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Constraining dark matter annihilation with the isotropic $\gamma$-ray background: Updated limits and future potential

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The nature of the isotropic $\gamma$-ray background (IGRB) measured by the Large Area Telescope (LAT) on the Fermi $\gamma$-ray space telescope (Fermi) remains partially unexplained. Non-negligible contributions may originate from extragalactic populations of unresolved sources such as blazars, star-forming galaxies or galactic millisecond pulsars. A recent prediction of the diffuse $\gamma$-ray emission from active galactic nuclei (AGN) with a large viewing angle with respect to the line of sight has demonstrated that this faint but numerous population is also expected to contribute significantly to the total IGRB intensity. A more exotic contribution to the IGRB invokes the pair annihilation of dark matter (DM) weakly interacting massive particles (WIMPs) into $\gamma$ rays. In this work, we evaluate the room left for galactic DM at high latitudes ($>10^\circ$) by including photons from both prompt emission and inverse Compton scattering, emphasizing the impact of the newly discovered contribution from misaligned AGN (MAGN) for such an analysis. Summing up all significant galactic and extragalactic components of the IGRB, we find that an improved understanding of the associated astrophysical uncertainties is still mandatory to put stringent bounds on thermally produced DM. On the other hand, we also demonstrate that the IGRB has the potential to be one of the most competitive future ways to test the DM WIMP hypothesis, once the present uncertainties are even slightly reduced. In fact, if MAGN contribute even at 90% of the maximal level consistent with our current understanding, thermally produced WIMPs would be severely constrained as DM candidates for masses up to several TeV.

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I. INTRODUCTION

The nature of dark matter (DM) remains one of the most intriguing mysteries in fundamental physics and cosmology. A viable investigation technique consists in the search for its stable annihilation products in the halo of galaxies, and in particular in the Milky Way. Making the common hypothesis for DM to consist of weakly interacting massive particles (WIMPs), one of the most promising indirect detection channels is through annihilation into $\gamma$ rays (see Ref. [1] for a recent review). Unprecedented $\gamma$-ray observations of diffuse emission and point sources by the Fermi-LAT [2] have stimulated the search for exotic components from DM annihilation in the Milky Way, in extragalactic nearby objects, as well as in cosmological structures [3–7]. The incontrovertible DM signature would be a $\gamma$-ray monochromatic line at energies around the WIMP mass. A recent analysis of Fermi-LAT data of the galactic center region has unveiled the feature of a narrow line close to 130 GeV [8–11], with an angular distribution consistent with the expectation for WIMP DM [1] and a statistical significance of at least 3σ after trials factor correction (in fact, more than 5σ when taking into account both spectral and spatial information of the incoming events [11]). While confirming this excess, the Fermi-LAT Collaboration finds that its significance is substantially reduced to a mere 1.6σ (albeit in somewhat different target regions) when considering a larger set of reprocessed data and a two-dimensional modeling of the energy dispersion [12,13]. The interpretation in terms of annihilating DM would in any case require the loop-suppressed direct annihilation into photons to be larger than typically expected for thermally produced

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DM, a fact that has already inspired considerable modeling efforts (see, e.g., the compilation in Refs. [1,14] for an overview). Only a larger exposure will allow us to finally settle possible issues concerning the statistical robustness and potential instrumental effects of the line feature; with the proposed new observation strategy for Fermi, recently positively reviewed by the collaboration, this could be achievable until the end of 2014 [14].

A faint γ-ray emission at high latitudes (|b| > 10°) has been measured by Fermi-LAT [15], showing a high degree of isotropy [16] and an energy spectrum compatible with a power law. Though its very nature is still unexplained, it is reasonable to believe it to be the superposition of (mainly) extragalactic unresolved point sources and, to a lesser extent, of astrophysical diffuse processes (see Ref. [17] and Sec. II for a detailed discussion). A possible contribution from DM annihilation, both from galactic and cosmological distances, can be hidden in this isotropic γ-ray background (IGRB) data as well [17–25]. Previous upper limits on the DM annihilation cross section from the IGRB [26–28] contribute between 10% and 100% to the IGRB intensity, depending on the astrophysical uncertainties involved. In the present paper, we extend and update the analysis in Ref. [17] by taking into account those new results on the isotropic diffuse flux predicted for misaligned AGN (MAGN) [26,27]. We find that the annihilation intensity of DM in the galactic halo may be severely constrained by the inclusion of this new diffuse astrophysical background, depending on the WIMP mass and on the annihilation channel considered.

In this context, it is worth noting that classical DM indirect detection targets like the galactic center or dwarf spheroidal galaxies, which currently result in the best available limits on DM annihilation [3,7,30–33], will at some point inevitably face fundamental limitations in the sense that even greatly increased statistics will not allow us to further improve those limits [1]. For ground-based telescopes, this is likely the case already for anything beyond the planned Cherenkov Telescope Array [34], while for future space-based missions there might be room for further improvement of the limits by up to one order of magnitude with respect to what can be expected by the end of the Fermi mission. Once the MAGN-related astrophysical uncertainties are under better control, the IGRB may thus well turn out to be the new driving force in setting ever more stringent limits on the DM annihilation rate.

