**SmB$_6$ electron-phonon coupling constant from time- and angle-resolved photoelectron spectroscopy**


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SmB$_6$ is a mixed valence Kondo system resulting from the hybridization between localized $f$ electrons and delocalized $d$ electrons. We have investigated its out-of-equilibrium electron dynamics by means of time- and angle-resolved photoelectron spectroscopy. The transient electronic population above the Fermi level can be described by a time-dependent Fermi-Dirac distribution. By solving a two-temperature model that well reproduces the relaxation dynamics of the effective electronic temperature, we estimate the electron-phonon coupling constant $\lambda$ to range from 0.13 $\pm$ 0.03 to 0.04 $\pm$ 0.01. These extremes are obtained assuming a coupling of the electrons with either a phonon mode at 10 or 19 meV. A realistic value of the average phonon energy will give an actual value of $\lambda$ within this range. Our results provide an experimental report on the material-electron-phonon coupling, contributing to both the electronic transport and the macroscopic thermodynamic properties of SmB$_6$.

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The electronic transport properties of SmB$_6$ have been the subject of intense studies since the first report of its mixed valence nature [1] and the observation of a Kondo gap opening when cooling below $T_K \sim 50$ K [2]. This Kondo gap opens as a result of the interaction between the delocalized $d$ electrons and the $f$ electrons acting as localized magnetic impurities [3]. Despite the observation of a gap opening at the Fermi level by spectroscopic measurements, transport experiments show signs of residual conductivity [4]. The origin of this residual conductivity has puzzled the scientific community until the recent discovery of low-temperature metallic surface states [5], of potential, albeit debated, topological character [6–14].

The advent of topological insulators (TIs) has fueled the fast development of time- and angle-resolved photoelectron spectroscopy (tr-ARPES) [15–21]. This technique has been successfully exploited to access the unoccupied electronic states [22–24], as well as the temporal evolution of both the chemical potential ($\mu$) and the electronic temperature ($T_e$) after optical excitation [16–19].

In this Rapid Communication we report on the out-of-equilibrium electronic properties of SmB$_6$, as revealed by tr-ARPES. This study is motivated by the possibility to address the scattering mechanisms in SmB$_6$, as similarly reported for Bi-based binary TIs [15,16,18–20]. Ishida and co-workers have pioneered this out-of-equilibrium approach to the study of SmB$_6$, reporting a shift of the chemical potential ($\Delta \mu$) lasting up to hundreds of $\mu$s after optical excitation, for $T < T_K$ [25]. By assessing the out-of-equilibrium dynamics of $T_e$, here we provide insights on the temporal evolution of the time-dependent Fermi-Dirac (FD) distribution. A minimal two-temperature model (2TM) is applied to mimic the relaxation dynamics of $T_e$. By considering a coupling to phonon energies corresponding to the lowest-energy Sm modes at 10 meV [26,27] or 19 [28] to 20 meV [27], we estimate an interval for the possible values of the electron-phonon coupling constant $\lambda$: 0.13 $\pm$ 0.03 to 0.04 $\pm$ 0.01. This range is mostly determined by the fact that among the phonon modes detected for this material, those derived from the B$_6$ cage, i.e., those at energies $>20$ meV, weakly contribute. This finding can be of relevance to account for the details of the electronic transport and thermodynamical properties of SmB$_6$ [29].

In addition to the temporal evolution of the FD function, we reveal a difference in the effect of the optical excitation on the $d$ and $f$ states. In particular, the depletion of intensity which follows the optical excitation is mainly located in the $f$ bands. The electrons, which are excited in the $f$ state above the Fermi level ($E_F$), successively relax towards $E_F$ where intensity is observed over a broad momentum range. This suggests the transient population of empty $f$ states above $E_F$ [30].

Here, tr-ARPES experiments are performed at the T-ReX Laboratory, Elettra (Trieste, Italy); more details about the setup can be found in Refs. [17,31]. The photoelectrons are collected and analyzed by a SPECS Phoibos 225 hemispherical spectrometer, with energy and angular resolution set in the present experiment to 30 meV and 0.2° [17], respectively. The overall temporal resolution is equal to 250 fs. In the following, two data sets are analyzed with an absorbed fluence equal to 120 $\pm$ 25 and 75 $\pm$ 15 $\mu$J/cm$^2$, corresponding to an absorbed energy density equal to 30 $\pm$ 6 and 19 $\pm$ 4 J/cm$^3$, calculated by considering a penetration depth of 40 nm, as estimated from optical studies [32]. For the calculation of the absorbed fluence and energy density, a reflectivity $R = 0.5$ has been considered [32].
Single crystals of SmB$_6$ are grown via the optical floating zone technique, as described in Ref. [33]. They are cleaved in UHV at room temperature and transferred to a variable temperature cryostat. Measurements are performed at an equilibrium temperature of $\sim$120 K. At this temperature the Kondo gap is fully closed and the material transport properties are metallic, a condition necessary for the use of a 2TM.

