Constraints on diffuse gamma-ray emission from structure formation processes in the Coma cluster

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ABSTRACT
We analyse five-year (63 months) data of the Large Area Telescope on board Fermi satellite from the Coma galaxy cluster in the energy range between 100 MeV and 100 GeV. The likelihood analyses are performed with several templates motivated by models predicting gamma-ray emission due to structure formation processes. We find no excess emission and derive the most stringent constraints to date on the Coma cluster above 100 MeV, and on the tested scenarios in general. The upper limits on the integral flux range from $10^{-10}$ to $10^{-9}$ cm$^{-2}$ s$^{-1}$, and are stringent enough to challenge different scenarios. We find that the acceleration efficiency of cosmic ray protons and electrons at shocks must be below approximately 15 and 1 per cent, respectively. Additionally, we argue that the proton acceleration efficiency should be lower than 5 per cent in order to be consistent with radio data. This, however, relies on magnetic field estimates in the cluster. In particular, this implies that the contribution to the diffuse extragalactic gamma-ray background due to gamma-rays from structure formation processes in clusters of galaxies is negligible, below 1 per cent. Finally, we discuss future detectability prospects for Astro-H, Fermi after 10-yr of operation, and the Cherenkov Telescope Array.

Key words: galaxies: clusters: individual: Coma – gamma-rays: galaxies: clusters.

1 INTRODUCTION
According to the hierarchical scenario, structures form via accretion and merger of smaller objects into larger ones. Clusters of galaxies are the latest and largest structures to have formed in the Universe. They have typical radii of a few Mpc, and masses of about $10^{14}$–$10^{15}$ M$\odot$. Dark matter contributes for about 80 per cent of their mass, gas for 15 per cent and galaxies for 5 per cent (Voit 2005). During the course of a cluster formation, part of its gravitational binding energy, of the order of $10^{61}$–$10^{63}$ erg, should be dissipated through turbulence and structure formation (accretion and merger) shocks that accelerate charged particles such as protons and electrons. Even if only a small fraction of this energy goes into the particle acceleration, the process should be strong enough to make the clusters visible with non-thermal emissions such as radio synchrotron emission, and potentially in gamma-ray frequencies.

Diffuse radio synchrotron emission is detected in the Coma cluster both as a central radio halo and as a peripheral radio relic (e.g. Deiss et al. 1997; Brown & Rudnick 2011). This proves the presence of relativistic electrons and magnetic fields permeating the intracluster medium (ICM). Radio relics are apparently connected to structure-formation shocks (e.g. van Weeren et al. 2011), even though the details of the particle acceleration process at place are not clear yet (e.g. Ogrean et al. 2013; Pinzke, Oh & Pfrommer 2013). Radio haloes can be further divided into two categories: mini-haloes and giant haloes. The former is associated with relaxed, cool-core clusters, and typically extend over a few hundred kpc. The latter, such as the one found in Coma, is typically associated with cluster mergers and have Mpc-sizes (see Peretti et al. 2012, for a review). The generation mechanism of radio haloes is currently debated between re-acceleration (e.g. Brunetti & Lazarian 2007, 2011; Brunetti et al. 2012) and hadronic models (e.g. Pfrommer & Enßlin 2004a,b; Pfrommer, Enßlin & Springel 2008; Enßlin et al. 2011; Zandanel, Pfrommer & Prada 2014b).

Cosmic ray (CR) electrons can generate X-ray and gamma-ray emission through inverse Compton (IC) up-scattering of cosmic microwave background (CMB) photons. Additionally, if the radio emission is due to secondary electrons generated in hadronic interactions between CR protons and the ICM, it should be accompanied by a detectable gamma-ray emission generated from neutral pion decays.

Observationally, gamma-ray emission from clusters of galaxies were searched for the last several years to decade, but all these attempts resulted in no detection (for space-based cluster observations in the GeV band, see Reimer et al. 2003; Fermi-LAT Collaboration 2010a,c; Ando & Nagai 2012; Han et al. 2012; Zimmer, Conrad & Pinzke 2012; Huber et al. 2013 for ground-based...
observations in the energy band above $\sim$100 GeV, see Perkins et al. 2006; Perkins 2008; Domainko et al. 2009; Galante et al. 2009; HESS Collaboration 2009a,b, 2012; Kiuchi et al. 2009; VERITAS Collaboration 2009, 2012; MAGIC Collaboration 2010, 2012). Recently, both Fermi-LAT Collaboration (2013) and Prokhorov & Churazov (2013) performed a joint likelihood analysis of about 50 galaxy clusters. They found a significant gamma-ray excess in the direction of few objects, particularly Abell 400, which however is interpreted either as coming from active galactic nuclei (AGN) within the cluster or as un-modelled background.

The Large Area Telescope (LAT) on board Fermi satellite\(^1\) continuously surveys the gamma-ray sky since 2008 August, and its data represent a unique tool to test diffuse CR emission models in clusters of galaxies. Although many previous analyses of the Fermi-LAT data of galaxy clusters were based on the assumption that the clusters were simply point sources (PS) or have a very simple extended profile, a possible cluster gamma-ray emission could have very different spatial structure compared with what were investigated so far. Predicted gamma-ray emission profiles and spectra differ depending on models of cluster formation as well as particle acceleration, and thus, by detecting or constraining them, one could learn important physics thereof, which is still completely missing and well awaited.

