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Measurement of isolated-photon pair production in $pp$ collisions at $\sqrt{s} = 7$ TeV with the ATLAS detector

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ABSTRACT: The ATLAS experiment at the LHC has measured the production cross section of events with two isolated photons in the final state, in proton-proton collisions at $\sqrt{s} = 7$ TeV. The full data set collected in 2011, corresponding to an integrated luminosity of 4.9 fb$^{-1}$, is used. The amount of background, from hadronic jets and isolated electrons, is estimated with data-driven techniques and subtracted. The total cross section, for two isolated photons with transverse energies above 25 GeV and 22 GeV respectively, in the acceptance of the electromagnetic calorimeter ($|\eta| < 1.37$ and $1.52 < |\eta| < 2.37$) and with an angular separation $\Delta R > 0.4$, is $44.0^{+3.2}_{-3.2}$ pb. The differential cross sections as a function of the di-photon invariant mass, transverse momentum, azimuthal separation, and cosine of the polar angle of the largest transverse energy photon in the Collins-Soper di-photon rest frame are also measured. The results are compared to the prediction of leading-order parton-shower and next-to-leading-order and next-to-next-to-leading-order parton-level generators.

KEYWORDS: Hadron-Hadron Scattering
1 Introduction

The measurement at the LHC of the production cross section, in $pp$ collisions, of two isolated photons not originating from hadronic decays, $pp \rightarrow \gamma\gamma + X$, provides a tool to probe perturbative Quantum Chromodynamics (QCD) predictions and to understand the irreducible background to new physics processes involving photons in the final state. These processes include Higgs boson decays to photon pairs ($H \rightarrow \gamma\gamma$) or graviton decays predicted in some Universal Extra-Dimension models [1, 2].

Recent cross section measurements for di-photon production at hadron colliders were performed by the DØ [3] and CDF [4] collaborations at the $\sqrt{s} = 1.96$ TeV Tevatron $p\bar{p}$ collider, and by ATLAS [5] and CMS [6] using $\sqrt{s} = 7$ TeV $pp$ collisions recorded at the LHC in 2010.

In this paper, the production cross section of two isolated photons with transverse energies ($E_T$) above 25 GeV and 22 GeV respectively, in the acceptance of the ATLAS electromagnetic calorimeter ($|\eta| < 1.37$ and $1.52 < |\eta| < 2.37$) and with an angular separation
\( \Delta R > 0.4 \), is measured. The results are obtained using the data collected by the ATLAS experiment in 2011, which corresponds to an integrated luminosity\(^1\) of \((4.9 \pm 0.2) \text{ fb}^{-1}\), thus increasing the sample size by more than a factor of 100 compared to the previous measurement. The transverse energy thresholds for the two photons are higher than in the previous measurement \((16 \text{ GeV})\).

The integrated di-photon production cross section is measured, as well as the differential cross sections as a function of four kinematic variables: the di-photon invariant mass \((m_{\gamma\gamma})\), the di-photon transverse momentum \((p_{T,\gamma\gamma})\), the azimuthal\(^2\) separation between the photons in the laboratory frame \((\Delta \phi_{\gamma\gamma})\), and the cosine of the polar angle of the highest \(E_T\) photon in the Collins-Soper di-photon rest frame \((\cos \theta^*_{\gamma\gamma})\) [9]. The first distribution is of obvious interest for resonance searches; the second and the third provide important information in the study of higher-order QCD perturbative effects and fragmentation, especially in some specific regions such as the small \(\Delta \phi_{\gamma\gamma}\) limit; the fourth can be used to investigate the spin of di-photon resonances. For this purpose, the Collins-Soper rest frame is preferred to other frame definitions because of its robustness with respect to initial state radiation. The results are compared to the predictions from: parton-shower Monte Carlo generators, PYTHIA [10] and SHERPA [11]; parton-level calculations with next-to-leading-order (NLO) QCD corrections using the DIPHOX [12] program complemented by GAMMA2MC [13]; and at next-to-next-to-leading-order (NNLO), using 2\(\gamma\)NNLO [14]. The contribution from the di-photon decays of the particle recently discovered by ATLAS [15] and CMS [16] in the search for the Standard Model Higgs boson is not included in the theoretical calculations. It is expected to contribute around 1% of the signal in the \(120 < m_{\gamma\gamma} < 130 \text{ GeV}\) interval, and negligibly elsewhere.

2 The ATLAS detector

ATLAS [17] is a multipurpose detector with a forward-backward symmetric cylindrical geometry and nearly \(4\pi\) coverage in solid angle. The most relevant subdetectors for the present analysis are the inner tracking detector (ID) and the calorimeters.

The ID consists of a silicon pixel detector and a silicon microstrip detector covering the pseudorapidity range \(|\eta| < 2.5\), and a straw tube transition radiation tracker covering \(|\eta| < 2.0\). It is immersed in a 2 T magnetic field provided by a superconducting solenoid. The ID allows efficient reconstruction of converted photons if the conversion occurs at a radius of up to \(\approx 0.80 \text{ m}\).

The electromagnetic calorimeter (ECAL) is a lead/liquid-argon (LAr) sampling calorimeter providing coverage for \(|\eta| < 3.2\). It consists of a barrel section \((|\eta| < 1.475)\)
and two end-caps ($1.375 < |\eta| < 3.2$). The central region ($|\eta| < 2.5$) is segmented into three longitudinal layers. The first (inner) layer, covering $|\eta| < 1.4$ in the barrel and $1.5 < |\eta| < 2.4$ in the end-caps, has high granularity in the $\eta$ direction (between 0.003 and 0.006 depending on $\eta$), sufficient to provide event-by-event discrimination between single-photon showers and two overlapping showers from a $\pi^0$ decay. The second layer, which collects most of the energy deposited in the calorimeter by the photon shower, has a cell granularity of $0.025 \times 0.025$ in $\eta \times \phi$. The third layer is used to correct high energy showers for leakage beyond the ECAL. In front of the electromagnetic calorimeter a thin presampler layer, covering the pseudorapidity interval $|\eta| < 1.8$, is used to correct for energy loss before the ECAL.

The hadronic calorimeter (HCAL), surrounding the ECAL, consists of an iron/scintillator tile calorimeter in the range $|\eta| < 1.7$, and two copper/LAr calorimeters spanning $1.5 < |\eta| < 3.2$. The ECAL and HCAL acceptance is extended by two LAr forward calorimeters (using copper and tungsten as absorbers) up to $|\eta| < 4.9$.

Di-photon events are recorded using a three-level trigger system. The first level, implemented in hardware, is based on towers defined with a coarser granularity ($0.1 \times 0.1$ in $\eta \times \phi$) than that of the ECAL. They are used to search for electromagnetic deposits in $\eta \times \phi$ regions of $2 \times 1$ and $1 \times 2$ towers, within a fixed window of size $2 \times 2$ and with a transverse energy above a programmable threshold. The second- and third-level triggers are implemented in software and exploit the full granularity and energy calibration of the calorimeter to refine the first-level trigger selection.

### 3 Data and Monte Carlo samples

The data set analysed consists of the 7 TeV proton-proton collisions recorded by the ATLAS detector in 2011. Only events where the beam conditions are stable and the trigger system, the tracking devices, and the calorimeters are operational, are considered. Monte Carlo (MC) samples are produced using various generators as described below. Particle interactions with the detector material and the detector response are simulated with Geant4 [18]. The events are reconstructed with the same algorithms used for collision data. More details of the event generation and simulation infrastructure are provided in ref. [19].

