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Planet or brown dwarf? Inferring the companion mass in HD 100546 from the wall shape using mid-infrared interferometry

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ABSTRACT

Context. Giant planets form in protoplanetary disks while these disks are still gas-rich, and can reveal their presence through the annular gaps they carve out. HD 100546 is a gas-rich disk with a wide gap between a radius of ~1 and 13 AU, possibly cleared out by a planetary companion or planetary system.

Aims. We aim to identify the nature of the unseen companion near the far end of the disk gap.

Methods. We used mid-infrared interferometry at multiple baselines to constrain the curvature of the disk wall at the far end of the gap. We used 2D hydrodynamical simulations of embedded planets and brown dwarfs to estimate the viscosity of the disk and the mass of a companion close to the disk wall.

Results. We find that the disk wall at the far end of the gap is not vertical, but rounded-off by a gradient in the surface density. This gradient can be reproduced in hydrodynamical simulations with a single, heavy companion (>30 ... 80 M_Jup) while the disk has a viscosity of at least \( \alpha \geq 5 \times 10^{-3} \). Taking into account the changes in the temperature structure after gap opening reduces the lower limit on the planet mass and disk viscosity to \( 20 M_{\text{Jup}} \) and \( \alpha = 2 \times 10^{-3} \).

Conclusions. The object in the disk gap of HD 100546 that shapes the disk wall is most likely a 60-80 M_Jup brown dwarf, while the disk viscosity is estimated to be at least \( \alpha = 2 \times 10^{-3} \). The disk viscosity is an important factor in estimating planetary masses from disk morphologies: more viscous disks need heavier planets to open an equally deep gap.

Key words. radiative transfer – hydrodynamics – planet-disk interactions – stars: individual: HD 100546 – protoplanetary disks – turbulence

1. Introduction

Giant planets need to form before the gas in protoplanetary disks is dispersed, which makes some of these disks not only planet-forming, but most likely also planet-hosting. Current planet-finding techniques have difficulties in detecting planets around these young stars: transits are blocked from view by the disk, while radial velocity measurements are disturbed by the variability of the stellar photosphere (Setiawan et al. 2008; Huelamo et al. 2008), though (interferometric) imaging has identified a few possible companions (Kraus & Ireland 2012; Quanz et al. 2013).

However, planets can also reveal themselves in an indirect way, through their dynamical impact on the protoplanetary disk (e.g. Lin & Papaloizou 1979, 1986). A gap carved by a single planet has very little impact on the spectral energy distribution (SED), but could be identified by imaging of the disk (Steinacker & Henning 2003; Varnière et al. 2006; Wolf et al. 2007). Nonetheless, a class of so-called transitional disks have been identified on the basis of their low near-infrared excess, which is apparently caused by depleted inner regions (Strom et al. 1989; Muzerolle et al. 2004; Calvet et al. 2005). Long-wavelength imaging has confirmed that most of these indeed have enlarged inner holes or annular gaps (Brown et al. 2009; Andrews et al. 2011) and their size suggests that multiple planets must be responsible (Dodson-Robinson & Salyk 2011; Zhu et al. 2011) or an additional clearing mechanism is at work, such as dust filtration or grain growth (Zhu et al. 2012; Birnstiel et al. 2012). However, how these transitional disks sustain a substantial accretion rate with a depleted inner region remains a mystery, as does the underlying architecture of their planetary systems.

If present, the properties of an underlying planetary system may be inferred from the disk geometry. Giant planets will carve out deep and wide gaps in the gas and dust, and a whole suite of codes exists to study disk-planet interactions (see de Val-Borro et al. 2006, for a comparison of these codes). Comparing these results to observational constraints on the surface density profile allows one to estimate the mass and location of a planet (e.g. Tatulli et al. 2011).

In this work, we study the disk-planet interaction in the disk of HD 100546. It was identified by Bouwman et al. (2003) as a transitional disk on the basis of its SED even before the term
recent interferometric imaging has also revealed a (different) planetary candidate farther out in the disk, at 70 AU (Quanz et al. 2013).

The surface density profile around the gap can also be studied using mid-infrared interferometric data, providing additional constraints on the nature of a (planetary) companion. Using inclined ring models, Panić et al. (2012) have shown that the mid-infrared visibilities can not be reproduced by a sudden jump in intensity at the location of the disk wall at 13 AU, but that the emission from the edge increases smoothly over a few AU. This may indicate that the surface density does not show a sharp increase at 13 AU that points to a vertical wall, but gradually increases with radius. In this case the optical depth — which determines the height of the disk surface — also increases smoothly with radius, producing a more rounded-off wall. In this paper, we explore the observational appearance of these surface density profiles and how they can be explained by the gravitational and hydrodynamic interaction between a disk and a planet.