In this paper, we take a deeper look at the Fermi-LAT data for GeV gamma-ray emission from the Coma cluster and its possible diffuse emission induced by CR interactions. We chose Coma because it is one of the best-studied clusters, which is located in a local volume (its distance is about 100 Mpc). It also shows evidence of recent dynamical activities such as particle accelerations, as seen from presence of a giant radio halo and a radio relic. Together with the fact that there are no AGN found in the LAT data, these make Coma an ideal environment to test CR-induced gamma-ray emission. We perform dedicated analyses of 63-month Fermi-LAT data using well-motivated models for spatial emission distribution. Besides the simplest PS model, we investigate (1) models based on hydrodynamical simulations of the cluster formation that also trace interactions of CR protons with the ICM; (2) a model motivated by spatial profile of the radio relic, and (3) disc and ring-like profiles motivated by scenarios where primary electrons accelerated by accretion shocks dominate the cluster high-energy emission. We find no positive signatures in any of these scenarios, and thus, put the most constraining upper limits (ULs) to date on the gamma-ray flux from Coma for each model and interpret them in terms of constraints on parameters of cluster formation and CR physics.

This paper is organized as follows. In Section 2, we describe details of the Fermi-LAT data analyses for Coma. Several theoretical model templates of the gamma-ray emission are explained in Section 3. We present our results in Section 4 and conclude in Section 5.

\section{Data Analysis}

We analysed 63 months (2008-08-04 15:43:37 to 2013-11-08 03:01:59) of Fermi-LAT reprocessed Pass 7 (P7REP) data of the Coma galaxy cluster using Fermi Science Tools (v9r32p5).\(^2\) We adopted the standard event selection cuts suggested by the LAT collaboration and analysed events between 100 MeV and 100 GeV. We analysed both SOURCE and CLEAN events (Fermi event class 2 and 3, respectively), adopting the corresponding latest instrumental response functions (P7REP_V15), and we found good agreement between the two. In the following, we report the results for the standard \textit{binned} likelihood analysis of the SOURCE events only.

We select a region of interest (ROI) of $10^\circ$ radius around the Coma cluster centre (RA = 194.95, Dec. = 27.94). We then bin the data into 0.1 pixels and 30 logarithmic steps in energy. This angular size is chosen to match the size of the point spread function achieved by Fermi-LAT at the highest energies, while it is significantly worse at low energies (about $10^\circ$ and $1^\circ$ at 100 MeV and 1 GeV, respectively; Fermi-LAT Collaboration 2012). The left-hand panel of Fig. 1 shows the photon count map of $14^\circ \times 14^\circ$, used for our binned analysis. The corresponding exposure map is computed for an area of $40^\circ \times 40^\circ$ centred on the cluster.

As a first step, we performed the analysis including all 26 PS within $15^\circ$ from the cluster centre, found in the 2-year

\footnotesize{\begin{itemize}
\item \(^1\) http://fermi.gsfc.nasa.gov/ \hspace{1cm} \(^2\) http://fermi.gsfc.nasa.gov/ssc/data/analysis/
\end{itemize}}
In order to compare with the latest constraints obtained from the Fermi-LAT Collaboration (2013), we calculate the UL for their extended model (which corresponds to our PP model; see next section) for energies above 500 MeV obtaining $3.2 \times 10^{-10}$ cm$^{-2}$ s$^{-1}$, Fermi-LAT Collaboration (2013) obtained $4 \times 10^{-10}$ cm$^{-2}$ s$^{-1}$. Note that we adopt slightly different radius, mass and gas density values for the cluster modelling with respect to Fermi-LAT Collaboration (2013) which imply that our total flux above 500 MeV is a factor of about 1.1 larger. We achieve a more stringent UL due to this choice and thanks to the longer observation time (they used 48 months of data). Note also that while Fermi-LAT Collaboration (2013) uses CLEAN events, we report the result for the SOURCE events.

### 3 DIFFUSE EMISSION FROM CRs

In this section, we describe in detail the tested diffuse emission models. We show some relevant model templates used in our analysis in Fig. 2.

#### 3.1 Gamma-rays from pion decays

Pinzke & Pfrommer (2010, hereafter PP) performed hydrodynamical simulations of galaxy clusters considering, in particular, diffusive shock acceleration at structure formation shocks. They provided predictions for the gamma-ray emission from CR protons and electrons, and showed that the emission coming from pion decays dominates over the IC emission of both primary and secondary electrons for gamma-rays with an energy above 100 MeV. They then provide a semi-analytical model for the pion-decay-induced emission that depends on a given cluster mass and ICM density. The

