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Measurement of the production of a $W$ boson in association with a charmed hadron in $pp$ collisions at $\sqrt{s}=13$ TeV with the ATLAS detector

G. Aad et al. (ATLAS Collaboration)

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I. INTRODUCTION

Parton distribution functions (PDFs) describe the momentum distributions of quarks and gluons inside nucleons. Currently, only limited information is available about the PDF of strange quarks in the proton. The sea distributions for the three light quarks, up, down, and strange, might be equal due to flavor SU(3) symmetry; alternatively the strange quark distribution might be suppressed due to its equal due to flavor SU(3) symmetry; alternatively the PDF of strange quarks in the proton. The sea distributions currently, only limited information is available about the PDF of strange quarks in the proton. The sea distributions of quarks and gluons inside nucleons.

In perturbative quantum chromodynamics (QCD), the production of a $W$ boson in association with a single charm quark occurs through the scattering of a gluon and a down-type quark, i.e. down, strange, or bottom, at leading order (LO), as shown in Fig. 1. The relative contributions to the cross section of $W+c$ production from each of the three different quarks depends on their PDFs and on the values of the three relevant terms from the Cabibbo-Kobayashi-Maskawa (CKM) mixing matrix [13,14]: $V_{cd}$, $V_{cs}$, and $V_{cb}$. At the LHC, the process $gs \rightarrow W^-c$ and its charge conjugate are dominant, while the process $gd \rightarrow W^-c$ ($gd \rightarrow W^+\bar{c}$) contributes only $\sim 10\%$ ($\sim 5\%$) to the $W^-c$ ($W^+\bar{c}$) rate. The difference between the $d$ and $\bar{d}$ contributions can be attributed to the presence of valence $d$-quarks [15]. The contribution from $b$-quark-initiated processes is negligible. The largest next-to-leading-order (NLO) contributions are the one-gluon-loop corrections to $gs \rightarrow W^-c$ ($gs \rightarrow W^+\bar{c}$); however, various other partonic initial states such as $q\bar{q}'$, $gg$, and $q\bar{q}$ or $\bar{q}q$ are also present.

The idea of using $W+c$ events to measure the strange PDF was first proposed in Refs. [16,17] and their production was first observed at the Tevatron [18]. At the LHC, it has been measured both by ATLAS and CMS using data.
taken at \(\sqrt{s} = 7\) TeV [19–21] and by CMS using data taken at \(\sqrt{s} = 8\) and 13 TeV [22,23]. Measurements of \(W + c\) production in the forward region at \(\sqrt{s} = 7\) and 8 TeV have also been performed by the LHCb Collaboration [24]. In these measurements, the charm quark or anticharm is tagged either by the presence of a jet of particles containing a secondary vertex or a semileptonic decay to a muon, or by explicit reconstruction of a \(D^+\) or \(D^{+*}\) meson or its charge conjugate, collectively written as \(D^{(*)}\).

This paper presents a measurement of \(W\) boson production in association with a \(D^{(*)}\) meson using 140 fb\(^{-1}\) of \(\sqrt{s} = 13\) TeV proton-proton (\(pp\)) collision data recorded by the ATLAS detector at the LHC. Events in which the \(W\) boson decays to an electron or a muon (and the associated neutrino) are studied and the presence of the charm quark is detected through explicit charmed hadron reconstruction. The measurement does not require the presence of a reconstructed jet. The production of charmed hadrons is studied using the following decay modes (and their charge conjugates):

(i) \(D^+ \to K^-\pi^+\pi^+\) and

(ii) \(D^{+*} \to D^0\pi^+ \to (K^-\pi^+)\pi^+\).

The signal \(W + D^{(*)}\) events are extracted through a profile likelihood [25] fit to the reconstructed secondary-vertex mass distribution for the \(D^+\) and the mass difference \(m(D^{+*} - D^0)\) for the \(D^{+*}\). The main backgrounds are single-\(W\)-boson events that do not contain the requisite \(D^{(*)}\) decays and \(t\bar{t}\) events.

In \(W + c\) production, at LO the \(W\) boson and charm quark always have opposite-sign electric charges, i.e., either \(W^+ + \bar{c}\) or \(W^- + c\). For those processes where one of the initial-state partons is a strange or antistrange quark, this charge correlation remains at NLO and next-to-next-to-leading order (NNLO) [15]. However, many of the backgrounds (e.g. heavy-flavor pair production or \(b\)-hadron production from \(t\bar{t}\) events) have equal rates for the production of leptons and \(D^{(*)}\) with opposite-sign (OS) or same-sign (SS) charges. This is exploited in the analysis by extracting the signal as the difference of the numbers of OS and SS candidates denoted by OS–SS, and extrapolating the background estimate from SS candidates. The \(t\bar{t}\) background with events containing \(W \to cs\) decays is not charge symmetric and is measured \textit{in situ} by categorizing the events according to whether \(b\)-tagged jets separated in phase space from the \(D^{(*)}\) candidate are present.

The \(W + D^{(*)}\) cross sections, \(\sigma_{\text{fid}}^{\text{OS-SS}}(W + D^{(*)})\), are measured in a fiducial region defined by requirements for \(W\) boson and \(D^{(*)}\) meson selection. The requirements for \(W\) boson selection are a charged lepton, \(e\) (or \(\mu\)), of transverse momentum \(p_T > 30\) GeV and pseudorapidity \(|\eta| < 2.5\). The requirements for \(D^{(*)}\) meson selection are \(p_T(D^{(*)}) > 8\) GeV and \(|\eta(D^{(*)})| < 2.2\). The total fiducial cross section is presented along with two differential cross sections, in \(p_T(D^{(*)})\) and \(|\eta(D^{(*)})|\). The measurements are performed separately for events with positively and negatively charged \(W\) bosons and the ratio \(R^c_\text{fid} \equiv \sigma_{\text{fid}}^{\text{OS-SS}}(W^+ + D^-)/\sigma_{\text{fid}}^{\text{OS-SS}}(W^- + D^+)\) is also presented. These measurements are compared with QCD predictions obtained using state-of-the-art PDF sets [9,12,26–31].

An important development in the theoretical study of \(W + c\) production is the recent publication of the first NNLO calculation [32] of the process. This calculation includes an off-shell treatment of the \(W\) boson and is performed in a five-flavor scheme using the infrared- and collinear-safe flavored \(k_t\) algorithm [33] and neglecting \(c\)-quark finite-mass effects. Nondiagonal CKM matrix elements and the dominant NLO electroweak (EW) corrections are included. Scale uncertainties obtained using this calculation are below 2%, significantly smaller than PDF uncertainties for most PDF set choices. Such NNLO calculations will ultimately allow the incorporation of \(W + c\) measurements into NNLO PDF fits. For \(W + c\)-jet measurements, comparisons with NNLO predictions require that cross sections be unfolded to jet observables calculated in the flavored \(k_t\) scheme; such unfolded results are not currently available. Alternatively, in the case of \(W + D^{(*)}\) measurements, the charm fragmentation function could in the future be incorporated into theory predictions using methods pioneered in Ref. [34].

\[\begin{align*}  
\text{FIG. 1. The leading-order diagrams for } W^- + c \text{ production.} 
\end{align*}\]
The measurements presented here are compared with QCD calculations with NLO plus parton-shower accuracy. The baseline framework for these calculations and the QCD scale uncertainties associated with them is MadGraph5_aMC@NLO [35]. Theoretical uncertainties associated with the choice of matching scheme are assessed using the difference between predictions obtained with MadGraph5_aMC@NLO and those obtained with recent calculations [36] implemented in the Powheg event generator [37].

This paper is structured as follows. Section II introduces the ATLAS detector. The data and Monte Carlo simulation samples used in the analysis are discussed in Sec. III. Section IV describes the physics objects used in the analysis and their selection criteria. The reconstruction and selection of charmed mesons are discussed in Sec. V. The event selection is summarized in Sec. VI. Signal and background modeling are described in Sec. VII. Section VIII presents the method used to extract the \( W + D^{(*)} \) differential cross section and Sec. IX summarizes the relevant systematic uncertainties. The cross-section measurements and their comparison with theoretical predictions are presented in Sec. X. Conclusions are provided in Sec. XI.

II. THE ATLAS DETECTOR

The ATLAS detector [38] at the LHC covers nearly the entire solid angle around the collision point.\(^2\) It consists of an inner tracking detector surrounded by a thin superconducting solenoid, electromagnetic and hadron calorimeters, and a muon spectrometer incorporating three large superconducting air-core toroidal magnets.

The inner-detector system (ID) is immersed in a 2 T axial magnetic field and provides charged-particle tracking in the range \( |\eta| < 2.5 \). The high-granularity silicon pixel detector covers the vertex region and typically provides four measurements per track, the first hit normally being in the insertable B-layer (IBL) installed before Run 2 [39,40]. It is followed by the silicon microstrip tracker, which usually provides eight measurements per track. These silicon detectors are complemented by the transition radiation tracker (TRT), which enables radially extended track reconstruction up to \( |\eta| = 2.0 \). The TRT also provides electron identification information based on the fraction of hits (typically 30 in total) above a higher energy-deposit threshold corresponding to transition radiation.

\[^2\text{ATLAS uses a right-handed coordinate system with its origin at the nominal interaction point (IP) in the center of the detector and the z-axis along the beam pipe. The x-axis points from the IP to the center of the LHC ring, and the y-axis points upward. Cylindrical coordinates } (r, \phi) \text{ are used in the transverse plane, } \phi \text{ being the azimuthal angle around the z-axis. The pseudorapidity is defined in terms of the polar angle } \theta \text{ as } \eta = -\ln(\tan(\theta/2)). \text{ Angular distance is measured in units of } \Delta R = \sqrt{(\Delta \eta)^2 + (\Delta \phi)^2}.\]

The calorimeter system covers the pseudorapidity range \( |\eta| < 4.9 \). Within the region \( |\eta| < 3.2 \), electromagnetic calorimetry is provided by barrel and end cap high-granularity lead/liquid-argon (LAr) calorimeters, with an additional thin LAr presampler covering \( |\eta| < 1.8 \) to correct for energy loss in material upstream of the calorimeters. Hadron calorimetry is provided by the steel/scintillator-tile calorimeter, segmented into three barrel structures within \( |\eta| < 1.7 \), and two copper/LAr hadron end cap calorimeters. The solid angle coverage is completed with forward copper/LAr and tungsten/LAr calorimeter modules optimized for electromagnetic and hadronic energy measurements, respectively.

The muon spectrometer (MS) comprises separate trigger and high-precision tracking chambers measuring the deflection of muons in a magnetic field generated by the superconducting air-core toroidal magnets. The field integral of the toroids ranges between 2.0 and 6.0 T m across most of the detector. Three layers of precision chambers cover the region \( |\eta| < 2.7 \). They consist of layers of monitored drift tubes, complemented by cathode-strip chambers in the forward region, where the background is highest. The muon trigger system covers the range \( |\eta| < 2.4 \) with resistive-plate chambers in the barrel, and thin-gap chambers in the end cap regions.

Interesting events are selected by the first-level trigger system implemented in custom hardware, followed by selections made by algorithms implemented in software in the high-level trigger [41]. The first-level trigger accepts events from the 40 MHz bunch crossings at a rate below 100 kHz, which the high-level trigger further reduces in order to record events to disk at about 1 kHz.

An extensive software suite [42] is used in data simulation, in the reconstruction and analysis of real and simulated data, in detector operations, and in the trigger and data acquisition systems of the experiment.

III. DATA AND MONTE CARLO SAMPLES

A. Dataset description

Events are selected from \( \sqrt{s} = 13 \) TeV pp collision data collected by ATLAS in the period between 2015 and 2018 (Run 2 of the LHC). After data quality requirements [43] are applied to ensure that all detector components are in good working condition, the dataset amounts to an integrated luminosity of 140 fb\(^{-1}\). The uncertainty in the combined 2015–2018 integrated luminosity is 0.83% [44] obtained using the LUCID-2 detector [45] for the primary luminosity measurements, complemented by measurements using the inner detector and calorimeters. The absolute luminosity scale was determined using van der Meer scans during dedicated running periods in each year and extrapolated to physics data-taking using complementary measurements from several luminosity-sensitive detectors.
Events were recorded by either single-electron or single-muon triggers. The minimum $p_T$ threshold ranged during data-taking from 24 to 26 GeV for electrons and from 20 to 26 GeV for muons. Triggers with low $p_T$ thresholds, below 60 GeV for electrons and below 50 GeV for muons, include isolation requirements. For electrons, the requirement is $p_T^{\text{iso}}(\Delta R_{\text{var}} < 0.2)/p_T < 0.10$, where $p_T^{\text{iso}}(\Delta R_{\text{var}} < 0.2)$ is the scalar sum of transverse momenta of additional nearby tracks within a variable-size cone, $\Delta R_{\text{var}}$, around the electron. The cone size has a maximum value of 0.2 and decreases as a function of the electron’s $p_T$ as 10 GeV/$p_T$(GeV) [46]. The muon isolation criterion is constructed by summing the $p_T$ of ID tracks with $p_T^{\text{trk}} > 1$ GeV around the muon candidate satisfying $\Delta z < 6$ mm, with $\Delta z$ being the distance of the track from the primary vertex in the $z$-direction. This cut was found to be inefficient in events with high pile-up in 2017 and was tightened to $\Delta z < 2$ mm, which allowed the loosening of the isolation criterion for data-taking in 2018. The muon isolation cut is then defined as $p_T^{\text{iso}}(\Delta z)/p_T < 0.07$, where $p_T^{\text{iso}}(\Delta z)$ is the scalar sum of transverse momenta of additional nearby tracks [47]. Triggers with higher $p_T$ thresholds of 60 and 140 GeV for electrons and 50 GeV for muons are added to increase the selection efficiency.

B. Simulated event samples for signal and background modeling

Monte Carlo (MC) simulations are used to model the signal and all backgrounds except multijet. Samples produced with various MC generators are processed using a full detector simulation [48] based on GEANT4 [49] and then reconstructed using the same algorithms as the data. The effect of multiple interactions in the same and neighboring bunch crossings (pile-up) is modeled by overlaying each simulated hard-scattering event with inelastic $pp$ events generated with PYTHIA 8.186 [50] using the NNPDF2.3LO set of PDFs [51] and a set of tuned parameters called the A3 tune [52]. The MC events are weighted to reproduce the distribution of the average number of interactions per bunch crossing ($\langle \mu \rangle$) observed in the data, scaled up by a factor of $1.03 \pm 0.04$ to improve agreement between data and simulation in the visible inelastic $pp$ cross section [53]. A reweighting procedure is applied to all MC samples to correct the charmed hadron production fractions to the world-average values [54,55]. The change in the individual charmed meson production fractions is as large as 20%, depending on the MC configuration. An overview of all signal and background processes and the generators used to model them is given in Table I, and further information about the relevant generators configurations is provided below. Processes with more than one jet, known as multileg processes, can have different numbers of jets in each event. To improve the accuracy of calculations, samples with different jet multiplicities are often merged. In such multileg samples, the QCD accuracy for each jet multiplicity is specified in the table.

<table>
<thead>
<tr>
<th>Process</th>
<th>ME generator</th>
<th>QCD accuracy</th>
<th>ME PDF</th>
<th>PS generator</th>
<th>UE tune</th>
<th>HF decay</th>
</tr>
</thead>
<tbody>
<tr>
<td>W + jets (background modeling)</td>
<td>Sherpa 2.2.11</td>
<td>0–2j@NLO + 3–5j@LO</td>
<td>NNPDF3.0NNLO</td>
<td>Sherpa</td>
<td>Default</td>
<td>Sherpa</td>
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<tr>
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<td>aMC@NLO (CKKW-L)</td>
<td>0–4j@LO</td>
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<td>PYTHIA 8</td>
<td>A14</td>
<td>EvtGen</td>
</tr>
<tr>
<td>W + jets</td>
<td>aMC@NLO (FxFx)</td>
<td>0–3j@NLO</td>
<td>NNPDF3.1NNLO_LUXQED</td>
<td>PYTHIA 8</td>
<td>A14</td>
<td>EvtGen</td>
</tr>
<tr>
<td>W + $D^{(*)}$ (signal modeling and theory predictions)</td>
<td>Sherpa 2.2.11</td>
<td>0–1j@NLO + 2j@LO</td>
<td>NNPDF3.0NNLO</td>
<td>Sherpa</td>
<td>Default</td>
<td>EvtGen</td>
</tr>
<tr>
<td>W + $D^{(*)}$</td>
<td>aMC@NLO (NLO)</td>
<td>NLO</td>
<td>NNPDF3.0NNLO</td>
<td>PYTHIA 8</td>
<td>A14</td>
<td>EvtGen</td>
</tr>
<tr>
<td>W + $D^{(*)}$</td>
<td>aMC@NLO (FxFx)</td>
<td>0–3j@NLO</td>
<td>NNPDF3.1NNLO_LUXQED</td>
<td>PYTHIA 8</td>
<td>A14</td>
<td>EvtGen</td>
</tr>
</tbody>
</table>

Backgrounds

<table>
<thead>
<tr>
<th>Process</th>
<th>ME generator</th>
<th>QCD accuracy</th>
<th>ME PDF</th>
<th>PS generator</th>
<th>UE tune</th>
<th>HF decay</th>
</tr>
</thead>
<tbody>
<tr>
<td>$Z$ + jets</td>
<td>Sherpa 2.2.11</td>
<td>0–2j@NLO + 3–5j@LO</td>
<td>NNPDF3.0NNLO</td>
<td>Sherpa</td>
<td>Default</td>
<td>Sherpa</td>
</tr>
<tr>
<td>$t\bar{t}$</td>
<td>POWHEG BOX v2</td>
<td>NLO</td>
<td>NNPDF3.0NNLO</td>
<td>PYTHIA 8</td>
<td>A14</td>
<td>EvtGen</td>
</tr>
<tr>
<td>Single-$t$, $Wt$</td>
<td>POWHEG BOX v2</td>
<td>NLO</td>
<td>NNPDF3.0NNLO</td>
<td>PYTHIA 8</td>
<td>A14</td>
<td>EvtGen</td>
</tr>
<tr>
<td>Single-$t$, $t$-channel</td>
<td>POWHEG BOX v2</td>
<td>NLO</td>
<td>NNPDF3.0NNLO</td>
<td>PYTHIA 8</td>
<td>A14</td>
<td>EvtGen</td>
</tr>
<tr>
<td>Single-$t$, $s$-channel</td>
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<td>NNPDF3.0NNLO</td>
<td>PYTHIA 8</td>
<td>A14</td>
<td>EvtGen</td>
</tr>
<tr>
<td>$t\bar{t}V$</td>
<td>aMC@NLO</td>
<td>NLO</td>
<td>NNPDF3.0NNLO</td>
<td>PYTHIA 8</td>
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<td>EvtGen</td>
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<tr>
<td>Diboson fully leptonic</td>
<td>Sherpa 2.2.2</td>
<td>0–1j@NLO + 2–3j@LO</td>
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<tr>
<td>Diboson hadronic</td>
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<td>Default</td>
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</tr>
</tbody>
</table>
1. Background $V + \text{jets}$ samples

Three generator configurations are used to model inclusive vector boson ($W$ or $Z$) plus jet production. These samples are used to estimate the $W + D^{(*)}$ backgrounds and the corresponding experimental and theory systematic uncertainties.

