A Sample of Low-energy Bursts from FRB 121102

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Abstract

We present 41 bursts from the first repeating fast radio burst (FRB) discovered (FRB 121102). A deep search has allowed us to probe unprecedentedly low burst energies during two consecutive observations (separated by one day) using the Arecibo telescope at 1.4 GHz. The bursts are generally detected in less than one-third of the 580 MHz observing bandwidth, demonstrating that narrowband FRB signals may be more common than previously thought. We show that the bursts are likely faint versions of previously reported multi-component bursts. There is a striking lack of bursts detected below 1.35 GHz and simultaneous Very Large Array observations at 3 GHz did not detect any of the 41 bursts, but did detect one that was not seen with Arecibo, suggesting preferred radio emission frequencies that vary with epoch. A power-law approximation of the cumulative distribution of burst energies yields an index −1.8 ± 0.3, which is much steeper than the previously reported value of −0.7. The discrepancy may be evidence for a more complex energy distribution. We place constraints on the possibility that the associated persistent radio source is generated by the emission of many faint bursts (~700 ms⁻¹). We do not see a connection between burst fluence and wait time. The distribution of wait times follows a log-normal distribution centered around ~200 s; however, some bursts have wait times below 1 s and as short as 26 ms, which is consistent with previous reports of a bimodal distribution. We caution against exclusively integrating over the full observing band during FRB searches, because this can lower signal to noise.

Key words: galaxies: dwarf – methods: observational – radiation mechanisms: non-thermal – radio continuum: general

1. Introduction

Fast radio bursts (FRBs) are bright (peak flux density 0.01–100 Jy), millisecond-duration radio pulses of extragalactic origin (Thornton et al. 2013). The physical source of FRBs has been a mystery since the first example was discovered over 10 years ago (Lorimer et al. 2007). The bursts must arise from coherent radiation from a small emission region, and both cataclysmic explosions and longer-lived progenitors have been hypothesized (see the reviews by Katz 2018b; Platts et al. 2018; Popov et al. 2018, and references therein). To date, over 60 FRB sources have appeared in the literature. All have a large dispersion measure (DM), in excess of the expected Galactic contribution along the line of sight (Cordes & Lazio 2002), which, in the absence of a host-galaxy association, is the primary evidence for their extragalactic origin. The observed durations of the bursts range between 0.03 and 26 ms (Farah et al. 2017; Michilli et al. 2018b) and they have been detected over a reasonably large fractional bandwidth, which can teach us about their spectra as long as instrumental effects do not dominate. The bandwidth of the recording systems that have detected FRBs ranges from 16 to 580 MHz and is as large as 4 GHz for observations of one source (Gajjar et al. 2018; Zhang et al. 2018).

Some bursts have been detected with (sub-)millisecond temporal structure (Champion et al. 2016; Farah et al. 2018; Hessels et al. 2018; Shannon et al. 2018) thanks to (in some cases) real-time coherent de-dispersion or raw-voltage capture. However, the observed durations of most bursts are limited by the recorded time resolution, intra-channel dispersive smearing or scattering in some cases, making it difficult to study their spectro-temporal structure (Bhandari et al. 2018).

Despite extensive follow-up observations (e.g., Petroff et al. 2015; Shannon et al. 2018), only two FRBs have been seen to repeat (Spitler et al. 2016; The CHIME/FRB Collaboration et al. 2019b). The repeatability of some sources raises the possibility that all FRBs can repeat, or suggests that there are at least two classes of FRBs within the currently observed sample (e.g., Connor & Petroff 2018; Palaniswamy et al. 2018; Ravi 2019). FRB 121102 (Spitler et al. 2014) is unique in that it was the first FRB source with repeated bursts detected (Scholz et al. 2016; Spitler et al. 2016) and is therefore the most extensively monitored FRB source to date.

The ability to observe multiple bursts from FRB 121102 permits unprecedented studies of an FRB source and its environment. In particular, FRB 121102 was localized to 100 mas precision (Chatterjee et al. 2017); a low-mass, low-metallicity dwarf host galaxy with a star-forming region was identified at z ∼ 0.19 (Bassa et al. 2017; Kokubo et al. 2017; Tendulkar et al. 2017); the bursting source was associated with a compact, persistent radio source offset by ≤40 pc (Marcote et al. 2017); and an exceptionally high, and variable rotation measure (RM) of ∼10⁵ rad m⁻² was measured, pointing to an extreme magneto-ionic environment around the burst source (Michilli et al. 2018b). The recent discovery of a second repeating source (FRB 180814) by the Canadian Hydrogen...
Intensity Mapping Experiment (CHIME) has not yet resulted in a precise localization (The CHIME/FRB Collaboration et al. 2019b). As yet, no other published FRB has been precisely localized and definitively associated with a host galaxy, thereby greatly limiting our understanding of their progenitors.

