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Measurement of charged-particle event shape variables in inclusive $\sqrt{s} = 7$ TeV proton-proton interactions with the ATLAS detector

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The measurement of charged-particle event shape variables is presented in inclusive inelastic $pp$ collisions at a center-of-mass energy of 7 TeV using the ATLAS detector at the LHC. The observables studied are the transverse thrust, thrust minor, and transverse sphericity, each defined using the final-state charged particles’ momentum components perpendicular to the beam direction. Events with at least six charged particles are selected by a minimum-bias trigger. In addition to the differential distributions, the evolution of each event shape variable as a function of the leading charged-particle transverse momentum, charged-particle multiplicity, and summed transverse momentum is presented. Predictions from several Monte Carlo models show significant deviations from data.

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I. INTRODUCTION

Event shape variables describe the structure of hadronic events and the properties of their energy flow. In this analysis, three event shape observables $[1,2]$ are measured: the transverse thrust, the thrust minor, and the transverse sphericity, each built from the momenta of charged particles using tracking information from proton-proton collisions at $\sqrt{s} = 7$ TeV collected with the ATLAS detector $[3]$. Event shape observables are among the simplest experimentally measured quantities and, depending on the events being considered, may have sensitivity to both the perturbative and nonperturbative aspects of quantum chromodynamics (QCD).

Event shapes in hadronic collisions were investigated first at the Intersecting Storage Rings $[4]$ and at the S$p$S $[5,6]$ at CERN to examine the emergence of jets, and later at Tevatron $[7]$ to study the dependence of the event shape observables on the transverse energy of the leading jet and on contributions from the underlying event. At the Large Hadron Collider (LHC), event shape observables were recently studied in inclusive interactions $[8]$ and multijet events $[9,10]$. In $e^+e^-$ and $ep$ deep-inelastic scattering experiments, the study of the energy flow in hadronic final states has allowed tests of the predictions of perturbative QCD, and the extraction of a precise value for the strong coupling constant $\alpha_s$ $[11-17]$.

The study of event shape observables in inclusive inelastic collisions plays an important role in understanding soft-QCD processes at LHC center-of-mass energies $[18]$, where “soft” refers to interactions with low momentum transfer between the scattering particles. Soft interactions cannot be reliably calculated from theory and are thus generally described by phenomenological models, usually implemented in Monte Carlo (MC) event generators. These models contain many parameters whose values are a priori unknown and thus need to be constrained by measurements. Inclusive and semi-inclusive observables sensitive to soft-QCD processes have been measured at the LHC by the ATLAS $[19-21]$, CMS $[22,23]$, and ALICE $[24,25]$ collaborations. The measurements presented in this paper can further constrain the event generator models, which encapsulate our understanding of these soft processes.

In this analysis, the event shape observables are constructed from six or more primary charged particles in the pseudorapidity range $|\eta| < 2.5$ and with transverse momentum $p_T > 0.5$ GeV $[26]$. Primary charged particles are defined as those with a mean proper lifetime $\tau > 30$ ps, produced either directly in the $pp$ interaction or from the subsequent decay of particles with a shorter lifetime. The particle level refers to particles as they emerge from the proton–proton interaction. The detector level corresponds to tracks as measured after interaction with the detector material, and includes the detector response. The results are corrected for detector effects, using simulation, to obtain distributions of the event shape variables defined at particle level which can be directly compared to MC models.

This paper is organized as follows: Section II defines the event shape variables; the detector is described in Sec. III; Sec. IV discusses the MC models used in this analysis; Secs. V and VI respectively describe the event selections and background contributions. The correction of the data back to particle level and estimation of the systematic uncertainties are described in Secs. VII and VIII; the results are discussed in Sec. IX and finally the conclusions are presented in Sec. X.

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II. EVENT SHAPE OBSERVABLES

In particle collisions, event shape observables describe the geometric properties of the energy flow in the final state. A single event shape variable can distinguish in a continuous way between configurations in which all the particles are flowing (forward and backward) along a single axis and configurations where the energy is distributed uniformly over the 4π solid angle. If defined as a ratio of measured quantities, the corresponding systematic uncertainties may be small.