Simulated di-photon events are generated with both Pythia 6.4.21 and Sherpa 1.3.1. Pythia uses the modified leading-order MRST2007 [20] parton distribution functions (PDFs) while Sherpa uses the CTEQ6L1 [21] PDFs. The Pythia event-generator parameters are set according to the ATLAS AMBT2 [22] tune, while the Sherpa parameters are the default ones of the Sherpa 1.3.1 distribution. Photons originating from the hard scattering and quark bremsstrahlung are included in the analysis. The MC di-photon signal is generated with a photon $E_T$ threshold of 20 GeV; one million events are produced both with Pythia and Sherpa. They are used to model the transverse isolation energy (see section 4) distribution of signal photons, to compute the reconstruction efficiency and to study the systematic uncertainties on the reconstructed quantities. Background $\gamma$-jet events are generated using Alpgen [23] with the CTEQ6L1 PDF set.
4 Event selection

Events are collected using a di-photon trigger with a nominal transverse energy threshold of 20 GeV for both photon candidates. The photon trigger objects are required to pass a selection based on shower shape variables computed from the energy deposits in the second layer of the electromagnetic calorimeter and in the hadronic calorimeter. The requirements are looser than the photon identification criteria applied in the offline selection. In order to reduce non-collision backgrounds, events are required to have a reconstructed primary vertex with at least three associated tracks and consistent with the average beam spot position. The signal inefficiency of this requirement is negligible.

Photons are reconstructed from electromagnetic energy clusters in the calorimeter and tracking information provided by the ID as described in ref. [24]. Photons reconstructed near regions of the calorimeter affected by read-out or high-voltage failures are not considered.\(^3\) The cluster energies are corrected using an in-situ calibration based on the \(Z\) boson mass peak [25], and the determination of the pseudorapidities is optimized using the technique described in ref. [15]. In order to benefit from the fine segmentation of the first layer of the electromagnetic calorimeter to discriminate between genuine prompt photons and fake photons within jets, the photon candidate pseudorapidity must satisfy \(|\eta| < 1.37\) or \(1.52 < |\eta| < 2.37\). We retain photon candidates passing loose identification requirements, based on the same shower shape variables — computed with better granularity and resolution — and the same thresholds used at trigger level. The highest-\(E_T\) (“leading”) and second highest-\(E_T\) (“subleading”) photons within the acceptance and satisfying the loose identification criteria are required to have \(E_{T,1} > 25\) GeV and \(E_{T,2} > 22\) GeV, respectively. The fraction of events where the two selected photon candidates are not matched to the photon trigger objects is negligible. The angular separation between the two photons, \(\Delta R = \sqrt{(\Delta \eta)^2 + (\Delta \phi)^2}\), is required to be larger than 0.4, in order to avoid one photon candidate depositing significant energy in the isolation cone of the other, as defined below.

Two further criteria are used to define the signal and background control regions. Firstly the tight photon selection [24] (abbreviated as \(T\) in the following) is designed to reject hadronic jet background, by imposing requirements on nine discriminating variables computed from the energy leaking into the HCAL and the lateral and longitudinal shower development in the ECAL. Secondly the transverse isolation energy \(E_{T,iso}\) is computed from the sum of the positive-energy topological clusters with reconstructed barycentres inside a cone of radius \(\Delta R = 0.4\) around the photon candidate. The algorithm for constructing topological clusters suppresses noise by keeping only those cells with a significant energy deposit and their neighbouring cells. The cells within \(0.125 \times 0.175\) in \(\eta \times \phi\) around the photon are excluded from the calculation of \(E_{T,iso}\). The mean value of the small leakage of the photon energy from this region into the isolation cone, evaluated as a function of the photon transverse energy, is subtracted from the measured value of \(E_{T,iso}\) (meaning that \(E_{T,iso}\) can be negative). The typical size of this correction is a few percent of the photon transverse energy. The measured value of \(E_{T,iso}\) is further corrected by subtracting the estimated

\(^3\)This requirement leads to a typical loss of 0.8% to 1.4% on the photon reconstruction efficiency, depending on the data-taking period.
contributions from the underlying event and additional pp interactions. This correction is computed on an event-by-event basis, by calculating the transverse energy density from low-transverse-momentum jets, as suggested in refs. [26, 27]. The median transverse energy densities of the jets in two \( \eta \) regions, \( |\eta| < 1.5 \) and \( 1.5 < |\eta| < 3.0 \), are computed separately, and the one for the region containing the photon candidate pseudorapidity is multiplied by the total area of all topological clusters used in the calculation of the isolation variable in order to estimate the correction. Signal photons are required to pass the tight selection (“tight photons”) and the isolation requirement \( I, -4 < E_{T}^{\text{iso}} < 4 \) GeV. A total of 165 767 pairs of tight, isolated photons are selected. The fraction of events in which an additional photon pair passes all the selection criteria, except for the requirement on the two photons being the leading and subleading \( E_{T} \) candidates, is less than 1 per 100 000. The non-tight (\( \tilde{T} \)) photon candidates are defined as those failing the tight criteria for at least one of the shower-shape variables that are computed from the energy deposits in a few cells of the first layer of the electromagnetic calorimeter adjacent to the cluster barycentre. Photon candidates with \( 4 < E_{T}^{\text{iso}} < 8 \) GeV are considered non-isolated (\( \tilde{I} \)).

5 Signal yield extraction

After the selection, the main background is due primarily to \( \gamma \)-jet and secondarily to di-jet (jj) final states, collectively called “jet background” in the following. Two methods, the two-dimensional sidebands and the two-dimensional fit, already exploited in ref. [5], are used to perform an in-situ statistical subtraction of the jet background from the selected photon candidate pairs, as described in section 5.1.

After the jet background contribution is subtracted, a small residual background contamination arises from events where isolated electrons are misidentified as photons. This contribution is estimated as described in section 5.2.

5.1 Jet background subtraction

Both the two-dimensional sidebands and the two-dimensional fit methods use the photon transverse isolation energy and the tight identification criteria to discriminate prompt photons from jets. They rely on the fact that the correlations between the isolation and the tight criteria in background events are small, and that the signal contamination in the non-tight or non-isolated control regions is low.

The two-dimensional sidebands method counts the numbers of photon candidate pairs where each of the candidates passes or fails the tight and the isolation criteria. Four categories are defined for each photon, resulting in 16 categories of events. The inputs to the method are the numbers of events in the categories and the signal efficiencies of the tight and isolation requirements. The correlation between these two requirements is assumed to be negligible for background events. The method allows the simultaneous extraction of the numbers of true di-photon signal, \( \gamma j, j \gamma \) \(^4\) and jj background events, and the tight and isolation efficiencies for fake photon candidates from jets (“fake rates”). The

\(^4\)Here and in the following, \( \gamma j, j \gamma \) denotes the events where the leading (subleading) candidate is a true photon, and the other candidate a true jet.
The expected number of events in each category is written as a function of the parameters (yields, efficiencies, fake rates and correlation factors) and the system of 16 equations is solved with a $\chi^2$ minimization procedure. This method is an extension of the one used in our previous di-photon analysis [5]. It allows the extraction of different isolation fake rates for jets in $j\gamma$ or $jj$ events as well as a correlation factor for the isolation of jet pairs.

