Measurement of the top quark charge in pp collisions at $\sqrt{s} = 7$ TeV with the ATLAS detector


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Measurement of the top quark charge in \( pp \) collisions at \( \sqrt{s} = 7 \) TeV with the ATLAS detector

The ATLAS collaboration

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**Abstract:** A measurement of the top quark electric charge is carried out in the ATLAS experiment at the Large Hadron Collider using 2.05 fb\(^{-1}\) of data at a centre-of-mass energy of 7 TeV. In units of the elementary electric charge, the top quark charge is determined to be 0.64 ± 0.02 (stat.) ± 0.08 (syst.) from the charges of the top quark decay products in single lepton \( t\bar{t} \) candidate events. This excludes models that propose a heavy quark of electric charge \(-4/3\), instead of the Standard Model top quark, with a significance of more than 8\(\sigma\).

**Keywords:** Hadron-Hadron Scattering, Top physics

**ArXiv ePrint:** 1307.4568
It is generally accepted that the particle discovered at Fermilab in 1995 [1, 2] is the Standard Model (SM) top quark. However, a few years after the discovery a theoretical model appeared proposing an “exotic” quark of charge −4/3 and mass ≈ 170 GeV as an alternative to the SM top quark at this mass value [3]. Though this model has already been experimentally excluded a precise measurement of the top quark charge is important as it is one of the basic top quark properties. A strong preference for the SM top quark with electric charge of +2/3 (in units of the electron charge magnitude) was reported by the D0 and CDF collaborations [4, 5] but without the ultimate 5σ exclusion of a possible exotic quark with charge of −4/3. The CDF and D0 exclusion limits are 95%1 and 92%,

1The CDF collaboration has recently submitted an update of their analysis for publication, which results in a limit of 99% [6].
respectively. Therefore, it is still important to carry out a more precise measurement to definitively resolve this question with more than 5σ confidence level. Due to the excellent ATLAS detector performance, the analysis presented here not only demonstrates that the particle presently denoted by “top quark” is really the SM top quark decaying into a b-quark and a W⁺ boson, but also allows for a direct measurement of its electric charge with a significantly improved precision. Moreover, from an experimental point of view it is interesting to demonstrate the high flavour tagging performance of the ATLAS experiment, i.e. its capability to distinguish between jets initiated by quarks and anti-quarks used in this study to find the correct Wb pairing in the W⁺W⁻b̄b system of the assumed tt̄ final state.

The dominant decay channel of the top quark is to a b-quark through the charged weak current: \( t \rightarrow W^+b \) (\( \bar{t} \rightarrow W^-\bar{b} \)). The measurement of the top quark charge requires the charges of both the W boson and the b-quark to be determined. While the former can be determined through W’s leptonic decay, the b-quark charge is not directly measurable due to quark confinement in hadrons. However, it is possible to establish a correlation between the charge of the b-quark and the charges of the collimated hadrons from the b-quark hadronization that form a b-jet. Within this approach, the charge can be determined using the lepton + jets (\( tt \rightarrow \ell^\pm \nu jjb\bar{b} \)) or the dilepton (\( tt \rightarrow \ell^+\ell^-\nu\nu b\bar{b} \)) channel. This paper presents the results of a top quark charge analysis based on the charges of the hadrons associated with the jet originating from a b-quark (b-jet) using the statistically more significant lepton + jets channel.

2 The ATLAS detector

The ATLAS detector is a multi-purpose particle physics apparatus operating at the beam interaction point IP1 of the Large Hadron Collider (LHC). A complete description is provided in ref. [7]. ATLAS uses a right-handed coordinate system with its origin at the centre of the detector (the nominal interaction point) and the z-axis along the beam pipe. The x-axis points to the centre of the LHC ring, and the y-axis points upward.

The innermost part is an inner tracking detector (ID) comprising a silicon pixel detector, a silicon microstrip detector, and a transition radiation tracker. The inner detector covers the pseudorapidity\(^2\) range \(| \eta | < 2.5\) and is surrounded by a thin superconducting solenoid providing a 2 T axial magnetic field, and by liquid-argon (LAr) electromagnetic sampling calorimeters with high granularity. An iron/scintillator tile calorimeter provides hadronic energy measurements in the central pseudorapidity range (\(| \eta | < 1.7\)). The endcap and forward regions are instrumented with LAr sampling calorimeters for electromagnetic (EM) and hadronic energy measurements up to \(| \eta | = 4.9\). The calorimeter system is surrounded by a muon spectrometer incorporating three superconducting toroid magnet assemblies, providing a toroidal magnetic field with bending power between 2.0 Tm and 7.5 Tm, and a pseudorapidity coverage of \(| \eta | < 2.7\).

\(^2\)The pseudorapidity is defined in terms of the polar angle with respect to the beam axis, θ, as \( \eta = -\ln(\tan(\theta/2)) \).
3 Data and simulation samples

This analysis uses the proton-proton collision data collected by the ATLAS experiment from March to August 2011 at a centre-of-mass energy of $\sqrt{s} = 7$ TeV corresponding to an integrated luminosity of $2.05 \pm 0.04$ fb$^{-1}$ [8]. The data for the top quark charge study were collected using a single-muon and a single-electron trigger (see details in section 4). In this analysis we also use the dijet data sample collected using the combined muon-jet trigger which requires a reconstructed muon matched to a 10 GeV jet in the calorimeter.

Simulated event samples are used to estimate both the signal selection efficiency and some of the background contributions and also to calibrate the $b$-jet charge measurement. The response of the ATLAS detector is simulated using GEANT4 [9] and the resulting events are reconstructed by the same software [10] used for data.

The MC@NLO Monte Carlo (MC) generator v3.41, based on the next-to-leading-order (NLO) matrix elements [11, 12] with CTEQ6.6 [13] parton distribution functions (PDFs), is used for the parton-level hard scattering in $t\bar{t}$ production, and is interfaced to the HERWIG (v6.5) generator [14, 15] for simulation of the hadronization and fragmentation processes and to JIMMY [16] for simulation of the underlying event from multiple parton interactions. The POWHEG generator [17] in combination with the PYTHIA [18] or HERWIG generators is used for studying parton-shower systematic uncertainties. For the study of other systematic uncertainties (top quark mass dependence, initial and final state radiation (ISR/FSR)), $t\bar{t}$ samples produced with the Acermc generator [19] interfaced with PYTHIA are used. The expected $t\bar{t}$ event yield is normalized to the cross-section of 164.6 pb, obtained with approximate next-to-next-to-leading-order (NNLO) QCD calculations [20]. Electroweak single-top-quark production is simulated using the MC@NLO generator and the event samples are normalized to approximate NNLO cross sections: 65 pb ($t$-channel) [21], 4.6 pb ($s$-channel) [22] and 15.7 pb ($Wt$ channel) [23].

The background from $W$ + jets and $Z$ + jets production is simulated with the ALPGEN v2.13 generator [24] and CTEQ6L1 [25] PDFs in exclusive bins of parton multiplicity for multiplicities of less than five, and inclusively for five or more. The events are processed by HERWIG and JIMMY. The overall $W$+ jets and $Z$+ jets samples are normalized to the NNLO inclusive cross sections [26]. Diboson samples are produced using HERWIG and JIMMY with MRST2007LO [27] PDFs. Dijet samples used for crosscheck purposes (see section 8) are generated using the PYTHIA generator with the ATLAS AMBT2B PYTHIA tune [28] and with MRST2007LO PDFs.

