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Glycolysis in Bloodstream Form Trypanosoma brucei Can Be Understood in Terms of the Kinetics of the Glycolytic Enzymes*

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In trypanosomes the first part of glycolysis takes place in specialized microbodies, the glycosomes. Most glycolytic enzymes of Trypanosoma brucei have been purified and characterized kinetically. In this paper a mathematical model of glycolysis in the bloodstream form of this organism is developed on the basis of all available kinetic data. The fluxes and the cytosolic metabolite concentrations as predicted by the model were in accordance with available data as measured in non-growing trypanosomes, both under aerobic and under anaerobic conditions. The model also reproduced the inhibition of anaerobic glycolysis by glyceraldehyde, although the amount of glyceraldehyde needed to inhibit glycolysis completely was lower than experimentally determined. At low extracellular glucose concentrations the intracellular glucose concentration remained very low, and only at 5 mM of extracellular glucose, free glucose started to accumulate intracellularly, in close agreement with experimental observations. This biphasic relation could be related to the large difference between the affinities of the glucose transporter and hexokinase for intracellular glucose. The calculated intraglycosomal metabolite concentrations demonstrated that enzymes that have been shown to be near-equilibrium in the cytosol must work far from equilibrium in the glycosome in order to maintain the high glycolytic flux in the latter.

In several respects glycolysis in trypanosomes differs from glycolysis in other eukaryotes. In these parasites most glycolytic enzymes occur sequestered in a specialized organelle closely related to peroxisomes (1) (for reviews see Refs. 2–5). As in trypanosomes 90% of the protein content of these microbodies consists of glycolytic enzymes; they are called glycosomes. In glycosomes glucose is converted to 3-phosphoglycerate (3-PGA), 1 which is metabolized to pyruvate in the cytosol. The NADH produced in the glycosomes by glyceraldehyde-3-phosphate dehydrogenase (GAPDH) is used to reduce dihydroxyacetone phosphoglycerate (DHAP) to glycerol 3-phosphate (Gly-3-P). Subsequently, Gly-3-P is reoxidized by molecular oxygen via a glycerol-3-phosphate oxidase (GPO) in the mitochondria, and DHAP returns to the glycosomes. In the organelles there is no net ATP production or consumption by glycolysis, since the consumption of ATP by hexokinase (HK) and phosphofructokinase (PFK) is balanced by phosphoglycerate kinase (PGK). Only in the cytosol there is net glycolytic ATP production by pyruvate kinase (PYK). Under anaerobic conditions Gly-3-P is converted to glycerol with the concomitant production of ATP via the reverse reaction of glycerol kinase (GK) (1, 2, 6, 7). Unlike the corresponding enzymes in most other organisms, the glycosomal HK and PFK of trypanosomes are hardly subject to allosteric regulation (8–10). In trypanosomes not PFK but PYK is activated by fructose 2,6-bisphosphate (11–13), and consistently, 6-phosphofructo-2-kinase and fructose-2,6-bisphosphatase are found in the cytosol (14).

Trypanosoma brucei, the parasite that causes African sleeping disease in humans and nagana in livestock, is transmitted by the tse-tse fly. When living in the mammalian bloodstream Trypanosoma brucei has neither a functional Krebs cycle nor oxidative phosphorylation nor does it store any carbohydrates. Consequently, complete inhibition of glycolysis kills the organism. Because of the differences between mammalian and trypanosomal glycolysis, this pathway is a major potential target for drugs against the African sleeping disease (15). Many of the glycolytic enzymes of trypanosomes resemble, however, the corresponding enzymes of the hosts of the latter. A drug that interferes strongly with trypanosome glycolysis may well compromise this metabolic pathway in its host where glycolysis is also essential. Consequently, it is important to design drugs that strongly inhibit glycolysis in trypanosomes but only weakly that of their hosts. This design task is complicated by the fact that the effect of modulation of an enzyme activity on a metabolic flux also depends on the properties of other enzymes in the metabolic pathway (16–18). Nevertheless, recent developments may well bring such rational drug design within reach. In the past decade most glycolytic enzymes of T. brucei have been purified and characterized extensively, both structurally and kinetically. Furthermore, fluxes and glycolytic in-

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1 The abbreviations used are: 3-PGA, 3-phosphoglycerate; AK, adenylate kinase; ALD, fructose-1,6-bisphosphate aldolase; 1,3-BPGA, 1,3-bisphosphoglycerate; DHAP, dihydroxyacetone phosphate; ENO, enolase; Fru-1,6-BP, fructose 1,6-bisphosphate; Fru-6-P, fructose 6-phosphate; Glc, glucose; G, ratio of product and substrate concentrations; GA-3-P, glyceraldehyde-3-phosphate; GAPDH, glyceraldehyde-3-phosphate dehydrogenase; GDH, glycerol-3-phosphate dehydrogenase; GK, glycerol kinase; Gly-3-P, glycerol 3-phosphate; G-6-P, glucose 6-phosphate; GPO, glycerol-3-phosphate oxidase; HK, hexokinase; [Glc]c, intracellular glucose; Kequil, equilibrium constant; kcat, turnover rate; Km, Michaelis constant; [Glc]o, extracellular glucose; PEP, phosphoenolpyruvate; 2-PGA, 2-phosphoglycerate; PGI, glucose-phosphate isomerase; PFK, phosphofructokinase; PFKP, phosphoglycerate kinase; PGM, phosphoglycerate mutase; PYK, pyruvate kinase; TIM, triose-phosphate isomerase.

This paper is available on line at http://www-jbc.stanford.edu/jbc/
Modeling Trypanosome Glycolysis

Stoichiometry and Conserved Moieties—The model contains the glycolytic pathway, including the branch to glycerol and the utilization of ATP (Fig. 1). The two glucose transport steps, i.e., across the plasma membrane and the glycosomal membrane, were lumped into one, because in kinetic experiments no distinction between them has been made so far (23). The glycosomal membrane was taken to be impermeable to metabolites (24), except for those that need to be transported across this membrane (Fig. 1). Nothing is known about the kinetics of the transport of 3-PGA, Gly-3-P, and DHAP. These steps were assumed to be in equilibrium and mutually independent. The concentration of inorganic phosphate in the glycosome was assumed to be saturating. At steady state adenylate kinase (AK) should be at equilibrium. When the known kinetics of glucose-phosphate isomerase (PGI) (25) and triose-phosphate isomerase (TIM) (26) were implemented explicitly, these enzymatic steps were closer to equilibrium (the ratio of the steady-state product and substrate concentrations divided by the equilibrium constant exceeded 0.8 for both reactions), and therefore, they were further treated as equilibrium reactions. This facilitated the calculations with hardly any effect on the outcome. Experimentally it has been shown that the cytosolic enzymes phosphoglycerate mutase (PGM) and enolase (ENO) operate near equilibrium (27). Accordingly, they were treated as if in equilibrium. Finally, the transport of glycerol out of the cells was assumed to be in equilibrium. The kinetics of all other enzymes and the transport of glucose and pyruvate were implemented explicitly in the model.