The two-dimensional fit method consists of an extended maximum likelihood template fit to the two-dimensional distribution of the transverse isolation energies $E_{T,i}^{iso}$ and $E_{T,2}^{iso}$ of the two photon candidates in events belonging to the $T\cdot T$ sample, i.e. where both photons satisfy the tight identification criteria. The fit is performed in the isolation range $-4 < E_{T,i}^{iso} < 8$ GeV ($i = 1, 2$). The correlations between the transverse isolation energies of the two candidates in di-photon, $\gamma j$, and $j\gamma$ events are found to be negligible in MC samples, and the products of two one-dimensional templates for $E_{T,1}^{iso}$ and $E_{T,2}^{iso}$ are used for each of the three event species. For the $jj$ component, large correlations are observed in data, and a two-dimensional template is used. The two-dimensional fit is described in detail in our previous paper [5]. There are two differences between the present and previous analyses: the use now of binned distributions instead of smooth parametric functions for the photon and jet templates, and the correction for signal leakage in the background templates, as described below.

The transverse isolation energy distributions of the signal photons and the corresponding efficiencies of the signal requirement $-4 < E_{T}^{iso} < 4$ GeV are obtained from the SHERPA di-photon sample, separately for the leading and the subleading candidates. In the two-dimensional fit method, the templates are shifted by $+160$ and $+120$ MeV respectively in order to maximize the likelihood, as determined from a scan as a function of the shifts. These values are also used to compute the signal efficiencies of the isolation requirement needed in the two-dimensional sidebands method. Shifts of similar size between ATLAS data and MC simulation have been observed in the transverse isolation energy distribution, computed with the same technique (based on topological clusters inside a cone of radius 0.4), of electron control samples selected from $Z \rightarrow ee$ decays with a tag-and-probe method. The $E_{T}^{iso}$ distributions of prompt photons in $\gamma j$ and $j\gamma$ events are assumed to be identical to that of prompt photons in di-photon events, as found in simulated samples. The tight identification efficiencies for prompt photons, needed in the two-dimensional sidebands method and in the final cross section measurement, are estimated using the same di-photon MC sample. The shower shape variables are corrected for the observed differences between data and simulation in photon-enriched control samples. Residual differences between the efficiencies in the simulation and in data are corrected using scale factors determined from control samples of photons from radiative $Z$ boson decays, electrons selected with a tag-and-probe technique from $Z \rightarrow ee$ decays, and photon-enriched control samples of known photon purity [28]. After applying these corrections, the photon identification efficiency in the simulation is estimated to reproduce the efficiency in data to within 2%. For the two-dimensional fit, the transverse isolation energy template of the leading (subleading) jet in $j\gamma$ ($\gamma j$) events is extracted directly from data where one candidate passes the non-tight and the other passes both the tight identification and isolation (TI) requirements. For $jj$ events, the two-dimensional template is obtained from data in which the two candidates...
Figure 1. Projections of the two-dimensional fit to the transverse isolation energies of the two photon candidates: leading photon (left) and sub-leading photon (right). The photon templates from Sherpa are shifted by +160 MeV (+120 MeV) for the leading (subleading) photon. Solid circles represent the observed data. The (black) solid line is the fit result, the (violet) dash-dotted curve shows the $\gamma\gamma$ component. The (red) dotted line shows in the left (right) figure the contribution from $\gamma j$ ($j\gamma$) events. In both figures, the (blue) dashed line represents a broad background component in the photon candidates’ sample: for the leading candidate this is due to $j\gamma$ and $jj$ final states, whereas for the sub-leading candidate it comes from $\gamma j$ and $jj$ final states.

<table>
<thead>
<tr>
<th>Yield</th>
<th>two-dimensional sidebands results</th>
<th>two-dimensional fit results</th>
</tr>
</thead>
<tbody>
<tr>
<td>$N_{\gamma\gamma}$</td>
<td>113 200 ±600 (stat.) ±5000−8000 (syst.)</td>
<td>111 700 ±500 (stat.) ±4500−7600 (syst.)</td>
</tr>
<tr>
<td>$N_{\gamma j}$</td>
<td>31 500 ±400 (stat.) ±3900−3100 (syst.)</td>
<td>31 500 ±300 (stat.) ±4800−3600 (syst.)</td>
</tr>
<tr>
<td>$N_{j\gamma}$</td>
<td>13 000 ±300 (stat.) ±2500−800 (syst.)</td>
<td>13 900 ±300 (stat.) ±3400−2100 (syst.)</td>
</tr>
<tr>
<td>$N_{jj}$</td>
<td>8 100 ±100 (stat.) ±1900−1400 (syst.)</td>
<td>8 300 ±100 (stat.) ±300−2100 (syst.)</td>
</tr>
</tbody>
</table>

Table 1. Total yields for two candidates satisfying the tight identification and the isolation requirement $-4 < E_{\text{iso}}^T < 4$ GeV. Both statistical and total systematic uncertainties are listed.

are required to be non-tight. The correlation is found to be about 8%. The jet background templates are corrected for signal leakage in the control samples, estimated from the Sherpa sample.

Figure 1 shows the projections of the two-dimensional fit to the transverse isolation energies of the leading and subleading photon candidates. The yields for each of the four components extracted with the two-dimensional sidebands method and the two-dimensional fit are given in table 1. The di-photon purity is around 68% and the di-photon yields agree within 1.5% between the two methods.

To obtain the differential signal yields as a function of the di-photon kinematic variables, such as $m_{\gamma\gamma}$, $p_{T,\gamma\gamma}$, $\Delta\phi_{\gamma\gamma}$ and $\cos\theta^*_{\gamma\gamma}$, the above methods are applied in each bin of the variables. Figure 2 shows the differential spectra of the signal and background components obtained with the two-dimensional fit. In some regions of the di-photon spectra, discrepancies with the two-dimensional sidebands results are larger than those observed for the integrated yield. The results from the two-dimensional fit are used to extract the nominal cross sections, while differences between the results obtained with the two methods are included in the final systematic uncertainty.
Figure 2. Differential spectra in data (solid circles) and from the two-dimensional fit, for the \( \gamma \gamma \) (hollow histogram), \( \gamma j + j \gamma \) (light solid histogram), and \( jj \) (dark solid histogram) contributions. The spectra are shown for the following di-photon variables: \( m_{\gamma \gamma} \) (top left), \( p_{T, \gamma \gamma} \) (top right), \( \Delta \phi_{\gamma \gamma} \) (bottom left), \( \cos \theta^*_\gamma \) (bottom right).

Several sources of systematic uncertainty on the signal yield, estimated after the jet background subtraction, are considered. The dominant uncertainty originates from the choice of the background control regions and accounts for both the uncertainty on the background transverse isolation energy distribution and its correlation with the identification criteria. It is first estimated by varying the number of relaxed criteria in the non-tight definition. For the integrated di-photon yield, the effect is found to be \( +3\% \pm 6\% \). In some bins of the \( m_{\gamma \gamma} \) and \( p_{T, \gamma \gamma} \) spectra where the size of the control samples is small, neighbouring bins are grouped together to extract the jet background templates. Since the background transverse isolation energies depend mildly on these kinematic variables, a systematic uncertainty is evaluated by repeating the yield extraction with jet templates from the adjacent groups of neighbouring bins. The uncertainty on the estimated signal yield is at most \( \pm 9\% \).

