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Frequency of the ultranarrow 1S_0 - 3P_2 transition in ^{87}Sr

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We determine the frequency of the ultranarrow ^{87}Sr 1S_0 - 3P_2 transition by spectroscopy of an ultracold gas. This transition is referenced to four molecular iodine lines that are observed by Doppler-free saturation spectroscopy of hot iodine vapor. The frequency differences between the Sr and the I_2 transitions are measured with an uncertainty of 0.5 MHz. The absolute frequency of the ^{87}Sr 1S_0 - 3P_2 ($F' = 7/2$) transition is 446 648 775(30) MHz and limited in accuracy by the iodine reference. This work prepares the use of the Sr 1S_0 - 3P_2 transition for quantum simulation and computation.

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I. INTRODUCTION

Atoms with two valence electrons, such as the alkaline-earth metals or ytterbium, possess ultranarrow intercombination transitions from their singlet ground state to metastable triplet states. The 1S_0 - 3P_0 transition, which connects two states that are free of electronic magnetic moment, is used as frequency reference in optical atomic clocks [1] and is of interest for quantum simulation [2–6], computation [7–9], and gravitational wave detection [10–12]. The 1S_0 - 3P_2 transition is equally narrow [13], but it connects the ground state to an excited state with electronic magnetic moment. This property has enabled high-resolution imaging of an Yb quantum gas in a magnetic field gradient [14,15], a method that could also provide selective access to qubits in a quantum computer [7,8]. Isotopes with nuclear spin exhibit hyperfine structure in the 3P_2 state, which will make it possible to induce nuclear spin state specific ac Stark shifts and Raman couplings using the 1S_0 - 3P_2 transition. This property might allow the creation of artificial gauge fields that are significantly less hampered by off-resonant scattering of photons or collisions between metastable state atoms compared to schemes exploiting broader transitions [16–20] or using metastable atoms [3,5,21]. Ultracold mixtures containing 3P_2 atoms have been obtained from quantum gases of ground-state atoms by excitation on the 1S_0 - 3P_2 transition, leading to the discovery of Feshbach resonances between Yb 1S_0 and 3P_2 atoms [22]. These resonances are interesting for quantum information processing [7–9], are predicted to show signatures of quantum chaos [23], and have been exploited to form Feshbach molecules [24,25]. Also mixtures of 3P_2 Yb with Li have been created

[26,27] and their collisional stability has been investigated [28–32]. The 1S_0 - 3P_2 transition might also be useful to create quantum gases with quadrupole interactions [33–37].

Many of these applications require quantum degenerate gases and so far three two-valence-electron elements have been cooled to quantum degeneracy: Yb [38], Ca [39], and Sr [40]. The frequency of the 1S_0 - 3P_2 transition is only well known for Yb. Strontium has properties that significantly distinguish it from Yb, offering different opportunities. It enables higher phase space densities directly by laser cooling, which makes it possible to create quantum gases with large atom number or with high repetition rate [41]. Its fermionic isotope ^{87}Sr has a nuclear spin of 9/2, which should enable better Pomeranchuk cooling [42,43] or larger synthetic dimensions [44]. In order to combine these favorable properties with the possibilities offered by the 1S_0 - 3P_2 transition, the frequency of this transition needs to be determined to at least the megahertz level.

In this article we report the measurement of the ultranarrow 1S_0 - 3P_2 transition in ^{87}Sr by direct optical excitation. We perform loss spectroscopy of an ultracold strontium sample and determine the resonance frequency by comparison to four spectral lines of molecular iodine, which serves as a natural and documented reference. The iodine lines are identified by comparing a gigahertz-wide iodine spectrum around the Sr lines with the spectra calculated by the IODINESPEC5 software [45]. The accuracy of the measurement is limited by the uncertainty in iodine transition frequencies, whereas the precision is limited by frequency drifts of an optical resonator used for spectroscopy laser stabilization. The relative frequency between the Sr transition and specific iodine lines is obtained with an accuracy of 0.5 MHz and the absolute frequency is limited by the iodine line accuracy of 30 MHz. These measurements open the door to using the Sr 1S_0 - 3P_2 transition for important applications, such as the creation of artificial gauge fields or quantum computation.

