.01176] [INSPIRE].

[54] T.A. Wagner, S. Schlamminger, J.H. Gundlach and E.G. Adelberger, *Torsion-balance tests of the weak equivalence principle*, *Class. Quant. Grav.* **29** (2012) 184002 [arXiv:1207.2442] [INSPIRE].

[55] A. Hees, O. Minazzoli, E. Savalle, Y.V. Stadnik and P. Wolf, *Violation of the equivalence principle from light scalar dark matter*, *Phys. Rev. D* **98** (2018) 064051 [arXiv:1807.04512] [INSPIRE].

[56] M. Bishof et al., *Improved limit on the ^{225}Ra electric dipole moment*, *Phys. Rev. C* **94** (2016) 025501 [arXiv:1606.04931] [INSPIRE].

[57] ACME collaboration, *Improved limit on the electric dipole moment of the electron*, *Nature* **562** (2018) 355 [INSPIRE].

[58] T.S. Roussy et al., *An improved bound on the electron's electric dipole moment*, *Science* **381** (2023) 46 [arXiv:2212.11841] [INSPIRE].

[59] Y. Ema, T. Gao and M. Pospelov, *Improved Indirect Limits on Muon Electric Dipole Moment*, *Phys. Rev. Lett.* **128** (2022) 131803 [arXiv:2108.05398] [INSPIRE].

JHEP11(2023)012

[60] ARIADNE collaboration, *Progress on the ARIADNE axion experiment*, *Springer Proc. Phys.* **211** (2018) 151 [arXiv:1710.05413] [INSPIRE].

[61] ARIADNE collaboration, *Source Mass Characterization in the ARIADNE Axion Experiment*, *Springer Proc. Phys.* **245** (2020) 71 [arXiv:2011.10141] [INSPIRE].

[62] N. Crescini, C. Braggio, G. Carugno, P. Falferi, A. Ortolan and G. Ruoso, *The QUAX-g_p g_s experiment to search for monopole-dipole Axion interaction*, *Nucl. Instrum. Meth. A* **842** (2017) 109 [arXiv:1606.04751] [INSPIRE].

[63] N. Crescini, C. Braggio, G. Carugno, P. Falferi, A. Ortolan and G. Ruoso, *Improved constraints on monopole-dipole interaction mediated by pseudo-scalar bosons*, *Phys. Lett. B* **773** (2017) 677 [arXiv:1705.06044] [INSPIRE].

[64] Y.V. Stadnik and V.V. Flambaum, *Searching for dark matter and variation of fundamental constants with laser and maser interferometry*, *Phys. Rev. Lett.* **114** (2015) 161301 [arXiv:1412.7801] [INSPIRE].

[65] H. Grote and Y.V. Stadnik, *Novel signatures of dark matter in laser-interferometric gravitational-wave detectors*, *Phys. Rev. Res.* **1** (2019) 033187 [arXiv:1906.06193] [INSPIRE].

[66] S.M. Vermeulen et al., *Direct limits for scalar field dark matter from a gravitational-wave detector*, arXiv:2103.03783 [INSPIRE].

[67] A. Branca et al., *Search for an Ultralight Scalar Dark Matter Candidate with the AURIGA Detector*, *Phys. Rev. Lett.* **118** (2017) 021302 [arXiv:1607.07327] [INSPIRE].

[68] K. Van Tilburg, N. Leefer, L. Bougas and D. Budker, *Search for ultralight scalar dark matter with atomic spectroscopy*, *Phys. Rev. Lett.* **115** (2015) 011802 [arXiv:1503.06886] [INSPIRE].

[69] A. Hees, J. Guéna, M. Abgrall, S. Bize and P. Wolf, *Searching for an oscillating massive scalar field as a dark matter candidate using atomic hyperfine frequency comparisons*, *Phys. Rev. Lett.* **117** (2016) 061301 [arXiv:1604.08514] [INSPIRE].

[70] T. Kalaydzhyan and N. Yu, *Extracting dark matter signatures from atomic clock stability measurements*, *Phys. Rev. D* **96** (2017) 075007 [arXiv:1705.05833] [INSPIRE].

[71] C.J. Campbell, A.G. Radnaev, A. Kuzmich, V.A. Dzuba, V.V. Flambaum and A. Derevianko, *A Single-Ion Nuclear Clock for Metrology at the 19th Decimal Place*, *Phys. Rev. Lett.* **108** (2012) 120802 [arXiv:1110.2490] [INSPIRE].