These rounded-off walls are a natural outcome of hydrodynamical models of disk-planet interaction, where the detailed shape of the radial surface density profile depends on planet mass, disk thickness, and viscosity (Crida et al. 2006; Lubow & D’Angelo 2006). The mass of the planet will therefore be reflected in the shape of the disk wall, which can be constrained with MIDI, the mid-infrared interferometer on the Very Large Telescope. We explain this in more detail in Sect. 2. In addition to the planets mass, the viscosity in the disk wall is a critical parameter in determining the gap shape.

We used a 2D radiative transfer code to model both SED and mid-infrared visibilities to determine the shape of the surface density profile in the disk wall at the far end of the gap (Sect. 3). We then tried to reproduce this surface density profile with a hydrodynamical code to constrain the planet mass and disk viscosity (Sect. 4). We discuss the companion mass and robustness of our result in Sect. 5 and summarize our results in the conclusion.

### 2. Interferometric signature of a disk wall

The visibility versus baseline curve is a Fourier transform of the surface brightness profile. Therefore, the visibility curve of a continuous disk decreases monotonously with baseline (gray dotted line in Fig. 1), as contributions from different radii add up to a smooth curve. In this case, the visibility is a direct measure of the spatial extent of a source. However, in a disk with a gap, the situation is much more complex. The material at the far end of the gap (disk wall) intercepts a much larger fraction of the stellar light than in a continuous disk, creating a peak in the surface brightness at that location, (red line in Figs. 2 and 3). The flux contribution from this radius will then dominate over that of the other radii, both in the SED and visibilities. Its Bessel function will contribute more to the visibilities than those from other radii, resulting in the characteristic gap signature in the visibility curve, showing multiple minima (bounces or nulls) and maxima (sidelobes) (Fig. 1, red line).

The detailed shape of the visibility curve of a gapped disk depends on the structure of the disk wall: a vertical wall (defined as a step function in the surface density) will create a narrow peak in the surface brightness profile with a typical width of a few AU. This non-zero width is due to inclination and optical depth effects caused by the vertical structure. It has much more power in the sidelobes, making the gap structure visible at very

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1 At the time of writing, there are no published observations that constrain the gap size at (sub)millimeter wavelengths.

2 Assuming the inner and outer radius of the disk lie outside the emitting region, so there is no discontinuity in surface brightness at any radius.

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In this section we constrain the shape of the surface density profile in the disk wall from the visibilities presented by Paníć et al. (2012). The inner disk is – at least in the small dust grains probed by MIDI – very compact, <0.7 AU. This is perhaps best illustrated by plotting the correlated flux on the 41 m baseline into the SED of Fig. 4. This baseline probes scales about 2 to 3 AU and therefore filters out most of the emission from the outer disk. The correlated flux seems consistent with the 1700 K blackbody emission from the inner rim, with only little additional flux from colder material. We placed the inner rim at 0.25 AU, consistent with the near-infrared interferometric constrains from Benisty et al. (2010) and Tatulli et al. (2011). Because the temperature behind the inner rim at 0.25 AU drops off very rapidly with radius, we found that the inner disk cannot extend farther out than 0.3 AU (in small grains), unless

### 3. Deriving the wall shape

In this section we constrain the shape of the surface density profile in the disk wall from the visibilities presented by Paníć et al. (2012) and Leinert et al. (2004). To do so, we need to first calculate the density and temperature structure in the disk wall for a given surface density profile. Because the structure of a rounded disk wall can strongly deviate from that of a geometrically thin disk, this task is especially well-suited for 2D radiative transfer codes – also because the disk wall near the midplane is completely shadowed by the inner disk, while the upper part is fully illuminated. In addition, we need to calculate the vertical structure in the disk wall, which strongly deviates from that of a continuous disk due to radial and vertical temperature gradients.

We used MCMax (Min et al. 2009), a 2D radiative transfer code that self-consistently calculates the temperature and vertical density structure for a given surface density profile in an axisymmetric geometry. We assumed the gas to be in vertical hydrostatic equilibrium, and because the SED shows no sign of dust settling of small grains (Mulders et al. 2013), we assume the dust and gas distributions to be equal. The SED and visibilities were calculated using ray-tracing to compare them with the observations. We used the SED fit with a vertical wall presented in Mulders et al. (2011) as a starting point, refined it using the constraints from Paníć et al. (2012), and fit the SED and visibilities simultaneously to constrain the surface density in the disk wall. For completeness, all model parameters are displayed in Table 1.

To generate visibilities from the observed correlated fluxes, we need to divide them by an observed total flux. Because the total flux measured with MIDI is affected by flux losses from the MIDI slit (see Paníć et al. 2012), we used the flux measured with ISO to generate visibilities. The larger field of view of ISO also includes more large-scale PAH emission, with narrow features around 7.9, 8.6 and 11.3 μm, which are inversely imprinted in the visibilities, but which we did not model. These visibilities, together with those presented by Leinert et al. (2004), are shown in Fig. 5. We used the position angle of 145° and inclination of 53° derived by Paníć et al. (2012) to compute visibilities from our disk models.