Four moiety conservation relations were derived from the stoichiometry as depicted in Fig. 1 by using the metabolic modeling program SCAMP (28). These correspond to the adenine nucleotides in the glycosome and the cytosol, respectively, the nicotinamide adenine dinucleotides in the glycosome, and the organic phosphate that is not exchanged with inorganic phosphate. None of the reactions modifies these sums:

\[
[\text{ATP}]_c + [\text{ADP}]_c + [\text{AMP}]_c = C_1 \quad (\text{Eq. 1})
\]

\[
[\text{ATP}]_g + [\text{ADP}]_g + [\text{AMP}]_g = C_2 \quad (\text{Eq. 2})
\]

\[
[\text{NADH}]_c + [\text{NAD}]_c = C_3 \quad (\text{Eq. 3})
\]

\[
[\text{Gly-3-P}]_c + [\text{Gly-3-P}]_g + [\text{DHAP}]_c + [\text{DHAP}]_g + [\text{Glc-6-P}]_c + [\text{Glc-6-P}]_g + [\text{Fru-6-P}]_c + [\text{Fru-6-P}]_g + [\text{ADP}]_c + [\text{ADP}]_g + [\text{AMP}]_c + [\text{AMP}]_g = C_4 \quad (\text{Eq. 4})
\]

The \([\text{ }]_c\) refers to the cytosolic concentration and the \([\text{ }]_g\) to the glycosomal concentration. \(V_c\) is the cytosolic volume and \(V_g\) the glycosomal volume in \(\mu\)l per mg of cell protein. In Equation 4 the concentrations of

\[
[\text{Gly-3-P}]_c + [\text{DHAP}]_c \left(1 + \frac{V_g}{V_c}\right) + [\text{Glc-6-P}]_c + [\text{Fru-6-P}]_c + [\text{Glc-6-P}]_g + [\text{Fru-6-P}]_g + 2[\text{ADP}]_c + [\text{ATP}]_c = C_4
\]

in which

\[
[\text{Gly-3-P}] = [\text{Gly-3-P}]_c = [\text{Gly-3-P}]_g \quad (\text{Eq. 6})
\]

and

\[
[\text{DHAP}] = [\text{DHAP}]_c = [\text{DHAP}]_g \quad (\text{Eq. 7})
\]

The two distinct pools of adenine nucleotides occur as a consequence of the assumed impermeability of the glycosomal membrane for these compounds. The fourth conserved moiety (Equations 4 and 5) is also a consequence of the compartmentation. If glycolysis occurred in one compartment, ATP utilization (Reaction 18 in Fig. 1), for example, would modify this sum. As the glycosomes occupy 4.3% of the total cellular volume (29), the ratio \(V_g/V_c\) amounts to 22.3. \(C_2\) and \(C_4\) were estimated from Ref. 27, by using that 1 g wet weight corresponds to 80 mg of protein and 1 ml of total cellular volume corresponds to 175 mg of
The $V_{\text{max}}$ values of the glycosomal enzymes were derived from the reported glycosomal enzyme concentrations and from the turnover rates ($k_{\text{cat}}$) reported after in vitro measurements. Other $V_{\text{max}}$ values were based on reported transport and activity assays. The $V_{\text{max}}$ of pyruvate transport was estimated as described in the text.

<table>
<thead>
<tr>
<th>Enzyme</th>
<th>Concentration (% of cell protein)</th>
<th>$k_{\text{cat}}$ (µmol min$^{-1}$ (mg enzyme$^{-1}$))</th>
<th>$V_{\text{max}}$ (nmol min$^{-1}$ (mg cell protein$^{-1}$))</th>
</tr>
</thead>
<tbody>
<tr>
<td>Glucose transport</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>HK</td>
<td>0.25</td>
<td>250$^a$</td>
<td>106.2 (23)</td>
</tr>
<tr>
<td>PFK</td>
<td>0.39</td>
<td>200 (10)</td>
<td>625</td>
</tr>
<tr>
<td>ALD</td>
<td>1.23</td>
<td>15 (35)</td>
<td>184.5</td>
</tr>
<tr>
<td>GAPDH</td>
<td>0.50</td>
<td>294 (48)</td>
<td>1470</td>
</tr>
<tr>
<td>PGK</td>
<td>0.16</td>
<td>400 (49)</td>
<td>640</td>
</tr>
<tr>
<td>PYK</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>GDH</td>
<td>0.25</td>
<td>170$^b$</td>
<td>425</td>
</tr>
<tr>
<td>GPO</td>
<td></td>
<td></td>
<td>368 or 0$^c$ (50)</td>
</tr>
<tr>
<td>GK</td>
<td></td>
<td></td>
<td>0 or 200$^c$</td>
</tr>
<tr>
<td>Pyruvate transport</td>
<td></td>
<td></td>
<td>160</td>
</tr>
</tbody>
</table>

* A.-M. Loiseau, unpublished results.
* M. Callens, D. Kuntz, O. Bos, and F. Opperman, unpublished results.
* To simulate aerobic conditions GK was switched off ($V_{\text{max}} = 0$) and to simulate anaerobic conditions GPO was switched off (see "Substrate and Product Concentrations").
* The $V_{\text{max}}$ of GPO was expressed as nmol Gly-3-P min$^{-1}$ (mg cell protein$^{-1}$). Two molecules of Gly-3-P are converted per molecule of O$_2$.

The total cell protein (29). $C_1$ and $C_2$ were chosen arbitrarily, but their values hardly affected the results. The values for $C_1 = 3.9$ mM, $C_2 = 3.9$ mM, $C_3 = 4$ mM, and $C_4 = 120$ mM. This value for $C_3$ is high, because [Gly-3-P] and [DHAP] are multiplied by the factor $1 + V/V'$. Only when [Gly-3-P] and [DHAP] become low, this high sum implies high concentrations of the glycosomal metabolites. This did not occur in the simulations reported in this paper (results not shown).