SmB$_6$ crystallizes in the CsCl-type structure with $Pm\bar{3}m$ point group symmetry and lattice constant $a = 4.13$ Å. Sm atoms and a B$_6$ cage occupy the corners and the body-centered position of the cubic cell, as depicted in Fig. 1(a). Sample cleavage exposes the (001) surface, and the corresponding projected surface Brillouin zone is shown in Fig. 1(b). The tr-ARPES measurements have been carried out along the $\bar{\Gamma}X$ high symmetry direction, in the region indicated by the gray rectangle. The $d$ bands are expected to cross $E_F$ within this momentum window, as illustrated by the green dashed lines schematizing the $d$-band contour [7–11,13].

Figure 1(c) shows the band structure at $\sim$500 fs before optical excitation. Two nondispersive bands, traced by white dashed lines, are identified and attributed to the Sm $4f$-state multiplets $^6H_{7/2}$ and $^6H_{5/2}$ at binding energies of $\sim$0.035 and $\sim$0.180 eV, respectively. These flat states intersect a highly dispersive band derived from the Sm $d$ orbitals, indicated by a dashed green line, crossing $E_F$ at $k_F \sim 0.35$ Å$^{-1}$. The intensity of this state is found to be highly suppressed in $s$ polarization, in agreement with the literature [9,13].

The momentum distribution curve (MDC) integrated in the energy window $E - E_F = 10 \pm 10$ meV[inset of Fig. 1(c)] shows the $d$-state peak, whose width is comparable with synchrotron-based measurements performed at higher photon energies (30–70 eV). The dispersion of the $d$ band resembles results obtained for $k_x$ far from the bulk high symmetry directions [9]. This is in agreement with our estimated $k_z \sim 2.7\pi/a$.

Figure 1(d) shows the modification of the electronic properties after optical excitation, for the highest absorbed energy density, resulting from the difference between the ARPES data 300 fs after and 500 fs before the arrival of the optical excitation. The color scale indicates with red (blue) the positive (negative) signal variation. The first noticeable feature, which characterizes the out-of-equilibrium electronic properties of SmB$_6$, is the different response of the two sets of bands to the optical excitation. A depletion of intensity (blue) is visible in the two nondispersive $f$ states, whereas it is not observed along the dispersive $d$ band. We ascribe this effect to the higher density of states (DOS) of the $f$ state, which seems to dominate the optical absorption processes.

Since the experiments are performed at $T > T_K$ and $E_F$ is crossed by the dispersive $d$ band, we expect the material response to the optical excitation to be metallic. Hence, at short time scales immediately after optical excitation, electrons thermalize due to electron-electron scattering and relax towards $E_F$ where their distribution is described by a time-dependent FD function [15–17,34–36]. This process is assumed to occur within the pump pulse duration [35,36]. Figure 1(d) shows that, after thermalization, electrons occupy a broad momentum region above $E_F$, thus suggesting the possible existence of unoccupied nondispersing $f$-like states above $E_F$ [30]. The aim of our work is to evaluate the electron-phonon coupling constant from the temporal evolution of $T_e$, thus in the following we will focus only on the out-of-equilibrium dynamics of the time-dependent effective FD distribution, without entering in the details of the dispersion of the unoccupied states.

In order to estimate the time scale over which the electronic temperature relaxes, we now turn our attention to the temporal evolution of the ARPES signal. Figure 1(e) shows the temporal evolution of the change in photoemission intensity integrated along the dashed green line in Fig. 1(d). In order...
to quantitatively describe the characteristic relaxation times. The inset shows a zoom at $E_F$ of the EDCs at $-400$ and $+300$ fs.

Region 1 (orange), at $E - E_F \sim 0.125$ eV, is characterized by a peak whose relaxation dynamics is comparable to our experimental temporal resolution. This prevents us from accessing the fast electronic dynamics responsible for the thermalization processes. At energies closer to $E_F$ the dynamics slows down, as expected in a thermalized electron system [17,21]. The intensity relaxes to a plateau value larger than the equilibrium one. The full relaxation of the excited population is obtained through a second relaxation channel, having a time scale exceeding that achievable by the present experiment. From a single exponential fit to the traces, we observe that the relaxation dynamics in proximity of $E_F$ has the same characteristic time $\tau = 800 \pm 50$ fs both above (region 2, brown) and below (region 3, light blue) $E_F$. This points to the fact that the dynamics is dominated by the thermal broadening of the FD distribution. The positive dynamics of region 4 (green), between the $f$ multiplets, is delayed, and we ascribe this finding to a thermal broadening of the $f$ states, rather than a purely electronic effect. This point will be clarified later within the frame of the 2TM.