#### 3.1. Inner disk

As shown by Paníć et al. (2012), the inner disk is – at least in the small dust grains probed by MIDI – very compact, <0.7 AU. This is perhaps best illustrated by plotting the correlated flux on the 41 m baseline into the SED of Fig. 4. This baseline probes scales about 2 to 3 AU and therefore filters out most of the emission from the outer disk. The correlated flux seems consistent with the 1700 K blackbody emission from the inner rim, with only little additional flux from colder material. We placed the inner rim at 0.25 AU, consistent with the near-infrared interferometric constrains from Benisty et al. (2010) and Tatulli et al. (2011). Because the temperature behind the inner rim at 0.25 AU drops off very rapidly with radius, we found that the inner disk cannot extend farther out than 0.3 AU (in small grains), unless
Table 1. Model parameters.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
<th>Reference</th>
</tr>
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<tbody>
<tr>
<td>$T_{\text{eff}}$ [K]</td>
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<td>[1]</td>
</tr>
<tr>
<td>$L_*$ [$L_\odot$]</td>
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<td>[1]</td>
</tr>
<tr>
<td>$M_*$ [M$_\odot$]</td>
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<td>[1]</td>
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<td>[2]</td>
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<td>$\Sigma_{\text{in}}$ [AU]</td>
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<td>[3]</td>
</tr>
<tr>
<td>$\Sigma_{\text{out}}$ [AU]</td>
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<td>†</td>
</tr>
<tr>
<td>$\Sigma_{\text{exp}}$ [AU]</td>
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<td>[4]</td>
</tr>
<tr>
<td>$\Sigma_{\text{wall}}$ [AU]</td>
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<td>†</td>
</tr>
<tr>
<td>$M_{\text{max}}$ [M$_\odot$]</td>
<td>5 $\times$ 10$^{-5}$</td>
<td>†</td>
</tr>
<tr>
<td>Vertical structure</td>
<td>hydrostatic</td>
<td></td>
</tr>
<tr>
<td>$\Sigma_{\text{inner}}(r)$ [g/cm$^2$]</td>
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<td>†</td>
</tr>
<tr>
<td>$\Sigma_{\text{outer}}(r)$ [g/cm$^2$]</td>
<td>0.0004 (r/AU)$^{-1}$</td>
<td>†</td>
</tr>
<tr>
<td>$\Sigma_{\text{wall}}(r)$ [g/cm$^2$]</td>
<td>see Eq. (1)</td>
<td>†</td>
</tr>
<tr>
<td>$\Sigma_{\text{exp}}(r)$ [g/cm$^2$]</td>
<td>0.2 (r/AU)$^{-1}$</td>
<td>†</td>
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<td>[5]</td>
</tr>
<tr>
<td>$a_{\text{max}}$ [$\mu$m]</td>
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<td>[5]</td>
</tr>
<tr>
<td>Shape</td>
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<tr>
<td>Silicate fraction [%]</td>
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<tr>
<td>Carbon fraction [%]</td>
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<td>†</td>
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<td>PA</td>
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<td>[6]</td>
</tr>
<tr>
<td></td>
<td>145</td>
<td>[6]</td>
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</table>

Notes. Parameters with a dagger (†) are (re)fitted.


the surface density power law is steeper than $r^{-1}$. This tiny inner disk is similar to that in the transitional disk T Cha (Olofsson et al. 2013). The normalization of the surface density ($\Sigma_{\text{in}}$) was fitted to the near-infrared excess.

In addition, there is a weak feature apparent at 10 micron, though it is not clear whether this is a mineralogical feature in the inner disk or due to the structure of the outer disk. The outer disk wall also contributes to the correlated flux and creates similar features – which we discuss extensively in the next section. If we treat the observed feature strength as an upper limit to the real feature strength, the feature is too weak to be consistent with a rim made out of the same small amorphous silicate grains as the outer disk wall. Because the temperature of the inner rim is higher than the crystallisation temperature of silicates – and possibly also higher than its sublimation temperature – we used a composition of pure iron, which also fits the SED (Fig. 4). We can mix in a few percent of silicates or corundum (FeAl$_2$O$_3$, which has a higher sublimation temperature) to fit the weak 10 micron feature in the correlated spectrum, but this is not required for a good fit to the visibilities and has no effect on the results presented in this paper.

3.2. Vertical wall

As explained in Sect. 2, the presence of a disk wall creates structures in the visibility as a function of baseline, which is reflected in the spectrally resolved visibilities as well (Fig. 5). This is most clearly seen in the 14.9 m baseline, where a bounce is present at 10.5 $\mu$m. Bounces are also present around 8.5 $\mu$m in the 15.8 and 16.0 m baselines. The longer baselines do not show such pronounced structures.