![Figure 2](http://mnras.oxfordjournals.org/)

\[
\text{UL integrated } F \times 10^{-9} \text{ cm}^{-2} \text{ s}^{-1} \times (10^{-1} \text{ cm})^{1.18} \times (10^{-2} \text{ s})^{0.09} = 0.62
\]

\[
\text{UL} = F \times 10^{-9} \text{ cm}^{-2} \text{ s}^{-1} \times (10^{-1} \text{ cm})^{1.18} \times (10^{-2} \text{ s})^{0.09} = 2.91
\]

\[
\text{UL} = F \times 10^{-9} \text{ cm}^{-2} \text{ s}^{-1} \times (10^{-1} \text{ cm})^{1.18} \times (10^{-2} \text{ s})^{0.09} = 2.59
\]

\[
\text{UL} = F \times 10^{-9} \text{ cm}^{-2} \text{ s}^{-1} \times (10^{-1} \text{ cm})^{1.18} \times (10^{-2} \text{ s})^{0.09} = 2.59
\]

\[
\text{UL} = F \times 10^{-9} \text{ cm}^{-2} \text{ s}^{-1} \times (10^{-1} \text{ cm})^{1.18} \times (10^{-2} \text{ s})^{0.09} = 2.59
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\text{UL} = F \times 10^{-9} \text{ cm}^{-2} \text{ s}^{-1} \times (10^{-1} \text{ cm})^{1.18} \times (10^{-2} \text{ s})^{0.09} = 2.59
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\text{UL} = F \times 10^{-9} \text{ cm}^{-2} \text{ s}^{-1} \times (10^{-1} \text{ cm})^{1.18} \times (10^{-2} \text{ s})^{0.09} = 2.59
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\]
The CR proton acceleration efficiency attains its maximum, \( \xi_p \), for high Mach number shocks, while it is lower for lower Mach numbers. The exact Mach number dependence of the acceleration efficiency is very uncertain. In this work, we use as reference the PP simulations that depend on the Enßlin et al. (2007) model for diffusive shock acceleration for which \( \xi_p \), in the case of interest for clusters, is reached for Mach numbers of about 3. We note, however, that more detailed models such as the Kang & Ryu (2013) model, in the context of non-linear diffusive shock acceleration, shows a different dependence, and the acceleration efficiency saturates at higher Mach numbers with respect to Enßlin et al. (2007). Because of the early saturation in the Enßlin et al. (2007) model, our constraints on the efficiency could be regarded as conservative in the low Mach number regime where more refined models show lower efficiencies.

\[ F_{\gamma, pp}(>E) = A_p \lambda_{\gamma, pp}(>E) \int k_{pp}(R) \, dV, \]

where \( \lambda_{\gamma, pp}(>E) \) and \( k_{pp}(R) \) contain the spectral and spatial information, respectively, and are given in PP. \( A_p \) is a dimensionless scale parameter related to the maximum CR proton acceleration efficiency \( \xi_p \) for diffusive shock acceleration, which is the maximum ratio of CR energy density that can be injected with respect to the total dissipated energy at the shock. \( A_p = 1 \) for \( \xi_p = 0.5 \), and decreases for smaller efficiencies obeying a non-linear relation (PP). However, note that the relation \( A_p - \xi_p \) is linear for CR protons with an energy \( \gtrsim 10 \) GeV which corresponds to pion-decay emission with energies \( \gtrsim 1 \) GeV (Pinzke, private communication).

The PP predictions have already been challenged by recent gamma-ray observations (MAGIC Collaboration 2010, 2012; Pinzke, Pfrommer & Bergström 2011; Han et al. 2012; VERITAS Collaboration 2012; Fermi-LAT Collaboration 2013), suggesting either that the maximum CR proton acceleration efficiently at shocks is significantly lower than 50 per cent, an optimistic value adopted in simulations, or the presence of CR streaming and diffusion out of the cluster core (Enßlin et al. 2011; Wiener, Oh & Guo 2013; Zandanel et al. 2014b).

We test the PP spatial and spectral semi-analytical model for the Coma cluster, where the cluster mass is taken from Reiprich & Böhringer (2002) and the ICM radial profile from Briel, Henry & Boehringer (1992). In the PP model, only about 5 per cent of the total emission is coming from radii beyond the virial radius, and therefore, we decide to limit our analysis within the virial radius \( R_{200} = 2.3 (h/0.7)^{-1} \) Mpc.

Note, however, that assuming the magnetic field in the cluster is distributed according to

\[ B(r) = B_0 \left( \frac{\rho_{gas}(r)}{\rho_{gas}(0)} \right)^{\alpha_B}, \]

where \( \rho_{gas} \) is the ICM distribution, \( B_0 = 5 \) \( \mu \)G and \( \alpha_B = 0.5 \) as suggested by Faraday rotation (FR) measurements in Coma (Bonafede et al. 2010), the radio synchrotron emission (see, e.g. appendices of Zandanel et al. 2014b) predicted by the PP semi-analytical model does not match the spatial profile of the giant radio halo of the cluster at 1.4 GHz (Deiss et al. 1997), being much more peaked, as shown in Fig. 3. Additionally, it overproduces the central radio emission for a maximum acceleration efficiency \( \gtrsim 5 \) per cent (assuming a linear scaling of \( A_p \) with \( \xi_p \)).

