Herschel images of Fomalhaut: an extrasolar Kuiper belt at the height of its dynamical activity


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An extrasolar Kuiper belt at the height of its dynamical activity

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ABSTRACT

Context. Fomalhaut is a young (2 ± 1 × 108 years), nearby (7.7 pc), 2 M⊙ star that is suspected to harbor an infant planetary system, interspersed with one or more belts of dusty debris.

Aims. We present far-infrared images obtained with the Herschel Space Observatory with an angular resolution between 5.7′′ and 36.7′′ at wavelengths between 70 μm and 500 μm. The images show the main debris belt in great detail. Even at high spatial resolution, the belt appears smooth. The region in between the belt and the central star is not devoid of material; thermal emission is observed here as well. Also at the location of the star, excess emission is detected. We aim to construct a consistent image of the Fomalhaut system.

Methods. We use a dynamical model together with radiative-transfer tools to derive the parameters of the debris disk. We include detailed models of the interaction of the dust grains with radiation, for both the radiation pressure and the temperature determination. Comparing these models to the spatially resolved temperature information contained in the images allows us to place strong constraints on the presence of grains that will be blown out of the system by radiation pressure. We use this to derive the dynamical parameters of the system.

Results. The appearance of the belt points toward a remarkably active system in which dust grains are produced at a very high rate by a collisional cascade in a narrow region filled with dynamically excited planetesimals. Dust particles with sizes below the blow-out size are abundantly present.

Key words. stars: individual: Fomalhaut – circumstellar matter – planetary systems – radiative transfer – zodiacal dust

1. Introduction

Fomalhaut was one of the first main-sequence stars shown to have an infrared excess caused by dust grains in orbit around the star (Aumann 1985). Further studies of this phenomenon have shown that approximately 15% of solar-like main-sequence stars have a detectable amount of debris (Bryden et al. 2006). Belts of debris typically reside in planetary systems at locations where no planets have formed because either the formation time scale for planets was too long, such as in the solar system’s Kuiper belt, or because other planets in the system have stirred up the belt before a planet could be formed, such as in the solar system’s asteroid belt (Wyatt 2008; Krivov 2010).

Fomalhaut’s disk was previously imaged from the ground at 450 μm and 850 μm, and from space with the Spitzer (Holland et al. 2003) and the Hubble Space Telescopes (HST; Stapelfeldt et al. 2004; Kalas et al. 2005). A planet candidate has been reported in the disk, though 3rd epoch confirmation of this object is still uncertain (Kalas et al. 2008, 2011; Janson et al. 2012). The most prominent feature in the disk is the main belt, which is located outside of 130 AU. The center of this belt is shifted with respect to the star, implying significant eccentricity, probably caused by gravitational interaction with one or more planets (Kalas et al. 2005, 2008; Chiang et al. 2009).

2. Observations

2.1. Herschel images

Far-infrared images of Fomalhaut have been obtained with the PACS (Poglitsch et al. 2010) and SPIRE (Griffin et al. 2010; Swinyard et al. 2010) instruments aboard the Herschel Space Observatory (Pilbratt et al. 2010) in five photometric filters centered around 70 μm, 160 μm (PACS), 250 μm, 350 μm and 500 μm (SPIRE). The Observation IDs are 1342211953, 1342211954 (PACS) and 1342195939 (SPIRE). The full width at half maximum (FWHM) of the point-spread functions (PSFs) indicate a spatial resolution of the observations of 5.7′′, 11.3′′, 18.1′′, 25.1′′ and 36.7′′ for the five bands respectively. This
corresponds to 43, 86, 140, 190 and 280 AU at the distance to Fomalhaut.

The PACS data were processed in the Herschel interactive processing environment (HIPE, Ott 2010) version 6.0, applying the standard pipeline steps. The flux conversion was done using version 5 of the response calibration. Signal glitches due to cosmic-ray impacts were masked using the PACS photMMT-Deglitching task in HIPE on the detector timeline. Then a first coarse map was projected. A high-pass filter was applied to remove the low frequency drifts. To avoid the introduction of artefacts, we used the coarse map to mask out the disk from the detector timeline prior to the application of the filter. The scale of the high-pass filter was 15 frames for the blue maps (70 μm), and 25 frames for the red maps (160 μm). The detector time-series signals were then summed up into a map using the PACS phot-Project task. The pixel scale for the 70 μm map was set to 1″, while the scale for the 160 μm map was 2″. The source was covered in two independent observations, scanning the sky in two orthogonal directions. We combined the two detector time series and projected these together into the final maps.

Also the SPIRE data were reduced using HIPE. The high signal-to-noise ratio of these data allowed us to create oversampled maps with pixel scales of 3″, 4.2″ and 7″ in the 250 μm, 350 μm and 500 μm bands respectively, equating to approximately 6 samples per beam FWHM. The standard pipeline script provided with HIPE was used to reduce the data, with the naiveMapper task being used to construct the maps. A simple linear baseline subtraction was the only filtering performed on these data.