Fig. 5. Observed visibilities for HD 100546 on different projected baseline lengths and orientations (diamonds). We used the total flux from ISO to calculate visibilities from the correlated fluxes. The colored lines show the same models as Fig. 1. The model without a gap is not shown.

A disk model with a vertical wall at 14 AU can reproduce the location of these bounces at the shortest baselines (Fig. 5, red lines). However, this model overestimates the visibilities at these baselines. In addition, the vertical wall model predicts structures at the 41 and 74 m baselines that are not observed. To fit the visibilities at all baselines, we rounded off the disk wall as described in Sect. 2. This reduces the power in the sidelobes, thus reducing the visibilities at the shortest baselines and smoothing out structures at the longer baselines.

3.3. Rounded-off wall

We rounded off the disk wall by modifying its surface density power law using the following function:

$$
\Sigma_{\text{wall}}(r < r_{\text{exp}}) = \Sigma_{\text{outer}} r^{-1} \exp \left(-\frac{1 - r/r_{\text{exp}}}{w}\right)
$$

$$
\Sigma_{\text{wall}}(r \geq r_{\text{exp}}) = \Sigma_{\text{outer}} r^{-1},
$$

where $\Sigma_{\text{outer}}$ is the normalization constant for the outer disk surface density fitted to the SED, $r_{\text{exp}}$ is the radius where the drop-off of the surface density sets in, and $w$ is a measure of how
round the disk wall is. This function is essentially a Gaussian similar to the vertical scale height, but with a different exponent of 3 as in Lubow & D’Angelo (2006), Eq. (5). Both \( w \) and \( r_{\text{exp}} \) are free fitting parameters. Examples of the resulting surface density distributions are shown in Fig. 2. Although different parametrizations than the one introduced here are possible, this particular one was chosen because it also accurately describes the outcome of our hydrodynamical simulations in the next section.

We first rounded off the disk wall using \( w = 0.20 \) and \( r_{\text{exp}} = 19 \) AU (Fig. 2, red dotted line), consistent with the shape of the disk wall as modeled by Tatulli et al. (2011). Although this produces a smoother surface brightness profile than a vertical wall (Fig. 3) with less power in its sidelobes (Fig. 1), it still produces too much structure on the 41 and 74 meter baselines and overpredicts the shortest baselines. To completely remove all structure on the longer baselines, we rounded off the disk wall even more. Our best-fit model has \( w = 0.36 \) and \( r_{\text{exp}} = 29 \) AU, shown by the blue lines in Figs. 1–3, and 5. There is a small range of solutions with almost equally good fits, ranging from \( w = 0.33 \) and \( r_{\text{exp}} = 26 \) AU to \( w = 0.40 \) and \( r_{\text{exp}} = 35 \) AU. The total parameter space explored ranges from \( w = 0.00 \) to \( w = 0.60 \), and from \( r_{\text{exp}} = 10 \) to 40 AU.

We note that due to disk asymmetries and variability, as discussed by Pančić et al. (2012), it is impossible to find a perfect fit to all data with a single axisymmetric model. Especially the 8 to 9 \( \mu \)m region dominated by the inner disk is affected by this, as observations taken at the same projected baseline length and position angle but at a different date have a different shape. However, the structures arising from vertical walls are not seen in any of the observations, so we are confident that our results for the wall shape are robust. Fitting each baseline separately does provide better fits, but does not change our fit parameters by more than \( \Delta w = 0.02 \) and \( \Delta r_{\text{exp}} = 2 \) AU.

4. Deriving planet mass and disk viscosity

In this section, we show how a planet can explain the observed shape of the disk wall. The micron sized-dust grains observed with MIDI are a good tracer of the gas: they are well-coupled to the disk, pushing material outside of its orbit outward and material inside of it inward. However, gas flows back into the gap due to pressure gradients and viscous spreading, which tends to close the gap. Therefore, the shape of the surface density around a planet depends on its mass, the disk viscosity and scale height (Crida et al. 2006; Lubow & D’Angelo 2006). In general, a heavier planet can carve out a deeper and wider gap, while a more viscous or thicker disk (higher pressure scale height) will reduce the gap width and depth.

4.1. Gap opening

A planet embedded in a disk opens a gap by exerting a torque on the disk, pushing material outside of its orbit outward and material inside of it inward. However, gas flows back into the gap due to pressure gradients and viscous spreading, which tends to close the gap. Therefore, the shape of the surface density around a planet depends on its mass, the disk viscosity and scale height (Crida et al. 2006; Lubow & D’Angelo 2006). In general, a heavier planet can carve out a deeper and wider gap, while a more viscous or thicker disk (higher pressure scale height) will reduce the gap width and depth.