Kinetic Equations—All available literature data (Tables I and II) on trypanosome enzyme kinetics have been obtained at 25°C, except for glucose transport (27°C) (23).

The kinetics of GPO and the transport of pyruvate across the plasma membrane were described by irreversible Michaelis-Menten kinetics:

\[
V = V' \cdot \frac{S}{K_S + \frac{S}{K_S}} \quad \text{(Eq. 8)}
\]

in which $S$ is the substrate concentration. The measured rate of zero-trans pyruvate influx was well below the steady-state rate of pyruvate production (30). This may be due to asymmetry of the transporter, but most probably the long time scale of the uptake assay (30 s) (30) also led to an underestimation of the rate, because pyruvate cannot be metabolized and accumulates. Therefore the $V_{\text{max}}$ for efflux was adjusted so that the pyruvate concentration in the model agreed with the measured intracellular pyruvate concentration of 21 mM (31).

The kinetics of HK were described by a Michaelis-Menten type equation for two non-competing product-substrate couples:

\[
V = V' \cdot \frac{S_1}{K_S_1 + \frac{S_1}{K_S_1}} \cdot \frac{S_2}{K_S_2 + \frac{S_2}{K_S_2}} \quad \text{(Eq. 9)}
\]

in which $S_1$ is ATP, $S_2$ is intracellular glucose, and $P_1$ is ADP. Thus the competitive product inhibition by ADP was included. Glucose 6-phosphatase (Glc-6-P) had no effect on the rate (8).

The kinetics of GAPDH, PGK, glycerol-3-phosphate dehydrogenase (GDH), and GK were described by a reversible Michaelis-Menten equation for two non-competing product-substrate couples:

\[
V = V' \cdot \frac{S_1}{K_S_1 + \frac{S_1}{K_S_1}} \cdot \frac{S_2}{K_S_2 + \frac{S_2}{K_S_2}} \quad \text{(Eq. 10)}
\]

The transport of glucose was described according to a 4-state model for a facilitated diffusion carrier (32). The experimental data (33) may indicate that the carrier is slightly asymmetric. However, the $V_{\text{max}}$ measured for efflux is lower than that for influx, whereas the $V_{\text{max}}$ for efflux is higher. As this would lead to a net flux in the absence of a glucose gradient, the apparent asymmetry was neglected. Rewritten into a Michaelis-Menten-like form the equations became:

\[
V_{\text{glucose transport}} = V' \cdot \frac{[\text{Glc}]_o - [\text{Glc}]_i}{K_{\text{Glc}} + [\text{Glc}]_o + \alpha \cdot [\text{Glc}]_i \cdot [\text{Glc}]_o/K_{\text{Glc}}} \quad \text{(Eq. 11)}
\]

in which $[\text{Glc}]_o$ and $[\text{Glc}]_i$ are the extracellular and intracellular glucose concentrations, respectively, and $K_{\text{Glc}}$ is 2 mM (23). From the assumed symmetry of the carrier and from the finding that the $V_{\text{max}}$ for equilibrium exchange was twice as high as the $V_{\text{max}}$ for zero trans-efflux, the factor $\alpha$ was calculated to be 0.75.

The rate of PKF exhibits a slightly cooperative dependence on the concentration of fructose 6-phosphate (Fru-6-P):

\[
P_{\text{PKF}} = V' \cdot \frac{(\text{Fru-6-P})^n}{K_{\text{Fru-6-P}}^n + (\text{Fru-6-P})^n} \cdot \frac{(\text{ATP})^n}{K_{\text{ATP}}^n + (\text{ATP})^n} \quad \text{(Eq. 12)}
\]

in which $K_{\text{Fru-6-P}} = 0.82$ mM, $K_{\text{ATP}} = 2.6 \cdot 10^{-2}$ mM, and $n = 1.2$ (9, 10).

The rate of PKY depends cooperatively on the concentration of PEP:

\[
P_{\text{PKY}} = V' \cdot \frac{(\text{PEP})^n}{K_{\text{PEP}}^n + (\text{PEP})^n} \cdot \frac{(\text{ADP})^n}{K_{\text{ADP}}^n + (\text{ADP})^n} \quad \text{(Eq. 13)}
\]

in which $K_{\text{PEP}} = 0.34(1 + [\text{ATP}]_o/0.57 + [\text{ADP}]_o/0.64)$ mM, $K_{\text{ADP}} = 0.114$ mM and $n = 2.6$ (12, 13). The equation for $K_{\text{PEP}}$ was fitted to the measurements of this parameter at different concentrations of ATP and ADP (12). Variable activation of PKY by fructose 2,6-bisphosphate (12) was neglected, as the concentration of this compound was largely saturating in bloodstream form trypanosomes in the presence of glucose (14), and consequently it is unlikely that it plays a regulatory role under these conditions.

Aldolase (ALD) works according to an ordered uni-bi mechanism. Glyceraldehyde 3-phosphate (GA-3-P) dissociates from the enzyme before DHAP does (34, 35). The rate equation reads:

\[
P_{\text{ALD}} = V' \cdot \frac{[\text{Fru-6-P}]^n [\text{GA-3-P}] [\text{DHAP}]}{K_{\text{Fru-6-P}}^n [\text{GA-3-P}] [\text{DHAP}] + (1 + [\text{Fru-6-P}]^n + [\text{GA-3-P}] [\text{DHAP}])} \quad \text{(Eq. 14)}
\]

in which $V'/V = 1.19, K_{\text{Fru-6-P}} = 9.1 \cdot 10^{-3} (1 + [\text{ATP}]_o/0.68 + [\text{ADP}]_o/1.51 + [\text{AMP}]_o/3.65)$ mM, $K_{\text{GA-3-P}} = 6.7 \cdot 10^{-2}$ mM, $K_{\text{DHAP}} = 1.5 \cdot 10^{-2}$ mM, and $K_{\text{GA-3-P}} = 9.8 \cdot 10^{-2}$ mM (35).
The sum of triose phosphates is of the system, which means that they were fixed for each steady-state. This rate equation corresponds to a far-from-equilibrium Michaelis-Menten-type kinetics. A pool \( [N] \) was defined by

\[
[N] = \frac{[3 - \text{PGA}][V_e + V_c] + [2 - \text{PGA}]V_c + [\text{PEP}]V_c}{V_{\text{tot}}}.
\]  

