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Mobility of Adsorbed Species in Zeolites: Methane, Ethane, and Propane Diffusivities

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Molecular dynamics simulations were performed in order to study the influence of the zeolite structure on molecular migration in the zeolite void space. The migration of methane in various zeolite environments was examined by using the all-silica polymorphs of zeolite EU-1, mordenite, and silicalite. Furthermore, diffusion simulations of ethane and propane in silicalite were carried out and computed diffusion characteristics were compared with experimental data.

Introduction

Computer simulations of adsorption and diffusion in zeolites have gained much interest over the last few years. This increasing interest is due to the notion that simulations may offer new insights into adsorption and diffusion phenomena that are of direct importance in studies on the catalytic activity and selectivity of zeolites.

Limitations arising from insufficient computer power hindered the application of computer simulations in the past. However, thanks to the advances made in the development of computer hardware and methodologies of computational chemistry, computer simulations now offer a valuable contribution to zeolite catalysis research.

Several adsorption and diffusion simulations in zeolites have been carried out recently. The first simulations, based on simple potential energy minimizations, identified preferred adsorption sites or potential energy maps of the zeolite inner void space. Later, Monte Carlo (MC) simulations were employed to study the average siting of methane in zeolite Y3 and in the zeolites ZSM-5 and mordenite;6 Leherete et al.7 studied concentration effects on water adsorption in ferrierite.

More recently, molecular dynamics (MD) simulations have been applied to determine time-dependent properties such as diffusion coefficients and intracrystalline site residence times for methane in the zeolites Y,8 mordenite,9 A,10 and ZSM-5,311 for benzene.

Summary

We have investigated the susceptibility toward nucleophilic attack, e.g. hydrolysis, of a group of cyclic ureas. We examined the surface electrostatic potentials of these molecules, focusing upon the regions above the acyl carbons, to determine the effects of various chemical and structural modifications, including the presence of NO2 and/or NF2 substituents. The relative hydrolytic stabilities of these systems have been predicted. For the poly-carbonyl molecules parabanic acid and alloxan, the magnitudes and locations of the maxima in their surface potentials are fully consistent with observed unusually short intermolecular distances in their crystalline forms.

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References:


in zeolite Y, for water in ferrierite, and for xenon in silicalite. In all studies mentioned, the computed dynamical results were in good agreement with experimental data. Furthermore, the adsorbrates were assumed to be rigid, which as a matter of fact seems a reasonable approximation considering the small size (methylene, water) and nature (benzene) of the adsorbrates.

In this paper, we will present the results of a systematic study on the influence of zeolite structure on the diffusivity of methane by considering the zeolites silicalite, mordenite, and EU-1. This particular choice allows us to compare migration of adsorbrates through microchannels with different dimensions and tortuositities. Furthermore, computational data on the diffusivities of methane, ethane, and propane in silicalite are presented and compared with experimental pulse field gradient NMR (PFG-NMR) data.

Zeolite Structures

Silicalite has a three-dimensional channel system with sinusoidal channels consisting of 10-membered rings running along the a direction and straight channels consisting of 10-membered rings running along the b direction. The silicalite channels are connected with each other to form intersections. Mordenite and zeolite EU-1 are both characterized by a one-dimensional channel system with side pockets, which can be entered from the main channels. However, whereas mordenite has main channels consisting of 12-membered rings running along the c direction and side pockets with entrances consisting of eight-membered rings along the b direction, zeolite EU-1 has main channels consisting of 12-membered rings running along the c direction and side pockets with entrances formed by 12-membered rings along the c direction. This particular choice of zeolite networks covers a range of possible structures, allowing us to study the influence of topology on the diffusion process.

Calculations Performed

For the simplest adsorbate considered in this paper, viz. methane, diffusion was simulated in the all-silica polymorphs of mordenite, zeolite EU-1, and silicalite. As a follow-up on this, the methane studies, ethane and propane diffusivities were examined in silicalite only. Experimental data on methane, ethane, and propane diffusivities in silicalite are available, so these studies enable us to verify the computational results.