The paper is organized as follows. In Sec. II we present the possible contributions to the IGRB and we discuss the relevance of unresolved extragalactic sources, notably MAGN. The expected galactic DM signal is described in Sec. III. The DM spectrum is made up by the prompt γ-ray component and photons from inverse Compton scattering (ICS) of electrons and positrons produced by DM annihilation. By subtracting the astrophysical components from the high latitudes γ-ray emission, in Sec. IV we derive upper limits on the DM annihilation cross section for several annihilation channels and under various assumptions for the MAGN contribution. We discuss the implications for DM indirect detection, as well as the dependence on the other possible astrophysical contributions. In Sec. V we present our conclusions.

II. DIFFUSE γ-RAY EMISSION FROM UNRESOLVED ASTROPHYSICAL SOURCES

The IGRB found at high latitudes (|b| > 10°) has been obtained by the Fermi-LAT Collaboration [15] after subtracting from the LAT data the contributions from pointlike sources, the galactic diffuse emission (which represents the major systematic uncertainty of that analysis), the background from CRs in the detector and solar photons. The energy spectrum of the IGRB is consistent with a power-law having spectral index \( \alpha = 2.41 \pm 0.05 \) and integrated intensity \( I(>100 \text{ MeV}) = (1.03 \pm 0.17) \times 10^{-5} \text{ cm}^{-2} \text{ s}^{-1} \text{ sr}^{-1} \). This diffuse emission likely arises from the superposition of several contributions from unresolved point-source populations, as well as from photons originating from truly diffuse processes (i.e., extended source contributions like from ultrahigh energy cosmic rays, nearby galaxy clusters or gravitationally induced shock waves during structure formation, see Ref. [17] and references therein). Most of the photons in the IGRB are believed to be of extragalactic origin. The truly diffuse processes are subdominant and may be non-negligible (% level) only at the high-energy end of the range explored by the Fermi-LAT. We have checked that the total UHECR diffuse emission predicted by [35] contributes to at most 0.3% of the measured IGRB. On the other side, the high energy (>100 GeV) emission from galaxy clusters predicted by [36] is \( O(10^{-2}) \) of the IGRB at 100 GeV. Given their very marginal role in the analysis undertaken here, they will be neglected from now on.

A. Misaligned AGN

Recently, a thorough analysis of the γ-ray flux from unresolved MAGN has demonstrated that this numerous but faint population may contribute between 10% and 100% to the measured IGRB [26,27]. A jet displacement of about 14° marks the separation between blazars and nonblazar (namely misaligned) AGN. In the unification model [37],

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1The 130 GeV feature described above does not show up in the IGRB—as expected for the annihilation rate of \( \langle \sigma v \rangle \sim 10^{-27} \text{ cm}^3 \text{ s}^{-1} \) inferred from the galactic center observation [6] (unless one adopts very optimistic models for the evolution and distribution of DM subhalos [29]).
radio galaxies are those misaligned active galaxies whose jet points on average at an angle \( > 44^\circ \), while lower angles indicate typically steep spectrum radio quasars. The result in Refs. [26,27] is based on the \( \gamma \)-ray data of 12 MAGN by Fermi-LAT, and is based on a correlation between their \( \gamma \)-ray and core radio luminosities. This correlation has been tested against the MAGN number count distribution, and validated by 95\% flux upper limits on the Fermi-LAT \( \gamma \)-ray data for a large sample of bright core radio MAGN. These results support the hypothesis that \( \gamma \)-ray photons are produced by synchrotron-self Compton scatterings by the same electrons responsible for the synchrotron emission at GHz frequencies. Ref. [26] quantifies several sources of uncertainty and estimates them to affect the diffuse emission from unresolved MAGN by about a factor of 10. The expected flux is therefore provided as a band (roughly decreasing with \( E^{-2.35} \)) affected by the extragalactic background light (EBL) absorption above 50 GeV. At 1 GeV, the MAGN flux (multiplied by \( E^2 \)) ranges from \( 6 \times 10^{-7} \) GeV cm\(^{-2}\) s\(^{-1}\) sr\(^{-1}\) to \( 5 \times 10^{-6} \) GeV cm\(^{-2}\) s\(^{-1}\) sr\(^{-1}\), while at 100 GeV the EBL absorption starts to be effective and the flux spans from \( 9 \times 10^{-9} \) GeV cm\(^{-2}\) s\(^{-1}\) sr\(^{-1}\) to \( 9 \times 10^{-8} \) GeV cm\(^{-2}\) s\(^{-1}\) sr\(^{-1}\). The result in Ref. [26] states that MAGN account for at least 10\% of the IGRB measured by Fermi-LAT [15] and can in principle explain most of it. Added to other possible diffuse emission components, this might almost close the room to an exotic diffuse contribution such as from DM annihilation in space. This point is the focus of our paper: evaluating how much the MAGN \( \gamma \)-ray diffuse emission constrains the presence of WIMP DM annihilating in the galactic halo. In the remainder of this section, we briefly discuss the astrophysical sources leading to a non-negligible diffuse \( \gamma \)-ray emission at \( |b| > 10^\circ \) (see Ref. [17] for further details).