4 Event selection

The reconstructed events are selected using criteria designed to identify the lepton + jets final states, i.e. $t\bar{t}$ events in which one of the $W$ bosons decays leptonically and the other hadronically. This sample also contains a significant fraction of $t\bar{t}$ events where both $W$ bosons decay leptonically, but one of the leptons is not reconstructed in the detector or fails the lepton identification requirements. In the simulated sample the events generated in both the single-lepton and dilepton channels are treated as signal if they satisfy the lepton + jets reconstruction criteria.
4.1 Object reconstruction

An electron candidate is defined as an energy cluster deposition in the EM calorimeter associated with a well-reconstructed charged particle track in the ID [29]. The candidate must have a shower shape consistent with expectations based on simulation, test-beam studies and $Z \to ee$ events in data. The associated ID track must satisfy quality criteria including the presence of high-threshold hits in the transition radiation tracker. All candidates are required to have transverse energy ($E_{T}$) above 25 GeV and $|\eta| < 2.47$, where $\eta$ is the pseudorapidity of the EM calorimeter cluster associated with the electron. Candidates in the transition region between the barrel and end-cap calorimeters (1.37 < $|\eta|$ < 1.52) are excluded.

Muon candidates are reconstructed by combining track segments from different layers of the muon chambers [30]. Such segments are assembled starting from the outermost layer, with a procedure that takes material effects into account, and are then matched with tracks found in the ID. The candidates are re-fitted exploiting the full track information from both the muon spectrometer and the ID. They are required to have transverse momenta ($p_{T}$) above 20 GeV and the candidate muon must be within $|\eta| < 2.5$.

Jet candidates are reconstructed using the anti-$k_{t}$ algorithm [31] with jet radius parameter $R = 0.4$. These jets are calibrated to the hadronic energy scale, using a $p_{T}$- and $|\eta|$-dependent correction factor obtained from simulation, test-beam and collision data [32].

The missing transverse momentum, $E_{T}^{\text{miss}}$, is calculated as the magnitude of the vector sum of the energy deposits in calorimeter cells associated with topological clusters [33], with the direction defined by the interaction vertex and position of the energy deposition in the calorimeter [34]. The calorimeter cells are associated with a parent physics object in a chosen order: electrons, jets and muons, such that a cell is uniquely associated with a single physics object. Cells belonging to electrons are calibrated at the EM energy scale whereas cells belonging to jets are corrected to the hadronic energy scale. Finally, the transverse momenta of muons passing the event selection are included, and the contributions from the calorimeter cells associated with the muons are subtracted. The remaining clusters not associated with electrons or jets are included at the EM energy scale.

Overlap between the different object categories is avoided by the following procedure. Jets within $\Delta R = 0.2$ of an electron passing the electron selection requirements are removed from the list of jet candidates. Muons within $\Delta R = 0.4$ of any jet with $p_{T} > 20$ GeV are rejected. In addition, if a selected electron is separated by less than $\Delta R = 0.4$ from any jet with $p_{T} > 20$ GeV, the event is rejected (for event selection see section 4.2).

Tracks used for the $b$-jet charge calculation (see section 5) are required to contain at least six hits in the silicon microstrip detector and at least one pixel hit. Only tracks with $p_{T} > 1$ GeV and $|\eta| < 2.5$ are considered. In addition, proximity to the $pp$ collision primary vertex$^{4}$ expressed in terms of impact parameter in the transverse plane, $d_{0}$, and

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$^{3}$ $\Delta R$ is defined as a distance, $\Delta R = \sqrt{(\Delta \eta)^{2} + (\Delta \phi)^{2}}$, in $\eta$-$\phi$ space, where $\eta$ is the pseudorapidity and $\phi$ is the azimuthal angle around the beam pipe.

$^{4}$ The primary vertex is chosen as the reconstructed vertex with the highest $\sum p_{T}^{2}$ of associated tracks. At least five tracks with $p_{T} > 0.4$ GeV are required.
along the beam direction, $z_0$, and good track fit quality are also required. The applied selection requirements on $d_0$ and $z_0$ are $|d_0| < 2$ mm and $|z_0 \cdot \sin(\theta)| < 10$ mm, and that on the quality of the track fit is $\chi^2/ndf < 2.5$.

For all reconstructed objects in the simulation, corrections are applied to compensate for the difference in reconstruction efficiencies and resolutions between data and simulation.

### 4.2 Selection of $t\bar{t}$ candidates

The $t\bar{t}$ candidates in the electron + jets or muon + jets final states are first selected with a single-electron or single-muon trigger with transverse energy or momentum thresholds at 20 GeV or 18 GeV, respectively. Events passing the trigger selection are required to contain exactly one reconstructed lepton, with $E_T > 25$ GeV for an electron or $p_T > 20$ GeV for a muon. At least four jets with transverse momenta $p_T > 25$ GeV and within the pseudorapidity range $|\eta| < 2.5$ are required. The missing transverse momentum, $E_T^{\text{miss}}$, has to exceed 35 GeV for the events with electrons, and 20 GeV for the events with muons. In addition, a primary vertex containing at least five charged particles with $p_T > 0.4$ GeV is required, and events containing jets with $p_T > 20$ GeV in poorly instrumented detector regions are removed.

The transverse mass of the leptonically decaying $W$ boson in the event is reconstructed as $m_T(W) = \sqrt{2p_T^l p_T^{\nu}(1 - \cos(\phi^l - \phi^\nu))}$, where the measured $E_T^{\text{miss}}$ magnitude and direction provide the transverse momentum, $p_T^l$, and azimuthal angle, $\phi^\nu$, of the neutrino, and the superscript $l$ stands for the $e$ or $\mu$. For events with electrons $m_T(W)$ has to exceed 25 GeV, while the sum of $m_T(W)$ and $E_T^{\text{miss}}$ has to exceed 60 GeV for the events with muons.

Finally, at least one jet is required to be $b$-tagged using the $b$-tagging procedure described in ref. [35]. The procedure combines an algorithm based on jet track impact parameters with respect to the primary vertex with an algorithm exploiting the topology of $b$- and c-hadron weak decays inside the jet. The combination of the two algorithms is based on artificial neural network techniques with MC-simulated training samples and variables describing the topology of the decay chain used as the neural network input [36]. The chosen $b$-tagging operating point corresponds to a 70% tagging efficiency for $b$-jets in simulated $t\bar{t}$ events, while light-flavour jets are suppressed by approximately a factor of 100.

These selection requirements, common to most of the ATLAS $t\bar{t}$ analyses (see e.g. [37]), are further referred to as the basic $t\bar{t}$ requirements. They are followed by requirements specific for reconstruction of the $b$-quark charge. In order to use the track charge weighting method (see section 5.1), the presence of a second $b$-tagged jet is required. Each of the two $b$-tagged jets has to contain at least two well-reconstructed tracks with transverse momenta above 1 GeV within the pseudorapidity range $|\eta| < 2.5$. A pairing criterion between the lepton and a $b$-jet is also applied (see section 5).