This article has the following structure: Section II describes the spectroscopy laser system, the iodine spectroscopy setup, and Sr sample preparation; Sec. III introduces relevant Sr transitions, presents initial coarse and final precise

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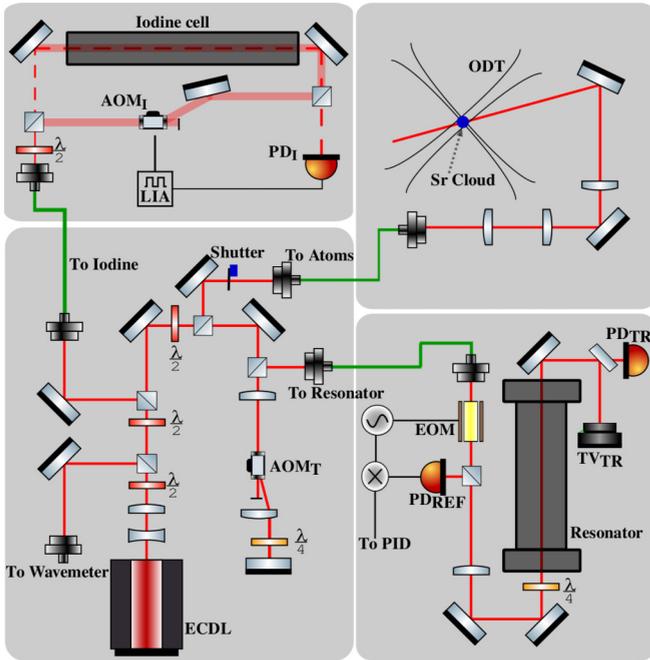


FIG. 1. Scheme of the spectroscopy setup. The light of an extended cavity diode laser (ECDL) is distributed to a wavemeter, an optical resonator, an iodine spectroscopy setup, and Sr samples in an optical dipole trap (ODT). The laser frequency is stabilized to a mode of an optical resonator. Acousto-optic modulator AOM_T introduces a controlled offset between the laser light and the resonator mode and is used to perform spectroscopy scans. To lock the light to the resonator the Pound-Drever-Hall method is used, for which an electro-optic modulator (EOM) creates sidebands on the light sent to the resonator and photodiode PD_{REF} measures the light intensity reflected from it. The light transmitted through the resonator is analyzed by TV camera TV_{TR} and photodiode PD_{TR} . The laser frequency can be referenced to iodine lines using the iodine spectroscopy setup, consisting of an iodine vapor cell, AOM_I , PD_I , and a lock-in amplifier (LIA).

determination of the $^1S_0-^3P_2$ transition frequency and analyzes the measurement error. Conclusions are given in Sec. IV.

II. EXPERIMENTAL DETAILS

A. $^1S_0-^3P_2$ spectroscopy laser setup

Light for the spectroscopy of Sr and iodine is produced by an external cavity diode laser (ECDL; wavelength: 671 nm; power: 24 mW; diode: Toptica LD-0670-0035-AR-1); see Fig. 1. The ECDL is locked to an optical resonator by the Pound-Drever-Hall method [46]. The resonator uses a Zerodur spacer, is length tunable by two piezos that compensate each other's thermal expansion [47], and is kept under vacuum, with the vacuum chamber placed inside a thermally insulating box. A frequency shift of 550–850 MHz is introduced by an acousto-optic modulator (AOM) between the ECDL and the light used for locking. Spectroscopy scans are performed by slowly varying the AOM frequency so that the lock follows. The feedback loop uses a fast proportional-integral-differential (PID) controller (Toptica FALC 110), providing feedback of 1.9 MHz bandwidth to the ECDL current and

10 kHz bandwidth to the ECDL grating. Based on the error signal, we estimate the laser linewidth to be at most 85 kHz. The light is sent through polarization-maintaining single-mode optical fibers to the Sr sample and to the iodine spectroscopy setup. The absolute frequency of the spectroscopy laser can be obtained with a wavemeter (Toptica HighFinesse WSU-30, accuracy of 30 MHz) calibrated to the frequency of the 7.4-kHz-wide $^1S_0-^3P_1$ transition of ^{88}Sr , known to within 10 kHz [48]. The calibration laser's absolute frequency is determined by spectroscopy of a Sr Bose-Einstein condensate to better than 50 kHz and its frequency stability is better than 10 kHz, as verified by successful operation of a $^1S_0-^3P_1$ line magneto-optical trap (MOT). The wavemeter calibration is done each day immediately before the data collection runs using the designated calibration port of the wavemeter.