(Taken from the extracellular and the intracellular concentrations of glycerol were set to zero. The extracellular concentration of pyruvate and both \( \text{[ATP]} \) and \( \text{[ADP]} \) ratios were measured ratios. Equation 15 should not be extrapolated to very high concentrations it was reversed. If one were to allow free accumulation of glyceral, the rate under anaerobic conditions was twice the rate under aerobic conditions (38). As the relation between the rate of ATP utilization and the \( \text{[ATP]}/\text{[ADP]} \) ratio seemed close to linear, we assumed

\[
v_{\text{ATP utilization}} = \frac{k}{\text{[ATP]}} \cdot \frac{\text{[ADP]}}{[\text{ADP}]}
\]  

(Eq. 15)

This rate equation corresponds to a far-from-equilibrium Michaelis-Menten reaction with dominant product inhibition. The value of \( k \) was adjusted to 50 nmol min \(^{-1} \) mg protein \(^{-1} \), so that the calculated steady-state \( \text{[ATP]}/\text{[ADP]} \) ratio under aerobic conditions corresponded to the measured ratio. Equation 15 should not be extrapolated to very high \( \text{[ATP]}/\text{[ADP]} \) ratios.

**Substrate and Product Concentrations**—The extracellular concentrations of glucose, \( O_2 \), pyruvate, and glycerol were treated as parameters of the system, which means that they were fixed for each steady-state calculation. Glucose was 5 mM, which is the concentration the trypanosomes encounter in the bloodstream (23). \( O_2 \) was taken to be saturated under aerobic conditions, whereas the flux through glycerol was completely blocked under anaerobic conditions by setting the \( V_{\text{G}} \) of GPO to zero. In the absence of glyceral, 10% of the total flux went to glyceral under aerobic conditions in contradiction with the corresponding experimental finding that no glyceral was produced (38). However, in the model only 0.5 \( \mu \)M of glyceral was required to inhibit this flux, and at higher concentrations it was reversed. If one were to allow free accumulation of glyceral, the rates of the reactions should reach equilibrium. The aerobic steady state was identical but easier to compute if the \( V_{\text{G}} \) of GFK was set to zero. The extracellular concentration of pyruvate and both the extracellular and the intracellular concentrations of glyceral were zero unless specified otherwise.

**Differential Equations**—If a reaction in the pathway was considered to be in equilibrium, its products and substrates were treated as a single metabolite pool. To this aim five pools were defined.

The sum of hexose phosphates in the glycosome is

\[
[\text{hexose-P}]_g = [\text{Glc-6-P}]_g + [\text{Fru-6-P}]_g
\]  

(Eq. 16)

The sum of triose phosphates is

\[
[\text{triose-P}] = \frac{[\text{DHAP}]V_e + [\text{DHAP}]V_c + [\text{GA-3-P}]V_c}{V_{\text{tot}}}
\]  

(Eq. 17)

\[
[\text{DHAP}]\left(1 + \frac{V_e}{V_g} + \frac{\text{[GA - 3-P]}}{V_g}\right)
\]  

\[
\left(1 + \frac{V_e}{V_g}\right)
\]

A pool \( [N] \) was defined by

\[
[N] = \frac{[\text{3-PGA}][V_e + V_c] + [2-\text{PGA}]V_c + [\text{PEP}]V_c}{V_{\text{tot}}}
\]  

(Eq. 18)

in which

\[
[3\text{-PGA}] = [3\text{-PGA}]_g = [3\text{-PGA}]_c
\]  

(Eq. 19)

Finally, two variables \( P_c \) and \( P_g \) were denoting the sums of high energy phosphates in the glycosome and the cytosol, respectively, were defined:

\[
P_c = 2[\text{ATP}]_c + [\text{ADP}]_c
\]  

(Eq. 21)

\[
P_g = 2[\text{ATP}]_g + [\text{ADP}]_g
\]  

(Eq. 22)

The following set of differential equations described the time-dependent behavior of glycolysis:

\[
\frac{d\text{[Glucose]}}{dt} = \frac{\left(v_{\text{glucose transport}} - v_{\text{HK}}\right)}{V_{\text{tot}}}
\]  

(Eq. 23)

\[
\frac{d\text{[hexose-P]}_g}{dt} = \frac{v_{\text{HK}} - v_{\text{PPK}}}{V_{\text{g}}}
\]  

(Eq. 24)

\[
\frac{d\text{[Fru-1,6-BP]}_g}{dt} = \frac{v_{\text{PPK}} - v_{\text{FALD}}}{V_{\text{g}}}
\]  

(Eq. 25)

\[
\frac{d\text{[triose-P]}}{dt} = \frac{2v_{\text{FALD}} - v_{\text{GAPDH}} - v_{\text{IDH}} + v_{\text{GPO}}}{V_{\text{tot}}}
\]  

(Eq. 26)

\[
\frac{d[v_{1,3-BPGA}]}{dt} = \frac{v_{\text{FALD}} - v_{\text{PPK}}}{V_{\text{g}}}
\]  

(Eq. 27)

\[
\frac{d\text{[NADH]}_c}{dt} = \frac{v_{\text{GAPDH}} - v_{\text{NADH}}}{V_{\text{c}}}
\]  

(Eq. 28)

\[
\frac{d\text{[PYR]}_c}{dt} = \frac{v_{\text{PPK}} - v_{\text{pyruvate transport}}}{V_{\text{c}}}
\]  

(Eq. 29)

\[
\frac{d\text{[NAD]}_g}{dt} = \frac{v_{\text{GAPDH}} - v_{\text{NAD}}}{V_{\text{g}}}
\]  

(Eq. 30)

\[
\frac{d\text{[ADP]}_c}{dt} = \frac{v_{\text{PPK}} - v_{\text{FALD}}}{V_{\text{c}}}
\]  

(Eq. 31)

\[
\frac{d\text{[ATP]}_c}{dt} = \frac{v_{\text{FALD}} - v_{\text{ATP utilization}}}{V_{\text{c}}}
\]  

(Eq. 32)

The total intracellular volume \( V_{\text{tot}} \) was taken constant at 5.7 \( \mu \)M total cellular protein (29). The time \( t \) was expressed in minutes and the enzyme rates \( v \) in nmol min \(^{-1} \) mg cell protein \(^{-1} \). In order to obtain the time derivatives of the concentrations in \( \text{mmol min}^{-1} \), a correction was made for the volume of the compartment in which a metabolite pool resides. As the \( K_m \) values were expressed in \( \text{mm} \), the metabolite concentrations were obtained in \( \text{mm} \) as well.

