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Published in:
Astrophysical Journal

DOI:
10.1088/0004-637X/774/1/42

Link to publication

Citation for published version (APA):

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A CHANDRA/HETGS CENSUS OF X-RAY VARIABILITY FROM Sgr A* DURING 2012


1 Boston University Department of Astronomy, Boston, MA 02215, USA; neilenj@bu.edu
2 MIT Kavli Institute for Astrophysics and Space Research, Cambridge, MA 02139, USA; mnowak@space.mit.edu, houck@space.mit.edu
3 Department of Astronomy, University of Illinois Urbana-Champaign, 1002 W. Green Street, Urbana, IL 61801, USA; gammie@illinois.edu
4 Department of Physics, University of Illinois Urbana-Champaign 1110 W. Green Street, Urbana, IL 61801, USA
5 Theoretical Astrophysics Center and Department of Astronomy, University of California, Berkeley, CA 94720-3411, USA
6 Astronomical Institute, “Anton Pannekoek,” University of Amsterdam, Postbus 94249, 1090 GE Amsterdam, The Netherlands; s.b.markoff@uva.nl, r.a.d.wijnands@uva.nl
7 Center for Interdisciplinary Exploration and Research in Astrophysics, Physics and Astronomy Department, Northwestern University, Evanston, IL 60208, USA
8 Department of Physics & Astronomy, University of Leicester, Leicester LE1 7RH, UK; su85@leicester.ac.uk
9 Department of Astronomy, University of Massachusetts, Amherst, MA 01002, USA; wgd@astro.umass.edu
10 Observatoire Astronomique de Strasbourg, Université de Strasbourg, CNRS, UMR 7550, 11 rue de l’Université, F-67000 Strasbourg, France; nicolas.grosso@astro.unistra.fr, delphine.porquet@astro.unistra.fr
11 Space Sciences Laboratory, 7 Gauss Way, University of California, Berkeley, CA 94720-7450, USA; jtomskic@ssl.berkeley.edu
12 Department of Astronomy, University of Michigan, 500 Church Street, Ann Arbor, MI 48109, USA; degenaar@umich.edu, jonnm@umich.edu
13 Department of Physics & Astronomy, College of Charleston, Charleston, SC 29424, USA; fragilep@cofc.edu

Received 2013 May 19; accepted 2013 July 25; published 2013 August 14

ABSTRACT

We present the first systematic analysis of the X-ray variability of Sgr A* during the Chandra X-ray Observatory’s 2012 Sgr A* X-ray Visionary Project. With 38 High Energy Transmission Grating Spectrometer observations spaced an average of 7 days apart, this unprecedented campaign enables detailed study of the X-ray emission from this supermassive black hole at high spatial, spectral and timing resolution. In 3 Ms of observations, we detect 39 X-ray flares from Sgr A*, lasting from a few hundred seconds to approximately 8 ks, and ranging in 2–10 keV luminosity from ∼1034 erg s−1 to 2 × 1035 erg s−1. Despite tentative evidence for a gap in the distribution of flare peak count rates, there is no evidence for X-ray color differences between faint and bright flares. Our preliminary X-ray flare luminosity distribution dN/dL is consistent with a power law with index −1.9±0.3; this is similar to some estimates of Sgr A*’s near-IR flux distribution. The observed flares contribute one-third of the total X-ray output of Sgr A* during the campaign, and as much as 10% of the quiescent X-ray emission could be comprised of weak, undetected flares, which may also contribute high-frequency variability. We argue that flares may be the only source of X-ray emission from the inner accretion flow.

Key words: accretion, accretion disks – black hole physics – radiation mechanisms: non-thermal

1 INTRODUCTION

Since the launch of the Chandra X-ray Observatory and XMM-Newton in 1999, X-ray observations of Sgr A*, the 4 × 106 M⊙ black hole at the center of our Galaxy, have revealed a supermassive black hole deep in quiescence, a profound inactivity punctuated roughly once a day by rapid flares (e.g., Baganoff et al. 2001, 2003; Melia & Falcke 2001; Genzel et al. 2010; Markoff 2010 and references therein). But rather than clarifying the nature of the X-ray emission, the flares from Sgr A* have added to the puzzle of its extremely low luminosity.

In weakly accreting black hole systems at all mass scales, there is a well-known three-way correlation between black hole mass, X-ray luminosity, and radio luminosity (the fundamental plane of black hole activity; Merloni et al. 2003; Falcke et al. 2004; Körding et al. 2006; Gültekin et al. 2009; see also Gallo et al. 2006; Yuan et al. 2009b). However, as demonstrated by Markoff (2005), Körding et al. (2006), and Plotkin et al. (2012), Sgr A* only lies on (or near) this fundamental plane during its X-ray flares; in quiescence, the supermassive black hole is a notable outlier. Thus it is evident that studies of the quiescent emission and the flare emission from Sgr A* probe inherently different physical processes, and that through the flares, we can explore the connections between Sgr A* and weakly accreting black holes, such as those in low-luminosity active galactic nuclei (LLAGN, e.g., Ho 2008; Markoff 2010; Yuan 2011 and references therein). The rarity of strong flares in other LLAGN (such as M81: Markoff et al. 2008; M31: Garcia et al. 2010, although see Li et al. 2011; see also Yuan et al. 2004) places Sgr A* in a unique position (apparently unable to produce continuous X-ray emission in accordance with the fundamental plane) and highlights the importance of understanding the physics of flares.

One such flare (Nowak et al. 2012) began on 2012 February 9 around 14:28:19 (UTC). With Chandra looking on, the 2–10 keV X-ray luminosity rose by a factor of at least ~130 over the course of an hour, reaching a value of about 5 × 1035 erg s−1 for a distance of 8 kpc. At its peak, the X-ray emission from this flare (the brightest X-ray flare ever observed from Sgr A*) equaled the normal bolometric luminosity of this supermassive black hole. Within another 30 minutes, it had vanished. But beyond the strong variability on short timescales, what makes this
flare and its record-breaking intensity so remarkable is that it
topped out at a maximum luminosity of $10^{-9} L_{\odot}$ (still far beneath
the luminosities originally studied on the fundamental plane; see
also Porquet et al. 2003). The majority of X-ray flares, however,
are much fainter, with average luminosities around $10^5$ the
quiescent level.

A summary of the phenomenology of flares from Sgr A* is
provided by Dodds-Eden et al. (2009). Studies of the Galactic
center detect approximately four times more flares in the near-
infrared (NIR) band than in X-rays (e.g., Genzel et al. 2003;
Eckart et al. 2006); the evidence suggests that every X-ray flare is
accompanied by a more-or-less simultaneous NIR flare, while
some NIR flares have no X-ray counterpart (e.g., Hornstein et al.
2007). In addition, while the spectral indices in these bands are
similar, the X-ray flux as seen by Chandra, XMM-Newton, and
Swift is not necessarily consistent with the extrapolated NIR
spectrum (e.g., Eckart et al. 2006). In both the IR (e.g., Hornstein
et al. 2007; Bremer et al. 2011) and the X-ray (Porquet et al.
2003, 2008; Nowak et al. 2012; Degenaar et al. 2013a), there has been some debate regarding the dependence of the flares’
spectral indices on luminosity. Given the complex relationship
between the NIR and X-ray emission, these dependences may be
key to understanding flare physics.

Despite the focused attention on both the quiescent X-ray
emission and the flares from Sgr A* during the last decade,
neither is completely understood. For reference, the quiescent
emission includes all X-ray emission within $1.25 \pm 6400$ AU $\approx
1.6 \times 10^6 R_g$ of Sgr A*, where $R_g = GM_{\odot}/c^2$ is the gravita-
tional radius and $M_{\odot}$ is the black hole mass. This includes
not only any emission from the hot inner accretion flow, but
also from the rest of the accretion flow on scales approaching
the Bondi radius (as well as stars, compact objects, and ex-
tended diffuse emission integrated along the line of sight, but
see Section 5.2 and Shcherbakov & Bagannoff 2010). The quies-
cent X-ray spectrum can be fitted as thermal bremsstrahlung
($kT = 2-3.5$ keV), and has shown so little variability over the
last 14 yr of monitoring that the only plausible physical scena-
rios for its origin are thermal plasma from large scales or a
cluster of coronally active stars (e.g., Falcke & Markoff 2000;
Quataert 2002; Baganoff et al. 2003; Yuan et al. 2002, 2003; Liu
et al. 2004; Xu et al. 2006; Sazonov et al. 2012; Nowak et al.
2012; but see Wang et al. 2013).