B. Iodine spectroscopy setup

Spectra of iodine molecule vapor (natural sample, essentially 100% $^{127}\text{I}_2$ [49]) contained in a heated quartz cell are recorded using Doppler-free saturated absorption spectroscopy [50,51]. We will now briefly describe the I_2 spectroscopy setup (see Fig. 1). The quartz cell is 60 cm long and kept at approximately 530 °C (not stabilized by feedback) in order to populate the higher vibrational levels of the iodine molecule [51]. A cold finger, stabilized at 20.0(3) °C, is used to set the iodine partial pressure. The collimated spectroscopy beam entering the setup (waist 0.7 mm, power 5 mW) is split into a pump and a probe beam. The probe beam (power 0.5 mW) is sent through the cell onto a photodiode that records the spectroscopy signal. The pump beam is frequency shifted by acousto-optic modulator AOM_I , after which it has approximately 3 mW of power, and gets sent through the iodine cell in a counterpropagating manner with respect to the probe [52]. We enhance the weak Doppler-free signal by lock-in detection. We use AOM_I to chop the pump beam at 50 kHz (square wave) and we demodulate the detected probe signal at that frequency on a lock-in amplifier (EG & G Instruments Model 7265) using a time constant of 100 ms. A few things are worth mentioning about this approach: first of all, the lock-in method is necessary, because the bare Lamb dips in the Doppler spectrum are too weak to be seen directly with the available power; secondly, the method is quite forgiving in terms of the chopping frequency, and in particular, the chopping frequency can be increased if one wants to reduce the time constant of the lock-in for faster scans, at the expense of signal to noise ratio [53]; thirdly, the method is forgiving to slight misalignment in the overlap of the pump and probe beams, imperfect collimation of the beams, and slight power fluctuations of pump and probe.

C. Strontium sample preparation and spectroscopy principle

Spectroscopy of the Sr $^1S_0-^3P_2$ transition is done on an ultracold cloud of ^{87}Sr in an equal mixture of all nuclear spin states contained in an optical dipole trap (ODT). The ODT consists of two horizontally propagating, linearly polarized 1064-nm beams crossing at right angles and having waists of approximately 70 and 60 μm and powers of 2.2 and 1.2 W; the beams have a 160 MHz frequency difference in

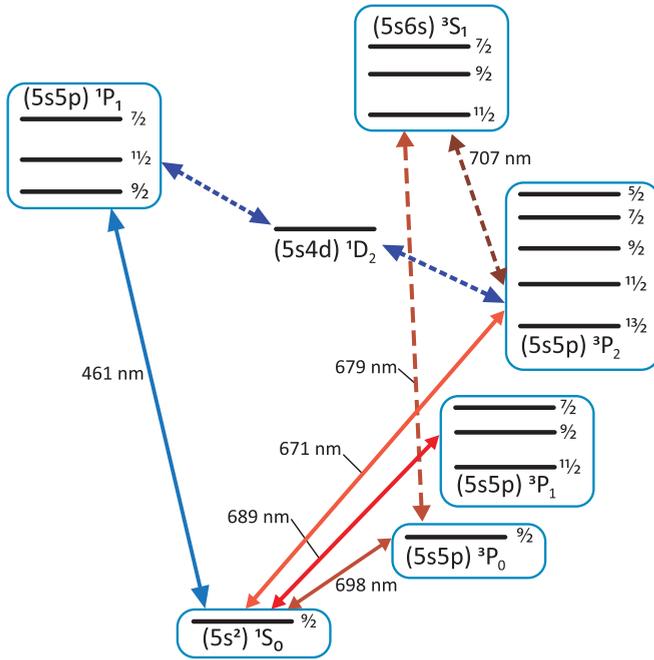


FIG. 2. Level scheme of the low-lying electronic states of ^{87}Sr . The transitions at 461 and 689 nm are used for MOTs, the transitions at 679 and 707 nm are repump transitions, the one at 698 nm is the clock line, and the transition at 671 nm is the 1S_0 - 3P_2 line whose frequency we measure in this work. The hyperfine structure of the 1D_2 is neglected because it is irrelevant for this work.

order to avoid mutual interference. To prepare the sample, a magneto-optical trap is loaded from a Zeeman-slowed atomic beam and then transferred into the ODT using the techniques described in Ref. [41]. We obtain a cloud of 2×10^5 Sr atoms at 730 nK, which has a $1/e$ width of $\sim 25 \mu\text{m}$ in the vertical direction and $\sim 38 \mu\text{m}$ in the horizontal direction. We reduce the residual magnetic field to less than 30 mG at the location of the atomic cloud. The Sr spectroscopy beam is focused to a waist of about $60 \mu\text{m}$ at the sample position. Spectroscopy is performed time-sequentially and measures frequency-dependent loss of ground-state atoms. A sample is prepared, exposed to spectroscopy light, which leads to atom loss, and the remaining ground-state atom number is detected by absorption imaging on the 1S_0 - 1P_1 transition.