In the nominal result, the photon isolation templates are taken from the SHERPA di-photon sample. A systematic uncertainty is evaluated by using alternative templates from the PYTHIA di-photon sample, and from data. The data-driven template for the leading (subleading) photon is obtained by selecting events where the requirement \( E_{T,iso}^\gamma < 8 \) GeV is removed for the leading (subleading) photon candidate, and normalizing the leading (subleading) photon isolation distribution in \( \bar{T} \cdot \bar{T} \) \((T \cdot \bar{T}) \) events, where the leading
(subleading) candidate fails the tight identification while the other candidate passes tight identification and isolation criteria, to the isolation distribution of leading (subleading) candidates in $T_\gamma T_\gamma$ events in the $7 < E_T^{\text{iso}} < 17$ GeV region. The difference between the two distributions is used as an estimate of the photon distribution. The Pythia di-photon sample exhibits higher tails than Sherpa at large values of $E_T^{\text{iso}}$. The data-driven template, on the other hand, is characterized by smaller tails than the Sherpa template, since it is obtained by assuming that the isolation region above 7 GeV is fully populated by background. The corresponding uncertainty on the signal yield is estimated to be $\pm 3\%$ of the integrated di-photon yield. It is rather uniform as a function of $m_{\gamma\gamma}$, $p_{T,\gamma\gamma}$, $\Delta\phi_{\gamma\gamma}$ and $\cos\theta^*_\gamma$, and always below 4%, except at very low $m_{\gamma\gamma}$ where it reaches $\pm 5\%$. The photon isolation template is, to a large extent, independent of the variables under study. Repeating the background subtraction procedure using photon isolation templates extracted in bins of the di-photon variable under study leads to variations of the estimated signal yield within $\pm 2\%$.

Other systematic effects have been considered, and found to be smaller than those previously discussed. The bias created by neglecting the dependence of the identification and isolation efficiencies on $\eta$ and $E_T$ is estimated to be of $+0.02\%$ and $-0.3\%$ respectively. The effect of assuming identical templates for photons in di-photon and in $\gamma$-jet events is evaluated by using instead templates from Alpgen $\gamma$-jet samples for photons in the $\gamma j$ and $j\gamma$ components. The uncertainty on the shifts applied to the MC photon templates ($\pm 10$ MeV for the leading photons and $\pm 5$ MeV for the subleading ones, as determined from the scan) is propagated to the di-photon yields. The impact of the identification efficiencies on the signal leakage correction is estimated by neglecting in the simulation the correction factors nominally applied to the shower shape variables to account for the observed differences between data and MC simulation. These effects produce systematic uncertainties of at most 0.5% on the differential spectra. Finally, no significant effect is observed due to the imperfect modelling of the material in front of the calorimeters.

5.2 Electron background subtraction

Isolated electrons from $W$ or $Z$ boson decays can be misidentified as photons, since the two particles ($e$ and $\gamma$) generate similar electromagnetic showers in the ECAL. Usually a track is reconstructed in the inner detector pointing to the electron ECAL cluster, thus isolated electrons misidentified as photons are mostly classified as converted candidates. Pairs of misidentified, isolated electrons and positrons ($ee$) from processes such as Drell-Yan, $Z \rightarrow ee$, $WW \rightarrow e\nu e\nu$, or of photons and $e^\pm$ from diboson production ($\gamma W \rightarrow e\nu$, $\gamma Z \rightarrow \gamma ee$), provide a background that cannot be distinguished from the di-photon signal based on the photon identification and isolation variables and must therefore be estimated in a separate way. The same procedure exploited in ref. [5], based on the number of $\gamma e$ ($N_{\gamma e}$) and $ee$ ($N_{ee}$) events observed in data, is used to estimate their contributions to the di-photon yield $N_{\gamma\gamma}$ after jet background subtraction.

For a given bin $i$ of the variable $X$ ($X = m_{\gamma\gamma}$, $p_{T,\gamma\gamma}$, $\Delta\phi_{\gamma\gamma}$, or $\cos\theta^*_\gamma$), the signal component $N_{\gamma\gamma}^{\text{sig}}$ in the $N_{\gamma\gamma}$ sample can be evaluated:

$$N_{\gamma\gamma}^{\text{sig}} = N_{\gamma\gamma} - \left[ f_{e\rightarrow\gamma} N_{\gamma e} - (f_{e\rightarrow\gamma})^2 N_{ee} \right] \left( 1 - (f_{e\rightarrow\gamma})^2 \right)^2$$

(5.1)
Figure 3. Fraction of electron background (impurity) as a function of $m_{γγ}$, $p_{T,γγ}$, $Δφ_{γγ}$, and $cosθ^*_{γγ}$.

The fake rates $f_{e→γ}$ and $f_{γ→e}$ are measured using $Z$ boson decays in data. $Z → ee$ decays are used to estimate $f_{e→γ}$ as $N^Z_{ee}/(2N^Z_{ee})$, where $N^Z_{γe}$ and $N^Z_{ee}$ are the numbers of $γe$ and $ee$ pairs with invariant mass within 1.5 $σ$ of the $Z$ boson mass. $Z → γee$ decays are similarly used to estimate $f_{γ→e}$ as $N^Z_{γee}/N^Z_{ee}$. The numbers of continuum background events are estimated from the sidebands of the $ee$, $γe$, $eee$ or $γee$ invariant mass distributions (51 – 61 GeV and 121 – 131 GeV), and subtracted from $N^Z_{ee}$, $N^Z_{γe}$, $N^Z_{eee}$ and $N^Z_{γee}$, respectively. Electrons must satisfy identification criteria based on their shower shape in the electromagnetic calorimeter, quality criteria for the associated track in the ID, and an isolation requirement $E^{iso}_T < 4$ GeV. The measured fake rates, including statistical and systematic uncertainties, are $f_{e→γ} = 0.062^{+0.040}_{-0.010}$ and $f_{γ→e} = 0.038^{+0.024}_{-0.007}$, where the systematic uncertainty is dominated by the dependence on the transverse energy of the candidate photon. Other sources include the uncertainties on $N^Z_{ee}$, $N^Z_{γe}$, $N^Z_{eee}$ and $N^Z_{γee}$ which are evaluated by changing the definition of the $Z$ boson mass window to ±2σ and ±1σ, and shifting the sidebands by ±5 GeV. The fraction of electron background as a function of $m_{γγ}$, $p_{T,γγ}$, $Δφ_{γγ}$, and $cosθ^*_{γγ}$ is shown in figure 3. The enhancements at $m_{γγ} ≈ m_Z$, low $p_{T,γγ}$ and $Δφ_{γγ} ≈ π$ are due to the large $Z$ boson production cross section.

6 Cross section measurement

This section describes the extraction of the final cross sections. The background-subtracted differential spectra are first unfolded to the generated-particle level, to take into account
reconstruction and selection efficiencies estimated from the simulation, and then divided by the integrated luminosity of the data sample and the trigger efficiency relative to the offline selection.

6.1 Efficiency and unfolding

The background-subtracted differential distributions obtained from the data are unfolded to obtain the particle-level spectra by dividing the signal yield in each bin of the di-photon observable under study by a “bin-by-bin” correction, which accounts for signal reconstruction and selection efficiencies and for finite resolution effects. The bin-by-bin nominal corrections are evaluated from the SHERPA di-photon simulated sample as the number of simulated di-photon events satisfying the selection criteria (excluding the trigger requirement) and for which the reconstructed value of the variable $X$ under consideration is in bin $i$, divided by the number of simulated di-photon events satisfying the nominal acceptance criteria at generator-level and for which the generated value of $X$ is in the same bin $i$. The generator-level photon transverse isolation energy is computed from the true four-momenta of the generated particles (excluding muons and neutrinos) inside a cone of radius 0.4 around the photon direction. The pile-up contribution is removed using an analogous method to the one for the experimental isolation variable, by subtracting the product of the area of the isolation cone and the median transverse energy density of the low-transverse-momentum truth-particle jets.

