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A measurement of $B^0 - \bar{B}^0$ mixing in $Z^0$ decays

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We have observed $B^0 - \bar{B}^0$ mixing in $Z^0 - b\bar{b}$ decays using hadronic events containing dileptons. The data sample corresponds to 118 200 hadron events at $\sqrt{s} \approx 220$ GeV. From a fit to the dilepton $p$ and $p_{\perp}$ spectra, we determine the mixing parameter to be $\chi_{B^0} = 0.178 \pm 0.048$.

1. Introduction

Flavor-changing weak interactions are able to transform a neutral meson into its antiparticle, leading to the possibility of flavor oscillations or mixing. This phenomenon is known to occur in the $K^0$-$\bar{K}^0$ system.

In 1987 evidence was presented by UA1 for a similar effect in the $B^0$-$\bar{B}^0$ system at the CERN proton-antiproton collider [1]. The charge of the lepton produced in the direct semileptonic decay of the $b$ quark can be used to tag the charge of the quark ($b \to \ell^- + \bar{\nu}_\ell$ and $\bar{b} \to \ell^+ + \nu_\ell$). Thus, like-sign dileptons can arise from mixing. The large fraction of like-sign events in the UA1 dimuon event sample was interpreted as originating from $B^0 - \bar{B}^0$ oscillations.

The mixing parameter $\chi_{B^0}$ gives the probability that a hadron containing a $b$ quark oscillates into a hadron containing a $\bar{b}$ quark at the time of its decay. Assuming the semileptonic branching ratios for all $B$ hadrons are equal, it can be expressed as

$$\chi_{B^0} = f_0 x_0 + f_\bar{0} x_\bar{0},$$

(1)

where $f_0$ and $f_\bar{0}$ are the fractions of $B^0$ and $B^0$ produced, and $x_0$ and $x_\bar{0}$ are the mixing parameters for $B^0$ and $B^\circ$ mesons. This parameter,

$$x_{B^0} = \frac{Br(b \to B^0 \to B^0 \mu^+ + X)}{Br(b \to B^\circ \mu^\pm + X)},$$

(2)

was determined by UA1 to be $0.121 \pm 0.047$.

Additional evidence for $B^0 - \bar{B}^0$ transitions was pro-
vided by the ARGUS detector at the DORIS II storage ring [2] and by the CLEO Collaboration at CESR [3]. These observations were based on the study of B mesons produced in γ(4S) decays, where no Bs are produced. The weighted average of these measurements is \( \chi_0 = 0.16 \pm 0.04 \). Other measurements have been made at PEP which are consistent with the presence of \( B^0 - \bar{B}^0 \) oscillations [4].

In this letter we present the first measurement of \( B^0 - \bar{B}^0 \) mixing performed at \( \sqrt{s} \approx M_Z \). We perform a maximum likelihood fit to the \( p \) and \( p_\perp \) spectra of dileptons observed in hadronic decays of the \( Z^0 \) in order to determine the \( B^0 - \bar{B}^0 \) mixing parameter \( \chi_B \). The \( p \) and \( p_\perp \) spectra of leptons in hadronic decays of the \( Z^0 \) have already been used to measure the partial width of the \( Z^0 \) into \( b\bar{b} \) and to determine the \( b\bar{b} \) forward–backward asymmetry [5, 6]. In this analysis we use dimuons, dielectrons and muon–electron events to select \( b\bar{b} \) events in which both B mesons decay semileptonically. The data sample corresponds to \( 5.5 \text{ pb}^{-1} \) collected during a scan of the \( Z^0 \) resonance using the L3 detector at LEP. The center-of-mass energies are distributed over the range

\[ 88.2 < \sqrt{s} < 94.2 \text{ GeV} \]

2. The L3 detector

The L3 detector covers 99% of 4π. The detector consists of a central tracking chamber, a high resolution electromagnetic calorimeter composed of BGO crystals, a ring of scintillation counters, a uranium and brass hadron calorimeter with proportional wire chamber readout, and a precise muon chamber system. These detectors are installed in a 12 m diameter magnet which provides a uniform field of 0.5 T along the beam direction.