III. DETERMINATION OF THE 1S_0 - 3P_2 TRANSITION FREQUENCY

Strontium levels and transitions that are relevant for this work are shown in Fig. 2. The transitions 1S_0 - $^3P_{0,2}$ are dipole forbidden in isotopes with pure spin-orbit (LS) coupling because of spin and total angular momentum selection rules [55]. A small dipole matrix element can be induced by mixing of the $^3P_{0,2}$ states with 1P_1 through the application of a magnetic field or through hyperfine coupling in the case of ^{87}Sr , the only stable Sr isotope with nuclear spin. For the bosonic ^{88}Sr the observation of the 1S_0 - 3P_0 clock transition has been reported with an external mixing field as low as 13 G [56,57]. Most Sr optical lattice clocks use fermionic Sr in order to exploit hyperfine mixing to enable the clock transition.

In this work we use fermionic ^{87}Sr , which allows dipole transitions between 1S_0 ($F = 9/2$) and 3P_2 ($F' = \{7/2, 9/2, 11/2\}$) with a linewidth of approximately 1 mHz by hyperfine mixing [13]. The transitions 1S_0 ($F = 9/2$)- 3P_2 ($F' = \{5/2, 13/2\}$) have $\Delta F = \pm 2$ and the ground and excited states have opposite parity, which makes them dipole forbidden. They are, however, still accessible as magnetic quadrupole transitions ($M2$) [58] and we observe the 1S_0 ($F = 9/2$)- 3P_2 ($F' = 5/2$) transition.

We determine the 1S_0 - 3P_2 transition frequency in two steps. The first step, described in Sec. III A, determines the transition indirectly to within ~ 100 MHz. This is sufficiently precise to find the transition with direct spectroscopy (see Sec. III B). In Sec. III C we discuss the error of our measurement.

A. Coarse, indirect determination

The 1S_0 - 3P_2 transition frequency has only been measured for the most abundant isotope ^{88}Sr with an accuracy of 120 MHz [59]. The ^{87}Sr 1S_0 - 3P_2 transition frequencies can be estimated by adding the ^{87}Sr 3P_2 hyperfine shifts, which have been determined by radio-frequency spectroscopy in hot Sr [60], and the isotope shift. Here we assume that the 1S_0 - 3P_2 isotope shift is the same as the measured 1S_0 - 3P_0 and 1S_0 - 3P_1 isotope shifts [61–63], which are both within 1 MHz of $f_{88} - f_{87} = 62$ MHz. We verify the estimated transition frequency by performing a simple, coarse and indirect frequency determination. We determine $f(^1S_0$ - $^3P_2)$ using conservation of energy: we measure $f(^3P_2$ - $^3S_1)$ and use the well-known transition frequencies $f(^1S_0$ - $^3P_0)$ and $f(^3P_0$ - $^3S_1)$ [64] to calculate $f(^1S_0$ - $^3P_2)$ (see Fig. 2). The 3P_2 - 3S_1 transition is dipole allowed, which makes it much broader and easier to find than the doubly forbidden millihertz-linewidth 1S_0 - 3P_2 transition. Similar schemes were used to determine the Sr 1S_0 - 3P_0 transition [64] and the Yb 1S_0 - 3P_2 transition [65].

To determine $f(^3P_2$ - $^3S_1)$ we use reservoir spectroscopy [66]. This technique relies on the fact that atoms in the 1S_0 - 1P_1 MOT cycle can decay through the 1D_2 state into the metastable and magnetic 3P_2 state, the low field seeking m_F substates of which are captured in the magnetic quadrupole field of the MOT. These atoms can be pumped back into the MOT cycle with light on a transition from the 3P_2 state to some higher-lying state that has a high chance of decaying into the ground state. We use the 3S_1 state as the higher-lying state, from which atoms decay to the ground state through the short-lived 3P_1 state. The 3P_2 - 3S_1 transition corresponds to a repump laser operating around 707 nm. Thus, when the repump laser is tuned to a resonance, the 3P_2 atoms from the magnetically trapped reservoir are quickly brought back into the 1S_0 - 1P_1 MOT cycle, rapidly increasing the number of ground-state atoms and causing a MOT fluorescence flash. There are nine repump resonances due to the number of hyperfine states in both 3P_2 and 3S_1 , but we do not need to measure all of those transitions to determine $f(^3P_2$ - $^3S_1)$.