In hadron collisions, where the center-of-mass frame of the interaction is usually boosted along the beam axis, event shape observables are often defined in terms of the transverse momenta, which are Lorentz invariant under such boosts. Different formulations of event shape observables are possible; the most intuitive is to calculate the event shape from all particles in an event. These are denoted by directly global event shapes [1,2]. In hadron collider experiments, it is not usually possible to detect all particles in an event due to the finite detector acceptance, limited at small scattering angles by the presence of the beam pipe. Event shapes which include only particles from a restricted phase space in pseudorapidity, η, are called central event shapes; in this analysis charged particles within the range [η] < 2.5 are used. These central event shapes are nevertheless sensitive to nonperturbative effects at low momentum transfer and provide useful information about the event structure for development of models of proton–proton collisions. The thrust is one of the most widely used event shape variables. The transverse thrust for a given event is defined as

$$T_\perp = \max_{\hat{n}} \frac{\sum_i |\vec{p}_{T,i} \cdot \hat{n}|}{\sum_i |\vec{p}_{T,i}|},$$

where the sum is performed over the transverse momenta \(\vec{p}_{T,i}\) of all charged particles in the event. The thrust axis \(\hat{n}_T\) is the unit vector \(\hat{n}\) that maximizes the ratio in Eq. (1). The transverse thrust ranges from \(T_\perp = 1\) for a perfectly balanced, pencil-like, dijet topology to \(T_\perp = 1\) for a circularly symmetric distribution of particles in the transverse plane, where \(\psi\) is the azimuthal angle between the thrust axis and each respective particle. It is convenient to define the complement of \(T_\perp\), \(\tau_\perp = 1 - T_\perp\), to match the behavior of many event shape variables, which vanish in a balanced dijet topology.

The thrust axis \(\hat{n}_T\) and the beam axis \(\hat{z}\) define the event plane. The transverse thrust minor measures the out-of-event-plane energy flow:

$$T_M = \frac{\sum_i |\vec{p}_{T,i} \cdot \hat{n}_m|}{\sum_i |\vec{p}_{T,i}|}, \quad \hat{n}_m = \hat{n}_T \times \hat{z}.$$

The transverse thrust minor is 0 for a pencil-like event in azimuth and \(2/\pi\) for an isotropic event.

Another widely used event shape variable is the sphericity, \(S\), which describes the event energy flow based on the momentum tensor,

$$S^\alpha\beta = \sum_i \frac{p_{\alpha,i} p_{\beta,i}}{|\vec{p}_i|^2},$$

where the Greek indices represent the \(x, y,\) and \(z\) components of the momentum of the particle \(i\). The sphericity of the event is defined in terms of the two smallest eigenvalues of this tensor, \(\lambda_2\) and \(\lambda_3\):

$$S = \frac{3}{2}(\lambda_2 + \lambda_3).$$

The sphericity has values between 0 and 1, where a balanced dijet event corresponds to \(S = 0\) and an isotropic event to \(S = 1\). Sphericity is essentially a measure of the summed \(p_T^2\) with respect to the event axis [27,28], where the event axis is defined as the line passing through the interaction point and oriented along the eigenvector associated with the largest eigenvalue, \(\lambda_1\). Similarly to transverse thrust, the transverse sphericity, \(S_\perp\), is defined in terms of the transverse components only:

$$S^{\perp} = \frac{1}{\lambda_1^{\perp} + \lambda_2^{\perp}},$$

$$S_\perp = \frac{2\lambda_2^{\perp}}{\lambda_1^{\perp} + \lambda_2^{\perp}},$$

where \(\lambda_2^{\perp} < \lambda_1^{\perp}\) are the two eigenvalues of \(S^{\perp}\).

