Cell-based models

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Modeling Filamentous Cyanobacteria

5.1 Introduction

Cyanobacteria form a large and diverse phylum of photoautotrophic prokaryotes (121). They are defined by their unique combination of pigments and their ability to perform oxygenic photosynthesis. They often live in colonial aggregates that can take on a multitude of forms (122). Of particular interest are the filamentous species, which often dominate the upper layers of microbial mats found in extreme environments such as hot springs, hypersaline water, deserts and the polar regions (123), but are also widely distributed in more mundane environments as well.

Many species of cyanobacteria are capable of gliding. Gliding is a form of cell movement that differs from crawling or swimming in that it does not rely on any obvious external organ or change in cell shape and it occurs only
in the presence of a substrate (124, 125). Gliding in filamentous cyanobacteria appears to be powered by a “slime jet” mechanism, in which the cells extrude a gel that expands quickly as it hydrates providing a propulsion force (126, 127), although some unicellular cyanobacteria use type IV pili for gliding (128). Individual cells in a trichome have two sets of pores for extruding slime. Each set is organized in a ring at the cell septae and extrudes slime at an acute angle (129). The sets extrude slime in opposite directions and so only one set is likely to be activated during gliding. An alternative hypothesis is that the cells use contractile elements to produce undulations running over the surface of the trichome, somewhat like an earthworm (130). The cells appear to coordinate their gliding direction by an electrical potential that establishes polarity in the trichomes, and thus establishes a “head” and the “tail” (131). Trichomes usually reverse their polarity randomly with an average period on the order of minutes to hours (132, 133). Many species also form a semi-rigid sheath that is left behind as a hollow tube as the trichome moves forward. When the trichome reverses direction, it can move back into the sheath or break out (132).

Cyanobacteria have strict light requirements. Too little light can result in insufficient energy production, and in some species may cause the cells to resort to heterotrophic respiration (123). Too much light can inhibit the cells, decrease photosynthesis efficiency and cause damage by bleaching. UV radiation is especially deadly for cyanobacteria, with normal solar levels being significantly detrimental for these microorganisms in some cases (134, 135). Filamentous cyanobacteria that live in microbial mats often migrate vertically and horizontally within the mat in order to find an optimal niche that balances their light requirements for photosynthesis against their sensitivity to photodamage. For example, the filamentous cyanobacteria Oscillatoria sp. and Spirulina subsalsa found in the hypersaline benthic mats of Guerrero Negro, Mexico, migrate downwards into the lower layers during the day in order to escape the intense sunlight and then rise to the surface at dusk (136). In contrast, Microcoleus chthonoplastes found in hypersaline mats at Salins-de-Giraud, Camargue, France migrate to the upper layer of the mat during the day and are spread homogeneously through the mat at night (137). An in vitro experiment using Phormidium uncinatum also demonstrated this species’ tendency to migrate in order to avoid damaging radiation (134, 135). These migrations are usually the result of some sort of photomovement, although other forms of taxis can also play a role (138).
Photomovement – the modulation of cell movement as a function of the incident light – is employed by the cyanobacteria as a means to find optimal light conditions in their environment. There are three types of photomovement: photokinesis, phototaxis and photophobic responses (132, 139, 140). Photokinetic microorganisms modulate their gliding speed according to the incident light intensity. For example, the speed with which \textit{Phormidium autumnale} glides increases linearly with the incident light intensity (141). Phototactic microorganisms move according to the direction of the light, such that positively phototactic species will tend to move roughly parallel to the light and towards the light source. Species such as \textit{P. uncinatum} cannot steer directly towards the light, but rely on random collisions to orient themselves in the right direction, after which they tend to move more towards the light source. Others, such as \textit{Anabaena variabilis}, can steer by actively bending the trichome (142). Finally, photophobic microorganisms respond to spatial and temporal light gradients. A step-up photophobic reaction occurs when an organism enters a brighter area field from a darker one and then reverses direction, thus avoiding the bright light. The opposite reaction, called a step-down reaction, occurs when an organism enters a dark area from a bright area and then reverses direction, thus remaining in the light.

Gliding filamentous cyanobacteria often display step-down photophobic reactions when their ‘heads’ (i.e. the leading 10-20% of the trichome) are shaded, causing the trichome to reverse direction. In addition, \textit{P. uncinatum} also reacts to light incident on the trichome tail (131). Shining a narrow beam of light on the rear of a trichome will induce it to reverse direction. The trichomes appear to compare the incident light between the head and the tail and if the tail receives more light than the head the trichome is highly likely to reverse its direction (133). Although considered a form of phototaxis by Gabai (133), the response does not depend on the direction of the light but on a light intensity gradient, and thus may better be considered a step-up photophobic response. However, the tail step-up response seems to have a different physiological basis than the step-down reactions originating from the head (133), which are triggered through the photosynthetic apparatus (143).