A rich diversity of models has been proposed to explain the
flares, both in terms of their energy injection mechanisms,
ranging from magnetic reconnection, stochastic acceleration, or
shocks in the accretion flow or jet to tidal disruption of asteroids,
and in terms of their radiation mechanisms, for which the X-ray
photon index $\Gamma \sim 2$ could be due to direct synchrotron,
synchrotron self-Compton (SSC), or inverse Compton processes
(e.g., Markoff et al. 2001; Liu & Melia 2002; Liu et al. 2004;
Yuan et al. 2003, 2004; Eckart et al. 2004, 2006; Marrone et al.
2008; Čadež et al. 2008; Kostić et al. 2009; Dodds-Eden et al.
The reduced rate of X-ray flares relative to the NIR
may be explained if the high-energy emission is dominated by
SSC, such that only events for which the column density of
synchrotron-emitting electrons is sufficiently large will produce
X-ray flares observable above the quiescent emission (e.g.,
Marrone et al. 2008 and references therein).

In order to address both the origin of the quiescent emission
and the physics of the flares (as well as to continue detailed
study of diffuse emission and transients in the Galactic center;
e.g., Baganoff et al. 2003; Muno et al. 2004, 2007, 2009; Park
et al. 2004; Ponti et al. 2010; Capelli et al. 2012), Chandra
undertook an unprecedented X-ray Visionary Project (XVP) in
2012 to observe Sgr A* for 3 Ms at high spectral resolution with
the High Energy Transmission Grating Spectrometer (HETGS;
Canizares et al. 2005). The excellent X-ray spectral resolution
provides a robust probe of the nature of the accretion flow
(Xu et al. 2006; Young et al. 2007; Sazonov et al. 2012), and
the high cadence and coverage of observations and the long
exposure time are ideal for the first-ever systematic study of
X-ray variability and flares from Sgr A*.

This paper is the first systematic study of X-ray flares
from Sgr A* during the 2012 Chandra XVP. Here we focus on
quantifying the properties (i.e., intensity and duration) of
the flares observed during our 38 Chandra observations and
characterizing the relationship between the quiescent emission
and the X-ray flares. Although prior Chandra, XMM-Newton,
and Swift observations have detected many flares, they used
different detectors and have very different spectral responses and
levels of pileup (Section 4.1.1); we leave a comprehensive
analysis for future work. The paper is organized as follows. In
Sections 2 and 3 we describe the Chandra observations and data
reduction and our method for identifying flares. In Section 4,
we assess the statistical properties of the flares, including their
peak brightnesses, fluences, durations, estimated luminosities,
and X-ray colors. We also explore the variability caused by
undetected flares. In Section 5, we discuss our results in the
context of flare models, multiwavelength flux distributions, and
the contribution of weak flares to the quiescent X-ray emission.

2. OBSERVATIONS AND DATA REDUCTION

During the 2012 XVP campaign, Chandra observed Sgr A*
38 times at high spectral resolution with the HETGS. The
observations, detailed in Table 1, took place between 2012
February 6 and October 29, with exposure times ranging from
14.53 ks to 189.25 ks. For thermal reasons, only five of the chips from the Advanced CCD Imaging Spectrometer-
Spectroscopy (ACIS-S) array were used during the campaign
(S0 was turned off). We reduce the data with standard tools from
the ciao analysis suite, version 4.5. The HETGS consists of two
transmission gratings, the High Energy Grating (HEG) and the
Medium Energy Grating (MEG), which disperse a fraction of
the incoming photons across the detector. With five chips, each
detected photon is recorded to a timing accuracy of 3.14 s, along
with its energy as measured by ACIS and its wavelength and
diffraction order as determined by the diffraction equation and
the tg_resolve_events tool. To study the X-ray variability of
Sgr A*, we extract 2–8 keV light curves of these events in
300 s bins, including only photons in the zeroth order (i.e., the undispersed photons) and the HEG and MEG ±first
orders (hereafter first-order photons). All our subsequent timing
analysis is done in the Interactive Spectral Interpretation System
(Houck & Denicola 2000; Houck 2002).

As reported in Nowak et al. (2012), a number of X-ray flares
are detected in these observations. It is an impossible task to
distinguish the Sgr A* photons from the underlying diffuse
emission. However, the short flare timescales and the absence
of associated optically thin radio flares (Section 4; Baganoff
et al. 2001) argue that the flare emission arises from close to the
black hole. For our purposes, then, it is sufficient to minimize
the background by using small extraction regions as in Nowak
et al. (2012): a ~2.5 pixel (1.25) radius circle for the zeroth-
order events, 5 pixel wide rectangular regions for the first-order
Table 1

2012 Chandra XVP Observations of Flares from Sgr A* 

<table>
<thead>
<tr>
<th>ObsID</th>
<th>Obs Start (MJD)</th>
<th>Exp. (ks)</th>
<th>Bkg. Rate</th>
<th>Flare Start</th>
<th>Flare Stop</th>
<th>Fluence (counts)</th>
<th>Peak Rate (counts s⁻¹)</th>
<th>Duration (s)</th>
<th># Subflares</th>
<th>F_{\text{abs}}^{2–8}</th>
<th>L_{\text{unabs}}^{2–10}</th>
</tr>
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<tbody>
<tr>
<td>13850</td>
<td>55963.026</td>
<td>60.06</td>
<td>5.9 ± 0.5</td>
<td>...</td>
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<td>...</td>
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<td>...</td>
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<tr>
<td>14392</td>
<td>55966.262</td>
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<td>6.2 ± 0.6</td>
<td>55966.433</td>
<td>55966.666</td>
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<td>0.021⁺0.01⁻0.008</td>
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<td>0.8</td>
<td>1.7</td>
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<tr>
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<td>5.9 ± 0.5</td>
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<tr>
<td>14394</td>
<td>55967.136</td>
<td>18.06</td>
<td>6.2⁺¹⁻⁰.⁹</td>
<td>...</td>
<td>...</td>
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<tr>
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<td>56001.365</td>
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<td>5.6 ± 0.6</td>
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<td>39.56</td>
<td>6.8 ± 0.7</td>
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<td>5.7 ± 1.0</td>
<td>56006.486</td>
<td>56006.493</td>
<td>35⁻³⁵</td>
<td>0.06⁻⁺0.02⁻⁻⁻⁻⁻⁻⁻⁻</td>
<td>600</td>
<td>1</td>
<td>3</td>
<td>7.4</td>
</tr>
</tbody>
</table>
| 14413 | 56007.281      | 14.72     | 6.1⁺¹⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻⁻ NOTIFY:
photons, and grating order tolerances of ±0.2. Since much of the background emission is found in the first order (Section 4), a search of the zeroth order alone would also have good sensitivity to flares. But the first order is essential for pileup calibration (Section 4.1.1), and we prefer to use the same events to detect, characterize, and calibrate our flares.

3. LIGHT CURVES AND FLARE DETECTION

The resulting X-ray light curves are shown in Figure 1. For observations spread over nine months and a number of spacecraft roll angles (which affects the diffuse emission in the grating extraction regions), there is remarkably little variation in the quiescent level (Table 1). Highlighting the stability of the baseline emission are the numerous narrow flares, which appear in over half of the 2012 observations (Table 1). Most apparent is the large flare early in the campaign, described in detail in Nowak et al. (2012), which is the brightest X-ray flare ever observed from Sgr A* (see also Porquet et al. 2003). Figure 1 includes several comparably bright flares and numerous moderate and weak flares. One 2 day observation (ObsID 13840) contains no flares, which is consistent with the average rate of ∼1 flare day⁻¹ (Section 5).

In order to detect and characterize these X-ray flares, we use an algorithm based on direct fits to the X-ray light curves shown in Figure 1. There are systematic uncertainties associated with any particular choice of search algorithm; the robustness of our search and an alternative method (the Bayesian Blocks routine; Scargle et al. 2013) are discussed in the Appendix. Here, we fit the 2–8 keV light curves with a model consisting of a constant baseline and Gaussian components to represent the flares. Because the count rates are small, we use the Cash statistic (Cash 1979) and the subp1ex fit method.

