Protoplanetary disks and exoplanets in scattered light

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Shadows cast on the transition disk of HD 135344B

Multiwavelength VLT/SPHERE polarimetric differential imaging


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Abstract

The protoplanetary disk around the F-type star HD 135344B (SAO 206462) is in a transition stage and shows many intriguing structures both in scattered light and thermal (sub-)millimeter emission which are possibly related to planet formation processes. We aim to study the morphology and surface brightness of the disk in scattered light to gain insight into the innermost disk regions, the formation of protoplanets, planet-disk interactions traced in the surface and midplane layers, and the dust grain properties of the disk surface. We have carried out high-contrast polarimetric differential imaging (PDI) observations with VLT/SPHERE and obtained polarized scattered light images with ZIMPOL in the $R$ and $I$ bands and with IRDIS in the $Y$ and $J$ bands. The scattered light images and
surface brightness profiles are used to study in detail structures in the disk surface and brightness variations. We have constructed a 3D radiative transfer model to support the interpretation of several detected shadow features. The scattered light images reveal with unprecedented angular resolution and sensitivity the spiral arms as well as the 25 au cavity of the disk. Multiple shadow features are discovered on the outer disk with one shadow only being present during the second observation epoch. A positive surface brightness gradient is observed in the stellar irradiation corrected ($r^2$-scaled) images in southwest direction possibly due to an azimuthally asymmetric perturbation of the temperature and/or surface density by the passing spiral arms. The disk integrated polarized flux, normalized to the stellar flux, shows a positive trend towards longer wavelengths which we attribute to large ($2\pi a \gtrsim \lambda$) aggregate dust grains in the disk surface. Part of the non-azimuthal polarization signal in the $U_\phi$ image of the $J$ band observation can be attributed to multiple scattering in the disk. The detected shadow features and their possible variability have the potential to provide insight into the structure of and processes occurring in the innermost disk regions. Possible explanations for the presence of the shadows include a $22^\circ$ misaligned inner disk, a warped disk region that connects the inner disk with the outer disk, and variable or transient phenomena such as a perturbation of the inner disk or an asymmetric accretion flow. The spiral arms are best explained by one or multiple protoplanets in the exterior of the disk although no gap is detected beyond the spiral arms up to $1''0$. 
4.1 Introduction

Protoplanetary disks around young stars are the birth environments of planets and studying them is essential for understanding the planet formation process. High-resolution imaging of protoplanetary disks in scattered light and thermal (sub-)millimeter emission reveals morphological structures related to disk evolution and planet-disk interactions among others. Transition disks with large dust cavities are of particular interest because they comprise a small sample of protoplanetary disks that are thought to be in the last stage of disk evolution and possibly planet formation during which the disk evolves from gas-rich protoplanetary disk to gas-poor debris disk. The spectral energy distributions (SED) of transition disks are characterized by a deficit in the infrared excess, relative to typical primordial disk targets, which is usually interpreted as a consequence of dust depletion in the inner regions of the disk (e.g., Strom et al. [1989], Skrutskie et al. [1990], Espaillat et al. [2014]). Imaging of transition disks can unambiguously establish whether a dust cavity is indeed present as well as other structures in the disk. Scattered light imaging at optical and near-infrared wavelengths traces small (micron-sized) dust grains in the disk surface whereas resolved (sub-)millimeter continuum observations trace the thermal radiation of larger (mm-sized) dust grains in the disk midplane.

HD 135344B (SAO 206462) is an F4Ve star (Dunkin et al. [1997]) with a transition disk which is located in the Scorpius OB2-3 (Upper Centaurus Lupus) star forming region at a distance of $140 \pm 42$ pc with an estimated age of $8^{+8}_{-4}$ Myr (van Boekel et al. [2005]). The star is part of a visual binary system and has a separation of $21''$ from the primary star, HD 135344 (SAO 206463) (Mason et al. [2001]), which is an A0V star (Houk [1982]). HD 135344B has been classified as a group Ib source by Meeus et al. [2001] because the SED rises in the mid-infrared yet lacks a $10 \mu$m silicate emission feature. Group I sources are expected to feature a large gap and exhibit mid-infrared excess dominated by reprocessing of stellar flux by the rim and the flared surface of the outer disk (Maaskant et al. [2013]). The infrared excess of the HD 135344B disk is $L_{\text{IR}}/L_\star = 0.53$ which is a typical value for group I protoplanetary disks (Dominik et al. [2003]). The main parameters of the system are summarized in Table 4.1.

Analysis of the SED by Brown et al. [2007] suggested that a large dust cavity with a radius of 45 au is present in the disk. Dust continuum (sub-)millimeter observations have confirmed the presence of the dust cavity and show a crescent-shaped asymmetry with a factor of two emission contrast due to an azimuthal asymmetry in the thermal disk structure and/or the distribution of the large dust grains (Brown et al. [2009]; Lyo et al. [2011]; Andrews et al. [2011]; Pérez et al. [2014]; Pinilla et al. [2015b]). ALMA observations of $^{13}\text{CO}$ and $^{18}\text{O}$ revealed a 25 au gas cavity in which the CO surface density is reduced by a factor of 10000 (van der Marel et al. [2016]).

The HD 135344B disk was first detected in scattered light with the Hubble Space Telescope (HST) which showed part of the outer disk but there was no unambiguous detection of any substructures (Grady et al. [2009]). Subaru/HiCIAO $H$ band polarimetric imaging
4 Shadows cast on the transition disk of HD 135344B

Table 4.1: Main parameters of HD 135344B

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
<th>Reference</th>
</tr>
</thead>
<tbody>
<tr>
<td>Right ascension (J2000)</td>
<td>15h 15m 48.44s</td>
<td>Tycho-2 catalog (Høg et al. 2000)</td>
</tr>
<tr>
<td>Declination (J2000)</td>
<td>−37° 09′ 16.059′</td>
<td>Tycho-2 catalog (Høg et al. 2000)</td>
</tr>
<tr>
<td>B [mag]</td>
<td>9.21 ± 0.02</td>
<td>Tycho-2 catalog (Høg et al. 2000)</td>
</tr>
<tr>
<td>V [mag]</td>
<td>8.708 ± 0.017</td>
<td>Tycho-2 catalog (Høg et al. 2000)</td>
</tr>
<tr>
<td>R [mag]</td>
<td>8.302 ± 0.016</td>
<td>Sitko et al. (2012)</td>
</tr>
<tr>
<td>I [mag]</td>
<td>7.979 ± 0.017</td>
<td>Sitko et al. (2012)</td>
</tr>
<tr>
<td>Y [mag]</td>
<td>7.80 ± 0.32</td>
<td>Estimated with a linear fit</td>
</tr>
<tr>
<td>J [mag]</td>
<td>7.279 ± 0.026</td>
<td>2MASS catalog (Skrutskie et al. 2006)</td>
</tr>
<tr>
<td>H [mag]</td>
<td>6.587 ± 0.031</td>
<td>2MASS catalog (Skrutskie et al. 2006)</td>
</tr>
<tr>
<td>K_s [mag]</td>
<td>5.843 ± 0.020</td>
<td>2MASS catalog (Skrutskie et al. 2006)</td>
</tr>
<tr>
<td>A_v [mag]</td>
<td>0.3</td>
<td>Andrews et al. (2011)</td>
</tr>
<tr>
<td>Spectral type</td>
<td>F4Ve</td>
<td>Dunkin et al. (1997)</td>
</tr>
<tr>
<td>L_ν [L_☉]</td>
<td>7.8</td>
<td>Andrews et al. (2011)</td>
</tr>
<tr>
<td>M_*, [M_☉]</td>
<td>1.7</td>
<td>Müller et al. (2011)</td>
</tr>
<tr>
<td>R_*, [R_☉]</td>
<td>1.4</td>
<td>Müller et al. (2011)</td>
</tr>
<tr>
<td>T_eff [K]</td>
<td>6810</td>
<td>Müller et al. (2011)</td>
</tr>
<tr>
<td>M_*/M_☉ yr⁻¹</td>
<td>(0.6−4.2) × 10⁻⁸</td>
<td>Sitko et al. (2012)</td>
</tr>
<tr>
<td>Distance [pc]</td>
<td>140±42</td>
<td>van Boekel et al. (2005)</td>
</tr>
<tr>
<td>Age [Myr]</td>
<td>8±3</td>
<td>van Boekel et al. (2005)</td>
</tr>
<tr>
<td>Dust mass [M_☉]</td>
<td>1.7 × 10⁻⁴</td>
<td>van der Marel et al. (2016)</td>
</tr>
<tr>
<td>Gas mass [M_☉]</td>
<td>2.4 × 10⁻²</td>
<td>van der Marel et al. (2016)</td>
</tr>
<tr>
<td>Outer disk inclination [deg]</td>
<td>11</td>
<td>Lyo et al. (2011)</td>
</tr>
<tr>
<td>Outer disk position angle [deg]</td>
<td>62</td>
<td>Pérez et al. (2014)</td>
</tr>
</tbody>
</table>

Observations by Muto et al. (2012) revealed two spiral arms which were discussed in the context of spiral density waves. Garufi et al. (2013) carried out VLT/NACO polarimetric imaging observations in the H and K_s bands which resolved a 28 au cavity. The outer radius of the scattered light cavity is approximately 20 au smaller than the (sub-)millimeter cavity which can be explained by spatial segregation of micron-sized and mm-sized dust grains (Garufi et al. 2013) which is a natural outcome of particle trapping by a pressure maximum, for example due to planet-disk interactions (e.g., Rice et al. 2006; Pinilla et al. 2012a; Zhu et al. 2012; de Juan Ovelar et al. 2013). More recently, angular differential imaging (ADI) observations with the Gemini Planet Imager (GPI) were presented by Wahhaj et al. (2015) who recovered the spiral arms and new streamer-like features.

