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Quantifiers in TIME and SPACE : computational complexity of generalized quantifiers in natural language

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