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Determination of α_s from hadronic event shapes measured on the Z^0 resonance

L3 Collaboration

O. Adriani^a, M. Aguilar-Benitez^b, S. Ahlen^c, H. Akbari^d, J. Alcaraz^e, A. Aloisio^f, G. Alverson^g,
M.G. Alviggi^f, G. Ambrosi^h, Q. Anⁱ, H. Anderhub^j, A.L. Anderson^k, V.P. Andreev^l,
T. Angelov^k, L. Antonov^m, D. Antreasyanⁿ, P. Arce^b, A. Arefiev^o, A. Atamanchuk^l,
T. Azemoon^p, T. Aziz^{q,r}, P.V.K.S. Babaⁱ, P. Bagnaia^s, J.A. Bakken^t, L. Baksay^u, R.C. Ball^p,
S. Banerjee^q, J. Bao^d, R. Barillère^e, L. Barone^s, R. Battiston^h, A. Bay^v, F. Becattini^a,
U. Becker^{k,j}, F. Behner^j, J. Behrens^j, S. Beingessner^w, Gy.L. Bencze^x, J. Berdugo^b, P. Berges^k,
B. Bertucci^h, B.L. Betev^{m,j}, M. Biasini^h, A. Biland^j, G.M. Bilei^h, R. Bizzarri^s, J.J. Blaising^w,
P. Blömeke^r, B. Blumenfeld^d, G.J. Bobbink^{e,y}, M. Bocciolini^a, R. Bock^r, A. Böhm^r, B. Borgia^s,
D. Bourilkov^m, M. Bourquin^v, D. Boutigny^w, B. Bouwens^y, E. Brambilla^f, J.G. Branson^z,
I.C. Brock^{aa}, M. Brooks^{ab}, C. Buisson^{ac}, A. Bujak^{ad}, J.D. Burger^k, W.J. Burger^v, J.P. Burq^{ac},
J. Busenitz^u, X.D. Caiⁱ, M. Capell^{ae}, M. Caria^h, F. Carminati^a, A.M. Cartacci^a, M. Cerrada^b,
F. Cesaroni^s, Y.H. Chang^k, U.K. Chaturvediⁱ, M. Chemarin^{ac}, A. Chen^{af}, C. Chen^{ag},
G.M. Chen^{ag}, H.F. Chen^{ah}, H.S. Chen^{ag}, J. Chen^k, M. Chen^k, M.L. Chen^p, W.Y. Chenⁱ,
G. Chiefari^f, C.Y. Chien^d, M. Chmeissani^p, S. Chung^k, C. Civinini^a, I. Clare^k, R. Clare^k,
T.E. Coan^{ab}, H.O. Cohn^{ai}, G. Coignet^w, N. Colino^e, A. Continⁿ, F. Crijns^{aj}, X.T. Cuiⁱ,
X.Y. Cuiⁱ, T.S. Dai^k, R. D'Alessandro^a, R. de Asmundis^f, A. Degré^w, K. Deiters^k, E. Dénes^x,
P. Denes^l, F. DeNotaristefani^s, M. Dhina^j, D. DiBitonto^u, M. Diemoz^s, H.R. Dimitrov^m,
C. Dionisi^{se}, M.T. Dovaⁱ, E. Drago^f, T. Driever^{aj}, D. Duchesneau^v, P. Duinker^y, I. Duran^b,
H. El Mamouni^{ac}, A. Engler^{aa}, F.J. Eppling^k, F.C. Erné^y, P. Extermann^v, R. Fabbretti^{ak},
M. Fabre^{ak}, S. Falciano^s, S.J. Fan^{af}, O. Fackler^{ae}, J. Fay^{ac}, M. Felcini^e, T. Ferguson^{aa},
D. Fernandez^b, G. Fernandez^b, F. Ferroni^s, H. Fesefeldt^r, E. Fiandrini^h, J. Field^v,
F. Filthaut^{aj}, G. Finocchiaro^s, P.H. Fisher^d, G. Forconi^v, T. Foreman^y, K. Freudenreich^j,
W. Friebel^{am}, M. Fukushima^k, M. Gailloud^{an}, Yu. Galaktionov^{o,k}, E. Gallo^a, S.N. Ganguli^q,
P. Garcia-Abia^b, S.S. Gau^{af}, D. Gele^{ac}, S. Gentile^{se}, S. Goldfarb^p, Z.F. Gong^{ah}, E. Gonzalez^b,
P. Göttlicher^r, D. Goujon^v, G. Gratta^{ao}, C. Grinnell^k, M. Gruenewald^{ao}, C. Guⁱ,
M. Guanziroliⁱ, J.K. Guo^{af}, V.K. Gupta^l, A. Gurtu^{e,q}, H.R. Gustafson^p, L.J. Gutay^{ad},
K. Hangarter^r, A. Hasanⁱ, D. Hauschildt^y, C.F. He^{af}, T. Hebbeker^r, M. Hebert^z, G. Herten^k,
U. Herten^r, A. Hervé^e, K. Hilgers^r, H. Hofer^j, H. Hoorani^v, G. Huⁱ, G.Q. Hu^{af}, B. Ille^{ac},
M.M. Ilyas^l, V. Innocente^{e,f}, H. Janssen^e, S. Jezequel^w, B.N. Jin^{ag}, L.W. Jones^p, A. Kasser^{an},
R.A. Khanⁱ, Yu. Kamyshkov^{ai}, P. Kapinos^l, J.S. Kapustinsky^{ab}, Y. Karyotakis^{e,w}, M. Kaurⁱ,
S. Khokharⁱ, M.N. Kienzle-Focacci^v, W.W. Kinnison^{ab}, D. Kirkby^{ao}, S. Kirsch^{am}, W. Kittel^{aj},
A. Klimentov^{k,o}, A.C. König^{aj}, E. Koffeman^y, O. Kornadt^r, V. Koutsenko^{k,o}, A. Koulbardis^l,
R.W. Kraemer^{aa}, T. Kramer^k, V.R. Krastev^{m,h}, W. Krenz^r, A. Krivshich^l, J. Krizmanic^d,
K.S. Kumar^{ap}, A. Kunin^{ap,o}, G. Landi^a, D. Lanske^r, S. Lanzano^f, P. Lebrun^{ac}, P. Lecomte^j,
P. Lecoq^e, P. Le Coultre^j, D.M. Lee^{ab}, I. Leedom^g, J.M. Le Goff^e, R. Leiste^{am}, M. Lenti^a,
E. Leonardi^s, J. Lettry^j, X. Leytens^y, C. Li^{ah,i}, H.T. Li^{ag}, P.J. Li^{af}, X.G. Li^{ag}, J.Y. Liao^{af},
W.T. Lin^{af}, Z.Y. Lin^{ah}, F.L. Linde^{e,y}, B. Lindemann^r, D. Linnhofer^j, Y. Liuⁱ,
W. Lohmann^{am,e}, E. Longo^s, Y.S. Lu^{ag}, J.M. Lubbers^e, K. Lübelmeyer^r, C. Luci^s,