The effects of photomovement on a population of trichomes can be observed in vitro by shining a column of light, called a light trap, on a culture of \textit{P. uncinatum}. The light scattered by the trichomes and particles already in the trap spot draws the trichomes in the surrounding dark area towards
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Figure 5.1 – Häder’s cyanograph experiment. A photographic negative is projected onto a Petri dish containing a culture of photophobic filamentous cyanobacteria (*Phormidium uncinatum*). The trichomes cover the lighter areas of the projection while uncovering the darker areas producing a photographic positive. Petri dish is 10 cm wide. Courtesy of Donat-Peter Häder.

The illuminated area by positive phototaxis. The trichomes enter the trap from the darker area freely, but will reverse direction whenever moving from the lighter area to the darker area due to step-down photophobic responses. Over the course of a few hours the trichomes will completely fill the trap, marking it with a darker color (144, 145, 146).

Häder demonstrated that trichomes can position themselves quite precisely within their environment through photomovement. In Häder’s cyanograph experiment (132, 147), a photographic negative is projected onto a Petri dish containing a culture of *P. uncinatum*. After a few hours, the trichomes move away from the darker areas onto the lighter areas, forming a photographic positive on the culture (Fig. 5.1). The experiment demonstrates that photomovement is effective not just for discrete light traps, but
for minutely patterned, continuously differentiated light fields as well.

In the study presented here, we explore the advantages of photophobia as a means for optimizing light exposure through the use of a computational model for motile trichomes. Each trichome is modeled as a self-propelled long thin elastic rod equipped with a simple model of photophobia, including both step-up and step-down reactions. Previous models of the photomovement of filamentous cyanobacteria by Burkart and Häder (145) and Hader and Burkart (146) using partial differential equations demonstrated how a combination of phototaxis and step-down photophobic responses can lead to the accumulation of trichomes in light traps. Our model is a large individual based system that allows us to simulate responses to static and dynamic light fields, as well as quantify the advantage of using the photophobic mechanism for optimizing light exposure compared to random gliding, and also show how the length and gliding speed of the trichomes can influence this process.

Somewhat similar models exist of gliding bacteria applied to Myxobacteria, whose fruiting-body formation behavior is used as a model system for primitive morphogenesis. Myxobacteria not only glide using a slime extrusion (A-motility) but also by extension and retraction of type IV pili that can attach to other individuals and pull them closer (S-motility). Like the cyanobacteria, they also reverse their direction of movement periodically. Wu et al. (148, 149) developed a cell-based model of the gliding *M. xanthus* and predicted that the periodic reversals are essential for swarming and increase cell alignment. They were also able to predict the optimum reversal period for swarm expansion to within measurement error of actual cells. Models similar to the one used in this study have recently been used to study the dynamics of cell-cell collisions in Myxobacteria (150, 151). Ginelli et al. (152) also use a similar deterministic model for myxobacteria, albeit for short inflexible rods and only on a small-scale. The advantage of our approach is that we can scale our simulations to the full domain size (i.e. a 10 cm Petri dish) by using massively parallel graphics processing units (GPUs).

5.2 Methods

5.2.1 A Model of Filamentous Cyanobacteria

We used a two-dimensional computational model for gliding phototactic trichomes. Each trichome is modeled as a thin flexible rod of diameter $d$
and total length $L$. Each rod is discretized into $N = \text{round}(L/50)$ segments of equal length, yielding $N + 1$ equally spaced vertices $\langle r_0, \ldots, r_N \rangle$ (Fig. 5.2A). The movement of the trichomes is determined by the viscous dynamics presented in §3.1.4.

Running a simulation step consists of calculating the sum of all the forces acting on each vertex and solving the resulting system of differential equations using a numerical integration method. The boundary conditions are such that the vertices are restricted to a circular domain with an inelastic boundary. Any force or impulse against the domain boundary is met with an equal reaction force and so the following conditions are enforced after each time step:

$$\|r - c\| \leq D/2$$
$$\ddot{r} \cdot \hat{n} \leq 0, \text{ if } \|r - c\| = D/2 \quad (5.1)$$

where $r$ is the displacement of any vertex in the system, $c = \langle D/2, D/2 \rangle$ denotes the center of the circular domain and $\hat{n} = (r - c)/\|r - c\|$ is the unitary vector pointing from the center of the domain towards the vertex.

For each time step all the forces exerted on each vertex $i$ are calculated. The forces arise from (a) trichome elasticity, including tensile and bending strain, (b) gliding and (c) collisions:

$$F_i = \sum F^T_i + \sum F^B_i + F^G_i + \sum F^C_i \quad (5.2)$$

**Trichome Elasticity**

Each vertex is subject to a force that derives from the local tensile and bending strain at the vertex. Torsion is ignored. Each edge $\langle r_i, r_{i+1} \rangle$ is assumed to behave as an elastic rod, which exerts a linear restorative force when under uniaxial load:

$$F^T_{i,i+1} = AE \frac{r_{i,i+1} - l}{l} \quad (5.3)$$

where $A$ denotes the rod’s cross sectional area, $E$ denotes the elastic modulus of the rod, $r_{i,i+1}$ denotes the distance between the two vertices and $l$ denotes the length of the segments.