The following distributions are measured:

(i) normalized distributions: \((1/N_{ev})dN_{ev}/d\tau^{ch}_\perp\), \((1/N_{ev})dN_{ev}/dT^{ch}_\perp\), \((1/N_{ev})dN_{ev}/dS^{ch}_\perp\); (ii) average values: \(\langle \tau^{ch}_\perp \rangle\), \(\langle T^{ch}_\perp \rangle\) and \(\langle S^{ch}_\perp \rangle\) as functions of \(N_{ch}\) and \(\sum\vec{p}_T\); where \(N_{ev}\) is the number of events with six or more charged particles within the selected kinematic range; \(N_{ch}\) is the number of charged particles in an event; \(\sum\vec{p}_T\) is the scalar sum of the transverse momenta of the charged particles in the event. The event shape observables \(\tau^{ch}_\perp\), \(T^{ch}_\perp\), and \(S^{ch}_\perp\) are defined as above, with the superscript indicating that they are constructed from charged particles. The three normalized differential distributions are studied separately for

(i) 0.5 GeV < \(p_T^{lead}\) ≤ 2.5 GeV,
(ii) 2.5 GeV < \(p_T^{lead}\) ≤ 5.0 GeV,
(iii) 5.0 GeV < \(p_T^{lead}\) ≤ 7.5 GeV,
(iv) 7.5 GeV < \(p_T^{lead}\) ≤ 10.0 GeV, (v) \(p_T^{lead}\) > 10 GeV, where \(p_T^{lead}\) is the transverse momentum of the highest \(p_T\) (leading) charged particle.
III. THE ATLAS DETECTOR

The ATLAS detector [3] covers almost the full solid angle around the collision point with layers of tracking detectors, calorimeters, and muon chambers. The components that are relevant for this analysis are the tracking detectors. The inner tracking detector has full coverage in azimuthal angle $\phi$ and covers the pseudorapidity range $|\eta| < 2.5$. It consists of a silicon pixel detector (pixel), a semiconductor tracker (SCT), and for $|\eta| < 2.0$, a straw-tube transition radiation tracker. These detectors, immersed in a 2 T axial magnetic field, are located at a radial distance from the beam line of 50.5–150 mm, 299–560 mm, and 563–1066 mm, respectively. They provide position resolutions typically of 10 $\mu$m, 17 $\mu$m, and 130 $\mu$m for the $r$-$\phi$ coordinate, and of 115 $\mu$m and 580 $\mu$m for the $z$ coordinate in the case of the pixel and SCT detectors.

The measurements presented here use events triggered by the minimum-bias trigger scintillator (MBTS) system [29]. The MBTS detectors are mounted at each end of the tracking detector at $z = \pm 3.56$ m and are segmented into eight sectors in azimuth and two concentric rings in pseudorapidity ($2.09 < |\eta| < 2.82$ and $2.82 < |\eta| < 3.84$). The MBTS trigger was configured to require at least one hit above threshold from either side of the detector in coincidence with a fast beam-pickup device ensuring that the event is compatible with a bunch crossing.

IV. MONTE CARLO MODELS

Monte Carlo (MC) event samples are used to compute the detector acceptance and reconstruction efficiency, determine background contributions, correct the measurements for detector effects, and to calculate systematic uncertainties. Finally, different phenomenological models implemented in the MC generators are compared to the data corrected to the particle level.

The PYTHIA6 [30], PYTHIA8 [31], and HERWIG++ [32,33] event generators were used to produce the simulated event samples for the analysis. These generators implement leading-logarithm parton shower models matched to leading-order matrix element calculations with different hadronization models and orderings for the parton shower. The PYTHIA 6 and PYTHIA 8 generators use a hadronization model based upon fragmentation of color strings and a $p_T$-ordered or virtuality-ordered shower, whereas the HERWIG++ generator implements a cluster hadronization scheme with parton showering ordered by emission angle. The PYTHIA8 generator uses a multiparton interaction (MPI) model interleaved with both initial-state and final-state radiation, and all three processes compete against each other for emission phase space in the resulting evolution. The HERWIG++ UE7-2 tune employs color reconnection. Different settings of model parameters, tuned to reproduce the existing experimental data, were used for the MC generators. Table I shows the different MC models used in this paper.

The reference model for this analysis is chosen to be PYTHIA6 AMBT1. Samples generated with this tune were passed through the ATLAS detector and trigger simulations [44] based on GEANT4 [45] and then reconstructed and analyzed using the same procedure and software that are used for the data. Reconstructed MC events are then used to correct the data for detector effects. The sample generated with an older version of HERWIG++, 2.5.0 with no additional tuning, was also passed through the full detector simulation and the analysis chain for systematic studies of unfolding corrections.