After a first pass to estimate the baseline count rate, we perform an automated search for narrow flares on an observation-by-observation basis. In the algorithm, each time bin is examined: if the count rate is below the (fixed) quiescent level, it is ignored (see Section 4.4.1 for a comparison of the data to a Poisson process). Otherwise, we add a “flare” at the center of the bin: a faint narrow Gaussian with an initial 1σ width σ₁ = 150 s. We fit for the flare amplitude and then allow σ₁ to vary as well. We restrict σ₁ to be between 100 s and 1600 s (empirically determined limits, below which the bin size starts to become large relative to the flare FWHM and above which confusion from nearby flares can interfere with the search process). If the resulting amplitude is larger than the quiescent level at 99% confidence for a single trial, the Gaussian component is identified as a real flare, and we fit for the best amplitude, center, and width.

Because the brightest flare (Nowak et al. 2012) showed marked asymmetry, we also perform a search for time substructure in the detected flares. Leaving the initial (significant) component free, we add additional “subflares” as above, with flare center times constrained to occur within ±2σ₁ of the main component, until additional substructure is no longer significant at the 90% level. The substructure is equally likely to appear before and after the peak. Finally, once all flares and substructure have been identified, we calculate 90% confidence limits for each parameter, including the background level. We define the start (stop) time of a flare to be the minimum (maximum) value of the 2σ₁ lower (upper) limits for all its subflares. For each flare, we tabulate the start and stop times, durations, background count rates, rise and decay times, and note whether the flare was truncated by the beginning or end of an observation. We use customized models to fit for the peak count rate and the fluence within the start and stop times of each flare directly.

Figure 1. Top: combined zeroth- and first-order 2–8 keV Chandra X-ray light curve of Sgr A* in 300 s bins for the entire 2012 XVP campaign with gaps removed; events are extracted from a 2.5 pixel radius circular region around the source for the zeroth order and 5 pixel wide rectangular regions for the first-order light curves. A number of flares of varying intensity are apparent, and are indicated by dotted red lines. Short blue horizontal lines indicate sample observations shown in the bottom panel. Bottom: sample light curves of an observation with (left) and without (right) detected flares. ObsID 13854 (left) shows four moderately bright flares within 20 ks.

(A color version of this figure is available in the online journal.)
(fitting for these parameters and their uncertainties is faster and more reliable than combining all the subflares and propagating their uncertainties).

Using this algorithm, we detect a total of 39 flares in 21 observations; the remaining 17 observations appear to be consistent with quiescent emission and/or undetectable flares. We report the measured properties of the 39 detected flares in Table 1. The flares range in duration from 400 s (our shortest allowed time) to about 7800 s, in fluence from 8 counts to 706 counts, and in peak count rate from 0.015 counts s\(^{-1}\) to 0.23 counts s\(^{-1}\). The fluences are divided roughly 3:2 between the zeroth and first orders. As discussed in Nowak et al. (2012), there is some ambiguity associated with the peak count rates, since there may be substructure in the flares on timescales shorter than the present binning (see their Figure 2). Strictly speaking, the peak rates reported here are peak rates on timescales of 300 s, and should be regarded as lower limits on the “instantaneous” peak count rate during the flare. We affirm Nowak et al.’s suggestion that the least ambiguous properties of a flare are its absorbed 2–8 keV fluence and mean flux, as measured above the quiescent/background emission.

For comparison to Nowak et al. (2012), in addition to the fluence, Table 1 also includes estimates of the mean absorbed 2–8 keV flux and the mean unabsorbed 2–10 keV luminosity of each flare for comparison to Nowak et al. (2012). We assume that all flares have the same Γ = 2 power law X-ray spectrum (see Section 4.3.1), so that the flux and luminosity of a flare are proportional to its mean count rate\(^{17}\) (defined as the pileup-corrected fluence divided by the duration). We normalize to the brightest flare, which Nowak et al. (2012) found had a mean absorbed 2–8 keV flux of \(8.5 \pm 0.9 \times 10^{-12} \text{ erg cm}^{-2} \text{ s}^{-1}\), and an unabsorbed 2–10 keV luminosity of \(L_X = 19.2^{+5.2}_{-3.7} \times 10^{34} \text{ erg s}^{-1}\). Only the luminosity and flux are corrected for photon pileup (see Section 4.1.1); the rest of the quantities (i.e., count rates and fluences) in Table 1 represent raw data.

4. FLARE STATISTICS

At first glance, the flares appear to make a relatively minor contribution to the X-ray emission from the Galactic center: the total duration of the observed flares is only 104.4 ks (a duty cycle of 3.5%), and the integrated fluence of all 39 flares, \(\sim 3400\) counts, is small relative to the \(\sim 22,000\) total counts in our extraction region. Much of the first-order flux is diffuse background emission, however, and the zeroth-order counts suggest that flares may have contributed as much as \(\sim 30\%\) of the total X-ray emission from the inner \(1.25\) during the 2012 XVP. This is precisely the ratio implied by a comparison of the summed energy of the observed flares, \(E_f = 5 \times 10^{59} \text{ erg}\), and the total energy emitted in quiescence \(E_q \sim 10^{50} \text{ erg}\) (calculated from the steady quiescent luminosity, \(L_q = 3.6 \times 10^{33} \text{ erg s}^{-1}\); Nowak et al. 2012). Again, we note that much of the steady quiescent X-ray emission could originate far from Sgr A*, near the Bondi radius.

With the origin of both the flares and the quiescent emission (e.g., Sazonov et al. 2012, but see Wang et al. 2013) still unclear, in this section we focus on three questions of immediate interest: (1) are there multiple populations of flares, and if so, (2) how does the spectral hardness of the flares vary with their luminosity and duration, and (3) how much do undetected flares contribute to the baseline/quiescent emission of Sgr A*?

4.1. Observational Biases

Before we can address these questions, we must quantify their intrinsic properties. In the present study, this requires compensating our observed statistics for pileup, which tends to reduce observed count rates, as well as incompleteness and false detections in our flare-finding algorithm.

4.1.1. Pileup Correction

Pileup occurs when two or more photons land in a single event detection cell (for Chandra, a 3 x 3 pixel “island”) during a single CCD frame; the resulting charge pattern on the CCD may be interpreted as a single energetic event, or it may be discarded. The net result is that pileup leads to reduced count rates and harder CCD spectra. The gratings, on the other hand, are pileup free up to relatively high count rates because the incident flux is dispersed over many more pixels. Thus we can use the first-order light curves to correct for any possible pileup in the zeroth-order count rates.

To make this correction, we need to express the total observed count rate (i.e., the sum of the observed count rates in the zeroth and first orders, \(r = r_0 + r_1\) in terms of the incident rate \(\Lambda_i\) and the first-order rate \(\Lambda_1\). Note that in pileup calculations, all rates are expressed as counts per CCD frame (i.e., 3.1 s for five chips), not per unit time. Following Nowak et al. (2012) Equation (2), \(r\) can be written as

\[
\rho = \Lambda_i \left[ 1 + \frac{K}{\alpha \Lambda_1} \left( \frac{r_1}{r_0} \right) - 1 \right] \exp(-\Lambda_1) \left( \frac{r_1}{\Lambda_i} \right),
\]

where \(K\) is a dimensionless function of the spectral shape; it is also the proportionality constant for Equation (2) in Nowak et al. (2012). \(\alpha\) is the grade migration parameter in the pileup model: the odds of detecting \(N\) piled photons as a single event is \(\propto N^{\alpha - 1}\) (Davis 2001). Here we assume \(\alpha = 1\) (Nowak et al. 2012).

The faintest flares in the 2012 XVP peak at observed count rates \(< 0.04 \text{ counts s}^{-1}\) (see Section 4.2); the average count rate in these flares is \(r_f \sim 0.019 \text{ counts s}^{-1} = 0.062 \text{ counts frame}^{-1}\). In these faintest flares, we measure \(r_1 = 0.52r_f\); we suppose that pileup is negligible here, so that \(r_f = \Lambda_i\). Plugging these numbers into Equation (1), we find \(K = 0.94\) for the \(\Gamma = 2\) flares. With \(K\) known, we can use Equation (1) to calculate the pileup-corrected incident count rate \(\Lambda_i\) for any observed count rate \(r\), as long as the incident radiation has approximately the same spectrum as the faint flares. With no significance evidence for variations in the flare spectrum with count rate (Section 4.3.1), this approximation is good enough for the purposes of pileup corrections. For each flare, then, we calculate pileup-corrected peak count rates and fluences (recalling that the fluence is the product of the mean rate and the duration\(^{18}\)). In all cases, the pileup correction is less than 20%, consistent with the estimate for the brightest flare (Nowak et al. 2012).