The near-infrared-excess in the SED of HD 135344B is an indicator for dust at small orbital radii (Brown et al. 2007; Carmona et al. 2014). A dust belt at sub-au distance from the star was confirmed by mid- and near-infrared interferometric observations (Carmona...
4.2 Observations and data reduction

et al. 2014; Menu et al. 2015) with possibly a misalignment of the inner and outer disk (Fedele et al. 2008). Multi-epoch spectroscopic and near-infrared photometric observations show variability over the course of months which might be related to instabilities in or perturbations of the inner disk (Sitko et al. 2012). HD 135344B is accreting at a rate of $10^{-8} \, M_\odot \, yr^{-1}$ (Sitko et al. 2012) and rotating near break-up velocity (Müller et al. 2011).

We aim to study the morphology and surface brightness of the HD 135344B disk in scattered light to gain better insight into previously detected structures. This requires high-resolution and high-contrast imaging with the best sensitivity possible. Therefore, we use polarimetric differential imaging (PDI; e.g., Kuhn et al. 2001; Apai et al. 2004a) which is a powerful technique to suppress the unpolarized speckle halo from a star and reveal the scattered light from a protoplanetary disk surface which is orders of magnitude fainter (e.g., Quanz et al. 2011; Hashimoto et al. 2012; Grady et al. 2013; Avenhaus et al. 2014a; Thalmann et al. 2015).

In this paper, we present $R$, $I$, $Y$, and $J$ band VLT/SPHERE (Spectro-Polarimetric High-contrast Exoplanet REsearch; Beuzit et al. 2008) PDI observations of HD 135344B. The spiral arms and dust cavity are detected with unprecedented angular resolution and sensitivity, and several new disk features are revealed. Total intensity images that have been obtained with SPHERE will be presented in a forthcoming paper (Maire et al. 2017). In Sect. 4.2 we describe the observations and data reduction procedure. In Sect. 4.3 we study the morphology, surface brightness and color of the scattered light. In Sect. 4.4 we use a 3D radiative transfer model to provide a possible interpretation for several detected shadow features and we fit the shape of the spiral arms in the context of planet-disk interactions. In Sect. 4.5 we discuss the results with a focus on the innermost disk regions, the formation of spiral arms, and Atacama Large Millimeter/submillimeter Array (ALMA) dust continuum observations. In Sect. 4.6 we summarize the main conclusions.

4.2 Observations and data reduction

The observations were carried out during the nights of 30 March 2015 ($Y$ band), 31 March 2015 ($R$ and $I$ band), and 02 May 2015 ($J$ band) with the SPHERE instrument which is mounted on the Nasmyth A platform of the Unit Telescope 3 (UT3) at ESO’s Very Large Telescope (VLT). ZIMPOL (Zurich IMaging POLarimeter; Thalmann et al. 2008; Schmid et al. 2012) and IRDIS (Infra-Red Dual-beam Imager and Spectrograph; Dohlen et al. 2008; Langlois et al. 2014) are the optical and near-infrared imaging component of SPHERE, respectively. SPHERE contains an extreme adaptive optics system (SAXO) to correct for atmospheric wavefront perturbations (Fusco et al. 2006; Petit et al. 2014).

4.2.1 SPHERE/ZIMPOL

HD 135344B was observed simultaneously with the $R_{PRIM}$ filter ($\lambda_c = 0.626 \, \mu m$, $\Delta \lambda = 0.149 \, \mu m$) and the $I_{PRIM}$ filter ($\lambda_c = 0.790 \, \mu m$, $\Delta \lambda = 0.153 \, \mu m$) in the SlowPol
4 Shadows cast on the transition disk of HD 135344B

Table 4.2: Summary of observations

<table>
<thead>
<tr>
<th>Observing Conditions</th>
<th>Instrument</th>
<th>Filter</th>
<th>Date</th>
<th>DIT (s)</th>
<th>NDIT</th>
<th>NINT</th>
<th>Total Integration Time</th>
<th>DIFF [s]</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>IRDIS Y</td>
<td>(ND)</td>
<td>31 Mar 2015</td>
<td>1.03</td>
<td>3</td>
<td>1.26</td>
<td>0.84</td>
<td>0.04</td>
</tr>
<tr>
<td></td>
<td>ZIMPOL R</td>
<td>(ND)</td>
<td>31 Mar 2015</td>
<td>1.05</td>
<td>4</td>
<td>2.5</td>
<td>1.25</td>
<td>0.03</td>
</tr>
<tr>
<td></td>
<td>ZIMPOL I</td>
<td>(ND)</td>
<td>31 Mar 2015</td>
<td>1.05</td>
<td>4</td>
<td>1.5</td>
<td>0.84</td>
<td>0.04</td>
</tr>
<tr>
<td></td>
<td>IRDIS J</td>
<td>(ND)</td>
<td>02 May 2015</td>
<td>1.25</td>
<td>2</td>
<td>3</td>
<td>0.84</td>
<td>0.04</td>
</tr>
<tr>
<td></td>
<td>IRDIS J</td>
<td>(ND)</td>
<td>02 May 2015</td>
<td>1.22</td>
<td>1.15</td>
<td>12</td>
<td>1.03</td>
<td>0.03</td>
</tr>
<tr>
<td>Average airmass</td>
<td></td>
<td></td>
<td></td>
<td>1.02</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Average differential image motion monitor (DIMM) seeing in the optical with the standard deviation in parenthesis;</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

1 The total integration time per half-wave plate (HWP) position is given by the multiplication of the detector integration time (DIT), the number of detector integrations (NDIT), and the number of NDIT summed over all dither positions (NINT).

4 A neutral density (ND) filter with a ∼ 10−1 transmissivity was used.
4.2 Observations and data reduction

detector mode of ZIMPOL. The instrument converts the polarization of the incoming light into two intensity modulated beams with a polarization modulator and a polarization beam splitter. Each of the two beams is registered on an individual demodulating detector with a field of view of $3'5 \times 3'5$. In SlowPo1 mode, the de-modulation frequency of the two orthogonal polarization directions is reduced to $\sim 27$ Hz which is a factor of $\sim 36$ lower than in FastPo1 mode (Bazzon et al. [2012] Schmid et al. [2012]). This enables a longer readout time for each individual frame and a factor of $\sim 10$ reduction of readout noise. This mode is particularly useful for background limited regions of the image. The effective pixel scales are $3.5837 \pm 0.0006$ by $3.6045 \pm 0.0005$ mas and $3.5873 \pm 0.0005$ by $3.6081 \pm 0.0006$ mas for camera 1 (I band) and camera 2 (R band), respectively (Ginski et al., in prep.). The difference in pixel scale comes from a remaining anamorphic magnification difference between the horizontal and vertical detector direction, even if mostly compensated by the toric mirrors in the common path infrastructure (CPI; Hugot et al. [2012]).

The ZIMPOL observations were carried out with a detector integration time (DIT) of 10 s to reach a high signal-to-noise (S/N) but without strongly saturating the detector. No coronagraph was used in order to be sensitive to the innermost disk regions but the data is not usable inside approximately 30 mas due to saturation effects. The central octopole pattern that is visible between 30 and 100 mas in both the $Q_\phi$ and $U_\phi$ images (see Fig. 4.1) is likely an instrumental effect and/or a low-wind effect which reduces the S/N very close to the star. Unsaturated frames were obtained with the use of an additional neutral density filter ($\sim 10^{-1}$ transmissivity). This allows us to estimate the angular resolution of the images and to do a photometric calibration (see Appendix 4.A). The average differential image motion monitor (DIMM) seeing during the observations was $\sim 0.7''$.

Four half-wave plate (HWP) positions were cycled ($0^\circ$, $45^\circ$, $22.5^\circ$, and $67.5^\circ$) to enable construction of Stokes $+Q$, $-Q$, $+U$, and $-U$, respectively. Each HWP orientation was successively used for eight integrations. The observations comprised three dithering positions with steps of 71 mas to minimize the contribution of bad pixels. A total number of 26 complete polarimetric cycles were obtained and a single polarimetric cycle and single dithering position was used for the total intensity measurement. The total integration time per HWP position was 960 s and an additional 40 s per HWP position with the neutral density filter (see Table 4.2).

The raw frames of the ZIMPOL observations were split into the two beams, R and I band, and the polarization states were extracted from the odd and even detector rows (Thalmann et al. [2008]). Standard data reduction routines were applied including flat field, bias frame, and bad pixel correction (Avenhaus et al. [2014b]). The stellar position was determined using an asymmetric 2D Gaussian fit because of the non-square nature of the ZIMPOL pixels. We have used a correction of $-1.188^\circ$ for the rotational offset of the HWP with respect to true north (see Eq. 4.2) which is determined by minimizing the integrated signal in the $U_\phi$ image. The frames have been upscaled by a factor of two in vertical direction to make the pixels square, they were centered with the derived stellar location,
and non-linear pixels have been masked out. Instrumental polarization is corrected by equalizing the integrated flux of the ordinary and extraordinary beam between 0′′1 and 1′′0 (Avenhaus et al. 2014b). $Q_{\phi}$ and $U_{\phi}$ frames (see Sect. 4.2.3) were obtained for each HWP cycle and combined with a mean-stacking. Astrometric calibration was performed on the final $Q_{\phi}$ and $U_{\phi}$ images (Ginski et al., in prep.). A more exhaustive description of the data reduction technique is provided in the appendix of Avenhaus et al. (2014b).

The angular resolution of the ZIMPOL observations is determined from a reduced and non-saturated total intensity frame. The full width half maximum (FWHM) of the point spread function (PSF) is 33.5 mas and 28.5 mas for $R$ and $I$ band, respectively, which are comparable due to the smaller diffraction limit in $R$ band but a higher Strehl ratio in $I$ band.

### 4.2.2 SPHERE/IRDIS

In addition to the ZIMPOL PDI observations, we carried out IRDIS dual-polarization imaging (DPI) observations at two different epochs approximately one month apart. We note that PDI and DPI are equivalent techniques but there is an instrumental difference between ZIMPOL and IRDIS (Thalmann et al. 2008; Langlois et al. 2014). We observed HD 135344B with the BB_Y filter ($\lambda_c = 1.043 \mu m, \Delta \lambda = 0.140 \mu m$) and without coronagraph during a HWP experiment which resulted in an on-source integration time of 151 s per HWP position with a DIT of 0.84 s. The IRDIS detector has a pixel scale of approximately 12.26 mas per pixel and a $11'' \times 11''$ field of view. The HWP that controls the orientation of the polarization was cycled through $0^\circ$, $45^\circ$, $22.5^\circ$, and $67.5^\circ$ to obtain the linear components of the Stokes vector. We completed seven polarimetric cycles with an average DIMM seeing of $\sim 0.9''$ (see Table 4.2).