In order to evaluate the evolution of the electronic temperature $T_e$, as well as of the chemical potential shift $\Delta \mu$, we fit a time-dependent FD function to the energy distribution curves (EDCs) extracted from Fig. 1(e) for all the delay times. Figure 2(b) shows selected EDCs at $-400$, $+300$, $+2000$, and $+5300$ fs, vertically offset for clarity, along with the corresponding fits (black dashed lines). The broadening of the FD distribution is more clearly visible in the inset, which shows a zoom at $E_F$ of the two EDCs at $-400$ and $+300$ fs. The fitting function results from the convolution of a Gaussian function, accounting for the experimental energy resolution, with the result of the product of a time-dependent FD distribution and a function describing the density of states [16]. In the present study, the latter is the sum of two Lorentzian components for the $f$ multiplets in the occupied density of states, at $-19 \pm 4$ eV, and a constant accounting for the DOS of the $d$ band. In performing the fit of the experimental EDCs, we only let $T_e$ and $\Delta \mu$ vary with time. The reason for letting free only two fitting parameters is phenomenological: The parameters in the density-of-states function, when allowed to vary, do not produce an improvement of the $\chi^2$ of the fit.

Figures 3(a) and 3(b) show the dynamics of $\Delta \mu$ and $T_e$, respectively. Results are reported for both data sets, with excitation energy densities equal to $30 \pm 6$ J/cm$^3$ (black) and $19 \pm 4$ J/cm$^3$ (green). After optical excitation, both $\Delta \mu$ and $T_e$ relax with a single exponential behavior, with a
similar characteristic excitation time $\tau = 800 \pm 50$ fs. The values of $\Delta \mu$ are small but comparable with the previous work of Ishida et al. [25]. However, we point out that in the present study we are not sensitive to the surface photovoltage effect which is expected to slow the $\Delta \mu$ relaxation dynamics for $T < T_K$ [25]. The fact that the relaxation of $T_e$ is well mimicked by a single decaying exponential justifies the choice of a minimal 2TM for extracting $\lambda$. The evolution of the electron and lattice temperatures ($T_i$) is described by the following rate equations [36,37]:

$$\frac{\partial T_e}{\partial t} = \frac{S(t)}{C_e} - \frac{3\lambda \Omega^3 (n_e - n_l)}{\hbar \pi k_b^2 T_e}, \quad (1)$$

$$\frac{\partial T_i}{\partial t} = \frac{C_i}{C_l} \frac{3\lambda \Omega^3 (n_e - n_l)}{\hbar \pi k_b^2 T_e}. \quad (2)$$

$S(t)$ describes the optical excitation with a Gaussian profile and absorbed energy density equal to $\sim 30 \pm 6$ and $\sim 19 \pm 41 \text{J/cm}^2$, respectively. The error bar associated with the energy density propagates into an error bar on the free fitting parameters in the 2TM, including $\lambda$, $\Omega$ corresponds to the phonon frequency.

From optics, neutron scattering, and symmetry analysis we expect only phonon modes at 10 meV (acoustic) [26,27], 19–20 meV [27,28] ($T_{19}$), and three higher energies vibrational and rotational modes of the B$_6$ cage at 89.6 meV ($T_{25}$) and 141.7 meV ($E_S$) and 158.3 meV ($A_{1g}$) [26]. In the Eliashberg formalism, $\lambda$ results from the coupling of all the phonon modes, where the contribution from each mode is divided by its phonon energy. For this reason we expect the coupling to the high-energy $B_6$ modes to be weak. This hypothesis is well supported by analogy with the calculations performed on a similar compound, YF$_6$, which show that the electron-phonon coupling constant $\lambda$ is dominated by the low-energy $Y$ phonon modes, while the high-energy phonons associated with the $B_6$ modes only weakly contribute to $\lambda$ [38].

For these reasons, we have performed our analysis by considering the coupling to the low-energy Sm modes at 10 meV [26,27] and 19 [28] to 20 meV [27], respectively. $k_b$ is the Boltzmann constant and $n_e$ and $n_l$ are the Bose-Einstein (BE) distribution functions for phonons calculated at temperatures $T_e$ and $T_l$, respectively. In the model we assumed a particular form for the electron-phonon coupling, i.e., $\alpha^2 F(\omega) \propto \delta(\omega - \Omega)$, but no approximations are applied to the BE statistics. This is because the measured electronic temperature is not high enough to justify the commonly used “high-temperature” approximation of the BE statistics [37].