For the bending resistance forces we use a phenomenological model based on the observation that the bending resistance of a straight elastic rod is
Figure 5.2 – Model components. (A) Trichomes are modeled as thin flexible rods that are discretized into sequences of 50 \( \mu \text{m} \) edges. Each edge is loaded with a linear spring. (B) The local bending moment is a function of the radius of curvature. (C) Trichomes can glide along their long axis and reverse their direction of movement photophobically. (D) Trichome collisions are defined between edge-vertex pairs. A vertex that penetrates an edge’s volume is repulsed by equal and opposite forces between the pair.
proportional to the curvature of the rod (153):

\[ M = \frac{E I}{R} \]  \hspace{1cm} (5.4)

where \( M \) denotes the bending moment generated at the ends of the rod, \( E \) denotes the elastic modulus of the rod, \( I = \pi/4 \times (d/2)^4 \) denotes the second moment of area of the rod’s cross section the and \( R \) denotes the radius of curvature (Fig. 5.2B). We use this model to calculate the local bending forces within the trichome by applying it to pairs of consecutive segments. The bending moment generated by two connected segments is estimated by assuming that the radius of curvature is the radius of the unique circle defined by the three vertices (Fig. 5.2B). The bending moment is converted into forces acting on the three vertices by assuming that the two outer vertices rotate around the middle vertex, each with moment \( M \), such that the total torque and total force acting on the three vertices is zero:

\[
\begin{align*}
F_{i-1}^B &= M \frac{r_{i-1} \times \hat{b}}{r_{i-1} \cdot r_{i-1}} \\
F_{i+1}^B &= -M \frac{r_{i+1} \times \hat{b}}{r_{i+1} \cdot r_{i+1}} \\
F_i^B &= -(F_{i-1}^B + F_{i+1}^B)
\end{align*}
\]  \hspace{1cm} (5.5)

where \( r_{i,j} = r_i - r_j \) and \( \hat{b} \) denotes a pseudo-vector normal to the plane defined by the three vertices:

\[ \hat{b} = \frac{r_{i-1,i} \times r_{i+1,i}}{||r_{i-1,i} \times r_{i+1,i}||} \]  \hspace{1cm} (5.6)

and is oriented into or out of the plane according to whether the trichome is bent to the “left” or to the “right” at the middle vertex. The resulting set of forces tends to move the three vertices onto a straight line, while the tensile forces restore each segment to its initial length.

**Gliding Motility**

As described in the introduction, most filamentous cyanobacteria glide along their long axis. They are unable to steer (with the notable exception of *Anabaena* sp.), but they do reverse their direction of movement randomly (132).
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The propulsion force is probably generated by slime extruding from pores located all along the trichome’s length (126). The slime swells as it leaves the pores and generates a force tangential to the trichome. Likewise, the virtual trichomes are assumed to be able to exert a tangential force against a substrate. The propulsion force is applied at each vertex and is tangential to the trichome at that point (Fig. 5.2C). The trichomes are also assumed to be polarized and that this polarization controls the direction of movement of the trichomes, resulting in the following equation:

\[ \mathbf{F}_{G}^{i} = p \, P \, \eta \, \mathbf{t}_i \quad i = 0, \ldots, N \]  

(5.7)

where \( p \in \{-1, 1\} \) denotes the polarity of the trichome, \( P \) denotes the gliding speed, \( \eta \) is the drag coefficient of the trichome and \( \mathbf{t}_i \) denotes a vector that is tangent to the trichome at vertex \( i \) and is given by:

\[ \mathbf{t}_i = \begin{cases} \frac{r_{i,0}}{l} & i = 0 \\ \frac{r_{i+1,i-1}}{2l} & 0 < i < N \\ \frac{r_{N,N-1}}{l} & i = N \end{cases} \]

(5.8)

**Collisions**

Each trichome has its own exclusive volume that is impenetrable. Each trichome segment is modeled as a capsule-shaped volume composed of a cylinder with semi-spherical caps. Any vertex that enters an edge’s exclusive area is repelled (Fig. 5.2D). The repulsion force intensity is given by:

\[ F_{C} = \begin{cases} -R(r - d)/d & 0 \leq r \leq d \\ 0 & r > d \end{cases} \]

(5.9)

where \( r \) denotes the length of the displacement vector between the edge and the vertex, \( d \) denotes the trichome diameter and \( R \) the repulsion strength. The force is applied to the vertices using the same method presented in §4.2.3.