Sherpa: The nominal MC generator used for this analysis is Sherpa 2.2.11 [56]. NLO-accurate matrix elements (ME) for up to two partons, and LO-accurate matrix elements for between three and five partons, are calculated in the five-flavor scheme using the Comix [57] and OpenLoops [58–60] libraries. The $b$- and $c$-quarks are treated as massless at matrix-element level and massive in the parton shower. The Hessian NNPDF3.0NNLO PDF set [61] is used. The default matrix-element level and massive in the parton shower. The calculation uses a five-flavor scheme with massless $b$-quarks at the matrix-element level, and massive $c$-quarks in the PYTHIA 8 shower. At the event-generation level, the jet transverse momentum is required to be at least 10 GeV, with no restriction on the absolute value of the jet pseudorapidity. The PDF set used for event generation is NNPDF3.1NNLO_LUXQED. The merging scale is set to $Q_{\text{cut}} = 20$ GeV. Scale variations where $\mu_i$ and $\mu_f$ are varied independently by a factor of 2 or 0.5 in the matrix element are included as generator event weights. The decays of bottom and charmed hadrons are performed by EvtGen 1.7.0.

2. Signal $W + D^{(*)}$ signal samples

Only about 2% of the events in the inclusive $W + \text{jets}$ samples pass the $W + D^{(*)}$ fiducial requirements. This, coupled with the branching ratios of 9.2% (2.5%) to the $D^{+}$ ($D^{(*)}$) decay mode of interest, means that even very large $W + \text{jets}$ samples provide statistically inadequate measurements of the $W + D^{(*)}$ fiducial efficiency. Filtered signal samples are therefore used to enhance the statistical precision. The generated events are filtered to require the presence of a single lepton with $p_T > 15$ GeV and $|\eta| < 2.7$ and either a $D^{(*)}$ or a $D^{+}$ meson with $p_T > 7$ GeV and $|\eta| < 2.3$. EvtGen 1.7.0 is used to force all $D^0$ mesons to decay through the mode $D^0 \rightarrow K^- \pi^+$ and all $D^+$ mesons to decay through the mode $D^+ \rightarrow K^+ \pi^+$ (plus charge conjugates). EvtGen describes this three-body $D^+$ decay using a Dalitz plot amplitude that includes contributions from the $K^0(892)$, $K^{*0}(1430)$, $K^{*0}(1680)$, and $\k(800)$ resonances, as measured by CLEO-c [75].

These samples are used for signal modeling, for calculating the detector response matrix and fiducial efficiencies with small statistical uncertainties, and for determining the $W + D^{(*)}$ signal mass distribution used in the statistical analysis described in Sec. VIII. The amc@NLO+Py 8 (NLO) simulation described below is also used to calculate the theory predictions with the up-to-date PDF sets in Sec. X. Three such filtered samples are used.

Sherpa 2.2.11 $W + D^{(*)}$: To reduce the per-event CPU time for the generation of the $W + D^{(*)}$ signal datasets, Sherpa 2.2.11 is configured to have lower perturbative accuracy than...
for the inclusive $V + \text{jets}$ samples described above. Events are generated with NLO-accurate matrix elements for up to one jet, and LO-accurate matrix elements for two partons, in the five-flavor scheme. Other Sherpa parameters are set to the same values as for the baseline inclusive samples and uncertainties are evaluated using the same variations in QCD scale and $\alpha_s$ as for the baseline. The production cross section for this configuration differs from that of the inclusive sample by $\sim 2\%$. The two configurations show no significant differences in kinematic distributions associated with the $D^{(*)}$ meson or $W$ boson.

\[
\text{amC@NLO+Py8 (NLO) } W + D^{(*)}: \text{MadGraph5_aMC@NLO 2.9.3 is used to generate the } W + c\text{-jet process at NLO accuracy. A finite charm quark mass of } m_c = 1.55 \text{ GeV is used to regularize the cross section, and a full CKM matrix is used to calculate the hard-scattering amplitudes. The values of } \mu_s \text{ and } \mu_f \text{ are set to half of the transverse mass of all final-state partons and leptons. The PDF set used for event generation is } \text{NNPDF3.0NNLO with } \alpha_s = 0.118. \text{ The matrix-element calculation is interfaced with PYTHIA 8.244 for the modeling of the parton shower, hadronization, and underlying event and the A14 tune is employed. Scale variations where } \mu_s \text{ and } \mu_f \text{ are varied independently by a factor of 2 or 0.5 in the matrix element are included as generator process weights.}
\]

\[
\text{amC@NLO+Py8 (FxFx) } W + D^{(*)}: \text{Events are generated using the same PYTHIA 8 configuration as used for the inclusive amC@NLO+Py8 (FxFx) sample, but with the event-level filtering and configuration described above.}
\]

3. Top-quark pair production background samples

The production of $t\bar{t}$ events is modeled using the POWHEG BOX v2 [76–79] generator which provides matrix elements at NLO in the strong coupling constant $\alpha_s$ with the NNPDF3.0NLO PDF and the $h_{\text{damp}}$ parameter set to 1.5 $m_{\text{top}}$ [80]. The functional form of $\mu_s$ and $\mu_f$ is set to the default scale $\sqrt{m_{\text{top}} + p_T^2}$. The diagram removal scheme [93] is employed to handle the interference with $t\bar{t}$ production [80]. Top quarks are decayed at LO using MadSpin to preserve all spin correlations. The events are interfaced with PYTHIA 8.230 using the A14 tune and the NNPDF2.3LO PDF set. The decays of bottom and charmed hadrons are simulated using EvtGen 1.6.0. The inclusive cross section is corrected to the theory prediction calculated at NLO in QCD with NNLL soft-gluon corrections [94,95].

4. $Wt$-channel single-top background samples

Single-top $Wt$ associated production is modeled using the POWHEG BOX v2 generator which provides matrix elements at NLO in the strong coupling constant $\alpha_s$ in the five-flavor scheme with the NNPDF3.0NLO parton distribution function set. The functional form of $\mu_s$ and $\mu_f$ is set to the default scale $\sqrt{m_{\text{top}} + p_T^2}$. The diagram removal scheme [93] is employed to handle the interference with $t\bar{t}$ production [80]. Top quarks are decayed at LO using MadSpin to preserve all spin correlations. The events are interfaced with PYTHIA 8.230 using the A14 tune and the NNPDF2.3LO PDF set. The decays of bottom and charmed hadrons are simulated using EvtGen 1.6.0. The inclusive cross section is corrected to the theory prediction calculated at NLO in QCD with NNLL soft-gluon corrections [94,95].

5. $t$-channel and $s$-channel single-top background samples

Single-top $t$-channel ($s$-channel) production is modeled using the POWHEG BOX v2 generator at NLO in QCD using the four-flavor (five-flavor) scheme and the corresponding NNPDF3.0NLO set of PDFs. The events are interfaced with PYTHIA 8.230 using the A14 tune and the NNPDF2.3LO set of PDFs.

The uncertainty due to initial-state radiation (ISR) is estimated by simultaneously varying the $h_{\text{damp}}$ parameter and $\mu_s$ and $\mu_f$, and choosing the VarSc up and down variants of the A14 tune as described in Ref. [96]. The impact of final-state radiation is evaluated by halving and doubling the renormalization scale for emissions from the parton shower.

3The $h_{\text{damp}}$ parameter controls the transverse momentum $p_T$ of the first additional emission beyond the leading-order Feynman diagram in the parton shower and therefore regulates the high-$p_T$ emission against which the $t\bar{t}$ system recoils.
6. $t\bar{t}+V$ background samples

The production of $t\bar{t}V$ events, where $V$ denotes either $W$, $Z$, or $e^+e^-$ produced through $Z/\gamma$ interference, is modeled using the MadGraph5_aMC@NLO 2.3.3 [35] generator at NLO with the NNPDF3.0NNLO parton distribution function. The events are interfaced with PYTHIA 8.210 using the A14 tune and the NNPDF2.3LO PDF set. The uncertainty due to ISR is estimated by comparing the nominal $t\bar{t}V$ sample with two additional samples, which have the same settings as the nominal one, but with the var3 up or down variation of the A14 tune.

7. Diboson background samples

Samples of diboson final states ($VV$) are simulated with the Sherpa 2.2.1 or 2.2.2 [56] generator depending on the process (see Table I), including off-shell effects and Higgs boson contributions, where appropriate. Fully leptonic final states and semileptonic final states, where one boson decays leptonically and the other hadronically, are generated using matrix elements at NLO accuracy in QCD for up to one additional parton and at LO accuracy for up to three additional parton emissions. Samples for the gluon-loop-induced processes $gg \rightarrow VV$ are generated using LO-accurate matrix elements for up to one additional parton emission for both the cases of fully leptonic and semileptonic final states. The matrix-element calculations are matched and merged with the Sherpa parton shower using the MEPS@NLO prescription. The virtual QCD corrections are provided by the OpenLoops library. The NNPDF3.0NNLO set of PDFs is used along with the dedicated set of tuned parton-shower parameters developed by the Sherpa authors.

Matrix element to parton-shower matching [64] is employed for different jet multiplicities, which are then merged into an inclusive sample using an improved CKKW matching procedure which is extended to NLO accuracy using the MEPS@NLO prescription. These simulations are NLO accurate for up to one additional parton and LO accurate for up to three additional partons. The virtual QCD correction for matrix elements at NLO accuracy is provided by the OpenLoops library. The calculation is performed in the $G_\mu$ scheme [97], ensuring an optimal description of pure electroweak interactions at the electroweak scale.

IV. OBJECT SELECTION

The selection and categorization of $W+D^{(*)}$ candidate events depend on the reconstruction and identification of electrons, muons, tracks, and jets. Proton-proton interaction vertices are reconstructed from charged-particle tracks with $p_T > 500$ MeV in the ID. The presence of at least one such vertex with a minimum of two associated tracks is required, and the vertex with the largest sum of $p_T^2$ of associated tracks is chosen as the primary vertex (PV).

Three different categories of leptons are used in the analysis: baseline, loose, and tight. Here, “leptons” include electrons and muons, but exclude $\tau$-leptons. Baseline leptons are required to have $p_T > 20$ GeV, while loose and tight leptons are required to have $p_T > 30$ GeV. Tight leptons are required to meet isolation requirements. Antitight leptons are required to pass the loose requirements, but fail the tight requirements. They are used in the data-driven multijet production estimation described in Sec. VII C. Full electron and muon selection criteria are given in the text below and summarized in Table II.

Tracks used in the electron and muon reconstruction are required to be associated with the PV, using constraints on the transverse impact-parameter significance ($|d_0^{BL}/\sigma(d_0^{BL})|$) and the longitudinal impact parameter ($c_0^{BL}$). The transverse impact-parameter significance is calculated with respect to the measured beamline position and must satisfy $|d_0^{BL}/\sigma(d_0^{BL})| < 3.0$ for muons and $|d_0^{BL}/\sigma(d_0^{BL})| < 5.0$ for electrons. The longitudinal impact parameter of the track is the longitudinal distance along the beamline between the point where $|c_0^{BL}/\sigma(c_0^{BL})|$ is measured and the primary vertex. Tracks are required to have $|c_0^{BL}\sin\theta| < 0.5$ mm, where $\theta$ is the polar angle of the track.

Electron candidates are reconstructed from an isolated energy deposit in the electromagnetic calorimeter matched to a track in the ID and must pass the tight likelihood-based working point [98]. Electrons must be in the fiducial pseudorapidity region of $|\eta| < 2.47$, excluding the

<table>
<thead>
<tr>
<th>Features</th>
<th>Electrons</th>
<th>Muons</th>
</tr>
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<tbody>
<tr>
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<tr>
<td>Isolation</td>
<td>No</td>
<td>Yes</td>
</tr>
</tbody>
</table>

TABLE II. Lepton categories used in this analysis.
transition region $1.37 < |\eta| < 1.52$ between the calorimeter barrel and end caps. The tight electrons are required to meet the “tight” isolation criteria [98] based on a combination of the track-based and calorimeter-based isolation. The track-based isolation is $p_{T}^{\text{iso}}(\Delta R_{\text{var}} < 0.2)/p_{T} < 0.06$, with a variable cone size as defined in Sec. III A. The tracks are required to have $p_{T}^{\text{track}} > 1$ GeV and are required to be associated with the primary vertex. The calorimeter-based isolation is $E_{T}^{\text{cone20}}/p_{T} < 0.06$, where $E_{T}^{\text{cone20}}$ is the sum of the transverse energy of positive-energy topological clusters whose barycenter falls within a $\Delta R < 0.2$ cone centered around the electron, corrected for the energy leakage, pile-up, and underlying event, as described in Ref. [98]. Electron energy scale is calibrated following the procedure given in Ref. [98].

Muon candidates are reconstructed in the region $|\eta| < 2.5$ by matching tracks in the MS with those in the ID. The global refitting algorithm [99] is used to combine the information from the ID and MS subdetectors. Muons are identified using the tight quality criteria [100] characterized by the numbers of hits in the ID and MS subsystems. The tight muons are required to pass the tight isolation working point, based on a combination of the track-based and particle-flow-based [101] isolation. The requirement is $(p_{T}^{\text{track}}(\Delta R_{\text{var}} < 0.3) + 0.4 \times E_{T}^{\text{flow20}})/p_{T} < 0.045$, where the track-based isolation uses a variable cone size as defined in Sec. III A, with a maximum size of $\Delta R = 0.3$. The tracks are required to have $p_{T}^{\text{track}} > 500$ MeV and are required to be associated with the primary vertex. The $E_{T}^{\text{flow20}}$ is the sum of the transverse energy of neutral particle-flow objects in a cone of size $\Delta R < 0.2$ around the muon [100]. Muon momentum calibration is performed using the prescription in Ref. [99].

Jets are reconstructed from particle-flow objects [101] using the anti-$k_{t}$, [102,103] jet-reconstruction algorithm with a distance parameter $R = 0.4$. Candidate jets are required to have $p_{T} > 20$ GeV and $|\eta| < 5.0$. The jet energy scale calibration restores the jet energy to that of jets reconstructed at the particle level, as described in Ref. [104]. The jets from pile-up interactions are suppressed using the Jet Vertex Tagger algorithm (JVT) [105].

Jets with $|\eta| < 2.5$ and $p_{T} > 20$ GeV containing $b$-hadrons are identified by a deep neural network tagger, DL1r [106–108], that uses displaced tracks, secondary vertices, and decay topologies. The chosen working point has 70% efficiency for identifying $b$-jets in a simulated $t \bar{t}$ sample and the measured rejection factor (the inverse misidentification efficiency) for $c$-jets (light jets) is about 11 (600) [108]. The $b$-jets are defined according to the presence of $b$-hadrons with $p_{T} > 5$ GeV within a cone of size $\Delta R = 0.3$ around the jet axis. If a $b$-hadron is not found and a $c$-hadron is found, then the jet is labeled a $c$-jet. Light jets are all the rest.

The missing transverse momentum ($E_{T}^{\text{miss}}$) in the events is calculated as the negative vector sum of the selected high-$p_{T}$ calibrated objects (jets and baseline electrons and muons), plus a “soft term” reconstructed from tracks not associated with any of the calibrated objects [109,110].

To avoid cases where the detector response to a single physical object is reconstructed as two different final-state objects, e.g., an electron reconstructed as both an electron and a jet, an overlap removal strategy is used. If the two calorimeter energy clusters from two electron candidates overlap, the electron with the highest $E_{T}$ is retained. If a reconstructed electron and muon share the same ID track, the muon is rejected if it is calorimeter tagged, meaning the muon is identified as a reconstructed ID track that extrapolates to the calorimeter energy deposit of a minimum-ionizing particle without a MS signal [100]; otherwise the electron is rejected. Next, jets within $\Delta R = 0.2$ of electrons are removed. In the last step, electrons and muons within $\Delta R = 0.4$ of any remaining jet are removed. This overlap removal procedure is performed using the baseline leptons.

V. CHARMED MESON RECONSTRUCTION

Events containing $c$-quarks are identified by explicitly reconstructing charmed mesons in charged, hadronic decay channels. Two charmed hadron decay channels are used: $D^{+} \rightarrow K^{+} \pi^{+} \pi^{+}$ and $D^{*+} \rightarrow D^{0} \pi^{+} \rightarrow (K^{+} \pi^{+}) \pi^{+}$ (and charge conjugates). The invariant mass distribution $m(D^{+})$ [mass difference $m(D^{+} - D^{0})$] used in the fit for the $D^{+} (D^{*+})$ channel is described in Sec. VIII.

ID tracks satisfying $|\eta| < 2.5$ and $|z_{0} \sin \theta| < 5$ mm are used for $D^{(*)}$ meson reconstruction. The loose track quality requirement is applied [111]. The $D^{+} (D^{*})$ candidate is reconstructed using ID tracks with $p_{T} > 800$ MeV (600 MeV). A geometric separation of $\Delta R < 0.6$ among the tracks is required. Tracks corresponding to the baseline leptons used for the $W$ boson candidates are excluded. The $D^{+}$ candidates are required to have three tracks with total charge $= \pm 1$. The two tracks with the same charge are assigned the charged pion mass and the remaining track is assigned the kaon mass. The $D^{0}$ candidates are required to have two tracks with total charge $= 0$. One track is assigned the charged pion mass and the other is assigned the charged kaon mass. Both possible choices for the mass assignment are retained until matching to the prompt pion from the $D^{(*)}$ decay is performed. Tracks from the $D^{+} (D^{*})$ candidate are fitted to a common secondary vertex (SV), with a fit $\chi^{2}$ required to be $\chi^{2} < 8.0(10.0)$. To reduce the contribution from pile-up and from $b$-hadron decays, the transverse impact parameter of the $D^{(*)}$ candidate’s flight path with respect to the PV is required to satisfy $|d_{0}| < 1.0$ mm and the candidate is required to have a 3D impact-parameter significance $\sigma_{3D} < 4.0$, where $\sigma_{3D}$ is the distance of closest approach of the candidate’s flight path to the PV divided by the uncertainty in that distance. These selection criteria and
those described below were determined by optimizing the OS–SS signal significance, using MC predictions to estimate the signal, and mass sidebands to estimate the background.