D. Luckey^{n,k}, L. Ludovici^s, L. Luminari^s, W.G. Ma^{ah}, M. MacDermott^j, P.K. Malhotra^{q,1}, R. Malikⁱ, A. Malinin^{w,o}, C. Maña^b, D.N. Mao^p, Y.F. Mao^{ag}, M. Maolinbay^j, P. Marchesini^j, F. Marion^w, A. Marin^c, J.P. Martin^{ac}, L. Martinez-Laso^e, F. Marzano^s, G.G.G. Massaro^y, T. Matsuda^k, K. Mazumdar^q, P. McBride^{ap}, T. McMahon^{ad}, D. McNally^j, Th. Meinholz^r, M. Merk^{aj}, L. Merola^f, M. Meschini^a, W.J. Metzger^{aj}, Y. Miⁱ, G.B. Mills^{ab}, Y. Mirⁱ, G. Mirabelli^s, J. Mnich^r, M. Möller^r, B. Monteleoni^a, R. Morand^w, S. Morganti^s, N.E. Moulaiⁱ, R. Mount^{ao}, S. Müller^r, A. Nadtochy^l, E. Nagy^x, M. Napolitano^f, H. Newman^{ao}, C. Neyer^j, M.A. Niazⁱ, L. Niessen^r, H. Nowak^{am}, G. Organtini^s, D. Pandoulas^r, S. Paoletti^a, G. Passaleva^{ah}, S. Patricelli^f, M. Pauluzzi^h, F. Pauss^j, Y.J. Pei^r, D. Perret-Gallix^w, J. Perrier^v, A. Pevsner^d, M. Pieri^{e,a}, P.A. Piroué^t, F. Plasil^{ai}, V. Plyaskin^o, M. Pohl^j, V. Pojidaev^{o,a}, N. Produit^v, J.M. Qian^p, K.N. Qureshiⁱ, R. Raghavan^q, G. Rahal-Callot^j, G. Raven^y, P. Razis^{aq}, K. Read^{ai}, D. Ren^j, Z. Renⁱ, M. Rescigno^s, S. Reucroft^g, A. Ricker^r, S. Riemann^{am}, O. Rind^p, H.A. Rizviⁱ, B.P. Roe^p, M. Röhner^r, S. Röhner^r, L. Romero^b, J. Rose^r, S. Rosier-Lees^w, R. Rosmalen^{aj}, Ph. Rosselet^{an}, A. Rubbia^k, J.A. Rubio^{e,b}, H. Rykaczewski^j, M. Sachwitz^{am}, E. Sajan^h, J. Salicio^{e,b}, J.M. Salicio^b, G.S. Sanders^{ab}, A. Santocchia^h, M.S. Sarakinos^k, G. Sartorelliⁿⁱ, M. Sassowsky^r, G. Sauvage^w, V. Schegelsky^l, K. Schmiemann^r, D. Schmitz^r, P. Schmitz^r, M. Schneegans^w, H. Schopper^{ar}, D.J. Schotanus^{aj}, S. Shotkin^k, H.J. Schreiber^{am}, J. Shukla^{aa}, R. Schulte^r, S. Schulte^r, K. Schultze^r, J. Schütte^{ap}, J. Schwenke^r, G. Schwering^r, C. Sciacca^f, I. Scott^{ap}, R. Sehgalⁱ, P.G. Seiler^{ak}, J.C. Sens^{e,y}, L. Servoli^h, I. Sheer^z, D.Z. Shen^{al}, S. Shevchenko^{ao}, X.R. Shi^{ao}, E. Shumilov^o, V. Shoutko^o, E. Soderstrom^t, A. Sopczak^z, C. Spartiotis^d, T. Spickermann^r, P. Spillantini^a, R. Starosta^r, M. Steuer^{n,k}, D.P. Stickland^t, F. Sticozzi^k, H. Stone^v, K. Strauch^{ap}, B.C. Stringfellow^{ad}, K. Sudhakar^{q,r}, G. Sultanovⁱ, R.L. Sumner^t, L.Z. Sun^{ah,i}, H. Suter^j, R.B. Sutton^{aa}, J.D. Swainⁱ, A.A. Syedⁱ, X.W. Tang^{ag}, L. Taylor^g, C. Timmermans^{aj}, Samuel C.C. Ting^k, S.M. Ting^k, M. Tonutti^r, S.C. Tonwar^q, J. Tóth^x, A. Tsaregorodtsev^l, G. Tsiopolitis^{aa}, C. Tully^{ao}, K.L. Tung^{ag}, J. Ulbricht^j, L. Urbán^x, U. Uwer^r, E. Valente^s, R.T. Van de Walle^{aj}, I. Vetlitsky^o, G. Viertel^j, P. Vikasⁱ, U. Vikasⁱ, M. Vivargent^w, H. Vogel^{aa}, H. Vogt^{am}, I. Vorobiev^o, A.A. Vorobyov^l, L. Vuilleumier^{an}, M. Wadhwaⁱ, W. Wallraff^r, C.R. Wang^{ah}, G.H. Wang^{aa}, J.H. Wang^{ag}, Q.F. Wang^{ap}, X.L. Wang^{ah}, Y.F. Wang^a, Z.M. Wang^{i,ah}, A. Weber^r, J. Weber^j, R. Weill^{an}, T.J. Wenaus^{ac}, J. Wenninger^v, M. White^k, C. Willmott^b, F. Wittgenstein^e, D. Wright^t, R.J. Wu^{ag}, S.X. Wuⁱ, Y.G. Wu^{ag}, B. Wyslouch^k, Y.Y. Xie^{al}, Y.D. Xu^{ag}, Z.Z. Xu^{ah}, Z.L. Xue^{al}, D.S. Yan^{al}, X.J. Yan^k, B.Z. Yang^{ah}, C.G. Yang^{ag}, G. Yangⁱ, K.S. Yang^{ag}, Q.Y. Yang^{ag}, Z.Q. Yang^{al}, C.H. Yeⁱ, J.B. Ye^{ah}, Q. Yeⁱ, S.C. Yeh^{af}, Z.W. Yin^{al}, J.M. Youⁱ, N. Yunusⁱ, M. Yzerman^y, C. Zaccardelli^{ao}, P. Zemp^j, M. Zengⁱ, Y. Zeng^r, D.H. Zhang^y, Z.P. Zhang^{ah,i}, B. Zhou^c, J.F. Zhou^r, R.Y. Zhu^{ao}, H.L. Zhuang^{ag}, A. Zichichi^{n,e,i} and B.C.C. van der Zwaan^y