**Photophobia**

Although cyanobacteria trichomes often display all three types of photomovement, photophobia is considered to be the main driver of pattern formation (132) and therefore only this mechanism is included in the model. The
photophobia model is directly based on observations from Gabai (133) who showed that trichomes of *P. uncinatum* are sensitive to step-down reactions at the head as well as step-up reactions at the tail. Photophobic reactions are simulated by reversing the trichome polarity $p$ (and thus the trichome movement direction) with probability $q$ at each time step. The probability $q$ is a function of the light difference between the head and tail of the trichome:

$$q = \begin{cases} 
\Delta t / T_{\text{light}} & \Delta I \geq 1 - s \\
\Delta t / T_{\text{indiff}} & |\Delta I| < s \\
\Delta t / T_{\text{dark}} & \Delta I \leq -(1 - s)
\end{cases}$$

(5.10)

where $\Delta t$ is the timestep taken during numerical integration, $\Delta I$ denotes the difference in average light intensity measured over $c = 10\%$ of the total trichome length at the trichome head and tail (154, 155); $s$ is the photophobic sensitivity of the trichomes and $T_{\text{light}} > T_{\text{indiff}} > T_{\text{dark}}$ are the average reversal periods for trichomes moving into a lighter area, indifferent light or a darker area. Note that we assume that the light function is normalized such that $I = 0$ corresponds to ‘black’ i.e. total darkness and $I = 1$ corresponds to ‘white’ i.e. the maximum light intensity in the domain. We also assume that $I = 1$ is the optimum light intensity for the trichomes, which they strive to achieve.

### 5.2.2 Simulation Setup

For all our simulations a 10 cm disk with variable number of trichomes is initialized such that a certain predefined domain coverage was achieved, as described in the results section. For the static light field a $2024 \times 2024$ pixel monochrome picture of the Tower Bridge, London was used (inverted to simulate a photographic negative, Fig. 5.3A). Linear interpolation was used between the pixels to obtain a smooth light field. Each simulation corresponds to either 8 or 16 hours of simulated real time. The default parameter values used are listed in Table 6.1.

### 5.2.3 Programming and Data Analysis

The model was programmed using C++ and CUDA and run on an nVidia GTX295 graphics processing unit. For each simulation up to 400 system states
were saved, including each trichome’s average exposure at that time. The visualization was done by binning all the vertices from 20 consecutive states into a 2024 x 2024 pixel domain. This superposition serves to enhance the cyanobacterial “signal” and compensate for the limited number of trichomes that fit in the 2D domain. The binned data was then scaled exponentially to enhance contrast and converted to an 8-bit grayscale image.

5.3 Results

5.3.1 Modeling Cyanographs

As an initial test of our model, we sought to simulate the cyanograph experiment. Cyanographs are formed by projecting a photographic negative onto a culture of photophobic filamentous cyanobacteria in a Petri dish. Due to photophobic responses, the trichomes redistribute themselves in the light field and after a few hours a photographic positive becomes “imprinted” onto the culture. For the cyanograph simulations in this study, a high con-
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Figure 5.3 – Light fields. (A) Light field used for the first and second round of simulations based on a photograph of the London Tower Bridge. (B) Randomly generated light field used in the third round of simulations. The field is composed of overlapping spots that cover the whole area. Spot diameter (O) and light intensity (I) vary from 0.2 to 2 mm and 0 to 1 respectively. The solid white line corresponds to the domain boundary.

Contrast photograph of the London Tower Bridge (Fig. 5.3A) with a clear sky background forming a vertical gradient was used.

The Petri dish is modeled as a 2D circular domain of 10 cm diameter in which the trichomes are laid. The boundary conditions are rigid and inelastic so that the trichomes are unable to traverse the dish’s boundary and are deflected upon collision. Initially, 3.5% of the domain is covered with a uniform population of trichomes, all having identical properties. The trichomes are evenly spaced in the domain and each is placed with a random orientation. For the visualization, 20 consecutive states of the simulation are superimposed in order to obtain a clearer “signal” of the cyanobacterial imprint (see Methods).

Simulations using different trichome populations were performed. First the photophobic sensitivity parameter (s) was varied. This parameter can vary between $0 \leq s \leq 1$, with $s = 0$ representing total insensitivity to light and $s = 1$ “perfect” sensitivity i.e. any difference in light between the trich-
Figure 5.4 – Modeling cyanographs. Images represent 20 superimposed states of a single simulation. Simulations are run with uniform trichome populations. Each parameter value corresponds to a different simulation. Domain radius is 10cm. The number of trichomes per simulation depends on the trichome length (the coverage of the domain is fixed) and varies between $1.5 \times 10^4 – 2.8 \times 10^5$. Standard errors of the mean (SEMs) were very small due to the large sample sizes and are omitted. (A-C) Length and speed fixed to $L = 0.5\text{ mm}$ and $v = 10 \text{ µm s}^{-1}$ respectively; Sensitivity varied between $0 \leq s \leq 1$. Images correspond to $s = 0.4, 0.7, 0.9$ respectively. (D) Graph plotting trichome exposure against trichome sensitivity. The photophobic mechanism starts to become effective from $s > 0.4$. Exposure increases roughly linearly, peaking at a 16% increase for “perfectly” sensitive trichomes. (E-G) Sensitivity and speed fixed to $p = 1$ and $v = 10 \text{ µm s}^{-1}$ respectively; length varied between $0.1 \text{ mm} \leq L \leq 2 \text{ mm}$. Images correspond to $L = 0.1, 0.5, 2 \text{ mm}$ respectively. (H) Log-linear plot of trichome exposure against trichome length.
ome ends can trigger a response. Simulations across the entire range of sensitivity were run in $\Delta s = 0.1$ steps with the trichome length and gliding speed fixed to 0.5 mm and 10 $\mu$m s$^{-1}$ respectively. The results are shown in Fig. 5.4A-D. For $s < 0.4$ the photographic image does not emerge from the simulations. However for increasing values of $s$ the picture emerges gradually, similar to a lifting fog, starting with the golden crown at the top of the towers (Fig. 5.4A). For $s > 0.8$ the towers become clearly outlined and smaller structures, such as the windows, balconies, stones and buildings on the north bank, begin to reveal themselves in detail (Fig. 5.4B-C). For $s = 1.0$, a dramatic shift in the image quality occurs as a detailed, high contrast picture emerges and one can make out the individual beams, windows, arches and other small substructures which embellish the bridge (Fig. 5.4B). Also, the large shadows cast by the bridge to the left of the picture have disappeared to reveal the structures beneath. The trichomes also move up the gradient in the background, leaving a dark streak at the top of the domain, as well as pick out and enhance small details in the sky, such as the spot between the towers (due to a dirty lens) and the airplane contrails in the upper left corner, which are not present for lower parameter values.

