Measurement of the top quark mass in the $t\bar{t} \rightarrow$ lepton+jets channel from $\sqrt{s} =$8 TeV ATLAS data and combination with previous results

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Abstract The top quark mass is measured using a template method in the $t\bar{t} \rightarrow$ lepton+jets channel (lepton is $e$ or $\mu$) using ATLAS data recorded in 2012 at the LHC. The data were taken at a proton–proton centre-of-mass energy of $\sqrt{s} = 8$ TeV and correspond to an integrated luminosity of 20.2 fb$^{-1}$. The $t\bar{t} \rightarrow$ lepton+jets channel is characterized by the presence of a charged lepton, a neutrino and four jets, two of which originate from bottom quarks ($b$). Exploiting a three-dimensional template technique, the top quark mass is determined together with a global jet energy scale factor and a relative $b$-to-light-jet energy scale factor. The mass of the top quark is measured to be $m_{\text{top}} = 172.08 \pm 0.39$ (stat) $\pm 0.82$ (syst) GeV. A combination with previous ATLAS $m_{\text{top}}$ measurements gives $m_{\text{top}} = 172.69 \pm 0.25$ (stat) $\pm 0.41$ (syst) GeV.

1 Introduction

The mass of the top quark $m_{\text{top}}$ is an important parameter of the Standard Model (SM). Precise measurements of $m_{\text{top}}$ provide crucial information for global fits of electroweak parameters [1–3] which help to assess the internal consistency of the SM and probe its extensions. In addition, the value of $m_{\text{top}}$ affects the stability of the SM Higgs potential, which has cosmological implications [4–6].

Many measurements of $m_{\text{top}}$ in each $t\bar{t}$ decay channel were performed by the Tevatron and LHC collaborations. The most precise measurements per experiment in the $t\bar{t} \rightarrow$ lepton+jets channel are $m_{\text{top}} = 172.85 \pm 0.71$ (stat) $\pm 0.84$ (syst) GeV by CDF [7], $m_{\text{top}} = 174.98 \pm 0.58$ (stat) $\pm 0.49$ (syst) GeV by D0 [8], $m_{\text{top}} = 172.33 \pm 0.75$ (stat) $\pm 1.03$ (syst) GeV by ATLAS [9] and $m_{\text{top}} = 172.35 \pm 0.16$ (stat) $\pm 0.48$ (syst) GeV by CMS [10]. Combinations are performed, by either the individual experiments, or by several Tevatron and LHC experiments [11]. In these combinations, selections of measurements from all $t\bar{t}$ decay channels are used. The latest combinations per experiment are $m_{\text{top}} = 173.16 \pm 0.57$ (stat) $\pm 0.74$ (syst) GeV by CDF [12], $m_{\text{top}} = 174.95 \pm 0.40$ (stat) $\pm 0.64$ (syst) GeV by D0 [13], $m_{\text{top}} = 172.84 \pm 0.34$ (stat) $\pm 0.61$ (syst) GeV by ATLAS [14] and $m_{\text{top}} = 172.44 \pm 0.13$ (stat) $\pm 0.47$ (syst) GeV by CMS [10].

In this paper, an ATLAS measurement of $m_{\text{top}}$ in the $t\bar{t} \rightarrow$ lepton+jets channel is presented. The result is obtained from $pp$ collision data recorded in 2012 at a centre-of-mass energy of $\sqrt{s} = 8$ TeV with an integrated luminosity of about 20.2 fb$^{-1}$. The analysis exploits the decay $t\bar{t} \rightarrow W^+W^-b\bar{b} \rightarrow \ell\nu q\bar{q}'b\bar{b}$, which occurs when one $W$ boson decays into a charged lepton ($\ell$ is $e$ or $\mu$ including $\tau \rightarrow e, \mu$ decays) and a neutrino ($\nu$), and the other into a pair of quarks. In the analysis presented here, $m_{\text{top}}$ is obtained from the combined sample of events selected in the electron+jets and muon+jets final states. Single-top-quark events with the same reconstructed final states contain information about the top quark mass and are therefore included as signal events.

