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Self-Organization of Vegetation in Arid Ecosystems

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Vegetation in arid regions of Africa, America, Australia, and Asia reveals remarkable patterns, such as spotted vegetation, labyrinths, gap patterns, and regular bands (Bromley et al. 1997; Aguiar and Sala 1999; Klausmeier 1999; Leprun 1999; Couteron and Lejeune 2001; Von Hardenberg et al. 2001). Here, the term “arid” refers to environments characterized by an extended dry season, where yearly potential evaporation exceeds yearly rainfall, and where plant growth is limited by water availability. The two-phase mosaics of vegetation alternating with bare soil as observed in arid ecosystems differ in scale and shape, depending on slope gradient and rainfall. When slope gradient is $\leq 0.2\%$ and mean annual rainfall ranges from 200 to 550 mm yr$^{-1}$, observed vegetation patterns include spots with a diameter of 5–20 m, labyrinths with a vegetated band width of 10–50 m (fig. 1a), and gap patterns with bare spots in the vegetation with a diameter of 5–20 m (fig. 1b; Bromley et al. 1997; Aguiar and Sala 1999; Ludwig et al. 1999b; Valentin et al. 1999; Couteron and Lejeune 2001). On slopes steeper than 0.2% in arid regions, typical regular-banded vegetation patterns with a band width in the range of a few tens of meters are observed (Klausmeier 1999; Leprun 1999; Valentin et al. 1999; d’Herbes et al. 2001).

Scientists are still searching for possible unifying mechanisms to explain this range of spatial patterns (Tongway and Ludwig 2001), and an important question of this research is whether this range is the result of preexisting environmental heterogeneity, the result of spatial self-organization, or both (Klausmeier 1999; Couteron and Lejeune 2001; HilleRisLambers et al. 2001; Von Hardenberg et al. 2001). Here, we contribute to the ongoing debate about vegetation pattern formation in arid ecosystems by presenting novel, spatially explicit model analyses and results, extending on the work of HilleRisLambers et al. (2001). Our results show that these different vegetation patterns observed in arid ecosystems might all be the result of spatial self-organization, caused by one single mechanism: water infiltrates faster into vegetated ground than into bare soil, leading to net displacement of surface water to vegetated patches. This model differs from earlier model results (Klausmeier 1999; Couteron and Lejeune 2001; HilleRisLambers et al. 2001; Von Hardenberg et al. 2001).
primarily in two ways: it is fully mechanistic, and it treats the lateral flow of water above and below the soil as separate, not independent, variables. Although the current model greatly simplifies the biophysics of arid systems, it can reproduce the whole range of distinctive vegetation patterns as observed in arid ecosystems, indicating that the proposed mechanism might be generally applicable. We further show that self-organized vegetation patterns can persist far into regions of high aridity, where plants would become extinct if homogeneously distributed, pointing to the importance of this mechanism for maintaining productivity of arid ecosystems (Noy-Meir 1973).

Our analyses are based on the model first developed in HilleRisLambers et al. (2001), which we now briefly review. Vegetation patterning is generally linked to the mechanism by which plants increase surface-water infiltration into the soil, in combination with low annual rainfall conditions (Bromley et al. 1997; Klausmeier 1999; Leprun 1999; Ludwig et al. 1999a; HilleRisLambers et al. 2001). During rain showers, some rainwater will infiltrate into the soil, while the remainder will run off as surface water to other areas. With increasing plant density, the rate of infiltration of surface water into the soil will asymptotically approach a maximum (Rietkerk and van de Koppel 1997). Lateral flow of surface water is due to pressure differences measured by the slope of the thickness of the surface-water layer and can be described with a single diffusion term (Bear and Verruut 1990; HilleRisLambers et al. 2001). Part of the infiltrated soil water subsequently evaporates or moves out of reach of plant roots by drainage and lateral subsurface flow due to capillary forces (Hills 1971; Lawrence Dingman 1994). Soil water uptake and plant growth are both assumed to be saturation functions of soil-water availability (de Wit 1958; Rietkerk et al. 1997). Plant dispersal, through seed or vegetative propagation, is approximated by a diffusion term (Okubo 1989; Cain 1990; HilleRisLambers et al. 2001).