V. EVENT AND TRACK SELECTION

The data used for the analysis presented here were collected in April 2010 with a minimal prescale factor for the minimum-bias trigger. The only further requirement for selecting the data sample is that the MBTS trigger and all inner detector subsystems were at nominal operating conditions. In each event the reconstructed vertices are ordered by the $\Sigma p_T^2$ over the tracks assigned to each vertex, and the vertex with the highest $\Sigma p_T^2$ is taken as the primary interaction vertex of the event. To reduce the
contribution from beam-related backgrounds and decays of long-lived particles, and to minimize the systematic uncertainties, events are rejected if they contain any other vertex reconstructed with four or more tracks.

If there is only one vertex in the event, or if any additional vertex in the event has three or fewer tracks, all tracks from the event that pass the track selection (described below) are retained. After this selection, the fraction of events with more than one proton–proton interaction in the same bunch crossing (referred to as pileup) is found to be approximately 0.1% and this residual contribution is therefore neglected. The average number of $pp$ interactions per bunch crossing during this data-taking period was less than 0.15, indicating a negligible pileup contribution. The MC samples used have no pileup contribution.

Events are required to contain at least six tracks that fulfill the following criteria:

(i) $p_T > 0.5$ GeV;
(ii) $|\eta| < 2.5$;
(iii) a minimum of one pixel and six SCT hits;
(iv) a hit in the innermost pixel layer, if the corresponding pixel module was active;
(v) transverse and longitudinal impact parameters with respect to the primary vertex, $|d_0| < 1.5$ mm and $|z_0| \sin \theta < 1.5$ mm;
(vi) a track-fit probability $\chi^2 > 0.01$ for tracks with $p_T > 10$ GeV in order to remove mismeasured tracks.

Tracks with $p_T > 0.5$ GeV are less prone than lower-$p_T$ tracks to inefficiencies and systematic uncertainties resulting from interactions with the material inside the tracking volume.

After event selection, the analysis is based on approximately $17 \times 10^6$ events containing approximately $300 \times 10^6$ tracks. For the PYTHIA6 generator and for the PYTHIA8 generator, which has a harder diffractive model than the former, the contribution to the event shape observables from diffractive events is negligible when requiring six or more tracks in the event.

The $p_T$ distributions of all tracks and of the leading track in the selected event are shown in Fig. 1. The fraction of events in each $p_T^{lead}$ bin is shown in Table II.

### VI. BACKGROUND CONTRIBUTIONS

#### A. Backgrounds

Backgrounds comprise beam-induced events, due to beam-gas and beam-material interactions, as well as non-beam backgrounds from cosmic-ray interactions and detector noise. The contribution of these background events remaining after the event selection is estimated using the number of pixel hits not associated with reconstructed tracks. This multiplicity includes unassigned hits from low-$p_T$ looping tracks, but is dominated at higher multiplicities by hits from charged particles produced in inelastic interactions of protons with the residual gas inside the beam pipe. The vertex requirement removes most of the beam background events and the residual contribution is below 0.1%. As the level of background is very low, no explicit background subtraction is performed.

#### B. Secondary track fraction

The primary charged-particle multiplicities are measured from selected tracks after correcting for the fractions of secondary and poorly reconstructed tracks in the sample. The potential background from fake tracks is found from MC studies to be less than 0.01% [19].

Nonprimary tracks arise predominantly from hadronic interactions, photon conversions to positron–electron pairs in the detector material, and decays of long-lived particles. For $p_T > 0.5$ GeV the contribution from photon conversions is small. The systematic uncertainty from secondary decays is included in the uncertainties associated with the tracking performance.

### VII. CORRECTION TO PARTICLE LEVEL

To facilitate comparison with theoretical predictions and other measurements, the event shape distributions for charged particles are presented at particle level, after

![FIG. 1 (color online). The distribution of the transverse momentum of all tracks and of the leading transverse momentum track in data at detector level. The uncertainties shown are statistical. Where not visible, the statistical error is smaller than the marker size.](image-url)
correction for trigger and event selection efficiencies, as well as detector resolution effects. A two-step correction procedure is used: first, corrections for event selection efficiency are applied, followed by an additional bin-by-bin correction to account for tracking inefficiencies, possible bin migrations, and any remaining detector effects.