A deeper IRDIS observation was done with the BB_J filter ($\lambda_c = 1.245 \mu m, \Delta \lambda = 0.240 \mu m$) for which we used a small apodized Lyot coronagraph with an inner working angle (IWA) of 80 mas. The total integration time per HWP position was 1152 s with a DIT of 32 s corresponding to 12 completed polarimetric cycles. A non-coronagraphic (unsaturated) frame was obtained at the start and the end of the observations with a 0.84 s DIT and an additional neutral density filter with $\sim 10^{-1}$ transmissivity. Seeing conditions were good ($\sim 0.7''$) and the spiral arms were visible after a single detector integration.

The ordinary and extraordinary beam were extracted from the raw frames of the IRDIS detector after which a dark frame, flat field, and bad pixel correction were applied (Avenhaus et al. 2014b). To accurately determine the position of the star behind the coronagraph we used dedicated center calibration frames at the beginning and the end of the science sequence. These are coronagraphic images in which a periodic 2D modulation is applied to the deformable mirror that causes four equidistant echoes of the stellar PSF to appear in a cross-shaped pattern outside of the coronagraph (Marois et al. 2006b; Sivaramakrishnan & Oppenheimer 2006). A linear interpolation between the two center frames is used to determine the stellar position in all frames. For the non-coronagraphic $Y$
4.3 Results

band observations, we have determined the stellar position by fitting a 2D Moffat function to the saturated PSF profile.

Similar to the ZIMPOL observations, the instrumental polarization of the $J$ band observation is corrected by equalizing the ordinary and extraordinary beam. The instrumental polarization of the $Y$ band observations is determined by integrating the flux in an annulus with an inner radius of six pixels and outer radius of nine pixels centered on the star for Stokes $Q$ and $U$ separately. The corresponding total intensity frames are multiplied with the integrated flux value after which it is subtracted from the Stokes $Q$ or $U$ image (Canovas et al. 2011). The $Q_\phi$ and $U_\phi$ images were obtained from the Stokes $Q$ and $U$ images with a mean stacking. The angular resolution of the IRDIS $J$ band image is 38.5 mas. No unsaturated frames were obtained during the $Y$ band observations and a determination of the angular resolution from the science data is not possible.

4.2.3 Azimuthal Stokes parameters

We convert the linear Stokes parameters, $Q$ and $U$, into their azimuthal counterparts, $Q_\phi$ and $U_\phi$, which are defined as (cf. Schmid et al. 2006):

$$Q_\phi = Q \cos 2\phi + U \sin 2\phi$$

$$U_\phi = Q \sin 2\phi - U \cos 2\phi,$$

where $\phi$ is the position angle of a location $(x, y)$ in the disk image with respect to the stellar position $(x_0, y_0)$. The azimuthal location, measured in counterclockwise direction from the positive $x$-axis, is given by

$$\phi = \arctan \frac{y-y_0}{x-x_0} + \theta,$$

where $\theta$ corrects for small instrumental offsets such as an angular misalignment of the HWP. In this way, $Q_\phi > 0$ for single scattered light from protoplanetary dust grains that introduce positive polarization at the observed scattering angles. This implies that the polarization vectors point in azimuthal direction, in contrast to $Q_\phi < 0$ which corresponds to polarization in radial direction. The polarized intensity, $PI = \sqrt{Q^2 + U^2}$, is similar to the $Q_\phi$ flux when multiple scattering can be neglected. In that case, the $U_\phi$ image does not contain any scattered light from the disk and can be used to estimate the noise level of the $Q_\phi$ image. In contrast to $PI$, $Q_\phi$ does not contain any bias from computing the squares of $Q$ and $U$ when noise is present in the image (Schmid et al. 2006).

4.3 Results

4.3.1 Polarized light imagery

Figures 4.1 and 4.2 show the ZIMPOL and IRDIS polarized intensity images, respectively, and the corresponding S/N maps of HD 135344B. The disk is clearly detected with all
Figure 4.1: ZIMPOL $R$ band (top two rows) and ZIMPOL $I$ band (bottom two rows) polarized intensity images. The field of view is $1''4 \times 1''4$ and the central star is positioned in the center of each image. The left column shows the $Q_\phi$ and $U_\phi$ polarized intensity images (see Sect. 4.2.3). The center column shows the $Q_\phi$ and $U_\phi$ images scaled with the deprojected distance squared from the star to each pixel for an inclination of $11^\circ$ and a position angle of the major axis of $62^\circ$. All images are shown on a linear color stretch, with companion $Q_\phi$ and $U_\phi$ images having the same minimum and maximum value. Orange corresponds to positive values, blue to negative values, and black is the zero point. The right column shows the signal-to-noise (S/N) maps of the $Q_\phi$ and $U_\phi$ images which are obtained from the $U_\phi$ images. The contour levels correspond to the standard deviation values that are shown on the right of the S/N map colorbar.
Figure 4.2: IRDIS Y band (top two rows) and IRDIS J band (bottom two rows) polarized intensity images. The J band $U_\phi$ images are shown with a ten times harder color stretch than the J band $Q_\phi$ images. The 80 mas inner working angle of the coronagraph of the J band observations has been masked out. See caption of Fig. 4.1 for further details.
filters and a great amount of structure is seen with high S/N in the $Q_\phi$ images. The left columns show the unscaled $Q_\phi$ and $U_\phi$ polarized intensity images and the center columns the stellar irradiation corrected ($r^2$-scaled) $Q_\phi$ and $U_\phi$ images for which each pixel has been multiplied with the square of the deprojected distance to the stellar position at the center of each image. The correction compensates for the inverse-square law of the irradiation of the disk by the central star and attempts to provide an estimate of the spatial distribution of the dust grains in the disk surface. We have assumed a disk inclination of 11° and a position angle of the major axis of 62° (see Table 4.1) and did not correct for the vertical extent of the disk.

Negative valued pixels are identified in the central regions of the unscaled $Q_\phi$ images, where instrumental effects, PSF smearing effects (Avenhaus et al. 2014a), and low-wind effects dominate, and also in the outer disk regions were the scattered light flux becomes comparable to the background noise level. The inner dust disk of HD 135344B is expected to be located at sub-au distance from the star (Carmona et al. 2014) and a direct detection is not possible. However, the signal pattern in the inner regions of the ZIMPOL images is expected to contain some of the smeared scattered light from the inner disk but at this point it is not clear how significant this is with respect to the instrumental signal.

The S/N maps in Figs. 4.1 and 4.2 are estimated from the $U_\phi$ images. We binned the pixel values in linearly spaced annuli (one pixel wide) around the star and calculated the standard deviation within each annulus which yields an estimate of the noise level in the $Q_\phi$ image as function of radial separation from the star. The S/N is calculated from the ratio of the absolute pixel values in the $Q_\phi$ image and the $U_\phi$ standard deviation in the corresponding annuli. For the $U_\phi$ S/N maps, we used the ratio of the absolute pixel values in $U_\phi$ image and the standard deviations from the $U_\phi$ annuli.

Multiple scattering in a moderate inclined and axisymmetric disk will produce non-azimuthal polarization in the $U_\phi$ image with values up to $\sim$5% of the $Q_\phi$ flux (Canovas et al. 2015). For a nearly face-on disk, the $U_\phi$ signal will be lower since forward scattering of large dust grains ($2\pi a \gtrsim \lambda$, with $a$ the grain radius and $\lambda$ the photon wavelength) reduces the number of multiple scattered photons that are directed towards the observer. A hard color stretch of the $J$ band $U_\phi$ image (see Fig. 4.2) is required to reveal the non-zero residual.

We determine the ratio of the azimuthally integrated $U_\phi$ and $Q_\phi$ signal in 25 linearly spaced annuli around the star between 0′′05 and 1′′0 (see Fig. 4.3). The number of bins is chosen such that the width of each annulus is approximately equal the angular resolution of the image. The $J$ band observation is used for this analysis because of the high S/N compared to the other filters. We have used the absolute pixel values because the annulus integrated $U_\phi$ signal from a face-on and axisymmetric disk will be zero. As expected, the ratio approaches unity both in the cavity ($\lesssim$0′′2) and the outermost disk region ($\gtrsim$0′′7) because the scattered light flux in the $Q_\phi$ image is similar to the noise level. The integrated $U_\phi$ signal is between 2.5% and 3% of the integrated $Q_\phi$ signal where the S/N is largest, that is, where the $U_\phi/Q_\phi$ ratio reaches a minimum in Fig. 4.3. This might suggest that
the effect of multiple scattering in the disk is non-negligible.

### 4.3.2 Disk morphology and brightness asymmetries

The disk is clearly detected from approximately 0\arcsec\,1 up to 0\arcsec\,7 in the $r^2$-scaled $Q_\phi$ images of both ZIMPOL and IRDIS (see Figs. 4.1 and 4.2). Additionally, there is a tentative detection of the disk in $J$ band from 0\arcsec\,7 to 1\arcsec\,0 (see Sect. 4.3.4). We have identified a number of structures in the $r^2$-scaled $Q_\phi$ images which are related to the morphology and surface brightness of the disk. The features have been labeled in Fig. 4.4 and will be described in more detail below. The figure shows a color composite image of the $r^2$-scaled ZIMPOL $R$ and $I$ band images. We have scaled the $I$ band image by a factor of 1.05 to correct for the larger photometric flux in $I$ band with respect to $R$ band (Coulson & Walther 1995).