B. Blazars

The census of the sources detected by the Fermi-LAT [38,39] indicates that the largest population is made by blazars, a class of AGN with their jet oriented along the l.o.s., thus leading to a significant observed \( \gamma \)-ray flux. The analysis of the spectral and statistical properties of the resolved Fermi-LAT blazars [40] shows that the unresolved counterpart is a sizable component, able to explain up to 20\%–30\% of the IGRB. The contribution from the two distinct populations of Flat Spectrum Radio Quasars (FSRQs) and BL Lacertae (BL Lacs) objects has been found to follow a power-law spectrum with respectively a somewhat softer (\( \alpha_{FSRQs} = 2.45 \pm 0.03 \)) and harder (\( \alpha_{BL\text{Lacs}} = 2.23 \pm 0.03 \)) spectral index. Recently, Ref. [41] has evaluated the FSRQ contribution to the diffuse \( \gamma \)-ray flux using a new determination of the spectral energy distribution and luminosity function. The resulting flux is predicted with an uncertainty of less than a factor of two. It represents no more than 10\% of the IGRB in the 0.1–100 GeV, and becomes negligible for E \( \gtrsim 20 \) GeV. Also, [42,43] find that the maximal contribution from blazars are about 10\% and 20\%, respectively.

C. Millisecond pulsars

The second-most abundant population of the Fermi-LAT sky is represented by galactic pulsars and Millisecond Pulsars (MSPs). It has been argued that the latter population may be brighter in \( \gamma \) rays than ordinary pulsars as a consequence of their rapid spin frequency [44]. Moreover, MSPs are expected to be more numerous at high latitudes, since they have typical ages that can largely exceed the oscillation time across the galactic disk [45]. The prediction of the diffuse \( \gamma \)-ray flux due to high latitudes (\( |b| > 10^\circ \)) unresolved MSPs is estimated to be about 10\% at \( \approx 3 \) GeV, where it reaches its maximum value due to the adopted broken power-law spectrum [17]. The considered model results to be compatible with the analysis of the \( \gamma \)-ray anisotropies performed in [16]. Indeed we derived the integrated flux from MSPs for \( |b| > 30^\circ \), which results to be 1.44\% and 1.11\% of the IGRB in the 1–2 GeV and 2–5 GeV, respectively. These numbers are compatible with the upper limits of about 1.5\% found by [16] in the anisotropy analysis. In the Second Fermi catalog [39] only about 20 MSPs at \( |b| > 10^\circ \) are listed, but the number of galactic (nonglobular cluster) MSPs has recently risen to 40 [46]. The statistical properties of such a population could improve the prediction for the unresolved component. Such an analysis is beyond the scope of the present paper, but is anyway not expected to modify any of the results and conclusions presented here. In the following, we refer to the unresolved MSPs diffuse \( \gamma \)-ray flux and its estimated uncertainty as reported in Ref. [17].