Zandanel et al. (2014b, hereafter ZPP) extended the PP semi-analytical model with the inclusion of an effective parametrization for CR transport phenomena, effectively redefining \( k_{pp}(R) \) of equation (1). Since the CR transport is determined by competition among advection due to turbulent motion of gas, CR streaming, and diffusion, its efficiency can be represented by a parameter

\[ \gamma_u = \frac{\tau_u}{\tau_{u,s}}, \]

i.e. a ratio of a characteristic time-scale of streaming, \( \tau_u \), and that of turbulence, \( \tau_{u,s} \) (Enßlin et al. 2011). The parameter \( \gamma_u \) ranges from 100, for highly turbulent cluster and centrally peaked CR distributions, to 1, for relaxed clusters and flat distributions as CRs move towards the outskirts. When \( \gamma_u \geq 100 \), the model reproduce the advection-dominated case of PP, where CR transport treatment is not included. We test the ZPP model for the case of \( \gamma_u = 2 \) (ZPP-2), matching the observed surface brightness profile of the

\[ \text{Figure 3. Surface brightness of the Coma cluster calculated as in ZPP. Left. Surface brightness of the giant radio halo at 352 MHz (Brown & Rudnick 2011) and 1.4 GHz (Deiss et al. 1997). Shown are the ZPP-2 model, and the ZPP-100 and PP models scaled down with } A_p = 0.1 \text{ such that they do not overshoot the radio emission. Right. Gamma-ray surface brightness for energies above 100 MeV for the ZPP-2 model, and ZPP-100 and PP models scaled down with } A_p = 0.1. \]
Coma radio halo at 1.4 GHz (see Fig. 3). Note that Coma is classified as merging cluster and one would expect it to be turbulent and not relaxed. Therefore, according to Enßlin et al. (2011), high \( \gamma_u \) values and a centrally peaked CR distribution should be realized. Wiener et al. (2013) found a solution to this problem showing that, when considering turbulent damping, turbulence may promote outward streaming more than inward advection, therefore allowing for flat CR profiles also in turbulent clusters.

At this point, one may ask how representative is the giant radio halo of the Coma cluster, particularly the parameters’ values needed for its modelling. While we cannot say with certainty that these are common to all merging clusters hosting diffuse radio emission without an extensive analysis of the whole sample, we note that ZPP found the same characteristics, in particular the need for low \( \gamma_u \) values, in the giant radio halo of the merging cluster Abell 2163. This is due to the large radial extension and shallow profile of the surface brightness of these objects, which appear to be a common property among giant radio haloes (Feretti et al. 2012).

However, ZPP showed that even in the extreme case of a flat CR distribution, \( \gamma_u = 1 \), it is not possible to hadronically reproduce the 352 MHz surface brightness of the giant radio halo of Coma (Brown & Rudnick 2011). This favours re-acceleration models (Brunetti et al. 2012), or hybrid scenarios where only part of the radio emission is of hadronic origin (see ZPP for an extensive discussion). In this case, a centrally peaked CR distribution could still be realized and only partially contribute to the total observed radio emission. We therefore test also a ZPP model with \( \gamma_u = 100 \) (ZPP-100). Note that this is decreasing slightly faster towards the cluster outskirts than the PP model because of the inclusion of the characteristic radial decline of the temperature (ZPP; see Figs 2 and 3).

Also for the ZPP models we limit our analysis within \( R_{200} \). Both for PP and ZPP models, we let the normalization of the emission to vary. The spectral shape is fixed to the PP model prediction, featuring the characteristic pion bump at GeV energies followed by a concave spectrum that approaches a power law with spectral index of about 2.2 at TeV energies (see fig. 12 of PP). We warn that by fixing the CR spectra to the PP findings, we exclude a potential free parameter that would affect our conclusions (see e.g. MAGIC Collaboration 2012; VERITAS Collaboration 2012).

### 3.2 Gamma-ray from IC scattering

Kushnir & Waxman (2009) developed an analytical model, adopting a CR power-law energy spectrum with a spectral index of \( -2 \), and predicted that the IC emission from primary electrons accelerated at accretion shocks dominates over the pion-decay-induced emission. Considering the differences in acceleration efficiency and injected spectra may reconcile the findings by Kushnir & Waxman (2009) and PP (see Fermi-LAT Collaboration 2013, for a detailed discussion). However, instead of the centrally concentrated gamma-ray emission from neutral pion decays, Kushnir & Waxman (2009) found a spatially extended IC-induced emission out to the accretion shocks beyond the cluster’s virial radius. This model predict a practically flat gamma-ray emission up to the outer accretion shocks location where it should then peak (see fig. 2 of Kushnir & Waxman 2009). We therefore test this model with a flat disc template of 1’ of radius. We consider a power-law spectrum with a fixed \( \Gamma = -2 \).

Kushnir & Waxman (2009) predict that the radio emission should be dominated by secondaries. The corresponding profile of the radio surface brightness is similar to the ZPP model with a low \( \gamma_u \) value, potentially being able to explain the 1.4 GHz data for the Coma giant halo but also suffering the same problems discussed in the previous section when trying to reproduce the 352 MHz data. Additionally, we note that Kushnir & Waxman (2009) assume a constant magnetic field in the cluster core, which is in contrast with FR estimates in Coma (Bonafede et al. 2010), and implies a shallower radio profile. Accretion of intracluster gas should generate strong virial shock waves around galaxy clusters and, according to several scenarios, this could potentially lead to ring-like emission features at different frequencies (Loeb & Waxman 2000; Totani & Kitayama 2000; Waxman & Loeb 2000; Miniati 2002; Keshet et al. 2003; Keshet, Waxman & Loeb 2004; Kocsis, Haiman & Frei 2005; Kushnir & Waxman 2010). Note however that latest state-of-the-art cosmological hydrodynamical simulations of galaxy clusters do not show the presence of such features (Pfrommer 2008; Pfrommer et al. 2008; PP).