Two prominent spiral arms, S1 and S2 (Muto et al. 2012; Garufi et al. 2013), are visible in all $Q_\phi$ images (see Fig. 4.4) and can be traced from the outer disk cavity edge at $\sim$0\arcsec\,2 to $\sim$0\arcsec\,6 ($\sim$28-64 au). Spiral arm S1 separates from the cavity edge at a position angle (east of north) of $\sim$80° and spiral arm S2 at a position angle of $\sim$260°, both spiral arms span an azimuthal range of $\sim$240°. The spiral arms are approximately azimuthally symmetric in their location and pitch angle and have a surface brightness contrast of a factor of 2-3 with the background disk in the $r^2$-scaled images. There appears to be a spiral arm branch on the east side of the disk, also detected by Garufi et al. (2013), which we label S3 (see also the $r^2$-scaled $J$ band image in Fig. 4.2 where this feature is better visible). A kink in the S1 spiral arm is visible at a position angle of 225° (see Fig. 4.4) which is identified by the sudden change in pitch angle of the spiral arm. We will discuss this feature in Sect. 4.5.2 We infer that the near side is along the southern minor axis.
Figure 4.4: Color composite RGB image of ZIMPOL $R$ band (blue), ZIMPOL $I$ band (red), and the average of $R$ and $I$ band (green). The field of view is $1.4'' \times 1.4''$ and the main features that have been identified are labeled.

because of the preceding and receding CO lines (Pérez et al. 2014) and assuming that the observed spiral arms are trailing.

The scattered light cavity, initially revealed by Garufi et al. (2013), is clearly visible and has an approximate radius of $0.18$ (25 au). The cavity edge of the outer disk will be studied in the context of spatial segregation of dust grain sizes in Appendix 4.B. Multiple surface brightness depressions, which are unlikely to be related to changes in disk or dust properties, are in particular well detected in the high S/N $J$ band observation. These features are likely shadows that are cast by the innermost disk regions. We will identify the shadow features and elaborate on their detection in Sect. 4.3.5.

All filters show in the $r^2$-scaled $Q_\phi$ image a positive surface brightness gradient in southwest direction. In particular the ZIMPOL images show a distinct bright wedge-shaped region (see Fig. 4.4). The mean $r^2$-scaled pixel value in the bright wedge between $0.15''$ and $0.7''$ is a factor of 3.7 larger than the mean value from the same sized wedge in opposite direction. A possible interpretation of this brightness gradient will be discussed in Sect. 4.5.3.

The ZIMPOL and IRDIS observations reveal a similar disk morphology yet several differences in surface brightness are visible. The flux contrast of the S2 spiral arm with the S1 spiral arm, measured on opposite sides of the major axis, is approximately a factor of five larger in the ZIMPOL $R$ band image compared to the IRDIS $J$ band image. The faintness of the S2 spiral arm in the ZIMPOL images could be a shadowing effect by the
4.3 Results

![Graph showing disk-to-star flux ratio and filter transmission]

Figure 4.5: Disk-to-star flux ratio as determined from the $Q_\phi$ image, which only includes polarized scattered light from the disk, and an unsaturated total intensity image, which is dominated by the stellar halo. The three data points are the flux ratios in $R$, $I$, and $J$ band with $3\sigma$ error bars. The dashed line shows a weighted least squares fit of a linear function and the solid lines are the normalized transmission curves of the three filters.

outer disk rim which will become optically thin higher above the midplane at shorter wavelengths. The ZIMPOL images show a bright blob in the S2 spiral arm at a position angle of $\sim 100^\circ$ which does not seem to be affected by the shadowing of the outer disk rim possibly due to a local perturbation of the surface density or temperature which may result in an increased scattered light flux. A striped pattern in azimuthal direction is present in the ZIMPOL data which is likely an artifact of the rotation of the telescope spiders during the observation (see Fig. 4.4).

4.3.3 Disk color in polarized light

The fraction of stellar light that scatters from the disk surface towards the observer depends on disk properties such as the pressure scale height and surface density, as well as dust properties such as the single scattering albedo, phase function, and polarizability (which are related to grain size, structure, and composition). We determine the disk scattering efficiency from the $R$, $I$, and $J$ band observations by calculating the disk integrated polarized intensity in the $Q_\phi$ image with an annulus aperture ($0.1''$–$2.0''$) centered on the star (only disk signal because the stellar halo is unpolarized) and we use a $2.0''$ circular aperture to calculate the integrated total intensity of an (unsaturated) total intensity image (mainly stellar light). A correction is applied for the difference in DIT of the $Q_\phi$ polarized intensity frame and the total intensity frame. Additionally, we correct the total intensity frame for the transmissivity of the neutral density filter. We have neglected foreground extinction since it will affect the scattered light flux and stellar flux equally. For this analysis we could not include the $Y$ band observations since no unsaturated frames were obtained during the HWP experiment.
Figure 4.5 shows the disk-to-star flux ratio of the $R$, $I$, and $J$ band images. The uncertainties are derived from the $U_\phi$ image by propagating the error on each pixel value (see S/N maps of Figs. 4.1 and 4.2) to an error bar on the integrated flux ratio. A weighted least squares fit of a linear function shows that the disk scattering efficiency increases towards longer wavelengths. If we assume that the degree of polarization is approximately the same for the three filters (since it is only weakly dependent on wavelength), then we can conclude that the disk integrated polarized intensity is intrinsically red in color consistently in $R$, $I$, and $J$ band (see also the red color of the composite ZIMPOL image in Fig. 4.4). We note that the scattering geometry in the disk is very similar in the optical and near-infrared although near-infrared observations probe slightly deeper in the disk surface.

For sub-micron sized dust grains, the scattering cross section will be significantly larger at shorter wavelengths due to the $\lambda^{-4}$ wavelength dependence in the Rayleigh regime. We observe an opposite effect which indicates that larger dust grains ($2\pi a \gtrsim \lambda$) dominate the scattering opacity in the disk surface. Large dust grains give the disk a red appearance in scattered light because the shorter wavelength photons scatter more strongly in forward direction (i.e., into the disk) which makes the disk more faint at shorter wavelengths (Mulders et al. 2013a). Large dust grains in the disk surface need to have an aggregate structure which prevents them from settling efficiently towards the disk midplane. A detailed multi-wavelength study of the optical properties of compact dust aggregates by Min et al. (2016) showed that the effective albedo (scattering albedo with the forward scattering peak of the phase function excluded) of micron-sized aggregate dust grains increases from optical to near-infrared wavelengths.

### 4.3.4 Surface brightness profiles

We use the (unscaled) $Q_\phi$ images to obtain polarized surface brightness profiles along the major and minor axis of the disk which are shown in Fig. 4.6. A radial cut is made through the disk with an azimuthal width of 10° and 41, 35, and 30 linearly spaced bins in radial direction between 0″05 and 1″0 for $R$, $I$, and $J$ band, respectively. The number of bins has been chosen such that the bin width is approximately equal to the angular resolution of the image. The error bars show 1σ deviation in the corresponding bins of the unscaled $U_\phi$ images. The $Y$ band observation is excluded from the surface brightness profiles because no unsaturated total intensity frames were obtained which made a photometric calibration not possible.

Figure 4.6 shows the difference of the disk polarized surface brightness and the stellar magnitude in the same filter (see Table 4.1). In this way, each surface brightness profile is normalized to the stellar flux and depends mainly on the scattering properties of the dust grains (e.g., Quanz et al. 2012). We note that the IRDIS photometric calibration has a larger uncertainty than the ZIMPOL photometric calibration because we derive a zero-point for the $J$ band observation from the 2MASS stellar magnitude and the detector integrated...
4.3 Results

Figure 4.6: Polarized surface brightness profiles along the major axis (top) and minor axis (bottom) of the HD 135344B disk. The position angle of the axis (measured east of north) is shown in the top left and right, and the colors indicate different filters. Data points show the mean $Q_\phi$ surface brightness and the error bars show 1σ uncertainties determined from the corresponding $U_\phi$ image. We have rejected bins in which the mean $Q_\phi$ count rate is negative as well as lower limit error bars that correspond to negative flux values. We note that the error bars do not include the uncertainty from the photometric calibration. The dotted lines show 1σ and 5σ background levels in the $Q_\phi$ $J$-band image at large separation from the star.

The surface brightness profiles are overall similar in shape and the disk is clearly detected up to $\sim0'.7$. Two evident maxima are visible along each direction with the innermost maximum at $\sim0'.2$ corresponding to the cavity edge of the outer disk, possibly intertwined with a spiral arm. The second surface brightness maximum is located around $\sim0'.3$–$0'.4$ which is caused by a spiral arm. The S2 spiral arm is relatively faint around...
the major axis in the ZIMPOL images which was also seen in Fig. 4.4. The profiles along the 62° and 152° position angles show a third maximum around ~0.′′55 which was also detected by Garufi et al. (2013). It is most visible in the J band surface brightness profile as a result of the high S/N disk detection. On the west side of the disk (PA = 242° and PA = 332°), there is a tentative detection of the disk between 0.′′7 and 1.′′0. In that region, the J band flux is comparable to the 5σ level of the background noise in Q_φ.

The slope of the surface brightness profile beyond the spiral arms is determined by the shape of the unperturbed disk surface. Therefore, we fit the azimuthally averaged Q_φ profile between 0.′′7 and 0.′′9 with a power law function. An azimuthally averaged profile was used in order to enhance the faint scattered light flux at large disk radii. We performed a weighted least squares fit of a linear function in log-log space with the weights given by the standard deviations of the U_φ bins. The best-fit results of the power law exponents are −4.33 ± 0.11, −3.83 ± 0.15, −1.22 ± 0.40, and −2.71 ± 0.07 for R, I, Y, and J band, respectively. The values indicate that the surface height at which the disk in radial direction reaches an optical depth of unity might have a flat and not a flaring shape at disk radii ≥100 au (Whitney & Hartmann 1992).

### 4.3.5 Shadow features and indications for variability

Figure 4.7 shows a projection of the r^2-scaled Q_φ images from Figs. 4.1 and 4.2 onto a polar coordinates grid. The polar projections point out more clearly surface brightness changes in radial and azimuthal direction and we identify multiple local depressions in surface brightness which appear over a large radial distance with a modest azimuthal gradient. It seems unlikely that this is related to changes in dust properties and/or scattering geometry given the near face-on orientation of the disk (inclination is 11°), as well as the large radial extent and the azimuthal width of the local minima in surface brightness. Therefore, we interpret the surface brightness depressions as shadows that are cast by the innermost disk regions.