Several requirements are placed on the $D^+$ candidates to reduce combinatorial background. The angle between the kaon track in the rest frame of the $D^+$ candidate and the line of flight of the $D^+$ candidate in the center-of-mass frame is required to satisfy $\cos \theta(K) > -0.8$. The distance between the SV and the PV in the transverse plane is required to satisfy $L_{xy} > 1.1$ mm for $D^+$ candidates with $p_T < 40$ GeV and $L_{xy} > 2.5$ mm for $D^+$ candidates with $p_T > 40$ GeV. Kinematic requirements are applied to ensure orthogonality to other $D^{(*)}$ decays with similar final states. The contamination from $D^{*+} \to D^0 \pi^+ \to (K^- \pi^+)\pi^+$, which has the same final-state content as the $D^+ \to K^- \pi^+ \pi^+$ channel, is reduced by requiring $m(K\pi\pi) - m(K\pi) > 160$ MeV. Background from the $D_s^+ \to \phi \pi^+ \to (K^- K^+)\pi^+$ channel, with one of the kaons misidentified as a pion, is removed by requiring the mass of each pair of oppositely charged particles, assuming the kaon mass hypothesis, to be $m(K^-K^+) > |m_\phi - 8|\text{MeV}$. The world-average mass of the $\phi$ meson from the Particle Data Group (PDG) database [112], $m_\phi = 1019.455$ MeV, is used. Finally, a requirement is placed on the invariant mass of the $D^+$ candidates, $1.7 \text{ GeV} < m(D^+) < 2.2 \text{ GeV}$.

The $D^{*+}$ candidates are reconstructed by combining $D^0$ candidates with prompt tracks that are assigned the charged pion mass. Only combinations where the pion in the $D^0$ candidate has the same charge as the prompt pion are considered. The small mass difference between the $D^{*+}$ and $D^0$ mesons restricts the phase space of this associated prompt pion, which has low momentum in the $D^0$ rest frame and hence is referred to as the slow pion. Slow pion tracks are required to have $p_T > 500$ MeV and a transverse impact parameter of $|d_0| < 1.0$ mm with respect to the primary vertex. An $L_{xy} > 0$ mm requirement is applied to $D^0$ candidates. The mass of the $D^0$ candidate must be within 40 MeV of the PDG world-average value of the $D^0$ mass, $m_{D^0} = 1864.83$ MeV [112]. Additionally, the angular separation between the slow pion and the $D^0$ meson must be small, $\Delta R(\pi_{slow}, D^0) < 0.3$, and the invariant mass cut of $140 \text{ MeV} < m(D^{*+} - D^0) < 180 \text{ MeV}$ is imposed.

Combinatorial background from light jets is reduced by requiring $D^{(*)}$ candidates to be isolated. The transverse momenta of tracks in a cone of size $\Delta R = 0.4$ around the $D^{(*)}$ candidate are summed, and the sum is required to be less than the $p_T$ of the $D^{(*)}$. Background from semileptonic $B$ meson decays is reduced by requiring $\Delta R(D^{(*)}, \ell') > 0.3$. Finally, the $D^{(*)}$ candidates are required to have $8 \text{ GeV} < p_T < 150 \text{ GeV}$ and $|\eta| < 2.2$. The $\eta$ cut is applied to avoid the edge of the ID, where the amount of the detector material

| TABLE III. $D^{(*)}$ object selection criteria. For $D^{*+}$ candidates the cuts related to SV reconstruction are applied to the corresponding $D^0$ candidate. |
| --- | --- | --- |
| $D^{(*)}$ cut | $D^+$ cut value | $D^{*+}$ cut value [$D^0 \pi \to (K\pi)\pi$] |
| $N_{tracks}$ at SV | 3 | 2 |
| SV charge | $\pm 1$ | 0 |
| SV fit quality | $\chi^2 < 8$ | $\chi^2 < 10$ |
| Track $p_T$ | $p_T > 800 \text{ MeV}$ | $p_T > 600 \text{ MeV}$ |
| Track angular separation | $\Delta R < 0.6$ | $\Delta R < 0.6$ |
| Flight length | $L_{xy} > 1.1$ mm [$p_T(D^{*+}) < 40$ GeV] | $L_{xy} > 0$ mm |
| $L_{xy} > 2.5$ mm [$p_T(D^{*+}) \geq 40$ GeV] | $|d_0| < 1$ mm |
| SV impact parameter | $|d_0| < 1$ mm | $|d_0| < 1$ mm |
| SV 3D impact significance | $\sigma_{3D} < 4.0$ | $\sigma_{3D} < 4.0$ |
| Combinatorial background rejection | $\Sigma p_{\Delta R<0.4\, f_{tracks}} / p_{f(D^+)} < 1.0$ | $\Sigma p_{\Delta R<0.4\, f_{tracks}} / p_{f(D^{*+})} < 1.0$ |
| $D_s^{+} \to \phi \pi^+$ rejection | $m(K^+K^-) > |m_\phi - 8|\text{MeV}$ | $|d_0| < 1$ mm |
| $D^{*+}$ background rejection | $m(K\pi\pi) - m(K\pi) > 160$ MeV | $|d_0| < 1$ mm |
| $D^0$ mass | $\Sigma p_{\Delta R<0.4\, f_{tracks}} / p_{f(D^+)} < 1.0$ |
| $\pi_{slow} p_T$ | $p_T > 500$ MeV | $|d_0| < 1$ mm |
| $\pi_{slow}$ angular separation | $\Delta R(\pi_{slow}, D^0) < 0.3$ |
| $\pi_{slow} d_0$ | $|d_0| < 1$ mm |
| QCD background rejection | $\Delta R(D^{*+}, \ell') > 0.3$ | $\Delta R(D^{*+}, \ell') > 0.3$ |
| $D^{(*)}$ cut | 8 GeV $< p_T(D^{*+}) < 150$ GeV | 8 GeV $< p_T(D^{*+}) < 150$ GeV |
| $D^{(*)}$ cut | $|\eta(D^{*+})| < 2.2$ | $|\eta(D^{*+})| < 2.2$ |
| Invariant mass | $1.7 \text{ GeV} < m(D^{*+}) < 2.2 \text{ GeV}$ | $140 \text{ MeV} < m(D^{*+} - D^0) < 180 \text{ MeV}$ |
increases rapidly and thus reduces the reconstruction efficiency and degrades the resolution. The upper p_T cut is applied to reject the background from fake D^{(*)} mesons at high momentum and, because the predicted fraction of D^{(*)} mesons with p_T(D^{(*)}) > 150 GeV is small, it has no significant impact on the signal reconstruction efficiency. The full set of selection requirements for the D^{(*)} candidates is summarized in Table III.

VI. EVENT SELECTION

Events for the analysis are selected through requirements on leptons, E_T^{miss}, jets, and D^{(*)} mesons satisfying the criteria defined in Secs. IV and V and passing the single-lepton triggers as discussed in Sec. III. Reconstruction of W bosons is based on their leptonic decays to either an electron (W → eν_e) or a muon (W → μν_μ). The lepton is measured in the detector and the presence of a neutrino is inferred from E_T^{miss}. Events are required to have exactly one tight lepton with p_T > 30 GeV and |η| < 2.5. Events with additional loose leptons are rejected. To reduce the multijet background and enhance the W boson signal purity, additional requirements are imposed: E_T^{miss} > 30 GeV and m_T > 60 GeV, where the W boson transverse mass (m_T) is defined as \sqrt{2p_T(lep)E_T^{miss}(1 - \cos(Δφ)}) and Δφ is the azimuthal separation between the lepton and the missing transverse momentum. Candidate D^{(*)} mesons are reconstructed using a secondary-vertex fit as described in Sec. V. Any number of D^{(*)} meson candidates satisfying these criteria are selected, which accounts for the production of multiple mesons in a single event. Only events with one or more D^{(*)} candidates are selected.

Events selected in this way are used to extract the W + D^{(*)} observables with a profile likelihood fit defined in Sec. VIII. Furthermore, the selected events are categorized according to the b-jet multiplicity to separate the W + D^{(*)} signal process from the t\bar{t} background with events containing W → c\bar{s} decays. The ID tracks associated with the reconstructed D^{(*)} candidates are often also associated with a jet mistagged as a b-jet. To avoid categorizing these W + D^{(*)} signal events as events with one or more b-jets, the b-jets are required to be geometrically separated from reconstructed D^{(*)} mesons by satisfying ΔR(b-jet, D^{(*)}) > 0.4. Events with exactly zero such b-tagged jets are classified as the W + D^{(*)} signal region (SR) and events with one or more b-tagged jets comprise the Top control region (CR). In this way about 80% of the t\bar{t} background events are in the Top CR and about 99% of W + D^{(*)} signal events remain in the W + D^{(*)} SR, effectively reducing the amount of t\bar{t} background. Collectively, the W + D^{(*)} SR and Top CR are called the “fit regions.” These requirements are summarized in Table IV(a). The measured signal and background yields in the W + D^{(*)} SR are given in Sec. X. The yield of W + D^{(*)} signal events is about 5% of the t\bar{t} background yield in the Top CR.

The analysis exploits the charge correlation of the W boson and the charm quark to enhance the signal and reduce the backgrounds. The signal has a W boson and a D^{(*)} meson of opposite charge, while most backgrounds are symmetric in charge. Therefore, the signal is extracted by measuring the difference between the numbers of OS and SS W + D^{(*)} candidates, which is referred to as OS–SS. While the signal-to-background ratio is about unity in the OS region, the OS–SS W + D^{(*)} signal is an order of magnitude larger than the remaining background after the subtraction.

The W + D^{(*)} measurement is unfolded to a “truth” fiducial region defined at MC particle level to have exactly one truth lepton with p_T(\ell) > 30 GeV and |η(\ell)| < 2.5. The lepton must originate from a W boson decay, with τ decays excluded from the fiducial region. Lepton momenta are calculated using “dressed” leptons, where the four-momenta of photons radiated from the final-state leptons within a cone of ΔR = 0.1 around the lepton are
added to the four-momenta of leptons. Truth $D^{(*)}$ mesons are selected by requiring $p_T(D^{(*)}) > 8$ GeV and $|\eta(D^{(*)})| < 2.2$. The OS–SS subtraction is also applied to the truth fiducial events. This removes any charge-symmetric processes, which are expected to originate mostly from gluon splitting in the final state. The $E_T^{\text{miss}}$ and $m_T$ requirements and $b$-jet veto are not applied in the fiducial selection. The truth fiducial selection is summarized in Table IV(b). The fiducial efficiency is defined as the fraction of $W + D^{(*)}$ signal events from the truth fiducial region that pass the detector-level reconstruction and requirements in Table IV(a). In the unfolding, events where the reconstructed objects pass the event selection but the truth objects fail the truth fiducial requirements are treated as inefficiencies; cases where the reconstructed objects fail the reconstruction fiducial selection but the truth objects pass the truth selection are treated as inefficiencies.

VII. SIGNAL AND BACKGROUND MODELING

MC samples are used to construct signal and background mass templates, except for the multijet background, which is determined using a data-driven method (Sec. VII C). Generally, Sherpa 2.2.11 MC samples are used to model events containing a single $W$ boson and one or more reconstructed $D^{(*)}$ meson candidates because they provide the highest precision when simulating QCD processes and the highest statistical power among the available samples. For specific purposes, MG+Py8 (CKKW-L) and aMC@NLO+Py8 (NLO) MC samples are used in conjunction with Sherpa to account for shortcomings in Sherpa modeling of $D^{(*)}$ meson decays as described in Secs. VII A and VII B. MC truth information is used to categorize the MC $W + D^{(*)}$ events according to the origin of the tracks used to reconstruct the $D^{(*)}$ meson candidate:

(i) $W + D^{(*)}$ signal: If all tracks originate from the signal charmed hadron species ($D^+$ or $D^*$) and are assigned in the reconstruction to the correct particle species ($K^+\pi^+\pi^\pm$), then that reconstructed $D^{(*)}$ candidate is labeled as $W + D^{(*)}$ signal.

(ii) $W + e^{\text{match}}$: If all tracks originate either from a different charmed hadron species ($D^0$, $D_s$, or $c$-baryon) or from a different decay mode of a signal charmed meson [e.g. $D^+ \to \phi p^+ \to (K^+K^-)\pi^+$], the reconstructed $D^{(*)}$ candidate is labeled as $W + e^{\text{match}}$.

(iii) $W + e^{\text{mismatch}}$: If at least one but not all tracks belong to a single charmed hadron, the reconstructed $D^{(*)}$ candidate is labeled as $W + e^{\text{mismatch}}$.

(iv) $W +$ jets: If none of the tracks are matched to a particle originating from a charmed particle, the $D^{(*)}$ candidate is labeled $W +$ jets. This is the combinatorial background from the underlying event and pile-up.

Additional background categories modeled using MC simulation are the following:

(i) Top: Processes containing top quarks ($t\bar{t}$, single-$t$, $t\bar{t}X$) are jointly represented by the “Top” category, which is dominated by the $t\bar{t}$ process.

(ii) Other: Events from diboson and $Z +$ jets processes are combined into the “Other” category.

The signal and background samples used in the $W + D^+$ and $W + D^{++}$ fits are given in Table V. The rates at which $c$-quarks hadronize into different species of weakly decaying charmed hadrons in the MC samples are reweighted to the world-average values [55]. The weights improve agreement between data and MC simulation by modifying the signal and background normalizations and the shapes of the $W + D^{(*)}$ background templates by changing the relative contribution of each species. The normalization of the background templates changes by up to 3%, depending on the $D^{(*)}$ species.

<table>
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<th>Normalization</th>
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<td>Sherpa 2.2.11</td>
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<tr>
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<tr>
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<td>MG+Py8 (CKKW-L)</td>
</tr>
<tr>
<td>$W + e^{\text{match}}$ ($D^*$ channel)</td>
<td>Sherpa 2.2.11</td>
<td>Sherpa 2.2.11</td>
</tr>
<tr>
<td>$W + e^{\text{mismatch}}$</td>
<td>Sherpa 2.2.11</td>
<td>LIS Sherpa 2.2.11</td>
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<td>LIS Sherpa 2.2.11</td>
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<tr>
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<td>MG+Py8 (CKKW-L)</td>
<td>LIS MG+Py8 (CKKW-L)</td>
</tr>
</tbody>
</table>
A. Signal modeling

The Sherpa 2.2.11 $W + D^+$ signal sample with EvtGen decays is used for the modeling of the mass template in the $D^+$ channel. However, because the width of the $D^{*+}$ meson is set incorrectly in Sherpa 2.2.11, the mass shape in the $D^{*+}$ channel is taken from the AMC@NLO+Py8 (NLO) $W + D^{*+}$ signal sample instead. In both channels the normalization is taken from Sherpa 2.2.11 because it provides the best available statistical power for calculating the fiducial efficiency.

B. Modeling backgrounds with a single W boson

The $W + c^{\text{match}}$ background in the $D^+$ channel is modeled using MG+Py8 (CKKW-L) because the EvtGen decay tables and models used with MG+Py8 (CKKW-L) provide a better description of the $D$ meson decay rates and kinematics than those implemented in Sherpa 2.2.11. Corrections to account for LO to NLO effects in $W + D^{(*)}$ production are applied by reweighting the MG+Py8 (CKKW-L) MC truth distribution of $p_T(D^+)$ to the corresponding Sherpa 2.2.11 distribution. Sherpa 2.2.11 is also used in the $D^{*+}$ channel.

The $W + c^{\text{mismatch}}$ backgrounds are modeled using Sherpa 2.2.11 in both the $D^+$ and $D^{*+}$ channels. The $W + $ jets background is modeled using Sherpa 2.2.11 in the $D^+$ channel and MG+Py8 (CKKW-L) in the $D^{*+}$ channel because their descriptions of this background yield and invariant mass shape are closer to the data before the fit. These background MC samples suffer from large statistical uncertainties. A loose inclusive selection (LIS) method was developed to reduce these uncertainties. The LIS method is based on the observation that, for these backgrounds, the $D^{(*)}$ meson mass shapes are the same for both $W$ boson charges and do not depend on the $E_T^{\text{miss}}$ and $m_T$ cuts. Therefore, the LIS can be used to construct mass templates inclusively and without $E_T^{\text{miss}}$ and $m_T$ cuts. These inclusive mass distributions are then used for both $W$ boson charges. In the $D^{*+}$ channel, the LIS $W + $ jets background is fitted with a parametric function. This parametric function is then used to generate the template histogram which is used in the $W + D^{*+}$ fit.

C. Data-driven multijet background estimation

Multijet backgrounds arise if one or more constituents of a jet are misidentified as a prompt lepton. In the electron channel, multijet events pass the electron selection due to having misidentified hadrons, converted photons, or semileptonic heavy-flavor decays. In the muon channel, muons from heavy-flavor hadron decays are the dominant source. Collectively, these backgrounds are called “fake and nonprompt leptons.” MC-based predictions for the normalization and composition of these backgrounds suffer from large uncertainties. The background rate is therefore determined using the data-driven matrix method [113].

The matrix method takes advantage of the fact that fake and nonprompt leptons (F) are less well isolated than real leptons (R). Leptons can be split independently in two ways: by origin, R and F, or by the tight (T) and loose reconstruction criteria defined in Table II. Leptons satisfying the loose but not the tight criteria are labeled as antitight (!T). While the abundances of R and F leptons ($N_R$ and $N_F$) are not directly measurable in data, they can be related to the measurable numbers of tight and antitight leptons ($N_T$ and $N_{!T}$) via the efficiency $r (f)$ for a loose real (fake) lepton to also be tight:

$$
\begin{pmatrix}
N_T \\
N_{!T}
\end{pmatrix} =
\begin{pmatrix}
r & f \\
1 - r & 1 - f
\end{pmatrix}
\begin{pmatrix}
N_R \\
N_F
\end{pmatrix}.
$$

This expression is inverted to give an expression for the number of fake and nonprompt leptons in the $W + D^{(*)}$ SR, dependent on measurable quantities,

$$
N_{\text{fake}} = \frac{f}{r - f} ((r - 1) N_T + r N_{!T}).
$$

This matrix method relation is applied bin by bin to estimate the multijet background yield in the variable of interest.