A. Event-level correction

Trigger and vertexing efficiencies are taken from a previous analysis using the same data sample [19]. The efficiency of the MBTS trigger is determined from data using a control trigger and found to be fully efficient for the analysis requirement of at least six tracks. The vertex reconstruction efficiency is also measured in data by taking the ratio of the number of triggered events with a reconstructed vertex to the total number of triggered events. This ratio is also found to be very close to unity. The total correction applied to account for events lost due to the trigger and vertex requirements is less than 1% and it varies very weakly with the number of tracks associated with the primary vertex.

B. Bin-by-bin correction

The event shape observables presented here are sensitive to changes in the configuration of the selected tracks. Applying average track efficiencies to individual tracks on a track-by-track basis and reweighting tracks distorts the event shape distribution. A more robust approach is to apply bin-by-bin corrections to find the event shape distribution at particle level. Such a bin-by-bin correction is applied to all distributions after applying the event-level efficiency corrections described above.

The correction factors $C_{\text{bin}}$ are evaluated separately in each bin for each event shape observable,

$$C_{\text{bin}} = \frac{V_{\text{bin}}^{\text{Gen}}}{V_{\text{bin}}^{\text{Reco}, \text{eff corr}}}$$

where $V_{\text{bin}}^{\text{Gen}}$ and $V_{\text{bin}}^{\text{Reco}, \text{eff corr}}$ represent the generator-level MC value of the bin content and the reconstructed MC value after applying the event-level efficiency corrections for each bin, respectively. The corrected value of the bin content for an observable is found by multiplying the measured bin content by the corresponding correction factor. The bin sizes are chosen to be consistent with the resolution of the correction procedure.

The correction factors are calculated using the two different models implemented in PYTHIA6 AMBT1 and HERWIG++. This correction accounts for bin-by-bin migrations and tracking inefficiencies. For each distribution, the unfolding factor is typically within $\pm 10\%$ of unity for most of the range. It is very close to unity for the average values, except at the highest $\sum p_T$. The difference from unity becomes more pronounced at the statistically limited edges of the distributions. The correction factors for the inclusive

FIG. 2 (color online). The generated and reconstructed MC distributions of the complement of transverse thrust, the thrust minor, and the transverse sphericity are shown in the top part of each plot for the lowest $p_T^{\text{had}}$ range. The correction factors are shown in the lower parts for PYTHIA6 AMBT1 and the HERWIG++ default tune. The data are shown with only the efficiency corrections and statistical uncertainties. Where not visible, the statistical error is smaller than the marker size.
distributions of the three event shape observables are shown in the bottom panels of Fig. 2 for the two MC event generators mentioned above. Although the two MC generators have different distributions, the bin-by-bin correction factors are similar.

VIII. SYSTEMATIC UNCERTAINTIES

Systematic uncertainties on the measured distributions are assessed with the following sources of uncertainty included:

Tracking: The largest of the systematic uncertainties for the tracking inefficiency [19] is found to be due to the material description in the inner detector. This is determined to produce a relative uncertainty of 2% in the efficiency in the barrel region, rising to ~7% for 2.3 < |η| < 2.5. The contribution of the propagated uncertainty is found to be less than 1% of the content in each bin of the shape distributions.

Bin-by-bin correction model dependence: The remaining contributions to the overall systematic uncertainty result from the specific correction method used in this analysis. The bin-by-bin corrections in general depend on the number of charged particles and their p_T distributions, so there is some dependence on the event generators. In order to estimate this uncertainty, it is necessary to compare different plausible event generators, which deviate significantly from each other, but still give predictions close to the data. The corrected results using the two very different PYTHIA6 AMBT1 and HERWIG++ models are compared. As these two generators use very different soft-QCD models the difference is assigned as a systematic uncertainty. The generated and reconstructed distributions are shown in Fig. 2 for the two MC event generators and compared with the detector-level data.