4.2. Hydrodynamical model

We used the freely available 2D hydrodynamical code Fargo (Masset 2000) to model the surface density of the gas disk around an embedded planet’s orbit. Fargo is a solver to the Navier-Stokes and continuity equations in a differentially rotating disk in vertical hydrostatic equilibrium. It speeds up these calculations by removing the average azimuthal velocity component from these equations at each radius and at each time-step.

Because we focused on the steady-state wall shape, it is not necessary to follow the global evolution of the whole disk as Tatulli et al. (2011) have done. Instead, we focused on the surface density profile in the vicinity of the planet. We modeled the disk within a factor 5 in radius of the planet (i.e., 2 to 50 AU for a planet at 10 AU), far enough from the grid edges so that their location do not affect the shape of the surface density in the vicinity of the planet. The planetary candidate discovered by Quanz et al. (2013) lies outside this grid, and – assuming it is on a circular orbit – is therefore located too far away to influence the gap structure. We used square grid cells on a logarithmic grid, 384 in the azimuthal direction. We used a non-reflective boundary condition to suppress wave-reflection at the inner boundary and prevent mass from leaking out at the inner edge of the grid.

The model set-up is based on our best-fit radiative transfer model to the SED and visibilities. We used a surface density power law of \( r^{-1} \) for the initial surface density, similar to that of the outer disk. We used a pressure scale height derived from the scale height profile of our radiative transfer simulation from within the disk gap, i.e., between 0.3 and ~13 AU. Because our radiative transfer model is not vertically isothermal, the scale height is defined as the height above the midplane where the pressure drops off by \( e^{-1/2} \). The pressure scale height in this regime is well-fitted by a power law of the form \( H_p(r) = 0.025 r^{0.35} \), see also Fig. 9. We return to the influence of the chosen scale height profile in the discussion (Sect. 5.3).

To describe the viscous evolution of the disk, we used a viscosity of \( \alpha \) type (Shakura & Sunyaev 1973; Pringle 1981), consistent with our choice of \( r^{-1} \) for the initial surface density profile. For the long integration times required to reach a steady state, this viscosity agrees well with simulations of magnetohydrodynamical turbulence (Papaloizou et al. 2004). We explored the range from \( \alpha = 10^{-4} \) to \( \alpha = 5 \times 10^{-5} \), above which the time step calculation of Fargo may no longer be correct.

We considered a wide range of planets from 1 Jupiter mass to the hydrogen-burning limit at 80 Jupiter masses. The reason for considering these high planet masses is that higher viscosities tend to close the gap, requiring much heavier planets to keep the gap open. We followed the disk evolution for 10\(^6\) orbits of the planet around a 2.4 solar mass star (2 \( \times \) 10\(^4\) yr at 10 AU), after which all models have reached a steady-state. The planet was assumed to be on a circular orbit, and to neither migrate, nor accrete\(^3\).

4.3. Gap shape

To compare the surface density profiles produced by Fargo with our radiative transfer models, we used the analytical fit function of Eq. (1). This function was fitted to the surface density profile outside the radial location of the planet, between \( r_{\text{min}} \) and \( r_{\text{max}} \), where \( r_{\text{min}} \) is the location of the lowest gap depth outside the planets orbit \( (r_{\text{min}} > r_p) \), and \( r_{\text{max}} \) is taken near the edge of the grid at 4.5\( r_p \). This radius was chosen to be just inside the outer grid edge, to avoid the region where the spiral wake hits this edge and local boundary effects may be important.

\(^3\) With the exception of the model represented by the dotted line in Fig. 6, which uses the highest accretion efficiency as defined in Kley (1999).
Because the inner disk is already depleted by a factor of a hundred, the SED around 8 micron and will overpredict all visibilities. If the gap is not deep enough, its emission will fill the gap in the density profile, namely the depth of the gap (Tatulli et al. 2011).

This function fits the surface density profiles with an accuracy of about 10%. An example is shown in Fig. 6. The main deviations come from transient features at small spatial scales, while the overall shape is generally well produced. Note that we did not use the results of the hydrodynamical simulation inside the planet’s orbit, and instead assumed this region to be empty, as indicated by our radiative transfer model, see Sect. 5.2 for a discussion on the gap width.

In addition, we measure the depth of the gap by taking the lowest density value with respect to the unperturbed density ($\Sigma_{\text{off}} \times \alpha^{-1}$). Note that this is only a lower limit to the real depth of the gap: material that is corotating with the planet or orbits around it creates a surface density spike at the location of the planet. If planetary accretion is turned on, using the highest accretion efficiency following the prescription of Kley (1999), the spike disappears and the gap becomes deeper, typically by a factor of 2, though the shape of the disk wall at the far end of the gap does not change significantly, as shown by the dotted line in Fig. 6.