The measurement uses a template method, where simulated distributions are constructed for a chosen quantity sensitive to the physics parameter under study using a number of discrete values of that parameter. These templates are fitted to functions that interpolate between different input values of the physics parameter while fixing all other parameters of the functions. In the final step, an unbinned likelihood fit to the observed data distribution is used to obtain the value of the physics parameter that best describes the data. In this procedure, the experimental distributions are constructed such that fits to them yield unbiased estimators of the physics parameter used as input in the signal Monte Carlo (MC) samples. Consequently, the top quark mass determined in this way corresponds to the mass definition used in the MC simulation. Because of various steps in the event simulation, the mass measured in this way does not necessarily directly coincide with mass definitions within a given renormalization scheme.
e.g. the top quark pole mass. Evaluating these differences is a topic of theoretical investigations [15–19].

The measurement exploits the three-dimensional template fit technique presented in Ref. [9]. To reduce the uncertainty in $m_{\text{top}}$ stemming from the uncertainties in the jet energy scale (JES) and the additional $b$-jet energy scale (bJES), $m_{\text{top}}$ is measured together with the jet energy scale factor (JSF) and the relative $b$-to-light-jet energy scale factor (bJSF). Given the larger data sample than used in Ref. [9], the analysis is optimized to reject combinatorial background arising from incorrect matching of the observed jets to the daughters arising from the top quark decays, thereby achieving a better balance of the statistical and systematic uncertainties and reducing the total uncertainty. Given this new measurement, an update of the ATLAS combination of $m_{\text{top}}$ measurements is also presented.

This document is organized as follows. After a short description of the ATLAS detector in Sect. 2, the data and simulation samples are discussed in Sect. 3. Details of the event selection are given in Sect. 4, followed by the description of the reconstruction of the three observables used in the template fit in Sect. 5. The optimization of the event selection using a multivariate analysis approach is presented in Sect. 6. The template fits are introduced in Sect. 7. The evaluation of the systematic uncertainties and their statistical uncertainties are discussed in Sect. 8, and the measurement of $m_{\text{top}}$ is given in Sect. 9. The combination of this measurement with previous ATLAS results is discussed in Sect. 10 and compared with measurements of other experiments. The summary and conclusions are given in Sect. 11. Additional information about the optimization of the event selection and on specific uncertainties in the new measurement of $m_{\text{top}}$ in the $t\bar{t} \rightarrow \text{lepton + jets}$ channel are given in Appendix A, while Appendix B contains information about various combinations performed, together with comparisons with results from other experiments.

2 The ATLAS experiment

The ATLAS experiment [20] at the LHC is a multipurpose particle detector with a forward–backward symmetric cylindrical geometry and a near $4\pi$ coverage in the solid angle. It consists of an inner tracking detector surrounded by a thin superconducting solenoid providing a 2 T axial magnetic field, electromagnetic and hadronic calorimeters, and a muon spectrometer. The inner tracking detector covers the pseudorapidity range $|\eta| < 2.5$. It consists of silicon pixel, silicon microstrip, and transition radiation tracking detectors. Lead/liquid-argon (LAr) sampling calorimeters provide electromagnetic (EM) energy measurements with high granularity. A hadronic (steel/scintillator-tile) calorimeter covers the central pseudorapidity range ($|\eta| < 1.7$). The endcap and forward regions are instrumented with LAr calorimeters for both the EM and hadronic energy measurements up to $|\eta| = 4.9$. The muon spectrometer surrounds the calorimeters and is based on three large air-core toroid superconducting magnets with eight coils each. Its bending power is 2.0 to 7.5 T m. It includes a system of precision tracking chambers and fast detectors for triggering.

A three-level trigger system was used to select events. The first-level trigger is implemented in hardware and used a subset of the detector information to reduce the accepted rate to at most 75 kHz. This is followed by two software-based trigger levels that together reduced the accepted event rate to 400 Hz on average depending on the data-taking conditions during 2012.

3 Data and simulation samples

The analysis is based on $pp$ collision data recorded by the ATLAS detector in 2012 at a centre-of-mass energy of $\sqrt{s} = 8$ TeV. The integrated luminosity is 20.2 fb$^{-1}$ with an uncertainty of 1.9% [21]. The modelling of top quark pair ($t\bar{t}$) and single-top-quark signal events, as well as most background processes, relies on MC simulations. For the simulation of $t\bar{t}$ and single-top-quark events, the POWHEG-Box v1 [22–24] program was used. Within this framework, the simulations of the $t\bar{t}$ [25] and single-top-quark production in the $s$- and $t$-channels [26] and the $W$-channel [27] used matrix elements at next-to-leading order (NLO) in the strong coupling constant $\alpha_S$ with the NLO CT10 [28] parton distribution function (PDF) set and the $h_{\text{damp}}$ parameter set to infinity. Using $m_{\text{top}}$ and the top quark transverse momentum $p_T$ for the underlying leading-order Feynman diagram, the dynamic factorization and renormalization scales were set to $\sqrt{m_{\text{top}}^2 + p_T^2}$. The PYTHIA (v6.425) program [29] with the P2011C [30] set of tuned parameters (tune) and the corresponding CTEQ6L1 PDFs [31] provided the parton shower, hadronization and underlying-event modelling.