In particular the r^2-scaled Q_φ J band image shows with high S/N the locations and shapes of the shadow features. In the J band polar projection (top image of Fig. 4.7), we identify three shadow lanes (A, B, and C) at position angles of approximately −56°, 34°, and 169°, respectively, which manifest themselves as dark vertical bands in the polar projection (dashed lines). Additionally, a broader shadow (D) is identified which is bound by shadow lanes A and B. The decrease in surface brightness at the shadow locations is quantified in the bottom right of Fig. 4.9 which shows the radially integrated surface brightness of the unscaled Q_φ J band image. The figure shows that the location of shadowed region D is bound by shadow lanes A and B but it is distinct from shadows A and B in terms of integrated surface brightness.

The SPHERE PDI observations were carried out during two different epochs which were approximately one month apart (see Table 4.2). Here we refer to the R, I, and Y band observations as epoch 1 and the J band observations as epoch 2. Interestingly,
Figure 4.7: Polar projections of the $r^2$-scaled $Q_\phi$ images for $J$, $Y$, $I$, and $R$ band (top to bottom). The vertically dashed lines correspond to shadow lanes A, B, and C and are identical to the dashed lines in Fig. 4.9. The identified shadow features have been labeled in the $J$ band image. North corresponds to PA $= 0^\circ$ and positive position angles are measured east from north.
a comparison of the polar projections of the two epochs in Fig. 4.7 shows that shadow feature C is present in the $J$ band image but appears to be absent in the image projections of epoch 1. A possible explanation for shadow features A, B, and D is a warped inner disk. We will explore this scenario with a radiative transfer model in Sect. 4.4.1 and discuss the interpretation of the shadows in Sect. 4.5.1.

## 4.4 Modeling

### 4.4.1 Radiative transfer: shadows from a warped disk

A striking discovery of the SPHERE PDI observations is the presence of multiple shadows that are cast on the outer disk of HD 135344B. In Sect. 4.3.5, we identified four shadow features (A, B, C, and D) in the $J$ band $Q_{\phi}$ image (see Fig. 4.7) and we showed that shadow feature C was only present in the second observation epoch. To explain shadow features A, B, and D, we propose a scenario in which the unresolved inner disk of HD 135344B is misaligned with respect to the outer disk and both are connected through a warped disk region.

To test the warped disk hypothesis, we use the 3D radiative transfer code MCMax3D, which fully includes multiple scattering and polarization, to qualitatively reproduce shadow features A, B, and D. Shadow feature C is not included in the model because it appears to be variable and its origin is uncertain (see the discussion in Sect. 4.5.1). Also the spiral arms are not included since the shadow features are not affected by the presence of the spiral arms and including them would add unnecessary complexity.

We use the 3D version of the continuum radiative transfer code MCMax (Min et al. 2009) which calculates the thermal structure of the disk for a radially parametrized surface density distribution with a rounded disk rim (Hughes et al. 2008; Mulders et al. 2013b):

$$\Sigma(r) = \Sigma_0 r^{-\epsilon} \exp\left[-\left(\frac{r}{R_{\text{tap}}}\right)^{2-\epsilon}\right] \exp\left[-\left(\frac{1-r/R_{\text{round}}}{w}\right)^3\right],$$  \hspace{1cm} (4.3)

where $\Sigma_0$ is a normalization constant, $R_{\text{in}} < r < R_{\text{out}}$ the disk radius, $R_{\text{tap}}$ the tapering-off radius, $\epsilon$ the surface density power law index, $R_{\text{round}}$ the radius were the rounding of the surface density sets in, and $w$ a measure for how round the disk rim is. The surface density profile is scaled to the total dust mass, $M_{\text{dust}}$, within each zone. The vertical density distribution is assumed to be Gaussian, in cylindrical coordinates given by

$$\rho(r,z) = \frac{\Sigma(r)}{\sqrt{2\pi}H(r)} \exp\left[-\frac{z^2}{2H(r)^2}\right],$$  \hspace{1cm} (4.4)

where $H(r)/r = (H_0/r_0)(r/r_0)^\psi$ is the parametrization of the aspect ratio, $H(r)$ the pressure scale height, $H_0/r_0$ the aspect ratio at reference radius $r_0$, and $\psi$ the flaring index.
### Table 4.3: MCMax3D model parameters

<table>
<thead>
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<th>Parameter</th>
<th>Zone 1</th>
<th>Zone 2</th>
<th>Zone 3</th>
</tr>
</thead>
<tbody>
<tr>
<td>$R_{in}$ [au]</td>
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<td>25</td>
</tr>
<tr>
<td>$R_{out}$ [au]</td>
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<td>25</td>
<td>200</td>
</tr>
<tr>
<td>$R_{tap}$ [au]</td>
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<td>70</td>
<td>70</td>
</tr>
<tr>
<td>$R_{round}$ [au]</td>
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<td>-</td>
<td>27</td>
</tr>
<tr>
<td>$w^2$</td>
<td>0.3</td>
<td>-</td>
<td>0.3</td>
</tr>
<tr>
<td>$M_{dust}$ [$M_\odot$]</td>
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<td>$2 \times 10^{-11}$</td>
<td>$4 \times 10^{-4}$</td>
</tr>
<tr>
<td>$\epsilon^3$</td>
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<td>3</td>
<td>1</td>
</tr>
<tr>
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<td>0.01</td>
<td>0.07</td>
</tr>
<tr>
<td>$r_0^{5}$ [au]</td>
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<td>1</td>
<td>30</td>
</tr>
<tr>
<td>$\psi^6$</td>
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<td>0</td>
<td>0.25</td>
</tr>
<tr>
<td>$a^7$</td>
<td>$10^{-3}$</td>
<td>$10^{-1}$</td>
<td>$10^{-3}$</td>
</tr>
<tr>
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<td>0.01</td>
<td>0.01</td>
</tr>
<tr>
<td>$a_{max}$ [$\mu$m]</td>
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<td>1</td>
<td>1000</td>
</tr>
<tr>
<td>$a_{pow}$</td>
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<td>-3.5</td>
<td>-3.5</td>
</tr>
<tr>
<td>$i$ [deg]</td>
<td>-11.5</td>
<td>-11.5 : 11</td>
<td>11</td>
</tr>
<tr>
<td>PA [deg]</td>
<td>75</td>
<td>75 : 62</td>
<td>62</td>
</tr>
</tbody>
</table>

1. Tapering-off radius (see Eq. 4.3);
2. Roundness of the disk rim (see Eq. 4.3);
3. Surface density power law index (see Eq. 4.3);
4. Reference aspect ratio;
5. Reference radius;
6. Flaring index (see Eq. 4.4);

The grain size distribution of the dust is a power law with index $a_{pow}$ and a minimum and maximum grain size of $a_{min}$ and $a_{max}$, respectively, for which we use values from model 5 of Carmona et al. (2014) (see Table 4.3). The dust composition is 80% silicates and 20% carbon and the porosity of the grains is approximated with effective medium theory and set to 25%. We consider the grains to be irregular in shape by setting the maximum volume void fraction used for the distribution of hollow spheres (DHS) to 0.8 (Min et al. 2005). The composition, porosity, and irregularity are set to typical values from the European FP7 project DiscAnalysis (DIANA; Woitke et al. 2016). Grain size dependent dust settling is calculated with the prescription from Woitke et al. (2016) who follow the method from Dubrulle et al. (1995) but provide an adjustment for the parametrized vertical gas structure. The method assumes an equilibrium between gravitational settling and
turbulent mixing and depends on a single free parameter, the turbulent mixing strength $\alpha$. The main parameters of the radiative transfer model are specified in Table 4.3. We adopt the stellar temperature, luminosity, mass, and distance from Table 4.1.

The radiative transfer model for HD 135344B consists of three different zones which are independent in their disk structure and dust properties. We refer to those as zone 1, 2, and 3 which correspond to the misaligned inner disk, the warped transition region, and the outer disk, respectively (see Fig. 4.8). The location, shape, and surface brightness of shadow lanes A and B are mainly determined by the radial width, orientation, aspect ratio, and dust mass of the inner disk, as well as the aspect ratio and flaring of the outer disk. Shadow feature D is cast by the warped disk region and is mainly affected by the dust mass, surface density exponent, and the turbulent mixing strength of zone 2. Also the spatial scale on which the inner disk midplane transitions towards the outer disk midplane (see Eq. 4.5) affects shadow feature D.

The disk warp (zone 2) is modeled by transitioning the inner disk (zone 1) orientation stepwise towards the outer disk (zone 3) orientation. The inclination, $\theta_{\text{MCMax3D}}$, of the warped part of the disk is given by

$$\theta_{\text{MCMax3D}} = \theta_{\text{in}} + (\theta_{\text{out}} - \theta_{\text{in}}) \left[ \frac{R - R_{\text{out}}^{\text{inner}}}{R_{\text{in}}^{\text{outer}} - R_{\text{out}}^{\text{inner}}} \right]^{p_{\text{warp}}},$$

with $R_{\text{in/outer}}^{\text{inner}}$ the inner/outer radius of the inner disk, $R_{\text{in/outer}}^{\text{out}}$ the inner/outer radius of the outer disk, and $p_{\text{warp}}$ a parameter determining how quickly the inclination of the warped disk changes. We note that $\theta_{\text{MCMax3D}}$ is the inclination in the MCMax3D model and not the
Figure 4.9: Synthetic $Q_\phi$ (top left) and $U_\phi$ (bottom left) polarized intensity images and the radially collapsed surface brightness from the radiative transfer model (top right) and the IRDIS J band image (bottom right). The inset of the synthetic $Q_\phi$ image shows the PSF core of the J band observation. The MCMax3D radiative transfer model has been constructed to qualitatively reproduce shadow features A, B, and D. Both images have been scaled with the squared distance from each pixel to the star and are shown on a linear color stretch with the $U_\phi$ color stretch 100 times harder than the $Q_\phi$ stretch. The 80 mas inner working angle of the coronagraph of the J band observation has been masked out. The red dashed line in the top right figure shows the same radiative transfer model but without the warped disk region (zone 2). The vertically dashed lines show the locations of the surface brightness minima of shadow features A, B, and C. The error bars of the integrated surface brightness show 1σ of the corresponding position angle bin in the $U_\phi$ image.

inclination with respect to the detector plane. The azimuthal orientation in the warped part of the disk, $\phi_{MCMax3D}$, is changing in a similar way from the inner disk towards the outer disk. A power law exponent of $p_{\text{warp}} = 0.2$ gave the best result for reproducing shadow feature D.