In order to eliminate concentration effects when studying structural features, we scaled the loadings of the various zeolites according to the zeolite framework densities. As a reference, silicalite was given a loading, $\theta$, of two adsorbate molecules per Si24O48 unit. The density of silicalite is 17.9 T/1000 Å³, so for mordenite, having a density of 17.2 T/1000 Å³, $\theta = (17.2/17.9) \times 2 = 1.9$ adsorbate molecules/Si24O48, and for EU-1 (density = 17.2 T/1000 Å³), $\theta = 2$ adsorbate molecules/Si24O48.

In all cases, the simulations were carried out in a zeolite unit consisting of 192 T sites (1 × 1 × 2 unit cells). Thus the total number of adsorbates considered in the ensemble is 16 for silicalite and EU-1 and 15 for mordenite. Boundary effects were taken into account by applying periodic boundary conditions. All simulations were performed by using the constraint dynamics method as described by Allen and Tildesley. The zeolite

| TABLE I: Potential Parameters for the van der Waals Interatomic Interactions |
|-----------------------------|-----------------------------|-----------------------------|
| Atom pair                  | $A$, kJ/mol Å²               | $B$, kJ/mol Å¹²              |
| C···C                      | 1742.99                     | 1897.055.5                  |
| C···H                      | 562.73                      | 2748.755.3                  |
| H···H                      | 191.38                      | 5370.25                     |
| C···O                      | 1970.07                     | 1138.724.0                  |
| H··O                       | 536.74                      | 14987.95                    |

| TABLE II: Diffusivities for Methane in the Zeolites Mordenite, EU-1, and Silicalite (D in 10⁻⁶ m²/s) Together with Effective Pore Diameters (in Å) for the Separate Directions |
|-----------------------------|-----------------------------|-----------------------------|
| Zeolite                     | $D_x$ diameter | $D_y$ diameter | $D_z$ diameter | $D$  |
| Mordenite                   | 0.01            | 0.07           | 4.5            | 7.0  | 0.28 |
| EU-1                        | 0.83            | 5.5            | 0.31           | 7.0  | 0.38 |
| Silicalite                  | 0.44            | 5.5            | 1.33           | 5.5  | 0.11 | 0.62 |

$t = 298$ K. $\theta = 1.9$CH₄/Si₂₄O₄₈. $\theta = 2$CH₄/Si₂₄O₄₈.

lattice as well as the adsorbate molecules was assumed to be rigid. All internal atom–atom distances of the adsorbrates were constrained with a tolerance of 10⁻⁴ Å.

Every time step, the adsorbate velocities were scaled in order to establish isothermal conditions for the adsorbate ensemble. The simulation temperature was 298 K, while the time step was 10⁻³ ps for methane and 10⁻⁴ ps for ethane and propane. The system was equilibrated over a time period typically in the order of 5 ps in order to suppress any undesirable simulation start-up effects. Sampling took place over 50, 5, and 3 ps for methane, ethane, and propane, respectively. The short simulation times for ethane and propane were imposed by the availability of computer time.

Potentials

The interatomic potentials between atoms of the zeolite lattice and atoms of the adsorbates and between atoms of different adsorbates are described by a van der Waals (6–12) Lennard-Jones potential:

$$\phi_{ij} = B/r^{12} - A/r^6$$

where $r$ is the interatomic distance and $A$ and $B$ are potential parameters.

Because we are studying nonpolar hydrocarbon molecules in all-silica zeolite polymorphs, Coulombic interactions are not taken into account. In the zeolite, the atomic radius of the silicon atoms is much smaller than the radius of the oxygen atoms. It is thus assumed that silicon atoms are effectively screened by oxygen and their contribution to the potential energy of the adsorbrates is not taken into account. Furthermore, their polarizability is negligible compared to that of the zeolite oxygen atoms, which further justifies this assumption. Potential parameters $A$ and $B$ for the various interatomic interactions between adsorbates and all the zeolites considered were determined following Kiselev et al. and are given in Table 1.