The real-lepton efficiency $r$ is determined from the data in auxiliary measurements [98,99] and extrapolated to the $W + D^{(*)}$ SR using MC samples. The real-lepton efficiency is estimated in three (four) bins in $\eta$ for electrons (muons) and in $p_T$ bins of 6 GeV width.

The fake-lepton efficiency $f$ is computed from the data in a dedicated region enriched in fake and nonprompt leptons, called the Fake CR. This region, orthogonal to the $W + D^{(*)}$ SR, is selected by inverting the $E_T^{\text{miss}}$ and $m_T$ requirements to $E_T^{\text{miss}} < 30$ GeV and $m_T < 40$ GeV. These requirements reduce the contribution of real leptons originating from $W$ boson decays. To further increase the Fake CR’s purity in fake and nonprompt leptons, processes with real leptons are estimated from MC simulation and subtracted from both tight and antitight subsets of Fake CR. The OS–SS subtraction is not performed for the calculation of the fake-lepton efficiencies because the multijet background is largely symmetric in OS and SS events. The number of tight leptons divided by the sum of tight and antitight gives the fake-lepton efficiency. The efficiency is estimated in three (four) bins in $\eta$ for electrons (muons) and in $p_T$ bins of 5 to 20 GeV width, depending on the available sample size. The fake-lepton efficiency, in the Fake CR, is in the range 50%–90% or 10%–70% for electrons and muons respectively.

Systematic uncertainties in the multijet estimation arise from several sources. Statistical uncertainties in the determination of the real- and fake-lepton efficiencies lead to systematic uncertainties of approximately 10% to 20% in the overall multijet yield. Uncertainties in the size of the...
real-lepton contamination in the Fake CR are assessed using two methods. First, the change in rate due to varying the QCD renormalization and factorization scales in MC samples is obtained. Second, the difference between the prompt rates determined using MG+py8 (CKKW-L) or Sherpa 2.2.11 $W+\text{jets}$ MC samples is evaluated. These two variations together result in relative uncertainties on the multijet yield of $\sim 20\%$ for the $D^+$ channel and $\sim 30\%$ for the $D^{\ast +}$ channel.

An additional systematic uncertainty is derived to account for the dependence of fake-lepton efficiencies on $E_\text{T}^{\text{miss}}$, which may arise from the different composition of fake background processes depending on the $E_\text{T}^{\text{miss}}$ (e.g. misidentified hadrons or semileptonic heavy-flavor decays), the correlation between the lepton isolation variables and $E_\text{T}^{\text{miss}}$, and the tendency of misidentified objects (e.g. jets misidentified as electrons) to give rise to $E_\text{T}^{\text{miss}}$ due to an incorrect assumption about the object type in their energy calibration. To estimate this, the Fake CR’s $E_\text{T}^{\text{miss}}$ cut is inverted to require $E_\text{T}^{\text{miss}} > 30$ GeV while its $m_T$ cut is retained to ensure orthogonality with the $W + D^{(*)}$ SR. This process provides an independent estimate of the multijet background. Differences between the multijet background yields in the $W + D^{(*)}$ SR obtained with these two choices of Fake CR cuts are $\sim 50\%$ for $D^+$ and $\sim 60\%$ for $D^{\ast +}$. While this multijet background estimate has large systematic uncertainties, the multijet yield in the $W + D^{(*)}$ SR is only up to $1\%$ of the signal yield in the electron channel and negligible in the muon channel. Thus the multijet background uncertainties are subdominant when estimating the overall background yield.

Figure 2 demonstrates the extrapolation of the multijet background from the Fake CR to the $W + D^{(*)}$ SR. Without the OS–SS subtraction, most of the $D$ mesons in the Top background originate from $B$ meson decays. This background is larger in the $D^+$ channel than in the $D^{\ast +}$ channel because the slow pion in the $D^*$ reconstruction chain is required to be associated with the PV and charmed mesons produced in $B$ meson decays often fail this requirement due to the sizable average lifetime of the $B$ mesons. The central values of the fake-lepton efficiencies are calculated in the $m_T < 40$ GeV region, but with the $E_\text{T}^{\text{miss}}$ requirement inverted ($E_\text{T}^{\text{miss}} < 30$ GeV). The figure instead shows the events with the $E_\text{T}^{\text{miss}} > 30$ GeV requirement corresponding to the $W + D^{(*)}$ SR selection. The prediction disagrees with the data at low $m_T$ due to an $E_\text{T}^{\text{miss}}$ dependence in the fake-lepton efficiencies that is not directly accounted for in the parametrization. A systematic uncertainty is introduced, as described above, by calculating the fake-lepton efficiencies with the $E_\text{T}^{\text{miss}} > 30$ GeV requirement and taking the full difference between the two multijet predictions as the uncertainty. Since this is the largest systematic uncertainty in the multijet background, the data are almost exactly covered by the one-standard-deviation variation in this region. Furthermore, the multijet prediction and the uncertainties are extrapolated into the $W + D^{(*)}$ SR with the $m_T > 60$ GeV requirement. To validate the extrapolation, the prediction is evaluated in a validation region (VR) with an $m_T$ requirement of $40$ GeV $< m_T < 60$ GeV. Figure 2 shows that the prediction in the VR is in agreement with the data within the systematic uncertainties, indicating that the multijet background is modeled well enough.

### VIII. CROSS-SECTION DETERMINATION

A statistical fitting procedure based on the standard profile-likelihood formalism used in LHC experiments [114,115] is used to extract the observables from the data with corresponding uncertainties:

(i) absolute fiducial cross sections:

$$\sigma_{\text{fid}}^{\text{OS–SS}}(W^{-} + D^{(*)})$$

and

$$\sigma_{\text{fid}}^{\text{OS–SS}}(W^{+} + D^{(*)}),$$

(ii) the cross-section ratio:

$$R_{\text{C3}} = \frac{\sigma_{\text{fid}}^{\text{OS–SS}}(W^{+} + D^{(*)})}{\sigma_{\text{fid}}^{\text{OS–SS}}(W^{-} + D^{(*)})},$$

(iii) differential cross sections for OS–SS $W^{-} + D^{(*)}$ and $W^{+} + D^{(*)}$.

The likelihood fit enables the estimation of background normalization and constraining of systematic uncertainties in situ by extracting the information from the data in mass-peak sidebands and control regions. It is a crucial ingredient in achieving percent-level precision in the $W + D^{(*)}$ cross-section measurement. The formalism of the profile likelihood fit is given in Sec. VIII A, Sec. VIII B explains how the “OS–SS” subtraction is incorporated, Sec. VIII C introduces the measurement of normalized differential cross sections, and Sec. VIII D defines the bin edges of the measured differential variables.

#### A. The profile likelihood fit

A binned likelihood function, $\mathcal{L}(\hat{\sigma}, \hat{\theta})$, is constructed as the product of Poisson probability terms for each bin of the input mass distributions, based on the number of data events and the expected signal and background yields. The product over the mass bins is performed for each differential bin, in bins of either $p_T(D^{(*)})$ or $|\eta(\ell^\prime)|$. The reconstructed invariant mass of the $D^+$ meson, $m(D^+)$, is used as input in the $D^+$ channel and the mass difference $m(D^{\ast +} - D^0)$ is used in the $D^\ast$ channel because it has better resolution than the $D^\ast$ invariant mass. The invariant mass bins in the $W + D^{(*)}$ SR are narrower in the peak region (with about eight bins) and wider in the tails, where the shape is more uniform (up to four bins). Only a single bin is fitted in each Top CR. The integrated $W + D^{(*)}$ SR invariant mass distributions are shown in Fig. 5 in Sec. X. The impact of systematic uncertainties is included via nuisance parameters, $\hat{\theta}$. Separate likelihood fits are performed for the $D^+$ and $D^{\ast +}$ channels and for $p_T(D^{(*)})$ and $|\eta(\ell^\prime)|$ distributions. A likelihood equation describing this fitting procedure is given in Eqs. (1)–(4):
FIG. 2. Modeling distributions of the $m_T$ variable using the matrix method to estimate the multijet background. The distributions are (a) $m_T$ in the $D^+$ electron channel, (b) $m_T$ in the $D^+$ muon channel, (c) $m_T$ in the $D^*/C3^+$ electron channel, (d) $m_T$ in the $D^*/C3^+$ muon channel. The “SM Tot.” line represents the sum of all signal and background samples and the corresponding hatched uncertainty band includes all matrix method systematic uncertainties, $E_{\text{miss}}$ systematic uncertainties, and QCD scale variations. The “Single W” component includes all contributions from Table V. The $D$ and $D^*/C3^+$ stand for $D^+$ and $D^*/C3^+$ mesons respectively and pion and kaon charges are omitted for brevity. Dashed vertical lines indicate the $m_T$ values defining the control, validation, and signal regions (CR, VR, and SR) as explained in the text. The last bin also includes the events with $m_T > 200$ GeV. The prompt processes estimated with MC samples are normalized to the expected SM cross sections given in Sec. III B.

\[
L(\vec{\sigma}, \vec{\theta}) = \prod_{\alpha} \left( \prod_i L(\vec{\sigma}, \vec{\theta})_{i}^{\alpha|\alpha} \times \prod_i L(\vec{\sigma}, \vec{\theta})_{i}^{\alpha|\alpha} \times \prod_i L(\vec{\sigma}, \vec{\theta})_{i}^{\alpha|\alpha} \times \prod_i L(\vec{\sigma}, \vec{\theta})_{i}^{\alpha|\alpha} \right) \times L_{\text{constr}},
\]

\[
L(\vec{\sigma}, \vec{\theta})_{i}^{\alpha|\alpha} = f \left( \sum_{\beta} \left[ \sigma_{\text{Tot}}^{\alpha|\alpha} \cdot R_{i}^{\alpha|\alpha}(\vec{\theta}) \cdot \mathcal{P}_{0i}(\vec{\theta}) \right] \cdot L(\theta_{\text{humi}}) \cdot B_{D^{(*)}} + B_{\text{Top}}(\vec{\theta}, \mu_{\text{Top}}) + \epsilon_{i}^{\alpha|\alpha} \right).
\]
\[ \mathcal{L}(\tilde{\theta}_i)^{\text{SS}} = f(N_i^{\text{SS}}|\gamma_i^{\text{SS}} \cdot \mathcal{R}_i^{\text{SS}}(\tilde{\theta}, \mu_{\text{Top}}) + c_i^{\text{SS}}), \]

\[ \mathcal{L}^{\text{constr}} = \prod_i g(\theta_i) \times \prod_{a,i} f(y_i^a), \]

where the index \( i \) represents the bins of the \( D^{(s)} \) mass distribution (either OS or SS) both in the \( n_{\text{jet}} = 0 \) \( W + D^{(s)} \) SR, as well as the single bin used in the \( n_{\text{jet}} > 0 \) Top CR. Indices \( \alpha \) and \( \beta \) represent the detector-level and truth differential bins respectively, and the index \( i \) represents the nuisance parameters \( \tilde{\theta} \). The expression \( f(k|\lambda) = \lambda^k e^{-\lambda}/k! \) is the Poisson probability density function. Furthermore,

(i) \( N_i^\alpha \) is the number of observed events in mass bin \( i \) and reconstructed differential bin \( \alpha \),

(ii) \( \sigma_{\text{fid}}^{\beta} \) is the fiducial cross section in differential bin \( \beta \) (one parameter per differential bin and \( W \) boson charge),

(iii) \( r^{\alpha\beta}(\tilde{\theta}) \) is the detector response matrix defined as the fraction of \( W + D^{(s)} \) events produced in truth fiducial bin \( \beta \) that also satisfy the \( W + D^{(s)} \) SR reconstruction criteria in bin \( \alpha \),

(iv) \( \mathcal{R}_i^{\alpha\beta}(\tilde{\theta}, \mu_{\text{Top}}) \) is the \( i \)th bin of the mass shape distribution of the signal sample corresponding to truth differential bin \( \beta \) in reconstructed differential bin \( \alpha \) (a separate invariant mass distribution for every non-zero bin in Fig. 3),

(v) \( \mathcal{L}(\theta_{\text{lumi}}) \) is the integrated luminosity,

(vi) \( B_{D^{(s)}} \) is the branching ratio of either the \( D^+ \) or \( D^{(*)} \) decaying into \( K \pi \pi \) (Ref. [112]),

(vii) \( \mathcal{R}_i^{\alpha\beta}(\tilde{\theta}, \mu_{\text{Top}}) \) is the total number of background events in mass bin \( i \) and reconstructed differential bin \( \alpha \), including the \( W + D^{(s)} \) signal events failing the truth fiducial selection [Table IV(b)],

(viii) \( \mu_{\text{Top}} \) is the normalization factor for the top-quark background,

(ix) \( c_i^{\alpha} \) is the “common floating component” in mass bin \( i \) and reconstructed differential bin \( \alpha \) (mathematical construct to enable likelihood minimization in OS–SS described further in Sec. VIII B),

(x) \( \tilde{\theta} \) represents all nuisance parameters that are profiled in the likelihood fit, and

(xi) \( \gamma_i^\alpha \) parameters are the Poisson-constrained parameters accounting for the MC statistical uncertainties in the combined signal-plus-background mass templates, following the simplified Beeston-Barlow technique [116].

The nuisance parameters \( \tilde{\theta} \) have Gaussian constraints \( g(\tilde{\theta}) \) in the likelihood with a mean of 0 and a standard deviation that corresponds to the one-standard-deviation variations of the associated systematic uncertainties determined from auxiliary measurements (e.g. lepton calibration described in Sec. IV). The \( \gamma_i^\alpha \) parameters are centered around 1 and may deviate from unity within the corresponding Poisson constraints reflecting the combined signal-plus-background statistical uncertainty in the invariant mass templates.

Response matrices for the \( D^+ \) and \( D^{(*)} \) channels are shown in Fig. 3 for differential \( p_T(D^{(*)}) \) and \( |\eta(c)| \) bins for nominal values of the nuisance parameters. Differential cross sections extracted in this way correspond to unfolding with matrix inversion. No regularization techniques were used because the detector response matrices are nearly diagonal and because the statistical uncertainties are sufficiently low.

**B. The OS–SS subtraction**

A fitting procedure exploiting the charge correlation between the \( W \) boson and the \( D^{(s)} \) meson was developed to perform the OS–SS subtraction within the likelihood fit. Instead of using OS–SS distributions in the fit, both the OS and SS regions enter the likelihood function and a common floating component is added in both regions. The additional component has one free parameter per invariant mass bin, and this parameter is correlated between the corresponding OS and SS regions. The common floating component is configured to absorb all charge-symmetric processes, which effectively translates the maximization of separate OS and SS likelihoods into a maximization of the OS–SS likelihood. This is done because the OS–SS event yields do not follow the Poisson distributions, which is a requirement for the data yields in the profile likelihood fit. Furthermore, this fitting procedure ensures that the yields of the individual signal and background components remain positive in the fit even though their OS–SS difference could be negative.

The method used to extract the OS–SS \( \sigma_{\text{fid}}^{\text{OS–SS}}(W + D^{(s)}) \) cross section from a simultaneous fit to OS and SS regions with the common floating component is demonstrated in Fig. 4 for the second bin of the \( p_T(D^{(*)}) \) distribution in the \( D^+ \) channel. The prefit OS, SS, and OS–SS distributions are shown on the left-hand side of Fig. 4 and the corresponding postfit distributions are on the right-hand side. The \( W + D^+ \) signal sample is split into three components (labeled bin 1, bin 2, and bin 3), which correspond to the diagonal and two off-diagonal elements immediately above and beneath the diagonal in Fig. 3(a). Since all other nondiagonal elements are zero, signal samples corresponding to truth fiducial bins 4 and 5 are not included. The common floating component is shown with the gray histograms named “Ch. Symm.” in the legend. The initial prefit values of the common floating component are arbitrary because every bin has a corresponding free parameter in the fit. This component is merely a mathematical construct to translate the minimization of separate OS and SS negative log-likelihoods into a minimization in OS–SS. The initial values in both the OS and SS regions are set to the difference between the data and the MC prediction in the SS region (different results
were not observed with other initial values). This ensures that the initial signal-plus-background predictions are positive and not too far away from the minimum. The plots illustrate the effectiveness of the OS–SS subtraction; the backgrounds are almost symmetric in OS and SS regions, so the resulting OS–SS distributions are largely dominated by the $W + D^{(*)}$ signal.