[72] M. Filzinger et al., *Improved Limits on the Coupling of Ultralight Bosonic Dark Matter to Photons from Optical Atomic Clock Comparisons*, *Phys. Rev. Lett.* **130** (2023) 253001 [arXiv:2301.03433] [INSPIRE].

[73] A.V. Sokolov and A. Ringwald, *Electromagnetic Couplings of Axions*, arXiv:2205.02605 [INSPIRE].

[74] MADMAX collaboration, *MADMAX: A Dielectric Haloscope Experiment*, *PoS* **ICHEP2020** (2021) 645 [INSPIRE].

[75] MADMAX Working Group collaboration, *Dielectric Haloscopes: A New Way to Detect Axion Dark Matter*, *Phys. Rev. Lett.* **118** (2017) 091801 [arXiv:1611.05865] [INSPIRE].

[76] IAXO collaboration, *Conceptual design of BabyIAXO, the intermediate stage towards the International Axion Observatory*, *JHEP* **05** (2021) 137 [arXiv:2010.12076] [INSPIRE].

JHEP11(2023)012

[77] N. Sherrill et al., *Analysis of atomic-clock data to constrain variations of fundamental constants*, *New J. Phys.* **25** (2023) 093012 [arXiv:2302.04565] [INSPIRE].

[78] C. O'Hare, *cajohare/axionlimits: Axionlimits*, https://cajohare.github.io/AxionLimits/, https://doi.org/10.5281/zenodo.3932430 (2020).

[79] Y.V. Stadnik, *Searching for Ultralight Scalar Dark Matter with Muonium and Muonic Atoms*, *Phys. Rev. Lett.* **131** (2023) 011001 [arXiv:2206.10808] [INSPIRE].

[80] B. Batell and A. Ghalsasi, *Thermal misalignment of scalar dark matter*, *Phys. Rev. D* **107** (2023) L091701 [arXiv:2109.04476] [INSPIRE].

[81] R. Janish and H. Ramani, *Muon g-2 and EDM experiments as muonic dark matter detectors*, *Phys. Rev. D* **102** (2020) 115018 [arXiv:2006.10069] [INSPIRE].

[82] ATLAS collaboration, *Search for pairs of scalar leptoquarks decaying into quarks and electrons or muons in $\sqrt{s} = 13$ TeV pp collisions with the ATLAS detector*, *JHEP* **10** (2020) 112 [arXiv:2006.05872] [INSPIRE].

[83] CMS collaboration, *Search for pair production of first-generation scalar leptoquarks at $\sqrt{s} = 13$ TeV*, *Phys. Rev. D* **99** (2019) 052002 [arXiv:1811.01197] [INSPIRE].

[84] J. de Vries, P. Draper, K. Fuyuto, J. Kozaczuk and B. Lillard, *Uncovering an axion mechanism with the EDM portfolio*, *Phys. Rev. D* **104** (2021) 055039 [arXiv:2107.04046] [INSPIRE].

[85] W. Dekens, J. de Vries, M. Jung and K.K. Vos, *The phenomenology of electric dipole moments in models of scalar leptoquarks*, *JHEP* **01** (2019) 069 [arXiv:1809.09114] [INSPIRE].

[86] W. Dekens, E.E. Jenkins, A.V. Manohar and P. Stoffer, *Non-perturbative effects in $\mu \to e\gamma$*, *JHEP* **01** (2019) 088 [arXiv:1810.05675] [INSPIRE].

[87] MUON (G-2) collaboration, *An Improved Limit on the Muon Electric Dipole Moment*, *Phys. Rev. D* **80** (2009) 052008 [arXiv:0811.1207] [INSPIRE].

[88] W. Dekens et al., *Unraveling models of CP violation through electric dipole moments of light nuclei*, *JHEP* **07** (2014) 069 [arXiv:1404.6082] [INSPIRE].

[89] A. Maiezza and M. Nemevšek, *Strong P invariance, neutron electric dipole moment, and minimal left-right parity at LHC*, *Phys. Rev. D* **90** (2014) 095002 [arXiv:1407.3678] [INSPIRE].

[90] J. de Vries, E. Mereghetti, R.G.E. Timmermans and U. van Kolck, *The Effective Chiral Lagrangian From Dimension-Six Parity and Time-Reversal Violation*, *Annals Phys.* **338** (2013) 50 [arXiv:1212.0990] [INSPIRE].