^a INFN – Sezione di Firenze and University of Firenze, I-50125 Florence, Italy

^b Centro de Investigaciones Energeticas, Medioambientales y Tecnologicas, CIEMAT, E-28040 Madrid, Spain

^c Boston University, Boston, MA 02215, USA

^d Johns Hopkins University, Baltimore, MD 21218, USA

^e European Laboratory for Particle Physics, CERN, CH-1211 Geneva 23, Switzerland

^f INFN – Sezione di Napoli and University of Naples, I-80125 Naples, Italy

^g Northeastern University, Boston, MA 02115, USA

^h INFN – Sezione di Perugia and Università Degli Studi di Perugia, I-06100 Perugia, Italy

ⁱ World Laboratory, FBLJA Project, CH-1211 Geneva, Switzerland

^j Eidgenössische Technische Hochschule, ETH Zürich, CH-8093 Zurich, Switzerland

^k Massachusetts Institute of Technology, Cambridge, MA 02139, USA

^l Nuclear Physics Institute, SU-188 350 St. Petersburg, USSR

- ^m *Bulgarian Academy of Sciences, Institute of Mechatronics, BG-1113 Sofia, Bulgaria*
ⁿ *INFN – Sezione di Bologna, I-40126 Bologna, Italy*
^o *Institute of Theoretical and Experimental Physics, ITEP, SU-117 259 Moscow, USSR*
^p *University of Michigan, Ann Arbor, MI 48109, USA*
^q *Tata Institute of Fundamental Research, Bombay 400 005, India*
^r *I. Physikalisches Institut, RWTH, W-5100 Aachen, FRG²*
and III. Physikalisches Institut, RWTH, W-5100 Aachen, FRG²
^s *INFN – Sezione di Roma and University of Rome “La Sapienza”, I-00185 Rome, Italy*
^t *Princeton University, Princeton, NJ 08544, USA*
^u *University of Alabama, Tuscaloosa, AL 35486, USA*
^v *University of Geneva, CH-1211 Geneva 4, Switzerland*
^w *Laboratoire de Physique des Particules, LAPP, F-74519 Annecy-le-Vieux, France*
^x *Central Research Institute for Physics of the Hungarian Academy of Sciences, H-1525 Budapest 114, Hungary*
^y *National Institute for High Energy Physics, NIKHEF, NL-1009 DB Amsterdam, The Netherlands*
^z *University of California, San Diego, CA 92182, USA*
^{aa} *Carnegie Mellon University, Pittsburgh, PA 15213, USA*
^{ab} *Los Alamos National Laboratory, Los Alamos, NM 87544, USA*
^{ac} *Institut de Physique Nucléaire de Lyon, IN2P3-CNRS/Université Claude Bernard, F-69622 Villeurbanne Cedex, France*
^{ad} *Purdue University, West Lafayette, IN 47907, USA*
^{ae} *Lawrence Livermore National Laboratory, Livermore, CA 94550, USA*
^{af} *High Energy Physics Group, Taiwan, ROC*
^{ag} *Institute of High Energy Physics, IHEP, Beijing, China*
^{ah} *Chinese University of Science and Technology, Hefei, Anhui 230 029, China*
^{ai} *Oak Ridge National Laboratory, Oak Ridge, TN 37830, USA*
^{aj} *University of Nijmegen and NIKHEF, NL-6525 ED Nijmegen, The Netherlands*
^{ak} *Paul Scherrer Institut, PSI, CH-5232 Villigen, Switzerland*
^{al} *Shanghai Institute of Ceramics, SIC, Shanghai, China*
^{am} *Institut für Hochenergiephysik, O-1615 Zeuthen–Berlin, FRG²*
^{an} *University of Lausanne, CH-1015 Lausanne, Switzerland*
^{ao} *California Institute of Technology, Pasadena, CA 91125, USA*
^{ap} *Harvard University, Cambridge, MA 02139, USA*
^{aq} *Department of Natural Sciences, University of Cyprus, Nicosia, Cyprus*
^{ar} *University of Hamburg, W-2000 Hamburg, FRG*

