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### On the nature of heavy-fermion behaviour and high-field dilatation experiments

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To the memory of my mother