### 4.4. Results

The results of our parameter study are presented in Fig. 7, showing the width over which the surface density in the disk wall is rounded off ($w$ from Eq. (1)) as a function of planet mass and disk viscosity. A general trend is visible, where lower planet masses and disk viscosities produce more vertical walls ($w \sim 0.2$), while rounder walls are found at higher values ($w \sim 0.35$). This trend can be understood from a balance between viscous spreading and planetary torques: a high viscosity makes material flow inward, which smoothes the surface density profile, while a heavier planet mass allows the torques to act over a wider range, allowing for a shallower profile. However, for intermediate shapes there is no linear trend ($w \sim 0.25$ to 0.3).

There is an additional observational constraint on the surface density profile, namely the depth of the gap (Tatulli et al. 2011). If the gap is not deep enough, its emission will fill the gap in the SED around 8 micron and will overpredict all visibilities. Because the inner disk is already depleted by a factor of a hundred, the gap needs to be depleted by about a factor of about ten more (see Fig. 2), depending on the dust opacities. This minimum gap depth is shown with the dashed line in Fig. 7, and only models below this line have gaps that are deep enough. It shows that the disk viscosity is a crucial parameter in opening a disk gap: a Jupiter-mass planet may open a deep gap in an inviscid disk, but for the most viscous disks it requires an 80-Jupiter-mass planet to keep the gap deep enough. In general, we find that the planet mass needs to be scaled with the square root of viscosity to achieve a given gap depth.

There are two regions in this diagram with a wall shape consistent with our observations, $w \sim 0.33\ldots 0.40$. One region lies at low planetary masses ($<5 M_{\text{Jup}}$) and high viscosities ($\alpha > 2 \times 10^{-2}$). Although consistent with the planet mass estimate of Tatulli et al. (2011), the higher viscosity acts against gap opening, and these gaps are nowhere near deep enough to be consistent with observations, even if the planet were allowed to accrete. Another region lies at very high masses (30 to 80 $M_{\text{Jup}}$) and moderately high viscosities ($\alpha = 5 \times 10^{-3} \ldots 5 \times 10^{-2}$), which seems consistent with the observed gap depth, and puts the planet between 8 and 10 AU. Our best-fit model has a planet of 60 $M_{\text{Jup}}$ at 10 AU, a viscosity of $\alpha = 2 \times 10^{-2}$, and is shown in Fig. 6. The dependence of these results on the assumed temperature profile is discussed in Sect. 5.3.

These estimates of $\alpha$ are consistent with that of Mulders et al. (2013), who also found a high turbulent mixing strength of $\alpha_{\text{turb}} > 0.01$ by considering the degree of dust settling in the disk wall.

### 5. Discussion

#### 5.1. Planet or brown dwarf?

The shape of the disk wall points to a companion of thirty Jupiter masses or heavier, with a best fit at about 60 Jupiter masses. According to the IAU definition, this object would be a brown dwarf, and not a planet, making HD 100546 a misinterpreted...
The width of the gap from the hydrodynamical simulations, about 6 AU, is inconsistent with the derived size for the inner disk of less than one AU. The planet itself is heavier than the disk and probably does not migrate, allowing it to act as a barrier for material from the outer disk to reach the inner disk. We neglected the global evolution of the disk, so it is possible that in reality, the inner disk drains onto the central star as in Tatulli et al. (2011). The near-infrared interferometric data used by the authors, however, do not directly constrain the outer radius of the inner disk, which they placed at 4 AU. The MIDI data do require the inner disk to be much smaller than the 4 AU previously assumed (see also Panić et al. 2012). Therefore, an additional mechanism might be necessary for clearing the inner regions.

Additional planets closer to the star could explain the extent of the gap, because they might deplete the inner regions (Dodson-Robinson & Salyk 2011; Zhu et al. 2011). Because the torques on the disk are strongest close to a planet, we expect only the outermost planet in the gap to shape the disk wall. Another mechanism could be dust filtration at the outer edge, which would block dust particles from crossing the gap together with the gas and would reduce the dust to gas ratio of the inner disk (Zhu et al. 2012). However, the high viscosities we infer are less favorable for trapping dust in the outer disk wall (Pinilla et al. 2012). In addition, grain growth could contribute to depleting the inner disk of small grains, see Birnstiel et al. (2012). Resolved millimeter observations of the gap, such as can be delivered with the Atacama Large Millimeter Array, will be crucial to investigate this.