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We present a study of the global event shape variables thrust and heavy jet mass, of energy–energy correlations and of jet multiplicities based on 250 000 hadronic Z^0 decays. The data are compared to new QCD calculations including resummation of leading and next-to-leading logarithms to all orders. We determine the strong coupling constant $\alpha_s(91.2 \text{ GeV}) = 0.125 \pm 0.003 (\text{exp}) \pm 0.008 (\text{theor})$. The first error is the experimental uncertainty. The second error is due to hadronization uncertainties and approximations in the calculations of the higher order corrections.

1. Introduction

The strong coupling constant has been determined to second order in α_s from hadronic decays of the Z^0 produced in e^+e^- collisions using measurements of jet multiplicities [1–5], energy–energy correlations [6–

8,4] and other event shape variables [3,8,4,5]. The dominant error is due to contributions beyond second order in the perturbative expansion, which are not included in the corresponding QCD calculations.

Recently new calculations of hadronic event shapes including the second order results and the resummation of leading and next-to-leading logarithms to all orders in QCD perturbation theory have been made [9–11]. Therefore the theoretical uncertainties due to uncalculated terms are expected to be reduced with

¹ Deceased.

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respect to second order calculations. The new computations are available for the global event shape variables thrust [12] and heavy jet mass [13] and for energy-energy correlations [14] in the back-to-back region. Also the average jet multiplicity calculated in the new k_{\perp} jet clustering scheme [15] has been computed [16] however certain terms have not yet been included in the resummation [17].

We report here on measurements of those four event shape variables at the Z^0 resonance using the L3 detector at LEP. Comparing our data to the predictions of the new QCD calculations we derive values for the strong coupling constant α_s at $\sqrt{s} = m_Z$.

2. The L3 detector

The L3 detector covers 99% of 4π [18]. The detector consists of a central tracking chamber, a high resolution electromagnetic calorimeter composed of bismuth germanium oxide crystals, a ring of scintillation counters, a uranium and brass hadron calorimeter with proportional wire chamber readout, and an accurate muon chamber system. These detectors are installed in a 12 m diameter magnet which provides a uniform field of 0.5 T along the beam direction.

For the present analysis, we use data collected in the following ranges of polar angle:

- $40^\circ < \theta < 140^\circ$ for the tracking chamber,
- $11^\circ < \theta < 169^\circ$ for the electromagnetic calorimeter,
- $5^\circ < \theta < 175^\circ$ for the hadron calorimeter,
- $36^\circ < \theta < 144^\circ$ for the muon chambers.

3. Selection of hadronic events

Events collected at a center of mass energy of $\sqrt{s} = 91.2$ GeV from the 1991 LEP running period, corresponding to an integrated luminosity of about 8 pb^{-1} , are used for this analysis.

The primary trigger for hadronic events requires a total energy of about 15 GeV in the calorimeters. This trigger is in logical OR with a trigger using the barrel scintillation counters and with a charged track trigger. The combined trigger efficiency for selected hadronic events exceeds 99.9%.

Events of type $e^+e^- \rightarrow$ hadrons are selected and analyzed by two independent methods: one is based on the energy measured in the electromagnetic and hadronic calorimeters, the other one uses charged tracks measured in the tracking chamber. The results presented in this paper are based on the calorimeter method, which is the more precise one. The track measurements are used to cross check the first method and to estimate the experimental errors.

For the calorimeter based selection, we require:

- $N_{\text{cluster}} > 12$,
- $0.6 < E/\sqrt{s} < 1.4$,
- $|E_{\parallel}|/E < 0.4$, $E_{\perp}/E < 0.4$,

where E is the total energy observed in the calorimeters, E_{\parallel} is the energy imbalance along the beam direction, E_{\perp} is the energy imbalance in the plane perpendicular to the beam direction, and N_{cluster} is the number of calorimetric clusters with energy greater than 100 MeV. We select 248 100 hadronic events.

The selection based on charged tracks is described in detail in ref. [19]. We require at least 5 tracks originating close to the interaction point, each with a transverse momentum of at least 100 MeV with respect to the beam axis. A cut on the polar angle of the thrust axis of $|\cos \theta_{\text{thrust}}| < 0.7$ ensures that the selected events are well contained in the tracking chamber. With these criteria we find 169 700 hadronic Z^0 decays.

Monte Carlo studies show that the efficiencies of the two selections are 98.5% and 66.7% respectively. The low efficiency for the second method is due to the $\cos \theta_{\text{thrust}}$ cut. The main background sources are $\tau^+\tau^-$ and $e^+e^- \rightarrow$ hadrons final states. Applying the same cuts to background Monte Carlo events, the contaminations in the selected $e^+e^- \rightarrow$ hadrons samples are estimated to be less than 0.2% for the first selection, and to be less than 0.1% for the second selection.