C. Normalized differential cross section

Normalized differential cross sections are generally more powerful than absolute differential cross sections in distinguishing between the observed data and the theory predictions since overall systematic uncertainties such as those in the integrated luminosity and branching ratio cancel out in the normalized differential cross sections. To extract the normalized differential cross sections and the total fiducial cross section, $\sigma_{\text{fid}}^{\text{tot}}$, instead of extracting the five absolute differential cross sections. By default, a substitution of the free parameters in the likelihood fit is made as shown in Eq. (5):

$$
\sigma_{\text{fid}}^{i} \rightarrow \sigma_{\text{fid}}^{\text{tot}} \times \sigma_{\text{rel}}^{i},
\sigma_{\text{fid}}^{2} \rightarrow \sigma_{\text{fid}}^{\text{tot}} \times \sigma_{\text{rel}}^{2},
\ldots
\sigma_{\text{fid}}^{N} \rightarrow \sigma_{\text{fid}}^{\text{tot}} \times \left[ 1 - \sum_{i=1}^{N-1} \sigma_{\text{rel}}^{i} \right],
$$

where $\sigma_{\text{fid}}^{i}$ is the absolute fiducial cross section in truth differential bin $i$ and $\sigma_{\text{rel}}^{i}$ is the corresponding normalized differential cross section. The value of $N$ is 5 in all cases. By definition, the sum of all normalized differential cross sections is 1. This substitution is performed separately for
FIG. 4. A demonstration of the OS–SS $W + D^{(*)}$ cross-section fit. Prefit $m(D^*)$ distributions for the $W^+ + D^+ p_T(D^*)$ bin 2: (a) OS, (b) SS, and (c) OS–SS. The corresponding postfit distributions: (d) OS, (e) SS, and (f) OS–SS. The SM Tot. line represents the sum of all signal and background samples. The corresponding prefit uncertainty bands include MC statistical uncertainties only and the postfit uncertainty bands include the total uncertainty extracted from the fit. The gray histograms represent the charge-symmetric common floating component and the three histograms associated with the signal samples are the truth bins of the $p_T(D^*)$ differential distribution.
each charge, $W^+ + D^{(s)}$ and $W^- + D^{(s)}$. Furthermore, a similar substitution is made for the $R_c^\pm$ parameter. The normalization factor for the $\sigma^{\text{fid}}_{\text{OS-SS}}(W^+ + D^{(s)})$ total fiducial cross section is replaced by the expression shown in Eq. (6):

$$\sigma^{\text{tot}}_{\text{fid}}(W^+ + D^{(s)}) \rightarrow R_c^\pm \times \sigma^{\text{tot}}_{\text{fid}}(W^+ + D^{(s)}). \quad (6)$$

The free parameters in the fit after these substitutions are $\sigma^{\text{rel}}_1, \ldots, \sigma^{\text{rel}}_{N-1}$ for each charge (eight parameters in total), $R_c^\pm$, and $\sigma^{\text{tot}}_{\text{fid}}(W^+ + D^{(s)})$. The central values of all additional observables can be deduced from these free parameters; however, systematic uncertainties can only be calculated for the parameters directly included in the fit (with a likelihood scan explained in Sec. IX A). To achieve this, several fits with different substitutions of parameters are performed:

1. $\sigma^1(W^- + D^{(s)}), \ldots, \sigma^N(W^- + D^{(s)}), \sigma^1(W^+ + D^{(s)}), \ldots, \sigma^N(W^+ + D^{(s)})$,
2. $\sigma^{\text{rel}}_1(W^- + D^{(s)}), \ldots, \sigma^{\text{rel}}_{N-1}(W^- + D^{(s)}), \sigma^{\text{rel}}_1(W^+ + D^{(s)}), \ldots, \sigma^{\text{rel}}_{N-1}(W^+ + D^{(s)})$, $R_c^\pm$, $\sigma^{\text{tot}}_{\text{fid}}(W^- + D^{(s)})$, and
3. $\sigma^{\text{rel}}_1(W^- + D^{(s)}), \ldots, \sigma^{\text{rel}}_{N-1}(W^- + D^{(s)}), \sigma^{\text{rel}}_1(W^+ + D^{(s)}), \ldots, \sigma^{\text{rel}}_{N-1}(W^+ + D^{(s)})$, $\sigma^{\text{tot}}_{\text{ fid}}(W^+ + D^{(s)}), R_c^\pm$.

These three fits allow a precise determination of the central values and systematic uncertainties of all observables, including absolute and normalized differential cross sections. In all cases the number of free parameters is the same and the minimization procedure reaches the same minimum, yielding identical results.

### D. Differential cross-section bins

The bin edges of the five differential $p_T(D^{(s)})$ bins are given in Table VI. The last bin starts at 80 GeV and has no upper limit. The number of bins and the bin edges were chosen such that the expected data statistical uncertainty is about 1%-2% in the first four bins. The available MC sample sizes also play an important role in determining the bin size; up to a 1% statistical uncertainty is present in the diagonal elements of the detector response matrix. Similar to the $p_T(D^{(s)})$ fits, five bins are chosen in $|\eta(\ell)|$ to provide percent-level precision. Furthermore, the absolute value of the pseudorapidity is used to further reduce the statistical uncertainty because there is no additional discriminating power in measuring the sign of the pseudorapidity. The $|\eta(\ell)|$ bin edges are also given in Table VI.

With five differential bins per $W$ boson charge there are ten differential cross sections in total represented with the free parameters $\hat{\sigma}$ in the likelihood fit. Regions with both charges of the $W$ boson are included in the fit at the same time in order to extract the cross-section ratio $R_c^\pm$. SRs in the $n_{\text{bjet}} = 0$ category are split between the two $W$ charges, into OS and SS events, and into the five differential bins: $[W^-, W^+] \times \{\text{OS, SS}\} \times 5 = 20$ regions. The $n_{\text{bjet}} > 0$ CRs are split in the same way with the exception of differential bins since the normalization of the backgrounds from top-quark production is extracted from the data only inclusively. The relative contribution of the top-quark background in the $W + D^{(s)}$ SR is small (about 5% of the signal yield for $D^+$ and negligible for $D^0$), so the modeling of the differential spectrum in the top-quark background simulation has a negligible impact on the result. The regions used in the fit are summarized in Table VII.

### Table VI. The differential $p_T(D^{(s)})$ and $|\eta(\ell)|$ bins used in the measurement. The last $p_T(D^{(s)})$ bin has no upper limit.

| Bin number | $p_T(D^{(s)})$ bin edges (GeV) | $|\eta(\ell)|$ bin edges |
|------------|-------------------------------|--------------------------|
| 1          | [8, 12]                       | [0.0, 0.5]               |
| 2          | [12, 20]                      | [0.5, 1.0]               |
| 3          | [20, 40]                      | [1.0, 1.5]               |
| 4          | [40, 80]                      | [1.5, 2.0]               |
| 5          | [80, \infty)                 | [2.0, 2.5]               |

### Table VII. A schematic of the signal and control regions (SR and CR) used in the fit. The bin numbers correspond to either the $p_T(D^{(s)})$ or $|\eta(\ell)|$ differential bins listed in Table VI. The table indicates that the invariant mass distribution is fitted in each $W + D^{(s)}$ SR, with $m(D^{(s)})$ standing for $m(D^+)$ in the $D^+$ channel and $m(D^{*+} - D^0)$ in the $D^*$ channel, while only a single bin is fitted in the Top CR.

<table>
<thead>
<tr>
<th>$W$ charge</th>
<th>$W + D^{(s)}$ SR ($n_{\text{bjet}} = 0$)</th>
<th>Top CR ($n_{\text{bjet}} &gt; 0$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$D^{(s)}$ charge</td>
<td>$W^-$</td>
<td>$W^+$</td>
</tr>
<tr>
<td>Bin 1</td>
<td>OS</td>
<td>SS</td>
</tr>
<tr>
<td>Bin 2</td>
<td>OS</td>
<td>SS</td>
</tr>
<tr>
<td>Bin 3</td>
<td>Fit the $m(D^{(s)})$ distribution</td>
<td>Fit total yield</td>
</tr>
</tbody>
</table>
IX. SYSTEMATIC UNCERTAINTIES

The measurements in this analysis are affected by several sources of systematic uncertainty. The first category related to detector-interaction and reconstruction processes, includes uncertainties in lepton and jet reconstruction, energy resolution, and energy scale, in lepton identification, isolation, and trigger efficiencies, in $b$-jet tagging efficiencies, and in the total integrated luminosity and pileup reweighting. These uncertainties affect the $W + D^{(*)}$ signal efficiency by altering the detector response matrix, yields of the background processes estimated with MC simulation, and the signal and background invariant mass templates used in the profile likelihood. These uncertainties are correlated between all samples and regions in the likelihood fit and are generally derived from auxiliary measurements:

Charged leptons: Electron and muon reconstruction, isolation, identification, and trigger efficiencies, and the energy/momentum scale and resolution are derived from data using large samples of $J/\psi \to \ell\ell'$ and $Z \to \ell\ell'$ events \cite{98,99}. Systematic variations of the MC efficiency corrections and energy/momentum calibrations applied to MC samples are used to estimate the signal selection uncertainties.

Jets and missing transverse momentum: Jet energy scale and energy resolution uncertainties affect the signal efficiency and background yields indirectly by altering the reconstructed $E_T^{\text{miss}}$ in the event and hence the selection efficiency of the $E_T^{\text{miss}}$ and $m_T$ cuts. Systematic variations of the jet energy calibration are applied to MC samples to estimate signal selection uncertainties using the methodology described in Ref. \cite{104}. In total, there are 20 independent jet energy scale variations and eight independent jet energy resolution variations. None of the single variations have an impact of more than 1% on the signal selection efficiency. Similarly, variations in $E_T^{\text{miss}}$ reconstruction are derived specifically for the soft-term estimation following the methodology in Ref. \cite{110}. Furthermore, a single nuisance parameter is included to model the uncertainty in the JVT selection efficiency.

Flavor tagging: The uncertainty in the calibration of the $b$-tagging efficiencies and mistag rates is derived from data using samples of dileptonic $t\bar{t}$ events for $b$-jets and $c$-jets \cite{106,117} and a data sample enriched in light-flavor jets for light jets \cite{118}. Since the majority (>99%) of $W + D^{(*)}$ signal events have no additional $b$-tagged jets, these variations have a negligible impact on the signal efficiency. Nevertheless, the variations in $b$-tagging efficiency have an impact of up to 10% on the relative yields of the top-quark backgrounds in the $W + D^{(*)}$ SR and Top CR.

Pileup and luminosity: The uncertainty in the integrated luminosity is 0.83% \cite{44}, which is obtained using the LUCID-2 detector \cite{45} for the primary luminosity measurements. MC samples are reweighted to have the number of pile-up vertices match the pile-up distribution measured in the Run 2 data. To account for the uncertainty in the pile-up estimation, variations of the reweighting are applied to the MC samples. In addition to affecting the background yields, it also has a small impact on the resolution of the reconstructed $D^+$ meson mass peak and the $m(D^{(*)} - D^0)$ mass difference.

SV reconstruction: Uncertainties in the secondary-vertex reconstruction efficiency arise from potential mismodeling of the amount and location of ID material, from the modeling of hadronic interactions in GEANT4, and from possible differences between the impact-parameter resolution in data and MC events. These uncertainties are evaluated by generating large single-particle samples of $D^+$ and $D^{(*)}$ decays with the same $p_T$ and $\eta$ distributions as the baseline $W + D^{(*)}$ MC samples. These “single-particle gun” (SPG) samples are simulated multiple times with different simulation parameters, mirroring the procedure in Ref. \cite{111}: passive material in the whole ID scaled up by 5%, passive material in the IBL scaled up by 10%, and passive material in the Pixel detector services scaled by 25%. In addition to the variations in the amount of detector material, a SPG sample where the physics model in the GEANT4 toolkit was changed to QGSP_BIC from FTFP_BERT \cite{49} was generated.

The impact of the uncertainty in the ID material distribution is evaluated by comparing the efficiency obtained using the baseline simulation and that obtained using altered material distributions. For each variation the relative change in the $D^{(*)}$ reconstruction efficiency is parametrized as a function of $p_T(D^{(*)})$ and $\eta(D^{(*)})$ separately for positive and negative charges of the mesons and separately for $D^+$ and $D^{(*)}$ mesons. The impact of changing the physics model was found to be negligible. The relative change in the reconstruction efficiency due to the increased amount of the ID material was found to vary by 1%-4%. The uncertainty is largest for low $p_T(D^{(*)})$ and high $\eta(D^{(*)})$. Because $D^{(*)}$ candidates in the signal and in the $t\bar{t}$ background do not necessarily have the same $p_T(D^{(*)})$ spectrum, their tracking efficiency NPs are treated as separate parameters to minimize the correlation between them. The $t\bar{t}$ background has large yields in the Top CR and could affect the shape of the $p_T(D^{(*)})$ signal distribution via pulls in the tracking efficiency uncertainties. The measured cross sections would change by up to 1.0% if the parameters were correlated, but this difference is covered by the associated systematic uncertainties.

Furthermore, the effect of the ID material variations on the shape of the $D^+$ invariant mass peak and the $m(D^{(*)} - D^0)$ mass difference is evaluated by fitting the mass distributions with a double-sided Crystal Ball function, with yield modeling decoupled from the peak position. The width and position of the peak are characterized with the width and mean of the central Gaussian distribution respectively. The shift in the position of the $D^+(D^{(*)})$ peak was found to be up
to 0.2 MeV (0.05 MeV). The impact on the resolution of the peak was evaluated from the difference between the squares of the nominal width and the width obtained from each variation. The resolution was found to be smeared by up to 4.0 MeV (0.2 MeV) for the $D^+$ ($D^{*+}$) peak. The variations in the peak position and resolution are implemented in the likelihood fit as shape uncertainties with no impact on the signal yield, but this additional freedom in the fit is necessary to achieve good agreement between the data and the fit model.

An additional systematic uncertainty is applied to cover ID track impact-parameter resolution differences between simulation and data after the ID alignment is performed [119]. The difference is evaluated using minimum-bias data and the resulting uncertainty is extrapolated to higher $p_T$ with muon tracks from Z boson decays [111]. The uncertainty is propagated to the $W + D^{(*)}$ measurement by generating $D^+$ and $D^{*+}$ SPG samples where the impact parameters of the ID tracks are smeared before performing the SV fit for the $D^{(*)}$ reconstruction. The relative change in the $D^{(*)}$ reconstruction efficiency was found to be up to 5% for high-$p_T$ $D^{(*)}$ mesons and about 1.5% at low $p_T$ (i.e. $p_T < 40$ GeV). The systematic uncertainties in the $D^{(*)}$ meson reconstruction efficiency related to ID track impact-parameter resolution and ID material variations are among the largest systematic uncertainties in the analysis.

Signal modeling: The signal modeling uncertainty is derived by comparing the fiducial region efficiencies for the signal Sherpa 2.2.11, aMC@NLO+Py8 (FXfX), and aMC@NLO+Py8 (NLO) $W + D^{(*)}$ simulations. In each differential bin, the maximum difference between the nominal MC simulation (Sherpa) and either of the MadGraph5_aMC@NLO simulations is taken and a symmetric systematic uncertainty is applied in the two directions. The uncertainty is correlated between the differential bins and $W$ boson charges. It accounts for the fact that the choice of MC simulation for unfolding affects the measured values of the observables because of differences in the ME calculation, PS simulation, and heavy-flavor quark fragmentation and hadronization. The uncertainty ranges from 1% to 4%, depending on the bin, and is generally one of the largest uncertainties in the analysis. The relatively large difference in fiducial efficiency between Sherpa and MadGraph5_aMC@NLO simulations arises from the modeling of the correlation between $W$ boson and $D^{(*)}$ meson kinematics when the $E_T^{miss}$ and $m_T$ cuts are applied at the detector level. Including the same $E_T^{miss}$ and $m_T$ cuts in the truth fiducial definition would reduce the uncertainty; however, it would give rise to a large background from signal $W + D^{(*)}$ events that fail the truth $E_T^{miss}$ and $m_T$ selection, but pass the detector-level selection due to the poor $E_T^{miss}$ resolution, ultimately increasing the total uncertainty.

Additional uncertainties are considered by varying the QCD scales, the PDFs, $\alpha_s$, and the virtual EW corrections in Sherpa 2.2.11. The PDF variations, $\alpha_s$ uncertainty, and EW corrections were found to have a negligible effect on the fiducial efficiency. The effect of QCD scale uncertainties is defined by the envelope of variations resulting from changing the renormalization and factorization scales by factors of 2 with an additional constraint of $0.5 \leq \mu_R/\mu_F \leq 2$. In most differential bins the effect was found to be smaller than the corresponding difference between Sherpa and MadGraph5_aMC@NLO. Lastly, the uncertainties in the $D^+ \rightarrow K^-\pi^+\pi^+$ and $D^{*+} \rightarrow D^0\pi^+\pi^-\pi^+$ branching ratios [112] are applied as uncertainties of 1.7% and 1.1%, respectively, in the signal yield in the likelihood fit.

Background MC modeling: The implementation of the background modeling uncertainties varies between the backgrounds. For $W + c_{\text{match}}$, $W + c_{\text{mismatch}}$, and $W + J$ backgrounds, Sherpa 2.2.11 QCD scale, PDF, and $\alpha_s$ variations are used. Among the three, the QCD scale uncertainty generally has the largest effect and leads to a 10%–30% uncertainty in the yield of the corresponding background process, depending on the differential bin. The uncertainty is constrained in the likelihood fit by the small statistical uncertainties in the tails of the invariant mass distributions in the $D^*$ and $D^{*+}$ channels, reducing its impact on the observables. As in the case of the signal process, these uncertainties are correlated between the differential bins. An additional modeling uncertainty is included by taking the full difference between Sherpa and MadGraph5_aMC@NLO predicted background yields. To be conservative, this uncertainty is taken to be uncorrelated between the differential bins. This avoids the assumption that either of the simulations have an a priori perfect description of the shape of the differential variable [i.e. $p_T(D^{(*)})$ or $|\eta(c)|$], and provides more flexibility in the likelihood fit.

Internal event weight variations in the MadGraph5_aMC@NLO 2.3.3 $t\bar{t}$ simulation are used to determine the effect of the PDF uncertainty on the top-quark background. The uncertainty due to initial-state radiation is estimated by simultaneously varying the $h_{\text{damp}}$ Parameter and the $\mu_t$ and $\mu_F$ scales, and choosing the Var3c up and down variants of the A14 tune as described in Ref. [96]. The impact of final-state radiation is evaluated by halving and doubling the renormalization scale for emissions from the parton shower. Uncertainties in the $t\bar{t}$ ME calculation and PS are estimated by replacing the nominal $t\bar{t}$ prediction with two alternative simulations: POWHEG+Herwig 7.04 and MadGraph5_aMC@NLO +PYTHIA 8 and taking the full difference as a systematic uncertainty. For other small backgrounds ($Z + J$ and diboson events) a conservative 20% uncertainty in their yields is used. Due to the high purity of the $W + D^{(*)}$ signal process in the $W + D^{(*)}$ SR selection, background modeling uncertainties are subdominant in the statistical analysis.

Charm hadronization: The $W + c_{\text{match}}$ and $W + c_{\text{mismatch}}$ backgrounds in the $D^+$ channel have large contributions from weakly decaying charged mesons incorrectly
reconstructed as $D^+ \rightarrow K^−\pi^+\pi^+$ [e.g. $D_s^+ \rightarrow \phi\pi^+ \rightarrow (K^+K^-)\pi^+$ reconstructed as $D^+ \rightarrow K^−\pi^+\pi^+$]. Two sources of associated systematic uncertainty are included: uncertainties in the charmed hadron production fractions and uncertainties in the charmed hadron branching ratios. Charmed hadron production fractions in the MC samples are reweighted to the world-average values as described in Sec. VII B. Following the procedure in Ref. [55], three eigenvector variations of the event weights are derived to describe the correlated experimental systematic uncertainties associated with the measurements of the charmed hadron production fractions. The uncertainty affects the relative background yield by up to 3% and also the shape of the background invariant mass distribution because the different charmed hadron species populate different ranges of the reconstructed $D^+$ invariant mass. The impact of the uncertainties in the charmed hadron branching ratios is estimated in a conservative way by generating SPG $D^+$ samples with all branching ratios shifted simultaneously in a correlated manner to cover the systematic uncertainties in charmed hadron decays reported in Ref. [112]. The relative change in the background yield and shape of the $W + e^{\text{match}}$ background with respect to the nominal SPG configuration is propagated to the Sherpa MC sample and implemented in the statistical analysis. The size of the uncertainty is up to 5%. Both sources of charmed hadronization uncertainty related to background processes were found to have a negligible impact on all observables.