### 5 Top quark charge determination

The correlation between the top or exotic quark charge and the charges of their decay products can be used for the quark charge determination. In the SM the top quark is
expected to decay according to

$$t^{(2/3)} \rightarrow b^{(-1/3)} + W^{(+1)},$$

(5.1)

while the exotic quark \((t_X)\) with charge \(-4/3\) is assumed to decay according to

$$t_X^{(-4/3)} \rightarrow b^{(-1/3)} + W^{(-1)},$$

(5.2)

where the electric charges of the particles are indicated in parentheses. Considering the subsequent leptonic decay of the \(W\) bosons, \(W^{\pm} \rightarrow \ell^{\pm} + \nu_{\ell}(\bar{\nu}_{\ell})\), the expectation for the SM case is that a positively charged lepton \(\ell^+\) is associated with the \(b\)-quark \((Q_b = -1/3)\) from the same top quark, while for the exotic case it is just the opposite: \(\ell^-\) is paired with the \(b\)-quark. In the SM case the product of charges of the top or anti-top quark decay products \((Q_{\ell^+} \times Q_b\) or \(Q_{\ell^-} \times Q_{\bar{b}}\)) always has a negative sign while in the exotic case the sign is positive.

The charge of the \(W\) boson is taken from the charge of the high-\(p_T\) lepton in the event. The charge of the quark initiating the \(b\)-jet is estimated from a weighted average of the charges of the tracks in the jet (see section 5.1). A lepton–\(b\)-jet pairing criterion (hereafter referred to as \(\ell b\)-pairing) is then applied to match the \(W\) boson to the \(b\)-jet from the same top quark (see section 5.2).

### 5.1 Weighting procedure for \(b\)-jet charge calculation

For the determination of the effective \(b\)-jet charge a weighting technique \([38, 39]\) is applied in which the \(b\)-jet charge is defined as a weighted sum of the \(b\)-jet track charges,

$$Q_{b\text{-jet}} = \frac{\sum_i Q_i |\vec{j} \cdot \vec{p}_i|^\kappa}{\sum_i |\vec{j} \cdot \vec{p}_i|^\kappa},$$

(5.3)

where \(Q_i\) and \(\vec{p}_i\) are the charge and momentum of the \(i\)-th track, \(\vec{j}\) defines the \(b\)-jet axis direction, and \(\kappa\) is a parameter which was set to be 0.5 for the best separation between \(b\)- and \(\bar{b}\)-jets mean charges using the standard MC@NLO \(t\bar{t}\) simulated sample.

The calculation of the \(b\)-jet charge uses a maximum number of ten tracks with \(p_T > 1\) GeV associated with the \(b\)-jet within a cone of \(\Delta R < 0.25\). The \(b\)-jet tracks used in the calculation of the effective \(b\)-jet charge include not only the charged decay products of the \(b\)-hadron, but also \(b\)-fragmentation tracks, and can possibly also contain tracks from multiple interactions or pile-up. The mean number of charged tracks within the \(b\)-jet cone is six for \(t\bar{t}\) \(b\)-jets. If there are more than ten associated tracks, the highest-\(p_T\) tracks are chosen. The maximum number of tracks, the minimum track \(p_T\) and the value of \(\Delta R\) were optimized using the standard MC@NLO \(t\bar{t}\) simulated sample. The optimization takes into account that the pile-up effect can be stronger for the high track multiplicity events and that low-\(p_T\) tracks, coming mainly from gluons, could dilute the jet charge.

The variable that is used to distinguish between the SM and exotic model scenarios is the combined lepton–\(b\)-jet charge (hereafter referred to as the combined charge) which is defined as

$$Q_{\text{comb}} = Q_{b\text{-jet}}^{\ell} \cdot Q_{\ell},$$

(5.4)
where $Q_{\ell b-jet}$ is the charge of the $b$-jet calculated with equation (5.3)\(^5\) and $Q_\ell$ the charge of the lepton, the two being associated via the $\ell b$-pairing described below.

5.2 Lepton and $b$-jet pairing algorithm

The $\ell b$-pairing is based on the invariant mass distribution of the lepton and the $b$-jet, $m(\ell, b\text{-jet})$. If the assignment is correct, assuming an ideal invariant mass resolution, $m(\ell, b\text{-jet})$ should not exceed the top quark mass provided that the decaying particle is the SM top quark. Otherwise, if the lepton and $b$-jet are not from the same decaying particle, there is no such restriction. This is shown in figure 1, where the invariant mass distribution of a lepton and a $b$-jet in the signal MC sample is plotted for the correct pairing and the wrong pairing, for events fulfilling the basic $t\bar{t}$ selection requirements. For MC events the reconstructed $b$-jet is paired with a parton-level $b$-quark if their separation $\Delta R < 0.2$; similarly, $\Delta R < 0.2$ is required for the matching between parton-level and reconstructed leptons.

The $\ell b$-pairing requires events with two $b$-tags and only the events with $b$-jets that satisfy the conditions:

$$m(\ell, b\text{-jet}_1) < m_{\text{cut}} \quad \text{and} \quad m(\ell, b\text{-jet}_2) > m_{\text{cut}}$$

or

$$m(\ell, b\text{-jet}_2) < m_{\text{cut}} \quad \text{and} \quad m(\ell, b\text{-jet}_1) > m_{\text{cut}}$$

are accepted. Here $b\text{-jet}_1$ and $b\text{-jet}_2$ denote the two $b$-tagged jets ordered in descending order of transverse momentum. The optimal value for the $\ell b$-pairing mass cut, $m_{\text{cut}}$, is

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\(^5\)The superscript $\ell$ is added to $Q_{b\text{-jet}}$ to stress that the $b$-jet is paired with a lepton.
a trade-off between the efficiency ($\epsilon$) and purity ($P$) (see section 6.1) of the $l\bar{b}$-pairing method. It was found by maximizing the quantity $\epsilon(2P-1)^2$ which is largest and nearly constant in the region 140 GeV to 165 GeV. The value for the $l\bar{b}$-pairing mass cut is chosen to be $m_{\text{cut}} = 155$ GeV. A similar interval for the optimal value of $m_{\text{cut}}$ was obtained using the relative uncertainty of the mean combined charge as an alternative figure of merit in the optimization.

The efficiency of the $l\bar{b}$-pairing procedure, defined as the ratio of the number of $l\bar{b}$-pairs after and before the invariant mass cuts in equation 5.5, is small ($\epsilon=28\%$), but it gives a high purity ($P=87\%$). The efficiency of the full set of selections used in the analysis, with respect to the basic $t\bar{t}$ requirements, is reduced not only by the $l\bar{b}$-pairing conditions but also by the requirement of the second $b$-tag (70% efficiency) and, to a lesser extent, by the $b$-jet track requirements (see section 4.1) with efficiency around 99%.

6 Signal and background expectations

The sensitivity for determining the SM top quark charge in the lepton+jets channel is investigated using MC and data control samples with the aim of finding the $Q_{\text{comb}}$ expectations for the SM signal and background. Both single-lepton ($t\bar{t} \to \ell\nu jj\bar{b}\bar{b}$) and dilepton ($t\bar{t} \to \ell\nu(\ell'\nu'\bar{b}\bar{b})$) samples are included for the signal.

6.1 Reconstructed signal distribution

In the MC analysis of the top quark charge the MC@NLO, POWHEG and Acermc $t\bar{t}$ samples are used. MC@NLO is taken as the default generator. The $b$-jet charge spectra reconstructed for the $t\bar{t}$ electron+jets events from MC@NLO are presented in figure 2. The distributions of $Q_{b-\text{jet}}$ for $b$-jets paired with positive and negative leptons are shown after the $l\bar{b}$-pairing. In addition, the $Q_{\text{comb}}$ spectrum (see equation (5.4)) is also shown in the plot.

The peaks at $\pm 1$ in figure 2 correspond to the cases where all the tracks within the $b$-jet cone of $\Delta R = 0.25$ have charges of the same sign. In these cases the weighting procedure (equation (5.3)) gives $Q_{b-\text{jet}} = \pm 1$.