We observe three 3P_2 - 3S_1 repump resonances, which we can attribute to specific transitions between hyperfine states in the 3P_2 and 3S_1 manifolds using knowledge of the 3P_2 hyperfine structure [60], knowledge of the 3S_1 hyperfine structure [64], and selection rules. The absolute frequencies of these transitions are obtained with the wavemeter

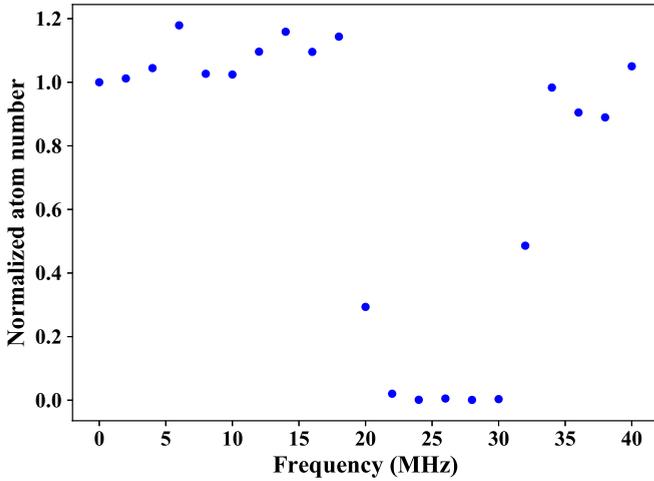


FIG. 3. Spectrum of the $^1S_0 (F = 9/2) - ^3P_2 (F' = 11/2)$ transition broadened by using a large Rabi frequency (spectroscopy laser power of 4.5 mW). The zero of the frequency axis is chosen arbitrarily.

that is also part of the $^1S_0 - ^3P_2$ spectroscopy setup. These measurements, combined with the known transition frequencies $f(^1S_0 - ^3P_0)$ and $f(^3P_0 - ^3S_1)$ [64], provide estimates of the individual transition frequencies $f[^1S_0 (F = 9/2) - ^3P_2 F' = \{7/2, 9/2, 11/2\}]$. This determination has an accuracy of ~ 100 MHz and confirms the estimated transition frequencies. Using this good starting point we now expect to find the transitions quickly in a direct spectroscopy search.

B. Precise, direct determination

We perform direct spectroscopy of the $^1S_0 - ^3P_2$ transitions using Sr samples in an ODT. When the spectroscopy laser is tuned into resonance, ground-state atoms are excited to the metastable 3P_2 state. Atoms in this state are transparent to the $^1S_0 - ^1P_1$ absorption imaging beam and furthermore likely lost by inelastic collisions [67]. To find a resonance we measure the fraction of 1S_0 atoms remaining in the ODT as a function of spectroscopy laser frequency, while keeping other parameters, such as illumination time and laser power, constant. During the first search for the transition we use the full power of the spectroscopy beam (4.5 mW). We repeatedly prepare Sr samples and use each to scan a 1 MHz frequency interval over 1 s. An example for the resulting spectrum is shown in Fig. 3 and determines all $^1S_0 - ^3P_2$ transitions to within 10 MHz, using the known 3P_2 hyperfine splittings.

In order to determine the transition frequency with more precision we zoom in on the detected broad spectroscopy signals by recording spectra with 0.45 mW of spectroscopy laser power and reduced frequency interval and illumination time per sample. The narrowest spectroscopy signals for $F' = \{7/2, 9/2, 11/2\}$ are shown in Fig. 4 together with Gaussian fits, the parameters of which are summarized in Table I. The values of the transition frequencies measured with the wavemeter are also reported in Table I, and the uncertainty is dominated by wavemeter inaccuracy.

Next we determine the frequency difference between four iodine transitions and the $^{87}\text{Sr } ^1S_0 (F = 9/2) - ^3P_2 (F' = 7/2)$ transition. This allows us to determine the frequency of the