Multijet estimation: The multijet background and its uncertainties are estimated in the Fake CR, as described in Sec. VII C and the corresponding systematic uncertainties are implemented as nuisance parameters in the likelihood fit. Due to the difficulty of estimating the multijet background in the $W + D^{(*)}$ SR selection, the relative uncertainties are large (>50%). However, the multijet background is largely symmetric between OS and SS regions and its relative size is reduced in the OS–SS subtraction. Despite the large relative uncertainty in the multijet yield, the impact on the measured observables is therefore negligible.

Finite size of MC samples: MC statistical uncertainties affect the measurement in several ways. The binomial uncertainties in the $W + D^{(*)}$ fiducial efficiencies calculated with the Sherpa MC samples are propagated into the likelihood fit via nuisance parameters affecting the yield of the signal sample. There is one parameter per nonzero element of the detector response matrix. The statistical uncertainty in the diagonal elements is less than 1%, while the uncertainty in the off-diagonal elements exceeds 10%. However, because the off-diagonal elements have small values compared to diagonal ones, the corresponding statistical uncertainty has a negligible impact on the results. Furthermore, statistical uncertainties associated with the bins of the invariant mass distributions are implemented as constrained “$\gamma$” parameters in the likelihood fit as explained in Sec. VIII. There is one such parameter per invariant mass bin and their impact on the observables is of the order of 1%.

### A. Evaluation of the overall systematic uncertainty

The impact of each individual systematic uncertainty on the observables is calculated by performing two likelihood fits with the corresponding nuisance parameter ($\theta$) fixed to its postfit one-standard-deviation bounds. The changes in the values of the normalization factors associated with the observables, relative to the unconditional likelihood fit, are then taken as the impact of the given systematic uncertainty on the observables. Several nuisance parameters are grouped together by summing their impact on the observables in quadrature. A summary of the dominant systematic uncertainties is given in Table VIII for inclusive cross

<table>
<thead>
<tr>
<th>Uncertainty (%)</th>
<th>$D^+$ channel</th>
<th>$D^{(*)}$ channel</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\sigma^{\text{OS-SS}}_{\text{fid}}(W^- + D^{(*)})$</td>
<td>$\sigma^{\text{OS-SS}}_{\text{fid}}(W^- + D^{(*)})$</td>
<td>$R^\pm(\Delta)$</td>
</tr>
<tr>
<td>SV reconstruction</td>
<td>3.0</td>
<td>2.9</td>
</tr>
<tr>
<td>Jets and $E_T^{\text{miss}}$</td>
<td>1.7</td>
<td>1.9</td>
</tr>
<tr>
<td>Luminosity</td>
<td>0.8</td>
<td>0.8</td>
</tr>
<tr>
<td>Muon reconstruction</td>
<td>0.6</td>
<td>0.7</td>
</tr>
<tr>
<td>Electron reconstruction</td>
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</tr>
<tr>
<td>Multijet background</td>
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<td>0.2</td>
</tr>
<tr>
<td>Signal modeling</td>
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<td>2.1</td>
</tr>
<tr>
<td>Background modeling</td>
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<td>1.2</td>
</tr>
<tr>
<td>Finite size of MC samples</td>
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<td>1.2</td>
</tr>
<tr>
<td>Data statistical uncertainty</td>
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<td>0.5</td>
</tr>
<tr>
<td>Total</td>
<td>4.6</td>
<td>4.6</td>
</tr>
<tr>
<td>$\sigma^{\text{OS-SS}}_{\text{fid}}(W^- + D^{(*)})$</td>
<td>2.3</td>
<td>2.3</td>
</tr>
<tr>
<td>$\sigma^{\text{OS-SS}}_{\text{fid}}(W^- + D^{(*)})$</td>
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<td>0.5</td>
</tr>
<tr>
<td>$R^\pm(\Delta)$</td>
<td>0.8</td>
<td>0.8</td>
</tr>
<tr>
<td>$R^\pm(\Delta)$</td>
<td>0.7</td>
<td>0.7</td>
</tr>
<tr>
<td>$R^\pm(\Delta)$</td>
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<tr>
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<td>$R^\pm(\Delta)$</td>
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<tr>
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</tr>
<tr>
<td>$R^\pm(\Delta)$</td>
<td>3.7</td>
<td>3.7</td>
</tr>
</tbody>
</table>
sections and the cross-section ratio $R^{\pm}_c$. The table demonstrates that most of the systematic uncertainties are correlated between the positive and negative charge channels and therefore cancel out in the $R^{\pm}_c$ calculation. The dominant uncertainties in $R^{\pm}_c$ are the data and MC statistical uncertainties. Uncertainties in differential bins are summarized in Appendix A. Similar to the $R^{\pm}_c$ calculation, uncertainties with no dependence on the differential variable cancel out in the normalized cross section. For example, the SV reconstruction efficiency uncertainties almost completely cancel out in normalized $|\eta(\ell)|$ cross sections because the $D^{(*)}$ SV reconstruction has no dependence on the lepton pseudorapidity. However, the same uncertainties do not cancel out in the $p_T(D^{(*)})$ measurement because there is a strong dependence on $p_T(D^{(*)})$.

X. RESULTS AND COMPARISON WITH THEORETICAL PREDICTIONS

Postfit comparisons between the data and MC distributions for the $D^+$ and $D^{(*)}$ channels are shown in Fig. 5 separately for the $W^-$ and $W^+$ channels. Most of the data points are within the resulting 1σ systematic uncertainty band. The $W + D^{(*)}$ SR postfit yields obtained with the likelihood fit are given in Tables IX and X. Yields are
TABLE IX. Postfit yields in the OS–SS $W + D^+$ SR from the $p_T(D^+)$ differential fit. The data statistical uncertainty is calculated as $\sqrt{N_{OS} + N_{SS}}$. Uncertainties in individual SM components are the full postfit systematic uncertainties.

| Sample                  | OS–SS $W + D^+$ SR $[p_T(D^+)]$ fit | OS–SS $W + D^+$ SR $[|\eta|]$ fit |
|-------------------------|------------------------------------|-----------------------------------|
|                         | $W^- + D^+$                        | $W^+ + D^+$                        | $W^+ + D^+$                        |
| $W^\pm + D^\mp$ (bin 1) | 26430 $\pm$ 510                   | 26180 $\pm$ 550                   | 31530 $\pm$ 530                   |
| $W^\pm + D^\mp$ (bin 2) | 39090 $\pm$ 660                   | 38610 $\pm$ 660                   | 30560 $\pm$ 650                   |
| $W^\pm + D^\mp$ (bin 3) | 43520 $\pm$ 660                   | 41510 $\pm$ 670                   | 25640 $\pm$ 470                   |
| $W^\pm + D^\mp$ (bin 4) | 15330 $\pm$ 350                   | 14520 $\pm$ 350                   | 23890 $\pm$ 450                   |
| $W^\pm + D^\mp$ (bin 5) | 2740 $\pm$ 120                    | 2346 $\pm$ 93                     | 15860 $\pm$ 480                   |
| $W^+ + c_{\text{match}}$ | 24800 $\pm$ 2400                 | 24300 $\pm$ 2400                 | 23500 $\pm$ 2600                 |
| $W^+ + c_{\text{mismatch}}$ | 34300 $\pm$ 2500                | 29700 $\pm$ 2400                 | 33900 $\pm$ 2500                 |
| $W^+ + \text{jets}$     | 1300 $\pm$ 140                    | 1900 $\pm$ 150                    | 2200 $\pm$ 150                    |
| $t\bar{t}$ + single top | 6500 $\pm$ 550                    | 6220 $\pm$ 590                    | 6520 $\pm$ 540                    |
| Other                   | 1030 $\pm$ 430                    | 1830 $\pm$ 460                    | 1060 $\pm$ 450                    |
| Multijet                | 730 $\pm$ 410                     | 1070 $\pm$ 450                    | 1180 $\pm$ 640                    |
| Total SM                | 195800 $\pm$ 1200                 | 188200 $\pm$ 1300                 | 195800 $\pm$ 1300                 |
| Data                    | 195800 $\pm$ 1100                 | 188200 $\pm$ 1100                 | 195800 $\pm$ 1100                 |

TABLE XI. Measured fiducial cross sections times the single-lepton-flavor $W$ boson branching ratio and the cross-section ratios. $R^\pm(D^{(*)})$ is obtained by combining the individual measurements of $R^\pm(D^+)$ and $R^\pm(D^{(*)})$ as explained in the text.

<table>
<thead>
<tr>
<th>Channel</th>
<th>$\sigma_{\text{fid}}^{\text{OS-SS}}(W + D^{(*)}) \times B(W \rightarrow \ell \nu)$ (pb)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$W^- + D^+$</td>
<td>50.2 $\pm$ 0.2(stat) $^{+2.1}_{-3.3}$ (syst)</td>
</tr>
<tr>
<td>$W^+ + D^-$</td>
<td>48.5 $\pm$ 0.2(stat) $^{+2.1}_{-3.3}$ (syst)</td>
</tr>
<tr>
<td>$W^- + D^+$</td>
<td>51.1 $\pm$ 0.4(stat) $^{+1.9}_{-1.8}$ (syst)</td>
</tr>
<tr>
<td>$W^+ + D^-$</td>
<td>50.0 $\pm$ 0.4(stat) $^{+1.9}_{-1.8}$ (syst)</td>
</tr>
</tbody>
</table>

The resulting cross sections $\sigma_{\text{fid}}^{\text{OS-SS}}(W + D^{(*)}) \times B(W \rightarrow \ell \nu)$ and $R^\pm(D^{(*)})$ are presented in Table XI. The results presented here are obtained using the $p_T(D^{(*)})$ fit; results from the differential $|\eta|$ fit are compatible. Ratios of cross sections obtained in the $D^+$ and $D^{(*)}$ channels are consistent with predictions obtained using the world-average production fractions, $\sigma(W + D^+)/\sigma(W + D^{(*)}) = 1.01 \pm 0.034$, where

shown for both the $p_T(D^{(*)})$ and $|\eta|$ fits. Background yields and the integrated signal yields are consistent between the two fits in both the $D^+$ and $D^{(*)}$ channels. The systematic uncertainties in the integrated yields are slightly lower in the $p_T(D^{(*)})$ fits than in the $|\eta|$ fits because the dominant systematic uncertainties depend more strongly on $p_T(D^{(*)})$ and are therefore more constrained in the fit.
FIG. 6. Impact of systematic uncertainties, for the 20 largest contributions, on the fitted cross section from the $p_T(D^{(*)})$ fits, sorted in decreasing order. Impact on (a) $\sigma_{\text{OS-SS}}(W^- + D^+)$, (b) $\sigma_{\text{OS-SS}}(W^+ + D^-)$, (c) $\sigma_{\text{OS-SS}}(W^- + D^+/C^3)$, and (d) $\sigma_{\text{OS-SS}}(W^+ + D^-/C^3)$. The impact of prefit (postfit) nuisance parameters $\bar{\theta}$ on the signal strength are shown with empty (colored) boxes. The postfit central value ($\hat{\theta}$) and uncertainty are shown for each parameter with black dots.
the 3.4% uncertainty is obtained using the (correlated) uncertainties in the $D^{*}/C_{3}$ and $D^{+}/C_{3}$ production fractions [54]. The measured differential cross sections in bins of $p_{T}(D^{*}/C_{3})$ are given in Appendix B. The statistical uncertainty is larger in the $D^{*}/C_{3}$ channel because the branching ratio for that mode is smaller than the one for $D^{+}$; the relative sizes of the systematic uncertainties are similar because they are largely independent of the channel. A combined value of $R_{C}^{2}(D^{*}/C_{3})$ is derived from the individual measurements of $R_{C}^{2}(D^{+})$ and $R_{C}^{2}(D^{*})$. Systematic uncertainties are largely uncorrelated between the channels. As shown in Table VIII, they are dominated by the uncorrelated MC statistical uncertainties. After correcting for differences between the chosen fiducial regions, these measurements are consistent with, but more precise than, the CMS $W + D^{*}$ results presented in Ref. [23], performed with $35.7 \text{ fb}^{-1}$ of data.

The impact of the nuisance parameters on the fitted values of the absolute fiducial cross section in the differential $p_{T}(D^{*})$ fits is shown as a “ranking plot” in Fig. 6. The 20 nuisance parameters with the largest contribution are ordered by decreasing impact on the corresponding observable. The postfit central values and uncertainties of the corresponding parameters are given in the same plots. The ranking plots demonstrate that most nuisance parameters with large impact on the integrated fiducial cross section do not deviate significantly from the initial values in the likelihood fit. The parameters associated with the signal...
parameters are constrained by the observed width of the amplitudes. For each PDF set, the uncertainty is obtained from a choice of parton-shower model are estimated from a prescription \[120\]. Uncertainties associated with the choice of NLO matching algorithm are assessed by replacing the A14 tune with its default tune. Differences between predictions associated with the choice of NLO matching algorithm are assessed by comparing the \textsc{amc@nlo+py8} (NLO) cross sections with those obtained using the calculation described in Ref. [36]. This calculation is based on the \textsc{powhel} event generator, which uses the \textsc{powheg box v2} interface to implement \textsc{powheg} NLO matching. A charm quark mass \( m_c = 1.5 \text{ GeV} \) is used to regularize the cross section. Effects of nondiagonal CKM matrix elements and off-shell \( W \) boson decays including spin correlations are taken into account in both the \textsc{amc@nlo+py8} (NLO) and \textsc{powhel} calculations. For these comparisons, the renormalization and factorization scales are set to one half of the transverse mass calculated using all final-state partons and leptons, and the \textsc{abmp16_3_nlo} PDF set with \( \alpha_s = 0.118 \) and Monash PyTHIA 8.2 tune are used for both samples. The uncertainty in the direct charm production fractions is assessed using the results from Ref. [54].

Figure 7 shows the measured fiducial cross sections for each of the four channels compared with the theoretical predictions obtained using different NNLO PDF sets, including a PDF set tailored to describe the strangeness of the proton—NNPDF3.1_strange \[12\]. Results for all four channels show a consistent pattern. The experimental precision is comparable to the PDF uncertainties and smaller than the total NLO theory uncertainty. All PDF sets are consistent with the measured cross sections once the combined theory and PDF set uncertainties are considered.

The cross-section ratio, \( R_{W^+D^0} \), is shown for the combined \( D^+ \) and \( D^{+*} \) channel measurements in Fig. 8. This combined result is consistent with theoretical predictions for all PDF sets, although the prediction obtained using NNPDF4.0NNLO shows some tension with the measurement. Unlike the cross-section measurements, which are dominated by systematic uncertainties, the measurements of \( R_{W^+D^0} \) have comparable statistical and systematic uncertainties. PDF set uncertainties for \( R_{W^+D^0} \) fall into two categories. Those sets that impose the restriction that the strange-sea be symmetric \((s = \bar{s})\), such as CT18 and AMB16, predict \( R_{W^+D^0} \) with high precision while PDF fits that allow the \( s \) and \( \bar{s} \) distributions to differ, such as NNPDF or MSHT, have larger uncertainties. These measurements are consistent with the predictions obtained with PDF sets that impose a symmetric \( s-\bar{s} \) sea, suggesting that any \( s-\bar{s} \) asymmetry is small in the Bjorken-\( x \) region probed by this measurement. Reference [15] presents a detailed study of the NLO and NNLO fiducial cross sections for different charm-jet selections. That study uses the same lepton fiducial definition as this paper. While \( W + c \)-jet cross-section calculations cannot be compared with \( \sigma_{\text{OS-SS}}^{\text{OS-SS}}(W + D^{(*)}) \) measurements, they provide insight into the behavior of \( R_{W^+D^0} \). The \( W + c \)-jet \( R_{W^+D^0} \) value calculated at NLO using an OS–SS selection is consistent within statistical uncertainties with that obtained mass-peak shape uncertainties have the most significant pulls in the fit; however, the impact of the corresponding systematic uncertainties on the observables is small (up to 1% for cross sections and negligible for \( R_{W^+D^0} \)). These parameters are constrained by the observed width of the \( D^{(*)} \) peaks in the data. The NP shifts depend on the charge of the \( D^{(*)} \) meson and are therefore treated with independent parameters for each charge. They account for the small residual resolution degradation that is not accounted for in the MC simulation.

Theoretical predictions of the \( W + D^{(*)} \) cross section for a variety of state-of-the-art PDF sets are obtained using the signal \textsc{amc@nlo+py8} (NLO) samples with the configuration described in Sec. III B 1. A finite charm quark mass of \( m_c = 1.55 \text{ GeV} \) is used to regularize the cross section and a full CKM matrix is used to calculate the hard-scattering amplitudes. For each PDF set, the uncertainty is obtained from the alternative generator weights using the \textsc{lhapdf} prescription \[120\]. Uncertainties due to the choice of \textsc{pythia 8} tune are assessed by replacing the A14 tune with the Monash tune \[121\]. Uncertainties associated with the choice of parton-shower model are estimated from a comparison of events generated with the baseline configuration and events generated with \textsc{herwig 7.2} [122] using its default tune. Differences between predictions associated with the choice of NLO matching algorithm are assessed by comparing the \textsc{amc@nlo+py8} (NLO) cross sections with those obtained using the calculation described in Ref. [36]. This calculation is based on the \textsc{powhel} event generator, which uses the \textsc{powheg box v2} interface to implement \textsc{powheg} NLO matching. A charm quark mass \( m_c = 1.5 \text{ GeV} \) is used to regularize the cross section. Effects of nondiagonal CKM matrix elements and off-shell \( W \) boson decays including spin correlations are taken into account in both the \textsc{amc@nlo+py8} (NLO) and \textsc{powhel} calculations. For these comparisons, the renormalization and factorization scales are set to one half of the transverse mass calculated using all final-state partons and leptons, and the \textsc{abmp16_3_nlo} PDF set with \( \alpha_s = 0.118 \) and Monash PyTHIA 8.2 tune are used for both samples. The uncertainty in the direct charm production fractions is assessed using the results from Ref. [54].

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for $W + D^{(*)}$ using MadGraph5_aMC@NLO and the same PDF set (NNPDF3.1). The NNLO+EW(NLO) value of the $W + c$-jet $R_c^2$ is smaller than the NLO value by $\sim 1\%$, but the two are consistent within the quoted $1\%$ statistical uncertainty. The effects of NNLO scale uncertainties on $R_c^2$ are below $0.3\%$. These results suggest that the PDF comparisons presented in Fig. 8 are likely to look similar for a NNLO +EW(NLO) calculation.