The model is a set of three partial differential equations describing the dynamics of three state variables: plant density (P; \( \text{g m}^{-2} \)), soil water (W; mm), and surface water (O; mm). The full model reads

\[
\begin{align*}
\frac{\partial P}{\partial t} &= c \times g_{\text{max}} \times \frac{W}{W + k_1} \times P - d \times P + D_p \Delta P, \\
\frac{\partial W}{\partial t} &= \alpha \times \frac{P + k_2 \times W_0}{P + k_2} - g_{\text{max}} \times \frac{W}{W + k_1} \\
&\quad \times P - r_w \times W + D_s \Delta W, \\
\frac{\partial O}{\partial t} &= R - \alpha \times \frac{P + k_2 \times W_0}{P + k_2} + D_o \Delta O,
\end{align*}
\]

where \( c \) (g mm\(^{-1}\) m\(^{-2}\)) is the conversion of water uptake by plants to plant growth, \( g_{\text{max}} \) (mm g\(^{-1}\) m\(^{-2}\) d\(^{-1}\)) is the maximum specific water uptake, \( k_1 \) (mm) is a half-saturation constant of specific plant growth and water uptake, \( d \) (d\(^{-1}\)) is the specific loss of plant density due to mortality, \( D_p \) (m\(^2\) d\(^{-1}\)) is plant dispersal, \( \alpha \) (d\(^{-1}\)) is the maximum infiltration rate, \( k_2 \) (g m\(^{-2}\)) is the saturation constant of water infiltration, \( W_0 \) (—) is the water infiltration rate in the absence of plants, \( r_w \) (d\(^{-1}\)) is the specific soil water loss due to evaporation and drainage, \( D_s \) (m\(^2\) d\(^{-1}\)) is the diffusion coefficient for soil water, \( R \) (mm d\(^{-1}\)) is rainfall, and \( D_o \) (m\(^2\) d\(^{-1}\)) is the diffusion coefficient for surface water (HilleRisLambers et al. 2001). Plausible parameters were obtained from the literature and were set as follows: \( c = 10, g_{\text{max}} = 0.05, k_1 = 5, D_p = 0.1, \alpha = 0.2, k_2 = 5, W_0 = 0.2, r_w = 0.2, D_s = 0.1, D_o = 100, d \) ranges between 0 and 0.5, and \( R \) ranges between 0 and 3 (Hills 1971; Oborny and Cain 1997; Rietkerk et al. 1997; Klausmeier 1999; HilleRisLambers et al. 2001). A Laplacian operator was added for diffusion. We extended the original model in case of a slope by replacing the diffusion term \( D_o \Delta O \) with \( v \partial O / \partial x \) (eq. [1c]), in which \( v \) is the downhill

![Figure 1: Aerial photographs from patterned vegetation in Niger (S. Prince, personal communication.) Scale is 400 × 400 m. a, Labyrinths with spots; b, gap pattern.](image-url)
flow that is set to 10 m d$^{-1}$. The two-dimensional numerical simulations were forward Euler integrations of the finite-difference equations resulting from discretization of the diffusion operator. The spatial mesh consisted of a rectangular grid of 200 $\times$ 200 elements with reflecting boundary conditions. Simulations were started by introducing random plant peaks in 1% of the grid elements, which were all set in the plantless equilibrium of $W = R/r_w$ and $O = R/(\alpha W_0)$. For the one-dimensional analysis, the bifurcation analysis program Content (Kuznetsov and Levitin 1997) was used.