D. Star-forming galaxies

Though their number density is larger than that of the blazars, star-forming (SF) galaxies are more difficult to detect in \( \gamma \) rays because of their less intense luminosities. Based on three years of Fermi-LAT data, Ref. [47] analyzes a sample of 64 SF galaxies beyond the Local Group, detecting only four objects in \( \gamma \) rays: two are typical star-burst galaxies (M82 and NGC 253), while the other two host Seyfert 2 nuclei (NGC 1068, NGC 4945). None of the remaining 60 source candidates has shown an excess above the background. The contribution of SF galaxies to the IGRB is evaluated in Ref. [47] by exploiting the correlation between infrared and \( \gamma \)-ray luminosities [48]. In order to compute the diffuse emission, the differential photon flux of an individual galaxy has to be modeled. Given the lack of statistics, the \( \gamma \)-ray average spectral properties of SF galaxies are difficult to firmly establish, although differences in the spectra of quiescent and star-burst galaxies are expected to be present. To take into account this effect, Ref. [47] adopts two possible \( \gamma \)-ray spectra supposed to bracket the possible contribution from multiple types of SF galaxies. The first one refers to Milky Way-like SF galaxies (model MW), the second one assumes a power-law spectrum in agreement with the properties of the Fermi-LAT detected star-burst galaxies (model PL).
The predictions differ in particular above 5 GeV, where the MW model gets significantly softer. At 100 GeV the PL model overpredicts the MW one by one order of magnitude. The estimates span 4%–23% of the IGRB intensity above 100 MeV. Higher predictions, in particular in the low energy tail (not relevant in deriving the constraints on the DM annihilation cross section), have been obtained in [49,50]. As a summary of this section, we show in Fig. 1 the contributions to the IGRB discussed above, with uncertainty bands as reported in the relevant references (roughly corresponding to 1σ deviations). The Fermi-LAT IGRB data [15] are shown along with the power-law fit (solid black line). The solid dark-green curve refers to the expected diffuse γ-ray flux from unresolved MAGN [26], the light-green band bracketing the corresponding uncertainty. The other displayed components are: SF galaxies (the MW model is depicted by the dashed dark-blue line (area)), MSPs (dot-dashed red line and orange band), FSRQs (purple dotted line and pink band), and BL Lacs (dotted dark-grey line and light-grey band). The BL Lacs flux follows a power-law, while the specific shape of the FSRQ contribution is the result of a more recent, sophisticated analysis of their spectral energy distribution and luminosity function [41]. The crossing point for the two curves is around 1–2 GeV: above this energy the BL Lacs flux dominates over the one from FSRQs. The γ rays from unresolved MSPs show a peculiar spectrum peaked at about 1 GeV (resulting from the primary electron cooling due to curvature radiation) and dominate over the blazar spectra from 300 MeV up to 3–4 GeV. A similar low-energy bumped flux comes from the SF galaxies contribution. The MAGN is clearly the dominant component over the whole energy range (notice that for $E_\gamma \gtrsim 30$ GeV the BL Lacs flux is actually expected to drop in the same way as the MAGN flux, due to EBL absorption, but this has not been taken into account in the flux estimate referred to here). In the following, we define $\Sigma_{\text{BMS}}$ as the sum of the contributions from Blazars (both BL Lacs and FSRQs), MSPs and SF galaxies.

In Fig. 2 we display a few representative choices for the astrophysical backgrounds, as a function of the photon energy. The solid blue (red dashed) line corresponds to the minimal (best fit) prediction for all the contributions. The green short-dashed (brown dotted) curve has been obtained from the sum of the best fit models for $\Sigma_{\text{BMS}}$ and the 60% (85%) of the maximally expected flux from MAGN. Data points are again for the IGRB [15].

III. DIFFUSE γ-RAY EMISSION FROM DARK MATTER IN THE GALACTIC HALO

The self-annihilation of DM particle pairs in the haloes of galaxies may give birth, among other species, to γ rays. The intensity of these energetic photons depends on the elementary process at stake and on the spatial distribution of DM. The flux $\Phi_\gamma(E_\gamma,\psi)$ of γ rays produced by WIMP pair annihilation in the angular direction $\psi$ is given by [51–53]:

![Graph showing the predicted diffuse γ-ray fluxes for various unresolved point-source populations.](image-url)
\[ \Phi(E_g, \psi) = \frac{1}{4\pi} \frac{\langle \sigma v \rangle}{m_p^2} \frac{dN_\gamma}{dE_g} I(\psi), \]  
(1)

where \( m_p \) is the WIMP mass. The factor \( \langle \sigma v \rangle \) defines the annihilation cross section times the relative velocity, averaged over the galactic velocity distribution function, while \( dN_\gamma/dE_g \) is the \( \gamma \)-ray production source spectrum per DM annihilation event. The last term \( I(\psi) \) is the integral performed along the l.o.s. of the squared DM density distribution:

\[ I(\psi) = \int_{\text{l.o.s.}} \rho^2(r(\lambda, \psi)) d\lambda. \]  
(2)

Here \( \psi \) is the angle between the l.o.s. and the direction towards the galactic center, defined as a function of the galactic latitude \( b \) and longitude \( l \) (\( \cos \psi = \cos b \cos \lambda \)). When comparing with experimental data, Eq. (2) must be averaged over the telescope viewing solid angle, \( \Delta\Omega \):

\[ I_{\Delta\Omega} = \frac{1}{\Delta\Omega} \int_{\Delta\Omega} I(\psi(b, l)) d\Omega. \]  
(3)

The photon spectrum \( dN_\gamma/dE_g \) depends on the elementary processes ruling the annihilation. For the continuum \( \gamma \)-ray flux, we consider here i) prompt emission, where the photons are found in final-state showers or hadronic decays of the annihilation products, and ii) ICS by energetic electrons and positrons—produced in the same way—off the interstellar radiation field (ISRF). We have calculated the spectrum for the prompt emission of both photons and \( e^\pm \) with the PYTHIA MONTE CARLO code (version 8.162) [54]. The ICS has been computed from those \( e^\pm \) interacting with ambient photons, following the prescription in [55]. Once produced, energetic electrons may diffuse due to stochastic scatterings on galactic magnetic field inhomogeneities, and lose energy through interactions with the ISRF. The ISRF is composed by the Cosmic Microwave Background (CMB) photons, the infrared radiation (IR) produced by the absorption and the subsequent reemission of starlight by the galactic dust, and by the starlight (SL) originating from stars of the Galactic disk. Given the energies at stake, galactic diffusion may be safely neglected and only energy losses have been included, as usually assumed in the literature [56]. Electromagnetic energy losses are treated here in the fully relativistic Klein-Nishina regime. The photon density distribution has been assumed as an average field with different normalizations for different sky regions (the SL and IR are concentrated along the galactic disk), following Ref. [55]. Specifically, between 10° and 20° all the three fields (CMB, IR, SL) are present, while for latitudes \( |b| > 20° \) only CMB remains. Energy losses due to synchrotron radiation have been taken into account in the region of latitude 10° < \( |b| < 20° \), with a value of \( B = 2 \mu G \) for the galactic magnetic field, and neglected above \( |b| > 20° \) given the very low intensity of \( B \) at high latitudes [57–60]. Switching off the synchrotron radiation would increase the ICS \( \gamma \)-ray flux from DM by less than 30%, resulting in a decrease of the upper limits on \( \langle \sigma v \rangle \) (shown in the following Sect. IV) by 10%.