Alternative corrections are calculated with the PYTHIA di-photon sample or using a simulated di-photon sample which contains additional material upstream of the calorimeter. The variations induced on the measured cross sections by the alternative corrections are taken as systematic uncertainties, due to the uncertainty on the generated kinematic distributions, on the relative fraction of direct and fragmentation di-photon production, and on the amount of material in the ATLAS detector. The effect on the total cross section is within $+2.0^-5.0\%$ for $m_{\gamma\gamma}$, $\pm3.0\%$ for $p_{T,\gamma\gamma}$, $+3.0^-4.0\%$ for $\Delta\phi_{\gamma\gamma}$ and $+2.0^-3.0\%$ for $\cos\theta_{\gamma\gamma}$.

The effect of the uncertainty on the efficiency of the photon identification criteria is estimated by varying the identification efficiency in the simulation by its uncertainty [28]. The uncertainties on the electromagnetic (photon) energy scale and resolution are also propagated to the final measurement by varying them within their uncertainties [25]. The effect on the differential cross section is typically $+1^-2\%$. Other uncertainties, related to the dependence on the average number of pile-up interactions of the efficiencies of the photon identification and transverse isolation energy requirements and to the observed data-MC shift in the photon transverse isolation energy distributions, are found to be negligible.

A closure test has been performed by unfolding the differential spectra of di-photon events selected in the PYTHIA signal sample with the bin-by-bin coefficients determined using the SHERPA sample, and comparing the unfolded spectra to the truth-level spectra in the same PYTHIA sample. Non-closure effects of at most 2% have been found and included in the final systematic uncertainty.

More sophisticated unfolding methods which account for migrations between bins, either based on the repeated (iterative) application of Bayes’ theorem [29] or on a least-square minimization followed by a regularization of the resulting spectra [30] have also been
investigated. The differences between the unfolded spectra obtained with these methods and the spectra extracted with the bin-by-bin corrections are negligible compared to the other uncertainties and therefore the bin-by-bin method was chosen for the final results.

6.2 Trigger efficiency correction

The unfolded spectra are then corrected for the event-level trigger efficiency, defined as the fraction of di-photon events — satisfying all the selection criteria — that pass the di-photon trigger used to collect the data. The trigger efficiency is measured in data using a bootstrap technique \cite{31} from samples selected with fully efficient unbiased triggers with a lower threshold, and taking into account kinematic correlations between the photon candidates. The differences between the measured di-photon trigger efficiency and the efficiency estimated with simulated di-photon samples, or by applying the bootstrap technique to single-photon triggers and neglecting correlations between the two photon candidates, have been assigned as systematic uncertainties. The total trigger efficiency is then:

\[ \varepsilon_{\text{trig}} = \left( 97.8^{+0.8}_{-1.5} \text{(stat.)} \pm 0.8 \text{(syst.)} \right) \% \] (6.1)

Using di-photon simulated samples, the trigger efficiency has been estimated to be constant, within the total uncertainties, as a function of the four di-photon observables under investigation.

6.3 Results

The differential cross sections as a function of \( m_{\gamma\gamma}, p_{T,\gamma\gamma}, \Delta \phi_{\gamma\gamma}, \text{ and } \cos \theta^*_{\gamma\gamma} \) are extracted following the unfolding procedure described in section 6.1 and using the trigger efficiency quoted in eq. (6.1). The numerical results are listed in appendix A.

The integrated cross section is measured by dividing the global \( \gamma\gamma \) yield (obtained after subtracting the electron contribution from the two-dimensional fit result in table 1) by the product of the average event selection efficiency (from the simulation), trigger efficiency and integrated luminosity. The selection efficiency is defined as the number of reconstructed simulated di-photon events satisfying the detector-level selection criteria divided by the number of generated events satisfying the equivalent truth-level criteria, thus correcting for reconstructed events with true photons failing the acceptance cuts. It is computed from simulated di-photon events, reweighting the spectrum of one of the four di-photon variables under study in order to match the differential background-subtracted di-photon spectrum observed in data. Choosing different variables for the reweighting of the simulated events leads to slightly different but consistent efficiencies, with an average value of 49.6% and an RMS of 0.2%. Including systematic uncertainties on the photon reconstruction and identification efficiencies, from the same sources described in section 6.1, the event selection efficiency is estimated to be 49.6\(^{+1.9}_{-1.7}\)%. The dominant contributions to the efficiency uncertainty are from the photon identification efficiency uncertainty (±1.2%), the energy scale uncertainty (±1.2%), and the choice of the MC generator and the detector simulation (±0.9%). Negligible uncertainties are found to arise from the energy resolution, the isolation requirement (evaluated by shifting the isolation variable by the observed data-MC...
difference) and from the different pile-up dependence of the efficiency in data and MC
simulation. With an integrated luminosity of $(4.9 \pm 0.2) \text{fb}^{-1}$ at $\sqrt{s} = 7 \text{ TeV}$, we obtain
an integrated cross section of $44.0^{+3.2}_{-4.2} \text{ pb}$, where the dominant uncertainties are the event
selection efficiency and the jet subtraction systematic uncertainties. As a cross-check, the
integrals of the one-dimensional differential cross sections are also computed. They are
consistent with the measured integrated cross section quoted above.

### 7 Comparison with theoretical predictions

The results are compared both to fixed-order NLO and NNLO calculations, obtained with
parton-level MC generators (DIPHOS+GAMMA2MC and 2\gamma NNLO), and to the generated-
particle-level di-photon spectra predicted by leading-order (LO) parton-shower MC gener-
ants used in the ATLAS full simulation (PYTHIA and SHERPA). The contribution from the
particle recently discovered by ATLAS and CMS in the search for the Standard Model
Higgs boson is not included in the predictions: it is expected to be around 1% of the
signal in the $120 < m_\gamma \gamma < 130 \text{ GeV}$ interval, and negligible elsewhere. The contribution
from multiple parton interactions is also neglected: measurements by DØ \[\text{32}\] and AT-
LAS\[\text{5}\] show that events with two jets (in $\gamma$+jets or W+jets) have a contamination between
5% and 10% from double parton interactions. In our data sample, the fraction of selected
di-photon candidates with at least two additional jets not overlapping with the photons
and not from pile-up is around 8%, thus the overall contribution to the signal from multiple
parton interactions is estimated to be lower than 1%.

The main differences between the four predictions are the following:

- **2\gamma NNLO** provides a NNLO calculation of the direct part of the di-photon production
cross section, but neglects completely the contribution from the fragmentation com-
ponent, where one or both photons are produced in the soft collinear fragmentation
of coloured partons.

- **DIPHOS** provides a NLO calculation of both the direct and the fragmentation parts of
the di-photon production cross section. It also includes the contribution from the box
diagram ($gg \rightarrow \gamma\gamma$), which is in principle a term of the NNLO expansion in the strong
coupling constant $\alpha_s$, but — due to the large gluon luminosity at the LHC \[\text{33}\] —
gives a contribution comparable to that of the LO terms. For these reasons, higher-
order contributions to the box diagrams, technically at NNNLO but of size similar
to that of NLO terms, are also included in our calculation by using GAMMA2MC.