Statistical uncertainty of bin-by-bin correction: In addition to the model-dependent uncertainty in the bin-by-bin correction, there is also a statistical uncertainty due to the finite size of the MC sample. The statistical fluctuations of the PYTHIA6 AMBT1 correction factor are found to be negligible for most of each distribution, increasing to a few percent in the tails of the distributions. This is also added to the overall systematic uncertainty estimate.

The systematic uncertainty due to the small number of residual multiple proton–proton interactions is estimated to be negligible.

All the above mentioned systematic uncertainties are added in quadrature. Table III lists representative values for the various contributions to the systematic uncertainty in the content of each bin for all the event shape observables away from the edges of the distributions.

IX. RESULTS AND DISCUSSION

The distributions of the complement of the transverse thrust, thrust minor, and transverse sphericity are presented in Figs. 3–5, in different p_T^{lead} ranges. The behavior of the average values of the shape variables as functions of the charged-particle multiplicity, N_{ch}, and transverse momentum scalar sum, \( \sum p_T \), is presented in Fig. 6. Predictions from the PYTHIA6 AMBT2B, PYTHIA6 DW, PYTHIA6 Z1, PYTHIA8 A2, and HERWIG++ UE7-2 models are also shown. AMBT2B is chosen instead of AMBT1, which was used to correct the data back to the particle level because it shows a slight improvement in reproducing the distributions of charged-particle transverse momentum and multiplicity [36].

The distributions shown in Figs. 3–5 indicate a prevalence of spherical events in the lower p_T^{lead} ranges. A slight shift toward less spherical events and a broadening of the distributions is observed for events starting with p_T^{lead} > 7.5 GeV in Fig. 3(d) for \( \tau^\perp_{ch} \) and in Fig. 4(d) for \( T_M^\perp \). For both variables, a transition to less spherical events is seen for p_T^{lead} > 10 GeV in Figs. 3(e) and 4(e). The distribution of transverse sphericity is more sensitive to the increase of p_T^{lead}, and shows a marked shift toward less spherical events starting at p_T^{lead} > 5.0 GeV in Fig. 5(c). The average value of the distributions, the rms width, and the skewness of the distributions are given in Table IV, which supports this observation. Mean values of the complement of transverse thrust and the transverse thrust minor are observed to initially rise with increasing p_T^{lead}, with their maximum value in the range 2.5 < p_T^{lead} < 5 GeV, before decreasing. A similar trend is observed by the ALICE Collaboration, which has measured the transverse sphericity distribution selecting charged particles with |η| < 0.8, in inelastic 7 TeV pp collisions [8].

Overall, the PYTHIA6 tune Z1, tuned to the underlying event distributions at the LHC, agrees the best with most of the distributions. The PYTHIA6 DW tune predictions are consistently furthest from the data, as seen in the \( \tau^\perp_{ch} \) and \( T_M^\perp \) distributions. This is not unexpected as DW is tuned to reproduce the Tevatron data and does not agree with the charged-particle multiplicity and p_T distributions in LHC data [19]. However it performs similarly to other models/tunes for the S^h_{ch} distribution in intermediate to high p_T^{lead} values, as is seen in Figs. 5(c)–5(e). The AMBT2B tune, which is based on minimum-bias LHC data, shows better agreement for the lowest p_T^{lead} distributions than for the intermediate p_T^{lead} distributions, as is seen in Fig. 3(a) and in Fig. 4(a). Compared to the PYTHIA6 AMBT2B tune, the predictions of the PYTHIA8 A2 and HERWIG++ UE7-2 tunes show better agreement with the data in the intermediate to high p_T^{lead} ranges. The UE7-2 tune, based like Z1 on LHC
MEASUREMENT OF CHARGED-PARTICLE EVENT SHAPE... PHYSICAL REVIEW D 88, 032004 (2013)