The difference between the mean $b$-jet charges associated with $\ell^+$ and $\ell^-$ is clearly seen in figure 2. The results of the MC $b$-jet charge analysis are summarized in table 1, where the mean combined charges and charge purities are shown for different MC generators and the individual lepton+jets channels. The uncertainties in the mean combined charges of all MC samples are downgraded to the integrated luminosity of 2.05 fb$^{-1}$ corresponding to the size of the processed data sample. The charge purity, $P_Q$, is defined as

$$P_Q = \frac{N(Q_{\text{comb}} < 0)}{N(Q_{\text{comb}} < 0) + N(Q_{\text{comb}} \geq 0)},$$  \hspace{1cm} (6.1)$$

where $N(Q_{\text{comb}} < 0)$ and $N(Q_{\text{comb}} \geq 0)$ denote the number of events with $Q_{\text{comb}} < 0$ and $Q_{\text{comb}} \geq 0$, respectively. It is an important parameter which defines the quality of the $b$-jet charge weighting procedure. The higher $P_Q$ is relative to 50%, the better the
flavour tagging identification is, i.e. the ability to distinguish between jets initiated by $b$- and $\bar{b}$-quarks. As shown in table 1, our procedure produces $P_Q$ near 60%.

In general, as it follows from table 1, there is good agreement among the MC@NLO, POWHEG and ACERMC results on $Q_{comb}$. The combined (electron + muon channels) expectations agree to within 4%. Good agreement is also seen between the individual channels.

To evaluate the effect of the reconstruction on the combined charge, the mean associated $b$-jet charge reconstructed using the $\ell b$-pairing is compared with that based on the correct association of the lepton and $b$-jet using a MC generator-level matching. The comparison is carried out using the MC@NLO $t\bar{t}$ samples and the results are shown in table 2 for the electron + jets, muon + jets and combined electron + muon channels. The larger value of the average $Q_{comb}$ for the MC matching can be explained by its 100% pairing purity. Table 2 shows that the expected mean combined charges obtained for the electron and muon channels are compatible within statistical errors for the MC matching. In the $\ell b$-pairing case a difference of 2.4σ between the electron and the muon channel is seen. The difference can be explained by the non-identical selection criteria used for these two channels and by the slight dependence of the $\ell b$-pairing efficiency and purity on lepton and $b$-jet transverse momentum. To illustrate that the analyzed sample of data does not have sufficient statistical power to be sensitive to such a difference, the statistical uncertainty quoted in table 1 has been scaled to the luminosity of the analyzed data sample (2.05 fb$^{-1}$).

6.2 Background
The main background processes for the top quark charge measurement in the lepton + jets channel are: $W+$ jets production (the most significant background), $Z+$ jets, multi-jet, diboson and single-top-quark production. The single-top-quark background gives the same
Table 1. The expected mean combined charges ($\langle Q_{\text{comb}} \rangle$) and charge purities ($P_Q$) for the electron ($e$), muon ($\mu$) and combined ($e+\mu$) channels compared for the $t\bar{t}$ MC@NLO, Powheg+Herwig, Powheg+Pythia and Acermc+Pythia simulated signal at 7 TeV in the lepton + jets channel obtained with the $\ell b$-pairing. The $\langle Q_{\text{comb}} \rangle$ values are shown with their statistical uncertainties scaled to the integrated luminosity of 2.05 fb$^{-1}$ (see text). The uncertainty of $P_Q$ is obtained from the full MC sample and is not downgraded to the integrated luminosity of the data as $P_Q$ reflects the quality of the charge weighting procedure.

<table>
<thead>
<tr>
<th>Generator</th>
<th>Channel</th>
<th>$\langle Q_{\text{comb}} \rangle$</th>
<th>$P_Q$</th>
</tr>
</thead>
<tbody>
<tr>
<td>MC@NLO</td>
<td>$e$</td>
<td>-0.0802 ± 0.0065</td>
<td>0.610 ± 0.003</td>
</tr>
<tr>
<td></td>
<td>$\mu$</td>
<td>-0.0776 ± 0.0058</td>
<td>0.603 ± 0.003</td>
</tr>
<tr>
<td></td>
<td>$e+\mu$</td>
<td>-0.0787 ± 0.0043</td>
<td>0.606 ± 0.002</td>
</tr>
<tr>
<td>Powheg+Herwig</td>
<td>$e$</td>
<td>-0.0739 ± 0.0070</td>
<td>0.595 ± 0.010</td>
</tr>
<tr>
<td></td>
<td>$\mu$</td>
<td>-0.0787 ± 0.0063</td>
<td>0.600 ± 0.008</td>
</tr>
<tr>
<td></td>
<td>$e+\mu$</td>
<td>-0.0766 ± 0.0047</td>
<td>0.602 ± 0.006</td>
</tr>
<tr>
<td>Powheg+Pythia</td>
<td>$e$</td>
<td>-0.0824 ± 0.0068</td>
<td>0.613 ± 0.010</td>
</tr>
<tr>
<td></td>
<td>$\mu$</td>
<td>-0.0703 ± 0.0063</td>
<td>0.594 ± 0.008</td>
</tr>
<tr>
<td></td>
<td>$e+\mu$</td>
<td>-0.0756 ± 0.0046</td>
<td>0.602 ± 0.006</td>
</tr>
<tr>
<td>Acermc+Pythia</td>
<td>$e$</td>
<td>-0.0728 ± 0.0065</td>
<td>0.598 ± 0.011</td>
</tr>
<tr>
<td></td>
<td>$\mu$</td>
<td>-0.0786 ± 0.0058</td>
<td>0.609 ± 0.008</td>
</tr>
<tr>
<td></td>
<td>$e+\mu$</td>
<td>-0.0760 ± 0.0043</td>
<td>0.604 ± 0.007</td>
</tr>
</tbody>
</table>

Table 2. Comparison of the mean combined charge, $\langle Q_{\text{comb}} \rangle$, for the electron ($e$), muon ($\mu$) and combined ($e+\mu$) channels obtained using the MC matching and $\ell b$-pairing. The charges are shown with their statistical uncertainties for the full $t\bar{t}$ MC@NLO sample.

<table>
<thead>
<tr>
<th>Pairing type</th>
<th>$e$</th>
<th>$\mu$</th>
<th>$e+\mu$</th>
</tr>
</thead>
<tbody>
<tr>
<td>MC matching</td>
<td>-0.1014 ± 0.0009</td>
<td>-0.1006 ± 0.0008</td>
<td>-0.1010 ± 0.0006</td>
</tr>
<tr>
<td>$\ell b$-pairing</td>
<td>-0.0802 ± 0.0008</td>
<td>-0.0776 ± 0.0007</td>
<td>-0.0787 ± 0.0005</td>
</tr>
</tbody>
</table>

The sign of the mean $b$-jet charge as the signal. The MC simulation is expected to predict correctly all the processes with the exception of the multi-jet production and the normalization of the $W+$ jets production. Though the probability for a multi-jet event to pass the event selection is very low, the production cross section is several orders of magnitude larger than that of top quark pair production, and due to fake leptons the multi-jet events can contribute to the background. This background is determined in a data-driven way employing the so-called Matrix Method [37]. This technique is based on the determination of the number of data events passing the full set of analysis selection criteria (tight selection) and that for a looser selection obtained by dropping the isolation requirement on the lepton. Using the number of events passing the tight and loose selections and the efficiencies for true and fake leptons, the number of fake-lepton events passing the tight $t\bar{t}$ selection criteria is found. The efficiencies are determined using appropriate control samples as is explained in detail in ref. [37].