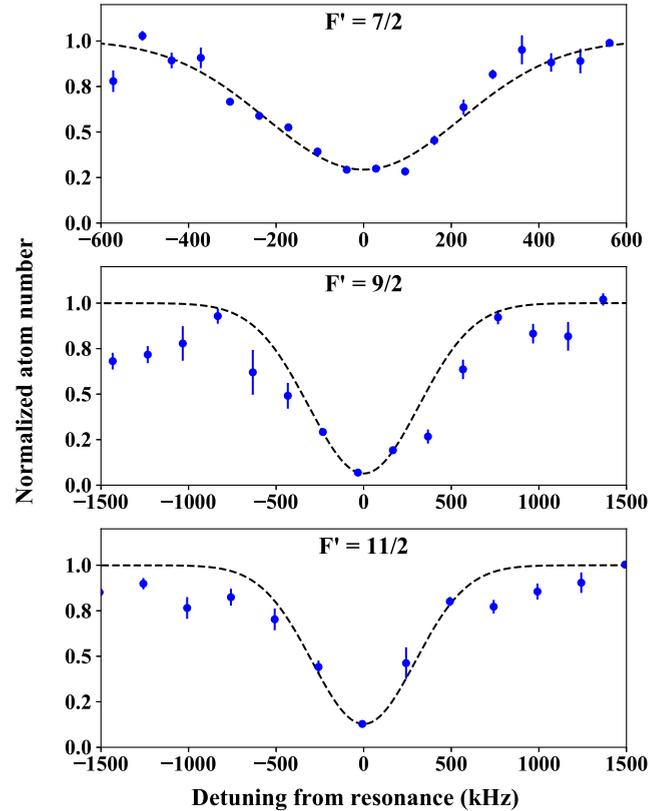


FIG. 4. High-resolution spectra of the $^1S_0 - ^3P_2 (F' = \{7/2, 9/2, 11/2\})$ transition in ^{87}Sr measured by atom loss spectroscopy in an ODT using low spectroscopy beam power (0.45 mW). The atom numbers are normalized to the ones far away from any spectroscopy signal. The error bars represent the standard error of five measurements per data point.

Sr transition with the accuracy of the known iodine transition frequencies, which currently is the same as the accuracy of the wavemeter (30 MHz), but can be improved in the future with iodine spectroscopy alone [51]. More importantly the accuracy of the frequency difference (0.5 MHz) is much higher than the accuracy of the absolute frequency, which makes it possible to find the Sr transition with simple iodine spectroscopy and to lock the Sr laser to iodine lines.

The $F' = 7/2$ state is used for iodine comparison because it is within the spectroscopy AOM tuning range of the strong iodine transitions ($J' - J'' = 32 - 33$) ($\nu' - \nu'' = 9 - 9$)

TABLE I. Frequencies and measured linewidths of the $^1S_0 - ^3P_2$ transition to three different hyperfine states in the 3P_2 manifold. The frequencies are determined using a wavemeter, whereas the full-width half-maximum (FWHM) linewidths are obtained from Gaussian fits to the spectroscopy signals shown in Fig. 4.

F'	Frequency (MHz)	FWHM linewidth (MHz)
7/2	446 648 769(30)	0.52(4)
9/2	446 647 793(30)	0.74(3)
11/2	446 646 618(30)	0.69(8)