The central tracking chamber is a time expansion chamber which consists of 2 cylindrical layers of 12 and 24 sectors, with 62 wires measuring the \( R-\phi \) coordinate. The average single wire resolution is 58 \( \mu \text{m} \) over the entire cell. The double-track resolution is 640 \( \mu \text{m} \). The fine segmentation of the BGO detector and the hadron calorimeter allow us to measure the direction of jets with an angular resolution of 2.5°, and to measure the total energy of hadronic events from \( Z^0 \) decay with a resolution of 10.2%. The muon detector consists of 3 layers of precise drift chambers, which measure a muon’s trajectory 56 times in the bending plane, and 8 times in the non-bending direction.

For the present analysis, we use the data collected in the following ranges of polar angles:

- for the central chamber, \( 41° < \theta < 139° \),
- for the hadron calorimeter, \( 5° < \theta < 175° \),
- for the muon chambers, \( 35.8° < \theta < 144.2° \),
- for the electromagnetic calorimeter, \( 42.4° < \theta < 137.6° \).

A detailed description of each detector subsystem, and its performance, is given in ref. [7].

3. Selection of \( b\bar{b} \) events

Events of the type \( Z^0 \rightarrow b\bar{b} \) are identified by the observation of leptons coming from the semileptonic decay of the \( b \) or \( \bar{b} \) quark. In order to identify both \( B \) hadrons, we look for hadronic events containing at least two leptons (muons or electrons).

These events are triggered by several independent triggers. The primary trigger requires a total energy of 15 GeV in the BGO and hadron calorimeters. A second trigger for inclusive muon events requires one of sixteen scintillation counter \( \phi \) sectors in coincidence with a track in the muon chambers. These triggers, combined with an independent charged track trigger and a barrel scintillation counter trigger, give a trigger efficiency greater than 99.9% for hadronic events, including those containing one or more leptons.

In this analysis we first select hadronic events using the following criteria:

1) \( E_{\text{cal}} > 38 \text{ GeV} \),
2) longitudinal energy imbalance: \( |E_1|/E_{\text{vis}} < 0.4 \),
3) transverse energy imbalance: \( E_\perp/E_{\text{vis}} < 0.5 \),

where \( E_{\text{cal}} \) is the total energy observed in the calorimeters, and \( E_{\text{vis}} \) is the sum of the calorimetric energy and the energy of the muon as measured in the muon chambers.

The number of jets is found using a two-step algorithm which groups the energy deposited in the BGO crystals and in the hadron calorimeter towers into clusters, before collecting the clusters into jets [8]. We require that there be at least one jet which has more than 10 GeV in the calorimeters.

The clustering algorithm normally reconstructs one cluster in the BGO for each electron or photon.
shower, and a few clusters for $\tau$'s. We reject $\tau^+\tau^-$ events by requiring a minimum of 10 clusters in the BGO, each with energy greater than 100 MeV.

A total of 118 200 hadronic events were collected during the scan of the $Z^0$ in the 1989 and 1990 running periods. For the inclusive electron analysis only the data from 1990 is used, which corresponds to 104 400 hadronic events.

Muons are identified and measured in the muon chamber system. We require that a muon track consists of track segments in two of three layers of muon chambers, and that the muon track points to the interaction region. We make the additional requirement that the transverse distance of closest approach of the muon track is less than $3\sigma$ from the vertex, and that the longitudinal distance of closest approach is less than $4\sigma$. The effects of multiple scattering of the muon in the calorimeters are included in the errors. In order to be used in this analysis, the momentum of the muon must be larger than 4 GeV. Charge confusion is negligible for muon candidates in this sample (< 1%).