We do not include intramolecular or intramolecular interactions since all simulations are performed on rigid frameworks and adsorbates. This assumption was made for two reasons: firstly, because framework flexibility is not expected to affect the diffusion of relatively small adsorbate molecules to a great extent and, secondly, to save computing time so that longer simulation times can be achieved.

Results and Discussion

*Methane in Silicalite, Mordenite, and EU-1.* Figures 1, 2, and 3 display the mean-square displacements versus time for methane molecules migrating in the zeolites mordenite, EU-1, and silicalite, respectively. The subfigures a, b, and c represent diffusion in the x, y, and z directions, respectively, while the subfigures d represent the overall mean-square displacements versus time. The x, y, and
Figure 1. Mean-square displacement versus time for methane molecules migrating in mordenite in the $x$ (a), $y$ (b), and $z$ (c) direction. (d) The overall displacement. $\theta = 1.9 \text{CH}_4/\text{Si}_2\text{O}_{48}$; $T = 298 \text{K}$.

Figure 2. Mean-square displacement versus time for methane molecules migrating in zeolite EU-1 in the $x$ (a), $y$ (b), and $z$ (c) direction. (d) The overall displacement. $\theta = 2 \text{CH}_4/\text{Si}_2\text{O}_{48}$; $T = 298 \text{K}$.

$z$ directions correspond with the crystallographic $a$, $b$, and $c$ axes. The straight lines drawn in the figures are obtained via a linear regression fit to the calculated data.

Although mordenite and EU-1 (Figures 1 and 2, respectively) have a similar framework topology, the diffusion behavior of methane in these systems differs considerably. All diffusion coefficients for the separate directions together with the effective pore diameters are listed in Table II. For mordenite, effectively only diffusion in the $z$ direction is observed. From this table, we see that diffusion along the $z$ direction in mordenite is 1 to 2 orders of magnitude greater than diffusion for the $x$ and $y$ directions. For zeolite EU-1, this is not the case. An expected diffusion along the $x$ direction is observed, but diffusion along the $z$ direction occurs as well. This is a contribution from diffusion into the side pockets, which should average to zero over a long simulation time.

Obviously, in zeolite EU-1, migration from one side pocket to another occurs. In mordenite, this kind of migration is not observed. A possible explanation for this difference might be the difference between the diameters of the microchannels through which migration takes place. The side pockets of EU-1 are composed of 12-membered rings, while the side pockets in mordenite are composed of eight-membered rings. The side pockets in mordenite have an entrance diameter that is approximately of the same order of magnitude as the molecular diameter of methane ($\approx 4.3 \text{Å}$). Thus, whereas methane can easily enter and leave the side pockets in EU-1, the situation in mordenite is somewhat different. It can be envisaged that methane is trapped in the mordenite side pockets (which has already been observed in earlier
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Figure 3. Mean-square displacement versus time for methane molecules migrating in silicalite in the x (a), y (b), and z (c) direction. (d) The overall displacement. \( \theta = 2\text{CH}_4/\text{Si}_2\text{O}_4\); \( T = 298 \text{ K} \).

Figure 4. Migration of methane molecules at \( T = 298 \text{ K} \) in (A) mordenite (\( \theta = 1.9\text{CH}_4/\text{Si}_2\text{O}_4 \), z direction is vertically displayed, y direction horizontally), (B) zeolite EU-1 (\( \theta = 2\text{CH}_4/\text{Si}_2\text{O}_4 \), x direction is vertically displayed, z direction horizontally), and (c) silicalite (\( \theta = 2\text{CH}_4/\text{Si}_2\text{O}_4 \), z direction is vertically displayed, y direction horizontally). The dots represent the centers of mass of the methane molecules at subsequent time intervals. The density of the dots is a measure of the residence time.