The apparent FRB 121102 burst activity changes between observing epochs, with periods of enhanced source activity (Scholz et al. 2016; Oppermann et al. 2018), though it is unclear whether this means that the source itself is intrinsically more active. While an underlying periodicity between the bursts would be strong evidence for a rotating neutron star progenitor, analysis of the burst arrival times has yet to identify a clear periodicity (e.g., Scholz et al. 2016; Zhang et al. 2018). 

Bursts detected at 1.4 GHz were not seen in simultaneous 150 MHz observations (Houben et al. 2019). Optical, X-ray, and \( \gamma \)-ray observations that are contemporaneous with the detections of radio bursts have not found any prompt multi-wavelength counterparts to the bursts themselves, nor is there any detectable persistent X-ray and \( \gamma \)-ray emission (Hardy et al. 2017; Scholz et al. 2017).

The detection of a large sample of bursts from FRB 121102, at observing frequencies ranging from 1 to 8 GHz (e.g., Scholz et al. 2016; Spitler et al. 2016, 2018; Law et al. 2017; Gajjar et al. 2018; Hessels et al. 2018; Michilli et al. 2018b; Zhang et al. 2018), has led to a variety of observed spectra. For instance, they cannot be consistently described by a single spectral index, some bursts exhibit a frequency dependent profile evolution, and burst spectra from Law et al. (2017) are typically limited to 500 MHz wide Gaussian envelopes. Additionally, Hessels et al. (2018) presented a sample of bright bursts showing sub-components in their spectra.

The physical nature of FRB 121102 and the reason for its variable burst spectrum are the subject of many theoretical models (Platts et al. 2018). Recent models have been proposed that involve a neutron star in the immediate vicinity of an accreting massive black hole (Pen & Connor 2015; Bassa et al. 2017; Marcote et al. 2017; Tendulkar et al. 2017; Michilli et al. 2018b; Zhang et al. 2018). Other possibilities include a millisecond magnetar as the central engine of a powerful supernova remnant (e.g., Murase et al. 2016; Beloborodov 2017; Cao et al. 2017; Metzger et al. 2017; Nicholl et al. 2017). Extrinsic propagation effects have been invoked to describe the unusual burst structure and morphology (Cordes et al. 2017; Hessels et al. 2018; Main et al. 2018). Plasma lenses in the local environment of FRB 121102 could collectively create caustics that produce an amplification of the burst brightness in certain frequency bands (Clegg et al. 1998; Cordes et al. 2017). Alternatively, the burst spectra could be intrinsic, for instance originating from maser emission (e.g., Beloborodov 2017; Waxman 2017; Metzger et al. 2019). Pulsar giant pulses have also been shown to be poorly described by a single spectral index (e.g., Meyers et al. 2017). Otherwise, a combination of both intrinsic and extrinsic effects could be at play.

In an effort to understand the emission mechanism and environment of FRB 121102, we continue to collect and investigate its bursts. Here, we present 41 bursts from FRB 121102 detected at 1.4 GHz using the Arecibo Observatory in two observations from 2016 September on consecutive days. This sample was selected for our analysis due to the large volume of bursts detected in each observation (18 and 23 bursts, respectively) and the short time between observations (the minimum possible wait time before FRB 121102 transits Arecibo, i.e., one day). The sample includes all bursts that were found, down to an unprecedentedly low detection threshold (via careful visual inspection), and in combination with its size is therefore the largest sample of 1.4 GHz bursts presented to date. The observations are quasi-contemporaneous with the high signal-to-noise ratio (S/N) sample from Hessels et al. (2018) and concurrent with the Very Large Array (VLA) sample presented in Law et al. (2017).