Recently, Keshet et al. (2012) claimed the detection of a ring-like structure in the gamma-ray sky map of the Coma cluster in the VERITAS data (VERITAS Collaboration 2012) and interpreted this as IC-induced emission due to accretion shocks around the cluster. Therefore, we searched for the presence of this structure: it is a 0.5-wide elliptical shape with a semi-minor axis of about 1.3, elongated towards the east–west direction. We consider cases where the semi-major axis is of 2’, and of 3’ with the structure tilted towards the south-west direction for 5’. The latter case corresponds to the best fit of Keshet et al. (2012), confirmed also by comparison with simulations by Keshet et al. (2003). We refer to these as ellipse models. We additionally consider the case of a 0.5-wide ring with radius of \( R_{200} \) (ring model). In all the cases, we uniformly fill the tested structure, and we consider a power-law spectrum with a fixed \( \Gamma = -2 \).

We finally consider also a phenomenological template based on the radio relic observed in Coma outskirts, which is associated with structure-formation phenomena. Recent observations, both in radio and X-rays, support the idea that it is connected to an infall shock front due to the NGC 4839 group falling on to the cluster (Brown & Rudnick 2011; Akamatsu et al. 2013; Ogrean & Brüggen 2013; Simionescu et al. 2013) rather than a cluster-merger shock. Either way, the corresponding CR electrons could generate IC gamma-ray emission. We use the Green Bank Telescope (GBT) observation at 1.4 GHz presented by Brown & Rudnick (2011) to generate a spatial template for the relic. We can use such an approach if we assume that the magnetic field is almost uniform across the relic (Bonafede et al. 2013). This approximation is well justified in our case considering the poor Fermi angular resolution with respect to radio observations. We therefore use the outermost contour of the GBT radio relic image from fig. 2 of Brown & Rudnick (2011) to construct its spatial template, which we uniformly fill. We refer to this as the relic model. We let the normalization to vary, and we use a power law for the radio spectrum with a fixed \( \Gamma = -1.18 \), as inferred from the observed radio spectrum (Thierbach, Klein & Wielebinski 2003).

### 4 RESULTS AND IMPLICATIONS

In the following subsections, we discuss the implications of our findings for each of the considered models. Table 1 summarizes the obtained ULs.

#### 4.1 Pion-decay emission

In the PP and ZPP-100 models, assuming a maximum CR proton acceleration efficiency of 50 per cent, we would expect a total flux
above 100 MeV and within $R_{200}$ of 4.14 and $3.24 \times 10^{-9}$ cm$^{-2}$ s$^{-1}$, respectively. The obtained ULs (see Table 1) are a factor of 0.26 and 0.28 of the theoretical expectations, respectively. This suggest that the maximum CR proton acceleration efficiency at shocks must be lower than about 15 percent, or implies the presence of significant CR propagation out of the cluster core in order to lower the central emission. Our ULs also set a limit to the CR-to-thermal pressure in the Coma cluster, $X_{\text{CR}} = P_{\text{CR}}/P_{\text{th}}$ (volume-averaged within $R_{200}$; see, e.g. ZPP), to be less then approximately 1.3 and 0.6 per cent for the PP and ZPP-100 model, respectively, within $R_{200}$. Note that the limits on both the flux and CR pressure for the PP model are more stringent than those obtained in the previous work on the Coma cluster (Pinzke et al. 2011; Han et al. 2012; VERITAS Collaboration 2012; Fermi-LAT Collaboration 2013).

If CR streaming and diffusion are in action in the cluster, we would expect a much flatter emission profile which is represented by the ZPP-2 model. This model matches the 1.4 GHz Deiss et al. (1997) surface brightness profile of the Coma radio halo, assuming the magnetic field is distributed accordingly to FR measurements ($B_0 = 5 \, \mu G$, $\alpha_B = 0.5$; Bonafede et al. 2010). The predicted gamma-ray flux above 100 MeV within $R_{200}$ is $2.36 \times 10^{-9}$ cm$^{-2}$ s$^{-1}$. In this case, $X_{\text{CR}}$ within $R_{200}$ is much higher, about 17 percent, as streaming causes the CR pressure to rise in the cluster’s outskirts with respect to the IC pressure (see fig. 2 of ZPP). However, $X_{\text{CR}}$ reduces to 2.7 per cent within $R_{200}/2$. The corresponding flux UL shown in Table 1, $1.81 \times 10^{-9}$ cm$^{-2}$ s$^{-1}$, challenges the ZPP-2 model. However, a slightly different choice of parameters can still circumvent this limit while reproducing the 1.4 GHz radio data (ZPP), e.g. in case of $\gamma_0 = 3$ and $\alpha_B = 0.4$, the predicted gamma-ray flux above 100 MeV is about $1.3 \times 10^{-9}$ cm$^{-2}$ s$^{-1}$, whereas the UL hardly changes.