[91] H. An, X. Ji and F. Xu, *P-odd and CP-odd Four-Quark Contributions to Neutron EDM*, *JHEP* **02** (2010) 043 [arXiv:0908.2420] [INSPIRE].

[92] W. Dekens, L. Andreoli, J. de Vries, E. Mereghetti and F. Oosterhof, *A low-energy perspective on the minimal left-right symmetric model*, *JHEP* **11** (2021) 127 [arXiv:2107.10852] [INSPIRE].

[93] G. Senjanović and V. Tello, *Restoration of Parity and the Right-Handed Analog of the CKM Matrix*, *Phys. Rev. D* **94** (2016) 095023 [arXiv:1502.05704] [INSPIRE].

JHEP11(2023)012

[94] ATLAS collaboration, *Search for new phenomena in dijet events using 37 fb^{-1} of pp collision data collected at $\sqrt{s} = 13$ TeV with the ATLAS detector*, *Phys. Rev. D* **96** (2017) 052004 [arXiv:1703.09127] [INSPIRE].

[95] CMS collaboration, *Search for narrow and broad dijet resonances in proton-proton collisions at $\sqrt{s} = 13$ TeV and constraints on dark matter mediators and other new particles*, *JHEP* **08** (2018) 130 [arXiv:1806.00843] [INSPIRE].

[96] CMS collaboration, *Search for W' bosons decaying to a top and a bottom quark at $\sqrt{s} = 13$ TeV in the hadronic final state*, *Phys. Lett. B* **820** (2021) 136535 [arXiv:2104.04831] [INSPIRE].

[97] CMS collaboration, *Search for W' bosons decaying to a top and a bottom quark in leptonic final states at $\sqrt{s} = 13\,TeV$*, CMS-PAS-B2G-20-012 (2023).

[98] ATLAS collaboration, *Search for vector-boson resonances decaying into a top quark and a bottom quark using pp collisions at $\sqrt{s} = 13$ TeV with the ATLAS detector*, arXiv:2308.08521 [INSPIRE].

[99] ATLAS collaboration, *Search for a right-handed gauge boson decaying into a high-momentum heavy neutrino and a charged lepton in pp collisions with the ATLAS detector at $\sqrt{s} = 13$ TeV*, *Phys. Lett. B* **798** (2019) 134942 [arXiv:1904.12679] [INSPIRE].

[100] CMS collaboration, *Search for a right-handed W boson and a heavy neutrino in proton-proton collisions at $\sqrt{s} = 13$ TeV*, *JHEP* **04** (2022) 047 [arXiv:2112.03949] [INSPIRE].

[101] S. Bertolini, L. Di Luzio and F. Nesti, *Axion-mediated forces, CP violation and left-right interactions*, *Phys. Rev. Lett.* **126** (2021) 081801 [arXiv:2006.12508] [INSPIRE].

[102] S.D. Bass and M. Doser, *Quantum sensing for particle physics*, arXiv:2305.11518 [INSPIRE].

[103] HERMES collaboration, *Precise determination of the spin structure function g(1) of the proton, deuteron and neutron*, *Phys. Rev. D* **75** (2007) 012007 [hep-ex/0609039] [INSPIRE].

[104] M. Hoferichter, J. Ruiz de Elvira, B. Kubis and U.-G. Meißner, *High-Precision Determination of the Pion-Nucleon σ Term from Roy-Steiner Equations*, *Phys. Rev. Lett.* **115** (2015) 092301 [arXiv:1506.04142] [INSPIRE].

[105] ETM collaboration, *Direct Evaluation of the Quark Content of Nucleons from Lattice QCD at the Physical Point*, *Phys. Rev. Lett.* **116** (2016) 252001 [arXiv:1601.01624] [INSPIRE].

[106] BMW collaboration, *Ab initio calculation of the neutron-proton mass difference*, *Science* **347** (2015) 1452 [arXiv:1406.4088] [INSPIRE].

[107] D.A. Brantley et al., *Strong isospin violation and chiral logarithms in the baryon spectrum*, arXiv:1612.07733 [INSPIRE].

[108] M. Denis and T. Fleig, *In search of discrete symmetry violations beyond the standard model: Thorium monoxide reloaded*, *J. Chem. Phys.* **145** (2016) 214307.

[109] T. Fleig, *$\mathcal{P},\mathcal{T}$-odd and magnetic hyperfine-interaction constants and excited-state lifetime for HfF^+*, *Phys. Rev. A* **96** (2017) 040502 [arXiv:1706.02893] [INSPIRE].