4.1.2. Incompleteness and False Positives

In order to assess the incompleteness of our sample and the false positive rate, we perform a suite of Monte Carlo

\(^{17}\) Especially for flares with relatively low fluence, where the observed counts may not adequately sample the intrinsic spectrum, the uncertainty associated with these scalings is likely large.

\(^{18}\) An alternative approach would involve integrating over the time-dependent pileup rate; the difference is well within our confidence limits.
simulations based on our fits to the observed light curves. To evaluate the false positive rate, we generate 100 Poisson-random realizations of the baseline emission in each observation and search for flares. No flares are detected, which suggests that our rate of identifying background fluctuations as flares is <1%, and that all of our detected flares are likely real.

We quantify our flare detection efficiency $f$ with simulations in which we inject flares, generate Poisson-random realizations, search for flares, and use the detection rate to assess the incompleteness of our sample. For each observation, we simulate 500 light curves with randomly placed Gaussian flares: 25 flares for each of 20 different peak count rates (logarithmically spaced between 0.01 and 0.3 counts s$^{-1}$). To set the duration of each inserted flare, we randomly sample the observed duration distribution. When we search these simulated light curves, we define a flare inserted at time $t$ with width $\sigma_t$ as detected if our algorithm finds a flare in the time interval $t \pm 3\sigma_t$. With these results we can calculate $f$ for the binned distributions (see Section 4.3). At the low end, we have $f \gtrsim 0.2$–0.5; the incompleteness is not important for flares with fluences $\gtrsim 80$ counts or peak rates above 0.04 counts s$^{-1}$. To create efficiency-corrected histograms, we interpolate to find the detection efficiency at each observed flare, then take the sum of $f^{-1}$ in each bin (effectively dividing each histogram value by the average value of $f$ for the flares in that bin). We perform additional simulations to confirm (using our fluence distribution) that Poisson noise in the injected flares does not change our results to within the quoted errors.

### 4.2. Flare Demographics

In Figure 2, we present the relationships between the raw and pileup-corrected peak count rates, fluences, and durations of the 39 X-ray flares. We see moderate/strong correlations between the fluence of a flare and both its peak count rate (correlation coefficient $\rho \sim 0.89$) and duration ($\rho \sim 0.54$), but almost no correlation ($\rho \sim 0.27$) between the peak count rate of a flare and its duration. Pileup does not have a significant effect on these correlations. The top panel of Figure 2 shows the peak count rate versus fluence of the Sgr A$^*$ flares. Most of the flares are clustered around fluences $\sim 60$ counts, with peak count rates in the range 0.02–0.1 counts s$^{-1}$. At high fluence, the distribution of flares appears to narrow considerably. This does not appear to be an issue of incompleteness. For reference, we overplot a line representing a signal-to-noise ratio (S/N) of 3, as well as lines of constant duration for single Gaussian flares with $1\sigma$ widths of 100 s (our minimum allowed width) and 2500 s, which correspond to flare durations of 400 s and 10 ks. We expect good sensitivity to flares inside this region. Thus the narrow distribution at high fluence is likely physical, and may indicate that the brightest flares have a preferred timescale ($\tau \sim 4$–6 ks).

### 4.3. Flare Distributions

The distributions of the flare properties may also provide clues to their physical origin. In Figure 3, we present the binned differential distributions of the flare fluence, peak count rate, duration, and luminosity (all corrected for detection efficiency and for pileup; Sections 4.1.1 and 4.1.2). These are our best assessment of the intrinsic flare properties in the observed range of parameters. Assuming Poisson uncertainties on each histogram bin, a power law model provides a good fit to

![Figure 2. Relationships between the peak count rate, fluence, and duration of the 39 flares detected during the XVP. Top: peak count rate and fluence, with lines marking the expected relationship for 400 s flares, 10 ks flares, and flares with S/N $\sim 3$. Middle: peak count rate and duration; the gap in peak rate around 0.04 counts s$^{-1}$ is apparent. Bottom: fluence and duration are strongly correlated. Squares denote flares that are truncated by the beginning/end of an observation. (A color version of this figure is available in the online journal.)](image)
the distributions of durations and luminosities (red curves in Figure 3; see Table 2 for fit parameters). The luminosity distribution falls off as $dN/dL \propto L^{-1.9}$, while the duration distribution falls off as $dN/dT \propto T^{-0.9}$. The fluence and peak rate distributions, however, are not as well described by a single power law (the best fits, $dN/dF \sim F^{-1.5}$ and $dN/dR \sim R^{-1.9}$, lead to $\chi^2_{\nu} \sim 1.6$ and 1.9; see Table 2). As an alternative, we try a high-end cutoff power law, shown in blue in Figure 3.

This model provides an improved fit to the fluence distribution, but not the peak rate distribution (see Section 4.3.1). Based on the properties of the brightest flare (Nowak et al. 2012), the best fit fluence cutoff of $\sim 160$ counts corresponds to an absorbed 2–8 keV fluence of $10^{38}$ erg cm$^{-2}$ and a total 2–10 keV energy of $2 \times 10^{38}$ erg. Although the additional parameter is clearly not required to describe the duration distribution, the best-fit cutoff is about 3300 s, which is similar to the orbital period in the inner accretion flow around Sgr A$^\star$. Neither of these cutoffs is well constrained.

An observational reason to prefer the models with a cutoff, however, is the absence of longer and brighter flares. For example, starting at our highest bins and integrating the best-flux fitting the best fit duration, we would have expected to see $3.8_{-2.8}^{+4.5}$ very luminous flares and $52_{-28}^{+48}$ very long flares if the power laws continued indefinitely. The cutoffs reduce these numbers by factors of 2.3 and 14, respectively. Currently the result is marginal, but incorporating the two dozen previously observed XMM-Newton and Chandra flares will help determine the range over which the flare properties are distributed as power laws.

4.3.1. Gaps and X-Ray Colors

One reason for the poor quality of the fits to the peak count rate distribution is an apparent gap near $R \sim 0.04$ counts s$^{-1}$ (Figure 2). The gap is also apparent as a dip in $dN/dR$ in Figure 3. Using the same scaling as in Table 1, the corresponding peak X-ray luminosity is roughly $5.4 \times 10^{34}$ erg s$^{-1}$. There may also be a narrow gap around durations of $\sim 2$ ks that appears in the characteristic timescale (fluence divided by peak rate) of the flares, as well as the flares durations as measured by the Bayesian Blocks method (see the Appendix).

These gaps are particularly interesting given our search for multiple flare populations. There are many ways to test the statistical significance of a gap in a distribution (or, alternatively, whether the distribution is bimodal). One such test is the critical bandwidth test (Silverman 1981; Minotte 1997; Hall & York 2001). The critical bandwidth $h_{crit}$ is defined as the smallest smoothing parameter for which the Gaussian kernel density estimate $f_{h_{crit}}$ has a single mode. The test involves drawing sample

![Table 2](Image)

**Table 2:** Fits to Flare Distributions

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Fluence</th>
<th>Peak Rate</th>
<th>Duration</th>
<th>Luminosity</th>
</tr>
</thead>
<tbody>
<tr>
<td>$N$</td>
<td>$6^{+40}_{-34}$</td>
<td>$0.7^{+1.6}_{-0.6}$</td>
<td>$5^{+21}_{-4}$</td>
<td>$50 \pm 20$</td>
</tr>
<tr>
<td>$\Gamma$</td>
<td>$-1.5 \pm 0.2$</td>
<td>$-1.9^{+6}_{-5}$</td>
<td>$-0.9 \pm 0.2$</td>
<td>$-1.9^{+6}_{-0.4}$</td>
</tr>
<tr>
<td>$\chi^2/\nu$</td>
<td>$8.18/5$</td>
<td>$9.7/5$</td>
<td>$3.3/5$</td>
<td>$4.6/5$</td>
</tr>
</tbody>
</table>

Note: Power law and cutoff power law fits to the distributions in Figure 3. $N$ is the power law normalization and $\Gamma$ is the power law index. Errors are 90% confidence limits for a single parameter. Errors on $N$ are typically large because they involve extrapolating outside the domain of the data.

An observational reason to prefer the models with a cutoff, however, is the absence of longer and brighter flares. For example, starting at our highest bins and integrating the best-fit power law and cutoff power law fits to the distributions in Figure 3. $N$ is the power law normalization and $\Gamma$ is the power law index. Errors are 90% confidence limits for a single parameter. Errors on $N$ are typically large because they involve extrapolating outside the domain of the data.