To calculate a steady state all above time derivatives of metabolite concentrations were set to zero. The resulting system of nonlinear equations was solved numerically for the metabolite concentrations.

**Table II**

<table>
<thead>
<tr>
<th>Enzyme</th>
<th>( K_m ) (mM)</th>
<th>( V_{\text{max}}/V^c )</th>
<th>( K_{s1} ) (mM)</th>
<th>( K_{s2} ) (mM)</th>
<th>( K_{p1} ) (mM)</th>
<th>( K_{p2} ) (mM)</th>
</tr>
</thead>
<tbody>
<tr>
<td>One-substrate reactions</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>HK (8)</td>
<td>1.7 (Gly-3-P)</td>
<td>0.116 (ATP)</td>
<td>0.1 (Gly)</td>
<td>0.126 (ADP)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>GAPDH (48)</td>
<td>0.67</td>
<td>0.15 (GA-3-P)</td>
<td>0.45 (NAD(^+))</td>
<td>0.1 (1,3-BPGA)</td>
<td>0.02 (NADH)</td>
<td></td>
</tr>
<tr>
<td>PGK (49)</td>
<td>0.029</td>
<td>0.05 (1,3-BPGA)</td>
<td>0.1 (ADP)</td>
<td>1.62 (3-PGA)</td>
<td>0.29 (ATP)</td>
<td></td>
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<tr>
<td>GDI(^h)</td>
<td>0.07</td>
<td>0.85 (DHAP)</td>
<td>0.015 (NADH)</td>
<td>6.4 (Gly-3-P)</td>
<td>0.6 (NAD(^+))</td>
<td></td>
</tr>
<tr>
<td>GK (6)</td>
<td>176</td>
<td>5.1 (Gly-3-P)</td>
<td>0.12 (ADP)</td>
<td>0.12 (Gly)</td>
<td>0.19 (ATP)</td>
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</tr>
<tr>
<td>Two-substrate reactions</td>
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<td></td>
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<tr>
<td>GDH</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

\(^{a}\) A.-M. Loiseau, unpublished results.
\(^{b}\) Conjectured, in agreement with an equilibrium constant of 3.3\( \times \)10\(^{-5} \) in the catabolic direction (51).
\(^{c}\) M. Callens, D. Kuntz, O. Bos, and F. Opperdoes, unpublished results.
When [Glc-6-P] was known [Fru-6-P] was calculated from Equation 16. from the equilibrium pools as follows. The individual metabolite concentrations were calculated metabolites, and consequently, the corresponding equilibrium con-
sstants were 1. The individual metabolite concentrations were calculated from the equilibrium pools as follows.

Equations 19, 20, 37, and 38 it follows that
\[ \text{Equilibrium Reactions—} \]
The equilibrium constants are found in Ta-

The equilibrium equation of TIM is

\[ \text{The other solution of the quadratic equation gives negative concentra-
tions of ADP and was not considered. The concentrations of ADP and}
\]

The other solution of the quadratic equation gives negative concentra-
tions of ADP and was not considered. The concentrations of ADP and AMP were calculated from Equations 21 and 1, respectively. To obtain the cytosolic concentrations [ATP]c, [ADP]c, and [AMP]c, Pc was substi-
tuted for P

Numerical Methods—The simulations were performed with the pro-
gram MLAB (Civilized Software, Bethesda). First a time-dependent simulation was performed by integrating Equations 23–32 with a Gear-Adams algorithm, until the system approached a steady state. Usually the initial values of all independent variables were arbitrarily chosen to be 1. Subsequently, the system of nonlinear equations defining the steady state was solved with a Marquardt-Levenberg algorithm, to which the final metabolite concentrations of the time-dependent simulation were given as initial values. An imposed constraint was that all concentrations should be positive, and, if they were involved in a conserved moiety, they should be smaller than the corresponding conserved sum. Finally, starting from the obtained solution a second time integration was performed to test the stability of the steady state. It was examined whether the steady state was unique, by varying the initial metabolite concentrations over a wide range. This never gave a different steady state, but this cannot be considered definite proof of uniqueness.

RESULTS

Fluxes and Concentrations Under Aerobic and Anaerobic Conditions—The first question we addressed was whether the combination of all information on the in vitro kinetics of the glycolytic enzymes leads to realistic fluxes and metabolite concentrations. We therefore calculated the steady-state glycolytic fluxes and metabolite concentrations using the model as described above. The rate of glucose consumption hardly changed upon a shift from aerobic to anaerobic conditions (Table IV). This is in agreement with measurements by Visser (38) who observed that the sum of pyruvate and glycerol production was the same under both conditions. Under aerobic conditions glucose was fully converted to pyruvate, while under anaerobic conditions equimolar amounts of pyruvate and glycerol were produced. The predicted cytosolic concentrations of DHAP, PEP, pyruvate, Gly-3-P, and [ATP]/[ADP] differed by less than a factor 2 from the measured cellular concentrations (27, 31) (Table V). The predicted concentrations of 3-PGA and 2-PGA deviated more from the concentrations obtained experimentally. The model-calculated ratios of the concentrations under aerobic and anaerobic conditions corresponded more closely to the experimental ratios. The concentration of Gly-3-P increased by a factor of 4 upon the shift from aerobic to anaerobic conditions, fully in agreement with the measurements (27). For the cytosolic pyruvate concentration and [ATP]/[ADP] ratio under aerobic conditions the correspondence between the model and the experiments was imposed, because the $V_{\text{max}}$ of the pyruvate transporter and the equation for ATP utilization were adjusted to fit these concentrations. The [ATP]/[ADP] ratio and the flux under anaerobic conditions, however, were kept free. Only the relation between the two was set by Equation 15.