As explained above, an intriguing alternative is that of a hybrid scenario where the hadronic component would make up only the central part of the observed radio emission (ZPP). If this would be the case, the more centrally peaked PP and ZPP-100 models would still be a viable option, but requiring that they do not overshoot the radio emission both at 1.4 GHz and at 352 MHz. Assuming $B_0 = 5 \, \mu G$ and $\alpha_B = 0.5$ sets both the PP and ZPP-100 fluxes to be a factor of about 0.1 of the theoretical expectations presented at the beginning of this section, corresponding to a maximum CR proton acceleration efficiency of about 5 percent. These are a factor of 3 lower than the Fermi-LAT ULs presented here. However, there is a wide parameter space between a flat profile ($\gamma_0 \sim 1$) and a totally advection-dominated profile ($\gamma_0 \sim 100$), leaving room for a possible detection of pion-decay emission in clusters with Fermi-LAT or Cherenkov telescopes, in particular with the planned Cherenkov Telescope Array.\(^6\) Indeed, if such an hybrid scenario were realized in nature, the synergy of radio and gamma-ray observations would be very important in understanding the relevance of CR protons in clusters, and also in breaking the degeneracy with magnetic field estimates and radio modelling.

Another alternative is that the observed radio emission is not of hadronic origin at all, but it is generated by re-acceleration of a seed population of electrons. This seed population could be made of secondary electrons, from CR proton–proton interactions with the ICM, that are re-accelerated to emitting energies at a later stage (Brunetti et al. 2012). Also in this case, a corresponding pion-decay-induced emission is expected, but at a much lower level. Using the spectra shown in fig. 6 of Brunetti et al. (2012), we estimated that the integral gamma-ray flux for energies 100 MeV–100 GeV would be at a level of $2.6-1.4 \times 10^{-10}$ cm$^{-2}$ s$^{-1}$ in this scenario, almost one order of magnitude lower than our current ULs.

### 4.2 IC emission

In this section, we discuss the implications of our analysis for the IC-induced emission from accretion shocks, and connected to the radio relic of Coma.

#### 4.2.1 Accretion shocks

Kushnir & Waxman (2009) predicted a IC-induced flux above 100 MeV and within 1˚ from the centre of the Coma cluster of about $10^{-8}$ cm$^{-2}$ s$^{-1}$. Our UL obtained with the disc template is $2.9 \times 10^{-9}$ cm$^{-2}$ s$^{-1}$, about a factor of 3 below their prediction. This limits the CR electron acceleration efficiency at shocks to be $\xi_e < 1$ per cent. The same is true for the prediction of Keshet et al. (2003). The absence of any kind of ring-shaped emission around the Coma cluster, and the comparison of our integral flux ULs above 100 MeV of about $2.5 \times 10^{-9}$ cm$^{-2}$ s$^{-1}$ with the predicted flux of about $4 \times 10^{-9}$ cm$^{-2}$ s$^{-1}$ (see equation 11 of Keshet et al. 2012), implies that the CR electron efficiency at shocks is $\xi_e < 0.5$ per cent. This is consistent with Fermi not having detected any of these structures (Keshet et al. 2003).

#### 4.2.2 The radio relic

We model the emission of the radio relic of Coma using the data compiled by Thierbach et al. (2003). As explained above, the electrons generating the radio emission can also emit hard X-rays and gamma-rays via IC scattering off the CMB photons. We therefore compute their synchrotron and IC emission (Blumenthal & Gould 1970; Rybicki & Lightman 1979), as done in Murgia et al. (2010). We do not make any a priori assumption on the electron acceleration mechanism, but simply adopt a phenomenological approach. We assume a power-law electron distribution $n(E) \propto E^{-\alpha_e}$. The free parameters are the normalization of the electron distribution, spectral index $\alpha_e$, integration limits ($E_{\text{min}}, E_{\text{max}}$), and the volume-averaged magnetic field $B_V$ across the relic region. The electron spectral index is well determined by the slope of radio spectrum $\alpha_r = 1.18$ (Thierbach et al. 2003) and fixed at $\alpha_e = 2\alpha_r + 1 = 3.36$. The low- and high-energy cut-offs of the electron distribution are not constrained by current data; in fact, the existing radio measurements allow us only to establish $E_{\text{min}}/m_e c^2 \lesssim 2500$ and $E_{\text{max}}/m_e c^2 \gtrsim 2 \times 10^6$. The low-energy cut-off is typically determined by the Coulomb losses and we fix it at $E_{\text{min}}/m_e c^2 = 200$ (see e.g. Sarazin 1999). For the high-energy cut-off, we assume $E_{\text{max}}/m_e c^2 = 2 \times 10^6$, corresponding to electron energies of 100 GeV. By varying the normalization such that the IC emission do not exceed the high-energy ULs, we can estimate a lower limit for the magnetic field needed to generate the observed synchrotron radio emission. We found this to be constrained by the X-ray UL from XMM–Newton observations (Feretti & Neumann 2006) as $B_V \gtrsim 1 \, \mu G$. We show this in Fig. 4. These values are consistent with the estimate of $B_V \approx 2 \, \mu G$ obtained from FR measurements in the cluster outskirts by Bonafede et al. (2013). This is about a factor of 6 higher than what previously obtained by extrapolating equation (2) to the relic location (Bonafede et al. 2010) and implies magnetic amplification in the relic region (Bonafede et al. 2013). In Fig. 4, we also show the case where we fix the magnetic field to $B_V = 2 \, \mu G$.