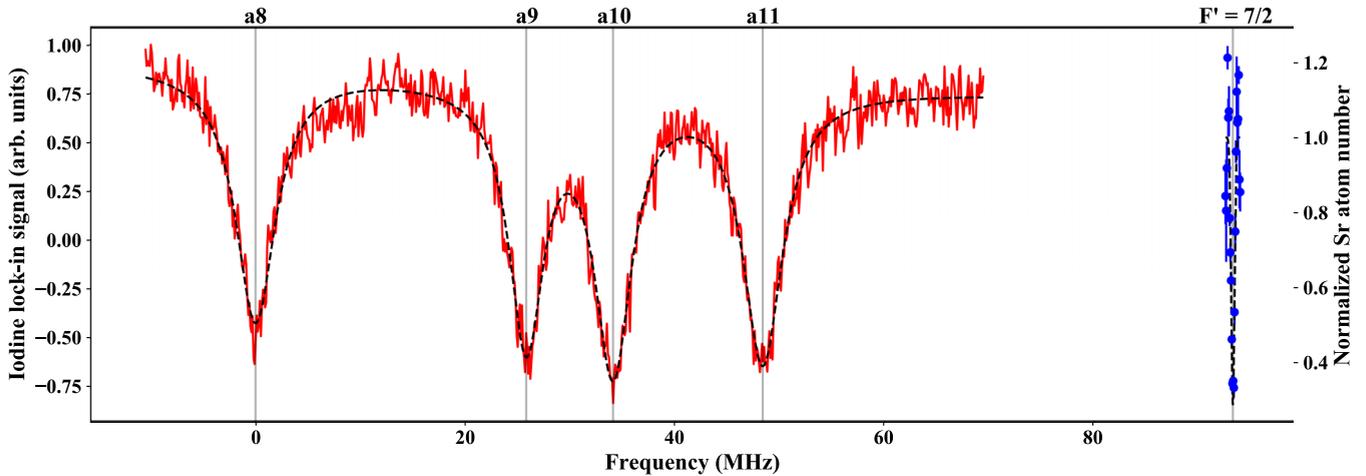


FIG. 5. Combined spectrum of the $^{87}\text{Sr } ^1S_0\text{-}^3P_2$ ($F' = 7/2$) line and iodine lines {a8, a9, a10, a11}. The red line is iodine data, the blue circles are ^{87}Sr data, and the black dashed lines are the fits to the respective spectra (multiple Lorentzian for iodine and Gaussian for ^{87}Sr). The center of each fitted spectral line is marked with a vertical gray line and labeled on top. The center of the a8 line is chosen as the zero of the frequency axis.

{a8, a9, a10, a11} [68]. The frequencies corresponding to the other hyperfine states in the 3P_2 manifold can be found by using this frequency and the known 3P_2 hyperfine splittings [60]. Figure 5 presents an example of a recorded iodine spectrum (scan time 1.5 min), fitted with Lorentzians, combined with the Sr spectrum, fitted with a Gaussian. In order to estimate the drift of the spectroscopy laser, we record four iodine spectra within a 2.5 h interval that encompasses the $^{87}\text{Sr } ^1S_0$ ($F = 9/2$)- 3P_2 ($F' = 7/2$) frequency measurement. The maximum change of the relative frequency between the iodine laser and the iodine lines is 250 kHz. Since the iodine line frequency is expected to change much less than that we attribute this frequency shift mainly to the lock of the spectroscopy laser to the reference cavity. Table II lists the fitted central frequency values of the iodine transitions, where each value is an averaged result from the fits to four measured spectra. Using the a8 frequency calculated by IODINE-SPEC5 we obtain 446 648 775(30) MHz for the $^{87}\text{Sr } ^1S_0$ ($F = 9/2$)- 3P_2 ($F' = 7/2$) transition frequency, which is consistent with the frequency determined by the wavemeter.

TABLE II. Measured frequencies of the iodine transitions {a8, a9, a10, a11} within the manifold P(33) (9-9) and the $^1S_0\text{-}^3P_2$ ($F' = 7/2$) transition frequency. The frequencies are reported with respect to the measured frequency of the a8 transition. The iodine transition frequencies are given for our conditions of the iodine cell (see text) and are shifted by $-100(15)$ kHz with respect to iodine lines at zero pressure and temperature. The error of the Sr transition is dominated by drifts of the reference resonator.

Transition	Frequency (MHz)
a8	0.00(3)
a9	25.88(3)
a10	34.17(5)
a11	48.39(4)
$^1S_0\text{-}^3P_2$ ($F' = 7/2$)	93.27(25)

The frequency of the $^1S_0\text{-}^3P_2$ ($F' = 5/2, 13/2$) $M2$ transitions can be determined from the previous measurement and the 3P_2 hyperfine splittings. Guided by this calculation we observe the $^1S_0\text{-}^3P_2$ ($F' = 5/2$) transition by direct optical excitation. Since it is an $M2$ transition it is expected to be much weaker than the HFM-E1 lines, and we indeed must use about 10 times larger intensity and a 20 times longer illumination time to induce observable atom loss on this transition compared to the case of the dipole transitions. Figure 6 shows a spectrum of this line recorded with a spectroscopy beam power of 4.5 mW and an illumination time of 10 s.

Based on our measurement of the $^1S_0\text{-}^3P_2$ transition and the previously reported results for the $^1S_0\text{-}^3P_1$ and $^3P_1\text{-}^3S_1$ transition frequencies and hyperfine splittings of all mentioned states [60,64], we can also give a more accurate value for the 3P_2 ($F = 7/2$)- 3S_1 ($F' = 7/2$) repump transition frequency, which evaluates to 423 914 969(30) MHz. The corresponding