---

6Fake lepton refers to both a non-prompt lepton and a jet misidentified as a lepton.
Table 3. Signal and background expectation after applying the $\ell b$-pairing separately for the electron and muon channels for 2.05 fb$^{-1}$ integrated luminosity. Here, DD stands for “data driven”, $N_{\ell b}$ is the mean number of lepton–$b$-jet pairs and $\langle Q_{\text{comb}} \rangle$ is the reconstructed mean combined charge. The non-top-quark background is the total background not including single-top-quark events. The uncertainties include the statistical uncertainties and the uncertainties in the cross sections and integrated luminosity.

The estimation of the $W$+ jets background relies to a large extent on MC simulation, which is assumed to correctly describe the kinematics of the individual $W$+ jets channels, but the overall normalization and flavour fractions are determined from data. The $W$+ jets background is divided into four flavour groups: $W+\bar{b}b+$jets, $W+c\bar{c}+$jets, $W+c+$jets and $W+$light-flavour-jets. The flavour composition of the jets is determined from data based on the fraction of $W+$ jet(s) events that have one or two tagged jets [40]. The MC predictions for the $W+\bar{b}b+$jets and $W+c\bar{c}+$jets components are scaled by a factor of 1.63 ± 0.76, the $W+c+$jets component by a factor of 1.11 ± 0.35, and the light-flavour $W+$jets component by a factor of 0.83 ± 0.18 (for details see ref. [41]).

The expected results for the electron and muon channels after all selections used in the analysis, including those used for the $\ell b$-pairing, are shown in table 3. The uncertainties in the expected number of the signal and background events include not only the statistical uncertainties but also the cross-section uncertainties, which vary from 10% for signal and single-top-quark production to 100% for the multi-jet background, and the uncertainty in the integrated luminosity (1.8%).

7 Results

The distributions of the reconstructed quantities involved in the top quark charge determination, namely the distributions of $b$-jet and lepton $p_T$, $E_T^{\text{miss}}$ and the number of tracks with $p_T > 1$ GeV in a $b$-jet, were compared to the expectations after applying the basic $t\bar{t}$ selection requirements and after the full set of the analysis requirements including two $b$-tags and $\ell b$-jet pairing. Fairly good agreement between data and MC distributions is observed. An example is seen in figure 3, which shows the $b$-jet $p_T$ distribution after the basic $t\bar{t}$ requirements and after the full set of the analysis requirements.

To test the $b$-jet charge weighting procedure (see eq. (5.1)), the reconstructed distributions of the mean value of the absolute $b$-jet charge, shown as a function of $b$-jet $p_T$ for the
Figure 3. Data and MC comparison of the $b$-jet $p_T$ distribution after the basic $t\bar{t}$ requirements (upper plots) and after the full set of requirements (bottom plots) for electron + jets (left) and muon + jets (right) events. The MC expectations for signal and background are normalized to $2.05 \text{ fb}^{-1}$ using the expected cross sections. The shaded area belongs to the MC distribution and corresponds to a combination of the statistical uncertainties and the uncertainties in the cross sections and the integrated luminosity.

$t\bar{t}$ candidate events in data and MC simulation, are compared in figure 4 after the basic $t\bar{t}$ requirements and after the $b\bar{b}$-pairing. The expected background is subtracted from the data distribution. The distributions in figure 4 are profile histograms containing in each bin the mean value with its uncertainty depicted as the corresponding error bar. Due to the high statistics of the MC samples, the error bars of the MC distributions are within the symbol size. Good agreement between the data and the MC simulation is observed. An advantage of using the absolute value of $b$-jet charge is that it can be used for comparison of data and MC in different stages of the candidate event selection while the combined charge is available only after the full set of selection criteria. The relation between the mean combined charge and the mean value of absolute $b$-jet charge was investigated in a dedicated
Figure 4. Data and MC comparison of the mean of the absolute value of the b-jet charge, $\langle |Q_{b-jet}| \rangle$, as a function of b-jet $p_T$ after the basic $t\bar{t}$ requirements (upper plots) and after the full set of requirements (bottom plots) for electron + jets (left) and muon + jets (right) events. The data are shown after subtraction of the expected background and MC stands for MC@NLO $t\bar{t}$ events. Only statistical uncertainties are shown.

MC study, which showed a linear dependence. In addition, figure 4 demonstrates that the mean b-jet charge depends only weakly on the b-jet $p_T$, especially for the distributions after the $\ell b$-pairing, which makes the charge weighting procedure insensitive to uncertainties in the b-jet $p_T$ distribution.

The increasing instantaneous LHC luminosity was accompanied by an increasing mean number of reconstructed pp interaction vertices per bunch crossing. This quantity, which is a measure of pile-up (presence of additional interactions in the event), increased from 6 to 17 during the analysed 2011 data-taking period. To assess the impact of pile-up, the mean of the absolute value of b-jet charge, $\langle |Q_{b-jet}| \rangle$, is reconstructed as a function of
Figure 5. Data and MC (MC@NLO) comparison of the mean of the absolute value of the $b$-jet charge, $\langle |Q_{b-jet}| \rangle$, as a function of vertex multiplicity after all the $t\bar{t}$ requirements for electron + jets (left) and muon + jets (right) events.

<table>
<thead>
<tr>
<th>Lepton channel</th>
<th>$N_{\ell b}^{\text{expect}}$</th>
<th>$N_{\ell b}^{\text{data}}$</th>
<th>$\langle Q_{\text{comb}} \rangle$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$e$</td>
<td>1600 ± 150</td>
<td>1638</td>
<td>-0.075 ± 0.006</td>
</tr>
<tr>
<td>$\mu$</td>
<td>2100 ± 200</td>
<td>2276</td>
<td>-0.074 ± 0.006</td>
</tr>
<tr>
<td>$e + \mu$</td>
<td>3700 ± 250</td>
<td>3914</td>
<td>-0.075 ± 0.004</td>
</tr>
</tbody>
</table>

Table 4. Number of $\ell b$-pairs expected from MC simulation ($N_{\ell b}^{\text{expect}}$) and observed in data ($N_{\ell b}^{\text{data}}$), and reconstructed mean combined charge, $\langle Q_{\text{comb}} \rangle$, for the data in the different lepton + jets channels compared to those expected in the SM and the exotic model (XM). The uncertainties include the statistical uncertainties scaled to 2.05 fb$^{-1}$ and the uncertainties in the cross sections and integrated luminosity.

the number of reconstructed $pp$ interaction vertices for both the data and MC samples and with the full set of the $t\bar{t}$ requirements used in this analysis including two $b$-tags and $\ell b$-pairing. No dependence is observed for the level of pile-up present in the data sample, as shown by figure 5 for the absolute value of $b$-jet charge. The same level of stability is observed for the combined charge as a function of the primary vertex multiplicity.

Figure 6 compares the $b$-jet charge spectra after the basic $t\bar{t}$ cuts for the data and the expected sum of signal and background normalized to the integrated luminosity of 2.05 fb$^{-1}$. The charge spectra are symmetric around zero and show good agreement between data and MC.