Studies\(^5\) and that the frequency of leaving and entering the side pockets is much lower in mordenite than in EU-1. This feature is demonstrated in Figure 4, parts A and B. These figures display the centers of mass at subsequent time intervals for all the methane molecules considered over a time period of 50 ps. The density of the dots at the various locations inside the zeolite framework can be regarded as a measure of the residence time at that location. In the mordenite framework (Figure 4A), the density of dots in the entrances to the side pockets is low compared to that at other locations in the zeolite. This indicates that the jump frequency between main channel and side pocket is very low. However, in the EU-1 framework (Figure 4B) the methane molecules seem to be free to move in and out of the side pockets.

Side pockets seem to have a considerable impact on molecular mass transport. If we consider the diffusion along the main channels of Eu-1 and mordenite, we do not observe a significant difference in diffusivity, although the pore diameter is much larger in mordenite than in EU-1. It can be envisaged that there are two factors that determine the diffusivity rate, and, in this case, the combination of these factors is averaged out.

The first factor that influences the migration rate is the pore diameter. An increase in pore diameter yields an increased migration rate. The second factor to be considered is the ability of the side pockets to trap adsorbates. The migration rate for methane in the main channel is greater in the mordenite structure than in EU-1 because the latter zeolite has a smaller pore diameter. However, as we have seen before, the mordenite side pockets are quite effective in trapping methane adsorbates, thus reducing migration in the main channel considerably. In the EU-1 structure, the adsorbates are less effectively trapped (cf. also Figure 4A,B) and thus migration rates are less reduced.

Another interesting feature emerges if we compare the diffu-
sivity of methane in silicalite along the straight channel with the diffusivities of methane in the main channels of EU-1 and mordenite. The diffusion rate in silicalite along the main channel is approximately twice as fast as in EU-1 and mordenite. This reflects not only the presence of side pockets but also the openness of the silicalite structure for diffusion. In the silicalite void space, migration along the straight channels might be interrupted temporarily if an adsorbate enters one of the sinusoidal channels perpendicular to the straight channels. However, at a following intersection, the adsorbate has the possibility of proceeding again along the original direction but in another straight channel. Thus, in silicalite migration in any direction is never blocked. However, in the case of adsorbates trapped by side pockets, only migration in one direction (out of the side pocket, perpendicular to the main channel) is possible and thus diffusion is strongly reduced.

By comparing the diffusivities of methane in silicalite along the x and y directions, we observe that the diffusivity along the sinusoidal channel is a factor of 3 lower than that along the straight channel. It should be noted, however, that diffusion in the x direction cannot proceed via a straight trajectory because of the tortuosity of the channels.

For silicalite it is observed that diffusion in the z direction readily occurs. Apparently, the adsorbate molecules are able to shift between the different channel systems since this is the only way in which migration along the z direction can occur. Figure 4C clearly shows the interconnection of the separate directions in the silicalite framework. Although silicalite has the smallest framework density, its openness for diffusion of methane is the highest of all zeolites considered.

Finally, we interpret our computational results in relation to experimental diffusivity measurements, in particular, PFG-NMR. The overall diffusion coefficients in Table II were obtained by taking the averages over the separate directions. By interpreting these figures, one should consider the time intervals between subsequent pulses in an PFG-NMR experiment and the timescale in which the MD simulations take place. For example, in EU-1, a diffusion coefficient of $0.31 \times 10^{-8}$ m$^2$/s in the z direction is calculated. However, this diffusion coefficient does not reflect the diffusivity that would be observed by PFG-NMR since no molecular mass transport along the z direction is possible. On the timescale of NMR, migration along the z direction would be averaged out. Since the timescale of MD is several orders of magnitude smaller, migration along the z direction is observed.

**Figure 5.** Mean-square displacement versus time for ethane molecules migrating in silicalite in the x (a), y (b), and z (c) direction. (d) The overall displacement. $\theta = 2C_2H_6/Si_{24}O_{48}$; $T = 298$ K.