\(^6\) http://www.cta-observatory.org/
Indeed, the NuSTAR out of reach of existing and future-planned gamma-ray instruments. With the electron population generating the Coma radio relic seems expected IC flux. Therefore, the high-energy emission associated 10 years of observation (Funk & Hinton 2013) is well above the expected IC flux. Therefore, the high-energy emission associated with the electron population generating the Coma radio relic seems out of reach of existing and future-planned gamma-ray instruments. In this case, a much more exciting picture is that of the current and next generations of X-ray satellites, such as NaSTAR (launched in 2012 June; Harrison et al. 2013) and Astro-H (to be launched in 2014; Takahashi et al. 2012). Indeed, the Astro-H Hard X-ray Imager (HXI) sensitivity curve (for a 100 ks exposure) shown in Fig. 4 demonstrates potential to finally break the radio–X-ray degeneracy in determining the magnetic field value. We warn, however, that the radio relic emission region is about 0.1 deg2, while the reported HXI sensitivity curve is for a PS and the HXI angular resolution is below 2 arcmin (Takahashi et al. 2012). Not surprisingly, the X-ray UL obtained with XMM–Newton (Feretti & Neumann 2006) is much more constraining than Fermi-LAT. In fact, the Fermi-LAT extragalactic (PS) sensitivity for 10 years of observation (Funk & Hinton 2013) is well above the expected IC flux. Therefore, the high-energy emission associated with the electron population generating the Coma radio relic seems out of reach of existing and future-planned gamma-ray instruments. In this case, a much more exciting picture is that of the current and next generations of X-ray satellites, such as NaSTAR (launched in 2012 June; Harrison et al. 2013) and Astro-H (to be launched in 2014; Takahashi et al. 2012). Indeed, the Astro-H Hard X-ray Imager (HXI) sensitivity curve (for a 100 ks exposure) shown in Fig. 4 demonstrates potential to finally break the radio–X-ray degeneracy in determining the magnetic field value. We warn, however, that the radio relic emission region is about 0.1 deg2, while the reported HXI sensitivity curve is for a PS and the HXI angular resolution is below 2 arcmin (Takahashi et al. 2012). Note that the pion-decay emission should be suppressed at the relic due to the lack of enough target ICM protons for hadronic interactions. Recently, Vazza & Brüggen (2014) tested the acceleration of protons by shock waves propagating through clusters against Fermi-LAT ULs, finding, similarly to this work, that the resulting central hadronic-induced emission lies very close to them. Their prediction for the hadronic-induced gamma-ray emission at the Coma relic, in the energy range of 200 MeV to 100 GeV, goes from 0.4 to $3 \times 10^{-12} \text{ cm}^{-2} \text{s}^{-1}$ depending on the adopted model (Vazza, private communication). This is very low, as expected from the low density of target protons at the relic location (Simionescu et al. 2013). Our UL on the relic template in this energy range is around $0.7 \times 10^{-10} \text{ cm}^{-2} \text{s}^{-1}$, about two orders of magnitude above expectations. Note also that this UL is significantly more stringent than the others we obtained because of the steeper spectrum.

We refrain from performing a similar synchrotron plus IC phenomenological modelling of the central giant radio halo of Coma as the corresponding volume average magnetic field, of about 2 µG (Bonafede et al. 2010), together with the extension of the radio emission area, of about 1 deg2, suggest that it would be extremely difficult to aim for a detection of the corresponding IC-induced emission, even with the next-generation X-ray satellites (see also Wik et al. 2011).

4.3 Diffuse extragalactic gamma-ray background

The constraints derived here not only affect particle acceleration modelling in clusters of galaxies, but also the possible contribution to the extragalactic gamma-ray background (e.g. Fermi-LAT Collaboration 2010b).

Loeb & Waxman (2000) estimated that the possible IC-induced emission at accretion shocks could be high enough to entirely explain the gamma-ray background. Keshet et al. (2003), by using N-body simulations, estimated this to be about 10 per cent for $\xi_s = 5$ per cent (see also Gabici & Blasi 2003). Our ULs imply that the possible IC-induced contribution must be lower than 1 per cent.

One can ask how much of the possible pion-decay-induced emission in galaxy clusters could contribute to the extragalactic gamma-ray background. Ando & Nagai (2008), with a simple analytical model, estimated this to be less than a few per cent (see also Colafrancesco & Blasi 1998). By making use of the mock galaxy clusters catalogues of Zandanel, Pfommer & Prada (2014a), which include the prediction for the pion-decay-induced emission in galaxy clusters following the ZPP prescription, we estimate this to be less than 1 per cent.

Summarizing, this means that acceleration of CR protons and electrons in galaxy clusters gives a negligible contribution to the diffuse extragalactic gamma-ray background. We note, however, that if the other possible contributions, such as from blazars and star-forming regions, are well understood, this could be a potentially interesting way to study relativistic particles in galaxy clusters.