In units of counts, counts s$^{-1}$, s, and $10^{34}$ erg s$^{-1}$ for the fluence, peak rate, duration, and luminosity distributions, respectively.

The cutoff power law is $N x^\Gamma \exp(-x/cutoff)$.

This model provides an improved fit to the fluence distribution, but not the peak rate distribution (see Section 4.3.1). Based on the properties of the brightest flare (Nowak et al. 2012), the best fit fluence cutoff of $\sim 160$ counts corresponds to an absorbed 2–8 keV fluence of $10^{38}$ erg cm$^{-2}$ and a total 2–10 keV energy of $2 \times 10^{38}$ erg. Although the additional parameter is clearly not required to describe the duration distribution, the best-fit cutoff is about 3300 s, which is similar to the orbital period in the inner accretion flow around Sgr A$^\star$. Neither of these cutoffs is well constrained.

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In units of counts, counts s$^{-1}$, s, and $10^{34}$ erg s$^{-1}$ for the fluence, peak rate, duration, and luminosity distributions, respectively.

The cutoff power law is $N x^\Gamma \exp(-x/cutoff)$.
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Notes. This shows the effects of pileup and contamination by diffuse X-ray emission on HR. $P_{\text{PK-S}}$ and $P_{\text{HR}}$ are the probabilities that the two types of flare differ, as described in Section 4.3.1. The top section reports HR based on all events extracted from the zeroth and first orders during the flares. The middle and bottom sections use only the first-order events to avoid pileup; we subtract events extracted from the zeroth and first orders during the flares. The middle section reports HR based on all events extracted from different extraction regions have different spectral responses, so their HR values should not be compared directly. For reference, the raw background events have $HR = 0.77 \pm 0.01$. Thus the flare is significantly harder than the quiescent emission.

Data from this kernel density distribution, finding new critical bandwidths $h_{\text{crit}}$ for the new samples, and comparing them to $h_{\text{crit}}$. In general, if the data drawn from the smoothed distribution frequently require more smoothing than the original data set, then the distribution is likely bimodal. Quantitatively, as described by Hall & York (2001), the bimodality is significant at the level $\alpha$ if for an appropriately chosen quantity $h_{\text{crit}}$, $P(h_{\text{crit}}/h_{\text{crit}} > \lambda_\alpha) > 1 - \alpha$.

Given the large range of observed peak rates, we perform this test in log space and find that $h_{\text{crit}} = 0.163$, which is $\sim 50\%$ larger than the average $1\sigma$ logarithmic uncertainty on the data. Using the Hall & York (2001) formula for $\lambda_\alpha(\alpha)$, we estimate that the gap in the peak rate distribution is significant at the $\sim 90\%$ level. The test does not specifically include measurement errors, but we find a similar significance level if we randomly sample the uncertainties instead of drawing new data from the kernel density distribution. Hereafter, we refer to flares above this gap as “bright” flares; those below the gap are “faint.” Although the duration gap is not significant at the $90\%$ level in the 39 durations as reported in Table 1, it appears in the Bayesian Blocks measurements and 2 ks is a reasonable timescale for dividing “long” and “short” flares.

In Nowak et al. (2012), we found that the brightest flare (ObsID 14392) appeared to be harder than its local background emission, and a Kolmogorov–Smirnov (K-S) test on the extracted events implied that the color difference between the flare and non-flare intervals was significant at a level of at least 95% (with a maximum $p$-value of $P = 4.6 \times 10^{-2}$ if we considered only zeroth-order photons). With 38 more flares, $\sim 2500$ additional flare photons, and much-improved statistics, we confirm that the flares are harder (see below and Table 3); the probability that the flares and the quiet emission have the same spectrum is indistinguishable from zero, even if we consider only the zeroth- or first-order photons alone. We are therefore confident that the X-ray spectrum of Sgr A* is harder during flares than in quiescence. Detailed spectral fits to all the observed flares will follow in future work, but here we focus on the X-ray colors of the flares above and below the peak rate and duration gaps.

We measure the X-ray color with a hardness ratio (HR), which we define as the ratio of the 4–8 keV counts to the 2–4 keV counts (we calculate uncertainties on HR assuming square-root uncertainties on the numerator and denominator). The comparison of HRs for different types of flares is detailed in Table 3. We calculate the significance of the apparent differences in HR in two ways: (1) a K-S test on the relevant event lists, and (2) a Monte Carlo estimate of the probability that the two HR values are equal given their errors (which we assume to be Gaussian). For example, a K-S test indicates that the observed energy spectrum during faint flares differs from the observed spectrum during bright flares at the $\sim 99.7\%$ level. Our HR-based estimate (using 1 million trials) implies an even higher level of significance, which could indicate that the errors on HR are underestimated or not Gaussian, or it could be due to the fact that it is easier to tell the difference between two numbers than two sets of many numbers: by using HR, we have condensed all the available spectral information into a single quantity.

There are two important caveats to these estimates, both of which we have alluded to above: pileup and the background/diffuse X-ray emission. Despite the null result (below), we believe it is instructive to explore the quantitative influence of these effects, especially because of their importance for future detailed spectral analysis of Sgr A*. Pileup affects the CCD spectrum at high fluxes, and may therefore bias the bright flares toward increased hardness. To account for this in Table 3, we perform the same calculations as above using only the first-order events (which are free of pileup; Section 4). Based on the results, it does not appear that pileup is a major source of bias. Part of the reason for this may be that the flare spectrum (Nowak et al. 2012) peaks around 4 keV, where our energy bands are delineated. Piled photons from the 2–4 keV band will therefore be detected in the 4–8 keV band, while piled photons in the harder band are not detected at all. So, to lowest order, pileup may therefore not result in a large change in HR for the bright flares.

One of the merits of the HR method over the K-S test is that it allows a rough subtraction of the underlying X-ray background, which turns out to be an important factor, since it is much softer than the flares and makes a larger fractional contribution to the faint flares. We use the rate of background events above and below 4 keV to estimate the expected number of background/diffuse photons during each type of flare. We then subtract these events from the appropriate energy band and recalculate HR; the results are shown in the bottom section of Table 3. Considering only the unpiled, background-subtracted first-order photons, there is no evidence for any HR changes between bright and faint flares or long and short flares.

This leaves the significance of the gaps up for debate. If flares above and below these gaps had different spectral properties, we might be more inclined to view the gaps as real gaps separating two distinct emission mechanisms. At present, we have no evidence for that conclusion, nor can we rule out a statistical fluctuation or a single flare mechanism with multiple characteristic timescales or luminosities.

Table 3
Flare Types and Hardness Ratios

<table>
<thead>
<tr>
<th>Type</th>
<th>HR</th>
<th>Type</th>
<th>HR</th>
</tr>
</thead>
<tbody>
<tr>
<td>Short</td>
<td>1.7 ± 0.1</td>
<td>Faint</td>
<td>1.443 ± 0.095</td>
</tr>
<tr>
<td>Long</td>
<td>1.82 ± 0.07</td>
<td>Bright</td>
<td>1.92 ± 0.07</td>
</tr>
<tr>
<td>$P_{\text{PK-S}}$</td>
<td>0.61</td>
<td>2.4 ± 10^{-3}</td>
<td></td>
</tr>
<tr>
<td>$P_{\text{HR}}$</td>
<td>0.13</td>
<td>4 ± 10^{-5}</td>
<td></td>
</tr>
</tbody>
</table>

No pileup (first order only)

<table>
<thead>
<tr>
<th>Type</th>
<th>HR</th>
<th>Type</th>
<th>HR</th>
</tr>
</thead>
<tbody>
<tr>
<td>Short</td>
<td>1.0 ± 0.1</td>
<td>Faint</td>
<td>0.94 ± 0.08</td>
</tr>
<tr>
<td>Long</td>
<td>1.1 ± 0.06</td>
<td>Bright</td>
<td>1.2 ± 0.05</td>
</tr>
<tr>
<td>$P_{\text{PK-S}}$</td>
<td>0.45</td>
<td>0.13</td>
<td></td>
</tr>
<tr>
<td>$P_{\text{HR}}$</td>
<td>0.18</td>
<td>4.2 ± 10^{-3}</td>
<td></td>
</tr>
</tbody>
</table>

Background subtracted, no pileup

<table>
<thead>
<tr>
<th>Type</th>
<th>HR</th>
<th>Type</th>
<th>HR</th>
</tr>
</thead>
<tbody>
<tr>
<td>Short</td>
<td>1.27 ± 0.25</td>
<td>Faint</td>
<td>1.4 ± 0.3</td>
</tr>
<tr>
<td>Long</td>
<td>1.4 ± 0.1</td>
<td>Bright</td>
<td>1.4 ± 0.1</td>
</tr>
<tr>
<td>$P_{\text{HR}}$</td>
<td>0.29</td>
<td>0.53</td>
<td></td>
</tr>
</tbody>
</table>
4.4. Flares and the Quiescent Emission

Because the origin of the quiescent X-ray emission from Sgr A* is still not well understood, and because the X-ray flares contribute one-third of the observed radiation from the inner 1′25 in the 2012 XVP, it is worth asking whether weak flares could make a significant contribution to the quiescent emission from Sgr A*. Specifically, given the observed fluence distribution, what fraction of the quiescent emission could be attributed to undetected flares?