The results for the combined charge are summarized in table 4. This table contains the number of reconstructed lepton–$b$-jet pairs along with the mean combined charge for the different channels. The uncertainties in the expected number of events in table 4 include the cross-section uncertainty and the 1.8% uncertainty in the integrated luminosity.
Figure 6. Data and MC comparison of the $b$-jet charge after the basic $t\bar{t}$ requirements for electron + jets (left) and muon + jets (right) events. The MC expectations for signal and background are normalized to 2.05 fb$^{-1}$ using the expected cross sections. The shaded area corresponds to a combination of statistical uncertainties and uncertainties in the cross sections and integrated luminosity.

The combined charge for the exotic model in table 4 was obtained by inverting the signal $t\bar{t}$ and single-top-quark combined charges while the non-top-quark background charge was not changed. The inversion of the $b$-jet charge (or lepton charge) in a lepton–$b$-jet pair, provided that the lepton and $b$-jet come from a top quark decay, corresponds to a change of the decaying quark charge from $2/3$ to $-4/3$. Such an approximation of the process with the exotic quark should be appropriate since the exotic quark differs from the top quark only in the electric charge. Although this could result in higher photon radiation in the exotic quark case, and consequently in a slightly softer $b$-jet $p_T$ spectrum, this should not influence the combined charge since the photon radiation in the top quark case is only a small effect and the $b$-jet charge depends only weakly on $b$-jet $p_T$. This was verified by studying the exotic quark combined charge directly using events generated by ACERMC. The ACERMC sample gives, within statistical uncertainties, a compatible result with that obtained using the inversion procedure applied to the SM MC@NLO sample.

From table 4 it can be concluded that the data agree with the SM top quark hypothesis within the uncertainties and that the observed and expected numbers of events are also consistent with each other. Figure 7 compares the reconstructed combined charge spectra for the data with MC expectations for signal and background after $\ell b$-pairing for the electron + jets (left) and muon + jets (right) final states, showing good agreement between the data and the SM expectations.

The top quark charge can be directly inferred from the background-subtracted $Q_{\text{comb}}$ data distribution using a $Q_{\text{comb}}$ to $b$-jet charge calibration coefficient obtained from MC. From the SM value of the $b$-quark charge ($Q_b = -1/3$) and the mean reconstructed value of the combined charge ($\langle Q_{\text{comb}} \rangle$) for signal events, the $b$-jet charge calibration coefficient
Figure 7. Distribution of the combined charge, $Q_{comb}$, in electron + jets (left) and muon + jets (right) final states. The full circles with error bars are data, the full black line corresponds to the SM scenario, and the dashed red line corresponds to the exotic model. The vertical line, labeled with $\langle Q_{comb} \rangle$, shows the mean value of the $Q_{comb}$ distribution obtained from data. Only statistical uncertainties are shown.

$C_b = Q_b / \langle Q_{comb} \rangle$ is found to be $4.23 \pm 0.03 \, (\text{stat.}) \pm 0.07 \, (\text{syst.})$ when evaluated using the full $t\bar{t}$ MC sample. The systematic uncertainty on $C_b$ is taken as half the difference between the values of the calibration coefficient for the electron and muon channels. As mentioned in section 6.1 the small difference between the mean combined charges of the electron and muon channels arises as a consequence of different selection criteria used for these channels. The mean combined charge depends slightly on $b$-jet $p_T$ and the $\ell b$-pairing purity and efficiency depend on lepton and $b$-jet $p_T$. Though these dependences are weak they should be taken into account if the common calibration coefficient is used. The top quark charge then can be calculated as

$$Q_{top} = 1 + Q_{comb}^{(\text{data})} \times C_b ,$$

where $Q_{comb}^{(\text{data})}$ is the reconstructed $b$-jet charge obtained from the data after the subtraction of the expected background.

The mean value of the top quark charge for the electron + jets channel is $Q_{top} = 0.63 \pm 0.04 \, (\text{stat.}) \pm 0.11 \, (\text{syst.})$ and that for the muon + jets channel is $Q_{top} = 0.65 \pm 0.03 \, (\text{stat.}) \pm 0.12 \, (\text{syst.})$. The combined result using both channels is $0.64 \pm 0.02 \, (\text{stat.}) \pm 0.08 \, (\text{syst.})$. This result is obtained from the mean of the combined histogram of $Q_{comb}$ for the two channels. The quoted systematic uncertainty includes uncertainties on the calibration constant and all the uncertainties on the mean combined charge as described below.
7.1 Systematic uncertainties

The studies of systematic uncertainties connected with the combined charge follow methods similar to those used in other top quark studies (see e.g. ref. [37]). Each systematic effect is investigated by varying the corresponding quantity by $\pm 1\sigma$ with respect to the nominal value. If the direction of the variation is not defined (as in the case of the estimate resulting from the difference of two models, e.g. HERWIG and PYTHIA), the estimated variation is assumed to be the same size in the upward and the downward direction and the uncertainty on $\langle Q_{comb} \rangle$ is symmetrized. The following effects are taken into account.

Monte Carlo generators — the systematic uncertainties from MC generators are estimated by comparing the results obtained with the MC@NLO and POWHEG generators.

Showering and hadronization — the POWHEG samples with shower models from PYTHIA or HERWIG are compared and the difference is taken as the uncertainty due to the showering model.

Top quark mass — the uncertainty resulting from the assumed top quark mass is estimated using simulated $t\bar{t}$ samples with top quark mass in the range of 167.5–177.5 GeV in steps of 2.5 GeV. After fitting the mean values of $Q_{comb}$ for different top quark mass samples the quoted systematic uncertainty is the largest of the differences between the fit function value at 172.5 GeV and at those at 172.5 $\pm$ 1.0 GeV.

Initial- and final-state radiation (ISR/FSR) — the ISR/FSR uncertainty is calculated using dedicated signal samples generated with ACERMC interfaced to PYTHIA. The parameters responsible for the level of ISR and FSR are varied in a range comparable to those used in the Perugia MC tunes [42]. Half of the difference between the minimum and maximum values of $\langle Q_{comb} \rangle$ is taken as the systematic uncertainty due to ISR/FSR.

Colour reconnection — the systematic uncertainty due to colour reconnection is determined using ACERMC interfaced to PYTHIA. Two different colour reconnection effects are simulated as described in refs. [42, 43] and for each effect the difference in the reconstructed combined charge between two levels of the colour reconnection is found. The larger difference is taken as the systematic uncertainty.

Missing transverse momentum — $E_T^{\text{miss}}$ is used in the event selection and can influence the reconstructed $Q_{comb}$. The impact of a possible mis-calibration is assessed by changing the measured $E_T^{\text{miss}}$ within its uncertainty. The systematic uncertainty of $E_T^{\text{miss}}$ includes the energy scale of clusters not associated with jets, electrons or muons and the accuracy of the pile-up simulations. The effect of a hardware failure in a part of the liquid-argon calorimeter is also taken into account. This uncertainty is assessed by varying the jet thresholds used for removing events with jets in the dead calorimeter region.

Multi-jet normalization — a 100% uncertainty on the number of multi-jet events due to the data-driven method is assumed in calculating the uncertainty of $\langle Q_{comb} \rangle$ connected with this normalization.