5 CONCLUSIONS

Since generation of shocks and particle acceleration in the shocks are generic predictions of large-scale-structure formation scenarios, one expects gamma-ray emission from clusters of galaxies by secondaries from CR proton–proton interactions with the ICM, and by IC scattering of CR electrons off the CMB. In this paper, we analysed 63-month (P7REP) data from Fermi-LAT photons between 100 MeV and 100 GeV from the Coma cluster, one of the best studied nearby galaxy clusters. Coma also shows recent activity of

\[ B_{\text{IC}} = 1.05 \mu \text{G} \]

\[ B_{\text{IC}} = 2 \mu \text{G} \]

\[ \text{Astro-H 100 ks} \]

\[ \text{Fermi-LAT 10 yr} \]

\[ \text{XMM-Newton} \]

\[ \text{Coma Radio Relic +} \]

Figure 4. Spectral energy distribution of the radio relic of the Coma cluster. The radio data are taken from the Thierbach et al. (2003) compilation, while the XMM–Newton UL is from Feretti & Neumann (2006). We have shown the synchrotron and IC emission for $B_{\text{IC}} = 1.05$ and 2 µG. Also shown are the PS sensitivities expected for Astro-H HXI in 100 ks Takahashi et al. (2012) and for Fermi-LAT in 10 yr (Funk & Hinton 2013).

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7 The emission modelled in Fig. 4 corresponds to the radio relic region reported by Thierbach et al. (2003), which is about 800 × 400 kpc, corresponding to about 400 arcmin2. Note that the total relic extension reported by Brown & Rudnick (2011), on which we base our relic template for the analysis of Section 2, is significantly larger with a transverse extent of about 2 Mpc. However, due to the very steep spectrum of the radio relic, we do not expect this to change our conclusion for the gamma-ray detectability.

8 Note that Vazza & Brüggen (2014) assume that relics trace outward propagating shocks, and this is uncertain in the case of the Coma cluster as the relic may be tracing an infall shock (Brown & Rudnick 2011; Akamatsu et al. 2013; Ogrean & Brüggen 2013; Simionescu et al. 2013).
a merger and accretion, and has both a radio relic and giant radio halo. These observations make Coma a promising gamma-ray source, such that one is able to test CR energy content in the galaxy cluster and also particle acceleration mechanisms. We tested several template models of the gamma-ray emission from Coma and found no positive signature corresponding to any of these models. We, however, obtained the most stringent constraints to date on the Coma cluster above 100 MeV, as summarized below (see also Table 1).

(1) PS model. We obtained a PS flux UL, assuming a power-law energy spectrum with an index of $-2$, of $F_{UL} = 0.6 \times 10^{-6} \text{cm}^{-2} \text{s}^{-1}$, which is better by a factor of a few compared with previous studies (e.g. Ando & Nagai 2012). Note, however, that a softer spectrum would cause the UL to increase (as in Fermi-LAT Collaboration 2013).

(2) Pion decays. In this case, the spatial profile depends on the efficiency of CR turbulent motion compared with that of streaming. We chose several profiles and found that the flux limits are $F_{UL} \simeq (0.9\text{--}1.8) \times 10^{-9} \text{cm}^{-2} \text{s}^{-1}$, where the latter (former) value is for a more (less) extended model as a result of higher (lower) efficiency of streaming. These limits constrain the predictions of PP and ZPP, which implies either that maximum CR proton acceleration efficiencies at shocks are lower than about 15 per cent, or the presence of significant CR propagation out of the cluster core. We also note that by comparing the advection-dominated centrally peaked profiles to the observed radio emission, the maximum CR proton acceleration efficiency is limited to be below about 5 per cent. Note, however, that these conclusions rely on the assumption of magnetic field estimates from FR measurements (Bonafede et al. 2010) and on a fixed CR spectrum (PP).

(3) IC emission. Motivated by predictions for IC-induced emission from electrons accelerated at accretion shocks, we investigated both a disc and ring-like emission template. We found ULs of $F_{UL} = (1.7\text{--}2.9) \times 10^{-9} \text{cm}^{-2} \text{s}^{-1}$, which is not consistent with low-energy extrapolation of a recent claim of positive detection of such a ring-like feature in the VERITAS data (Keshet et al. 2012). Additionally, this limits the CR electron acceleration efficiency at shocks to be less than 1 per cent both in the Keshet et al. (2003) and in the Kushnir & Waxman (2009) scenarios.

(4) Radio relic. We adopted an emission profile consistent with the Coma radio relic, and looked for the corresponding gamma-ray emission. The radio emission from the relic is interpreted as a synchrotron radiation from non-thermal electrons, and there should be a corresponding high-frequency component due to IC scattering from the same electrons. The gamma-ray-flux UL is $F_{UL} = 0.9 \times 10^{-10} \text{cm}^{-2} \text{s}^{-1}$, but this is too weak to constrain the electron population. This is because the expected energy range of the IC scattering off CMB photons is in X-rays for an electron population matching the radio relic synchrotron emission. Instead, we find that the current (NuSTAR) and future (Astro-H) X-ray telescopes have excellent prospects for detecting this IC emission.

(5) Diffuse extragalactic gamma-ray background. We conclude by noting that, following Keshet et al. (2003) our results imply that the possible IC-induced emission associated with structure formation shocks in clusters of galaxies can contribute to the diffuse extragalactic gamma-ray background by less than 1 per cent. At the same time, using the Zandanel et al. (2014a) mock galaxy cluster catalogues, we estimate that also the possible pion-decay-induced emission can contribute only by less than 1 per cent. This renders the contribution to the diffuse extragalactic gamma-ray background due to the high-energy photons from structure-formation processes in clusters of galaxies negligible.

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