The average steady-state light exposure experienced by the trichomes for each sensitivity value is shown in Fig. 5.4D. Average exposure is measured as the percentual increase above the average light intensity in the light field (approximately 0.72 in the case of the Tower Bridge photograph used). The graph shows that the level of detail shown in the cyanographs correlates positively with increased exposure. Exposure increases significantly with sensitivity, with the most sensitive trichomes receiving 16 percentage points more light than the non-photophobic trichomes. For the next series of simulations, trichome sensitivity was fixed to $s = 1$ and gliding speed to 10 $\mu$m s$^{-1}$ while trichome length was varied using the values $L = 0.1, 0.25, 0.5, 1.0, 2.0$ mm. The results are shown in Fig. 5.4E-H. For the shortest trichomes a surprising level of image quality was obtained (Fig. 5.4E). The resulting image displays both detail, with the smaller elements on the bridge clearly visible, and a remarkable level of shading, which is not seen with the longer trichomes. Increasing the trichome length results in decreasing image quality, as the trichomes tend to cluster in small niches of the image and migrate up the light gradient in the sky (Fig. 5.4F). The longest trichomes aggregated into large wave-like clusters in the lightest areas of the photograph and were effective at following the sky gradient towards the top of the domain (Fig. 5.4G).
The average light exposure measured for each population shows that exposure increases with trichome length (Fig. 5.4H), although the effect is less pronounced compared to the sensitivity parameter. Ultimately, the longest trichomes \( L = 2 \text{ mm} \) distribute themselves such that they receive 7 percentage points more light than the shortest \( L = 0.1 \text{ mm} \).

### 5.3.2 A Heterogeneous Population in a Static Light Field

Next we changed the simulation conditions to see how trichomes with different properties perform when competing for light. For this purpose the same light field was used but with different initial conditions. The domain coverage was increased to 16.2% and each trichome was initialized with a random length \( 0.02 \text{ mm} \leq L \leq 2 \text{ mm} \), sensitivity \( 0 \leq s \leq 1 \) and gliding speed \( 0 \mu \text{m s}^{-1} \leq v \leq 10 \mu \text{m s}^{-1} \). In total \( 1.2 \times 10^5 \) trichomes per simulation were used. The simulation was then run until reaching a steady state and the average exposure of subsets of the population were measured. The results are shown in Fig. 5.5.

In Fig. 5.5A, average exposure is plotted as a function of trichome sensitivity. The trend is similar to what was obtained in the previous simulations, although the least sensitive trichomes are actually slightly less exposed then average. Photophobia takes effect only for sensitivities \( s > 0.35 \), and so we limit our analysis of the effects of trichome length and gliding speed to the parameter range \( 0.35 \leq s \leq 1 \).

In Fig. 5.5B, average exposure is plotted as a function of trichome length. Each data point corresponds to a mean over a narrow range of trichome lengths and the full range of sensitivity and gliding speed (which accounts for the drop in average exposure compared to the uniform population simulations). The trend is similar to the results in the previous simulations, except exposure reaches a plateau for lengths \( L > 1 \text{ mm} \). In Fig. 5.5C, average exposure is plotted as a function of trichome gliding speed. Exposure increases with speed peaking at around 6 \( \mu \text{m s}^{-1} \) after which exposure stabilizes at 8% above average. The difference in exposure between the slowest trichomes and the fastest is approximately 6 percentage points. Fig. 5.5D shows the resulting cyanograph image when using a mixed population of trichomes.
Figure 5.5 – Trichome competition in the Tower Bridge field. Each of the $1.26 \times 10^5$ trichomes in the domain is assigned a random length ($0.02 \text{mm} \leq L \leq 2 \text{mm}$), photophobic sensitivity ($0 \leq s \leq 1$) and gliding speed ($0 \mu\text{m s}^{-1} \leq v \leq 10 \mu\text{m s}^{-1}$); 11 simulations were performed. Error bars are the standard deviations of simulation means. (A) Graph plotting exposure against photophobic sensitivity. For values $s < 0.35$, trichomes are exposed to slightly less than the average light in the domain. For $s > 0.35$, exposure increases markedly, peaking at a 12% exposure advantage for “perfectly” sensitive trichomes. (B) Graph plotting exposure against trichome length for sensitivities $0.35 \leq s \leq 1$. Exposure increases significantly up to 0.8 mm after which it plateaus. (C) Graph plotting exposure against gliding speed for sensitivities $0.35 \leq s \leq 1$. Exposure peaks at $7.5 \mu\text{m s}^{-1}$ then plateaus. (D) Composite image of 11 simulations after 8 hours.
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5.3.3 A Heterogeneous Population in a Dynamic Light Field