Table 1 summarizes the pixel scale, total map integration time and signal-to-noise ratio of the projected Herschel images. We also indicate the integration time per pixel, which is the total time a pixel in the central part of the projected map was seen by a detector pixel.

Figures 1–3 show that the system is well resolved at 70 μm, barely resolved at 500 μm, and marginally resolved at intermediate wavelengths. A first qualitative look at the images shows that the thermal emission of the dust in the belt around Fomalhaut appears smooth and not clumpy, contrary to what was expected by Wyatt & Dent (2002). The smoothness hints at a high dust replenishment rate by numerous collisions, rather than sporadic replenishment by rare collisional events. The apparent azimuthal brightness variations are due to geometric projection effects. Moreover, distances from the belt to the star vary along the belt, as it is eccentric. The southern ansa is located closer to the star than the northern ansa, and is therefore warmer and brighter. This is the so-called pericenter glow, first observed in a debris disk by Telesco et al. (2000). The planet candidate Fomalhaut b may produce local density enhancements. However, there is no evidence of an excess or a lack of dust emission near the position of Fomalhaut b, nor at any other location along the belt.

In the 70 μm image, the star shows up as an unresolved point source. The flux of this central source, however, exceeds the stellar photospheric flux. This is in agreement with excess flux close to the star previously found at near-infrared wavelengths and attributed to hot dust (Absil et al. 2009). The region between the unresolved central source and the belt is not devoid of dust either; the 70 μm image shows emission in this inner disk as well. The dust particles in this region either originated in the belt and spiraled in past the orbit of Fomalhaut b, or were released from an unresolved inner belt and moved outwards.

2.2. Belt geometry

The geometric properties of the belt were derived from the PACS 70 μm and 160 μm images in the following way. Along each pixel row and column intersecting the belt, the coordinates of the pixel with the highest surface brightness are determined. In this way, the position of the ring in the image is captured by a set of pixel coordinates (x, y) along the ring. An ellipse is fitted

<table>
<thead>
<tr>
<th>Image</th>
<th>Pixela (″)</th>
<th>Integration time (s) per pixel</th>
<th>SBb (mJy/″²)</th>
<th>SNRb</th>
</tr>
</thead>
<tbody>
<tr>
<td>PACS 70 μm</td>
<td>1</td>
<td>10 956</td>
<td>15.6</td>
<td>16.5</td>
</tr>
<tr>
<td>PACS 160 μm</td>
<td>2</td>
<td>10 956</td>
<td>16.7</td>
<td>6.28</td>
</tr>
<tr>
<td>SPIRE 250 μm</td>
<td>3</td>
<td>2906</td>
<td>2.1</td>
<td>1.90</td>
</tr>
<tr>
<td>SPIRE 350 μm</td>
<td>4.2</td>
<td>2906</td>
<td>2.8</td>
<td>0.59</td>
</tr>
<tr>
<td>SPIRE 500 μm</td>
<td>7</td>
<td>2906</td>
<td>3.6</td>
<td>0.19</td>
</tr>
</tbody>
</table>

Notes: (a) Pixel size of the projected image. (b) Surface brightness and signal-to-noise ratio in the brightest pixel of the image. (c) In the central part of the image where the source is located.
to these coordinates, which yields the major axis, the minor axis, and the position angle of the belt as it appears on the sky. The position of the star, relative to the belt center, is measured from the PACS 70 \( \mu \text{m} \) image by fitting a two-dimensional Gaussian curve to the central unresolved point source. From the parameters of the apparent ellipse, the stellar position, and the known distance to Fomalhaut, the orbital elements of the belt are computed: the semi-major axis \( a \), the eccentricity \( e \), the inclination \( i \), the longitude of the ascending node \( \Omega \), and the argument of periastron \( \omega \).

We repeat this ellipse-fitting procedure 1000 times by adding random noise in each spatial pixel (spaxel) of the image. The magnitude of this added noise is equal to three times the pixel-to-pixel noise of the original image, estimated by taking the standard deviation of the image outside the location of the Fomalhaut system on the sky. As a result of this added noise, the set of belt locations \((x, y)\) are not exactly the same for two different simulations (although several pixels may be in common). Also the measured stellar position varies. Each simulation will therefore yield slightly different parameters. Our final set of belt parameters are the mean values, and the errors the standard deviations, of the outcome of these 1000 simulations. The same procedure is applied to derive the belt parameters from the PACS 160 \( \mu \text{m} \) image. Because the star is not visible in this image, however, we use the relative stellar position measured in the 70 \( \mu \text{m} \) image.