- **PYTHIA** provides LO matrix elements for di-photon production and models the
higher-order terms through $\gamma$-jet and di-jet production in combination with initial-
state and/or final-state radiation. It also features parton showering and an underlying
event model;

\[\text{5}\] Article in preparation.
Sherpa has features similar to those of Pythia, and in addition includes the di-photon higher-order real-emission matrix elements. For this study, up to two additional QCD partons are generated.

The nominal factorization ($\mu_F$), renormalization ($\mu_R$), and — in the case of Diphox and Gamma2MC — fragmentation ($\mu_f$) scales are set in all cases to the di-photon invariant mass, $m_{\gamma\gamma}$. Different PDF sets are used by each program: CT10 NLO [34] for Diphox and Gamma2MC, MSTW2008 NNLO [35] for $2\gamma$NNLO, CTEQ6L1 for Sherpa and MRST2007 LO* for Pythia. The theoretical uncertainty error bands for Pythia and Sherpa include only statistical uncertainties. The theory uncertainty error bands for the NLO and NNLO predictions include in addition PDF and scale uncertainties. PDF uncertainties are estimated by varying each of the eigenvalues of the PDFs by $\pm 1\sigma$ and summing in quadrature separately positive and negative variations of the cross section. For Diphox and Gamma2MC, scale uncertainties are evaluated by varying each scale to $m_{\gamma\gamma}/2$ and $2m_{\gamma\gamma}$, and the envelope of all variations is taken as a systematic error; the final uncertainty is dominated by the configurations in which the scales are varied incoherently. For $2\gamma$NNLO, the scale uncertainty is evaluated by considering the variation of the predicted cross sections in the two cases $\mu_R = m_{\gamma\gamma}/2$, $\mu_F = 2m_{\gamma\gamma}$ and $\mu_R = 2m_{\gamma\gamma}$, $\mu_F = m_{\gamma\gamma}/2$.

Fixed-order predictions calculated at parton level do not include underlying event, pile-up or hadronization effects. While the ambient-energy density corrections to the photon isolation are expected to remove most of these effects from the photon isolation energy, it is not guaranteed that they correct the experimental isolation back to exactly the parton-level isolation computed from the elementary-process partons. To estimate these residual effects, Pythia and Sherpa di-photon samples are used to evaluate the ratio of generator-level cross sections with and without hadronization and the underlying event, and subsequently, the parton-level cross sections are multiplied bin-by-bin by this ratio. The central value of the envelope of the Pythia and Sherpa distributions is taken as the nominal correction and half of the difference between Pythia and Sherpa as the systematic uncertainty. The typical correction factor is around 0.95.

Both Pythia and Sherpa are expected to underestimate the total cross section, because of the missing NLO (and higher-order) contributions. At low $p_T,\gamma \gamma$ and for $\Delta \phi,\gamma \gamma$ near $\pi$ where multiple soft gluon emission is important, Pythia and Sherpa are expected to better describe the shape of the differential distributions, thanks to the effective all-order resummation of the leading logs performed by the parton shower. On the other hand, in the same regions fixed-order calculations are expected to exhibit infrared divergences. Finally, $2\gamma$NNLO is expected to underestimate the data in regions populated by the contribution from fragmentation (low $\Delta \phi,\gamma \gamma$ and $m_{\gamma\gamma}$, and $\cos \theta^*_{\gamma\gamma} \approx 1$).

The total cross section estimated by Pythia and Sherpa with the ATLAS simulation settings is 36 pb, and underestimates the measured cross section by 20%. The Diphox+Gamma2MC total cross section is $39^{+7}_{-6}$ pb and the $2\gamma$NNLO total cross section is $44^{+6}_{-5}$ pb, where the uncertainty is dominated by the choice of the nominal scales.

The comparisons between the experimental cross sections and the predictions by Pythia and Sherpa are shown in figure 4. In order to compare the shapes of the MC
differential distributions to the data, their cross sections are rescaled by a factor 1.2 to match the total cross section measured in data. PYTHIA misses higher order contributions, as clearly seen for low values of $\Delta \phi_{\gamma\gamma}$, but this is compensated by the parton shower for $\Delta \phi_{\gamma\gamma}$ near $\pi$ and at low $p_{T,\gamma\gamma}$. It is worth noting that the shoulder expected (and observed) in the $p_{T,\gamma\gamma}$ cross section around the sum of the $E_T$ thresholds of the two photons [36] is almost absent in PYTHIA, while SHERPA correctly reproduces the data in this region. This is interpreted as being due to the additional NLO contributions in SHERPA combined with differences in the parton showers. Overall, SHERPA reproduces the data rather well, except at large $m_{\gamma\gamma}$ and large $|\cos \theta^{*}_{\gamma\gamma}|$.

The comparisons between the data cross sections and the predictions by $2\gamma$NNLO and DIPHOX+GAMMA2MC are shown in figure 5. In the $\Delta \phi_{\gamma\gamma} \simeq \pi$, low $p_{T,\gamma\gamma}$ region, DIPHOX+GAMMA2MC fails to match the data. This is expected because initial-state soft gluon radiation is divergent at NLO, without soft gluon resummation. Everywhere else DIPHOX+GAMMA2MC is missing NNLO contributions and clearly underestimates the data.

With higher order calculations included, $2\gamma$NNLO is very close to the data within the uncertainties. However, the excess at $\Delta \phi_{\gamma\gamma} \simeq \pi$ and low $p_{T,\gamma\gamma}$ is still present, as expected for a fixed-order calculation. Since the fragmentation component is not calculated in $2\gamma$NNLO, the data is slightly underestimated by $2\gamma$NNLO in the regions where this component is larger: at low $\Delta \phi_{\gamma\gamma}$, low mass, intermediate $p_{T,\gamma\gamma}$ (between 20 GeV and 150 GeV) and large $|\cos \theta^{*}_{\gamma\gamma}|$.

8 Conclusion

A measurement of the production cross section of isolated-photon pairs in $pp$ collisions at a centre-of-mass energy $\sqrt{s} = 7$ TeV is presented. The measurement uses an integrated luminosity of 4.9 fb$^{-1}$ collected by the ATLAS detector at the LHC in 2011. The two photons are required to be isolated in the calorimeters, to be in the acceptance of the electromagnetic calorimeter ($|\eta| < 2.37$ with the exclusion of the barrel-endcap transition region $1.37 < |\eta| < 1.52$) and to have an angular separation $\Delta R > 0.4$ in the $\eta, \phi$ plane. Both photons have transverse energies $E_T > 22$ GeV, and at least one of them has $E_T > 25$ GeV.

The total cross section within the acceptance is $44.0^{+3.2}_{-4.2}$ pb. It is underestimated by SHERPA and PYTHIA, which both predict a value of 36 pb with the current ATLAS simulation tune. The central value of the cross section predicted by DIPHOX+GAMMA2MC, 39 pb, is lower than the data but it is consistent with data within the theoretical ($^{+7}_{-6}$ pb) and experimental errors. The NNLO calculation of $2\gamma$NNLO ($\sigma_{\text{NNLO}} = 44^{+6}_{-5}$ pb) is in excellent agreement with the data.