Monte Carlo events were generated by the parton shower programs JETSET 7.3 [20] and HERWIG 5.3 [21] and passed through the L3 detector simulation [22].

4. Definition of variables

It is important to consider all the observables for which the new QCD calculations are available. Since they are affected differently by higher order effects

and hadronization corrections, a comparison of the corresponding α_s values allows an estimation of the size of theoretical uncertainties.

The global event shape variable thrust T [12] is defined as

$$T = \max \frac{\sum |\mathbf{p}_i \cdot \mathbf{n}_T|}{\sum |\mathbf{p}_i|},$$

where \mathbf{p}_i is the momentum vector of the hadron i . The thrust axis \mathbf{n}_T is determined by maximizing the above expression. The thrust values can vary between 0.5 and 1.

The heavy jet mass M_H is defined as [13]

$$M_H = \max[M_1(\mathbf{n}_T), M_2(\mathbf{n}_T)],$$

where $M_{1,2}$ are the invariant masses in the two hemispheres defined by the thrust axis:

$$M_l^2 = \left(\sum_{\text{hemisphere } l} p_i \right)^2,$$

where p_i is the four momentum of particle i . Here we use the normalized quantity

$$\rho = M_H^2/s.$$

The energy–energy correlation (EEC) [14] can be defined as a histogram of all angles between any particles i, j in hadronic events weighted with the product of their energies, and averaged over N events:

EEC(χ_{bin})

$$= \frac{1}{\Delta_{\text{bin}} \cdot N} \sum_{\text{events}} \sum_{i,j} \frac{E_i \cdot E_j}{s} \delta_{\text{bin}}(\chi_{\text{bin}} - \chi_{ij}).$$

$\delta_{\text{bin}}(\chi_{\text{bin}} - \chi_{ij})$ is 1 for angles χ_{ij} inside the bin around χ_{bin} and 0 otherwise. Δ_{bin} denotes the bin width. For 2-jet events most angles are close to 0° or 180° , while events with hard gluon radiation contribute to the central region. To determine α_s we use here the back-to-back region with $\chi \geq 90^\circ$, for which the new calculations have been performed [11].

Jets are reconstructed using the new “ k_\perp ” algorithm [15]. For each pair of particles i and j the expression

$$y_{ij} = 2[\min(E_i^2, E_j^2)/s](1 - \cos \theta_{ij})$$

is evaluated. E_i and E_j are the energies and θ_{ij} is the angle between particles i and j . The pair for which y_{ij} is smallest is replaced by a pseudoparticle l with four-momentum

$$p_l = p_i + p_j.$$

This procedure is repeated until all y_{ij} exceed the jet resolution parameter y_{cut} . The remaining (pseudo)particles are called jets. Increasing y_{cut} lowers the fraction of multijet events but increases the separation of the jets.

The difference between the k_\perp and the JADE jet algorithms [23], which we used previously [1] lies in the definition of y_{ij} . While in the JADE scheme the scaled invariant mass squared is used, the quantity y_{ij} in the new algorithm corresponds to the scaled relative transverse momentum k_\perp squared. Here we use the k_\perp jet algorithm, since in this scheme (but not in the JADE scheme) the resummation of the leading and next-to-leading terms is possible [24,25,16].

In this paper we measure the average jet multiplicity

$$\langle n_{\text{jet}} \rangle = \frac{1}{N} \sum_{i=1}^N n_{\text{jet}}^i$$

as a function of y_{cut} . Here N is the total number of events.

5. Measurement of event shape variables

The four distributions T , ρ , EEC and $\langle n_{\text{jet}} \rangle$ are measured separately from calorimetric clusters and charged tracks. In the first case energies and in the second case particle momenta are used. The particle masses are assumed to be zero. In the above definitions we replace the center of mass energy \sqrt{s} by the measured sum of all energies or momenta, respectively.

We measure the event shape distributions T , ρ , EEC and the jet fractions $f_i = \sigma_{i\text{-jets}}/\sigma_{\text{tot}}$ in the form of histograms. These distributions are corrected for detector effects, acceptance and resolution, and initial and final state photon radiation. The average jet multiplicity $\langle n_{\text{jet}} \rangle$ is then calculated from the jet fractions f_i . We choose the histogram bin widths such that they are bigger than the experimental resolution by a factor of at least 1.5. The detector resolution effects for the

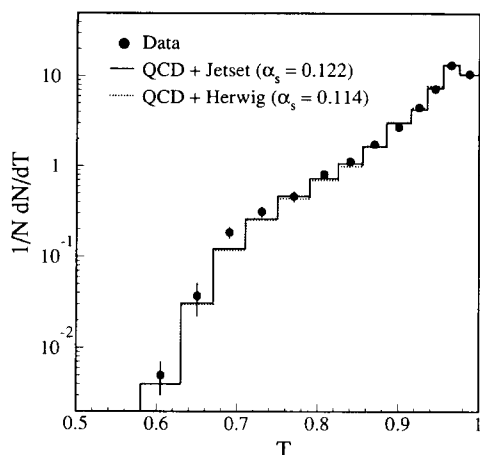


Fig. 1. Measured thrust distribution in comparison with the QCD predictions. The theoretical curves are calculated for a scale $\mu = 91.2$ GeV and the fitted $\alpha_s(m_Z)$ values as shown in the figure. The solid (dashed) line is obtained using JETSET (HERWIG) for the hadronization correction.

observables thrust and scaled heavy jet mass squared are corrected using the regularized unfolding program [25], as described in ref. [19]. The EEC distribution is corrected bin by bin [6]. The jet fractions are determined using a matrix unfolding procedure [1]. The resolution function is given implicitly by Monte Carlo events. They are generated by the programs JETSET 7.3 and HERWIG 5.3 and include the full detector simulation. To correct for detector acceptance and in particular for the cut in $\cos\theta_{\text{thrust}}$, we apply a bin-by-bin correction. Similarly we correct for initial and final state radiation. The systematic errors on each unfolded data point are due to uncertainties in the detector simulation and biases from the Monte Carlo program used for the unfolding. Statistical uncertainties are negligible. The sizes of the experimental errors are estimated by

- varying the energy response of the calorimeters in the Monte Carlo simulation,
- analyzing the difference in the unfolded distributions using the programs JETSET and HERWIG,
- comparing the corrected distributions obtained from calorimetric clusters and charged tracks.