The differential cross sections are shown in Figs. 9 and 10, together with the predicted cross sections obtained with different choices of NNLO PDF set. The patterns observed in the $D^+$ and $D^{*+}$ channels are consistent for both the differential $D^{(*)}p_T$ and $|\eta(\ell)|$ distributions. For each $D^{(*)}$ species and charge, the differential distributions are plotted in three separate panels. The top panel compares the measured differential cross section with theoretical
predictions obtained using the same PDF sets as in Fig. 7. Systematic uncertainties in the predictions are correlated between bins and are dominated by uncertainties in the normalization. Differences between PDF sets can be seen more clearly in the middle and lower panels, which show the normalized differential cross sections and the ratio of the predictions to the normalized cross sections, respectively. Because the integral of the normalized cross section across all bins is constrained to be unity, the measurements are highly correlated between bins: If the normalized cross section in one bin increases, that in another bin must decrease.

Variations in the shape of the $p_T(D^{(*)})$ distribution depend only weakly on the choice of PDF. Experimental sensitivity to this dependence is reduced by the presence of $p_T$-dependent systematic uncertainties in the $D^{(*)}$ fiducial...
efficiency. Thus, while measurements of the cross section as a function of \( p_T(D^{+}) \) are an important test of the quality of MC modeling, they do not provide incisive constraints on PDFs. Systematic uncertainties for \( \eta'(\ell) \) are small and highly correlated among bins, providing good sensitivity to PDF variations. Measured differential cross sections have a broader \( \eta'(\ell) \) distribution than the central values of the predictions obtained with any of the PDF sets. The significance of the discrepancy is reduced if the PDF uncertainties are considered.

The compatibility of the measurements and predictions is tested with a \( \chi^2 \) formula using experimental and theory covariance matrices,

\[
\chi^2 = \sum_{i,j}(x_i - \mu_i)(C^{-1})_{ij}(x_j - \mu_j),
\]

where \( x \) are the measured differential cross sections in the ten \( \eta'(\ell) \) bins, and \( \mu \) are the predicted cross sections in the same bin and depend on the choice of PDF set. The total covariance matrix \( C \) is the sum of the experimental covariance matrix, encoding the measurement error, and the theory covariance matrix describing the uncertainties in the theory predictions as described below. The \( \chi^2 \) is then converted to a \( p \)-value assuming 10 degrees of freedom. Experimental covariance matrices are given in Appendix C. The theory covariance matrix corresponding to the PDF uncertainty is calculated following the LHAPDF prescription [120]. Other theory uncertainties are assumed to be 100% correlated across differential bins.

The resulting \( p \)-values for the aMC@NLO predictions of the \( \eta'(\ell) \) differential cross sections with different PDF sets are given in Table XII for the \( D^+ \) channel and in Table XIII.

### Table XII

The \( p \)-values for compatibility of the measurement and the predictions, calculated with the \( \chi^2 \) formula using experimental and theory covariance matrices. The first column shows the \( p \)-values for the \( \eta'(\ell) \) \((D^+)\) differential cross section using only experimental uncertainties. The next columns show \( p \)-values when progressively more theory systematic uncertainties are included. The PDF predictions are based on NLO calculations performed using aMC@NLO and a full CKM matrix: ABMP16_5 [26], ATLASpdf21_T3 [9], CT18A, CT18 [27], MSHT20 [28], PDF4LHC21_40 [29], NNPDF31 [30], NNPDF31_str [12], NNPDF40 [31]. ABMP16_5, ATLASpdf21_T3, CT18A, and CT18 impose symmetric strange-sea PDFs.

| Channel | \( D^+ \, |\eta'(\ell)| \) |
|---------|------------------|
| p-value for PDF (%) | Experimental only | QCD scale | Hadronization and matching | PDF |
| ABMP16_5_nnlo | 7.1 | 11.8 | 12.9 | 19.8 |
| ATLASpdf21_T3 | 9.0 | 9.7 | 11.5 | 84.7 |
| CT18ANNLO | 0.7 | 1.0 | 1.1 | 76.0 |
| CT18NNLO | 1.4 | 6.1 | 6.3 | 87.6 |
| MSHT20nnlo_as118 | 2.7 | 2.9 | 3.3 | 45.6 |
| PDF4LHC21_40 | 3.9 | 5.3 | 5.6 | 75.8 |
| NNPDF31_nnlo_as_0118_hessian | 1.5 | 2.6 | 2.8 | 50.7 |
| NNPDF31_nnlo_as_0118_strange | 9.1 | 14.7 | 15.2 | 59.9 |
| NNPDF40_nnlo_as_01180_hessian | 9.9 | 10.2 | 10.2 | 43.7 |

### Table XIII

The \( p \)-values for compatibility of the measurement and the predictions, calculated with the \( \chi^2 \) formula using experimental and theory covariance matrices. The first column shows the \( p \)-values for the \( \eta'(\ell) \) \((D^+)\) differential cross section using only experimental uncertainties. The next columns show \( p \)-values when progressively more theory systematic uncertainties are included. The PDF predictions are based on NLO calculations performed using aMC@NLO and a full CKM matrix: ABMP16_5 [26], ATLASpdf21_T3 [9], CT18A, CT18 [27], MSHT20 [28], PDF4LHC21_40 [29], NNPDF31 [30], NNPDF31_str [12], NNPDF40 [31]. ABMP16_5, ATLASpdf21_T3, CT18A, and CT18 impose symmetric strange-sea PDFs.

| Channel | \( D^+ \, |\eta'(\ell)| \) |
|---------|------------------|
| p-value for PDF (%) | Experimental only | QCD scale | Hadronization and matching | PDF |
| ABMP16_5_nnlo | 22.8 | 23.7 | 25.0 | 28.8 |
| ATLASpdf21_T3 | 1.9 | 2.9 | 3.4 | 33.7 |
| CT18ANNLO | 6.5 | 6.9 | 7.8 | 47.3 |
| CT18NNLO | 9.4 | 19.2 | 19.7 | 52.8 |
| MSHT20nnlo_as118 | 7.0 | 9.4 | 10.4 | 31.3 |
| PDF4LHC21_40 | 14.2 | 14.2 | 15.2 | 51.4 |
| NNPDF31_nnlo_as_0118_hessian | 5.0 | 5.1 | 5.5 | 34.9 |
| NNPDF31_nnlo_as_0118_strange | 11.4 | 12.4 | 13.2 | 46.0 |
| NNPDF40_nnlo_as_01180_hessian | 4.5 | 6.1 | 6.4 | 36.0 |
for the \( D^{*+} \) channel. The \( p \)-values are calculated with progressively more systematic uncertainties included in the theory covariance matrix, ranging from an “Exp. Only” calculation, where no systematic uncertainties related to the theory predictions are included, to a calculation including all theory uncertainties: QCD scale, “hadronization and matching,” and PDF uncertainties. The hadronization and matching uncertainty is defined to be the quadrature sum of the uncertainty in the charm production fractions, two-point uncertainties associated with the choice of showering program (PYTHIA vs Herwig), the tune (A14 vs Monash), and the matching algorithm (amC@NLO vs POWHEG). These uncertainties are treated as fully correlated between the \( W^+ + D^- \) and \( W^- + D^+ \) channels. Without considering the theory uncertainties (i.e., just comparing the PDF central values with the experimental measurements) the \( p \)-values are below 10\% for all PDFs in the \( D^+ \) channel and most of the PDFs in the \( D^{*+} \) channel. Adding hadronization and QCD scale uncertainties increases the probabilities to at most 15\% in the channel. Adding hadronization and QCD scale uncertainties greatly increases the probabilities to at most 15\% in the \( D^+ \) channel and 25\% in the \( D^{*+} \) channel. Although the QCD scale uncertainty is a large uncertainty in the absolute cross section, it does not change the \( p \)-values significantly because the uncertainty is 100\% correlated between the \( |\eta(\ell')| \) bins, and it does not have a large impact on the shape of the differential distribution. Adding the PDF uncertainties greatly increases the \( p \)-values; the PDF uncertainty has a significant effect on the shape of the differential \( |\eta(\ell')| \) distribution. This suggests that including these measurements in a global PDF fit would provide useful constraints on the allowed PDF variations.

\section{XI. CONCLUSIONS}

Fiducial cross sections for \( W \) boson production in association with a \( D^{(*)} \) meson are measured as a function of \( p_T(D^{(*)}) \) and \( |\eta(\ell')| \) using 140.1 fb\(^{-1} \) of \( \sqrt{s} = 13 \) TeV \( pp \) collision data collected with the ATLAS detector at the Large Hadron Collider. A secondary-vertex fit is used to tag events containing a \( D^+ \) or a \( D^{*+} \) meson and a profile likelihood fit is used to extract the \( W + D^{(*)} \) observables. The single-lepton-species integrated cross sections and cross-section ratios for the fiducial region \( p_T(\ell') > 30 \) GeV, \( |\eta(\ell')| < 2.5 \), \( p_T(D^{(*)}) > 8 \) GeV, and \( |\eta(D^{(*)})| < 2.2 \) are measured to be

\[
\begin{align*}
\sigma_{\text{fid}}^{\text{OS-SS}}(W^- + D^+) &= 50.2 \pm 0.2 \text{(stat)}^{+2.4}_{-2.3} \text{(syst)} \text{ pb}, \\
\sigma_{\text{fid}}^{\text{OS-SS}}(W^+ + D^-) &= 48.5 \pm 0.2 \text{(stat)}^{+2.3}_{-2.2} \text{(syst)} \text{ pb}, \\
\sigma_{\text{fid}}^{\text{OS-SS}}(W^- + D^{*+}) &= 51.1 \pm 0.4 \text{(stat)}^{+1.9}_{-1.8} \text{(syst)} \text{ pb}, \\
\sigma_{\text{fid}}^{\text{OS-SS}}(W^+ + D^{*-}) &= 50.0 \pm 0.4 \text{(stat)}^{+1.9}_{-1.8} \text{(syst)} \text{ pb}, \\
R_\ell(D^{(*)}) &= 0.971 \pm 0.006 \text{(stat)} \pm 0.011 \text{(syst)}. 
\end{align*}
\]

The uncertainty in the measured absolute integrated and differential fiducial cross sections is about 5\% and is dominated by the systematic uncertainty. On the other hand, cross-section ratios and normalized differential cross sections are measured with percent-level precision and have comparable contributions from systematic and statistical uncertainties. The experimental precision of these measurements is comparable to the PDF uncertainties and smaller than the total theory uncertainty.

Measured differential cross sections as a function of \( |\eta(\ell')| \) have a broader distribution than the central values of the predictions. These measurements are, however, consistent with the predictions if the uncertainties associated with the PDF sets are included, indicating that these measurements would provide useful constraints for global PDF fits. The measured values of \( R_\ell^{\pm} \) are consistent with predictions obtained with a range of PDF sets, including those that constrain the \( s-\bar{s} \) sea to be symmetric.

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APPENDIX A: BREAKDOWN OF SYSTEMATIC UNCERTAINTIES IN DIFFERENTIAL BINS

The breakdown of uncertainties in the measured differential fiducial cross sections is summarized in Tables XIV–XVII. The uncertainties in the normalized cross sections are given in parentheses next to the uncertainties in the corresponding absolute cross-sections.

TABLE XIV. Summary of the main systematic uncertainties as percentages of the measured observable for the \( p_T(D^+) \) differential cross sections in the \( D^+ \) channel. The uncertainty in the corresponding normalized cross section is given in parentheses next to the uncertainty in the absolute differential cross section.

<table>
<thead>
<tr>
<th>Uncertainty (%)</th>
<th>( d\sigma^{OS-SS}(W^+ + D^+)/d(p_T(D^+)) )</th>
<th>( d\sigma^{OS-SS}(W^+ + D^+)/d(p_T(D^+)) )</th>
</tr>
</thead>
<tbody>
<tr>
<td>( p_T(D^+) ) bins (GeV)</td>
<td>([8, 12])</td>
<td>([8, 12])</td>
</tr>
<tr>
<td>SV reconstruction</td>
<td>3.1 (1.2)</td>
<td>3.1 (1.2)</td>
</tr>
<tr>
<td>Jets and ( E_T^{miss} )</td>
<td>1.8 (0.8)</td>
<td>1.8 (0.8)</td>
</tr>
<tr>
<td>Luminosity</td>
<td>0.8 (0.8)</td>
<td>0.8 (1.0)</td>
</tr>
<tr>
<td>Muon reconstruction</td>
<td>0.8 (0.2)</td>
<td>0.8 (0.2)</td>
</tr>
<tr>
<td>Electron reconstruction</td>
<td>0.2 (0.0)</td>
<td>0.2 (0.0)</td>
</tr>
<tr>
<td>Multijet background</td>
<td>0.3 (0.2)</td>
<td>0.3 (0.3)</td>
</tr>
<tr>
<td>Signal modeling</td>
<td>1.5 (3.2)</td>
<td>1.5 (3.2)</td>
</tr>
<tr>
<td>Background modeling</td>
<td>1.7 (1.4)</td>
<td>1.7 (1.4)</td>
</tr>
<tr>
<td>Finite size of MC samples</td>
<td>2.3 (1.7)</td>
<td>2.3 (1.7)</td>
</tr>
<tr>
<td>Data statistical uncertainty</td>
<td>1.2 (1.0)</td>
<td>1.2 (1.0)</td>
</tr>
<tr>
<td>Total</td>
<td>5.1 (4.0)</td>
<td>5.1 (4.0)</td>
</tr>
</tbody>
</table>

TABLE XV. Summary of the main systematic uncertainties as percentages of the measured observable for the \( |\eta|/c| \) differential cross sections in the \( D^+ \) channel. The uncertainty in the corresponding normalized cross section is given in parentheses next to the uncertainty in the absolute differential cross section.

| Uncertainty (%) | \( d\sigma^{OS-SS}(W^+ + D^+)/d(|\eta|/c|) \) | \( d\sigma^{OS-SS}(W^+ + D^+)/d(|\eta|/c|) \) |
|------------------|------------------------------------------|------------------------------------------|
| \( |\eta|/c| \) bins | \([0.0, 0.5]\) | \([0.0, 0.5]\) |
| SV reconstruction | 3.2 (0.1) | 3.2 (0.1) |
| Jets and \( E_T^{miss} \) | 1.6 (0.2) | 1.6 (0.2) |
| Luminosity | 0.8 (0.0) | 0.8 (0.0) |
| Muon reconstruction | 0.5 (0.2) | 0.5 (0.2) |
| Electron reconstruction | 0.2 (0.2) | 0.2 (0.2) |
| Multijet background | 0.2 (0.2) | 0.2 (0.2) |
| Signal modeling | 3.2 (0.4) | 3.2 (0.4) |
| Background modeling | 1.5 (0.8) | 1.5 (0.8) |
| Finite size of MC samples | 1.6 (1.3) | 1.6 (1.3) |
| Data statistical uncertainty | 1.0 (0.9) | 1.0 (0.9) |
| Total | 5.5 (1.7) | 5.5 (1.7) |
**TABLE XVI.** Summary of the main systematic uncertainties as percentages of the measured observable for the $p_T(D^*)$ differential cross sections in the $D^*$ channel. The uncertainty in the corresponding normalized cross section is given in parentheses next to the uncertainty in the absolute differential cross section.

<table>
<thead>
<tr>
<th>Uncertainty (%)</th>
<th>$d\sigma_{\text{fid}}^{\text{OS-SS}}(W^- + D^+)/d(p_T(D^*))$ (1/\sigma d\sigma/dp_T)</th>
<th>$d\sigma_{\text{fid}}^{\text{OS-SS}}(\bar{W}^+ + D^-)/d(p_T(D^*))$ (1/\sigma d\sigma/dp_T)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$p_T(D^*)$ bins [GeV]</td>
<td>[8, 12]</td>
<td>[12, 20]</td>
</tr>
<tr>
<td>SV reconstruction</td>
<td>2.4 (0.5) 2.3 (0.3) 2.3 (0.3) 2.4 (1.0) 4.5 (2.8)</td>
<td>2.4 (0.5) 2.3 (0.3) 2.3 (0.4) 2.5 (1.0) 4.8 (2.9)</td>
</tr>
<tr>
<td>Jets and $E_T^{\text{miss}}$</td>
<td>1.5 (0.6) 1.6 (0.5) 1.4 (0.5) 2.0 (1.3) 4.3 (3.2)</td>
<td>1.4 (0.6) 1.8 (0.6) 1.5 (0.4) 1.8 (1.3) 3.9 (3.2)</td>
</tr>
<tr>
<td>Luminosity</td>
<td>0.8 (0.0) 0.8 (0.0) 0.8 (0.0) 0.8 (0.0) 0.8 (0.0)</td>
<td>0.8 (0.0) 0.8 (0.0) 0.8 (0.0) 0.8 (0.0) 0.8 (0.0)</td>
</tr>
<tr>
<td>Muon reconstruction</td>
<td>0.8 (0.2) 0.7 (0.1) 0.6 (0.1) 0.5 (0.4) 0.6 (0.6)</td>
<td>0.8 (0.2) 0.7 (0.1) 0.6 (0.1) 0.5 (0.3) 0.5 (0.5)</td>
</tr>
<tr>
<td>Electron reconstruction</td>
<td>0.2 (0.1) 0.1 (0.2) 0.3 (0.2) 0.4 (0.2) 0.6 (0.4)</td>
<td>0.1 (0.1) 0.1 (0.2) 0.3 (0.2) 0.4 (0.2) 0.6 (0.4)</td>
</tr>
<tr>
<td>Multijet background</td>
<td>0.1 (0.1) 0.1 (0.1) 0.1 (0.1) 0.1 (1.0) 1.0 (1.0)</td>
<td>0.2 (0.1) 0.1 (0.1) 0.1 (0.1) 0.1 (0.1) 0.3 (0.4)</td>
</tr>
<tr>
<td>Signal modeling</td>
<td>3.7 (2.9) 2.6 (1.9) 3.1 (3.5) 3.5 (3.9) 1.2 (0.4)</td>
<td>3.7 (2.8) 2.6 (1.9) 3.1 (3.5) 3.5 (3.9) 1.2 (0.4)</td>
</tr>
<tr>
<td>Signal branching ratio</td>
<td>1.1 (0.0) 1.0 (0.0) 1.1 (0.0) 1.1 (0.0) 1.1 (0.0)</td>
<td>1.0 (0.0) 1.0 (0.0) 1.1 (0.0) 1.1 (0.0) 1.1 (0.0)</td>
</tr>
<tr>
<td>Background modeling</td>
<td>2.2 (1.3) 1.3 (0.6) 1.2 (0.7) 1.2 (0.9) 2.7 (2.2)</td>
<td>1.7 (0.8) 1.5 (0.5) 1.3 (0.7) 1.8 (1.5) 1.9 (1.8)</td>
</tr>
<tr>
<td>Finite size of MC samples</td>
<td>2.6 (1.9) 1.8 (1.4) 1.7 (1.4) 2.6 (2.3) 7.2 (6.9)</td>
<td>2.5 (1.8) 1.9 (1.4) 1.7 (1.4) 2.7 (2.4) 6.3 (6.0)</td>
</tr>
<tr>
<td>Data statistical uncertainty</td>
<td>1.8 (1.4) 1.2 (1.1) 1.1 (1.1) 1.9 (1.8) 5.0 (4.9)</td>
<td>1.9 (1.5) 1.3 (1.1) 1.2 (1.1) 2.0 (2.0) 5.7 (5.7)</td>
</tr>
<tr>
<td>Total</td>
<td>6.0 (3.8) 4.7 (2.7) 4.8 (4.0) 5.8 (5.1) 10.3 (8.9)</td>
<td>5.8 (3.8) 4.8 (2.7) 4.8 (4.0) 6.0 (5.3) 10.4 (9.1)</td>
</tr>
</tbody>
</table>

**TABLE XVII.** Summary of the main systematic uncertainties as percentages of the measured observable for the $|\eta(\ell)|$ differential cross sections in the $D^*$ channel. The uncertainty in the corresponding normalized cross section is given in parentheses next to the uncertainty in the absolute differential cross section.