The differential cross sections, as a function of the di-photon invariant mass, transverse momentum, azimuthal separation and of the cosine of the polar angle of the photon with largest transverse energy in the Collins-Soper di-photon rest frame, are also measured. Rather good agreement is found with Monte Carlo generators, after rescaling the PYTHIA and SHERPA distributions by a factor 1.2 in order to match the integrated cross section measured in data and fixed-order calculations, in the regions of phase space studied. All generators tend to underestimate the data at large $|\cos \theta^{*}_{\gamma\gamma}|$. SHERPA performs rather
Figure 4. Comparison between the experimental cross sections and the predictions obtained with parton-shower LO simulations: $m_{\gamma\gamma}$ (top left), $p_{T,\gamma\gamma}$ (top right), $\Delta\phi_{\gamma\gamma}$ (bottom left), $\cos\theta_{\gamma\gamma}^*$ (bottom right). The LO cross sections have been scaled to the total data cross section, by a factor 1.2. Black dots correspond to data with error bars for their total uncertainties, which are dominated by the systematic component. The simulated cross sections include only statistical uncertainties.
well for most differential spectra, except for high $m_{\gamma\gamma}$. Pythia is missing higher order contributions, but this is compensated by the parton shower for $\Delta \phi_{\gamma\gamma}$ near $\pi$ and at low $p_{T,\gamma\gamma}$. In these same regions the fixed-order calculations do not reproduce the data, due to the known infrared divergences from initial-state soft gluon radiation. Everywhere else Diphox+Gamma2MC is missing NNLO contributions and clearly underestimates the data. On the other hand, with inclusion of NNLO terms, $2\gamma$NNLO is able to match the data very closely within the uncertainties, except in limited regions where the fragmentation component — neglected in the $2\gamma$NNLO calculation — is still significant after the photon isolation requirement.

Acknowledgments

We thank the $2\gamma$NNLO authors for providing theoretical predictions of the NNLO diphoton cross section based on their code. We thank Leandro Cieri, Stefano Catani, Daniel De Florian, Michel Fontannaz, Jean-Philippe Guillet, Eric Pilon and Carl Schmidt, for fruitful discussions on the theoretical calculations and their uncertainties.

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A  Experimental differential cross section

The numerical values of the differential cross sections displayed in figures 4 and 5 are quoted in tables 2–5. For each bin of the $m_{\gamma\gamma}$, $p_{T,\gamma\gamma}$, $\Delta \phi_{\gamma\gamma}$, and $\cos \theta_{\gamma\gamma}$ variables, the
The listed total errors are the quadratic sum of statistical and systematic uncertainties. All values are divided by the bin width.

<table>
<thead>
<tr>
<th>$m_{\gamma\gamma}$ [GeV]</th>
<th>$d\sigma/dm_{\gamma\gamma}$ [pb/GeV]</th>
<th>Statistical error</th>
<th>Systematic errors</th>
<th>Total error</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>high</td>
<td>low</td>
<td>high</td>
<td>low</td>
</tr>
<tr>
<td>[0, 20)</td>
<td>0.0247</td>
<td>+0.0015</td>
<td>−0.0015</td>
<td>+0.0032</td>
</tr>
<tr>
<td>[20, 30)</td>
<td>0.0704</td>
<td>+0.0032</td>
<td>−0.0032</td>
<td>+0.0087</td>
</tr>
<tr>
<td>[30, 40)</td>
<td>0.091</td>
<td>+0.004</td>
<td>−0.004</td>
<td>+0.011</td>
</tr>
<tr>
<td>[40, 50)</td>
<td>0.252</td>
<td>+0.006</td>
<td>−0.006</td>
<td>+0.025</td>
</tr>
<tr>
<td>[50, 60)</td>
<td>0.880</td>
<td>+0.012</td>
<td>−0.012</td>
<td>+0.073</td>
</tr>
<tr>
<td>[60, 70)</td>
<td>0.857</td>
<td>+0.010</td>
<td>−0.010</td>
<td>+0.071</td>
</tr>
<tr>
<td>[70, 80)</td>
<td>0.626</td>
<td>+0.008</td>
<td>−0.008</td>
<td>+0.051</td>
</tr>
<tr>
<td>[80, 90)</td>
<td>0.384</td>
<td>+0.008</td>
<td>−0.008</td>
<td>+0.049</td>
</tr>
<tr>
<td>[90, 100)</td>
<td>0.305</td>
<td>+0.006</td>
<td>−0.006</td>
<td>+0.031</td>
</tr>
<tr>
<td>[100, 110)</td>
<td>0.212</td>
<td>+0.004</td>
<td>−0.004</td>
<td>+0.021</td>
</tr>
<tr>
<td>[110, 120)</td>
<td>0.148</td>
<td>+0.004</td>
<td>−0.004</td>
<td>+0.015</td>
</tr>
<tr>
<td>[120, 130)</td>
<td>0.122</td>
<td>+0.003</td>
<td>−0.003</td>
<td>+0.015</td>
</tr>
<tr>
<td>[130, 140)</td>
<td>0.0829</td>
<td>+0.0025</td>
<td>−0.0025</td>
<td>+0.0112</td>
</tr>
<tr>
<td>[140, 150)</td>
<td>0.0656</td>
<td>+0.0022</td>
<td>−0.0022</td>
<td>+0.0088</td>
</tr>
<tr>
<td>[150, 160)</td>
<td>0.0535</td>
<td>+0.0019</td>
<td>−0.0019</td>
<td>+0.0072</td>
</tr>
<tr>
<td>[160, 170)</td>
<td>0.0451</td>
<td>+0.0017</td>
<td>−0.0017</td>
<td>+0.0063</td>
</tr>
<tr>
<td>[170, 180)</td>
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<td>+0.0015</td>
<td>−0.0015</td>
<td>+0.0050</td>
</tr>
<tr>
<td>[180, 190)</td>
<td>0.0262</td>
<td>+0.0013</td>
<td>−0.0013</td>
<td>+0.0032</td>
</tr>
<tr>
<td>[190, 200)</td>
<td>0.0209</td>
<td>+0.0011</td>
<td>−0.0011</td>
<td>+0.0025</td>
</tr>
<tr>
<td>[200, 225)</td>
<td>0.0149</td>
<td>+0.0006</td>
<td>−0.0006</td>
<td>+0.0023</td>
</tr>
<tr>
<td>[225, 250)</td>
<td>0.00970</td>
<td>+0.00049</td>
<td>−0.00049</td>
<td>+0.00150</td>
</tr>
<tr>
<td>[250, 275)</td>
<td>0.00616</td>
<td>+0.00039</td>
<td>−0.00039</td>
<td>+0.00104</td>
</tr>
<tr>
<td>[275, 300)</td>
<td>0.00464</td>
<td>+0.00036</td>
<td>−0.00036</td>
<td>+0.00080</td>
</tr>
<tr>
<td>[300, 350)</td>
<td>0.00235</td>
<td>+0.00017</td>
<td>−0.00017</td>
<td>+0.00048</td>
</tr>
<tr>
<td>[350, 400)</td>
<td>0.00116</td>
<td>+0.00011</td>
<td>−0.00011</td>
<td>+0.00024</td>
</tr>
<tr>
<td>[400, 500)</td>
<td>4.69 e−04</td>
<td>+5.0 e−05</td>
<td>−5.0 e−05</td>
<td>+7.9 e−05</td>
</tr>
<tr>
<td>[500, 800)</td>
<td>8.6 e−05</td>
<td>+1.3 e−05</td>
<td>−1.3 e−05</td>
<td>+1.5 e−05</td>
</tr>
</tbody>
</table>