The experimental uncertainties are typically a few percent per histogram bin.

The corrected distributions of the observables T

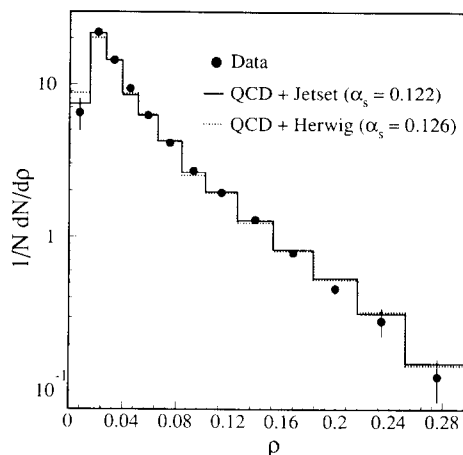


Fig. 2. Measured distribution of the variable scaled heavy jet mass squared ρ in comparison with the QCD predictions. The theoretical curves are calculated for a scale $\mu = 91.2$ GeV and the fitted $\alpha_s(m_Z)$ values as shown in the figure. The solid (dashed) line is obtained using JETSET (HERWIG) for the hadronization correction.

and ρ are shown in figs. 1 and 2 and given in tabular form in ref. [19]. The EEC distribution is shown in fig. 3 (back-to-back region only) and given in table 1. It agrees within errors with our previous measurement [6], which covered only the central region between 25.2° and 154.8° . The average jet multiplicities as function of y_{cut} are listed in table 2 and are shown in fig. 4.

6. QCD predictions

The QCD predictions in fixed order perturbation theory can not take into account the effect of multiple gluon emission. In second order calculations two gluons can be emitted at most. For variables like thrust, heavy jet mass etc. this leads to a singular behavior of the distributions in kinematic regions where multi-gluon emission becomes dominant. This is a direct consequence of the collinear and infrared divergence of the gluon emission cross section. It is possible to isolate the singular terms in every order of perturbation theory and to sum them up in the form of an exponential series. One thus obtains a meaningful result for all regions of phase space. In the calculations described in refs. [9-11] and used for this analysis, all

Table 1

Measured EEC distribution corrected for detector effects and photon radiation. The errors are the combined statistical and systematic uncertainties.

χ	EEC(χ)	χ	EEC(χ)
0.0°–3.6°	2.21 ± 0.10	176.4°–180.0°	0.80 ± 0.02
3.6°–9.0°	1.15 ± 0.06	171.0°–176.4°	1.27 ± 0.04
9.0°–14.4°	0.66 ± 0.02	165.6°–171.0°	0.90 ± 0.03
14.4°–19.8°	0.41 ± 0.01	160.2°–165.6°	0.60 ± 0.02
19.8°–25.2°	0.272 ± 0.008	154.8°–160.2°	0.418 ± 0.013
25.2°–30.6°	0.201 ± 0.006	149.4°–154.8°	0.307 ± 0.009
30.6°–36.0°	0.159 ± 0.005	144.0°–149.4°	0.237 ± 0.007
36.0°–41.4°	0.133 ± 0.005	138.6°–144.0°	0.190 ± 0.006
41.4°–46.8°	0.115 ± 0.004	133.2°–138.6°	0.157 ± 0.005
46.8°–52.2°	0.102 ± 0.003	127.8°–133.2°	0.134 ± 0.004
52.2°–57.6°	0.093 ± 0.003	122.4°–127.8°	0.117 ± 0.004
57.6°–63.0°	0.086 ± 0.003	117.0°–122.4°	0.104 ± 0.003
63.0°–68.4°	0.081 ± 0.002	111.6°–117.0°	0.095 ± 0.003
68.4°–73.8°	0.078 ± 0.002	106.2°–111.6°	0.088 ± 0.003
73.8°–79.2°	0.076 ± 0.003	100.8°–106.2°	0.083 ± 0.003
79.2°–84.6°	0.075 ± 0.002	95.4°–100.8°	0.079 ± 0.003
84.6°–90.0°	0.075 ± 0.002	90.0°–95.4°	0.076 ± 0.002

Table 2

Measured average jet multiplicities for the k_{\perp} algorithm. All numbers are corrected for detector effects and photon radiation. The errors are the combined statistical and systematic uncertainties.

y_{cut}	$\langle n_{\text{jet}} \rangle$
0.001	3.93 ± 0.07
0.002	3.20 ± 0.03
0.004	2.75 ± 0.018
0.006	2.581 ± 0.013
0.008	2.492 ± 0.010
0.010	2.428 ± 0.009
0.020	2.269 ± 0.006
0.040	2.153 ± 0.003
0.060	2.102 ± 0.003
0.090	2.071 ± 0.003
0.100	2.053 ± 0.003
0.120	2.038 ± 0.003
0.140	2.028 ± 0.002
0.160	2.021 ± 0.002
0.180	2.016 ± 0.001
0.200	2.012 ± 0.001
0.220	2.0077 ± 0.0010
0.240	2.0052 ± 0.0010
0.260	2.0029 ± 0.0010
0.280	2.0016 ± 0.0006