Numerical cold DM simulations predict cuspy density distribution in the inner parts of galaxies, like the Navarro-Frenk-White (NFW) [61] or Einasto [62] profile. Following a conservative approach, however, we evaluate the geometrical factor \( I(\psi) \) in Eq. (2) by adopting the cored Burkert model [63] for the radial DM density distribution, which is used as an alternative parameterization to fit observed rotation curves [64]:

\[ \rho(r) = \frac{\rho_s}{(1 + (r/r_s)^2)^2(1 + r^2/r_s^4)}. \]  
(4)

We note that numerical simulations typically support more cuspy profiles and our choice is thus exclusively motivated by that fact that it results in rather conservative limits on a DM contribution to the IGRB. The values of \( r_s \) and \( \rho_s \) have been derived fixing the local DM density \( \rho(r = r_\odot) = 0.4 \text{ GeV cm}^{-3} [65,66] (r_\odot = 8.33 \text{ kpc}) \) and fitting the halo DM mass \( M(r < r_0) \) contained within a certain radius \( r_0 \). Using available \( M(r < r_0) \) data for different values of \( r_0 \) [67–75], roughly in the range 20 kpc \( \lesssim r_0 \lesssim 300 \) kpc, we find a best fit value of \( r_s = 15 \) kpc. Numerically, we derive for \( I_{\Delta\Omega} \) in Eq. (3): 2.4, 1.9, 1.7, 2.0 (in units of \( \text{GeV}^2 \text{ cm}^{-6} \text{ kpc}^{-1} \)) for the sky regions 10° < \( |b| < 20° \), 20° < \( |b| < 90° \), \( |b| > 60° \), and \( |b| > 10° \), respectively. While in principle limits might somewhat improve when taking into account the different values of \( I_{\Delta\Omega} \) for different regions of the sky, we will in the following only consider the whole region \( |b| > 10° \) considered by the Fermi-LAT analysis [15] because not all of the astrophysical contributions quoted above can be easily rescaled to smaller subregions. We also note that when integrating Eq. (2) around the galactic center, different DM distributions \( \rho(r) \) may lead to very different results. However, since we study here only high latitude regions, the various models for \( \rho(r) \) give comparable values for \( I(\psi) \), and the uncertainty due to DM density modeling is rather small. For example, we find \( I_{\Delta\Omega}(|b| > 10°) \times \text{GeV}^{-2} \text{ cm}^6 \text{ kpc}^{-1} = 2.4 (2.5, 2.8) \) for the case of an isothermal sphere (a NFW [61], an Einasto [62]) profile. While the existence of a dark disk [76] may further enhance those values slightly, we will not consider this possibility in the following. We also do not include any contribution from subhaloes, which are predicted in numerical simulations of cosmological structure formation [77,78], and assume a smooth distribution of DM in the galactic halo for the sake of deriving conservative limits. Including the effect of substructures leads to an increase of the geometrical factor in Eq. (3), see e.g. Ref. [79], which would accordingly lower the upper limits we are going to present on \( \langle \sigma v \rangle \).
IV. CONSTRAINTS ON DARK MATTER ANNIHILATION INTO $\gamma$ RAYS

The constraints on DM are set, as usual, in terms of the velocity averaged annihilation cross section into $\gamma$ rays ($\langle \sigma v \rangle$) as a function of the WIMP mass $m_\chi$. All the other quantities in Eq. (1) are kept fixed. The galactic DM contribution is calculated following the prescriptions outlined in Sec. III. We do not include the diffuse $\gamma$-ray flux from DM in extragalactic structures [80,81], given the large model dependence on the assumed DM (sub-)halo profiles and their evolution. If the $\gamma$ rays from DM in extragalactic structures or subhaloes in the Milky Way halo were added to our fluxes, the ensuing upper limits on $\langle \sigma v \rangle$ would be further decreased. In these regards, the results we are going to present are meant to be conservative, i.e. leading to the highest possible value for the excluded $\langle \sigma v \rangle$.