The typical spatial patterns on flat ground that are generated by our model are revealed in a two-dimensional domain representing 400 $\times$ 400 m for different amounts of rainfall. For $R = 0.75$ mm d$^{-1}$, a spotted pattern is formed (fig. 2a), changing into labyrinths with spots for $R = 1.0$ (fig. 2b); a gap pattern is generated for $R = 1.25$ (fig. 2c). In the long run, both spots and gaps arrange themselves in a regular hexagonal pattern. On slopes, where surface water flows in one direction, the model generates regular vegetation bands, moving slowly uphill (fig. 2d).

In a one-dimensional analysis, we now demonstrate how the various patterns are interlinked and how they originate from the spatially homogeneous equilibrium. We also illustrate that self-organized vegetation patterns can persist far into regions of high aridity, where plants would become extinct if homogeneously distributed.

The model allows for a homogeneous equilibrium of plant density, soil water, and surface water. With decreasing rainfall, the homogeneous plant equilibrium decreases until plants become extinct for $R \leq 1.0$ (fig. 3a). Close to this extinction threshold, the homogeneous plant equilibrium is unstable against small spatial perturbations. This is indicative of the principle of pattern formation as first outlined by Turing (Turing 1952): pattern formation can occur if an equilibrium is stable to spatially homogeneous perturbations but unstable to heterogeneous perturbations. From the Turing instability points unstable nonhomogeneous equilibria originate which link up to a stable nonhomogeneous equilibrium. This stable nonhomogeneous equilibrium, which is characterized by a single plant peak (fig. 3b), exists for a wide range of rainfall rates, and

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Figure 2: Spatial patterns for different amounts of rainfall ($R$) after $t = 3,000$ d. Scale is 400 $\times$ 400 m. Plant mortality, $d$, is 0.25, with other parameters set at default values (see text). Plants are represented by dark green and bare soil by light brown. An animation of this model output is available on the on-line edition of The American Naturalist as an appendix. a, Spotted pattern, $R = 0.75$; b, labyrinths with spots, $R = 1.0$; c, gap pattern, $R = 1.25$; d, regular bands on slope (top on right-hand side; periodic boundary conditions), $R = 1.0$. 

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extends far into the region where homogeneous plant cover would go extinct \((R \leq 1.0)\). In general, the pattern formation leads to higher average plant productivity as compared to the homogeneous situation (cf. green and blue lines in fig. 3a). For a small rainfall range on the right-hand side of the Turing instability, the opposite is true. Here, a local gap in the plant cover is amplified (fig. 3c), leading to lower average plant productivity as compared with the homogeneous situation.

The predicted Turing instability region and limit points of spatial patterns can be plotted as a function of rainfall and plant mortality (fig. 4). The rainfall range for which spatial patterns are predicted widens with increasing plant mortality. The predicted patterns in the two-dimensional domain correspond to these distinct regions. Toward the upper limit of spatial patterns, a spotted pattern is formed (fig. 2a). A profile through a single spot closely resembles figure 3b. Moving away from the upper limit of spatial patterns toward the Turing instability region, labyrinths with spots are formed (fig. 2b). Within the Turing instability region and moving toward its lower limit, this pattern gradually changes into labyrinths with gaps. Beyond the lower limit of Turing instability, a gap pattern is generated (fig. 2c). A profile through a single gap closely resembles figure 3c.

We have demonstrated that the current model can adequately reproduce the whole range of distinctive vegetation patterns as observed in arid ecosystems, based on the net displacement of surface water to vegetated patches. In case of flat ground, the forms of the patterns generated by our model coincide with those found by Von Hardenberg et al. (2001); however, the scale of the patterns as well as the mechanism generating the patterns are different. The scale of the vegetation patterns generated by the current model is in the range of meters or a few tens of meters, while the scale of the patterns found by Von Hardenberg et al. (2001) is of the order of centimeters. This is due to the fact that our model takes the lateral flow of soil water as well as the lateral displacement of surface water into account, while Von Hardenberg et al. (2001) only consider transport of water in the soil, leading to