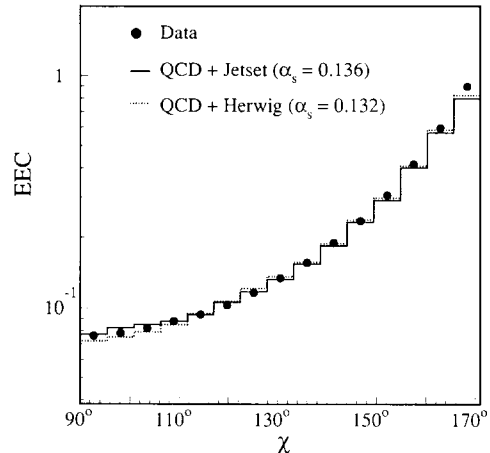


Fig. 3. Measured energy-energy correlation function EEC in comparison with the QCD predictions. The theoretical curves are calculated for a scale $\mu = 91.2$ GeV and the fitted $\alpha_s(m_Z)$ values as shown in the figure. The solid (dashed) line is obtained using JETSET (HERWIG) for the hadronization correction.

second order terms [26,27] are included together with leading and next-to-leading corrections to all orders. These corrections are of the form $\alpha_s^n \ln^m y$ with $n \geq 1$ and $m \geq n$. Subleading terms of the form $\alpha_s^n \ln^m y$ with $m < n$ are not included beyond second order

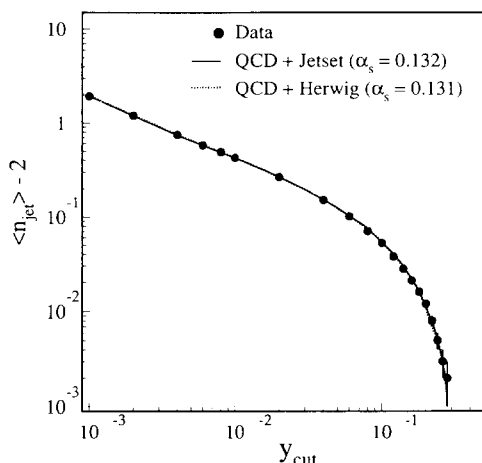


Fig. 4. Measured distribution of the average jet multiplicity $\langle n_{\text{jet}} \rangle$ as a function of y_{cut} in comparison with the QCD predictions. The theoretical curves are calculated for a scale $\mu = 91.2$ GeV and the fitted $\alpha_s(m_Z)$ values as shown in the figure. The solid (dashed) line is obtained using JETSET (HERWIG) for the hadronization correction.

($n > 2$). Here y stands for $1 - T$, ρ , $(1 + \cos\chi)/2$ and y_{cut} , respectively. In the 2-jet region y is small and the corrections large. An important improvement of the new QCD calculations with respect to the second order formulas is their ability to describe also the low y region. The authors of refs. [9–11,16] have provided us with computer programs which we used for the QCD calculations.

The calculations for the distributions of the four variables V ($= T, \rho, \chi, y_{\text{cut}}$) are given in the form of analytical functions

$$f^{\text{pert}}(V; s, \alpha_s(\mu), \mu).$$

The strong coupling constant α_s is evaluated at the renormalization scale μ . To translate the value $\alpha_s(\mu)$ into $\alpha_s(m_Z)$ we use the relation given in ref. [28] for 5 quarks. The QCD calculations contain terms to all orders in α_s , and $\mu = \sqrt{s}$ is expected to be a good choice of the renormalization scale [9–11,16]. We estimate the uncertainty due to the approximations made in the calculations of the terms beyond second order by a variation of the scale between $0.5\sqrt{s}$ and $2\sqrt{s}$. This leads to an estimated uncertainty in α_s of about $\Delta\alpha_s = \pm 0.005$.

To study the effects of hadronization and decays we use the parton shower programs JETSET 7.3 and

HERWIG 5.4 with string and cluster fragmentation, respectively. The fragmentation parameters are determined from a comparison of predicted and measured distributions for several event shape variables [19,29]. Both generators are found to give a good description of our measurements. We fold the perturbative calculations for T and ρ with the probability $p^{\text{non-pert}}(V', V)$ to find a value V after fragmentation and decays for a parton level value V' :

$$f(V) = \int f^{\text{pert}}(V') \cdot p^{\text{non-pert}}(V', V) dV'.$$

For the EEC distribution and the average jet multiplicity we apply a bin-by-bin hadronization correction. We compare the resulting differential cross section $f(V)$ to our measurements. The correction for hadronization and decays changes the perturbative prediction by less than 5% for the distributions thrust and scaled heavy jet mass squared, with the exception of the regions $T > 0.93$ and $\rho < 0.07$, where the effect reaches 15%. The EEC distribution is modified by 5%–15%. The quantity $\langle n_{\text{jet}} \rangle - 2$ is modified by less than 5%.

We estimate the uncertainties in the probabilities $p^{\text{non-pert}}(V', V)$ and the corresponding error in α_s by

- a change of fragmentation parameters in the JETSET model within their errors [19],

- a variation of the parton shower cutoff Q_0 between 1 GeV and 2 GeV in the JETSET program and of the fragmentation parameters accordingly [19],

- a comparison between the predictions of the two models JETSET and HERWIG.

The uncertainties estimated with the first two methods are found to be small ($\Delta\alpha_s = \pm 0.002$) compared to the differences between HERWIG and JETSET. Those correspond to differences in the measured strong coupling constants of up to 0.008.