For $m_{\text{top}}$ hypothesis testing, the $t\bar{t}$ and single-top-quark event samples were generated with five different assumed

\[ h_{\text{damp}} \] the $p_T$ of the first additional emission beyond the leading-order Feynman diagram in the parton shower and therefore regulates the high-$p_T$ emission against which the $t\bar{t}$ system recoils.
values of $m_{\text{top}}$ in the range from 167.5 to 177.5 GeV in steps of 2.5 GeV. The integrated luminosity of the simulated $t\bar{t}$ sample with $m_{\text{top}} = 172.5$ GeV is about 360 fb$^{-1}$. Each of these MC samples is normalized according to the best available cross-section calculations. For $m_{\text{top}} = 172.5$ GeV, the $t\bar{t}$ cross-section is $\sigma_{t\bar{t}} = 253^{+13}_{-15}$ pb, calculated at next-to-next-to-leading order (NNLO) with next-to-next-to-leading logarithmic soft gluon terms [32–36] with the Top++ 2.0 program [37]. The PDF- and $\alpha_S$-induced uncertainties in this cross-section were calculated using the PDF4LHC prescription [38] with the MSTW2008 68% CL NNLO PDF [39,40], CT10 NNLO PDF [28,41] and NNPDF2.3 5f FFN PDF [42] and were added in quadrature with the uncertainties obtained from the variation of the factorization and renormalization scales by factors of 0.5 and 2.0. The cross-sections for single-top-quark production were calculated at NLO and are $\sigma_{t} = 87.8^{+3.4}_{-1.9}$ pb [43], $\sigma_{Wt} = 22.4 \pm 1.5$ pb [44] and $\sigma_{s} = 5.6 \pm 0.2$ pb [45] in the $t-, Wt$- and the $s$-channels, respectively.

The ALPGEN (v2.13) program [46] interfaced to the PYTHIA6 program was used for the simulation of the production of $W^\pm$ or $Z$ bosons in association with jets. The CTEQ6L1 PDFs and the corresponding AUE2tune [47] were used for the matrix element and parton shower settings. The $W+$jets and $Z+$jets events containing heavy-flavour (HF) quarks ($Wb\bar{b}+$jets, $Zb\bar{b}+$jets, $Wc\bar{c}+$jets, $Zc\bar{c}+$jets, and $Wc+$jets) were generated separately using leading-order (LO) matrix elements with massive bottom and charm quarks. Double-counting of HF quarks in the matrix element and the parton shower evolution was avoided via a HF overlap-removal procedure that used the $\Delta R$ between the additional heavy quarks as the criterion. If the $\Delta R$ was smaller than 0.4, the parton shower prediction was taken, while for larger values, the matrix element prediction was used. The $Z+$jets sample is normalized to the inclusive NNLO calculation [48]. Due to the large uncertainties in the overall $W+$jets normalization and the flavour composition, both are estimated using data-driven techniques as described in Sect. 4.2. Diboson production processes ($WW$, $WZ$ and $ZZ$) were simulated using the ALPGEN program with CTEQ6L1 PDFs interfaced to the HERWIG (v6.520) [49] and JIMMY (v4.31) [50] programs. The samples are normalized to their predicted cross-sections at NLO [51].

All samples were simulated taking into account the effects of multiple soft $pp$ interactions (pile-up) that are present in the 2012 data. These interactions were modelled by overlaying simulated hits from events with exactly one inelastic collision per bunch crossing with hits from minimum-bias events produced with the PYTHIA (v8.160) program [52] using the A2 tune [53] and the MSTW2008 LO PDF. The number of additional interactions is Poisson-distributed around the mean number of inelastic $pp$ interactions per bunch crossing $\mu$. For a given simulated hard-scatter event, the value of $\mu$ depends on the instantaneous luminosity and the inelastic $pp$ cross-section, taken to be 73 mb [21]. Finally, the simulation sample is reweighted such as to match the pile-up observed in data.