Figure 4.9 shows the synthetic $r^2$-scaled $Q_\phi$ and $U_\phi$ images in J band as well as the radially integrated surface brightness of the synthetic and the observed $Q_\phi$ image. The synthetic Stokes $Q$ and $U$ images have been convolved with the PSF core from the J band observation (see inset of the synthetic $Q_\phi$ image in Fig. 4.9) before converting them into their azimuthal counterparts. The radially integrated surface brightness is obtained from the unscaled $Q_\phi$ images by adding all pixels between $0''2$ and $0''7$ in 33 linearly spaced
position angle bins. The number of bins is chosen such that the bin width at the inner radius approximately equals the angular resolution of the image. The error bars show $1\sigma$ of the pixel values in the corresponding position angle bin of the $U_\phi$ image. The error bars of the high S/N MCMax3D image correspond to a real spread in the $U_\phi$ signal as a result of multiple scattering in the disk because the synthetic $Q_\phi$ and $U_\phi$ image are noise-free. For the observed $J$ band image, it is a combined effect of multiple scattering and noise residual (see Sect. 4.3.1).

The radiative transfer model reproduces qualitatively the location, shape, and the surface brightness contrast of shadow features A, B, and D both in the polarized intensity image and the radially collapsed surface brightness. The inner disk requires a $22^\circ$ misalignment with the outer disk, a relatively small aspect ratio ($h_0 = 0.01$), and a dust mass of $2 \times 10^{-9} \, M_\odot$ to reproduce shadow features A and B. Reproducing shadow feature D requires a warped disk region (zone 2) with a steep surface density profile ($\epsilon = 3$) and a dust mass of $2 \times 10^{-11} \, M_\odot$. This is consistent with the SED suggesting that the inner dust disk emission is optically thick in thermal emission but transitions to optically thin in the cavity. Furthermore, we used $\alpha = 10^{-1}$ for zone 2 to make sure that the dust grains are vertically mixed. The effect of the warped disk region is shown in the radially integrated surface brightness of the MCMax3D model (top right of Fig. 4.9). The red dashed line shows the surface brightness of the same radiative transfer model but with zone 2 removed. In that case, only shadow features A and B are visible and the depression in surface brightness of shadow feature D is absent. Although shadow features A, B, and D are qualitatively reproduced, we note that the solution is not unique given the large number of free parameters that have an effect on the shadows. A more detailed study of each parameter is beyond the scope of this paper. Also, we did not attempt to fit the SED and the resolved millimeter emission.

### 4.4.2 Spiral arms as tracers of protoplanets

Although several mechanism for the excitation of spiral arms exist (see the discussion in Sect. 4.5.2), in this section we will study in more detail the scenario in which the HD 135344B spiral arms have been excited by forming protoplanets. A low-mass protoplanet triggers density waves at the Lindblad resonances of the disk in which it is embedded (Ogilvie & Lubow 2002). Interference of different azimuthal modes results in a one-armed spiral which can be approximated with linear perturbation theory when $M_p/M_\ast \ll (H(r)/r)^3$, where $M_p$ is the mass of the protoplanet, $M_\ast$ the stellar mass, $H(r)$ the pressure scale height, and $r$ the disk radius. Higher order perturbation terms become important when $M_p/M_\ast \sim (H(r)/r)^3$ which can lead to the presence of secondary spiral arm (Juhász et al. 2015; Zhu et al. 2015).

The shape of a planet-induced spiral arm as derived from density wave theory in the
4.4 Modeling

Figure 4.10: Best-fit spiral arm solutions for the protoplanets inside (green) and outside (purple) the scattered light cavity (see also Table 4.4). Blue points are the surface brightness maxima along each spiral arm that are used for the $\chi^2$ fitting. The plus symbols indicate the positions of the best-fit protoplanets.

A linear or weakly non-linear regime is given by (Rafikov 2002)

$$
\phi(r) = \phi_p \left[ \frac{1}{1 + \eta} - \frac{1}{1 - \zeta + \eta} \right] - \frac{\text{sgn}(r - r_p)}{h_p} \left[ \frac{1}{1 + \eta} - \frac{1}{1 - \zeta + \eta} \right],
$$

(4.6)

where $\zeta$ is the power law index in the $\Omega \propto r^{-\zeta}$ disk rotation profile and $\eta$ the power law index that determines the steepness of the sound speed profile, $c_s \propto r^{-\eta}$. The polar coordinates of the protoplanet location are $(r_p, \phi_p)$ and the disk aspect ratio at the protoplanet location is given by $h_p = c_s(r_p)/(r_p\Omega(r_p))$. The pitch angle of the spiral arm depends mainly on the temperature at the launching point of the density wave.

We use Eq. (4.6) to fit simultaneously spiral arms S1 and S2 in the $r^2$-scaled $Q_\phi J$ band image (e.g., Muto et al. 2012; Grady et al. 2013; Benisty et al. 2015) by selecting 27 and 38 azimuthally equidistant points of surface brightness maxima along the S1 and S2 spiral arm, respectively. We aim to find two separate solutions by restricting the radial position of the protoplanets to be either inside or outside the scattered light cavity. The disk aspect ratio is limited to $0.05 < h_p < 0.4$ such that it is consistent with radiative transfer modeling (Andrews et al. 2011; Carmona et al. 2014) and the temperatures required are still physical. The rotational profile is assumed to be Keplerian with $\zeta = 3/2$ and we use the flaring index, $\psi = \zeta - \eta - 1 = 0.25$, from the radiative transfer model in Sect. 4.4.1.
4 Shadows cast on the transition disk of HD 135344B

Table 4.4: Spiral arm best-fit results

<table>
<thead>
<tr>
<th>Protoplanets inside the scattered light cavity</th>
<th>Prior</th>
<th>Best-fit value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Aspect ratio ( h_{S1} )</td>
<td>([0.05, 0.4])</td>
<td>0.4</td>
</tr>
<tr>
<td>Planet S1 radial separation ( r_{S1} ) [au]</td>
<td>([0, 28])</td>
<td>24.3</td>
</tr>
<tr>
<td>Planet S1 position angle ( \phi_{S1} ) [deg]</td>
<td>([0, 360])</td>
<td>10.4</td>
</tr>
<tr>
<td>Planet S2 radial separation ( r_{S2} ) [au]</td>
<td>([0, 28])</td>
<td>21.9</td>
</tr>
<tr>
<td>Planet S2 position angle ( \phi_{S2} ) [deg]</td>
<td>([0, 360])</td>
<td>245.2</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Protoplanets beyond the scattered light cavity</th>
<th>Prior</th>
<th>Best-fit value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Aspect ratio ( h_{S1} )</td>
<td>([0.05, 0.4])</td>
<td>0.16</td>
</tr>
<tr>
<td>Planet S1 radial separation ( r_{S1} ) [au]</td>
<td>([28, 168])</td>
<td>168.0</td>
</tr>
<tr>
<td>Planet S1 position angle ( \phi_{S1} ) [deg]</td>
<td>([0, 360])</td>
<td>52.2</td>
</tr>
<tr>
<td>Planet S2 radial separation ( r_{S2} ) [au]</td>
<td>([28, 168])</td>
<td>99.0</td>
</tr>
<tr>
<td>Planet S2 position angle ( \phi_{S2} ) [deg]</td>
<td>([0, 360])</td>
<td>354.8</td>
</tr>
</tbody>
</table>

Changing \( \eta \) did not significantly change the results so it was fixed to 0.25. The image is deprojected by the disk inclination after which we performed a \( \chi^2 \) minimization of the parameter grid which consists of 30, 70, and 70 linearly spaced values for \( h_{S1} \), \( r_{S1}/r_{S2} \), and \( \phi_{S1}/\phi_{S2} \), respectively. We fit the launching point of both spiral arms and the aspect ratio at the launching point of spiral arm S1. The aspect ratio at the launching point of the S2 spiral arm is scaled with the flaring index from the aspect ratio of the S1 spiral arm. We note that linear perturbation theory requires two protoplanets to explain the two spiral arms which will be discussed in Sect. 4.5.2.

The best-fit results, together with the parameter priors, are given in Table 4.4 and the spiral arm solutions are superimposed on the \( r^2 \)-scaled \( J \) band image in Fig. 4.10. For the protoplanet solutions inside the scattered light cavity, we are not able to fit the innermost points of the surface brightness maxima (see Fig. 4.10). A better fit would require a disk aspect ratio larger than the upper limit of 0.4 which corresponds to temperatures that are unphysical at the disk radius that is studied. A similar result was obtained for the spiral arms of MWC 758 (Benisty et al. 2015). The second scenario, in which the protoplanets are located beyond the scattered light cavity, gives a more realistic best-fit result for the aspect ratio, \( h_{S1} = 0.16 \), and the brightness maxima in Fig. 4.10 are traced well by the best-fit spiral arms. However, the radial and azimuthal coordinates of those protoplanets show a degenerate correlation because the launching point of the density wave (i.e., the kink in the spiral arm) is not found by the fitting routine. The 2D Bayesian probability distributions of each set of free parameters and their marginalized probability distributions are shown in Fig. 4.14 of Appendix 4.C.
4.5 Discussion

4.5.1 Shadows as a probe for the innermost disk regions

The polarized scattered light images that have been obtained with SPHERE show multiple local minima in surface brightness which we have interpreted as shadows that are cast by dust located in the vicinity of the star (see Sect. 4.3.5). Even though high-contrast imaging with SPHERE allows us to resolve disk structures at small angular separations from the star, the inner disk of HD 135344B lies at an expected angular separation of \( \sim 7 \text{ mas} \) which is well beyond the reach of SPHERE. Therefore, the shadow features and possible variability provide a unique way of probing the innermost disk regions.