The bursts that we detect are predominantly faint (fluctue as low as 0.028 Jy ms) and relatively narrowband: i.e., they do not extend across the full 580 MHz observing bandwidth and many peak in the observing band and fade into the noise toward higher and lower frequencies. These properties originally led to many of the bursts being identified as radio frequency interference (RFI) in our first-pass search of the data. However, the consistent recurrence of such signals compelled further investigation. We present an analysis of all bursts detected in the two observations that includes examinations of burst spectra, burst energies, and wait times. Additionally, we focus on burst detectability to instruct future FRB observations and searches. Observations and data reduction are described in Section 2. The bursts are presented in Section 3 and our findings are discussed in Section 4.

2. Observations and Burst Search

The data were recorded using the 305 m William E. Gordon Telescope at the Arecibo Observatory with the L-Wide receiver\(^9\) (frequency range 1150–1730 MHz; system temperature \( T_{s\text{ys}} \approx 25 \text{ K} \); gain \( G \approx 10.5 \text{ K Jy}^{-1} \)) and the Puerto-Rican Ultimate Pulsar Processing Instrument (PUPPI) data recording backend, which records eight 100 MHz bands (each with 64 channels).\(^10\) The 8 bit PUPPI data were sampled with a time resolution of 10.24 \( \mu \)s and each channel spans 1.56 MHz; these were coherently de-dispersed to \( \text{DM} = 557.0 \text{pc cm}^{-3} \) during the observation, effectively mitigating intra-channel dispersive smearing to \( <8.5 \mu \text{s} \) per unit deviation from the fiducial DM value. Full Stokes information was recorded; however, given the source’s large RM, linear polarization is washed out at 1.4 GHz (Michilli et al. 2018b) rendering it undetectable in our data. A search for polarization in the brightest burst from our sample was conducted in Hessels et al. (2018) and did not yield a detection. Hence, we do not present any polarimetric analysis here, though searches are ongoing to identify potential Faraday conversion effects in the data (Vedantham & Ravi 2019).

The data were sub-banded and downsampled using `psrfits_subband` before searching for bursts. The frequency channel size was increased to 12.5 MHz and the data were downsampled in time to a resolution of 81.92 \( \mu \)s. The search was performed using PRESTO, a standard software package for pulsar searches (Ransom 2001).\(^11\) The standard RFI excision tool `rfifind` was not applied to the spectra to avoid masking large fractions of data. Instead, we opted to excise RFI pulses at later stages of the search process. We generated de-dispersed timeseries (summed across frequency channels) for DMs in the range of 461–661 pc cm\(^{-3}\) in steps of 1 pc cm\(^{-3}\), using `prepsubband`. The resulting timeseries were searched for

\(^9\) http://www.naic.edu/~astro/RXstatus/Lwide/Lwide.shtml
\(^10\) http://www.naic.edu/puppi-observing/
\(^11\) https://www.cv.nrao.edu/~sransom/presto/
single pulses using single_pulse_search.py to convolve boxcar functions of widths ranging from 81.92 μs to 24.576 ms, or, equivalently, 1–300 time bins. Events from each timeseries with S/N > 6 were grouped into astrophysical burst candidates, which were subsequently excluded if the group’s peak S/N < 8, and filtered for RFI using the routine presented by Michilli et al. (2018a). The recorded times of the remaining burst candidates were used to extract segments of time and frequency data (known as dynamic spectra) from the sub-banded data de-dispersed to the DM at which the candidate peaked in S/N. Finally, a diagnostic plot was created for each candidate, containing the de-dispersed dynamic spectrum, burst profile, and relevant metadata. The diagnostic plots (43 for Observation 1 and 82 for Observation 2) were inspected by eye to evaluate whether the candidates were astrophysical in nature, and each was assigned a ranking: RFI, maybe real, definitely real. Judgments were based on what we knew FRBs to look like at the time (late 2016/early 2017); however, the “maybe” ranking was included to avoid missing interesting and potentially recurring signals in the observations. Relevant factors considered in the judgment process include whether the peak DM value was reasonably close to the value reported in earlier studies of FRB 121102 bursts (Scholz et al. 2016; Spitler et al. 2016) and whether the burst extended across most of the frequency band (this was before Hessels et al. 2018 established that the bursts can appear quite narrowband at 1.4 GHz).

The data come from the ongoing monitoring of FRB 121102 (Arecibo program P3054; PI: L. Spitler). We present data from two observations taken on 2016 September 13/09:47:07 and 14/09:50:12, each reported in topocentric UT and lasting 5967 s and 5545 s, respectively. One of the bursts (B1) was previously reported in Hessels et al. (2018).