Our ability to answer this question robustly is limited by the (required) assumption that the fluence distribution can be extrapolated significantly below the observed fluence range. However, because the power law and cutoff power law fits differ significantly in slope at the low fluence end, $\Gamma = -(0.9-1.5)$, a comparison of the undetected fluence in these models should be indicative of the overall uncertainty on the extrapolation to low fluence.

To estimate the integrated fluence of undetected flares, we modify our model normalizations to be the integral of $F(dN/dF)$ from $10^{-4}$ counts to $\sim 8.5$ counts (the weakest detected flare). In the power law model, we find a total of $390^{+580}_{-180}$ counts below our detection limit; applying the same energy scalings as above, this corresponds to a fluence of $\sim 2.6 \times 10^{-8}$ erg cm$^{-2}$ and a total energy of $5.5 \times 10^{38}$ erg, or 5.1% of the steady X-ray output from the inner 1′25 during the XVP (the 90% upper limit is 10%). Note that here we are comparing background-subtracted fluences and background-subtracted X-ray emission, so the implication is that very weak flares do not contribute much more than 10% of the quiescent luminosity.

Indeed, the constraint is much tighter if we consider the cutoff power law model, in which there are $130^{+220}_{-90}$ counts below the detection limit (a fluence of $10^{-5}$ erg cm$^{-2}$ and a total energy of $2.2 \times 10^{38}$ erg, with a 90% upper limit to the fractional flare contribution of 2.9%). This is itself a slight overestimate, since for simplicity we calculate the integral as though there is no cutoff (which, at 160 counts, is well above the detection limit of 8.5 counts). If the distribution of very weak flares differs substantially from that of our detected flares, then it would be possible for the contribution to be greater.

4.4.1. Flares and Quiescent Variability

If weak flares contribute as much as 10% of the underlying X-ray emission, this should be apparent in the variability of the quiescent light curve. Is this excess variability present, and is it consistent with white noise? A stringent upper limit on correlated variability might imply that the X-rays come from an extended accretion flow or many independent sources (e.g., a star cluster; Sazonov et al. 2012; see also Wang et al. 2013).

If weak flares do not contribute to the X-ray variability, the waiting times between photons should be described by an exponential distribution. In order to avoid contamination by the diffuse background emission (see Section 4.3.1), we consider only quiescent photons detected in the zeroth order. We find 5480 pairs of such photons that are not separated by either flares or gaps between observations. The resulting distribution of waiting times is shown in the top panel of Figure 4; we assume $\sqrt{N}$ errors on each bin. A fit with an exponential curve is not formally acceptable ($\chi^2 = 1.72$ for 28 degrees of freedom), but suggests a characteristic rate $\lambda = 0.002$ s$^{-1}$, or a characteristic timescale of $\lambda^{-1} = 504 \pm 13$ s (90% errors). A cutoff power law provides a better fit, with $\lambda^{-1} = 570^{+26}_{-25}$ s and a power law slope of $-0.11 \pm 0.03$. In effect, this means that there are fewer short wait times than expected for a Poisson process (or more long wait times). This suggests some correlated variability on short timescales, perhaps due to undetected flares.

Nevertheless, it is difficult to visualize correlated waiting times, so we have also used the cutoff power law model to create a simulated power spectrum (since the observed light curve is contaminated by flares). Assuming the counts in each histogram bin are Poisson-distributed, we generate 10,000 new waiting time distributions and fit each with the same model. We use the resulting fit models to generate new sets of waiting times, from which we build simulated event arrival times and light curves. From these, we calculate binned power spectra, 19 taking the errors on each frequency bin to be the sample standard deviation of all 10,000 power spectra in that bin. We ignore all frequencies below $\sim 10^{-5}$ Hz (comparable to the mean value of one over the observation length), so as not to give overweight weight to frequencies that are not well represented in our data. Still, the errors are quite large, so we rebin the four lowest-frequency bins by a factor of four, and the next four bins by a factor of two. The resulting power spectrum (bottom panel of Figure 4) should be a decent approximation of the intrinsic...

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19 The normalization of each power spectrum is such that its integral over frequency gives the squared fractional rms variability; pure Poisson noise would have a power spectrum independent of frequency at a level $2/\nu$, where $\nu$ is the mean count rate (see Nowak et al. 1999 and references therein).
variability of the inner 1′25, free of contamination by strong flares and observational gaps.

We can draw several conclusions from this analysis. First, Poisson noise dominates the power in the plotted frequency range. But there is also a ∼10% variability component above pure Poisson noise (see also Sections 4.3 and 5). Within observational uncertainties, this component is consistent with uncorrelated noise, but is also well described by a power law (Pν ∝ ν−0.2) or a zero-frequency Lorentzian with a FHWM of ∼10−3 Hz. The timescale is comparable to the orbital period at the innermost stable circular orbit. The shape of the power spectrum is similar to what is seen in many X-ray binaries and AGN (e.g., Nowak et al. 1999; Uttley et al. 2002; McClintock & Remillard 2006; Wilkinson & Uttley 2009), but could also be produced by the superposition of many weak exponential flares with a characteristic duration of ∼1 ks (e.g., Aschwanden 2011 and references therein). This result, a ∼10% excess of power that is consistent with short, weak flares occurring on a range of timescales, corroborates our findings based on extrapolating the flare distribution to low fluence.

5. DISCUSSION

In 3 Ms of observations during 2012, Chandra detected a total of 39 X-ray flares from Sgr A*, spanning a factor of ∼20 in average luminosity (Table 1), with the brightest flare topping out at a peak luminosity of ∼5 × 1035 erg s−1 (Nowak et al. 2012). Most of the observed flares have moderate luminosity; just under half have luminosities above 10× the quiescent level. Accounting for systematic affects from our choice of search algorithm (see the Appendix for more details), we estimate a flare frequency of 1.14±0.11 flares day−1 above a luminosity of 1034 erg s−1, with bright flares (L > 1035 erg s−1) occurring every ∼11.5 days. Despite their rarity, the three brightest Chandra flares represent roughly a third of the observed flare emission in 2012, which is itself one-third of the total X-ray output of the inner 1′25 during the XVP. By our estimates, the unobserved flares make a ∼10% contribution to the quiescent flux from the accretion flow.

Taken at face value, the properties of the 39 observed flares provide relatively few clues to their physical origin, and seem to follow from the independence of the flare intensity on duration (which confirms what was observed in 2007 April with XMM-Newton; Porquet et al. 2008). Only two unusual features are immediately apparent in Figure 2: (1) the gap in the peak flare count rate and (2) the narrow distribution of peak rate versus fluence at high fluence. For reference, the gap-center luminosity is around 5 × 1032 erg s−1, approximately 15 times the quiescent luminosity of the inner 1′25 (Nowak et al. 2012). The gap in the peak count rate is unexpected but only marginally significant, and after controlling for pileup and carefully subtracting the quiescent emission, we find no evidence for any spectral variations above and below this gap. Thus it does not appear to provide evidence for distinct mechanisms of flare emission.