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**Figure 3:** a, Bifurcation diagram based on a one-dimensional model for a spatial range of 50 m. Plant mortality, \(d\), is 0.25, with other parameters as defaults (see text). Spatially homogeneous equilibria are in blue, nonhomogeneous equilibria are in red (showing maximum local plant densities). Solid lines denote stable equilibria, whereas dotted lines are unstable equilibria. The green line depicts the average plant density in the stable nonhomogeneous equilibrium. \(T_1\) \((R = 1.001)\) and \(T_2\) \((R = 1.259)\) are Turing instability points, and \(LP_1\) \((R = 0.557)\) and \(LP_2\) \((R = 1.312)\) are limit points. b, Profile of stable plant peak at \(R = 0.75\). Plant density in red, surface water in blue, and soil water in green. c, Profile of stable plant gap at \(R = 1.25\); lines as for b.
similar vegetation patterns but at a much finer spatial scale. This observation is of fundamental importance, reflecting spatial self-organization with respect to water resources at multiple scales, that is, at the scale of centimeters with respect to soil-water redistribution and at the scale of meters or a few tens of meters with respect to redistribution of surface water. Similar patterns on flat ground on the scale of a few tens of meters were also generated by a generic, single-variable vegetation model, based on the general premise that competitive interactions occur over a larger spatial scale than facilitative ones (Couteron and Lejeune 2001). Unlike this phenomenological model, our model explicitly incorporates the water dynamics thought to be responsible for vegetation pattern formation in arid ecosystems. Therefore, our results can be interpreted and evaluated in terms of parameters that have clear biophysical meanings. In case of a slope, our model results of patterns generated coincide with model results earlier reported (Klausmeier 1999) and strongly mimic observed patterns.

Our model predictions elucidate how rainfall and plant mortality may affect the types of patterns that are generated (fig. 4). Plant mortality in arid vegetation is greatly affected by shifts in grazing intensity. Grazing by livestock is the principal land use in arid ecosystems. Increased grazing by domestic livestock in the African Sahel and New Mexico, for instance, has led to greater exposure of bare soil, increased soil compaction and erosion by surface water runoff, and asymmetrical distribution of water and nutrients, creating patterned vegetation structures (Wood et al. 1987; Schlesinger et al. 1996; van de Koppel et al. 1997; Rietkerk et al. 2000). The finding that apparent homogeneous grazing (if the spatial heterogeneity of grazing is weak relative to the spatial heterogeneity of the vegetation) generates patterned vegetation structures appears typical of arid systems characterized by strong plant-soil feedbacks (Adler et al. 2001).

Water infiltration in sandy soils is usually higher than in clayey and silty ones, particularly if the latter is crust-forming. Thus, a higher water infiltration in the absence of plants (the parameter $W_0$ in our model) corresponds to sandy soils, whereas low water infiltration corresponds to silty and clayey soils. The parameter range for which spatial patterns are predicted narrows for higher values of water infiltration (not shown), so we predict that patterns tend to develop more frequently on fine-textured than on sandy soils.

The prevalence of social insect activities in arid ecosystems may also trigger more or less regular gap patterns in vegetation, that is, “termitaria-peppering” (Macfadyen 1950), through competitive interactions among colonies. However, we showed that this type of pattern (fig. 2c) may be the strict outcome of differential water availability.

In arid systems, large interannual rainfall fluctuations are strongly associated with the El Niño/Southern Oscillation phenomenon, triggering an increase in plant cover during wet years and a decrease or even desertification during droughts (Holmgren and Scheffer 2001; Holmgren et al. 2001). Vegetation structures may disintegrate and lose their natural water-harvesting function during recurring droughts, as the decrease of plant growth leads to overgrazing and vegetation collapse (Rietkerk and van de Koppel 1997; Rietkerk et al. 1997; van de Koppel et al. 2002). This in turn leads to export of water through overland flow or gully formation, resulting in desertification. Preserving the self-organized vegetation patterns during droughts and stimulating their recovery during wet years by adequate grazing management (Rietkerk et al. 1997; Holmgren and Scheffer 2001) might be crucial for maintaining productivity in arid ecosystems.

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