FIG. 3 (color online). Normalized distributions of the complement of transverse thrust using at least six charged particles with $p_T > 0.5$ GeV and $|\eta| < 2.5$ for different requirements on the transverse momentum of the leading charged-particle, $p_T^\text{lead}$. The error bars show the statistical uncertainty while the shaded area shows the combined statistical and systematic uncertainty. Where not visible, the statistical error is smaller than the marker size.
FIG. 4 (color online). Normalized distributions of transverse thrust minor using at least six charged particles with $p_T > 0.5$ GeV and $|\eta| < 2.5$ for different requirements on the transverse momentum of the leading charged-particle, $p_T^{\text{lead}}$. The error bars show the statistical uncertainty while the shaded area shows the combined statistical and systematic uncertainty. Where not visible, the statistical error is smaller than the marker size.
FIG. 5 (color online). Normalized distributions of transverse sphericity using at least six charged particles with $p_T > 0.5$ GeV and $|\eta| < 2.5$ for different requirements on the transverse momentum of the leading charged-particle, $p_T^{\text{lead}}$. The error bars show the statistical uncertainty while the shaded area shows the combined statistical and systematic uncertainty. Where not visible, the statistical error is smaller than the marker size.
FIG. 6 (color online). Mean values of the complement of transverse thrust, transverse thrust minor, and transverse sphericity (top to bottom) using at least six charged particles with $p_T > 0.5$ GeV and $|\eta| < 2.5$ versus charged-particle multiplicity of the event (left) and versus charged-particle transverse momentum scalar sum of the event (right). The error bars show the statistical uncertainty while the shaded area shows the combined statistical and systematic uncertainty. Where not visible, the statistical error is smaller than the marker size.
<table>
<thead>
<tr>
<th>$p_T^{\text{lead}}$ range</th>
<th>Mean</th>
<th>rms</th>
<th>Skewness</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.5 GeV &lt; $p_T^{\text{lead}}$ ≤ 2.5 GeV</td>
<td>0.227 ± 0.002</td>
<td>0.064 ± 0.008</td>
<td>-0.54 ± 0.03</td>
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<td>2.5 GeV &lt; $p_T^{\text{lead}}$ ≤ 5.0 GeV</td>
<td>0.240 ± 0.006</td>
<td>0.062 ± 0.001</td>
<td>-0.68 ± 0.04</td>
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<td>0.227 ± 0.007</td>
<td>0.065 ± 0.003</td>
<td>-0.55 ± 0.04</td>
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<td>7.5 GeV &lt; $p_T^{\text{lead}}$ ≤ 10 GeV</td>
<td>0.210 ± 0.010</td>
<td>0.068 ± 0.005</td>
<td>-0.36 ± 0.09</td>
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<td>$p_T^{\text{lead}}$ &gt; 10 GeV</td>
<td>0.185 ± 0.011</td>
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<td>-0.11 ± 0.28</td>
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<thead>
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<th>rms</th>
<th>Skewness</th>
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<td>0.490 ± 0.006</td>
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<td>$p_T^{\text{lead}}$ &gt; 10 GeV</td>
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<th>Skewness</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.5 GeV &lt; $p_T^{\text{lead}}$ ≤ 2.5 GeV</td>
<td>0.618 ± 0.005</td>
<td>0.190 ± 0.006</td>
<td>-0.35 ± 0.05</td>
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<tr>
<td>2.5 GeV &lt; $p_T^{\text{lead}}$ ≤ 5.0 GeV</td>
<td>0.579 ± 0.013</td>
<td>0.204 ± 0.003</td>
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<tr>
<td>5.0 GeV &lt; $p_T^{\text{lead}}$ ≤ 7.5 GeV</td>
<td>0.449 ± 0.019</td>
<td>0.206 ± 0.002</td>
<td>0.16 ± 0.24</td>
</tr>
<tr>
<td>7.5 GeV &lt; $p_T^{\text{lead}}$ ≤ 10 GeV</td>
<td>0.337 ± 0.017</td>
<td>0.183 ± 0.004</td>
<td>0.57 ± 0.09</td>
</tr>
<tr>
<td>$p_T^{\text{lead}}$ &gt; 10 GeV</td>
<td>0.230 ± 0.024</td>
<td>0.157 ± 0.007</td>
<td>1.06 ± 0.04</td>
</tr>
</tbody>
</table>

underlying event data, is expected to perform better in events characterized by a hard scatter, resulting in higher $p_T^{\text{lead}}$ values. However, the minimum-bias A2 tune shows a similar or slightly better level of agreement with data for the high $p_T^{\text{lead}}$ distributions, possibly indicating that the improved MPI modeling compared to PYTHIA6 tunes does play a role. All models tend to better reproduce the data selected with the higher $p_T^{\text{lead}}$ ranges.