As discussed in Sec. III, the geometrical factor at high latitudes is very slightly affected by modeling uncertainties. The choice we made on the Burkert profile and a smooth halo is meant to be conservative and different assumptions on the DM profile would lower the upper bounds we find by up to about 30% (in fact, considerably more for optimistic assumptions about DM substructure [80–82]).

A further uncertainty factor is the value of the local DM density, which can span the (generous) range 0.2–0.7 GeV cm$^{-3}$ [66]. Since $\rho_\odot$ enters squared in the flux, it has a non-negligible impact on the $\langle \sigma v \rangle$ bounds. If not explicitly stated differently, we will take $\rho_\odot = 0.4$ GeV cm$^{-3}$ in the following. To keep the analysis as model independent as possible, we will show our results assuming that DM annihilation proceeds via a single channel (branching ratio equal to one), studying separately the effect of each final state leading to $\gamma$-ray production.

Finally, we derive conservative limits on $\langle \sigma v \rangle$ by requiring that the total gamma-ray flux does not exceed any of the Fermi-LAT data points [15] by more than $\sigma$, which is a commonly adopted practice for this kind of constraints (see e.g. Ref. [6]). Our limits are thus set by the maximal $\langle \sigma v \rangle$ value for which $\Phi_i^{\mathrm{ex}} \leq \Phi_i^{\exp} + n \times \Delta(\Phi_i^{\exp})$ in all energy bins $i$, where $\Phi_i^{\exp}$ is the sum of the DM and astrophysical background fluxes in a given bin $i$, and $\Phi_i^{\exp}$ is the experimental data with error $\Delta(\Phi_i^{\exp})$. Given the one-sided nature of the limit, a $2\sigma$ ($3\sigma$) upper limit from the intensity data points thus nominally corresponds to a confidence level of 97.7% (99.9%). We typically quote $2\sigma$ limits—except for the case of a large MAGN contribution, e.g. the brown dotted line in Fig. 2, where we will instead consider the more conservative limits resulting from the requirement that no data point is exceeded by more than $3\sigma$.2

2Note that in such a situation, where the signal must obviously be very small, the upper limit on $\langle \sigma v \rangle$ that is inferred from an analysis like ours may be anomalously low (e.g. if the data “fluctuate very low relative to the expectation of the background-only hypothesis” [83]). For a general introduction to this problem, see Sec. 36.3.2.2 of the Particle Data Group review [83], or Ref. [84,85] for more details.

FIG. 3 (color online). Conservative $2\sigma$ upper limits on the velocity averaged DM annihilation cross section $\langle \sigma v \rangle$ into $e^\pm$ final states, as a function of the WIMP mass $m_\chi$. The blue dashed curve corresponds to the $\gamma$-ray spectrum from the prompt component only, the solid red line refers to the inclusion of ICS. The grey area indicates the typically adopted value for the cross section of thermally produced WIMPs, $\langle \sigma v \rangle \sim 3 \times 10^{-26}$ cm$^3$ s$^{-1}$.

As can be anticipated from Fig. 1, those limits are always set by the three data bins at 6.4–12.8, 12.8–25.6 and 25.6–51.2 GeV.

Fig. 3 represents the exclusion plot for DM annihilation into $e^\pm$ and it is emblematic of the effect of the ICS inclusion in the DM spectrum. The blue dashed curve corresponds to upper limits on $\langle \sigma v \rangle$ when the DM induced spectrum originates only from the prompt $\gamma$-ray component, while the solid red line refers to the inclusion of ICS. The astrophysical background is set to the minimal choice illustrated in Fig. 2. The effect of ICS inclusion starts to be important for high energies, i.e. at high DM masses, and the deviation from the prompt only limits reaches about two orders of magnitude at $\sim 10$ TeV. We notice that the uncertainties from ICS are small at the energies at which it is effective. For comparison, we also indicate in the same plot the “thermal” cross section of $\langle \sigma v \rangle \sim 3 \times 10^{-26}$ cm$^3$ s$^{-1}$ that results in the correct DM relic density in the simplest WIMP scenarios (i.e. velocity-independent annihilation and no coannihilations with other particles close in mass to the WIMP).

In Fig. 4 we study the effect of the various astrophysical backgrounds described in Sect. II on the room left for a possible DM contribution to the diffuse $\gamma$-ray flux, studying in particular the effect of MAGN and SF galaxies. The annihilation channel is fixed to $b\bar{b}$. In the left panel, we study the impact of the previously neglected MAGN component by fixing $\Sigma_{\text{BMS}}$ to the minimally allowed value: by increasing the MAGN contribution from its minimal to 70% of its maximally expected value [26], limits on a possible DM contribution could be improved by at least one order of magnitude compared to the most conservative assumptions concerning the astrophysical contributions.
The right panel of Fig. 4, on the other hand, demonstrates that the uncertainty in the flux from other astrophysical backgrounds generally has a less significant impact on the final limits. Here, we fix $\Sigma_{\text{BMS}}$ at the minimal level compatible with the expectations and vary the contribution from MAGN from the minimal to 70% of the maximally expected level. The right panel shows the impact of various choices for $\Sigma_{\text{BMS}}$ on the limits, fixing the MAGN contribution to the best-fit value derived in Ref. [26]. The constant line at $3 \times 10^{-26}$ cm$^3$ s$^{-1}$ represents the “thermal” cross section of DM in the simplest WIMP models.