Interestingly, the calculated [ATP]/[ADP] ratios in the cy-
Modeling Trypanosome Glycolysis

The steady-state metabolite concentrations under aerobic and anaerobic conditions

The values shown in brackets are the concentrations measured by Visser and Opperdoes (27). To express the latter concentrations in mM, 1 g of wet weight corresponded to 80 mg of protein and 1 ml of total cellular volume corresponded to 175 mg of total cell protein (29). Pyruvate was measured by Wiemer et al. (31). The equations and parameter values are specified under “Materials and Methods.” To simulate aerobic conditions, $V_{	ext{max}}$ was set to zero, while under anaerobic conditions $V_{	ext{max}}$ was set to zero.

<table>
<thead>
<tr>
<th>Metabolite</th>
<th>Concentration</th>
<th>Ratio, aerobic/anaerobic</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Glucose (c/g)</td>
<td>0.056</td>
<td>0.10</td>
<td>0.056</td>
</tr>
<tr>
<td>Glc-6-P (g)</td>
<td>0.44</td>
<td>0.44</td>
<td>0.44</td>
</tr>
<tr>
<td>Fru-6-P (g)</td>
<td>0.13</td>
<td>0.13</td>
<td>0.13</td>
</tr>
<tr>
<td>Fru-1,6-bisphosphate (g)</td>
<td>26</td>
<td>2.3</td>
<td>26</td>
</tr>
<tr>
<td>DHAP (c/g)</td>
<td>1.6 (2.6)</td>
<td>0.61 (1.1)</td>
<td>2.6 (2.3)</td>
</tr>
<tr>
<td>GA-3-P (g)</td>
<td>0.074</td>
<td>0.027</td>
<td>0.074</td>
</tr>
<tr>
<td>1,3-BPGA (g)</td>
<td>0.028</td>
<td>0.0097</td>
<td>0.028</td>
</tr>
<tr>
<td>2-PGA (c)</td>
<td>0.68 (4.8)</td>
<td>0.46 (1.2)</td>
<td>1.5 (4.1)</td>
</tr>
<tr>
<td>2-PGA (g)</td>
<td>0.13 (0.59)</td>
<td>0.085 (0.33)</td>
<td>1.5 (1.8)</td>
</tr>
<tr>
<td>PEP (c)</td>
<td>0.85 (0.74)</td>
<td>0.57 (0.39)</td>
<td>1.5 (1.9)</td>
</tr>
<tr>
<td>pyruvate (c)</td>
<td>21 (21)</td>
<td>1.6</td>
<td>21</td>
</tr>
<tr>
<td>Gly-3-P (c)</td>
<td>1.1 (2.0)</td>
<td>4.2 (7.9)</td>
<td>0.26 (0.25)</td>
</tr>
<tr>
<td>[NAI]/[NAD]</td>
<td>0.036</td>
<td>0.040</td>
<td>0.036</td>
</tr>
<tr>
<td>[ATP]/[ADP] (g)</td>
<td>0.48</td>
<td>0.29</td>
<td>0.48</td>
</tr>
<tr>
<td>[ATP]/[ADP] (c)</td>
<td>2.9 (2.9)</td>
<td>1.4 (1.2)</td>
<td>2.1 (2.4)</td>
</tr>
</tbody>
</table>

* c, cytosolic; g, glycosomal.

Steady-state $V_{K_c}$ for the reversible glycosomal enzymes that were not assumed to be in equilibrium

These were calculated with the equilibrium constants as they were implicitly used in the kinetic equations. The values given in brackets are the $V_{K_c}$ ratios in cell extracts (27).

<table>
<thead>
<tr>
<th>Enzyme</th>
<th>Aerobic $V_{K_c}$</th>
<th>Anaerobic $V_{K_c}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Glucose transport</td>
<td>$1.1 \times 10^{-2}$</td>
<td>$2.1 \times 10^{-2}$</td>
</tr>
<tr>
<td>ALD</td>
<td>$1.8 \times 10^{-1}$ (4.3)</td>
<td>$2.4 \times 10^{-1}$</td>
</tr>
<tr>
<td>GAPDH</td>
<td>$3.1 \times 10^{-1}$ (8.9-10^{-1})</td>
<td>$3.2 \times 10^{-1}$</td>
</tr>
<tr>
<td>PGK</td>
<td>$3.6 \times 10^{-2}$ (1.6-10^{-2})</td>
<td>$4.2 \times 10^{-3}$ (1.6-10^{-3})</td>
</tr>
<tr>
<td>GDH</td>
<td>$4.4 \times 10^{-3}$ (1.0, assumed)</td>
<td>$4.0 \times 10^{-2}$ (1.0, assumed)</td>
</tr>
</tbody>
</table>

$V_{K_c}$ does not distinguish between glucose and Glc-6-P (23). The measured $[\text{Glc}]_i$ was 1.9 mM, whereas the calculated $[\text{Glc}]_i$ was 0.44 mM. This discrepancy disappeared when the $V_{\text{max}}$ of GK for glycerol was decreased by 40% from 368 to 220 nmol Glycerol-3-P mm$^{-1}$ (mg protein)$^{-1}$. The rate of pyruvate production from 10 mM of glycerol was 80% of the rate of 10 mM of glucose, while experimentally only 50–60% was found (39, 40). This discrepancy disappeared when the $V_{\text{max}}$ of GPO was decreased by 40% from 368 to 220 nmol Glycerol-3-P mm$^{-1}$ (mg protein)$^{-1}$. Then the rate of pyruvate production at 10 mM of glucose was 134 nmol min$^{-1}$ (mg protein)$^{-1}$ compared with 79 nmol min$^{-1}$ (mg protein)$^{-1}$ (59%) at 10 mM of glycerol. Actually a GPO activity as low as 171 nmol Glc-3-P mm$^{-1}$ (mg protein)$^{-1}$ has also been reported for bloodstream form T. brucei at 25°C (41).

