Towards the architectures of macromolecules: Modeling of multi-dimensional polymer chain distributions
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TOWARDS THE ARCHITECTURES OF MACROMOLECULES
Modeling of Multi-Dimensional Polymer Chain Distributions

NAZILA YAGHINI
TOWARDS THE ARCHITECTURES OF MACROMOLECULES
MODELING OF MULTI-DIMENSIONAL POLYMER CHAIN DISTRIBUTIONS

ACADEMISCH PROEFSCHRIFT

ter verkrijging van de graad van doctor aan de Universiteit van Amsterdam
op gezag van de Rector Magnificus prof. dr. D.C. van den Boom
ten overstaan van een door het College voor Promoties ingestelde commissie,
in het openbaar te verdedigen in de Agnietenkapel

op dinsdag 24 maart 2015, te 14:00 uur

door

Nazila Yaghini
geboren te Tabriz, Iran
Promotiecommissie

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The research presented in this thesis was carried out at the Van ’t Hoff Institute for Molecular Sciences, University of Amsterdam with the financial support from Marie Curie Actions (initial training network, Nanopoly PITN-GA-2009-238700) and Dutch Polymer Institute, P.O.Box 902, 5600 AX Eindhoven, project # 674.
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