In microbial mats, trichomes must cope with continuously changing light conditions due to self-shading, sedimentation, changing weather and daylight. To see how the virtual trichomes cope in changing conditions, a procedure for simulating a dynamic light field was devised.

First the light field is initialized to uniform intensity \( I = 0.5 \). With a given frequency \( f \), a disk with a random diameter \( O \) ranging from \( 0.2 \text{ mm} \leq O \leq 2 \text{ mm} \) and centered at a random position in the field is filled with a random light intensity between \( 0 \leq I \leq 1 \). Over time the light field becomes a heterogeneous mix of overlapping dark and light disks, although the average intensity remains \( \bar{I} = 0.5 \) (Fig. 5.3B). After the field has been completely covered with disks, the trichomes are then placed in the domain as described in the previous section, with the sensitivity, length and gliding speed of each trichome chosen randomly. As the simulation runs, the light field continues to change at the given frequency and the trichomes continuously redistribute to the changing conditions by moving out of darker areas and into lighter ones (Fig. 5.6A-C).

Simulations were performed over a range of frequencies from 0 to 2048 s\(^{-1}\). In Fig. 5.6G the average exposure of the entire population of trichomes as a function of the spot frequency is plotted. Exposure decreases with spot frequency as it becomes more difficult for the trichomes to adapt to ever faster changes in the light field. In Fig. 5.6A-C close-ups of the simulation domains are shown. The overlapping contrasting disks of light and dark of the dynamic light field are in shades of gray and the trichomes are drawn in red. Lighter circles with a high trichome density are more common while darker circles show a lower trichome density, as the trichomes will tend to accumulate in the light traps.

The graphs in Fig. 5.6D-F show the average exposure of the trichomes over a 12-hour period (after the average exposure of the whole population had reached a steady state) as a function of the three parameters \( s, L \) and \( v \). In Fig. 5.6D exposure is measured as a function of sensitivity. The exposure profile here is very similar to what was observed for the cyanograph simulations. Photophobia takes effect starting at a lower sensitivity \( (s = 0.2) \), which is probably due to the broad range of light intensity of the spots. The least sensitive trichomes, \( s < 0.2 \), are underexposed, receiving less light than the light field mean. Exposure increases rapidly with sensitivity, peaking for
Figure 5.6 – Trichome competition in a dynamic light field. Same initial conditions as in Fig. 5.5, except a light field composed of overlapping circles of different light intensities is used instead of a static photograph. (A-C) Close ups of a simulation displaying the light field (greyscale) and trichomes (red). Every $1/f$ seconds the light intensity of a random spot in the domain is set to a random value $0 \leq I \leq 1$. The spots range in diameter from $0.2 \text{ mm} \leq O \leq 2 \text{ mm}$. Scale bars $1 \text{ mm}$. (D – F) Graphs plotting exposure against length (D), sensitivity (E) and gliding speed (F) for six different spot frequencies ($0 \text{s}^{-1}, 2 \text{s}^{-1}, 8 \text{s}^{-1}, 32 \text{s}^{-1}, 128 \text{s}^{-1}$ and $512 \text{s}^{-1}$). Different plot colors and symbols correspond to different frequency values, shown on the right-most axis. (G) Plot of average exposure of all trichomes as a function of spot frequency. (H – I) Contour plots demonstrating the relative importance of trichome length vs. sensitivity (H) and gliding speed vs. sensitivity (I). White contour labels indicate percentual exposure increase above average domain light.
5.3 – Results

trichomes with slightly less than maximal photophobia ($s \sim 0.9$), which have $> 40\%$ more exposure than the field mean. Increasing the spot frequency effectively scales the exposure curve downwards, but does not otherwise qualitatively affect the relation.