A simulation [54] of the ATLAS detector response based on GEANT4 [55] was performed on the MC events. This simulation is referred to as full simulation. The events were then processed through the same reconstruction software as the data. A number of samples used to assess systematic uncertainties were produced bypassing the highly computing-intensive full GEANT4 simulation of the calorimeters. They were produced with a faster version of the simulation [56], which retained the full simulation of the tracking but used a parameterized calorimeter response based on resolution functions measured in full simulation samples. This simulation is referred to as fast simulation.

4 Object reconstruction, background estimation and event preselection

The reconstructed objects resulting from the top quark pair decay are electron and muon candidates, jets and missing transverse momentum ($E_{T}^{\text{miss}}$). In the simulated events, corrections are applied to these objects based on detailed data-to-simulation comparisons for many different processes, so as to match their performance in data.

4.1 Object reconstruction

Electron candidates [57] are required to have a transverse energy of $E_T > 25$ GeV and a pseudorapidity of the corresponding EM cluster of $|\eta_{\text{cluster}}| < 2.47$ with the transition region $1.37 < |\eta_{\text{cluster}}| < 1.52$ between the barrel and the endcap calorimeters excluded. Muon candidates [58] are required to have transverse momentum $p_T > 25$ GeV and $|\eta| < 2.5$. To reduce the contamination by leptons from HF decays inside jets or from photon conversions, referred to collectively as non-prompt (NP) leptons, strict isolation criteria are applied to the amount of activity in the vicinity of the lepton candidate [57–59].

Jets are built from topological clusters of calorimeter cells [60] with the anti-$k_t$ jet clustering algorithm [61] using a radius parameter of $R = 0.4$. The clusters and jets are calibrated using the local cluster weighting (LCW) and the global sequential calibration (GSC) algorithms, respectively [62–64]. The subtraction of the contributions from pile-up is performed via the jet area method [65]. Jets are calibrated using an energy- and $\eta$-dependent simulation-based scheme with in situ corrections based on data [63]. Jets originating from pile-up interactions are identified via their jet vertex fraction (JVF), which is the $p_T$ fraction of associated tracks stemming from the primary vertex. The requirement JVF > 0.5 is applied solely to jets with $p_T < 50$ GeV.
and $|\eta| < 2.4$ \cite{65}. Finally, jets are required to satisfy $p_T > 25$ GeV and $|\eta| < 2.5$.

Muons reconstructed within a $\Delta R = 0.4$ cone around the axis of a jet with $p_T > 25$ GeV are excluded from the analysis. In addition, the closest jet within a $\Delta R = 0.2$ cone around an electron candidate is removed, and then electrons within a $\Delta R = 0.4$ cone around any of the remaining jets are discarded.

The identification of jets containing reconstructed $b$-hadrons, called $b$-tagging, is used for event reconstruction and background suppression. In the following, irrespective of their origin, jets tagged by the $b$-tagging algorithm are referred to as $b$-tagged jets, whereas those not tagged are referred to as untagged jets. Similarly, whether they are tagged or not, jets containing $b$-hadrons in simulation are referred to as $b$-jets and those containing only lighter-flavour hadrons from $u, d, c, s$-quarks, or originating from gluons, are collectively referred to as light-jets. The working point of the neural-network-based MV1 b-tagging algorithm \cite{66} corresponds to an average $b$-tagging efficiency of 70\% for $b$-jets in simulated $t\bar{t}$ events and rejection factors of 5 for jets containing a $c$-hadron and 140 for jets containing only lighter-flavour hadrons. To match the $b$-tagging performance in the data, $p_T$- and $\eta$-dependent scale factors, obtained from dijet and $t\bar{t} \rightarrow$ dilepton events, are applied to MC jets depending on their generated quark flavour, as described in Refs. \cite{66–68}.

The missing transverse momentum $E_T^{\text{miss}}$ is the absolute value of the vector $E_T^{\text{miss}}$ calculated from the negative vectorial sum of all transverse momenta. The vectorial sum takes into account all energy deposits in the calorimeters projected onto the transverse plane. The clusters are corrected using the calibrations that belong to the associated physics object. Muons are included in the calculation of the $E_T^{\text{miss}}$ using their momentum reconstructed in the inner tracking detectors \cite{69}.