Features A and B are narrow shadow lanes that could have been cast by a misaligned inner disk, similar to HD 142527 (Marino et al. 2015), because their location appears to be stationary between epoch 1 and 2. A misaligned inner disk will be replenished by gas and dust flowing from the outer disk, through a disk warp, towards the inner disk (e.g., Casassus et al. 2015) with a mass accretion rate of \( 10^{-8} \text{ M}_\odot \text{ yr}^{-1} \) (Sitko et al. 2012). A warped disk region might cast a (broad) shadow which is approximately bound by the shadows from the inner disk. This could explain shadow feature D which manifests itself as a subtle dimming of the surface brightness.

Shadow feature C is clearly detected in the \( J \) band observation but appears to be absent in the \( R, I, \) and \( Y \) band observations which indicates a variable or transient origin of this shadow such as an instability in or perturbation of the inner disk (Sitko et al. 2012), an accretion funnel flow (Müller et al. 2011), an (aperiodic) outflow from the rapidly rotating star (Müller et al. 2011), or an inclined circumplanetary disk.

To probe the dynamics of the innermost disk region, it would be possible to use variability of the casted shadows. In particular, an alternation in shape, location, and brightness of the shadow features gives an indication of the geometry, optical thickness, and variability timescale of the shadow casting dust. Time-dependent processes such as precession of a warped inner disk, asymmetric accretion flows, local perturbations of the inner disk, or a dusty disk wind may alter the shadows on various timescales.

Although a comparison of the two observation epochs shows a hint of variability for the direction and shape of shadows A and B (see Fig. 4.7), the \( R, I, \) and \( Y \) band observations are of significantly lower S/N than the \( J \) band observations which makes it difficult to compare with high precision the shadow locations in the polarized scattered light images. In addition, the wavelength dependent dust opacities might alter the shape of the shadow features which could resemble variability. Future observations will determine if these differences are explained by changes in the inner most disk regions or by the wavelength dependent dust opacities. Also, follow-up observations may provide insight into the variable or transient nature of shadow feature C which was only detected during in the second observation epoch.

A shadow that is cast by a clump in the vicinity of the central star will show an azimuthal
4 Shadows cast on the transition disk of HD 135344B

Figure 4.11: **Left**: IRDIS J band $r^2$-scaled $Q_\phi$ image shown with a ten times harder linear color stretch compared to the image in Fig. 4.2. Orange corresponds to positive pixel values, blue to negative pixel values, and black is the zero point. The 80 mas inner working angle of the coronagraph has been masked out. Features from the telescope spiders are clearly visible. **Right**: IRDIS J band $r^2$-scaled $Q_\phi$ image convolved with an elliptical Gaussian kernel ($132 \times 94$ mas) to match the angular resolution of the ALMA Band 9 observation from Pérez et al. (2014). The superimposed contours show the ALMA Band 9 (0.45 mm) dust continuum with the beam size in the bottom left. We assumed that the star is located in the cavity center of the ALMA image.

gradient when the Keplerian timescale of that clump is similar to or smaller than the time delay related to the finite speed of light with which the shadow traverses the disk. The variable shadow feature C shows a slight azimuthal gradient which could be a light travel time effect. The detected radial extent of shadow C is approximately $0''35$ which translates into an 6.8 hr time of flight. Over this distance, the position angle of the shadow changes by $\sim 25^\circ$ which would correspond to the orbital rotation of the clump while the shadow is traversing the disk with the speed of light. Translating this into an orbital frequency gives a radius of $\sim 0.06$ au.

4.5.2 The origin of the spiral arms

Spiral arms have been observed in scattered light images of several protoplanetary disks, including HD 135344B (Muto et al. 2012; Garufi et al. 2013; Wahhaj et al. 2015), MWC 758 (Grady et al. 2013; Benisty et al. 2015), HD 100546 (Boccaletti et al. 2013; Avenhaus et al. 2014b), HD 142527 (Casassus et al. 2012; Rameau et al. 2012; Canovas et al. 2013; Avenhaus et al. 2014a), and HD 100453 (Wagner et al. 2015a). They are caused by local perturbations of the disk surface density and/or scale height but their origin is still under debate. Interestingly, all these disks are in a transition stage and contain a large dust cavity which could be related to the observed spiral arms. Several mechanisms have been proposed, planet-disk interactions and gravitational instabilities will be discussed below.

Low-mass protoplanets embedded in a gaseous disk are known to excite density waves
4.5 Discussion

at Lindblad resonances which generates a one-armed spiral through their constructive interference (Goldreich & Tremaine 1979; Ogilvie & Lubow 2002). Spiral arm fitting in Sect. 4.4.2 showed that the spiral arms are best explained by protoplanets located exterior of the spiral arms since this allows for a physical aspect ratio of the disk, in contrast to the protoplanet solutions interior of the spiral arms. However, it was assumed that each spiral arm is excited by an individual low-mass, \( M_p/M_\ast \lesssim 10^{-3} \), planet. Several authors have shown, using 3D hydrodynamical and radiative transfer simulations, that a massive, \( M_p/M_\ast \gtrsim 6 \times 10^{-3} \), protoplanet in the exterior of the disk will excite both the \( m = 1 \) and \( m = 2 \) spiral arm with a morphology, pitch angle, and surface brightness contrast similar to HD 135344B and MWC 758 (Dong et al. 2015b, Zhu et al. 2015, Fung & Dong 2015). A kink is visible in the S1 spiral arm (see Fig. 4.4) which could be related to the launching point of the spiral density wave by a forming protoplanet (Muto et al. 2012). Fitting of the spiral arms did not result in a protoplanet solution at the location of the kink but Fig. 4.10 shows that the surface brightness maxima deviate from the best-fit solutions around this location.

The gap width that will be opened by the gravitational torque of a forming protoplanet is approximately given by the Hill radius,

\[
R_H = r \left( \frac{q}{3} \right)^{1/3}
\]

with \( r \) the disk radius and \( q \) the planet-star mass ratio, but can be as wide as 5 \( R_H \) (Dodson-Robinson & Salyk 2011). A massive protoplanet exterior of the HD 135344B spiral arms is expected to have opened a wide gap which might have been visible in scattered light. The left image in Fig. 4.11 shows the \( J \) band \( r^2 \)-scaled \( Q_\phi \) image on a hard color stretch which reveals scattered light up to disk radii of 1.′′0 without any indication of a gap exterior of the spiral arms. However, the depth of the gap in scattered light depends on the aspect ratio which, for a flaring disk, increases towards larger disk radii (Crida et al. 2006).

Spiral density waves are also triggered by self-gravity in case the protoplanetary disk is massive enough to become gravitationally unstable (e.g., Cossins et al. 2009, Kratter et al. 2010). We use the Toomre parameter to estimate the stability of the HD 135344B disk against self-gravity which is given by (Toomre 1964)

\[
Q(r) = \frac{k(r)c_s(r)}{\pi G \Sigma(r)},
\]

where \( k(r) \) is the epicycle frequency, \( c_s(r) \) the sound speed, \( G \) the gravitational constant, \( \Sigma(r) \) the total surface density, and \( Q(r) \lesssim 1 \) corresponds to a gravitationally unstable disk. We assume a Keplerian disk, optically thin temperature profile and estimate the disk mass from the optically thin ALMA band 7 (0.85 mm) dust continuum (Pinilla et al. 2015b). The disk mass is given by

\[
M_{\text{disk}}(r) = \frac{F_\nu(r)d^2}{\kappa_\nu B_\nu(T)},
\]

where \( F_\nu \) is the flux density, \( d \) the distance to the source, \( \kappa_\nu \) the millimeter dust opacity, and \( B_\nu(T) \) the Planck function. We use \( \kappa_\nu = 0.1(\nu/10^{12}\text{Hz}) \) cm² g⁻¹ (Beckwith et al.
Figure 4.12: Toomre parameter calculated from the ALMA band 7 (0.85 mm) dust continuum (Pinilla et al. 2015b) with a typical gas-to-dust ratio of \( g/d = 100 \), \( g/d = 80 \) (van der Marel et al. 2016), and \( g/d = 4 \) (Carmona et al. 2014). The dashed lines show the 25 au scattered light cavity, the 46 au millimeter cavity from Andrews et al. (2011), and the outer radius at which the spiral arms are visible.

which implicitly includes a gas-to-dust ratio of \( g/d = 100 \) and has a typical opacity slope for a protoplanetary disk in which grain growth has occurred (Testi et al. 2014). However, we note that Carmona et al. (2014) estimated \( g/d = 4 \) from detailed modeling of line observations, which would imply a strong gas depletion throughout the disk. In contrast with van der Marel et al. (2016) who obtained \( g/d = 80 \) from CO line and dust continuum observations with ALMA.

Figure 4.12 shows the calculated Toomre parameter as function of disk radius with a minimum of \( \sim 10 \) around 80 au which is an order of magnitude above the Toomre criterion when a gas-to-dust ratio of 100 is used. However, we note that the derivation of the Toomre parameter contains a number of uncertainties and assumptions such as the dust opacity, gas-to-dust ratio, temperature profile, and the exclusion of the dust mass in larger, centimeter sized grains. A marginal instability could have enhanced the amplitude and pitch angle of the spiral arms when triggered by one or multiple protoplanets (Pohl et al. 2015).

4.5.3 The interplay of surface and midplane

The polarimetric scattered light images show an overall positive surface brightness gradient towards the southwest side of the disk in the \( r^2 \)-scaled \( Q_\phi \) images of all filters. The gradient follows approximately the major axis and can therefore not be attributed to forward scattering. In addition, no strong forward scattering effect is expected given the low inclination of the disk (see the radiative transfer model in Sect. 4.4.1). Thus, the surface brightness gradient is presumably related to an asymmetry in the height of the
4.6 Conclusions

We have carried out VLT/SPHERE polarimetric differential imaging observations in $R$ and $I$ band with SPHERE/ZIMPOL and $Y$ and $J$ band with SPHERE/IRDIS which reveal the transition disk around HD 135344B in scattered light with high angular resolution. We have studied the morphology and surface brightness of the disk in the context of the innermost disk regions, the origin of the spiral arms, ALMA dust continuum observations and dust grain properties in the disk surface. A possible interpretation of shadow features A, B, and D has been supported by an MCMax3D radiative transfer model. The main
Conclusions on this work have been summarized below.