Degenaar et al. (2013a) reported six additional X-ray flares in 821 ks of Swift observations of the Galactic center, all with luminosities above 1035 erg s−1. Due to Swift’s wider point-spread function and the presence of relatively bright transients very close to Sgr A* (Muno et al. 2006; CXOGC J174540.0−290931: Muno et al. 2005a; Porquet et al. 2005; and the newly discovered pulsar SGR J1745−2900: Degenaar et al. 2013b; Dwelly & Ponti 2013; Mori et al. 2013; Kennea et al. 2013; Rea et al. 2013), some caution is warranted in attributing this variability to Sgr A*. However, Monte Carlo simulations based on the Chandra and Swift observing strategy confirm that the flare frequencies are consistent, although the Swift rate may be slightly higher. Further study of Chandra, Swift, and XMM-Newton observations is necessary to place hard limits on the flare frequency derivative. Because the Swift observations are much shorter than the typical flare duration, it is difficult to compare any other properties directly since there is a degeneracy between mean luminosity and peak luminosity for short observations. Although the brightest Swift flare was marginally softer, the six flares were consistent with a single X-ray spectral index (Degenaar et al. 2013a). Porquet et al. (2008) also found no evidence for a correlation between flare luminosity and X-ray photon index in a sample of bright XMM-Newton flares, so it may be that no such correlation exists.

The shape of the peak rate versus fluence distribution at high fluence may be more telling. Because flares of similar intensity would be easily detectable at any duration, it seems that the brightest flares have a characteristic timescale of about 5 ks (again, the brightest XMM-Newton flares are slightly shorter, about 3 ks; Porquet et al. 2003, 2008). This timescale is sufficiently generic that it can be reproduced by a number of models (see Markoff et al. 2001; Liu & Melia 2002; Liu et al. 2004; Dodds-Eden et al. 2010; Kusunose & Takahara 2011). For example, it is comparable to the orbital period within a few times the radius of the innermost stable circular orbit, as well as the characteristic flyby timescale for asteroids at a distance of ∼1 AU (Zubovas et al. 2012; see also Čadež et al. 2008; Kostić et al. 2009) and the Alfvén crossing time for magnetic loops near the black hole (Yuan et al. 2003, 2004).

The same can be said of the flare luminosity distribution, which falls off with X-ray luminosity as dN/dL ∼ L−1.9. This is consistent with several models. For example, the measured luminosity and peak rate distributions are similar to the distributions of solar flares (e.g., Crosby et al. 1993; Güdel 2004; Crosby 2011; Aschwanden & Freundel 2012), although it is not likely that coronal flares can reproduce the luminosity of flares reported in this paper (Sazonov et al. 2012 and references therein; the quasi-symmetric light curves are also unusual for stellar flares). The luminosity distribution is also consistent with the tidal disruption of asteroids (under the assumption that the mass function of asteroids in the central parsec is a power law with an index close to that obtained from collisional fragmentation cascade calculations for solid bodies in orbit around a solar-type star; Zubovas et al. 2012). Since the true asteroid mass function in the harsh environment of Sgr A* is unknown, the agreement between the data and this model is only tentative, and in any case this comparison should not be taken as a rejection of other models. Any viable model should be able to explain at least the luminosity distribution of the flares, the fluence distribution (which is dominated by the highest-fluence flares, since F2 dN/dF ∼ F8.5), as well as the lack of a strong correlation between the flare durations/intensities and the absence of ≥10 ks flares.

5.1. Comparison with the NIR

An alternative perspective on the origin of the flares comes from a comparison of the X-ray and IR variability properties (we leave the discussion of the radio/submillimeter flares for a later date; Yusef-Zadeh et al. 2006a, 2006b; Marrone et al. 2008; Falcke et al. 2009). Based on their analysis of over 10,000 NACO/Very Large Telescope (VLT) Ks-band images from 2004 to 2009, Dodds-Eden et al. (2011) found that the NIR
flux distribution could be described by a lognormal distribution with a power law tail at high flux. They suggested that this tail was evidence of two states (quiescent and flaring, for the lognormal and power law components, respectively) in the NIR emission. For their largest sample, they found a power law slope of $-2.70 \pm 0.14$, which is somewhat steeper than our observed slope of $-1.9^{+0.3}_{-0.6}$. For a smaller subset of their data with high-quality photometry, however, they found a marginally significant tail with a slope of $-2.1 \pm 0.6$, which is consistent with our observed X-ray luminosity distribution.

There are several reasons to proceed carefully with this comparison. The first is that we have estimated the fluxes and luminosities of our flares by supposing that these quantities are strictly proportional to the mean count rate of a flare, and calibrating by the brightest flare ever observed. We have no evidence at present for any color evolution with luminosity, but for flares with small numbers of photons undersampling of the X-ray spectrum may lead to significant uncertainties in this scaling (which we will estimate in future work), and definitive results will require spectral analysis of each flare.

The second reason to proceed with caution is that the actual distribution described by Dodds-Eden et al. (2011) is the distribution of all observed NIR fluxes from Sgr A*, while the quantity we have reported in this paper is the distribution of the average luminosities of X-ray flares. A strict comparison, which is beyond the scope of this paper but will be considered in future work, would require the distribution of the X-ray flux in each 300 s time bin during the 2012 XVP. If the similarity of the distributions remains after a proper and rigorous comparison, it would have interesting implications for the multivavelength variability properties of Sgr A*. For instance, if the NIR and X-ray flare emission mechanisms are synchrotron and SSC, respectively, then the fact that their flux distributions were similar might indicate that the Thompson optical depth of the flare-producing electrons is not a strong function of the intensity of the flares (see, e.g., Marrone et al. 2008; Witzel et al. 2012).

A third reason for caution comes from a later analysis (Witzel et al. 2012) of a larger (2003–2010) NACO/VLT NIR data set. The analysis of over 10,000 $K_s$-band images revealed that the NIR flux distribution is apparently consistent with a pure power law distribution (decreasing with NIR flux as $F_{\text{NIR}}^{-4.215 \pm 0.05}$). This conclusion is also supported by timing analysis by Meyer et al. (2008) and Do et al. (2009), who argue that the power spectrum of Sgr A* in the NIR is featureless (although see Meyer et al. 2009 for evidence of a power law break around a timescale of ~150 minutes). If these analyses are correct, then there is, in a sense, no such thing as an IR “flare” from Sgr A*: all the observed variability is a noise continuum.

In the context of our analysis, this would imply that the luminosity of a flare is not well defined. If it can be demonstrated in subsequent analysis that the X-ray flux distribution from the 2012 Chandra XVP is consistent with the NIR flux distribution as reported by Dodds-Eden et al. (2011) and Witzel et al. (2012), then perhaps there is also no such thing as an X-ray flare. Instead, the peaked X-ray variability observed by Chandra, XMM-Newton, and Swift would simply be the high-energy, high-luminosity end of a continuous multivavelength red noise process. Again, only those X-ray excursions that are sufficiently bright to appear above the “blanket” of the quiescent thermal emission (Markoff 2010) are detectable. In any case, with the brightest X-ray flares characterized by moderate spectral indices ($\Gamma \sim 2–2.4$; Nowak et al. 2012; Porquet et al. 2008, 2003) that can be reproduced by both synchrotron and SSC models (e.g., Yuan et al. 2003; Dodds-Eden et al. 2009; Eckart et al. 2012 and references therein), it seems that a systematic statistical comparison of the NIR/X-ray flux distributions may place the tightest constraints on the physics of variability in the Galactic center (see also Eckart et al. 2006). It may also be worth using the recent multivavelength coverage to revisit the relationship of the flares to the fundamental plane (Markoff 2005; Plotkin et al. 2012). Whatever the origin of the bright X-ray emission, it is clear that future studies of X-ray variability from Sgr A* will benefit greatly from the improved flare statistics provided by the 2012 Chandra XVP, with major progress to be made from focused comparisons of observations of the Galactic center across the electromagnetic spectrum.

5.2. Flares and Sgr A*’s Intrinsic X-Ray Emission

Whether or not “flares” are well defined, it is clear from our present analysis that the X-ray and IR do differ in one respect: there are at least two X-ray emission mechanisms at work around Sgr A*. We have demonstrated here that the quiescent emission cannot be considered to be the superposition of a number of weak flares, on the grounds of both energetics and X-ray color (of course, the X-ray color analysis is also supported by prior spectral studies of individual flares, e.g., Baganoff et al. 2001; Goldwurm et al. 2003; Porquet et al. 2003, 2008; Bélangier et al. 2005; Nowak et al. 2012). Superimposed on this quiescent background is a variable component whose origin (both in terms of the processes that impart energy to the electrons and the mechanisms by which that energy is released as X-rays) is unknown. Our analyses of the flare distributions and the quiescent light curve suggest that the faint (unobserved) end of this variable component could contribute as much as 10% of the apparent quiescent flux (see also Wang et al. 2013). In addition, weak flares with a characteristic timescale of 1 ks could produce the observed ~10% excess correlated variability in Figure 4.