**Table 2.** Experimental cross-section values per bin in pb/GeV for $m_{\gamma\gamma}$. The listed total errors are the quadratic sum of statistical and systematic uncertainties.
\begin{table}[h]
\centering
\begin{tabular}{|c|c|c|c|c|c|c|c|}
\hline
$\pt_{\gamma\gamma}$ & d$\sigma$/d$\pt_{\gamma\gamma}$ & Statistical error & Systematic errors & Total error \\
\hline
[0, 2) & 0.727 & $+0.022$ & $-0.022$ & $+0.057$ & $-0.092$ & $+0.061$ & $-0.094$ \\
[2, 4) & 1.75 & $+0.04$ & $-0.04$ & $+0.13$ & $-0.23$ & $+0.13$ & $-0.23$ \\
[4, 6) & 2.03 & $+0.04$ & $-0.04$ & $+0.15$ & $-0.23$ & $+0.15$ & $-0.23$ \\
[6, 8) & 1.88 & $+0.04$ & $-0.04$ & $+0.15$ & $-0.21$ & $+0.16$ & $-0.21$ \\
[8, 10) & 1.72 & $+0.03$ & $-0.03$ & $+0.13$ & $-0.19$ & $+0.14$ & $-0.19$ \\
[10, 12) & 1.40 & $+0.03$ & $-0.03$ & $+0.12$ & $-0.16$ & $+0.12$ & $-0.16$ \\
[12, 14) & 1.28 & $+0.03$ & $-0.03$ & $+0.10$ & $-0.13$ & $+0.11$ & $-0.13$ \\
[14, 16) & 1.122 & $+0.026$ & $-0.026$ & $+0.093$ & $-0.114$ & $+0.097$ & $-0.117$ \\
[16, 18) & 0.999 & $+0.024$ & $-0.024$ & $+0.086$ & $-0.090$ & $+0.090$ & $-0.093$ \\
[18, 20) & 0.810 & $+0.021$ & $-0.021$ & $+0.072$ & $-0.076$ & $+0.075$ & $-0.079$ \\
[20, 25) & 0.674 & $+0.012$ & $-0.012$ & $+0.056$ & $-0.074$ & $+0.058$ & $-0.075$ \\
[25, 30) & 0.492 & $+0.011$ & $-0.011$ & $+0.041$ & $-0.045$ & $+0.043$ & $-0.047$ \\
[30, 35) & 0.405 & $+0.009$ & $-0.009$ & $+0.034$ & $-0.043$ & $+0.035$ & $-0.044$ \\
[35, 40) & 0.325 & $+0.009$ & $-0.009$ & $+0.028$ & $-0.034$ & $+0.030$ & $-0.035$ \\
[40, 45) & 0.272 & $+0.008$ & $-0.008$ & $+0.023$ & $-0.027$ & $+0.024$ & $-0.028$ \\
[45, 50) & 0.282 & $+0.008$ & $-0.008$ & $+0.023$ & $-0.027$ & $+0.024$ & $-0.028$ \\
[50, 55) & 0.235 & $+0.007$ & $-0.007$ & $+0.023$ & $-0.025$ & $+0.025$ & $-0.026$ \\
[55, 60) & 0.194 & $+0.006$ & $-0.006$ & $+0.019$ & $-0.024$ & $+0.021$ & $-0.024$ \\
[60, 65) & 0.150 & $+0.006$ & $-0.006$ & $+0.015$ & $-0.016$ & $+0.016$ & $-0.017$ \\
[65, 70) & 0.102 & $+0.005$ & $-0.005$ & $+0.013$ & $-0.012$ & $+0.014$ & $-0.013$ \\
[70, 75) & 0.0836 & $+0.0041$ & $-0.0041$ & $+0.0103$ & $-0.0087$ & $+0.0111$ & $-0.0096$ \\
[75, 80) & 0.0748 & $+0.0036$ & $-0.0036$ & $+0.0087$ & $-0.0086$ & $+0.0094$ & $-0.0093$ \\
[80, 90) & 0.0521 & $+0.0021$ & $-0.0021$ & $+0.0059$ & $-0.0056$ & $+0.0063$ & $-0.0059$ \\
[90, 100) & 0.0381 & $+0.0017$ & $-0.0017$ & $+0.0043$ & $-0.0036$ & $+0.0047$ & $-0.0040$ \\
[100, 110) & 0.0239 & $+0.0013$ & $-0.0013$ & $+0.0028$ & $-0.0023$ & $+0.0031$ & $-0.0026$ \\
[110, 120) & 0.0175 & $+0.0011$ & $-0.0011$ & $+0.0024$ & $-0.0016$ & $+0.0027$ & $-0.0019$ \\
[120, 130) & 0.0106 & $+0.0009$ & $-0.0009$ & $+0.0015$ & $-0.0011$ & $+0.0017$ & $-0.0014$ \\
[130, 140) & 0.0090 & $+0.0008$ & $-0.0008$ & $+0.0012$ & $-0.0008$ & $+0.0015$ & $-0.0012$ \\
[140, 150) & 0.00646 & $+0.00064$ & $-0.00064$ & $+0.00089$ & $-0.00063$ & $+0.00110$ & $-0.00090$ \\
[150, 175) & 0.00333 & $+0.00031$ & $-0.00031$ & $+0.00047$ & $-0.00039$ & $+0.00056$ & $-0.00049$ \\
[175, 200) & 0.00195 & $+0.00023$ & $-0.00023$ & $+0.00025$ & $-0.00017$ & $+0.00034$ & $-0.00028$ \\
[200, 250) & 0.00077 & $+0.00010$ & $-0.00010$ & $+0.00012$ & $-0.00008$ & $+0.00016$ & $-0.00013$ \\
[250, 500) & $1.18e-04$ & $+1.7e-05$ & $-1.7e-05$ & $+1.8e-05$ & $-1.2e-05$ & $+2.5e-05$ & $-2.1e-05$ \\
\hline
\end{tabular}
\caption{Experimental cross-section values per bin in pb/GeV for $\pt_{\gamma\gamma}$. The listed total errors are the quadratic sum of statistical and systematic uncertainties.}
\end{table}
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<tr>
<th>$\Delta \phi_{\gamma\gamma}$</th>
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<th>Systematic errors</th>
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<td>high</td>
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<td>−0.09</td>
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<td>−0.09</td>
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Table 4. Experimental cross-section values per bin in pb/rad for $\Delta \phi_{\gamma\gamma}$. The listed total errors are the quadratic sum of statistical and systematic uncertainties.
Figure 5. Comparison between the experimental cross sections and the predictions obtained with DIPHOX+GAMMA2MC (NLO) and 2\gamma NNLO (NNLO): \(m_{\gamma\gamma}\) (top left), \(p_{T,\gamma\gamma}\) (top right), \(\Delta\phi_{\gamma\gamma}\) (bottom left), \(\cos\theta^*_{\gamma\gamma}\) (bottom right). Black dots correspond to data with error bars for their total uncertainties, which are dominated by the systematic component. The theoretical uncertainties include contributions from the limited size of the simulated sample, from the scale choice and from uncertainties on the parton distribution functions and on the hadronization and underlying event corrections.
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</table>

Table 5. Experimental cross-section values per bin in pb for $\cos\theta^*_\gamma$. The listed total errors are the quadratic sum of statistical and systematic uncertainties.
References


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