The geometric properties of the belt are summarized in Table 2. They are similar to those derived from optical scattering images (Kalas et al. 2005), apart from the argument of periastron \( \omega \). We find that the star is located almost perfectly on the apparent major axis of the belt on the sky, leading to \( \omega = 1^\circ \pm 6^\circ \). Kalas et al. (2005) do not explicitly mention the value, but \( \omega \) can be estimated from the measured difference (\( \delta = 14^\circ \)) between their longitude of the nodal line (\( \Omega = 156^\circ \)) and their belt center-star offset direction (\( 170^\circ \)), deprojected for the inclination (\( i = 65.6^\circ \)): \( \omega = \arctan(\tan \delta / \cos i) = 31^\circ \pm 6^\circ \). The reason for this discrepancy is unclear to us, but we are confident in our value. Our Herschel 70 \( \mu \text{m} \) image is unique in that it captures both the stellar light and the thermal dust emission simultaneously, in contrast to the HST images, where the direct starlight had to be blocked to be able to detect the light scattered by the belt. Our measurement of \( \omega \) is therefore more direct. To elaborate on this issue, we have tested both values of \( \omega \) with our radiative-transfer model (see Sect. 3). In the case of \( \omega = 31^\circ \), the pericenter glow in the model images is clearly off the major axis of the belt, toward the south, unlike the observed on-axis pericenter glow. The on-axis position of both star and pericenter glow, lead us to conclude that \( \omega \) must be close to zero degrees.

Although the HST optical images have a spatial resolution much higher than that of Herschel/PACS at 70 \( \mu \text{m} \) (0.5 AU vs. 43 AU at the distance of Fomalhaut), the error bars on the belt parameters are comparable. This is mainly due to the superb signal-to-noise ratio of the PACS images (see Table 1).

The belt properties derived from the 160 \( \mu \text{m} \) image are less certain. The derived semi-major axis (125 AU) is significantly smaller than the one derived from the 70 \( \mu \text{m} \) image (137.5 AU). We ascribe the difference to the lower angular resolution: The larger PSF at 160 \( \mu \text{m} \) makes the belt appear smaller, because it squeezes the locations of peak surface brightness inwards.

### 2.3. Spectral energy distribution

Herschel photometry was derived from the images described above, by integrating the flux within a circular aperture around the geometric center of the belt on the sky. We used an aperture radius of 52\(^{\prime}\), i.e. 400 AU at the distance of Fomalhaut (Table 3). The mentioned uncertainties consist of the statistical errors, amounting to \( \pm 10\% \) of the measured flux. According to the SPIRE and PACS documentation available from the Herschel Science Center web pages\(^2\), the absolute calibration error on the photometry is another 10\%.

Additional photometry of the Fomalhaut system was extracted from several online catalogues, available from http://vizier.ustrasbg.fr/viz-bin/VizieR Stellar photosphere models (Castelli & Kurucz 2003) were fitted to the optical Geneva photometry (Rufener 1988). We have interpolated between the grid models of Castelli & Kurucz (2003), according to the method explained in Degroote et al. (2011, their Sect. 2). The derived fundamental parameters of the star are an effective temperature \( T_{\text{eff}} = 8600 \pm 200 \, \text{K} \), a surface gravity \( \log g = 4.1 \pm 0.2 \, \text{dex} \), and an interstellar reddening \( E(B-V) < 0.08 \). The photometric angular diameter of the star is \( 2.20 \pm 0.04 \, \text{milliarcsec} \), in perfect agreement with interferometric measurements (Di Folco et al. 2004). The infrared photometry is taken from the AKARI/IRC and FIS All-Sky Survey point source catalogues (Ishihara et al. 2010; Yamamura et al. 2010), the ESO catalogue IR photometry of calibrator stars (van der Bliek et al. 1996), and the Spitzer Space Telescope MIPS catalogue (Su et al. 2006). The two sub-mm measurements, at 450 \( \mu \text{m} \) and 850 \( \mu \text{m} \), are consistent with the SPIRE photometry (Holland et al. 2003). The spectral energy distribution (SED) of the Fomalhaut system is shown in Fig. 5.

### 3. Modeling

#### 3.1. Three components

We use a three-component model to reproduce the detected thermal dust emission. A central, unresolved component responsible

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1 The model images are convolved with the PACS 70 \( \mu \text{m} \) PSF before comparison with the observations. All asymmetries related to the latter are hence taken into account.

2 http://herschel.esac.esa.int/
for the stellar plus excess emission at the location of the star, a narrow ring of dust produced in a collisional cascade for the belt, and a power-law surface density to reproduce residual emission inside the belt.