The narrowbandedness, faintness, and, in some cases, relatively large widths (up to 13.5 ms) of the bursts presented here make the DM determination less precise. A DM value of 560.5 pc cm$^{-3}$ was established for the high S/N bursts in Hessels et al. (2018) for which the temporal features are well resolved. Given that our sample is from the same epoch, we apply the same value to the bursts in this study and find this to work reasonably well.

### 3. Results

Dynamic spectra for the 18 bursts detected in the first observation (Observation 1) and for the 23 bursts detected in the second observation (Observation 2) are presented in Figure 1. While bursts B11 and B19 look similar to FRBs presented elsewhere (though see Shannon et al. 2018), many burst signals can be characterized as narrowband, spanning on average less than one-third of the full 580 MHz observing bandwidth (FWHM values) with many peaking in brightness within the observing band. To confirm the bursts’ astrophysical nature, we provide some examples without dispersion correction alongside the expected dispersive sweep at 560.5 pc cm$^{-3}$ in Figure 2. There is an apparent 5.3(5) ms wide second burst in the dynamic spectrum of B28, ~9 ms after the primary burst; it is unclear whether these are two unique bursts or a single, double-peaked burst.

The properties of each burst are summarized in tabular form in Table 1. We measure time and frequency peaks and FWHM values using a two-dimensional Gaussian fit (Hessels et al. 2018). The intrinsic burst durations range from 0.7–13.5 ms and are on average 4.2 ms. These values are consistent with previous detections at 1.4 GHz (e.g., Scholz et al. 2016; Spitler et al. 2016; Hardy et al. 2017). We quantify the narrowband nature of each burst by reporting the burst edges ($f_{\text{high}}$ and $f_{\text{low}}$ FWHM). Many burst spectra extend beyond the top of the band, and in this case we report the top of the observing band (1730 MHz). The top panel of Figure 3 shows the average burst spectrum weighted by the band-averaged burst S/N and corrected for bandpass variations. The burst spectrum as a function of arrival time is shown in the bottom panel. The midpoint of each burst’s frequency extent is represented in a histogram in a panel to the right. Collectively, Figure 3 shows a dearth of bursts below 1.35 GHz and suggests preferred burst frequencies at this epoch, possibly clustered in time as well, particularly in Observation 1.

The distribution of burst peak S/N (summed over the 580 MHz observing bandwidth and at the DM that maximizes S/N) is reported in Figure 4. Most bursts were detected just above the detection threshold. In green we show the scaled-up S/N values obtained using only frequency channels that contain burst signal, as opposed to the full observing bandwidth, as S/N is a function of burst bandwidth.

The cumulative distribution of isotropic burst energies is shown in Figure 5. We calculate isotropic energy, $E$, matching Law et al. (2017):

$$E = F(\text{Jy s}) \times \text{BW (Hz)} \times 10^{-23} \text{erg s}^{-1} \text{cm}^{-2} \text{Hz}^{-1} \times 4\pi \times L^2,$$

(1)

where $F$ is fluence, BW is bandwidth (both as reported in Table 1), and $L$ is the luminosity distance of FRB 121102, 972 Mpc (Tendulkar et al. 2017). We calculate the fluence of a burst over its FWHM duration and FWHM bandwidth. It is calculated by summing across frequency channels that contain the burst to create a timeseries, normalizing a 42 ms time window containing the burst, and converting the signal in each time bin within the FWHM into Jy units using the radiometer equation, as described in Equation (7.12) of Lorimer & Kramer (2005). The normalization step involves defining an off-pulse region and therefore different time resolutions (see caption of Figure 1) are used depending on burst S/N. We consider a conservative fractional error of 30% for the derived fluence values. Energies are inevitably underestimated by unknown amounts for bursts that extend up to the observing band edge. The apparent turnover at lower energies in Figure 5, is likely a reflection of bursts being detected close to the sensitivity limit ($\sim1.6 \times 10^{57}$ erg for bursts that have the average duration and bandwidth values found for our sample of 4.2 ms and 175 MHz, respectively). We use the method of maximum-likelihood to estimate the slope, $\gamma$, of a power-law fit ($R \propto E^{\gamma}$, where $R$ is the rate of bursts with energy $\geq E$ per hour) for various completeness thresholds $E_{\text{threshold}}$ (e.g., Crawford et al. 1970; James et al. 2019). The black vertical line drawn at $E_{\text{threshold}} = 2 \times 10^{57}$ erg marks the completeness value that we use in the cumulative energy distribution, and was chosen because it is consistent with both the observed turnover and aforementioned sensitivity limit, and is where the distribution of $\gamma$ as a function of $E_{\text{threshold}}$ flattens out. Omitting bursts that fall below

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threshold, we find $\gamma = -1.8 \pm 0.3$ (and by extension $\frac{dR}{dE} \propto E^{-2.8}$) for the combined sample of bursts and $\gamma = -1.6 \pm 0.5$ and $\gamma = -1.9 \pm 0.5$ for Observation 1 and 2, respectively.