We identify electrons in a two-step process, first finding electromagnetic clusters in the BGO calorimeter and then associating them with a charged track. To identify an electromagnetic cluster in a hadronic environment, we look for an energy cluster in the BGO calorimeter which contains at least 9 adjacent crystals each with more than 10 MeV. We then compute the ratio of the energy measured in the $3 \times 3$ array centered on the most energetic crystal and the energy measured in the $5 \times 5$ array, $E_9/E_{25}$, where both energy measurements have a position-dependent leakage correction applied. For an isolated electromagnetic shower, $E_9/E_{25}$ has an approximately gaussian distribution, centered at 1.0 with a width of 1%. For hadronic showers, or for electromagnetic showers that have been contaminated by a nearby shower, $E_9/E_{25}$ will be smaller than 1.0. We reject those clusters with $E_9/E_{25}$ less than 0.95. To further reduce the background from pions and kaons misidentified as electrons, we exclude any BGO cluster when there is more than 3 GeV of energy deposited in the hadron calorimeter behind the cluster inside a cone of half-angle 7° around its centroid.

To identify the electromagnetic cluster as an electron, we require a match within 5 mrad in the azimuthal angle between the centroid of the electromagnetic shower and a track in the central tracking chamber. The charge of the electron is measured in the tracking chamber. Tracks going through lower resolution regions adjacent to the anode and cathode planes are excluded to avoid charge confusion. In addition, we reject those tracks with a measured momentum transverse to the beam direction larger than 35 GeV. Fig. 1 shows the ratio of the electromagnetic energy measured in the calorimeter and the signed momentum measured in the tracking chamber $(qE/p)$ for electron candidates passing the above cuts. Two well-separated peaks are visible at $\pm 1$. The upper limit of the charge confusion is 1%. The tails at large $E/p$ are due to energetic photons and $\pi^0$'s that have been matched to a nearby track. We reject this background by requiring $E/p < 1.5$. We further require that the energy of the electron candidate be greater than 3 GeV.

As an example, fig. 2 shows a hadronic event containing a high momentum electron and a high momentum muon. Both leptons come from the interaction region and have positive charge.

To simulate inclusive dilepton events, we use the Lund parton shower program JETSET 7.2 [9] with $M_{t\bar{t}} = 290$ MeV and string fragmentation. For $b$ and $c$ quarks we use the Peterson fragmentation function [10]. The $b$-quark fragmentation function is ad-
adjusted to match our inclusive muon data [5]. The generated events are passed through the L3 detector simulation #1 which includes the effects of energy loss, multiple scattering, interactions and decays in the detector materials. We use the average of the semi-leptonic branching ratios measured by previous experiments #2. \( \text{Br}(b\rightarrow \mu) = (11.8 \pm 1.1)\% \), and \( \text{Br}(c\rightarrow \mu) = (8.0 \pm 1.0)\% \). These branching ratios are also used for \( b\rightarrow e \) and \( c\rightarrow e \).

4. \( B^0 - \bar{B}^0 \) mixing sample

The signature for \( B^0 - \bar{B}^0 \) mixing in inclusive lepton events is an event with two leptons of the same charge on opposite sides of the event. The leptons are considered to be on opposite sides when the angle between them is greater than 60°. The major background comes from \( Z^0\rightarrow b\bar{b} \) events, where one \( b \) decays into a prompt lepton \( b\rightarrow \ell^- \), and the second decays via the cascade \( b\rightarrow c\rightarrow \ell^- \), giving like-sign leptons. Because of the hard fragmentation and large mass of the \( b \) quark, the leptons from its semileptonic decay have large momentum \( p \) and large transverse momentum \( p_\perp \). These features can be used to identify prompt leptons from \( B \)-hadron decays. Fig. 3 shows the minimum of the two momenta for the leptons in the inclusive dilepton events which have passed the selection cuts given above. Fig. 4 shows the measured minimum transverse momentum with respect to the nearest jet, \( p_\perp \), of each dilepton pair. In defining the axis of the nearest jet, the measured energy of the lepton is first excluded from the jet. The fraction of events with two leptons from prompt \( b\rightarrow \ell \) decay increases at higher \( p \) and \( p_\perp \). Therefore, events with opposite side, high momentum and high \( p_\perp \) leptons are most probably from prompt \( b\rightarrow \ell \) decays. The observation of such events with like-sign leptons is indicative of \( B^0 - \bar{B}^0 \) mixing.

A summary of the dilepton data sample is given in table 1. The smaller number of events with electrons is due to the necessity of using strong isolation re-

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#1 The L3 detector simulation is based on GEANT Version 3.13 (September 1989) [11]. Hadronic interactions are simulated using the GHEISHA program [12].