We assume that the dust in the belt originates from a narrow source region, a ring between radii \( r_1 \) and \( r_2 \) in which dust grains are produced through collisions with a size distribution according to the equilibrium cascade: \( f(s) \propto s^{-3.5} \), with \( s \) defined as the radius of the grain (Dohnanyi 1969). The particles are assumed to be released from a parent body on an orbit inside the ring. For small grains, their orbits are modified by stellar radiation forces on the particles. The modification depends on the ratio \( \beta = F_{\text{rad}}/F_{\text{grav}} \) of radiation and gravitational forces acting on the particles. Particles with \( \beta < 0.5 \) will remain in bound orbits around the star, with periastrons \( r_p \) equal to their release points in the ring, and forced eccentricities \( e = \beta/(1-\beta) \) so that the semi-major axes become \( a = r_p/(1-e) \). Hence, particles with increasing \( \beta \) will find themselves in orbits with increasing eccentricities and apastron distances. Particles with a given \( \beta \) will produce a surface density distribution inversely proportional to \( 2\pi^2 a \sqrt{a^2-e^2} - (r-a)^2 \) in the region \( a(1-e) < r < a(1+e) \).

Particles with \( \beta > 0.5 \) will be on hyperbolic orbits, and gradually leave the system. These so-called blow-out particles are constantly replenished by the collisional cascade and contribute at low levels to the surface density outside of the ring. We assume that the small-grain extension of the collisional cascade power-law is replenished every \( t_{\text{repl}} \) years, which provides a scaling factor for the surface density of the blow-out particles. The replenishment time is a free parameter of the model.

For particles in the inner-disk region, we take a power-law size distribution with \( f(s) \propto s^{-3} \). Such a distribution will result from drawing grains by means of Poynting-Robertson (PR) drag from the belt (Burns et al. 1979), as explained in Appendix A. Moreover, we remove all particles with \( \beta > 0.5 \) from the inner disk, since these will be blown out quickly. The size distribution in the inner disk is not well constrained by the Herschel images, however. Besides PR drag, evaporating comets and additional debris belts closer to the star are possible sources of dust grains in the inner disk between star and outer belt that could have very different size distributions. Including only PR drag and assuming that no collisions occur in the PR stream inward of the source ring, a constant surface density in the inner disk is expected (see Appendix A), resulting in a surface brightness profile that is heavily peaked toward the central star but this is inconsistent with our observations. A planetary system inside the ring could clear out the particles as they drift in, creating a surface density profile that decreases toward the star. We model this distribution using a power-law surface density where the exponent is a free parameter.

The central source in the 70 \( \mu \)m image is modeled with a point source, convolved with the PSF of the PACS instrument at this wavelength. The model hence consists of three geometric components: a belt, an inner disk and a central point source.

### Table 2. Geometric properties of the elliptical belt.

<table>
<thead>
<tr>
<th>Semi-major axis (AU)</th>
<th>Optical</th>
<th>70 ( \mu )m</th>
<th>160 ( \mu )m</th>
</tr>
</thead>
<tbody>
<tr>
<td>( d )</td>
<td>141 ± 2</td>
<td>137.5 ± 0.9</td>
<td>125 ± 3 ( \mu )</td>
</tr>
<tr>
<td>Eccentricity ( e )</td>
<td>0.11 ± 0.01</td>
<td>0.125 ± 0.006</td>
<td>0.17 ± 0.07</td>
</tr>
<tr>
<td>Inclination ( i ) ((^\circ))</td>
<td>65.6 ± 0.4</td>
<td>65.6 ± 0.5</td>
<td>64 ± 2</td>
</tr>
<tr>
<td>Longitude of ascending node ( \Omega ) ((^\circ))</td>
<td>156.0 ± 0.3</td>
<td>156.9 ± 0.5</td>
<td>160 ± 2</td>
</tr>
<tr>
<td>Argument of periastron ( \omega ) ((^\circ))</td>
<td>31 ± 6</td>
<td>1 ± 6</td>
<td>...</td>
</tr>
<tr>
<td>Offset between star and ring center (AU)</td>
<td>15 ± 1</td>
<td>17.2 ± 0.9</td>
<td>...</td>
</tr>
</tbody>
</table>

Notes. (a) Kaleta et al. (2005). (b) At peak surface brightness. (c) Spatial resolution of the 160 \( \mu \)m image is insufficient to derive a reliable semi-major axis. (d) Star not visible at 160 \( \mu \)m. (e) In the plane of the belt.