5.3. Pressure scale height

As mentioned in Sect. 4.1, the disk thickness – set by the pressure scale height and thus by temperature – is an important factor in determining the wall shape because it controls how much material flows back into the gap. The pressure scale height is an input parameter of Farqo and remained fixed during the simulation. This is a highly idealized situation, and in reality, the scale height will change during gap opening when the disk wall heats up (Turner et al. 2012). This will, in turn, influence the gap structure, but coupling the hydrodynamical simulations to radiative transfer is far from trivial. In this section we describe how this coupling may affect our results and suggest directions for future work.

Because we are looking for a steady-state solution of the wall shape after many orbits, we can derive the scale height profile corresponding to this wall shape from our best-fit radiative transfer model to the SED and visibilities. This profile is shown in Fig. 8. In the region up to ~12 AU, i.e., within the disk gap, the vertical optical depth is so low that the midplane is not shielded, increasing the temperature by a factor of two and the pressure scale height by about 50% with respect to a disk without a gap (dashed line, see also Turner et al. 2012). Between ~12 and 30 AU, the gradual increase in optical depth starts to shield the midplane, leading to lower temperatures and scale height. Outside 30 AU, the scale height profile is close to that of a continuous disk.

In the parameter study, we used a parameterized scale height of the form $H_p(r) = 0.025 \times r^{0.39}$ (Fig. 8, dotted line). This parametrization describes the profile accurately up to ~12 AU, i.e., in most of the region modeled with Farqo. In addition, in the region where the intensity profile peaks (see Fig. 3) and where our observations are most sensitive, it is closer to the scale height of the best-fit radiative transfer model than that of a continuous disk is. However, the slope of the scale height profile after the peak in intensity at ~12 AU is very different. In a steady-state viscous disk without a gap, this slope sets the surface density distribution (e.g. Andrews et al. 2009). To see how this assumption affects our results, we designed the test described below.
We performed one iteration on the hydrodynamical structure of the disk of the planet to take into account the change in temperature structure of the disk after gap opening. We started with a subset of the hydrodynamical models presented in the previous section, shown in Table 2 and indicated by triangles in Fig. 7. These models span the entire range of wall shapes, from steep to rounded-off, and were initially calculated using the parameterized scale height profile. For each wall shape $w$, we calculated the temperature structure using our radiative transfer code, as described in Sect. 3. The radial location of the wall depends – in addition to the planets location – also on the planet mass, because more massive planets carve out wider gaps. Therefore we adjusted the location of the planet $r_{pl}$ – and hence that of the disk wall ($r_{exp}$, Eq. (1)) – to ensure that the radial intensity profile peaks at 12–13 AU for each wall shape, as in Fig. 3. This is equivalent to fitting the SED (but not the visibilities), since that only depends on the wall location, not its shape.

From these temperature structures we can calculate the scale height profiles, similar to Fig. 8. We used these (nonparameterized) profiles to rerun the hydrodynamical simulations, and measured the new wall shapes of these iterated models using Eq. (1). If the resulting radial location of the wall differs from that of the radiative transfer simulation, we reran the hydrodynamical simulation with the planet at a different radius, to ensure that the wall location between the two simulations is self-consistent. The wall shapes and location before and after iteration are shown in Table 2.

For walls that were already quite round before iterating on the scale height profile ($M > 30 \ M_{\text{Jup}}$ and $\alpha > 5 \times 10^{-3}$), using the calculated scale height from the radiative transfer model does not affect the wall shape significantly. For lower planet masses and disk viscosities, corresponding to steep walls before iteration, the wall shape does change. Iterating on the pressure profile makes these walls rounder by $\Delta w = 0.04$ to 0.07. An example of this is shown in Fig. 9, for a 20-Jupiter-mass planet in a moderately viscous disk ($\alpha = 2 \times 10^{-3}$). By looking at Fig. 7, this moves down the lower limit on the possible range of planet masses and disk viscosities from 30 to 20 Jupiter masses and from $\alpha = 5 \times 10^{-3}$ to $2 \times 10^{-3}$, respectively, becoming consistent with the estimates of Acke & van den Ancker (2006).

We show that iterating on the scale height profile in hydrodynamical simulations does affect the resulting wall shapes. However, we did not take the feedback of the disk structure on the pressure profile during the gap opening into account. To do this, one would need to recalculate the scale height profile during the hydrodynamical calculation, such that the wall shape and scale height profile are always self-consistent. However, this approach is clearly beyond the scope of this paper. We leave this for future work, but we do note that the temperature structure in the wall may contribute to its roundness and might play a role in other processes relevant to transitional disks, such as the accretion flow across the gap. Ideally, one would also take into account the 3D structure of the wall, through this might take a considerable computational effort due to the long integration times necessary to reach a steady state.