Conclusions on the shadow features:

- Multiple low surface brightness regions were discovered which have been interpreted as shadows casts by the innermost disk regions. An inner disk component that is 22° inclined with respect to the outer disk can explain shadow features A and B. A warp in the disk, that connects the misaligned inner and outer disk, can explain shadow feature D which is broad and bound by shadow features A and B.

- Shadow feature C is clearly detected in the $J$ band observation but appears to be absent in the earlier $R$, $I$, and $Y$ band observations. The variable or transient nature of this shadow could be explained by several scenarios, including a local perturbation of the inner disk or an accretion funnel flow from the inner disk onto the star.

Conclusions on the spiral arms:

- An explanation for the spiral arms could not be uniquely determined. In the context of linear perturbation theory, the spiral arms are best explained by two protoplanets orbiting exterior of the spiral arms. Protoplanet solutions inside the scattered light cavity seem unlikely because the spiral arm pitch angles would require unphysical disk temperatures.

- The surface brightness contrast and symmetry of the spiral arms indicate that a single massive protoplanet might have excited both the primary and secondary spiral arm interior of its orbit (Dong et al. [2015], Zhu et al. [2015], Fung & Dong [2015]), however no gap is detected in scattered light beyond the spiral arms up to 1.0.”

- Alternatively, there could be a marginal gravitational instability around 80 au given the large uncertainties on the calculated Toomre parameter.

Additional conclusions:

- The scattered light flux shows a positive gradient towards the southwest side of the disk in the stellar irradiation corrected $Q_\phi$ images which approximately coincides with the asymmetry of the sub-millimeter continuum emission. This could be the result of a temperature and/or surface density perturbation possibly related to the passing spiral arm.

- The disk color in polarized light is red which is an indication that large dust grains ($2\pi a \gtrsim \lambda$) dominate the scattering opacity in the disk surface. Large dust grains in the disk surface are expected to have an aggregate structure which provides them with aerodynamic support against settling towards the disk midplane.

- Part of the non-azimuthal polarization signal in the $U_\phi$ image of the $J$ band observation is likely the result of multiple scattering in the disk.
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4.A Photometric calibration

A photometric calibration is required for an absolute surface brightness comparison between filters. In this appendix, we will explain the photometric calibration procedure for the ZIMPOL and IRDIS observations.

The magnitude per pixel of the ZIMPOL observations is given by (Schmid et al., in
\[ m^*(F) = -2.5 \log \bar{C}^*(F) + zp(F) - X K_1(F) - m_{\text{mode}}(F), \]  
\[ (4.9) \]

where \( \bar{C}^* \) is the mean count rate in each pixel, \( zp(F) \) the zero point magnitude for a given filter \( F \), \( K_1(F) \) the atmospheric extinction parameter, \( X \) the airmass of the observation, and \( m_{\text{mode}} \) a correction of the zero point for the instrument configuration. The zero point magnitudes for the \( R \) and \( I \) band filter are 24.29 and 23.55, respectively, the atmospheric extinction parameters are 0.106 mag am\(^{-1}\) and 0.078 mag am\(^{-1}\) for \( R \) and \( I \) band, respectively, and the instrumental mode correction for SlowPol mode of ZIMPOL is \( m_{\text{mode}} = -1.93 \) (Schmid et al., in prep.). The airmass of the observations is provided in Table 4.2. The pixel values of the \( Q_\phi \) and \( U_\phi \) images have been corrected for the DIT such that pixel values are given in counts s\(^{-1}\). The magnitude per pixel is converted into a surface brightness with (Quanz et al. 2011)

\[ S = m^* + 2.5 \log A, \]
\[ (4.10) \]

where \( A \) is the square of the pixel scale in arcsec\(^2\) and \( S \) is in mag arcsec\(^{-2}\). The uncertainty in the ZIMPOL photometric calibration is approximately 10%.

As a photometric check, we determine the magnitude of HD 135344B from the data and compare this with a literature value. We use the unsaturated frames that were obtained at the end of the ZIMPOL observations and correct those for both the DIT and the response function of the neutral density filter. We subtract 0.1 counts s\(^{-1}\) from each pixel to correct for the dark current level of a 10 s DIT with ZIMPOL as estimated from the PSF profile. We use circular aperture photometry (1.5′ radius aperture centered on the star) to determine the integrated flux and we assume this to be the photometric signal of HD 135344B. From Eq. 4.9, we obtain a magnitude of 8.48 and 8.12 for \( R \) and \( I \) band, respectively, which are very similar to the literature values given in Table 4.1.

For the IRDIS observations, we do a more approximate photometric calibration as described in Quanz et al. (2011) which leads to a larger photometric uncertainty than the ZIMPOL calibration. The \( J \) band observation was carried out with a coronagraph but non-coronagraphic, unsaturated frames were obtained at the start and end of the observation (see Sect. 4.2). The IRDIS \( Y \) band observation was carried out without coronagraph and all frames are saturated in the PSF core. No unsaturated frames were obtained during the HWP experiment and we can not perform a photometric calibration on this data set.

We perform circular aperture photometry (1.5′ radius aperture centered on the star) on a reduced, unsaturated total intensity image in \( J \) band and assume this to be the photometric signal from HD 135344B. Next, we correct the total intensity image, the \( Q_\phi \) image, and the \( U_\phi \) image for their DIT (see Table 4.2). Also a correction is applied for the transmissivity of the \( J \) band filter and the neutral density filter. We can now estimate the zero point of the IRDIS \( J \) band observation by comparing the detector integrated \( J \) band flux with the 2MASS magnitude. The zero point count rate is given by (Quanz et al.
Table 4.5: Cavity edge best-fit results

<table>
<thead>
<tr>
<th>Filter</th>
<th>Maximum [au]</th>
<th>FWHM [au]</th>
</tr>
</thead>
<tbody>
<tr>
<td>ZIMPOL R band</td>
<td>24.23 ± 0.07</td>
<td>11.33 ± 0.28</td>
</tr>
<tr>
<td>ZIMPOL I band</td>
<td>24.55 ± 0.06</td>
<td>11.59 ± 0.26</td>
</tr>
<tr>
<td>IRDIS Y band</td>
<td>24.47 ± 0.08</td>
<td>10.82 ± 0.40</td>
</tr>
<tr>
<td>IRDIS J band</td>
<td>24.67 ± 0.04</td>
<td>11.11 ± 0.14</td>
</tr>
</tbody>
</table>

\[ I_{ZP} = I_{CR} 10^{0.4m_{2MASS}}, \]  

where \( I_{CR} \) is the aperture photometry count rate and \( m_{2MASS} \) the 2MASS magnitude of HD 135344B. From the inversion of Eq. 4.11, we can convert the count rate for each pixel to magnitude and subsequently to surface brightness (see Eq. 4.10). We note that the IRDIS photometric calibration includes a number of uncertainties and assumptions which leads to an estimated photometric error of 30-40%.

4.B The cavity edge of the outer disk

Spatial segregation of different dust grain sizes is expected to occur around a planet-induced gap edge (Zhu et al. 2012; de Juan Ovelar et al. 2013). The resolved millimeter cavity of the HD 135344B disk is indeed larger than the scattered light cavity as a result of dust filtration (Garufi et al. 2013). We will investigate if dust segregation also affects the location of the outer disk cavity edge in the ZIMPOL and IRDIS images by calculating azimuthally averaged brightness profiles. The profiles of the \( R \), \( I \), \( Y \), and \( J \) band images are shown in Fig. 4.13 with each profile normalized to its peak-value and given an arbitrary offset. We perform a weighted least squares fit of a Gaussian profile to the points between 0.1′′ and 0.2′′ with the weights provided by 1σ from the corresponding \( U_\phi \) bins at the same disk radii. The location of the cavity edge is given by the brightness maximum and the width of the cavity edge is given by the FWHM of the Gaussian profile.

The best-fit values, provided in Table 4.5, are very similar for all filters. The errors are derived from the \( \chi^2 \) minimization and are smaller than the spatial uncertainty from the pixel scales. We may conclude that there is no clear evidence of a wavelength dependence in the location and width of the cavity edge between the ZIMPOL and IRDIS data. The result is consistent with the red color of the scattered light (see Sect. 4.3.3) since the scattering opacity in the optical and near-infrared will be gray for grains that are large compared to the wavelength. For smaller grains, the scattering opacity is larger at shorter wavelengths which would have caused a smaller cavity radius in the optical. The FWHM of the cavity edge is approximately 80 mas which means that it is resolved with both the
Figure 4.13: Azimuthally averaged polarized surface brightness around the cavity edge of the outer disk. The profiles are shown in normalized units and with arbitrary offsets. The data points show the mean $Q_{\phi}$ value in each bin and the error bars show 1σ deviations in the corresponding $U_{\phi}$ bin. Solid lines show the best-fit Gaussian profiles (see also Table 4.5).

ZIMPOL and IRDIS observations (see Sect. 4.2).

4.C Spiral arm fitting probabilities

Figure 4.14 shows the 2D Bayesian probability distributions of each set of free parameters that were used for the simultaneous fitting of spiral arm S1 and S2 as explained in Sect. 4.4.2. The marginalized probabilities are shown in the top row of each column. The Bayesian probabilities are determined with $\exp(-\chi^2/2)$ from the $\chi^2$ solutions and normalized to a probability integrated value of unity.
Figure 4.14: Bayesian probabilities for the simultaneous fit of spiral arms S1 and S2 (see Fig. 4.4). The protoplanet locations have been restricted to either inside (top triangle diagram) or outside the scattered light cavity (bottom triangle diagram). The exponent of the sound speed profile is kept fixed to $\eta = 0.25$. The colored maps are the 2D probabilities of each set of free parameters and the top row of each column shows the marginalized probabilities of the free parameters that were fit.