The distribution of burst wait times is shown in the left panel of Figure 6 and is roughly consistent with a log-normal distribution centered at $207 \pm 1$ s for wait times greater than 10 s ($p$-value = 0.73; note the $\sim 1.5$ hr duration of each observation limits our ability to see wait times on the order of $\sim 1000$ s or greater). There is a separate group of wait times below 1 s. We do not see a relationship between the brightnesses of consecutive bursts and their wait times.

A simple periodicity search was carried out using PRESTO’s rrat_period, which conducts a brute force search for a greatest common denominator of the intervals between bursts, given a list of burst arrival times and some trial period. We searched up to spin frequencies of 200 Hz (corresponding to 5 ms, which is roughly the average burst width), but did not find consistent common denominator values. This method, however, only works if all bursts have nearly the same rotational phase. More sophisticated periodicity searches are ongoing.

4. Discussion

High-resolution data, known source DM, and a rigorous burst search process have allowed us to approach the theoretical detection threshold of the telescope (despite strong RFI) and probe low burst energies. For instance, Scholz et al. (2016) used an S/N cut of $\sim 12$ and would have missed many
In Section 4.1, we discuss the burst spectra. In Section 4.2, we discuss the distributions of burst energies and wait times. Finally, we show how our findings can inform the research community’s search strategy for new FRB sources and repeat bursts in Section 4.3.

4.1. Burst Spectra

In Section 2 we outlined our burst search method, which included manual candidate classification. Notably, many of the bursts presented in this study were initially placed in either the “maybe real” category or RFI; FRBs were not known to be narrowband at the time of the search. The burst candidates were later promoted to “definitely real” after more careful consideration of the candidates as a whole and in particular their recurrence.

In an attempt to understand this subset of bursts in the context of other FRB 121102 bursts, we compare to the multi-component bursts presented in Hessels et al. (2018; see Figure 7). The bursts presented in Hessels et al. (2018) were chosen strictly for their high S/N. The sub-bursts contained in the full multi-component burst envelope emit with a...
The characteristic bandwidth of $\sim 250\text{ MHz}$ at $1.4\text{ GHz}$ and envelopes are as large as $\sim 10\text{ ms}$ wide (Hessels et al. 2018). The sub-bursts drift down in frequency during the duration of the burst, and the leading edges of sub-bursts are often sharper than the trailing edges. Similarly, some bursts from our sample tend to lower frequencies with time, and some also fade toward the trailing edge (e.g., B12, B14, B18, B20, B37, B41). Our bursts typically have durations within the observed multi-component burst envelope sizes of the Hessels et al. (2018) sample. Hessels et al. (2018) argued that the narrowbandedness cannot be from propagation effects in the Milky Way. Similar spectral behavior has been observed in bursts from FRB 180814 (The CHIME/FRB Collaboration et al. 2019b).

We explore the possibility that the narrowband signals from this study are faint multi-component bursts where only the brightest sub-burst(s) and surrounding diffuse emission are detected. To do this, we characterize the noise around the burst to generate a Gaussian noise distribution from which noise is drawn and added to the multi-component burst until a $S/N$ of 3 is shown in blue for comparison (and is offset in time for clarity). The slight deviation from the expected sweep at later times for B8 is due to the ostensible sub-burst (see 4.1) visible in the de-dispersed version shown in Figure 1. Solid white lines are artifacts from frequency channels and time bins that were removed due to RFI contamination. These are also marked with red notches.