**TABLE III: Diffusivities for Methane, Ethane, and Propane in Silicalite (D in 10^{-8} m^2/s)**

<table>
<thead>
<tr>
<th>adsorbate</th>
<th>$D_x$</th>
<th>$D_y$</th>
<th>$D_z$</th>
<th>D</th>
</tr>
</thead>
<tbody>
<tr>
<td>methane</td>
<td>0.44</td>
<td>1.33</td>
<td>0.11</td>
<td>0.62</td>
</tr>
<tr>
<td>ethane</td>
<td>0.30</td>
<td>0.88</td>
<td>0.24</td>
<td>0.47</td>
</tr>
<tr>
<td>propane</td>
<td>0.30</td>
<td>0.90</td>
<td>0.03</td>
<td>0.41</td>
</tr>
</tbody>
</table>

$^*T = 298$ K, $\theta = 2$ adsorbates/Si$_2$O$_4$.

Thus, the experimental diffusion coefficients for methane in mordenite and EU-1 are estimated to be $0.77 \times 10^{-8}$ and $0.83 \times 10^{-8}$ m$^2$/s, respectively. For silicalite, on the other hand, migration in all directions is possible, so the overall diffusion coefficient of $0.62 \times 10^{-8}$ m$^2$/s for methane as quoted in Table II reflects the diffusion coefficient that would be measured by a PFG-NMR experiment. We predict, therefore, that measured diffusion coefficients for methane in the three zeolites should be very similar.

**Methane, Ethane, and Propane in Silicalite.** In this section we present results of MD simulations on the diffusivities of methane, ethane, and propane in silicalite. The computational results will be compared with experimental data obtained by PFG-NMR techniques.17

Figures 5a–c display the mean-square displacement of the ethane molecules in silicalite versus time. Figure 5d displays the overall mean-square displacement versus time. Figures 6a–d display the same data for propane in silicalite. The straight lines drawn in the figures are obtained via a linear regression fit to the calculated data.

Computed diffusion coefficients for the separate directions and the overall diffusion coefficient are listed in Table III. For comparison, the computational results for methane in silicalite are also presented in this table.

Computed overall diffusion coefficients are compared with experimental data in Figure 7. This figure represents the diffusion coefficient as a function of carbon number of the alkanes for a loading $\theta = 2$ adsorbate molecules/Si$_2$O$_4$ at $T = 298$ K. We see that for methane and ethane the agreement with experimental data is good. However, in the case of propane, a large deviation shows up. This may originate from the approximation of propane being rigid.

Examination of the diffusion coefficients for the separate directions in Table III and Figures 6a–d shows that diffusion in the
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**Figure 6.** Mean-square displacement versus time for propane molecules migrating in silicalite in the x (a), y (b), and z (c) direction. (d) The overall displacement. $\theta = 2\text{C}_3\text{H}_8/\text{Si}_2\text{O}_4\text{Si}; \ T = 298 \text{ K}$.

**Figure 7.** Diffusion coefficient in silicalite as a function of carbon number. $\theta = 2$ adsorbate molecules/$\text{Si}_2\text{O}_4\text{Si}; \ T = 298 \text{ K}$.

straight and sinusoidal channels readily occurs, but diffusion in the z direction is virtually negligible. This indicates that during the simulation the propane molecules were not able to shift from one channel system to another due to their rigidity. This computational artefact enhances the diffusivity considerably. Furthermore, it is highly unlikely that propane molecules migrate in the micropores like bouncing balls. For the smaller adsorbates (methane and ethane), this can be envisaged, but propane is expected to migrate along the zeolite walls in a creeping motion.\(^{(21)}\)

**Figure 8.** Adsorption enthalpy in silicalite as a function of carbon number. $\theta = 2$ adsorbate molecules/$\text{Si}_2\text{O}_4\text{Si}; \ T = 298 \text{ K}$.

resulting in a considerable decrease of the diffusion coefficient. However, the rigid constraint on the propane molecule does not


allow a creeping motion.