4.2 Background estimation

The contribution of events falsely reconstructed as $t\bar{t} \rightarrow$ lepton + jets due to the presence of objects misidentified as leptons (fake leptons) and NP leptons originating from HF decays, is estimated from data using the matrix-method \cite{70}. The technique employed uses $\eta$- and $p_T$-dependent efficiencies for NP/fake-leptons and prompt-leptons. They are measured in a background-enhanced control region with low $E_T^{\text{miss}}$ and from events with dilepton masses around the $Z$ boson peak \cite{71}, respectively. For the $W$+jets background, the overall normalization is estimated from data. The estimate is based on the charge-asymmetry method \cite{72}, relying on the fact that at the LHC more $W^+$ than $W^-$ bosons are produced. In addition, a data-driven estimate of the $Wbb$, $Wc\bar{c}$, $Wc$ and $W$+light-jet fractions is performed in events with exactly two jets and at least one $b$-tagged jet. Further details are given in Ref. \cite{73}. The $Z$+jets and diboson background processes are normalized to their predicted cross-sections as described in Sect. 3.

4.3 Event preselection

Triggering of events is based solely on the presence of a single electron or muon, and no information from the hadronic final state is used. A logical OR of two triggers is used for each of the $t\bar{t} \rightarrow$ electron + jets and $t\bar{t} \rightarrow$ muon + jets channels. The triggers with the lower thresholds of 24 GeV for electrons or muons select isolated leptons. The triggers with the higher thresholds of 60 GeV for electrons and 36 GeV for muons do not include an isolation requirement. The further selection requirements closely follow those in Ref. \cite{9} and are

- Events are required to have at least one primary vertex with at least five associated tracks. Each track needs to have a minimum $p_T$ of 0.4 GeV. For events with more than one primary vertex, the one with the largest $\sum p_T^2$ is chosen as the vertex from the hard scattering.
- The event must contain exactly one reconstructed charged lepton, with $E_T > 25$ GeV for electrons and $p_T > 25$ GeV for muons, that matches the charged lepton that fired the corresponding lepton trigger.
- In the $t\bar{t} \rightarrow$ muon + jets channel, $E_T^{\text{miss}} > 20$ GeV and $E_T^{\text{miss}} + m_W^\ell > 60$ GeV are required.
- In the $t\bar{t} \rightarrow$ electron + jets channel, more stringent requirements on $E_T^{\text{miss}}$ and $m_W^\ell$ are applied because of the higher level of NP/fake-lepton background. The requirements are $E_T^{\text{miss}} > 30$ GeV and $m_W^\ell > 30$ GeV.
- The presence of at least four jets with $p_T > 25$ GeV and $|\eta| < 2.5$ is required.
- The presence of exactly two $b$-tagged jets is required.

The resulting event sample is statistically independent of the ones used for the measurement of $m_{t\bar{t}}$ in the $t\bar{t} \rightarrow$ dilepton and $t\bar{t} \rightarrow$ all jets channels at $\sqrt{s} = 8$ TeV \cite{14,74}. The observed number of events in the data after this preselection and the expected numbers of signal and background events corresponding to the same integrated luminosity as the data are given in Table 1. For all predictions, the uncertainties are estimated as the sum in quadrature of the statistical uncertainty, the uncertainty in the integrated luminosity and all systematic uncertainties assigned to the measurement of $m_{t\bar{t}}$ listed in Sect. 8, except for the PDF and pile-up uncertainties, which are small. The normalization uncertainties listed

$$m_W^\ell = \sqrt{2 p_T \ell (1 - \cos \phi(\ell, E_T^{\text{miss}}))},$$

where $E_T^{\text{miss}}$ provides an estimate of the transverse momentum of the neutrino.
The observed numbers of events in data after the event preselection and the BDT selection (see Sect. 6). In addition, the expected numbers of signal events for $m_{\text{top}} = 172.5 \text{ GeV}$ and background events corresponding to the same integrated luminosity as the data are given. The uncertainties in the predicted number of events take into account the statistical and systematic sources explained in Sect. 4.3. Two significant digits are used for the uncertainties in the predicted events.