#2 The semileptonic branching ratios are taken from PEP and PETRA data, see ref. [13].
requirements to extract a clean electron sample in the presence of the hadronic background. The excess of $\mu^+\mu^+$ events compared to $\mu^-\mu^-$ events arises from the difference in the punch-through for positive and negative charged particles. Also shown are the number of events passing high $p_\perp$ cuts, which select preferentially $b\to\ell^-$, $b\to\ell^+$ events. In this selection, we require that electrons have $p_\perp > 1.0$ GeV and muons have $p_\perp > 1.5$ GeV and the two leptons are on opposite sides of the event.

To distinguish mixing events from background, lepton candidates can be classified into five categories:

1) Prompt $b\to\ell^-$. Included in the prompt $b\to\ell^-$ category are events with leptons from the cascades $b\to\tau^-\ell$, and $b\to c+\ell^+$ where $c\to\ell$. These cascades yield a lepton with the same sign as direct $b\to\ell^-$ decays.

2) Cascade $b\to c\to\ell$.

3) $b\to$-background coming from $B$-hadron decay.

4) Prompt $c\to\ell$.

5) Other backgrounds arising from $uds\to$ background and from fragmentation effects in $b\bar{b}$ events.

Background processes include: leptons from $\pi$ and $K$ decays, hadrons misidentified as electrons, punch-through, Dalitz decay and $\pi^\pm\gamma$ overlap for electrons. Leptons from $J$ decay contribute to 2% of the dilepton sample, but only 0.9% in the high $p_\perp$ sample, and
Table 2
Monte Carlo estimates of the fractions (in %) of various categories of dilepton events in the data sample. Since, in the presence of mixing, all charge combinations are possible, we omit the ± superscripts on the leptons.

<table>
<thead>
<tr>
<th>Lepton pair category</th>
<th>$p_\perp &gt; 0$</th>
<th>High-$p_\perp$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$b'\rightarrow \ell, b\rightarrow \ell$</td>
<td>36</td>
<td>80</td>
</tr>
<tr>
<td>$b'\rightarrow c, b'\rightarrow c, b\rightarrow \ell$</td>
<td>2</td>
<td>3</td>
</tr>
<tr>
<td>$b\rightarrow \ell, b\rightarrow c\rightarrow \ell$</td>
<td>32</td>
<td>10</td>
</tr>
<tr>
<td>$b\rightarrow \ell, b\rightarrow b\rightarrow \ell$</td>
<td>12</td>
<td>4</td>
</tr>
<tr>
<td>$c\rightarrow \ell, c\rightarrow \ell$</td>
<td>6</td>
<td>0</td>
</tr>
<tr>
<td>Others</td>
<td>12</td>
<td>3</td>
</tr>
</tbody>
</table>

have a negligible effect on our measurement.

Table 2 shows the results of Monte Carlo studies giving the fraction of each source of prompt dileptons and of background for data samples with no cut on $p_\perp$, and also with the high-$p_\perp$ requirement already described. These $p_\perp$ cuts correspond to prompt $b\rightarrow \ell$ probabilities for electrons and muons of about 80%. The high-$p_\perp$ sample can be used to estimate the $B^0-B^0$ mixing by simple event counting.

Using the data in table 1, we compute the ratio $N^{\pm\pm}/N^{++}$ for opposite-side, high-$p_\perp$ events to be $0.42 \pm 0.11$ while in the Monte Carlo (with $\chi_B=0$) we find $0.15 \pm 0.05$. Subtracting backgrounds estimated from Monte Carlo, and inserting our estimates of the fractions of various dilepton categories, we determine $\chi_B=0.13 \pm 0.05$ where the error is statistical only. Thus we observe clear evidence for $B^0-B^0$ mixing from simple event counting alone.

5. Determination of $\chi_B$

We perform an unbinned maximum likelihood fit to the $p$ and $p_\perp$ distributions for dilepton events in the data to determine the mixing parameter $\chi_B$. To define the probability that the data events contain two $b\rightarrow \ell$ decays, we use fully simulated Lund five-flavor Monte Carlo events, and also fully simulated and generator level $b$-flavor events, where one of the $b$ quarks is forced to decay semileptonically into $\mu$ or $e$. The generator level events are smeared to take into account detector effects.