Finally, Figure 8 displays computed and experimental adsorption enthalpies as a function of the alkane carbon number. For all three adsorbates considered, a good agreement between experiment and computation is found. This agreement indicates that the potentials used are fairly accurate. Therefore, we ascribe the mismatch of the proton diffusion coefficient in silicalite to the approximations made with respect to the rigidity of the adsorbate molecule.

Conclusions

In this paper we have shown that MD simulations can give detailed information on a molecular level of mass transport phenomena in porous solids. By considering a set of different

Oxidation of \([\text{Au}^+(\text{CN})_2]^\text{-}\). Formation of Dicyanogold(III) Oxide and Colloidal Monocyanogold(III) Oxide

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\([\text{Au}^+(\text{CN})_2]^\text{-}\) is oxidized by \('\text{OH}' radicals. The primary oxidation product is \([\text{(OH)}\text{Au}^{\text{III}}(\text{CN})_2]^\text{-}\) which is in equilibrium with its protonated form: \([\text{(OH)}\text{Au}^{\text{III}}(\text{CN})_2]^\text{+} + \text{H}^+ = [\text{(OH)}\text{Au}^{\text{III}}(\text{CN})_2]^\text{+}\text{H}^+\). The protonated and the deprotonated oxidation products undergo disproportionation to give the \(\text{Au}^{\text{III}}\) species which is also in equilibrium with a protonated form: \([\text{O-H}]\text{Au}^{\text{III}}(\text{CN})_2]^\text{+} + \text{H}^+ = [\text{(OH)}\text{Au}^{\text{III}}(\text{CN})_2]^\text{+}\text{H}^+\). In alkaline solution, the deprotonated \(\text{Au}^{\text{III}}\) species loses a water molecule to give the stable negatively charged dicyanogold(III) oxide \([\text{O}=\text{Au}^{\text{III}}(\text{CN})_2]^\text{-}\). In acidic media, splitting of \(\text{HCN}\) is taking place to give \(\text{O}=\text{Au}^{\text{III}}(\text{CN})\) which agglomerates rapidly into stable colloidal \(\text{Au}^{\text{III}}\). The absorption spectra of the various intermediates and of colloidal \(\text{Au}^{\text{III}}\) are reported.

Introduction

The effort of designing a photosystem capable of cyclic cleavage of water into \(\text{H}_2\) and \(\text{O}_2\) prompted the development of new types of catalysts capable of storage of electrons.\(^{1}\) It has been demonstrated by Henglein and co-workers and by other authors that extremely small colloidal metals and colloidal semiconductors can be generated in aqueous solution containing metal ions and additives when exposed to \(\gamma\)-radiolysis. For example, colloids of \(\text{Ag}^{2-8}\), \(\text{Au}^{9,10}\), \(\text{Mn}_2^{11-13}\), \(\text{IrO}_2^{14}\) and \(\text{RuO}_2^{15}\) were prepared successfully in situ in \(\gamma\)-irradiated solutions.

Gold may exist in solution in two different stable ionic forms which possess the +1 (aurous) and the +3 (auric) oxidation states. (The former is unstable except when complexed.) It has been however demonstrated (first by Faraday and later on by other workers\(^{9,10,16-29}\)) that gold may also exist in solution in a colloidal \(\text{Au}^0\) form. Its color varies between the red and the blue depending on the particle's size and shape.

More than 20 years ago, Ghosh-Mazumdar and Hart\(^{21}\) performed a pulse radiolysis study on the oxidation and the reduction of \([\text{Au}^+(\text{CN})_2]^\text{-}\) in aqueous solution which may be regarded today as a preliminary one. The authors obtained mainly the absorption spectra of the first intermediate resulting from the action of hydrated electrons and hydroxy radicals on \([\text{Au}^+(\text{CN})_2]^\text{-}\). The absorption spectra were ascribed to zerovalent and divalent gold. No attempt was done in that work to determine precisely these