<table>
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<th>Selection</th>
<th>Preselection</th>
<th>BDT selection</th>
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</thead>
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<td>38054</td>
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<td>$36100 \pm 5500$</td>
</tr>
<tr>
<td>Single-top-quark signal</td>
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<td>883 $\pm$ 85</td>
</tr>
<tr>
<td>NP/fake leptons (data-driven)</td>
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<td>9.2 $\pm$ 9.2</td>
</tr>
<tr>
<td>$W$ +jets (data-driven)</td>
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<td>300 $\pm$ 100</td>
</tr>
<tr>
<td>$Z$ +jets</td>
<td>430 $\pm$ 230</td>
<td>58 $\pm$ 33</td>
</tr>
<tr>
<td>$W$/$W$/$W$/$Z$/ZZ</td>
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<td>7.0 $\pm$ 5.2</td>
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<tr>
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<td>Data/(signal+background)</td>
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</tr>
</tbody>
</table>

Values below are included for the predictions shown in this section, but due to their small effect on the measured top quark mass they are not included in the final measurement.

For the signal, the 5.7% uncertainty in the $t\bar{t}$ cross-section introduced in Sect. 3 and a 6.0% uncertainty in the single-top-quark cross-section are used. The latter uncertainty is obtained from the cross-section uncertainties given in Sect. 3 and the fractions of the various single-top-quark production processes after the selection requirements. The background uncertainties contain uncertainties of 48% in the normalization of the diboson and $Z$+jets production processes. These uncertainties are calculated using Berends–Giele scaling [75]. Assuming a top quark mass of $m_{\text{top}} = 172.5 \text{ GeV}$, the predicted number of events is consistent within uncertainties with the number observed in the data.

5 Reconstruction of the three observables

As in Ref. [9], a full kinematic reconstruction of the event is done with a likelihood fit using the KLFITTER package [76,77]. The KLFITTER algorithm relates the measured kinematics of the reconstructed objects to the leading-order representation of the $t\bar{t}$ system decay using $t\bar{t} \rightarrow \ell \nu b_{\text{lep}} q_1 q_2 b_{\text{had}}$. In this procedure, the measured jets correspond to the quark decay products of the $W$ boson, $q_1$ and $q_2$, and to the $b$-quarks, $b_{\text{lep}}$ and $b_{\text{had}}$, produced in the semileptonic and hadron top quark decays, respectively.

The event likelihood is the product of Breit–Wigner (BW) distributions for the $W$ bosons and top quarks and transfer functions (TFs) for the energies of the reconstructed objects that are input to KLFITTER. The $W$ boson BW distributions use the world combined values of the $W$ boson mass and decay width from Ref. [3]. A common mass parameter $m_{\text{top}}^{\text{reco}}$ is used for the BW distributions describing the semileptonically and hadronically decaying top quarks and is fitted event-by-event. The top quark width varies with $m_{\text{top}}^{\text{reco}}$ according to the SM prediction [3]. The TFs are derived from the POWHEG+PYTHA $t\bar{t}$ signal MC simulation sample at an input mass of $m_{\text{top}} = 172.5 \text{ GeV}$. They represent the experimental resolutions in terms of the probability that the observed energy at reconstruction level is produced by a given parton-level object for the leading-order decay topology and in the fit constrain the variations of the reconstructed objects.

The input objects to the event likelihood are the reconstructed charged lepton, the missing transverse momentum and up to six jets. These are the two $b$-tagged jets and the four untagged jets with the highest $p_T$. The $x$- and $y$-components of the missing transverse momentum are starting values for the neutrino transverse-momentum components, and its longitudinal component $p_{\nu z}$ is a free parameter in the kinematic likelihood fit. Its starting value is computed from the $W \rightarrow \ell \nu$ mass constraint. If there are no real solutions for $p_{\nu z}$, a starting value of zero is used. If there are two real solutions, the one giving the largest likelihood value is taken.

Maximizing the event-by-event likelihood as a function of $m_{\text{top}}^{\text{reco}}$ establishes the best assignment of reconstructed jets to partons from the $t\bar{t} \rightarrow$ lepton + jets decay. The maximization is performed by testing all possibilities for assigning $b$-tagged jets to $b$-quark positions and untagged jets to light-quark positions. With the above settings of the reconstruction algorithm, compared with the settings used in Ref. [9], a larger fraction of correct assignments of reconstructed jets to partons from the $t\bar{t} \rightarrow$ lepton + jets decay is achieved. The performance of the reconstruction algorithm is discussed in Sect. 6.