The mean values of event shape observables as functions of $N_{ch}$ and $\sum p_T$ are shown in Fig. 6. They are seen to increase with $N_{ch}$, but the increase is less marked at values of $N_{ch}$ above about 30. For low values of $N_{ch}$, the mean values of the event shape variables correspond to less spherical events, while the average values for large multiplicity are largely consistent with the positions of the maxima of the corresponding distributions for the lowest $p_T^{\text{lead}}$ range. A similar trend is seen for distributions as a function of $\sum p_T$; however, for $\sum p_T$ over 100 GeV, the mean starts to decrease again, indicative of a dijet topology. In general, the MC models predict fewer high-sphericity events than are seen in the data. With the exception of PYTHIA 6 DW, the MC models seem to predict the behavior with multiplicity reasonably well in Fig. 6. However, the MC predictions are seen to differ in shape at very high $\sum p_T$, where the decrease of mean values happens in the MC predictions before the data. The behavior of mean transverse sphericity as a function of multiplicity measured by the ALICE Collaboration [8] exhibits a similar behavior to that observed here, with the data lying at values higher than predicted by the MC models.

**X. CONCLUSIONS**

The event shape observables, transverse thrust, transverse thrust minor, and transverse sphericity, have been measured in inelastic proton–proton collisions at $\sqrt{s} = 7$ TeV requiring at least six charged particles per event selected by a minimum-bias trigger. The distributions and mean values have been compared to predictions of different MC models tuned to inclusive particle distributions and underlying event data. The dependence of the event shapes on the number of charged particles, on the sum of charged-particle $p_T$ and on the leading charged-particle $p_T$ has been studied.

The distributions of all three event shape variables show an evolution toward less spherical events as $p_T^{\text{lead}}$ increases, but the effect is smaller for transverse thrust and thrust minor compared to transverse sphericity. The dependence of the event shape mean values as functions of $N_{ch}$ and $\sum p_T$ is similar, due the correlation between the two variables [19]. For each variable, the evolution toward a more spherical event shape with increasing multiplicity is rapid
initially and slows at higher multiplicities. All tested MC generators underestimate the fraction of events of spherical character and none reproduces accurately the event shape distributions. The MC tunes based on the properties of the underlying event show in general better agreement with the distributions. The MC tunes based on the properties of the character and none reproduces accurately the event shape generators underestimate the fraction of events of spherical initially and slows at higher multiplicities.

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M. J. Woudstra,82 K. W. Woźniak,39 K. Wraight,53 M. Wright,53 B. Wrona,73 S. L. Wu,173 X. Wu,49 Y. Wu,33b,mm
E. Wulf,35 B. M. Wynne,46 S. Xella,36 M. Xiao,136 S. Xie,48 C. Xu,33b,aa D. Xu,159 B. Yabsley,150 S. Yacoob,145a,nn
T. Yamanaka,155 J. Yamaoka,65 T. Yamaoka,155 Y. Yamaoka,155 Z. Yan,22 H. Yang,87 U. K. Yang,82 Y. Yang,60
Z. Yang,146a,146b S. Yanush,91 L. Yao,33a Y. Yao,15 Y. Yasu,65 G. V. Ybeles Smit,130 J. Ye,40 S. Ye,25 M. Yilmaz,4c
R. Yoosoofmiya,123 K. Yorita,171 R. Yoshida,6 C. Young,143 C. J. Young,118 S. Youssef,22 D. Yu,25 J. Yu,8 J. Yu,112
Z. Zinonos,122a,122b S. Zenz,15 D. Zerwas,115 G. Zevi della Porta,57 Z. Zhan,33d D. Zhang,33b,iv H. Zhang,88 J. Zhang,6
R. Zimmermann,21 S. Zimmermann,21 S. Zimmermann,48 M. Ziolkowski,141 R. Zitoun,3 L. Zivković,35
V. V. Zmouchko,128a G. Zobenig,173 A. Zoccoli,20a,20b M. zur Nedden,16 V. Zutshi,106 and L. Zwalinski30
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