### Table 3. Herschel photometry of Fomalhaut.

<table>
<thead>
<tr>
<th>Band</th>
<th>Integrated flux (Jy)( ^a )</th>
<th>Point source</th>
<th>Flux contribution (%)( ^b )</th>
<th>Inner disk</th>
<th>Belt</th>
<th>Blow-out grains</th>
</tr>
</thead>
<tbody>
<tr>
<td>PACS 70 ( \mu )m</td>
<td>10.8 ± 0.9</td>
<td>5</td>
<td>21</td>
<td>127</td>
<td>7</td>
<td></td>
</tr>
<tr>
<td>PACS 160 ( \mu )m</td>
<td>6.2 ± 0.6</td>
<td>2</td>
<td>23</td>
<td>75</td>
<td>7</td>
<td></td>
</tr>
<tr>
<td>SPIRE 250 ( \mu )m</td>
<td>2.7 ± 0.3</td>
<td>2</td>
<td>25</td>
<td>73</td>
<td>3</td>
<td></td>
</tr>
<tr>
<td>SPIRE 350 ( \mu )m</td>
<td>1.1 ± 0.1</td>
<td>2</td>
<td>27</td>
<td>71</td>
<td>2</td>
<td></td>
</tr>
<tr>
<td>SPIRE 500 ( \mu )m</td>
<td>0.50 ± 0.05</td>
<td>2</td>
<td>29</td>
<td>69</td>
<td>2</td>
<td></td>
</tr>
</tbody>
</table>

Notes. (a) Within a circular aperture with a radius of 52″ (400 AU) around the geometric center of the belt. (b) From the best-fit model. (c) The excess flux at the location of the star is 50 ± 10% of the stellar flux at 70 \( \mu \)m, or 0.17 ± 0.02 Jy.

The dust particles in our simulations are mixtures of common astronomical species, including water ice, following the composition proposed by Min et al. (2011). This is a mixture consistent with the solar abundances derived by Grevesse & Sauval (1998). The resulting composition contains by mass 32% silicates, 10% iron sulfide, 13% amorphous carbon, and 45% water ice.

To simulate inhomogeneous grains we mix the various materials using effective medium theory. For this we use the Bruggeman mixing rule (Bruggeman 1935; Voshchinnikov et al. 2007). We simulate porosity of the grains by adding a fraction of vacuum to the mixture. The grain shape is described by a distribution of hollow spheres (DHS, Min et al. 2005) with an irregularity parameter \( f_{\text{irr}} = 0.8 \). With a mild porosity of 25% vacuum, we find that the blow-out size for grains in the Fomalhaut system is 13 \( \mu \)m. We tested various values of the porosity and also dust particles without ice to mimic the effect of photosputtering (Grigorieva et al. 2007).
Fig. 3. *Herschel* far-infrared images of Fomalhaut. a) Observations, b) Model images, c) Absolute value of the residuals. The hatched circles indicate the spatial resolution. The color scale is linear rainbow to increase contrast at low surface brightness. The scale ranges from zero to maximum surface brightness (see Table 1) of the image in columns a) and b); In column c), the color scale is the same as in column a). North is up, east to the left.
For the initial size distribution formed by the collisional cascade we use a power law, as stated above, a minimum grain size of 1 μm, and a nominal maximum grain size of 5000 μm. The latter value is not well constrained by the observations. The size distribution at each location in the disk is computed following the dynamical model described above. The averaged mass absorption coefficients for grains formed in the collisional cascade with sizes below 13 μm, i.e. the blow-out grains, and the averaged opacities for grains larger than the blow-out size are plotted in Fig. 4. Note that these opacities do not necessarily represent the averaged opacities at any location in the disk since the size distribution is significantly altered by the radiation dynamics.

3.3. The model grid

We set up a grid of models with varying inner and outer radius for the ring where the planetesimals collide. We fixed the value of r₁ equal to the inner-edge radius of 133 AU that was well determined based on the HST images (Kalas et al. 2005). We also tested a slightly different r₁ of 123 and 143 AU. For the outer radius of the ring, we took r₂ = r₁ + [2, 5, 10, 20, 30, 40] AU. For the inner disk, we tested surface-density power laws proportional to r⁰ (PR), r⁻¹ and r⁻². The outer edge of the inner disk is set to the inner radius of the ring. On the inside, we assume that our icy dust particles sublime when they reach the sublimation temperature of water ice, i.e. 100 K in vacuum. This effectively cuts off the inner disk at an inner radius of ~35 AU.

3.4. Fitting approach

Model images in each of the five Herschel bands were created using the radiative-transfer code MCMax (Min et al. 2009). The code was modified to allow for an eccentric belt, with the star in one of the foci. The model images are convolved with the measured PSF of the PACS and SPIRE instruments at each observational wavelength. PACS and SPIRE images are obtained in broad-band filters. It is therefore not correct to directly compare the monochromatic model images with the observations. We take the filter transmission into account by computing model images at three wavelengths within each of the PACS and SPIRE bands.

First, a Pearson chi-square, summed over all spatial pixels where the surface brightness is larger than 20σ, judges the goodness-of-fit. Two quantities are computed to assess the goodness-of-fit. For the ring where the planetesimals collide. We fixed the value of r₁ equal to the inner-edge radius of 133 AU that was well determined based on the HST images (Kalas et al. 2005). We also tested a slightly different r₁ of 123 and 143 AU. For the outer radius of the ring, we took r₂ = r₁ + [2, 5, 10, 20, 30, 40] AU. For the inner disk, we tested surface-density power laws proportional to r⁰ (PR), r⁻¹ and r⁻². The outer edge of the inner disk is set to the inner radius of the ring. On the inside, we assume that our icy dust particles sublime when they reach the sublimation temperature of water ice, i.e. 100 K in vacuum. This effectively cuts off the inner disk at an inner radius of ~35 AU.