5.4. Gap eccentricity

Throughout this work, we assumed azimuthal symmetry for the disk. However, toward the highest companion masses in our simulations, the gap starts to become eccentric (see also Casassus et al. 2012). In addition, the chromatic phases measured with MIDI also show indications for an asymmetric outer

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**Table 2. Wall shape and location before and after iterating on the temperature structure.**

<table>
<thead>
<tr>
<th>$M_{\text{Jup}}$</th>
<th>$\alpha$</th>
<th>$w$ before iteration</th>
<th>$r_{exp}[\text{AU}]$</th>
<th>RT</th>
<th>$r_{exp}[\text{AU}]$</th>
<th>$w$ after iteration</th>
</tr>
</thead>
<tbody>
<tr>
<td>2</td>
<td>$5 \times 10^{-4}$</td>
<td>0.17</td>
<td>0.16</td>
<td>17</td>
<td>10.6</td>
<td>0.21</td>
</tr>
<tr>
<td>5</td>
<td>$5 \times 10^{-4}$</td>
<td>0.20</td>
<td>0.18</td>
<td>18</td>
<td>10.2</td>
<td>0.27</td>
</tr>
<tr>
<td>10</td>
<td>$10^{-3}$</td>
<td>0.23</td>
<td>0.20</td>
<td>19</td>
<td>9.6</td>
<td>0.28</td>
</tr>
<tr>
<td>20</td>
<td>$2 \times 10^{-3}$</td>
<td>0.26</td>
<td>0.23</td>
<td>21</td>
<td>9.2</td>
<td>0.33</td>
</tr>
<tr>
<td>40</td>
<td>$10^{-2}$</td>
<td>0.35</td>
<td>0.29</td>
<td>28</td>
<td>9.8</td>
<td>0.36</td>
</tr>
<tr>
<td>60</td>
<td>$2 \times 10^{-2}$</td>
<td>0.36</td>
<td>0.30</td>
<td>29</td>
<td>9.7</td>
<td>0.37</td>
</tr>
</tbody>
</table>

**Notes.** The wall shape $w$ and its location $r_{exp}$ are defined in Eq. (1). The location of the planet $r_{pl}$ follows from comparing the fitted wall location in the radiative transfer code ($r_{exp}$ in column RT) with that of the hydrodynamical simulation. This subset of models is highlighted by triangles in the parameter study of Fig. 7.
disk (Panić et al. 2012). Taking an azimuthal average over an eccentric gap can lead to a rounder surface density profile, but we will show that this is not the effect we observe or measure in our simulations.

From a modeling point of view, making a gap eccentric contributes to the roundness measured from an azimuthally averaged surface density profile under certain conditions. For example, an elliptical gap ($e = 0.4$) with a vertical wall has an azimuthally averaged surface density profile that appears to be slightly rounded off (we fit $w = 0.05$). This is much less round than the lowest roundness we measured in our simulations, which is $w = 0.17$ (for a circular gap). To investigate if the eccentricity may contribute to the inferred roundness we compared radial cuts of the surface density profile with azimuthally averaged ones. An example is shown in Fig. 10 for our best-fit model of HD 100546.

It may be possible to constrain the eccentricity from the the chromatic phases, hence providing an extra diagnostic on the companion mass, but this will require in-depth modeling of a more extended data set.

6. Conclusion

We have studied the gap shape in the disk of HD 100546. By comparing 2D radiative transfer models to the mid-infrared interferometric data presented in Panić et al. (2012), we found that:

– The disk wall at the far end of the gap is not vertical, but rounded off over a significant radial range. This shape can be explained by a gradual increase in the surface density over a range of ~10 to ~25 AU, creating a broad peak in the surface brightness profile around 12 AU that was also seen by Panić et al. (2012).
– The inner dust disk is extremely small in small grains. We confirmed the upper limit on its size of 0.7 AU found by Panić et al. (2012) and used our 2D radiative transfer model to constrain it even further, with no measurable contribution outside of 0.3 AU.
– The roundness or spatial extent of a disk wall can be inferred from spectrally resolved visibilities beyond the first null.

By comparing these results with hydrodynamical simulations of planet-disk interactions, we found that:

– The shape of the surface density profile in the disk wall of HD 100546 can be explained by a massive planet ($\gtrsim 30 \ldots 80 M_{\text{Jup}}$) in a viscous ($\alpha \gtrsim 5 \times 10^{-3}$) disk between 8 and 10 AU.
– The roundness of a disk wall in hydrodynamical simulations depends on the temperature structure in the disk wall: iterating on the scale height profile using radiative transfer changes this roundness.
– The disk viscosity is a crucial parameter in estimating planet masses from a derived surface density profile, acting against gap opening by the planet. For a given depth, the gap-opening mass of a planet increases with the square root of the disk’s viscosity.
– The effect of a single planet is not enough to explain the full width of the disk gap in HD 100546. Either an additional clearing mechanism or a multi-planet system is required to explain its extent.
– The object shaping the disk wall is most likely a brown dwarf, suggesting HD 100546 might be a binary system and not a transitional disk object.

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References