In Fig. 5.6E, exposure is plotted against trichome length. On average, all the trichomes are able to improve their exposure above the field mean regardless of length, so long as the spot frequency is not too high ($f < 512 \text{s}^{-1}$). For $f = 0 \text{s}^{-1}$ the light field is static. Unlike the Tower Bridge simulations however, exposure peaks for lengths between $0.61 \text{mm} < L < 1 \text{mm}$ and average exposure per trichome decreases slowly for increasing lengths. Increasing the spot frequency effectively scaled the exposure curve downwards. The exposure maximum was always for trichomes of length $0.61 \text{mm} < L < 0.74 \text{mm}$ for $f < 512 \text{s}^{-1}$. This is due to the average diameter of the spots, which is 1.1 mm, whereas the longest trichomes are 2 mm long. The long trichomes manage to accumulate on the smaller bright spots, however their ends protrude from the spot into the darker areas, reducing the average exposure of the trichome (Fig. 5.6C). For higher frequencies the trichomes cannot keep up with the quickly changing light field and are unable to improve their exposure above the light field mean.

In Fig. 5.6F, exposure as a function of gliding speed is shown. Exposure rapidly increases with gliding speed, but then peaks after which it declines slowly. The maximum is an increasing function of spot frequency because the faster trichomes cope better with a more quickly changing environment. For a static light field, the best exposure is obtained for $v \sim 3 \mu\text{m s}^{-1}$, whereas for spot frequencies $f \geq 512 \text{s}^{-1}$ the best exposure is for $v \geq 9.5 \mu\text{m s}^{-1}$.

In Fig. 5.6H, mean exposure across the whole range of spot frequencies tested is plotted against both sensitivity and length in a contour plot. The plot clearly shows the dominant effect of sensitivity over length. For the most sensitive trichomes however, length becomes a significant factor as trichomes in the 0.25 mm to 1 mm range do significantly better than longer or shorter trichomes. Finally, in Fig. 5.6I, a similar plot combining sensitivity and gliding speed is shown. Again, gliding speed appears to have the strongest effect for highly photophobic trichomes.
Chapter 5 – Modeling Filamentous Cyanobacteria

5.4 Discussion

Using a cell-based model, we have shown how gliding speed and trichome length complement photophobia and improve the exposure optimization process. Although we have focused on the increasing exposure, the results are also valid for the complementary problem of trichomes seeking to decrease their exposure.

5.4.1 Photophobia as an Exposure Optimization Mechanism

Using both uniform and mixed populations in static and dynamic light fields, we consistently found that the more photobically sensitive the trichomes are, the more light they are eventually exposed to. In fact real cyanobacteria have been found to be quite sensitive to light, and differences between head and tail as low as a 4% with a 0.03 lx threshold can trigger a response (132).

Filamentous cyanobacteria have been shown in vitro to accumulate in discrete light traps and also distribute themselves in smooth light fields (see Introduction). Although all three types of photomovement can play a role in optimizing light exposure, we found that a simple photophobic mechanism is sufficient to explain the emergence of cyanographs and that this mechanism is also effective in a dynamic light environment, suggesting that photophobia may be an effective strategy in vivo, e.g. in microbial mats.

Ramsing and Prufer-Bebout (159) proposed an alternative strategy. Based on observations of the photomovement of the mat-forming Microcoleus chthonoplastes, they found that this organism’s strategy is to minimize movement when conditions are good, by either moving less often or increasing the frequency of their reversals. When light is weak, they increase their range of motion, probing the environment for better conditions. They argue that this is a more realistic strategy, as probable conditions within the mat are such that light is diffusive and directionless, making phototaxis untenable, and that the light deeper within the mat varies gradually and that this would make photophobia ineffective. However, as the cyanograph experiments and our simulations show, photophobia can be effective in smooth light fields. It would be interesting to simulate trichomes competing for light using these two alternative strategies and compare.
5.4 – Discussion

5.4.2 Long Trichomes Enhance Exposure Optimization

Comparing the distribution of the longest and shortest trichomes in the populations in the Tower Bridge simulations gives some indication as to why the longer trichomes achieve better exposure. In the first example, the trichomes are exposed to parallel bands of light of varying quality and intensity (Fig. 5.7A). The shortest trichomes are for the most part able to escape the roughly uniform low-intensity bands (Fig. 5.7B), but, unlike the longer trichomes, are unable to cross the adjoining pattern of crosses and concentric boxes in order to reach the better light further down (Fig. 5.7C).

Figure 5.7 – Two portions of the Tower Bridge photographic negative where longer trichomes perform better than shorter trichomes. (A) Close up of the upper cross beams between the towers. (B) The shorter trichomes remain stuck in a finely patterned portion of the crossbeam. (C) In contrast, the longer trichomes are able to find more light below. (X) The photograph background is characterized by a smooth gradient. On the scale of an individual trichome, however, the gradient is weak and noisy. The shorter trichomes are for the most part not able to follow the gradient (Y), whereas the longer trichomes can (Z).
In Fig. 5.7X-Z, we compare the distribution of trichomes at the top of the light domain. This part of the photograph captures the sky on a clear day and is characterized by a smooth light gradient (Fig. 5.7X). In the photographic negative of the image, the sky appears lightest at the top and darkest at the bottom. On the scale of an individual trichome the gradient is fairly noisy and difficult to measure. The shorter trichomes show very little accumulation at the top of the domain, indicating that they are not able to pick up the gradient (Fig. 5.7Y). However, virtually all of the longer trichomes were able to follow the gradient and accumulated extensively at the top of the domain (Fig. 5.7Z).