**Variation of the Extracellular Glucose Concentration: the Model as Interpreter**

Using the silicone oil centrifugation technique Ter Kuile et al. (23) demonstrated that the intracellular glucose concentration [Glc], remained very low when the extracellular glucose concentration [Glc]$_o$ was kept below 5 mM. Above a [Glc]$_o$ of 5 mM a drastic increase of [Glc], was observed. The model reproduced this (Fig. 3, full lines), although the calculated [Glc]$_o$ remained lower than the measured [Glc]. The difference between model and experiment became most pronounced at the higher concentrations; at 10 mM of [Glc], the measured [Glc]$_o$ was 1.9 mM, whereas the calculated [Glc]$_o$ was only 0.3. This difference was due to the fact that the used assay does not distinguish between glucose and Glc-6-P (23). The Glc-6-P concentration averaged over the whole cell was 1.6 mM (27). This concentration should not be confused with the calculated glycosomal concentration. Subtraction of Glc-6-P gives a

FIG. 2. The steady-state glucose consumption rate under anaerobic conditions as a function of the glycerol concentration as modeled for various combinations of C$_4$ and the $K_M$ of GK for glycerol. I, C$_4$ = 120 mM and $K_M$$_{glycerol}$ = 0.12 mM; 2, C$_4$ = 360 mM and $K_M$$_{glycerol}$ = 0.12 mM; 3, C$_4$ = 120 mM and $K_M$$_{glycerol}$ = 1.2 mM; 4, C$_4$ = 360 mM and $K_M$$_{glycerol}$ = 1.2 mM. All other equations and parameters can be found under “Materials and Methods.”

Glycerol Titration Under Anaerobic and Aerobic Conditions—Under anaerobic conditions Gly-3-P is converted to glyceraldehyde by GK (2). As the $\Delta G^\circ$ of this reaction is strongly positive, glyceraldehyde effectively inhibits glycolysis at low concentrations (50% inhibition at 0.8 mM) (39). In the model, glycolysis was also inhibited by glyceraldehyde (Fig. 2), but 0.1 mM of glyceraldehyde reduced the glucose consumption already by 96.1%. Increasing the forward and reverse $V_{\text{max}}$ of GK, i.e. the amount of the enzyme, did not increase the resistance to glyceraldehyde (result not shown). The model concentration of Gly-3-P in the presence of 0.1 mM glyceraldehyde was 5.1 mM which is equal to the $K_M$ of GK for this metabolite. Gly-3-P is involved in one conserved moiety and, as it equilibrates across the glycosomal membrane, it is weighted by a factor 23.3. Thus a large decrease of other concentrations in this sum is required to compensate for an increase of Gly-3-P (Equation 5). It was conjectured that C$_4$ became a limiting factor under anaerobic conditions. Indeed, an increase of C$_4$ from 120 to 360 mM, substantially increased the flux in the presence of glyceraldehyde (Fig. 2) with a concomitant increase of Gly-3-P (not shown). A 10-fold increase of the $K_M$ of GK for glyceraldehyde, and thus the equilibrium constant of GK, further improved the glyceraldehyde resistance. A combination of both (C$_4$ = 360 mM and $K_M$$_{glycerol}$ = 1.2 mM) gave the maximum glyceraldehyde resistance. At a C$_4$ of 360 mM, however, under aerobic conditions the glycosomal concentration of fructose 1,6-bisphosphate (Fru-1,6-BP) increased to 136 mM. The concomitant increase of the osmotic pressure in the glycosomes might then lead to swelling or even bursting of the organelles. Obviously, simply increasing C$_4$ is not a realistic option.

Under aerobic conditions glyceraldehyde can be used as a substrate. This was simulated by including both GK and GPO in the model and by substituting glyceraldehyde for glucose. The modeled rate of pyruvate production from 10 mM of glyceraldehyde was 80% of the rate from 10 mM of glucose, while experimentally only 50–60% was found (39, 40). This discrepancy disappeared when the $V_{\text{max}}$ of GPO was decreased by 40% from 368 to 220 nmol Gly-3-P mm$^{-1}$ (mg protein)$^{-1}$. Then the rate of pyruvate production at 10 mM of glucose was 134 nmol min$^{-1}$ (mg protein)$^{-1}$ compared with 79 nmol min$^{-1}$ (mg protein)$^{-1}$ (59%) at 10 mM of glyceraldehyde. Actually a GPO activity as low as 171 nmol Glc-3-P mm$^{-1}$ (mg protein)$^{-1}$ has also been reported for bloodstream form T. brucei at 25°C (41).
or when the kinetic expression for HK is relatively low, a small increase of [Glc]i should suffice to increase the flux through HK so as to cope with the increased influx. In the limit to an extracellular glucose concentration of zero, the derivative of v glucose transport to [Glc] is zero, which means that initially the influx rate is insensitive to [Glc]. This is what happens during the first phase when at low [Glc], the [Glc] remains low. At increasing [Glc], the influx increases further, until [Glc] saturates HK, so that a further increase of [Glc] does not lead to a higher rate of phosphorylation. Consequently, [Glc] starts accumulating un-til it inhibits the influx rate to the extent that a steady state is attained. This is what happens in the second phase where [Glc] is accumulating. As the KM values are so different there is only a very small range of glucose concentrations at which both glucose transport and HK are sensitive to [Glc], and, therefore, the switch between the two phases is very sudden.

If the KM of HK for [Glc] were increased to 2 mM, a higher [Glc] should be required to stimulate HK, and this should already lead to a deceleration of glucose transport. In this case there should exist a broad range of [Glc] values at which both the transporter and HK are sensitive to [Glc], so that no sudden switch should be expected. Consistently, the calculated [Glc] was higher and the flux lower under these conditions.

Under both conditions, i.e. low and high KM of HK, the glycosomal [ATP]/[ADP] ratio decreased drastically with increasing flux. This was required for the PGK further downstream to be able to cope with the increased flux. A side effect is, however, that a decreasing [ATP]/[ADP] ratio inhibits the flux through HK. Thus, the increasing [Glc] serves partly to compensate for the decreased [ATP]/[ADP] ratio. If one treats HK and the further metabolism of glucose as one block (42, 43), it has an even higher affinity for glucose than HK on its own. This should make the biphasic shape of the [Glc] curve more pronounced, and, furthermore, it explains why the switch occurs when [Glc] is still below the KM of hexokinase for [Glc].

Sensitivity Analysis—One cannot expect all kinetic constants taken from the literature to be precisely correct. Therefore, we examined whether the results of our calculations depended strongly on the parameter values. All parameter values were varied independently by plus and minus 50% (results not shown). The system always evolved to a new steady state. Three types of responses were observed. Changes of some parameters, such as the equilibrium constant of AK, hardly caused any changes. In other cases only local effects were seen, e.g. variation of the KM of PGK for ATP led to a small change of the glycosomal [ATP]/[ADP] ratio. Some parameter changes led to global changes, mostly transmitted via the coenzymes. For instance an increase of the KM of GAPDH for GA-3-P led to a decrease of the flux, the [ATP]/[ADP] ratio in both compartments, the [NADH]/[NAD+] ratio, and the concentration of 1,3-bisphosphoglycerate (1,3-BPGA), and, furthermore, to an increase of intracellular glucose [Glc] and triose phosphate. However, the effects on the flux were rather small. The flux varied between 91 and 104% of the unmodulated flux when all possible parameter changes were taken into account. Only if the amounts of enzymes were decreased (i.e. the Vmax), larger changes were observed but always below 50%.