The lattice specific heat $C_l$ for a lattice base temperature of 120 K (110 K for 19 $\pm 4$ J/cm$^3$) is taken from Ref. [29], while the electronic specific heat is $C_e = \gamma T_e$, with $\gamma$ left free to vary as well as $\lambda$.

The best fit to $T_e$ is shown by the continuous and dashed red lines in Fig. 3(b), for the two excitation energy densities, respectively, whereas blue lines indicate the dynamics of $T_l$. The electronic and lattice temperatures equilibrate after approximately 2 ps, and $T_i$ is expected to recover its equilibrium value through lattice heat diffusion on time scales longer than the temporal window of our measurements [36]. The 2TM well reproduces the evolution of $T_e$, thus indicating that mechanisms, such as electronic heat diffusion, do not need to be taken into account for the case of the bad metal SmB$_6$, in contrast to conventional metals such as Ru(001) [39] and Gd(0001) [40]. The increase in $T_l$ accounts for the long lasting plateau observed in the dynamics across $E_F$ in regions 2 and 3 in Fig. 2(a). The increase in $T_l$ is delayed with respect to the optical excitation, as it turns out from the 2TM. This suggests a possible interpretation for the negative dynamics of region 4 in Fig. 2(a), whose maximum is reached at a later time than that of the other regions, as a consequence of thermal broadening of the $f$ multiplets due to the larger $T_i$. From the model we estimate a value of $\gamma$ equal to 5.8 $\pm$ 1.5 $\text{meV/mol K}^2$, in good agreement with the literature, where values of 7 $\text{meV/mol K}^2$ [41] and 2 $\text{meV/mol K}^2$ [42] are found.

Finally, an important result of our analysis is the evaluation of the electron-phonon coupling constant. From the 2TM, by considering the coupling dominated by the low-energy Sm phonons, either with $\Omega = 10 \text{meV}$ [26,27] or $\Omega = 19 \text{meV}$ [28] to 20 meV [27], we obtain a value of $\lambda \Omega^2$ equal to 130 $\pm$ 30 or 270 $\pm$ 70 $\text{meV}^3$, respectively. From these we extract two extreme values for $\lambda$ equal to 0.13 $\pm$ 0.03 and 0.04 $\pm$ 0.01. We can conclude that, for a realistic value of the average phonon energy between 10 and 19–20 meV, depending on the phonon density of states, $\lambda$ will lie between 0.13 $\pm$ 0.03 and 0.04 $\pm$ 0.01. Unfortunately, no theoretical or experimental estimations of $\lambda$ are available for SmB$_6$ in the literature. From a comparison with different hexaborides, we note that the range in which $\lambda$ falls for SmB$_6$ is slightly lower than those reported for LaB$_6$ ($\lambda = 0.17$–0.26 [43]), MgB$_6$ ($\lambda = 0.39$ [44]), and YB$_6$ ($\lambda = 0.86$ [45]).

Our estimation of $\lambda$ provides an insight into a fundamental physical property of SmB$_6$. The slightly smaller value, compared to other hexaborides, might reflect an intrinsic difference in the electron-phonon coupling. Nonetheless, it might also be ascribed to the fact that tr-ARPES is momentum selective. We point out that the $\lambda$ value is evaluated along the $\Gamma X$ high symmetry direction, and far from the zone boundary, owing to the small momentum window accessible with the available photon energy. We believe that our results represent a reference for future momentum integrated measurements of $\lambda$ that might extend further the comparison between the electron-phonon coupling in different hexaboride compounds.

In conclusion, we have exploited tr-ARPES to investigate the out-of-equilibrium electronic properties of SmB$_6$. After optical excitation, electrons are transferred predominantly from the localized $f$ multiplets to the unoccupied density of states. After thermalization, electrons can be described by a time-dependent Fermi-Dirac distribution. The temporal evolution of the electronic temperature is described within a minimal two-temperature model. The phonon density of states is unknown for SmB$_6$, hence we can establish a range of values for $\lambda$. By assuming that the electron-phonon coupling, along the $\Gamma X$ direction of the surface BZ, is preferentially mediated by the two lowest-energy Sm modes at 10 meV [26,27] or 19 [28] to 20 meV [27], we estimate $\lambda$ to fall in the range 0.13 $\pm$ 0.03 to 0.04 $\pm$ 0.01.

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