The likelihood function is determined from the number and type of the Monte Carlo leptons found within a rectangular box centered on each data lepton in $(p_1, p_{1\perp}, p_2, p_{2\perp})$ space. We allow the size of the box to increase until a minimum number of 40 Monte Carlo leptons are included. The likelihood function $L$ has the form

$$ L = \prod_{i=1}^{N_{\text{data}}} \frac{1}{V_{\text{box}}(i)} \sum_{k_1,k_2} N_{k_1,k_2}(i) W_{k_1,k_2}(i) . $$

The index $k$ indicates the category of the lepton source type, $N_k(i)$ is the number of simulated Monte Carlo leptons of this type found in the box with data lepton $i$, and $V_{\text{box}}(i)$ is the volume of the box. Even with large Monte Carlo statistics, the four dimensional space is sparsely populated in the region of interest, where both leptons have high $p$ and high $p_\perp$. Hence, each box can become large. Therefore, the relative weight of each Monte Carlo event in the box is calculated assuming exponential distributions in $p$ and $p_\perp$. The Monte Carlo events are generated with no mixing, $\chi_B=0$, and must be reweighted assuming that a fraction $\chi_B$ of the leptons from $B$-hadrons will change sign. After taking mixing into account, only Monte Carlo events which could have the same product of lepton charges $(q_1q_2)$ as the data event, and have the same topology (same-side or opposite-side dileptons) contribute to the likelihood function.

For dileptons of category $k_1$ and $k_2$, the weighting function is written as

$$ W_{k_1,k_2}(i) = (1-\chi_{k_1})(1-\chi_{k_2}) + \chi_{k_1}\chi_{k_2} $$

when the Monte Carlo event and data event have the same product of lepton charges $(q_1q_2)$ as the data event, and have the same topology (same-side or opposite-side dileptons) contribute to the likelihood function.

The amount of mixing, $\chi_B$, for each category is given by

$$ \chi_1 = \chi_B, \quad \text{for } b\rightarrow \ell, $$

$$ \chi_2 = \chi_B, \quad \text{for } b\rightarrow c\rightarrow \ell, $$

$$ \chi_3 = 0.5\chi_B, \quad \text{for } b\rightarrow B\text{-hadron}\rightarrow\text{background} $$

710
\( \chi_s = 0, \) for \( c \to \ell \),

\( \chi_s = 0, \) for other backgrounds.

From Monte Carlo studies we observe that the effective \( \chi \) is less than \( \chi_B \) for category 3, (backgrounds arising from B-hadron decays), even though at production the lepton candidates from this source do change sign with mixing. This is largely because many more of the \( K^- \) than \( K^+ \) are absorbed in the calorimeters.

When the Monte Carlo and the data have different charge products, we calculate the probability that mixing will cause the sign of one lepton to change. When the leptons are in opposite hemispheres, and \( (q_1q_2)^{MC} \neq (q_1q_2)^{Data} \), the weight is

\[
W_{k_1,k_2}(i) = \chi_{k_1}(1-\chi_{k_2}) + (1-\chi_{k_1})\chi_{k_2}.
\]

(5)

When the two data leptons are on the same side and both Monte Carlo leptons originate from the same b hadron, there is no sensitivity to \( \chi \), thus

\[
W_{k_1,k_2}(i) = 0.
\]

(6)

From the fit, we determine the mixing parameter,

\[
\chi_B = 0.178^{+0.049}_{-0.040},
\]

where the error is statistical only. The change in the logarithm of the likelihood function between this value and \( \chi_B = 0 \) is 32.3, or 8.0 standard deviations.

Table 3 lists the contributions to the systematic error in this measurement. We have estimated the error by changing several parameters by one standard deviation or more of their known (or estimated) uncertainties. We have estimated the contribution from reconstruction errors by an additional smearing of the \( p_\perp \) of each data lepton. The error coming from the uncertainty in assigning probabilities to events has been estimated by changing the number of leptons required in the fit box (in the range 20 to 90), as well as using different samples of Monte Carlo events. The combined systematic error on \( \chi_B \) is estimated to be 0.02.