Figure 2. Example burst dynamic spectra without correcting for dispersion. The time and frequency resolutions are 2.97 ms and 1.56 MHz, respectively. The expected dispersive sweep at $\text{DM} = 560.5\text{ pc cm}^{-1}$ is shown in blue for comparison (and is offset in time for clarity). The slight deviation from the expected sweep at later times for B8 is due to the ostensible sub-burst (see 4.1) visible in the de-dispersed version shown in Figure 1. Solid white lines are artifacts from frequency channels and time bins that were removed due to RFI contamination. These are also marked with red notches.
We do not rule out the possibility that these bursts are intrinsically narrowband, for example resulting from maser emission (e.g., Waxman 2017; Metzger et al. 2019). Another possible way to obtain narrowband signals is if the bursts have an intrinsic frequency-dependent brightness, but are inherently weak such that only the brightest portions are detected. It is likely that a combination of both intrinsic and extrinsic mechanisms are producing the observed complex spectra of FRB 121102 bursts. For instance, lensing may boost burst envelopes at preferred frequencies and the structures within the envelope may be intrinsic. However, there currently are not

another epoch where multiple bursts are seen, the separation of a double cusp would be different. A slightly more complex lens (such as a distorted Gaussian) can show multiple spectral islands; if there is a population of lensing structures, like filaments in the Crab Nebula (e.g., Temim et al. 2006), there can be even more islands. A related prediction is that for observations at different widely spaced frequencies, we would expect spectral islands to be different if seen at all in a separate frequency band. Further simultaneous observations at multiple observing bands are needed to improve our understanding of the spectral behavior of FRB 121102.

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many emission models that can explain the observed burst structure (though see Metzger et al. 2019).

4.2. Burst Energies and Wait Times

The cumulative distribution of observed burst energies from our study (Figure 5) is consistent with a single power-law fit with $\gamma = -1.8 \pm 0.3$, above $E_{\text{threshold}} = 2 \times 10^{37}$ erg. This value is at odds with the results of Law et al. (2017), where $\gamma = -0.7$ was found to consistently describe the cumulative energy distributions of a separate sample of FRB 121102 bursts detected by the VLA at 3 GHz, the Green Bank Telescope (GBT) at 2 GHz, and Arecibo (though with the slightly less sensitive ALFA receiver) at 1.4 GHz. The fluence values of the bursts detected by the latter two telescopes were scaled to energy with the assumption that the full bursts were detected (ALFA has an observing bandwidth of 323 MHz), which likely underestimates the energy in most cases. A completeness threshold was not applied to their sample. Law et al. (2017) suggested that a consistent power-law index for observations with different frequencies and detection rates is connected to the underlying emission mechanism. The Law et al. (2017) analysis includes bursts with energies $>2 \times 10^{37}$ Jy ms. Therefore, our sample of bursts probes the burst energy distribution of FRB 121102 to unprecedentedly low energies.

There are many potential complications to consider in analyzing the distribution of burst energies from FRB 121102. First, there are clearly parts of some bursts being missed due to the limited observing bandwidth. Second, there may be fainter burst sub-components that fall below the detection threshold. Third, the presence of extrinsic propagation effects would skew...
the results of any energy distribution. Therefore, expecting a power law to describe the cumulative energy distribution is likely an over-simplification. Additionally, determining where the sample is complete can have a large effect on the steepness of the slope (Figure 5, right). In any case, possible reasons for the difference in slope of the power-law approximation used here and in Law et al. (2017) can stem in part from the different energy range being sampled for a burst energy distribution that is more complex. For instance, Karuppusamy et al. (2010) have shown that the Crab pulsar’s pulse intensity distribution is multi-modal, peaking at lower intensities (the regular pulsar-like pulses), followed by a log-normal distribution and finally an extended power-law tail attributed to the Crab’s giant pulses. In contrast, regular pulsars are known to have consistent energy distributions from epoch to epoch, when sampling averaged pulses, and are typically described by a normal or exponential function (Hesse & Wielebinski 1974; Ritchings 1976). Single-pulse emission from both radio magnetars and pulsars, however, tend to have log-normal flux density distributions (Burke-Spolaor et al. 2012; Levin et al. 2012).

From the cumulative energy distribution and derived γ, we can test the hypothesis that the persistent radio source associated with FRB 121102 is due to the emission of many faint bursts that fall below the detection threshold of our telescopes. We do this by making the simple assumption that the energy distribution is described by $R \propto E^{\gamma}$ (see Section 3) at some minimum energy $E_{\text{min}}$, and by setting the known luminosity of the persistent source $L_p \approx 3 \times 10^{38}$ erg s$^{-1}$ (Marcote et al. 2017) equal to $E_{\text{min}}$ times the rate at $E_{\text{min}}$. Using our results from Figure 5 for $E_{\text{threshold}} = 2 \times 10^{37}$ erg, we can solve for $E_{\text{min}}$ using the following approximation:

$$L_p \approx R_{\text{threshold}} \left( \frac{E_{\text{min}}}{E_{\text{threshold}}} \right)^\gamma E_{\text{min}},$$

where $R_{\text{threshold}} = 360^{-1}$ s$^{-1}$ (the rate at $E_{\text{threshold}}$) and $\gamma = -1.8$. The resulting minimum energy $E_{\text{min}} = 4.5 \times 10^{32}$ erg corresponds to a rate of $\sim 700$ bursts per millisecond. Therefore, for the assumed power-law energy distribution and given that the burst widths in our sample are on the order of a millisecond, it is implausible that the persistent radio emission is generated by a high rate of low-energy bursts.

The giant pulse model has been proposed as an emission mechanism for FRBs, where bursts are extreme versions of giant pulses like those observed in the Crab pulsar (Connor et al. 2016; Cordes & Wasserman 2016; Katz 2016; Lyutikov et al. 2016). Pertinently, the lack of observed correlation between burst wait times and energy (Figure 6) is consistent with pulsar giant pulse emission (Karuppusamy et al. 2010). Of relevance to magnetar-related models, the log-normal shape of the burst wait time distribution from Figure 6 is also seen for soft gamma repeaters, which are a type of magnetar (Göğüş et al. 1999, 2000; Wang & Yu 2017).

A distinct smaller population of FRB 121102 burst wait times below 1 s has also been noted by Katz (2018a), Zhang et al. (2018), and Li et al. (2019). With those wait times omitted, a log-normal function can also reasonably describe the wait time distributions found in both studies, which peak at $\sim 75$ s and 170 s, respectively. The Li et al. (2019) analysis included the 4–8 GHz Zhang et al. (2018) bursts, which dominate the sample. Due to a larger sample of bursts, the gap between populations in the wait time distribution of the Zhang et al. (2018) bursts is slightly smaller (beginning at 600 ms) relative to ours. With a larger sample of bursts, we might see more wait times fill the observed gap. The constancy of the distribution of burst arrival time intervals for both of our observing days suggests that the burst detection rate can be consistent on $\sim$day timescales. Li et al. (2019) agree with our finding that burst fluence is independent of wait time. Studying burst wait times for (simultaneous) observations at different frequencies could provide additional constraints to the emission mechanism and/or extrinsic propagation effects involved.

We have uniform sensitivity to wait times between $\sim 1000$ s (on the order of the observation length) down to tens of milliseconds, at which point ambiguities in distinguishing multi-peak bursts from single bursts with small separations in arrival time (e.g., B28) complicate the analysis, as well as periodicity searches. For high S/N bursts, the separation between sub-bursts was found to be $\sim 1$ ms (Hessels et al. 2018). Zhang et al. (2018) have reported a burst pair separated by 2.56 ms which, if both are unique, would be the most closely spaced bursts detected to date. Other ambiguous pairs reported in their analysis are separated by the same order of time as the sub-components of burst B28 ($\sim 10$ ms). Excluding inconclusive cases and assuming B36 from our analysis is a singular burst, it has one of the shortest wait times observed to date at 26 ms.

4.3. Implications for FRB Searches

The definition of a “canonical” FRB is changing, and this is important for considering which detected signals are of genuine astrophysical origin (Foster et al. 2018). We emphasize that the standard pulsar single-pulse search techniques widely used in FRB searches are likely to have missed most of the bursts that we present. If not for the development of tailored search algorithms, conservative search filters (Michilli et al. 2018a), and human inspection (possible in this case because we are targeting a known source with known DM), the tally of Arecibo bursts from FRB 121102 would be reduced by about one third. Important to keep in mind is the fact that our
observations benefit from high frequency and time resolutions, and that the source DM was previously known. Assuming that there has not been a significant change in the activity level of these bursts, signals like the ones we present here have likely been missed in previous FRB\textsubscript{121102} observations presented in for example Spitler et al. (2016) and Scholz et al. (2016).

The features that set many of the bursts presented in this study apart from the other bursts observed from FRB\textsubscript{121102} and other FRB sources are their combined narrow bandwidth and faintness. In the rest of this subsection, we discuss the associated detection implications and suggest possible solutions.