Second, the maximum of the norm of the residuals is computed, providing the best possible fit to the 70 μm image, for each model in the grid.

Two quantities are computed to assess the goodness-of-fit. First, a Pearson chi-square, summed over all spatial pixels where the surface brightness is larger than 20σ, judges the goodness-of-fit. Second, the maximum of the norm of the residuals is computed, to control the most extreme deviation between model and observation. Similar values were determined for the Herschel images at longer wavelengths. While these images are not used in the NNLS fitting routine, the agreement between model and observations is checked a posteriori and taken into account to determine the best-fit model in the grid.

3.5. Best model

The best-fit model has a Pearson chi-square value, summed over all five images, of 0.42. The maximum pixel-to-pixel residual

Three wavelengths per band is sufficient to sample the smooth wavelength-dependence of the model within the band, while keeping the computational time limited.
occurs in the 250 μm image, where it amounts to 24% of the maximum surface brightness of the observation. The model images and residuals are shown in Fig. 3. The general accordance between model and observations is very good. The most significant residual structure is seen in the 250 μm image, where the belt appears to be more extended than the model predicts.

The best model has a debris source ring located between \( r_1 = 133 \text{ AU} \) and \( r_2 = 153 \text{ AU} \). The belt contains a total mass of \( 8 \times 10^{25} \text{ g} \) in dust grains up to sizes of 5000 μm. The replenishment time, determining the amount of blow-out grains present in the system, is very short, approximately 1700 yr, leading to a total mass of \( 3 \times 10^{24} \text{ g} \) in grains with sizes below 13 μm. The inner disk contains \( 4 \times 10^{23} \text{ g} \) of dust grains, and is responsible for 21–29% of the flux in the Herschel images (Table 3). Its surface density increases outward, linear with \( r \), to the inner radius of the ring. The central unresolved excess-emission component has an integrated flux that amounts to 50% of that of the star at 70 μm (Table 3).

The grain properties that best fit the SED and images are icy grains with a vacuum fraction of 25% by volume. However, we find little difference in total dust mass in blow-out grains - and hence in replenishment time- between models with different grain properties. This was to be expected: The key physical parameter that determines the thermal and dynamical properties of the dust particle is not the size, but the absorption efficiency. The grain model merely couples the absorption efficiency to a specific grain size, which is different for e.g. a different degree of porosity. Although grain models link different grain sizes to a similar absorption efficiency, it is this latter quantity that determines the appearance of the model. We conclude there is a significant amount of mass contained in grains with sizes smaller than the blow-out size in the Fomalhaut system. This conclusion is robust against assumptions for the grain structure and composition.

4. Results

4.1. Hot excess emission

Excess emission close to the star has been reported at near-infrared wavelengths (Absil et al. 2009). The SED of our model shows that the emission from the inner disk and belt only becomes visible at wavelengths beyond 20 μm. Closer inspection of the literature photometry shows that there is indeed a continuous excess above the stellar photospheric flux in the near- to mid-infrared wavelength range. In Fig. 6, the SED of this excess is shown. The PACS 70 μm photometric data point of the on-star excess is added. The error bars include the measurement uncertainties as listed in the different catalogues, but also the spread induced by uncertainties in the stellar model flux (typically 2% at these wavelengths). We note that we have integrated the stellar spectrum within each of the photometric filters before computing the residual excess flux, i.e., the excess SED is not affected by a spurious color correction.

The spectral shape of the excess cannot be represented by a single-temperature blackbody. This could point to the presence of hot dust that is not confined to a narrow asteroid belt, but is distributed over a range of distances close to the star (<20 AU). Alternatively, the excess may also be due to emitting gas. The slope of the excess emission is \( F_\nu \propto \nu^{0.8\pm0.1} \), close to the \( \nu^{0.6} \) behavior expected for free-free emission from a spherical wind with constant outflow velocity around a hot star, as derived by Panagia & Felli (1975). Using their Eq. (24), a reasonable stellar mass-loss rate of \( 10^{-8} M_\odot \text{ yr}^{-1} \) is computed for Fomalhaut. Although Absil et al. (2009) rejected free-free emission as the origin of the near-infrared excess based on the absence of an emission component or variability in the Hα line, our determination of the slope of the SED may revive the discussion on the origin of the excess. Further analysis is however beyond the scope of this paper.