<table>
<thead>
<tr>
<th>Contribution</th>
<th>Error</th>
</tr>
</thead>
<tbody>
<tr>
<td>changing the b ( \to \ell ) and c ( \to \ell ) branching ratios by their associated errors</td>
<td>0.0015</td>
</tr>
<tr>
<td>variation of the background fraction by ( \pm 15% )</td>
<td>0.0005</td>
</tr>
<tr>
<td>variation of the b fragmentation parameter ( \epsilon_b ) by ( \pm 50% )</td>
<td>0.0005</td>
</tr>
<tr>
<td>changing the definition of opposite side from 45\° to 90\°</td>
<td>0.003</td>
</tr>
<tr>
<td>smearing of the lepton transverse momentum by ( \Delta p_\perp / p_\perp = 25% )</td>
<td>0.005</td>
</tr>
<tr>
<td>introduction of an additional charge confusion of 0.5%</td>
<td>0.01</td>
</tr>
<tr>
<td>variation of the background mixing dependence, ( 0.25 &lt; \chi_s / \chi_B &lt; 1.0 )</td>
<td>(&lt;0.0005 )</td>
</tr>
<tr>
<td>variation of the exponential weighting of the ( p ) and ( p_\perp ) distributions within a box</td>
<td>0.007</td>
</tr>
<tr>
<td>probability assignment</td>
<td>0.01</td>
</tr>
</tbody>
</table>

Table 3: Systematic checks in the \( \chi_B \) measurement.

The combined systematic uncertainty, but does verify that the higher backgrounds at low \( p_\perp \) are not influencing the result.

As an additional check, a different method is used to measure the mixing parameter using the dileptons. In this method, probability functions are assumed to factorize, and are therefore evaluated independently (using the single lepton data and Monte Carlo) for each lepton as a function of \( p_L \) and \( p_\perp \), where \( p_L \) is the lepton momentum along the jet axis. This method requires much smaller Monte Carlo statistics, but does not take into account correlations between the lepton momenta. We find \( \chi_B = 0.14 \pm 0.04 \) where the error is statistical only, in good agreement with the other analysis.

6. Discussion

We can use our measurement of \( \chi_B \), along with the combined ARGUS and CLEO value for \( \chi_d \), to obtain information on \( \chi_s \). Since \( \chi_s \) has been measured to be large, \( 0.16 \pm 0.04 \), in the standard model the \( B_s^0 - B_s^0 \) mixing is expected to be maximal, i.e. \( \chi_s \approx 0.5 \). Assuming that the relative abundances of \( B_d \) and \( B_s \) mesons at LEP energies are given by \( f_d = 0.375 \) and \( f_s = 0.15 \) [14]; we show in fig. 5 a plot in the \( \chi_s - \chi_s \) plane corresponding to our measurement. Also shown in the figure is the ARGUS/CLEO value for \( \chi_d \).
Combining our result with that of ARGUS/CLEO and taking into account possible variations in the $f_d$ and $f_\epsilon$ parameters of up to 0.05, we obtain a value of $\chi_5 = 0.79^{+0.47}_{-0.20}$. Because $\chi_5$ must lie in the range $0 \leq \chi_5 \leq 0.5$, the classical statistical technique for computing a lower limit on $\chi_5$ cannot be used. We compute a 90% lower limit of $\chi_5 > 0.14$ with respect to the integral of the probability distribution between 0.0 and 0.5 [15].

7. Conclusions

We have measured mixing in the $B^0 - \bar{B}^0$ system using inclusive dilepton events from approximately 118,000 $Z^0$ decays. The uncertainty in $\chi_B$ is dominated by the statistics. We determine the $B^0 - \bar{B}^0$ mixing parameter to be $\chi_B = 0.178^{+0.049}_{-0.040}$, which is 8 standard deviations from zero. Our result is consistent with maximal mixing in the $B^0 - \bar{B}^0$ system as expected in the standard model.

References