Single-top-quark normalization — the cross sections of individual single-top-quark channels are simultaneously varied within their theoretical uncertainty by $\pm 1\sigma$ and the largest difference in the combined signal and background $\langle Q_{comb} \rangle$ with respect to the nominal one is quoted as the systematic uncertainty due to the single-top-quark production cross section [44].
$W + jets$ — the $W + jets$ cross section is varied within its theoretical uncertainty (the uncertainty for inclusive $W$ production of 4% and the additional uncertainty per each additional jet, of 24%, are added in quadrature). The uncertainties on the shapes of $W + jets$ kinematic distributions are assessed by varying several parameters, such as the minimum transverse momentum of the partons and the functional form of the factorization scale in ALPGEN. The $W + jets$ samples are reweighted according to each of these parameters and the quadratic sum of the uncertainties for the individual parameters is taken as the systematic uncertainty. Uncertainties connected with the scaling factors correcting the fractions of heavy flavour contributions in simulated $W + jets$ samples are also taken into account.

$Z + jets$ — the same prescription as for the normalization of $W + jets$ events is also applied to $Z + jets$ events.

$b$-tagging — the $b$-tagging efficiency and mistag probabilities in data and MC simulation are not identical. To reconcile the difference, $b$-tagging scale factors together with their uncertainties are derived per jet [35, 36]. They depend on the jet $p_T$ and $\eta$ and the underlying quark flavour. For the nominal result, the central values of the scale factors are applied, and the systematic uncertainty is estimated by changing their values within their uncertainties.

Lepton-related uncertainty — this item comprises the uncertainties due to MC modelling of the lepton identification, trigger efficiency, energy scale and energy resolution. Each simulated event is weighted with an appropriate scale factor (ratio of the measured efficiency to the simulated one) in order to reproduce the efficiencies seen in data. The uncertainties on the scale factors are included in the uncertainties on the acceptance values. Details can be found in ref. [37].

Jet energy scale — the jet energy scale (JES) and its uncertainty are derived by combining information from test-beam data, LHC collision data and MC simulations [45, 46]. The dependence of the JES uncertainty on the $p_T$ and $\eta$ of the reconstructed jet is used to scale the energy of each jet up or down by one standard deviation in the used MC sample. These variations are also propagated to the missing transverse energy. An uncertainty contribution to the JES due to pile-up events is also taken into account. An additional uncertainty is applied exclusively to $b$-jets. For each $b$-jet matched to a parton level $b$-quark a $p_T$-dependent uncertainty ranging from 2.5% for low-$p_T$ jets to 0.76% for high-$p_T$ jets is used.

The JES is the most significant source of systematic uncertainty. The reason is that changes in the JES have a large impact on the number of events with low-$p_T$ $b$-jets and the purity of the $\ell b$-pairing degrades at low $b$-jet $p_T$. The number of events at high and low JES varies with respect to the nominal scale by 25% and 14%, respectively.

Jet energy resolution — the impact of the jet energy resolution is assessed by smearing the jet energy before performing the event selection. The energy of each reconstructed jet in the simulation is additionally smeared by a Gaussian function such that the width of the resulting Gaussian distribution includes the uncertainty on the jet energy resolution.

Jet reconstruction efficiency — the impact of the uncertainty in the jet reconstruction efficiency is evaluated by randomly dropping jets from events and determining the
Table 5. The systematic uncertainties for the combined charge. The total uncertainty is calculated by adding the individual ones in quadrature.

<table>
<thead>
<tr>
<th>Source</th>
<th>Systematic uncertainty (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>MC statistics</td>
<td>0.7</td>
</tr>
<tr>
<td>MC generator</td>
<td>3.7</td>
</tr>
<tr>
<td>Parton shower</td>
<td>7.9</td>
</tr>
<tr>
<td>Colour reconnection</td>
<td>0.5</td>
</tr>
<tr>
<td>ISR/FSR</td>
<td>3.1</td>
</tr>
<tr>
<td>Top quark mass</td>
<td>0.3</td>
</tr>
<tr>
<td>Missing transverse energy</td>
<td>0.8</td>
</tr>
<tr>
<td>Jet energy scale</td>
<td>8.3</td>
</tr>
<tr>
<td>$b$-jet energy scale</td>
<td>3.3</td>
</tr>
<tr>
<td>Jet energy resolution</td>
<td>1.0</td>
</tr>
<tr>
<td>Jet reconstruction efficiency</td>
<td>0.7</td>
</tr>
<tr>
<td>$b$-tagging</td>
<td>0.3</td>
</tr>
<tr>
<td>Single top normalization</td>
<td>$&lt;0.1$</td>
</tr>
<tr>
<td>$W +$ jets</td>
<td>1.2</td>
</tr>
<tr>
<td>$Z +$ jets</td>
<td>0.1</td>
</tr>
<tr>
<td>Multi-jet normalization</td>
<td>1.0</td>
</tr>
<tr>
<td>Electron-related uncertainty</td>
<td>1.3</td>
</tr>
<tr>
<td>Muon-related uncertainty</td>
<td>1.8</td>
</tr>
<tr>
<td>$b$-hadron fractions</td>
<td>0.7</td>
</tr>
<tr>
<td>Total uncertainty of $e + \mu$-channel</td>
<td>13.2</td>
</tr>
</tbody>
</table>

variation of $\langle Q_{\text{comb}} \rangle$ with respect to that of the nominal sample, following the prescription described in ref. [32].

*Influence of $b$-hadron fractions* — in the hadronization process that leads to a $b$-jet, different $b$-hadrons can be formed and the combined charge can depend on the $b$-hadron type. In addition, the mixing of $B^0$ and $B^0_S$ mesons needs to be taken into account. For the $b$-jets containing $B^0$-mesons, it leads to a smaller mean combined charge in comparison with the jets containing charged $B$ mesons. The effect for jets containing $B^0_S$ mesons, where the mixing probability is 50%, should lead to zero mean combined charge. The measured mixing probabilities ($\chi_d = 0.186 (B^0)$ and $\chi_S = 0.5 (B^0_S)$) [47] are used to find the effective values of the mean combined charge for $b$-jets with $B^0$ and $B^0_S$ mesons. A study based on MC simulation shows that the mean combined charge for $b$-jets with $b$-baryons is about 74% of that for $b$-jets with $B^\pm$. The systematic uncertainty on the mean combined charge due to the uncertainties on the $b$-hadron production fractions, taken from ref. [45], has been evaluated by varying independently the production fractions for $B^0$ and $B^0_S$ mesons and $b$-baryons by 1 standard deviation up and down and adding the individual contributions in quadrature.

All other systematic uncertainties are small (less than 1%). A summary of all systematic uncertainties for the reconstruction of the combined charge in the electron and muon channels combined is shown in table 5.
Statistical comparison of the SM and exotic model

The main result of this analysis — the compatibility of the data with the SM hypothesis of the top quark charge of 2/3 — was evaluated using a statistical model. This model is based on the Cousins-Highland approach [48]. The test statistic used for this purpose is the mean value of the combined charge. Due to finite detector resolution and finite sample size, the mean value of the combined charge observed in the experiment can be treated as one realization of a random variable, \( \bar{Q} \), the distribution of which characterizes all possible outcomes of the experiment. This variable can be expressed as

\[
\bar{Q} = (1 - r_b - r_t) \cdot Q_s + r_b \cdot Q_b + r_t \cdot Q_t,
\]

where \( Q_s \), \( Q_b \), and \( Q_t \) are the combined charge mean values for the signal, background and single-top-quark processes, respectively, and \( r_b \) (\( r_t \)) is the fraction of the background (single-top-quark) events in the total sample of the candidate events.