4.2. Cometary debris

The temperature of the particles in the belt, ranging from 40 K to 100 K in our model, together with their now known location, requires the presence of particles with the absorption characteristics of small grains with sizes below the blow-out size. Paradoxically, HST imaging showed that the dust grains in the belt only scatter a very small fraction of the stellar light they receive into our line of sight (Kalas et al. 2005). This was interpreted as being due to the highly anisotropic scattering of compact particles larger than 100 μm (Min et al. 2010). Very small compact particles, which have the required absorption properties to fit the temperature of the belt in our images, are incompatible with this very low scattering efficiency. Vice versa, the thermal properties of large compact 100 μm particles are inconsistent with the observed thermal emission in the far-infrared.

To match both the scattered light images and our thermal infrared images, we need grains that absorb and emit like small grains, but scatter like large particles. We suggest here that this combination is characteristic of fluffy aggregates, similar to cometary interplanetary dust particles in our solar system (Fraundorf et al. 1982). Such aggregates behave in many aspects as loosely bound collections of small monomers, and thus can have the absorption properties of small grains, while exhibiting the scattering anisotropy expected from large particles (Volten et al. 2007). The resulting highly anisotropic scattering ensures that most of the light is not scattered into our line of sight, giving the particles a very low apparent scattering cross section.

Le Bouquin et al. (2009) have resolved the stellar rotation axis using near-infrared interferometry. Based on the orbital direction of Fomalhaut b (i.e., counterclockwise), they argue that the eastern side of the belt is in fact the far side. This side is the bright side in scattered light, and hence the authors conclude that the particles are predominantly backsaccattering, an observation
that was elaborated upon by Min et al. (2010). However, two assumptions are crucial in the determination of the belt orientation. First, Fomalhaut b must be a real planet in orbit. Second, the rotation axis of the planet’s orbit and of the star must have the same direction, i.e., the planet must have a prograde orbit. If Fomalhaut b is not a planet (and there is reason for skepticism, see Janson et al. 2012), the far side of the belt cannot be determined from the available observations. If the planet is real, but has a retrograde orbit, the orientation is reversed, and the bright side would be the nearest side of the belt. In the latter case, the particles would be predominantly forward scattering.

Apart from these considerations on the orientation of the Fomalhaut system, our “fluffy aggregate” suggestion is consistent with both forward and backward scattering, or at least not in conflict with either one. Large aggregates have the scattering properties of large grains, with a strong diffraction spike outside of the observable range of scattering angles ($\theta \notin [90^\circ - i = 25^\circ, 90^\circ + i = 155^\circ]$). Most of the stellar light would be scattered forward, but in a direction close to the plane of the belt. Whether the belt is dominated by backward or forward scattering at the observable scattering angles, would then depend on the specific scattering properties of the building blocks of the fluffy aggregate. Our suggestion does exclude large compact grains, because these grains do not have the thermal properties needed to explain the far-infrared Herschel images and the SED.

Fluffy aggregates have been invoked to explain the observed polarization properties of the debris disk around AU Mic (Graham et al. 2007). Here we used a different method to come to a similar conclusion on the morphology of the dust grains in the Fomalhaut system.

### 4.3. Mass loss in the belt

The amount of blow-out particles needed to reproduce the images (Fig. 3) and the SED (Fig. 5) can be directly converted into a mass-loss rate from the belt and, equivalently, to a dust production rate assuming a steady state. We find a mass-loss rate of $2 \times 10^{13}$ g yr$^{-1}$, corresponding to about two 10-km sized comets, or 2000 1-km-sized comets per day.

We can further estimate the total number of comets in the ring required to generate such a high collision rate. Assuming that the ring ranges from $r_1 = 133$ AU to $r_2 = 153$ AU and has a normalized half-height $h = H/(2r)$, its volume is $V = \frac{4}{3} \pi h (r_2^3 - r_1^3)$. The collision rate in the belt is then given by $N_c \rho_c \sigma_v \beta_s$, where $N_c$ is the number of comets in the belt, $\rho_c$ is the relative velocity between comets, and $\sigma_v = 4\pi r_c^2$ is the collisional cross section of two comets with radius $r_c$. Each collision destroys two comets with mass $\frac{\pi}{2} \rho_c v^2$, where $\rho_c$ is the specific density of a comet. The mass-loss rate is then $\frac{dM}{dt} = 16\pi^2 N_c^2 \rho_c v^2 r_c^5 / 3V$.

We take $h = 0.1$, $v_c \approx h_{\text{orb}} = 0.5$ km s$^{-1}$ (Dominik & Decin 2003), and $\rho_c = 0.6$ g cm$^{-3}$ (Britt et al. 2006), and find that a population of $2.6 \times 10^{11}$ 10-km-sized comets, or $8.3 \times 10^{13}$ 1-km-sized comets are required in the ring to produce the observed collision rate. The Oort Cloud of the solar system contains an estimated $10^{12} - 10^{13}$ comets which presumably came from the planetary system (Weissman 1991), so these numbers are not unreasonable. The total mass of the Fomalhaut belt is about 110 Earth masses, which can be compared to the approximately 30 Earth masses required in the primordial Kuiper belt to allow for the formation of Pluto and other trans-Neptunian dwarf planets (Stern 1996).