The effect of quark masses, in particular for $b\bar{b}$ events, which is not included in the QCD calculations, is found to be negligible for the measurement of α_s [30].

7. Results

In order to derive $\alpha_s(m_Z)$, we fit the theoretical distribution $f(V)$ to the measured event shape distributions for a fixed scale $\mu = \sqrt{s}$. For the fit we use

Table 3

Central values and errors of $\alpha_s(m_Z)$ derived from the event shape variables thrust, heavy jet mass, EEC and average jet multiplicity.

Observable	Fit range	$\alpha_s(m_Z)$	Exp. err.	Hadr. unc.	Scale unc.
thrust	$0.71 \leq T \leq 1.0$	0.118	± 0.004	± 0.004	+0.007 -0.004
jet mass	$0.0 \leq \rho \leq 0.3$	0.124	± 0.003	± 0.003	+0.006 -0.004
EEC	$90^\circ \leq \chi \leq 171^\circ$	0.134	± 0.003	± 0.003	+0.004 -0.006
$\langle n_{\text{jet}} \rangle$	$0.002 \leq y_{\text{cut}} \leq 0.1$	0.132	± 0.003	± 0.002	+0.005 -0.003

the ranges as given in table 3. In case of the variables T and ρ they correspond to regions dominated by 2 and 3-jet production ($y < 0.3$). The χ range corresponds to the region for which the new EEC calculations are available. Since the average jet multiplicities at neighboring y_{cut} values are strongly correlated, we have included in the fit only the points at $y_{\text{cut}} = 0.002, 0.02$ and 0.10 . We later compare data and QCD calculations for values of y_{cut} above 0.001, corresponding to a transverse momentum k_\perp of about 3 GeV. For smaller values of the jet resolution parameter the effects of hadronization and decays become very large. The values of $\alpha_s(m_Z)$ derived from the four event shape variables together with their systematic errors are shown in table 3. Figs. 1 to 4 show the QCD fits in comparison with the experimental data. Two curves are shown, corresponding to the hadronization correction using JETSET and HERWIG and the fitted α_s values. In all cases a good fit is obtained.

The results in table 3 are the mean values of the two α_s values obtained with JETSET and HERWIG fragmentation correction. The hadronization error is taken to be the quadratic average of half the difference of those two α_s values and the uncertainties estimated by changing fragmentation parameters and the parton shower cutoff inside JETSET as described above. The experimental uncertainties in table 3 are determined by repeating the α_s determination for different energy response factors and unfolding methods, and by using tracks instead of calorimetric clusters. The scale error is obtained by repeating the α_s fit for different values of the renormalization scale in the interval $0.5\sqrt{s} \leq \mu \leq 2\sqrt{s}$. For all these scales a good fit is obtained except for the energy-energy correlations, which give a large χ^2 value for scales below \sqrt{s} . To investigate the dependence of our results on the fit range we have omitted up to two bins at either end of the interval

and repeated the fit. In all cases the results differ from the α_s values quoted in table 3 by at most 0.001.

The values for the strong coupling constant derived from thrust and heavy jet mass are consistent with those reported in refs. [9,5,31]. The α_s value obtained from the average jet multiplicity agrees within errors with the strong coupling constant measured from the differential 2-jet rate [31].

The α_s values from the distributions thrust, heavy jet mass and energy-energy correlations are affected differently by higher order corrections and hadronization effects. To obtain a combined value for the strong coupling constant we take the unweighted average of the first three α_s values of table 3 and obtain $\alpha_s = 0.125 \pm 0.003$ (exp). Since in the calculation of the average jet multiplicity some terms are missing, we prefer not to include the last α_s value in table 3 in our combined result [17].

We estimate the total theoretical error, due to both the approximations in the higher order corrections and hadronization effects, independently – from the quadratically combined errors for hadronization and scale dependence in table 3, resulting in approximately $\Delta\alpha_s = \pm 0.006$, – and from the spread of the three α_s values from thrust, heavy jet mass and EEC, yielding ± 0.008 .

The two estimates agree well. We conservatively assign the larger one as the theoretical uncertainty in our α_s determination.

The combined result is therefore

$$\alpha_s(m_Z) = 0.125 \pm 0.003 \text{ (exp)} \pm 0.008 \text{ (theor)} .$$

This result agrees within errors with the values of the strong coupling constant which we measured pre-

viously^{#1}. The α_s value of 0.125 also agrees with our measurement of $\alpha_s = 0.134 \pm 0.030$ from an analysis of the partial hadronic Z^0 width [32].

8. Summary and conclusions

We have determined the strong coupling constant with a precision of 7% from hadronic event shapes measured on the Z^0 resonance using new QCD calculations including exponentiation of leading and next-to-leading terms. We obtain

$$\alpha_s(91.2 \text{ GeV}) \\ = 0.125 \pm 0.003(\text{exp}) \pm 0.008(\text{theor}).$$

The error is dominated by theoretical uncertainties due to approximations in the perturbative calculations and hadronization effects. This error is estimated from the spread of the α_s values obtained from the shape variables thrust, heavy jet mass and energy-energy correlations. Based on the results in table 3 we arrive at an estimate of the theoretical error which is larger than the estimate of about ± 0.004 in refs. [5,31]. A better determination of the theoretical uncertainties will become possible when the new calculation techniques have been applied to several more event shape variables.

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^{#1} We found $\alpha_s = 0.116 \pm 0.011$ from jet production [1], 0.122 ± 0.011 from energy-energy correlations and 0.115 ± 0.009 from the asymmetry of energy correlations [6]. The average of these numbers is 0.118 ± 0.010 .

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