Remarkably, a point source with ~10% of the quiescent luminosity is also required in order to fit the 1999–2010 radial surface brightness profile of Sgr A* (Shcherbakov & Baganoff 2010). Could this 10% point source emission be completely comprised of the weak flares described above? If so, there must be very little truly quiescent emission near the event horizon: the immediate environment of Sgr A*, i.e., the inner ~10R$_s$, emits almost no X-rays outside of flares. In other words, the quiescent X-ray emission from the inner 1" can be cleanly divided into weak X-ray flares from the inner accretion flow (the point source, $<10\%$) and steady thermal emission from plasma on scales comparable to the Bondi radius (the extended source, $\geq90\%$). This could explain why the underlying emission exhibits little variability compared to other accreting black holes (Figure 1; Nowak et al. 2012), and more importantly why Sgr A* appears to lie on the fundamental plane during flares (though it does not explain why Sgr A* is not always on the fundamental plane or why only Sgr A* exhibits these flares).

Implicit in this explanation are the assumptions that the flare luminosity distribution (1) can reliably be extended to very low fluxes, and (2) is stable over many, many dynamical times in the inner accretion flow (see the beginning of Section 5 and Degenaar et al. 2013a). The first point is interesting because for sufficiently faint flares, Sgr A* would have to be flaring constantly, and recent radiative GRMHD simulations (Drappeau et al. 2013) produce mildly variable X-ray emission at roughly the appropriate level ($10^{25–30}$ erg s$^{-1}$). The stability of the flare luminosity distribution may also pose a challenge to flare
models, but with the exception of asteroids these models do not predict flare distributions or their time dependence.

The $\lesssim 10\%$ luminosity of the inner accretion flow may place an important independent constraint on theoretical models, which have historically predicted a larger contribution (especially for the high inclinations, and in many cases spins, that are preferred by millimeter very long baseline interferometry observations and spectral observations, e.g., Mościbrodzka et al. 2009; Dexter et al. 2010; Broderick et al. 2011; Shcherbakov et al. 2012; Drappeau et al. 2013 and references therein). For example, the “best bet” model of Mościbrodzka et al. (2009), i.e., inclination $i = 85^\circ$ and spin $a_*=0.94$, predicts $L_X = 10^{32.9}$ erg s$^{-1}$, which is roughly twice the upper limit we have reported here.

Finally, we note that because the average X-ray luminosity of the accretion flow is $\lesssim 10\%$ of the observed quiescent emission, the brightest flare (Nowak et al. 2012) was actually $\lesssim 1300 \times$ more luminous than its local background. This peak-to-mean ratio is much larger than in the IR (~10–30; Kunneriath et al. 2010; Schönfeld et al. 2011; Dodds-Eden et al. 2011), and the variable X-ray/IR ratio may place important constraints on the flare production and emission mechanisms. For example, synchrotron models with cooling breaks (e.g., Kardashhev et al. 1962; Dodds-Eden et al. 2009; Trau et al. 2010) may lead to spectral slopes independent of flare luminosity, but may struggle to produce the weak flares discussed above. Inverse Compton scenarios, on the other hand, may naturally lead to larger flare amplitudes in the X-ray than NIR, but may also involve changes in spectral slope. Given the progress and promise of X-ray and multilwavelength studies of flares, as well as detailed observational and theoretical analysis of the quiescent X-ray spectrum and variability, there is significance cause for optimism that our 2012 campaign will reveal the nature of the accretion flow onto the supermassive black hole.

We thank all the members of the Sgr A$^*$ Chandra XVP collaboration,20 and we are immensely grateful to Chandra Mission Planning for their support during our 2012 campaign.

We thank John Houck, John Davis, and Feng Yuan for very useful discussions concerning the analysis and interpretation of our data. We acknowledge the role of the Lorentz Center, Leiden, and the Netherlands Organization for Scientific Research Vidi Fellowship 639.042.711 (S.M.), J.N. gratefully acknowledges funding support from NASA through the Einstein Postdoctoral Fellowship, grant PF2-130097, awarded by the Chandra X-ray Center, which is operated by the Smithsonian Astrophysical Observatory for NASA under contract NAS8-03060, and from NASA through the Smithsonian Astrophysical Observatory contract SV3-73016 to MIT for support of the Chandra X-ray Center, which is operated by the Smithsonian Astrophysical Observatory for and on behalf of NASA under contract NAS8-03060. F.K.B. acknowledges support from the Chandra grant G02-13110A under contract NAS8-03060. N.D. is supported by NASA through Hubble Postdoctoral Fellowship grant number HST-HF-51287.01-A. R.W. was partly supported by an European Research Council starting grant.

**APPENDIX**

Given the uncertainties associated with searching noisy signals for flares, it is worth attempting to evaluate the robustness of our flare detection algorithm and the subsequent conclusions. We proceed in several ways. First, we try slightly different binning schemes for our light curves (shifting the bins by one-half width, performing the search on barycenter-corrected data). The bin shifts produce essentially the same flare properties, with small changes ($n \sim 1$) in the number of flares depending on the specific binning. We have not explored different bin widths. Our Monte Carlo simulations (Section 4.3) provide an additional sense of the robustness of our algorithm, insofar as the false detection probability is negligible for our observed flares.

A more rigorous test of our systematic uncertainties can be made by using a completely different flare detection algorithm. For this, as noted in Section 2, we employ a Bayesian Blocks algorithm (Scargle et al. 2013). This method operates on the individual unbinned events and identifies statistically significant changes in the count rate (see, e.g., Baganoff et al. 2003; Nowak et al. 2012). For each change, we require a detection

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**Figure 5.** Comparison of the measured properties of the 34 flares detected by both the Bayesian Blocks algorithm and by direct fitting. Left: there is a strong correlation between the two measures of flare peak count rate, although the direct fitting method returns larger rates (this is likely because the Bayesian Blocks method treats flares as uniform-rate bins). Middle: the fluences measured by the two methods are statistically indistinguishable. Right: flare durations are strongly correlated, with more scatter about the mean relation. Note: circles, squares, and triangles identify flares that are truncated by the beginning/end of an observation according to neither method, both methods, and the Bayesian Blocks method, respectively.

(A color version of this figure is available in the online journal.)
significance of 96.9%, i.e., $1 - \exp(-3.5)$, which implies an overall significance for each detected flare of at least $\sim$99.9%. The method is explained thoroughly in Nowak et al. (2012), but the result is the decomposition of the X-ray light curve into a sequence of blocks and count rates, from which the flare properties can be measured.

The Bayesian Blocks algorithm returns a set of 45 flares. Of the features identified as flares, 34 are detected by both algorithms, with 5 detected only by the direct fitting method (Section 3), and 9 detected by the Bayesian Blocks algorithm alone. A direct comparison of the 34 definitively detected flares (Figure 5) reveals that both algorithms return similar properties for the flares. In the left panel, we show the measured peak rates with best fits. There is a strong correlation between the peak rates as estimated by the two methods, although the Bayesian Blocks findings values that are $\sim$75% smaller. This is likely due to the decomposition of smooth flares into uniform rate bins. The right panel shows the measure durations, which are in general rightward-skewed. The decomposition of smooth flares into uniform rate bins. The overall significance for each detected flare of at least $10^{-4}$. Rates as estimated by the two methods, although the Bayesian Blocks routine appears to underestimate the peak rates.

For the flares. In the left panel, we show the measured peak rates 

This is excellent assurance that despite a few small differences in the fit parameters, our characterization of the observed X-ray events is robust.

In addition to providing a measure of the uncertainty in the number of flares present in the XVP light curves and the reliability of our measurements, the comparison of the results of our two independent methods also illustrates the strengths and weaknesses of our flare detection algorithms. For instance, much of the discrepancy in the number of detected flares can be accounted for by the sensitivity of the Bayesian Blocks routine to long faint flares, which may be statistically significant but not particularly Gaussian. In fact, most of the nine flares not detected by the direct fitting method have peak count rates under $0.01\,\text{counts}\,\text{s}^{-1}$, which is below the sensitivity limit of the direct fitting method (Section 4.3). On the other hand, we note that the Bayesian Blocks routine appears to underestimate the peak count rates of the flares (relative to the direct fitting method), an effect that is likely due to treating the flares as blocks rather than smooth curves.

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