Interestingly, we find the same mass in Fomalhaut’s belt if we extrapolate the size distribution from the largest grains in our model (5000 $\mu$m) to the cometary regime, providing a second independent measurement of the same quantity. Crowding of planetesimals into a narrow belt through resonance capture by an outward-migrating planet can conceivably produce belts with high planetesimal content, and may have happened in our own solar system’s Kuiper belt during Neptune’s migration (Hahn & Malhotra 1999). Large amounts of mass in the outer regions of disks around A-type stars like Fomalhaut might explain the existence of planets found far away from the host star (Kalas et al. 2008; Marois et al. 2008), as in-situ planet formation could then have been possible.

### 5. Conclusion

The belt around Fomalhaut is a prototypical example of a steady-state collisional cascade. The high mass in blow-out grains evidences the extreme activity of the system. The dust particles are fluffy aggregates, similar in morphology to the cometary interplanetary dust particles in our solar system. This indicates that the planetesimals at the top of the collisional cascade are in fact comets.


### Appendix A: Particle size and surface density distribution in the inner disk

Here we compute the size distribution of dust grains in the inner disk under the assumption that these grains are moving inward due to Poynting-Robertson (PR) drag, and that no collisions occur in the PR stream inward of the source region. Because the absolute scaling (i.e., total dust mass) is determined by the fitting routine (see Sect. 3), we only consider the proportionality of the different processes.

We assume that the ring itself is in collisional equilibrium, so that the lifetime of particles is dominated by collisions for all bound particles. Even then, there will be a narrow slice close to the inner boundary of the ring where the time scale for a particle to move out of the ring by PR drag is shorter than its collisional destruction time scale. We assume that the particle flux seeping into the inner disk is proportional to the number of particles of a given size in that slice. Note that the width of this slice depends on grain size.

In the collisional ring itself, we assume that the size distribution is given by $f(s) \propto s^{\alpha}$, where $\alpha = -3.5$ in case of collisional equilibrium. First, we estimate the collisional time scale for particles of size $s$. The most important collision partners are grains with sizes near $s$, in a size range $\Delta s \propto s$ (Dominik & Decin 2003). If $v_c$ is the collision velocity and $\sigma_c$ is the collisional cross section, we see that the collisional time scales as $t_{\text{coll}} \propto (f(s) s \sigma_c)^{-1}$. We assume that $v_c$ is independent of grain size, i.e., particles with different sizes have similar orbits. Because $\sigma_c \propto s^2$, we find that $t_{\text{coll}} \propto s^{-(1+\alpha)}$.

PR drag pulls particles out of the ring. The inward velocity due to PR drag at a distance $r$ from the star is $v_{\text{PR}} \propto \frac{r}{r^2} \propto \frac{\beta v}{s^{1+\alpha}} \propto \frac{1}{s^\beta}$, where $s$ is the radius of the radiation and gravitational forces on a grain of size $s$. At the inner radius $r_1$ of the ring, $v_{\text{PR}}(r_1) \propto \beta s$. We now assume that the particle flux through $r_1$ into the inner disk is proportional to the material available in the narrow slice $dr = v_{\text{PR}}(r_1) f(s)$, where the PR
time scale is shorter than the collisional time scale. The particle flux is then proportional to $F(s) \propto f(s) \sigma_{\text{des}}(s) \propto s^{3} \beta(s) \propto s^{-3}$. Mass conservation in the flow through the inner disk then gives the surface density $\Sigma(s) = \frac{F(s)}{\pi s^2}$, where we now have to consider that $\sigma_{\text{des}}$ is no longer evaluated at the inner radius of the ring, but changes proportional to $\Sigma(s)^{-1}$. We find that $\Sigma(s) \propto \frac{\beta(s)}{\pi s^3} = s^{-3}$. For an undisturbed PR flow, the surface density depends on the grain size, but not on the distance to the star. Based on this reasoning, we use a size distribution $f(s) \propto s^{-3}$ in the inner disk. Note, however, that in reality, the size distribution may be modified by interactions with a planetary system. Also other sources of dust, such as evaporating comets or an unresolved inner belt, would give rise to different size distributions.

References

Brugamger, D. A. G 1935, Annalen der Physik, 416, 636
Lawson, C. L., & Hanson, R. J. 1974, Solving least squares problems (Englewood Cliffs, NJ: Prentice Hall, Inc.)
Min, M., Dullemond, C. P., Kama, M., & Dominik, C. 2011, Icarus, 212, 416
Yamamura, I., Makita, S., Ikeda, N., et al. 2010, VizieR Online Data Catalog, 2298

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