**DISCUSSION**

We constructed and tested an integral kinetic model that describes the steady-state behavior of glycolysis in the bloodstream form of T. brucei quantitatively. The model operates at the metabolic level (44). Because transcription and translation have not been included, the model may be limited to cells that do not grow or alter gene expression. Such conditions occur, for instance, in isolated cells in the absence of any nitrogen source, but in the presence of glucose. The model contains experimentally obtained kinetic expressions for most glycolytic enzymes in T. brucei. Because no information is available on the kinetics of transport of metabolites across the glycosomal membrane, the transport of glucose across the cytosolic and the glycosomal membrane was lumped, and the other transport steps across the latter membrane were assumed to be at equilibrium. Another limitation was the fact that the enzyme kinetics had been measured at 25 °C, while physiological studies had been performed at 37 °C. For this reason, relative changes of the flux rather than absolute fluxes were considered when the model
was compared with experimental results. To the extent that the $K_M$ values of the enzymes depend on the temperature and to the extent that the $V_{max}$ values of different enzymes exhibit different temperature dependences, one should expect the steady-state metabolite concentrations to depend on the temperature.

As all parameter values included in the model are based on measurements there may be experimental errors in them. Therefore, it was tested how the model reacted to variations of its parameters. Both local and global effects were observed. This was to be expected, because any realistic model should represent the flexibility of the living cell. However, the effects were relatively small, and particularly, none of the parameter changes affected the stability of the steady state. Therefore, we trust that minor adjustments of these parameters will not overturn our conclusions.

The model constructed in this paper was virtually completely based on in vitro determined enzyme kinetic data. It was not based on a data fit. In view of this, the model predictions correspond remarkably well to experimental data. The relative changes of the flux corresponded exactly, when aerobic and anaerobic conditions were compared. Also most metabolite concentrations deviated less than a factor 2 from the measured concentrations as far as these were available. The available concentrations have been measured in cell extracts, so if the glycosomal concentration is neglected because of the small relative volume of the glycosomes, they represent the cytosolic concentrations. As they were expressed on the basis of wet weight, which is not very accurate, the ratios of concentrations as they were expressed on the basis of wet weight, which is not very accurate, the ratios of concentrations and vice versa. This restriction may be relieved when the transport of Gly-3-P is coupled to the transport of DHAP. In that case the conservation equation of organic phosphate groups that are not exchanged with inorganic phosphate (Equation 5), is replaced by two equations:

$$[\text{Gly-3-P}]_k + [\text{DHAP}]_k + [\text{Glc-6-P}]_k + [\text{Fru-6-P}]_k + 2[\text{Fru-1,6-BP}]_k$$

$$+ [\text{GA-3-P}]_k + [1,3\text{ BPGA}]_k + 2[\text{ATP}]_k + [\text{ADP}]_k = C_4 \quad \text{(Eq. 45)}$$

and

$$[\text{Gly-3-P}]_e + [\text{DHAP}] = C_4 \quad \text{(Eq. 46)}$$

Then a change of the Gly-3-P concentration in the glycosome should have only small effects on the other metabolite concentrations. This should also exclude the possibility of a high osmotic pressure in the glycosomes in case of a drop of Gly-3-P and DHAP.

Glycosomal concentrations of Glc-6-P (4.4 mM), Fru-6-P (2.4 mM), Fru-1,6-BP (1.9 mM), DHAP (7.1 mM), GA-3-P (0.47 mM), and 1,3-BPGA (0.77 mM) have been estimated (45) on the basis of pulse-chase experiments (24). Except for [Fru-1,6-BP], these concentrations are 1 order of magnitude higher than the concentrations predicted by the model. One reason for the discrepancy may be the fact that the model neglects sequestration of metabolites by the enzymes, which may contribute substantially to the total metabolite concentrations due to the high intraglycosomal enzyme concentrations (46). However, the concentrations given by Misset and Opperdoes (45) were estimations. According to the pulse-chase experiments (24) 20–30% of hexose monophosphate (Glc-6-P plus Fru-6-P) and Fru-1,6-BP were labeled in the first fast phase (15 s) and the remaining 70 to 80% in the second slow phase (500 s and longer). The time constant of labeling is related to the size of a metabolite pool divided by the flux through this pool (47). Biphasic labeling kinetics imply that only part of a metabolite pool lies on the main branches of metabolism but do not specify its location. The quickly labeled fraction was interpreted to be the glycosomal fraction and the slowly labeled fraction to be the cytosolic fraction (24). The phosphoglycerates and PEP, however, were also labeled in two phases. The authors themselves suggested that PGM, ENO, and PYK might be attached to the glycosomes, but there is no direct evidence for this. Even if the concentrations of the hexose monophosphates and Fru-1,6-BP were correct, the estimated concentrations of DHAP, GA-3-P, and 1,3-BPGA should be considered with care. They were based on the total cellular concentrations, and the assumption that also for these metabolites the glycosomal fraction was 20–30% of the total amount. We have shown, however, that at the measured enzyme activities ALD, GAPDH, PGK, and GDH must work further from equilibrium in the glycosome than in the cytosol to support the high glycolytic flux. Therefore, one should perhaps refrain from extrapolating average cellular concentrations to glycosomal concentrations. Obviously it becomes important now to measure all glycosomal metabolite concentrations unambiguously.

In conclusion, we may say that our model shows that most of the available experimental data are consistent with each other, i.e. fluxes and concentrations are largely predicted by the known kinetic properties of the enzymes. To optimize the model, extra data on the transport of metabolites across the glycosomal membrane and on the intraglycosomal metabolite concentrations are required. In the light of the good correspondence between the model and the experiments, we expect the model to serve as a valuable heuristic tool. In particular we plan to use it to predict how the glycolytic flux depends quantitatively on the different enzyme activities. This then may prove to be very helpful in the search for new drugs against sleeping sickness.
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REFERENCES