<table>
<thead>
<tr>
<th>Uncertainty (%)</th>
<th>$d\sigma_{\text{fid}}^{\text{OS-SS}}(W^- + D^+)/d(\eta(\ell))$ (1/\sigma d\sigma/d\eta)</th>
<th>$d\sigma_{\text{fid}}^{\text{OS-SS}}(\bar{W}^+ + D^-)/d(\eta(\ell))$ (1/\sigma d\sigma/d\eta)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$</td>
<td>\eta(\ell)</td>
<td>$ bins</td>
</tr>
<tr>
<td>SV reconstruction</td>
<td>2.4 (0.1) 2.4 (0.0) 2.4 (0.1) 2.5 (0.1) 2.5 (0.2)</td>
<td>2.4 (0.1) 2.5 (0.1) 2.4 (0.2) 2.4 (0.1) 2.4 (0.1)</td>
</tr>
<tr>
<td>Jets and $E_T^{\text{miss}}$</td>
<td>1.4 (0.7) 1.5 (0.4) 1.4 (0.4) 1.6 (0.5) 1.4 (1.0)</td>
<td>1.5 (0.2) 1.5 (0.2) 1.4 (0.2) 1.3 (0.3) 1.1 (0.5)</td>
</tr>
<tr>
<td>Luminosity</td>
<td>0.8 (0.0) 0.8 (0.0) 0.8 (0.0) 0.8 (0.0) 0.8 (0.0)</td>
<td>0.8 (0.0) 0.8 (0.0) 0.8 (0.0) 0.8 (0.0) 0.8 (0.0)</td>
</tr>
<tr>
<td>Muon reconstruction</td>
<td>0.5 (0.2) 0.6 (0.1) 0.8 (0.1) 0.8 (0.1) 0.8 (0.2)</td>
<td>0.5 (0.2) 0.6 (0.1) 0.8 (0.1) 0.8 (0.1) 0.9 (0.2)</td>
</tr>
<tr>
<td>Electron reconstruction</td>
<td>0.2 (0.1) 0.2 (0.0) 0.3 (0.0) 0.4 (0.1) 0.3 (0.1)</td>
<td>0.2 (0.1) 0.3 (0.0) 0.3 (0.1) 0.3 (0.1) 0.3 (0.1)</td>
</tr>
<tr>
<td>Multijet background</td>
<td>0.1 (0.1) 0.1 (0.1) 0.1 (0.1) 0.2 (0.2) 0.2 (0.2)</td>
<td>0.1 (0.1) 0.1 (0.1) 0.1 (0.1) 0.1 (0.1) 0.2 (0.2)</td>
</tr>
<tr>
<td>Signal modeling</td>
<td>1.1 (2.7) 2.0 (0.2) 4.6 (2.7) 1.8 (0.4) 2.6 (0.7)</td>
<td>1.1 (2.7) 2.1 (0.2) 4.5 (2.7) 1.8 (0.4) 2.6 (0.8)</td>
</tr>
<tr>
<td>Signal branching ratio</td>
<td>1.1 (0.0) 1.0 (0.0) 1.0 (0.0) 1.1 (0.0) 1.1 (0.0)</td>
<td>1.1 (0.0) 1.0 (0.0) 1.0 (0.0) 1.0 (0.0) 1.1 (0.0)</td>
</tr>
<tr>
<td>Background modeling</td>
<td>1.4 (0.6) 1.8 (1.0) 1.5 (0.8) 1.7 (1.0) 1.1 (0.7)</td>
<td>1.4 (0.7) 1.8 (1.0) 1.3 (0.7) 1.7 (1.1) 1.6 (0.9)</td>
</tr>
<tr>
<td>Finite size of MC samples</td>
<td>1.9 (1.6) 1.9 (1.6) 2.2 (1.8) 2.6 (2.2) 3.3 (2.9)</td>
<td>1.8 (1.5) 1.9 (1.6) 2.1 (1.8) 2.7 (2.3) 3.8 (3.3)</td>
</tr>
<tr>
<td>Data statistical uncertainty</td>
<td>1.4 (1.3) 1.5 (1.3) 1.6 (1.5) 1.8 (1.6) 2.2 (2.0)</td>
<td>1.4 (1.3) 1.5 (1.3) 1.7 (1.5) 2.0 (1.8) 2.5 (2.3)</td>
</tr>
<tr>
<td>Total</td>
<td>4.1 (3.5) 4.6 (2.2) 6.2 (3.6) 5.0 (2.8) 5.5 (3.5)</td>
<td>4.1 (3.4) 4.7 (2.2) 6.2 (3.6) 5.0 (3.0) 6.0 (4.0)</td>
</tr>
</tbody>
</table>
**APPENDIX B: DIFFERENTIAL CROSS-SECTION TABLES**

The measured differential cross sections in bins of \( p_T(D^+) \) and \(|\eta(\ell)|\) are shown in Tables XVIII–XXI for the \( D^+ \) and \( D^* \) channels.

### Table XVIII. Measured \( p_T(D^+) \) differential fiducial cross section times the single-lepton-flavor W branching ratio in the \( W + D^+ \) channel. The displayed cross sections are integrated over each differential bin.

<table>
<thead>
<tr>
<th>( p_T(D^+) ) (GeV)</th>
<th>( \int \frac{d\sigma^{OS-SS}(W^- + D^+)}{d\sigma^{OS-SS}(W^+ + D^+)} / d(p_T(D^+)) ) (pb)</th>
<th>( 1/\sigma \int \frac{d\sigma^{OS-SS}(W^- + D^+)}{d\sigma^{OS-SS}(W^+ + D^+)} / d(p_T(D^+)) )</th>
</tr>
</thead>
<tbody>
<tr>
<td>[8, 12]</td>
<td>15.04 ± 0.19(stat) +0.76 -0.27 (syst)</td>
<td>0.2994 ± 0.0020(stat) +0.0117 -0.0116 (syst)</td>
</tr>
<tr>
<td>[12, 20]</td>
<td>15.34 ± 0.14(stat) +0.75 -0.25 (syst)</td>
<td>0.3054 ± 0.0026(stat) +0.0052 -0.0050 (syst)</td>
</tr>
<tr>
<td>[20, 40]</td>
<td>13.78 ± 0.12(stat) +0.92 -0.85 (syst)</td>
<td>0.2744 ± 0.0024(stat) +0.0088 -0.0087 (syst)</td>
</tr>
<tr>
<td>[40, 80]</td>
<td>5.13 ± 0.07(stat) +0.34 -0.31 (syst)</td>
<td>0.1021 ± 0.0014(stat) +0.0038 -0.0036 (syst)</td>
</tr>
<tr>
<td>[80, ( \infty )]</td>
<td>0.93 ± 0.04(stat) +0.09 -0.08 (syst)</td>
<td>0.0186 ± 0.0007(stat) +0.0014 -0.0013 (syst)</td>
</tr>
</tbody>
</table>

### Table XIX. Measured \(|\eta(\ell)|\) differential fiducial cross section times the single-lepton-flavor W branching ratio in the \( W + D^+ \) channel. The displayed cross sections are integrated over each differential bin.

| \(|\eta(\ell)|\) | \( \int \frac{d\sigma^{OS-SS}(W^- + D^+)}{d(\eta(\ell))} / d(p_T(D^+)) \) (pb) | \( 1/\sigma \int \frac{d\sigma^{OS-SS}(W^- + D^+)}{d(\eta(\ell))} / d(p_T(D^+)) \) |
|-----------------|---------------------------------|---------------------------------|
| [0.0, 0.5]      | 12.27 ± 0.13(stat) +0.61 -0.61 (syst) | 0.2446 ± 0.0023(stat) +0.0036 -0.0036 (syst) |
| [0.5, 1.0]      | 11.57 ± 0.12(stat) +0.61 -0.61 (syst) | 0.2305 ± 0.0022(stat) +0.0040 -0.0040 (syst) |
| [1.0, 1.5]      | 10.41 ± 0.12(stat) +0.61 -0.61 (syst) | 0.2075 ± 0.0022(stat) +0.0042 -0.0042 (syst) |
| [1.5, 2.0]      | 9.09 ± 0.11(stat) +0.43 -0.43 (syst) | 0.1810 ± 0.0020(stat) +0.0044 -0.0044 (syst) |
| [2.0, 2.5]      | 6.85 ± 0.11(stat) +0.37 -0.37 (syst) | 0.1365 ± 0.0020(stat) +0.0036 -0.0036 (syst) |

### Table XX. Measured \( p_T(D^{*+}) \) differential fiducial cross section times the single-lepton-flavor W branching ratio in the \( W + D^{*+} \) channel. The displayed cross sections are integrated over each differential bin.

<table>
<thead>
<tr>
<th>( p_T(D^{*+}) ) (GeV)</th>
<th>( \int \frac{d\sigma^{OS-SS}(W^- + D^{<em>+})}{d\sigma^{OS-SS}(W^+ + D^{</em>+})} / d(p_T(D^{*+})) ) (pb)</th>
<th>( 1/\sigma \int \frac{d\sigma^{OS-SS}(W^- + D^{<em>+})}{d\sigma^{OS-SS}(W^+ + D^{</em>+})} / d(p_T(D^{*+})) )</th>
</tr>
</thead>
<tbody>
<tr>
<td>[8, 12]</td>
<td>14.50 ± 0.26(stat) +0.85 -0.79 (syst)</td>
<td>0.2839 ± 0.0041(stat) +0.0102 -0.0102 (syst)</td>
</tr>
<tr>
<td>[12, 20]</td>
<td>15.88 ± 0.19(stat) +0.73 -0.69 (syst)</td>
<td>0.3110 ± 0.0034(stat) +0.0075 -0.0075 (syst)</td>
</tr>
<tr>
<td>[20, 40]</td>
<td>14.19 ± 0.16(stat) +0.65 -0.61 (syst)</td>
<td>0.2779 ± 0.0030(stat) +0.0095 -0.0095 (syst)</td>
</tr>
<tr>
<td>[40, 80]</td>
<td>5.42 ± 0.10(stat) +0.31 -0.29 (syst)</td>
<td>0.1062 ± 0.0019(stat) +0.0045 -0.0045 (syst)</td>
</tr>
<tr>
<td>[80, ( \infty )]</td>
<td>1.07 ± 0.05(stat) +0.10 -0.09 (syst)</td>
<td>0.0209 ± 0.0010(stat) +0.0016 -0.0016 (syst)</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>( p_T(D^{*+}) ) (GeV)</th>
<th>( \int \frac{d\sigma^{OS-SS}(W^- + D^{<em>+})}{d\sigma^{OS-SS}(W^+ + D^{</em>+})} / d(p_T(D^{*+})) ) (pb)</th>
<th>( 1/\sigma \int \frac{d\sigma^{OS-SS}(W^- + D^{<em>+})}{d\sigma^{OS-SS}(W^+ + D^{</em>+})} / d(p_T(D^{*+})) )</th>
</tr>
</thead>
<tbody>
<tr>
<td>[8, 12]</td>
<td>14.26 ± 0.27(stat) +0.82 -0.78 (syst)</td>
<td>0.2849 ± 0.0043(stat) +0.0100 -0.0100 (syst)</td>
</tr>
<tr>
<td>[12, 20]</td>
<td>15.60 ± 0.20(stat) +0.74 -0.70 (syst)</td>
<td>0.3118 ± 0.0036(stat) +0.0076 -0.0076 (syst)</td>
</tr>
<tr>
<td>[20, 40]</td>
<td>14.08 ± 0.17(stat) +0.68 -0.64 (syst)</td>
<td>0.2814 ± 0.0032(stat) +0.0070 -0.0070 (syst)</td>
</tr>
<tr>
<td>[40, 80]</td>
<td>5.11 ± 0.10(stat) +0.28 -0.28 (syst)</td>
<td>0.1022 ± 0.0020(stat) +0.0050 -0.0050 (syst)</td>
</tr>
<tr>
<td>[80, ( \infty )]</td>
<td>0.99 ± 0.06(stat) +0.09 -0.08 (syst)</td>
<td>0.0197 ± 0.0011(stat) +0.0017 -0.0017 (syst)</td>
</tr>
</tbody>
</table>
TABLE XXI. Measured $|\eta(\ell)|$ differential fiducial cross section times the single-lepton-flavor \(W\) branching ratio in the \(W + D^{(*)}\) channel. The displayed cross sections are integrated over each differential bin.

| $|\eta(\ell)|$ | \(\int d\sigma_{\text{fid}}^{\text{OS-SS}}(W^- + D^{(*)})/d(|\eta(\ell)|)\) (pb) | \(1/\sigma \int d\sigma_{\text{fid}}^{\text{OS-SS}}(W^- + D^{(*)})/d(|\eta(\ell)|)\) |
|-------------|----------------------------------|----------------------------------|
| [0.0, 0.5]  | 12.18 ± 0.18(stat) ±0.48(syst)   | 0.2405 ± 0.0031(stat) ±0.0078(syst) |
| [0.5, 1.0]  | 11.77 ± 0.17(stat) ±0.53(syst)   | 0.2325 ± 0.0031(stat) ±0.0042(syst) |
| [1.0, 1.5]  | 10.61 ± 0.17(stat) ±0.67(syst)   | 0.2095 ± 0.0031(stat) ±0.0065(syst) |
| [1.5, 2.0]  | 8.85 ± 0.16(stat) ±0.40(syst)    | 0.1748 ± 0.0029(stat) ±0.0039(syst) |
| [2.0, 2.5]  | 7.22 ± 0.16(stat) ±0.36(syst)    | 0.1427 ± 0.0028(stat) ±0.0040(syst) |

\[ \int d\sigma_{\text{fid}}^{\text{OS-SS}}(W^{+} + D^{(*)})/d(|\eta(\ell)|) \] (pb) \[ 1/\sigma \int d\sigma_{\text{fid}}^{\text{OS-SS}}(W^{+} + D^{(*)})/d(|\eta(\ell)|) \]

\begin{align*}
[0.0, 0.5] & \quad 12.52 ± 0.18(stat) ±0.50(syst) \\
[0.5, 1.0] & \quad 12.14 ± 0.18(stat) ±0.52(syst) \\
[1.0, 1.5] & \quad 10.29 ± 0.18(stat) ±0.58(syst) \\
[1.5, 2.0] & \quad 8.38 ± 0.16(stat) ±0.39(syst) \\
[2.0, 2.5] & \quad 6.55 ± 0.16(stat) ±0.37(syst) \\
\end{align*}

\(\int d\sigma_{\text{fid}}^{\text{OS-SS}}(W^{-} + D^{(*)})/d(|\eta(\ell)|)\)

\(1/\sigma \int d\sigma_{\text{fid}}^{\text{OS-SS}}(W^{-} + D^{(*)})/d(|\eta(\ell)|)\)

\begin{align*}
[0.0, 0.5] & \quad 12.52 ± 0.18(stat) ±0.50(syst) \\
[0.5, 1.0] & \quad 12.14 ± 0.18(stat) ±0.52(syst) \\
[1.0, 1.5] & \quad 10.29 ± 0.18(stat) ±0.58(syst) \\
[1.5, 2.0] & \quad 8.38 ± 0.16(stat) ±0.39(syst) \\
[2.0, 2.5] & \quad 6.55 ± 0.16(stat) ±0.37(syst) \\
\end{align*}

APPENDIX C: THE MEASUREMENT COVARIANCE MATRICES

Covariance matrices encoding the measurement error associated with the differential \(W + D^{(*)}\) cross-section measurement are given in Figs. 11–13. Covariance matrices are given separately for the \(D^+\) and \(D^-\) channels and separately for \(p_T(D^{(*)})\) categories.
and $|\eta(\ell)|$ differential bins. Covariance matrices encoding only the statistical uncertainty are given in Fig. 11. Figure 12 includes the full set of measurement uncertainties with postfit values of the nuisance parameters and Fig. 13 shows the covariance matrix with prefit values of the nuisance parameters.

FIG. 12. The combined statistical and systematic uncertainty covariance matrix for the differential $W + D^{(*)}$ fits: (a) $D^+ p_T(D^{(*)})$ fit, (b) $D^+ |\eta(\ell)|$ fit, (c) $D^+ p_T(D^{(*)})$ fit, and (d) $D^+ |\eta(\ell)|$ fit. The systematic uncertainties are evaluated with the postfit values of the nuisance parameters, corresponding to the measured differential cross sections.
FIG. 13. The combined statistical and systematic uncertainty covariance matrix for the differential $W + D^{(*)}$ fits: (a) $D^{+} p_{T}(D^{(*)})$ fit, (b) $D^{+} |\eta(\ell)|$ fit, (c) $D^{+} p_{T}(D^{(*)})$ fit, and (d) $D^{+} |\eta(\ell)|$ fit. The systematic uncertainties are evaluated with the prefit values of the nuisance parameters.


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