These examples suggest that the ability of the longer trichomes to measure light between more distant points enhances their capacity to navigate with noisy light signals, detect subtle gradients and avoid falling into small suboptimal light traps.

Ramsing and Prufert-Bebout (159) suggested that an effective long-term strategy for the trichomes may be bending into bundles as a way of limiting their motility and compacting themselves in illuminated areas. In our simulations, long trichomes tended to band together and passively curl, forming dense, wave-like sheets as they accumulated in the lighter areas (Fig. 5.6A-C). These structures appeared to be quite stable. Long trichomes that collided with a sheet tended to align with it and added to the structure. Trichomes were only occasionally deflected off of a sheet due to random collisions. Shorter trichomes, however, did not appear to form such structures and were less likely to become bound in this way. We did observe spontaneous alignment of the shorter trichomes, but these swarms were unstable and short lived. The formation of these sheets may be one reason why the longer trichomes perform better in the Tower Bridge simulations, as they may function as attractors and stabilizers in the brighter areas.

### 5.4.3 Fast Gliding Enhances Exposure Optimization

Clearly the trichomes have to move in order to distribute themselves effectively over the light field, but if the trichomes move too quickly we have seen that this can actually be detrimental for their overall exposure. One reason for this may be related to the fixed reversal periods used in all the simulations. As these periods are the same for all trichomes, faster trichomes will travel proportionally more between reversal periods. This may cause a trich-
ome to overshoot a small light trap, as it moves past it before a photophobic response can take effect. Reversal periods are likely to be an important parameter for optimizing exposure. Wu et al. (148) showed in their simulations that periodic reversals are essential for efficient Myxobacteria swarming, and that the 8 min average reversal period of these microorganisms is optimal for swarming.

### 5.4.4 Is the Trichome Optimal for Photomovement?

What are the advantages of forming trichomes for the cyanobacteria? Trichomes can resemble multicellular organisms due to their impressive degree of cooperation, integration and differentiation. Many filamentous species form differentiated cells within the colony to perform specific functions. Heterocysts specialize in fixing atmospheric nitrogen, which is then distributed to neighboring cells, whereas akinetes have thickened cells walls and are resistant to cold and desiccation, helping the organism to survive under harsh conditions (160, 161). Akinetes develop into hormogonia – short and fast trichomes specialized in seeking out better conditions and forming new colonies. Phormidium uncinatum (and probably other species) can share power (in the form of proton motive force) across the colony so that only a portion of the trichome need be illuminated for the entire trichome to be energized (162).

Cyanobacterial trichomes are typically only a few micrometers wide and are relatively long, on the order of a few millimeters. Apart from the advantages of colonial life mentioned above, our simulation results indicate that this particular format is beneficial for the trichomes because it helps their photophobic positioning in two ways.

First, our simulations suggest that gliding speeds on the order of a few µm/s are optimal for photophobic migration, as slower speeds result in worse exposure and faster speeds bring little gain. Filamentous cyanobacteria are able to achieve these speeds, whereas unicellular cyanobacteria typically glide at speeds on the order of a few µm/min. Filamentous species are faster probably due to the streamlined shape of the trichome as well as the coordinated movement of the cells within the colony, whose “slime jet” mechanism can provide a large collective thrust.

Second, we found that long trichomes are also beneficial for optimizing light exposure independently of gliding speed, as they are better at detecting light gradients and are less susceptible to noisy signals. Unfortunately,
studies on cyanobacteria rarely include data on trichome length. Studies of *Beggiatoa*, which are not cyanobacteria but are also filamentous and glide, have shown that populations have stable trichome length distributions, with an average length on the order of 1 mm to 2 mm and gliding speeds around 3 μm s\(^{-1}\) (163, 164). Since *Beggiatoa* also exhibits phobic and tactic behavior in response to light and oxygen gradients (165), their length and speed may be optimized for these responses. It is unknown whether trichome length is actively regulated. Typically, trichomes reproduce via transcellular fragmentation. Specific cells in the trichome – the necridia – die and serve as preferable breakage points when mechanical strain is applied by either bending or stretching (164, 156). There is evidence that the location and timing of necridia formation is under regulatory control, rather than being a totally random event (166). It would be interesting to associate the regulation of necridia differentiation with population length control, which in turn could be beneficial for phobic and tactic migrations.

### 5.4.5 Future Work

The model used for this study was conceived to be as simple as possible and is only an initial approach towards implementation of a large-scale cell-based modeling framework suitable for running on GPUs. To improve our framework, we are currently implementing and experimenting with various models of thin elastic rods, mathematical models of photophobia, inertia-less dynamics and higher order integration schemes in full 3D.

Finally, we would like to see the model predictions validated through experiments. It should be possible to create cultures with different lengths by using a homogenizer, and trichome gliding speed can be controlled via the agar fraction of the substrate. Trichome sensitivity may be difficult to quantify and control, however the model does not suggest an ideal sensitivity merely that the more sensitive trichomes are to light the better.