[110] A. Sunaga, M. Abe, M. Hada and B.P. Das, *Relativistic coupled-cluster calculation of the electron-nucleus scalar-pseudoscalar interaction constant W_s in ybf*, *Phys. Rev. A* **93** (2016) 042507.

JHEP11(2023)012

[111] M. Pospelov, *Best values for the CP odd meson nucleon couplings from supersymmetry*, *Phys. Lett. B* **530** (2002) 123 [hep-ph/0109044] [INSPIRE].

[112] C.-Y. Seng, *Relating hadronic CP-violation to higher-twist distributions*, *Phys. Rev. Lett.* **122** (2019) 072001 [arXiv:1809.00307] [INSPIRE].

[113] V.M. Belyaev and B.L. Ioffe, *Determination of Baryon and Baryonic Resonance Masses from QCD Sum Rules. 1. Nonstrange Baryons*, *Sov. Phys. JETP* **56** (1982) 493 [INSPIRE].

[114] C.-Y. Seng, J. de Vries, E. Mereghetti, H.H. Patel and M. Ramsey-Musolf, *Nucleon electric dipole moments and the isovector parity- and time-reversal-odd pion-nucleon coupling*, *Phys. Lett. B* **736** (2014) 147 [arXiv:1401.5366] [INSPIRE].

[115] B. Graner, Y. Chen, E.G. Lindahl and B.R. Heckel, *Reduced Limit on the Permanent Electric Dipole Moment of Hg199*, *Phys. Rev. Lett.* **116** (2016) 161601 [arXiv:1601.04339] [*Erratum ibid.* **119** (2017) 119901] [INSPIRE].

[116] J.J. Hudson, D.M. Kara, I.J. Smallman, B.E. Sauer, M.R. Tarbutt and E.A. Hinds, *Improved measurement of the shape of the electron*, *Nature* **473** (2011) 493 [INSPIRE].

[117] J. Engel, M.J. Ramsey-Musolf and U. van Kolck, *Electric Dipole Moments of Nucleons, Nuclei, and Atoms: The Standard Model and Beyond*, *Prog. Part. Nucl. Phys.* **71** (2013) 21 [arXiv:1303.2371] [INSPIRE].

[118] T. Fleig and M. Jung, *Model-independent determinations of the electron EDM and the role of diamagnetic atoms*, *JHEP* **07** (2018) 012 [arXiv:1802.02171] [INSPIRE].

[119] V.A. Dzuba, V.V. Flambaum and S.G. Porsev, *Calculation of P,T-odd electric dipole moments for diamagnetic atoms Xe-129, Yb-171, Hg-199, Rn-211, and Ra-225*, *Phys. Rev. A* **80** (2009) 032120 [arXiv:0906.5437] [INSPIRE].

[120] K.V.P. Latha, D. Angom, B.P. Das and D. Mukherjee, *Probing CP violation with the electric dipole moment of atomic mercury*, *Phys. Rev. Lett.* **103** (2009) 083001 [arXiv:0902.4790] [*Erratum ibid.* **115** (2015) 059902] [INSPIRE].

[121] N. Yamanaka, B.K. Sahoo, N. Yoshinaga, T. Sato, K. Asahi and B.P. Das, *Probing exotic phenomena at the interface of nuclear and particle physics with the electric dipole moments of diamagnetic atoms: A unique window to hadronic and semi-leptonic CP violation*, *Eur. Phys. J. A* **53** (2017) 54 [arXiv:1703.01570] [INSPIRE].

[122] V.F. Dmitriev and R.A. Sen'kov, *Schiff moment of the mercury nucleus and the proton dipole moment*, *Phys. Rev. Lett.* **91** (2003) 212303 [nucl-th/0306050] [INSPIRE].

[123] K. Yanase, N. Yoshinaga, K. Higashiyama and N. Yamanaka, *Electric dipole moment of ^{199}Hg atom from P, CP-odd electron-nucleon interaction*, *Phys. Rev. D* **99** (2019) 075021 [arXiv:1805.00419] [INSPIRE].

[124] J. Dobaczewski, J. Engel, M. Kortelainen and P. Becker, *Correlating Schiff moments in the light actinides with octupole moments*, *Phys. Rev. Lett.* **121** (2018) 232501 [arXiv:1807.09581] [INSPIRE].

JHEP11(2023)012