(note that setting the $\gamma$-ray flux from MAGN to the maximally allowed value would actually overshoot the Fermi data by more than $2\sigma$).

The right panel of Fig. 4, on the other hand, demonstrates that the uncertainty in the flux from other astrophysical backgrounds generally has a less significant impact on the final limits. Here, we fix the MAGN contribution to its best-fit value [26] and vary $\Sigma_{\text{BMS}}$ from its minimally to maximally predicted contribution as described in Section II. We also show that the choice of the underlying SF galaxy model introduces a certain systematic uncertainty: depending on the WIMP mass, the resulting limits are up to a factor of $\sim 3$ stronger for the PL than for the MW model (unless $\Sigma_{\text{BMS}}$ only contributes at the minimal level, in which case there is no difference because the MAGN contribution always dominates).

In Fig. 5, we show the effect of the MAGN contribution for various DM annihilation channels. In the top left panel, we present our most conservative limits, derived by fixing the background to the minimal scenario (see Fig. 2). For $b\bar{b}$, $\mu^+\mu^-$ and $\tau^+\tau^-$ final states, and DM masses below $\sim 100$ GeV, they are comparable with the limits previously derived in Ref. [17], where a similar modeling of the astrophysical background was considered; for $m_\chi > 100$ GeV the inclusion of ICS becomes important and consequently significantly improves our new limits with respect to those for leptonic channels. The right panel shows a more realistic scenario, where we take all astrophysical backgrounds to contribute at their expected best-fit values (dashed red curve in Fig. 2). Compared to the conservative case, this shifts down the upper bounds by a factor of roughly 2.

In the lower panels of Fig. 5, we take a more optimistic approach in order to illustrate the full potential of using the IGRB to constrain galactic DM annihilation. Assuming MAGN to contribute at 60% of the maximal flux (high background 1, corresponding to the short-dashed green curve in Fig. 2), for example, would result in limits that clearly start to approach the “thermal” cross section of $\langle \sigma v \rangle \sim 3 \times 10^{-26}$ cm$^3$ s$^{-1}$). Moving to the possibility of even higher levels for the MAGN contribution, we note that one quickly reaches a situation where already a small increase in the MAGN flux has an enormous impact on the allowed DM contribution—simply because the astrophysical backgrounds are already extremely close to the IGRB data points (with $2\sigma$ errors). In this limit, the validity of our method to obtain upper bounds clearly breaks down and a more sophisticated statistical treatment would be needed. In order to illustrate that one may still potentially be able to constrain the “thermal” annihilation rate up to DM masses of several TeV, we show in the bottom right panel of Fig. 5 the limits that result for an assumed MAGN contribution at 85% of the maximally predicted flux (high background 2, corresponding to the dotted brown curve in Fig. 2). Note that those limits were derived by requiring that no data point is exceeded by more than $3\sigma$, rather than $2\sigma$, in order to (partially) meet the above concerns.

Let us stress in passing that the inclusion of ICS $\gamma$ rays is particularly relevant for large DM masses ($m_\chi > 1$ TeV). This is the mass range which—for leptonic final states [86–89]—could in principle contribute to the observed rise in the cosmic ray positron fraction [90–92]. Our results strongly disfavor a DM candidate annihilating mainly into $e^+e^-$ with $\langle \sigma v \rangle > 0.3 (1) \times 10^{-26}$ cm$^3$ s$^{-1}$ for masses of about 1–3 (10) TeV. A bit looser constraints are obtained for annihilation into muons or tau leptons, the latter roughly at the level which is required to fit the AMS-02 data [87,89]. Assuming a relatively large MAGN contribution,
like e.g. in the scenario displayed in the bottom-left panel of Fig. 5, the IGRB would thus allow us to firmly rule out a DM explanation of the rising positron fraction. The non-inclusion of the EBL absorption for the BL Lac population might have some effect only in the minimal background scenario. From [93], one can estimate that the $\gamma$-ray flux at 80 GeV (the highest Fermi-LAT energy, see Figs. 1 and 2) for a population at $z = 0.5 (1)$ is reduced by 20(50)% from the source to the Earth. The upper limits on $<\sigma v>$ would therefore be modified by a negligible factor, and only for the highest masses shown in our plots (constrained indeed by the highest experimental data).