The SM acceptance (critical) region [49, 50] is defined as \( \bar{Q} < 0 \) (\( \bar{Q} > 0 \)). The decision boundary \( \bar{Q} = 0 \) unambiguously determines the confidence level \( \alpha \) (probability to exclude the SM scenario if it is true) and the so-called false negative rate \( \beta \) (the probability of failing to reject the alternative hypothesis if it is true). The quantities \( Q_s \), \( Q_b \), \( Q_t \), \( r_b \) and \( r_t \) are the nuisance parameters of the method and are assumed to be Gaussian random variables. The Gaussian nature of the combined charges was tested with 10 million MC experiments. In each experiment the mean combined charge was found by averaging 1000 combined charges generated from a MC-simulated combined charge spectrum for the muon channel. The obtained distribution of the mean combined charges was normally distributed and the Gaussian fit to the distribution showed a goodness-of-fit of \( \chi^2/ndf = 86/103 \). Their uncertainties scaled to the data integrated luminosity (2.05 fb\(^{-1}\)) are summarized in table 6. The two hypotheses are compared by calculating the \( p \)-value [49], the probability of obtaining a test statistic at least as extreme as the one that was actually observed provided that the null hypothesis is true. In order to obtain the \( p \)-value for the observed values of the test statistic \( \langle Q_{\text{comb}} \rangle \) (see the data column of table 4), pseudo-experiments for both hypotheses, the SM as well as the exotic model, have been performed. To take into account a possible difference between MC and experimental data, a scale factor (SF) is defined as the ratio of experimental to MC mean combined charges for a QCD \( b \)-jet sample. The scale factor SF was found using double \( b \)-tagged dijet events containing a soft muon, where

\[
\begin{array}{|c|c|c|c|c|c|}
\hline
\text{Channel} & Q_s & Q_b & Q_t & r_b & r_t \\
\hline
\mu & -0.078 \pm 0.006 & -0.052 \pm 0.028 & -0.051 \pm 0.038 & 0.088 \pm 0.025 & 0.038 \pm 0.011 \\
\mu + \mu & -0.079 \pm 0.004 & -0.038 \pm 0.023 & -0.058 \pm 0.028 & 0.079 \pm 0.016 & 0.040 \pm 0.008 \\
\hline
\end{array}
\]

Table 6. The nuisance parameters: the expected combined charge mean values and their standard deviations for the signal \( (Q_s) \), non-top-quark background \( (Q_b) \), single-top-quark background \( (Q_t) \) and the fractions of non-top-quark \( (r_b) \) and single-top-quark \( (r_t) \) backgrounds for an integrated luminosity of 2.05 fb\(^{-1}\).
Figure 8. The expected distribution of the mean value of the combined charge, $\bar{Q}$, for the electron and muon channels resulting from pseudo-experiments for the SM (solid blue line) and the exotic (dashed red line) hypothesis for an integrated luminosity of $2.05 \text{ fb}^{-1}$. The magenta vertical line represents the value measured in the data.

The charge of the soft muon determines the flavour of the $b$-jet (i.e. if $b$ or $\bar{b}$ initiated the jet). This technique gives $SF = 1.00$ with a spread $\sigma = 0.19$. The technique based on the absolute value of the $b$-jet charge, i.e. based on the data-to-MC ratio from figure 4, leads to a scale factor compatible with unity with a spread $\sigma = 0.02$. To be conservative, the former value is used. The SF uncertainty is added in quadrature to the statistical and systematic uncertainties of the combined mean charge.

In figure 8 the distributions from the pseudo-experiments of the observed mean combined charge ($\bar{Q}$) are shown for both hypotheses, the SM (solid blue line) and the exotic model (dashed red line). The magenta line in this plot corresponds to the experimentally observed value $Q_{\text{obs}}$. The figure shows the results for the combined electron and muon channels. Each of these distributions is obtained from pseudo-experiments in which the nuisance parameters are sampled from Gaussian distributions with the mean values and standard deviations taken from table 6. In addition, the sampled charge $\bar{Q}$ is Gaussian-smeared by the mean combined charge systematic uncertainty and by the SF uncertainty.

The $p$-values for the SM and the exotic model, the distance of $Q_{\text{obs}}$ from the expected value of the exotic combined charge in standard deviations, and the quantities $\alpha$ and $\beta$, are summarized in table 7 for the combined electron and muon ($e + \mu$) channel as well as for the electrons ($e$) and muons ($\mu$) channels separately.

From table 7 it can be seen that the data are fully compatible with the SM. The $p$-values for the SM scenario are high (the two-sided $p$-value is more than 80%) while those for the exotic hypothesis are very small (less than $10^{-7}$). None of the 20 million exotic-hypothesis pseudo-experiments have $\bar{Q}$ values below the observed value of the mean combined charge. Converting the $p$-value into the number of standard deviations for the exotic-scenario mean combined charge distribution, an exclusion at the level higher than $8\sigma$ is obtained for the combination of the electron and muon channels. This result assumes Gaussian-distributed
nuisance parameters, as supported by the performed MC experiments. Due to fact that most of the systematic uncertainties were combined and are common to the electron and muon channels, the differences in the nuisance parameters do not lead to large differences in the exclusion limits for the individual channels.

9 Conclusion

The top quark charge has been studied using 2.05 fb$^{-1}$ of data accumulated by the ATLAS experiment at a centre-of-mass energy of 7 TeV. The measured top quark charge is $0.64 \pm 0.02$ (stat.) $\pm 0.08$ (syst.). This result strongly favours the Standard Model and excludes models with an exotic quark with charge $-4/3$ instead of the top quark by more than 8$\sigma$.

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<table>
<thead>
<tr>
<th>Channel</th>
<th>$p_{SM}$</th>
<th>$p_{XM}$</th>
<th>$\sigma_{XM}$ (s.d.)</th>
<th>$\alpha$</th>
<th>$\beta$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$e$</td>
<td>0.813</td>
<td>&lt; 10$^{-7}$</td>
<td>8.8</td>
<td>6.1 $\times$ 10$^{-6}$</td>
<td>1.1 $\times$ 10$^{-5}$</td>
</tr>
<tr>
<td>$\mu$</td>
<td>0.960</td>
<td>&lt; 10$^{-7}$</td>
<td>8.5</td>
<td>2.4 $\times$ 10$^{-6}$</td>
<td>4.0 $\times$ 10$^{-5}$</td>
</tr>
<tr>
<td>$e + \mu$</td>
<td>0.892</td>
<td>&lt; 10$^{-7}$</td>
<td>8.9</td>
<td>2.4 $\times$ 10$^{-6}$</td>
<td>1.5 $\times$ 10$^{-5}$</td>
</tr>
</tbody>
</table>

Table 7. The $p$-values for the SM ($p_{SM}$) and exotic model ($p_{XM}$); the distance $\sigma_{XM}$ of the observed value, $Q_{\text{obs}}$, from the expected value of the exotic combined charge in standard deviations (s.d.); the significance level ($\alpha$) and the false negative rate ($\beta$) for the integrated luminosity of 2.05 fb$^{-1}$. 

nuisance parameters, as supported by the performed MC experiments. Due to fact that most of the systematic uncertainties were combined and are common to the electron and muon channels, the differences in the nuisance parameters do not lead to large differences in the exclusion limits for the individual channels.

9 Conclusion

The top quark charge has been studied using 2.05 fb$^{-1}$ of data accumulated by the ATLAS experiment at a centre-of-mass energy of 7 TeV. The measured top quark charge is $0.64 \pm 0.02$ (stat.) $\pm 0.08$ (syst.). This result strongly favours the Standard Model and excludes models with an exotic quark with charge $-4/3$ instead of the top quark by more than 8$\sigma$.

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