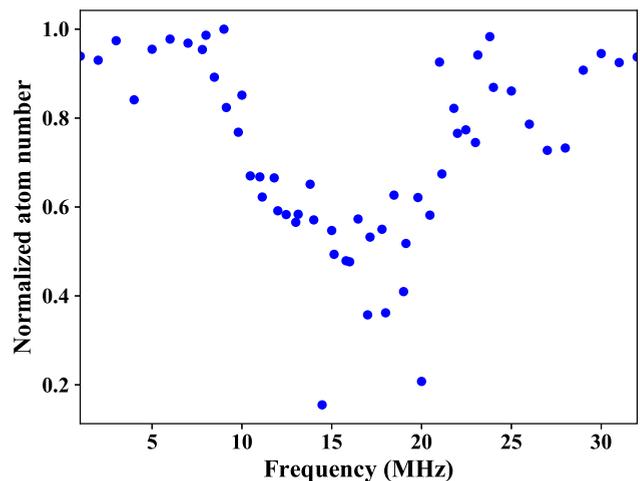


FIG. 6. Spectrum of the 1S_0 ($F = 9/2$)- 3P_2 ($F' = 5/2$) $M2$ transition with a spectroscopy beam power of 4.5 mW. The zero of the frequency axis is chosen arbitrarily.

values involving any other hyperfine states can be easily calculated from the known hyperfine splittings [60,64].

C. Error analysis

We measure absolute frequencies in two ways: using the wavemeter or using iodine lines as reference [45]. Both methods have an uncertainty of 30 MHz, which dominates all other sources of error. We also determine the relative frequency between the Sr transitions and the iodine lines. The error in the relative frequency is much smaller than the absolute error and will be discussed in the following.

The error in the relative frequency measurement has statistical and systematic components. Statistical errors arise from the drifts of the Fabry-Perot resonator to which the laser is locked, from errors in the fits used to determine the center of spectral lines, and from iodine line shifts by iodine temperature and pressure changes [69,70]. Systematic errors are the collisional shifts of the iodine lines, which effectively move our frequency reference point from its literature value [69], and the ac Stark shift of the Sr transitions by the dipole trap light.

The dominant contribution to the statistical error comes from changes of the cavity resonance to which the spectroscopy laser is locked while the measurements are performed. This error is estimated by recording iodine spectra several times before, during, and after the one-hour timespan during which the Sr spectra are recorded, and then analyzing the drift of the relative frequency between the cavity resonance and the iodine lines. We assume that the iodine lines do not change significantly over this timespan (the validity of that assumption will be analyzed below), therefore the drift is due to changes of the resonator frequency. The maximum drift we observe is 250 kHz.

Errors also originate from pressure and temperature shifts of the iodine lines. Compared to a zero temperature and pressure gas the iodine lines are shifted by $\delta f_{I_2} = \alpha_S P_2 T^{-7/10}$ at pressure P and temperature T , where $\alpha_S = -400(60)$ kHz K^{7/10} Pa⁻¹ is an empirically determined proportionality constant [69]. P_2 is set by the cold finger temperature, and the relevant iodine vapor pressure equation is given in Ref. [51], whereas T is set by the iodine cell body temperature. Statistical errors arise from uncertainties in P and T . The cold finger temperature uncertainty of 0.3 K translates into a pressure uncertainty below 1 Pa. The body temperature has an uncertainty below 20 K. These uncertainties lead to a statistical error of 3 kHz in the iodine line frequency. The systematic shift of the iodine lines is $\delta f_{I_2} = -100(15)$ kHz, where the dominant contribution to the error arises from

uncertainties in α_S . The values reported in Table II are given in the presence of this shift.

Another source of error is the light shift induced on the Sr transition by the ODT. We obtain an upper limit for this shift by recording spectra using ODT depths up to a factor 2 higher or lower than the depth used usually. We do not observe a correlation of the transition frequency with the ODT depth, which we attribute to drifts of the reference resonator during the few hours that we spent to record this data. We conclude that the light shifts are at the most as large as the resonator drifts of 250 kHz, which is consistent with a calculation using the Sr transition strengths of [71]. Adding statistical and systematic errors we arrive at a total error of 0.5 MHz. The Sr spectroscopy lines are broadened by ODT light shifts, the Doppler effect, Zeeman shifts of the unresolved m_F levels, and collisional effects.

IV. CONCLUSION

We have determined the frequency of the $^{87}\text{Sr } ^1S_0\text{-}^3P_2$ transition with an accuracy of 30 MHz and the frequency difference of that transition to molecular iodine lines with an accuracy of 0.5 MHz. This knowledge enables the use of simple iodine spectroscopy to find the $^{87}\text{Sr } ^1S_0\text{-}^3P_2$ transition frequency or to lock a Sr $^1S_0\text{-}^3P_2$ laser. Our work prepares the use of this Sr transition for applications, such as quantum simulation or computation.

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