As already mentioned, our results improve the limits derived in Ref. [17] at DM masses above $\sim$100 GeV due to the inclusion of ICS; the best-fit scenario displayed in Fig. 5 strengthens those limits further by a factor of $\sim$2 due to the contribution from MAGN. Our constraints for high masses are significantly stronger than those obtained from the ICS contribution alone in an analysis of preliminary Fermi data [55], and stronger by an overall factor of roughly 4 (for $b\bar{b}$) compared to those obtained for the analysis of 1y IGRB data in a smaller sky region than considered here [96]. Compared to the Fermi analysis of possible galactic DM contributions to the IGRB [3], with no background modeling, our conservative limits are comparable for $b\bar{b}$ and $\tau^+\tau^-$ final states (for $m_\chi \gtrsim 20$ GeV). Very similar (projected) limits are also found in an independent analysis [24], which however tends to find slightly more stringent constraints on TeV DM models than Ref. [3]. The adopted background modeling in the Fermi analysis [3], on the other hand, leads to bounds comparable with our MAGN best fit choice for $m_\chi \sim 100$ GeV; for higher masses $m_\chi \gtrsim 1$ TeV, the bounds in the MAGN best fit case are a factor of roughly 3 stronger.

Let us finally remark that the bounds on $<\sigma v>$ we have derived here are consistent with constraints from different...
targets in the sky obtained with very different astrophysical backgrounds and measurement systematics. In particular, our “optimistic” limits on the DM annihilation cross section—assuming an MAGN flux which is 60% of its maximal theoretical prediction—are generally competitive with the bounds from the joint likelihood analysis of 10 dwarf spheroidal galaxies [7]. In fact, for TeV masses and leptonic final states, our constraints are at least comparable even under the conservative assumption of a minimal MAGN contribution (though one should note that for such large DM masses, galactic center constraints are typically even stronger [94]). We also obtain comparable results at low masses with bounds on leptonic channels from radio emission [95], which in turn depend significantly on astrophysical and cosmological assumptions. At masses $m_x \gtrsim 100$ GeV our bounds from $\gamma$ rays are stronger, independently of the amount of MAGN included in the background. Finally, our conservative constraints are stronger than those obtained from galaxy cluster [5,96] and CMB observations [97].

V. CONCLUSIONS

In this work, we have considered the contribution of annihilating galactic DM to the IGRB and presented an updated calculation of the resulting upper bounds on the DM annihilation cross section $\langle \sigma v \rangle$. In deriving these bounds, we took into account both prompt and ICS emission for DM-induced $\gamma$ rays. For the astrophysical $\gamma$-ray background, we included all relevant contributions at their minimally expected level, in particular the contribution from unresolved MAGN that has been pointed out only very recently. Given that we only consider high galactic latitudes, our results are very robust and barely depend on the choice of DM density profile (apart from an overall normalization corresponding to the local DM density, which may either strengthen or weaken those bounds by a factor of at most 3). Let us stress that our bounds are very conservative in that they do not include the expected—and potentially very sizable—effect from DM substructures at galactic or extragalactic distances.

The resulting IGRB bounds on $\langle \sigma v \rangle$ are still competitive with, or more stringent than, limits from radio data, CMB or galaxy cluster observations. In particular, our results—along with stringent limits from antiproton data [98–100]—strongly disfavor a DM-based explanation of the unexpected rise in the cosmic ray positron fraction at high energies that was recently confirmed by AMS-02 [92], at least if MAGN do not contribute at the most minimal level currently allowed. The main reason for this is the sizable ICS emission in $\gamma$ rays that is induced by the high annihilation rate into leptonic channels required to fit the positron data.

Even more importantly, we have demonstrated that there is significant room for future improvement of limits on the DM annihilation rate derived from the IGRB. In fact, under the optimistic (though by no means unrealistic) assumption that the astrophysical processes considered here contribute more or less at the maximal level consistent with our present understanding, a “thermal” value of $3 \times 10^{-26}$ cm$^3$ s$^{-1}$ for the annihilation cross section could be excluded up to DM masses of several TeV. Notably, such a limit will be impossible to reach even for far-future ground-based observations of point or extended sources like dwarf galaxies or the galactic center. Even for space-based observations of dwarf galaxies, which presently set the most robust and stringent bounds of this kind, it will be extremely challenging for extended future missions to probe thermally produced DM for such large masses.

The most important contribution to the IGRB originates from unresolved MAGN, which we have included here for the first time in the context of putting limits on DM annihilation. In order to actually exploit the great potential of the IGRB discussed above, a reduction of the relatively large theoretical uncertainty on the diffuse $\gamma$-ray flux from unresolved MAGN is thus mandatory. In particular, one would need several tens of detected MAGN in $\gamma$ rays to be able to directly determine their $\gamma$-ray luminosity function (which is presently derived from radio observations); this goal is well in reach for Fermi-LAT and next generation $\gamma$-ray telescopes. At some point, also an improved understanding of the other astrophysical contributions will help to push limits further down—especially if one can develop the underlying modeling to a level that allows us to predict those contributions not only as an all-sky average but as a function of the viewing angle. Given the expected significantly increased statistics for future IGRB observations, finally, chances are good that the IGRB will turn out to be one of the most efficient future means of probing thermally produced DM.

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