The search techniques used to generate our burst candidates involve consideration of the peak S/N, obtained after summing all de-dispersed frequency channels. A burst’s S/N depends on multiple factors (Cordes & McLaughlin 2003), including the width and the intrinsic fluence of the burst, which is defined as the area of the burst (i.e., the amplitude after adding signal across the frequency band, multiplied by burst width). S/N scales with fluence, $F$, and width, $w$, as

$$S/N \propto \frac{F}{\sqrt{w}}.$$  \hfill (3)

Thus, narrower bursts are more easily discerned from the noise than wider bursts of equivalent fluence. A burst’s limited bandwidth will also contribute significantly in lowering the peak S/N, as it will be diluted by noisy frequency channels after summing together in frequency to create the timeseries. This effect is demonstrated in Figure 4 and is directly visible by comparing the black and gray burst profiles in Figure 1. Therefore, Equation (3) should be modified to take into account the fraction of the band where signal is detected over the noise level, $\nu_{\text{signal}} / \nu_{\text{band}}$,

$$S/N \propto \frac{F}{\sqrt{w} \left( \frac{\nu_{\text{signal}}}{\nu_{\text{band}}} \right)}.$$  \hfill (4)
It is very likely that FRB signals that do not fill the entire observing bandwidth are being missed. In this study, we have shown that the three aforementioned properties (faint, narrow in frequency, and wide in time) that can reduce detectability often overlap, compounding the difficulty of detecting such signals.

Deviations from the true source DM in the de-dispersed timeseries reduces the peak S/N value in a directly proportional fashion (Cordes & McLaughlin 2003). Bursts that are narrow in frequency, large in temporal width, and faint will contribute to uncertainties in the DM measurement, regardless of the method of determination used (e.g., visual dynamic spectrum alignment or peak S/N maximization). Furthermore, de-dispersed timeseries at a wide range of DMs constitute a fundamental aspect of single-pulse searches, especially if the source DM is unknown. As described in Section 2, events found in each timeseries are grouped into astrophysical candidates. It is in this crucial grouping step where bursts similar to those presented in this analysis can be missed. According to Cordes & McLaughlin (2003), bursts narrower in time will peak more sharply in their distribution of S/N as a function of DM, causing them to be easier to find. Therefore, search algorithms sensitive to slow peak S/N turnovers in the timeseries are necessary to detect wider bursts that are also faint. The challenge is compounded for narrowband bursts, as their S/N versus DM distribution will be similar to that of narrowband RFI.

Burst candidate classifiers usually consider broadband bursts. It could be important to change this aspect, despite the associated difficulty in distinguishing between real bursts and narrowband RFI, as the bursts become progressively narrower. For repeating FRBs, more weight could be given to a burst candidate if others have been seen to peak at that frequency. Especially with the advent of new telescopes with larger fractional observing bandwidths (e.g., CHIME/FRB Collaboration et al. 2018), observers may wish to consider the effects of peak S/N dilution in the case of narrowband bursts. A possible solution is to apply matched filtering techniques in the frequency domain, though this will be computationally costly and increase the number of candidates (Zhang et al. 2018).

5. Conclusions

We have presented and analyzed 41 FRB 121102 bursts resulting from two consecutive 1.4 GHz observations at the Arecibo Observatory and rigorous burst search methods. Our analysis has probed the faintest bursts from FRB 121102 in a period of high burst detection rate. We have shown the bursts to be detectable at preferred frequency ranges that vary between epochs on timescales of ∼days, which is expected if plasma lensing is at play. Additionally, we have demonstrated that we have likely observed faint versions of previously reported bursts showing complex structure. We have found a power-law fit to the cumulative burst energy distribution to be at odds with previously reported slope values, and have discussed possible reasons for the discrepancy. We have placed constraints on the idea that the persistent radio source associated with FRB 121102 is from a high rate of low-energy bursts. We have found the wait time between bursts to follow a log-normal distribution, which has also been observed in previous FRB 121102 studies as well as some magnetars. We have identified a sub-group of bursts with wait times below 1 s, which is consistent with previous reports. The faint and narrowband bursts that we have presented bolster the findings of recent studies that show that FRBs are not always detectable across the full observing band. We have discussed the challenges associated with detecting such signals, and have provided recommendations for future FRB searches to minimize the likelihood of missing new FRBs and possible repeat bursts.

Facility: Arecibo.

Software: Astropy (Astropy Collaboration et al. 2013, 2018), PRESTO (Ransom 2001), PSRCHIVE (Hotan et al. 2004), psrfitutils.13

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13 https://github.com/demorest/psrfit-utils