The value of $m_{\text{top}}^{\text{reco}}$ obtained from the kinematic likelihood fit is used as the observable primarily sensitive to the underlying $m_{\text{top}}$. The invariant mass of the hadronically decaying $W$ boson $m_{W}^{\text{reco}}$, which is sensitive to the JES, is calculated from the assigned jets of the chosen permutation. Finally, an observable called $R_{bq}^{\text{reco}}$, designed to be sensitive to the JES, is computed as the scalar sum of the transverse momenta of the two $b$-tagged jets divided by the scalar sum of the transverse momenta of the two jets associated with the hadronic $W$ boson decay:

$$R_{bq}^{\text{reco}} = \frac{p_{T}^{b_{\text{had}}} + p_{T}^{b_{\text{lep}}}}{p_{T}^{q_1} + p_{T}^{q_2}}.$$
The values of $m_{w}^{\text{reco}}$ and $R_{bq}^{\text{reco}}$ are computed from the jet four-vectors as given by the jet reconstruction instead of using the values obtained in the kinematic likelihood fit. This ensures the maximum sensitivity to the jet calibration for light-jets and $b$-jets.

Some distributions of the observed event kinematics after the event preselection and for the best permutation are shown in Fig. 1. Given the good description of the observed number of events by the prediction shown in Sect. 4.3 and that the measurement of $m_{\text{top}}$ is mostly sensitive to the shape of the distributions, the comparison of the data with the predictions is based solely on the distributions normalized to the number of events observed in data. The systematic uncertainty assigned to each bin is calculated from the sum in quadrature of all systematic uncertainties discussed in Sect. 4.3. Within uncertainties, the predictions agree with the observed distributions in Fig. 1, which shows the transverse momentum of the lepton, the average transverse momentum of the jets, the transverse momentum of the hadronically decaying top quark $p_{T\text{,had}}$, the transverse momentum of the $t\bar{t}$ system, the logarithm of the event likelihood of the best permutation and the distance $\Delta R$ of the two untagged jets $q_1$ and $q_2$ assigned to the hadronically decaying $W$ boson. The distributions of transverse momenta predicted by the simulation, e.g. the $p_{T\text{,had}}$ distribution shown in Fig. 1c, show a slightly different trend than observed in data, with the data being softer. This difference is fully covered by the uncertainties. This trend was also observed in Ref. [14] for the $p_{T\text{,bq}}$ distribution in the $t\bar{t}$ → dilepton channel and in the measurement of the differential $t\bar{t}$ cross-section in the lepton+jets channel [78].

In anticipation of the template parameterization described in Sect. 7, the following restrictions on the three observables are applied: $125 \leq m_{\text{top}}^{\text{reco}} \leq 200$ GeV, $55 \leq m_{W}^{\text{reco}} \leq 110$ GeV, and $0.3 \leq R_{bq}^{\text{reco}} \leq 3$. Since in this analysis only the best permutation is considered, events that do not pass these requirements are rejected. This removes events in the tails of the three distributions, which are typically poorly reconstructed with small likelihood values and do not contain significant information about $m_{\text{top}}$. The resulting templates have simpler shapes, which are easier to model analytically with fewer parameters. The preselection with these additional requirements is referred to as the standard selection to distinguish it from the boosted decision tree (BDT) optimization for the smallest total uncertainty in $m_{\text{top}}$, discussed in the next section.

6 Multivariate analysis and BDT event selection

For the measurement of $m_{\text{top}}$, the event selection is refined enriching the fraction of events with correct assignments of reconstruction-level objects to their generator-level counter-part which should be better measured and therefore lead to smaller uncertainties. The optimization of the selection is based on the multivariate BDT algorithm implemented in the TMVA package [79]. The reconstruction-level objects are matched to the closest parton-level object within a $\Delta R$ of 0.1 for electrons and muons and 0.3 for jets. A matched object is defined as a reconstruction-level object that falls within the relevant $\Delta R$ of any parton-level object of that type, and a correct match means that this generator-level object is the one it originated from. Due to acceptance losses and reconstruction inefficiencies, not all reconstruction-level objects can successfully be matched to their parton-level counterparts. If any object cannot be unambiguously matched, the corresponding event is referred to as unmatched. The efficiency for correctly matched events $\epsilon_{\text{cm}}$ is the fraction of correctly matched events among all the matched events, and the selection purity $\pi_{\text{cm}}$ is the fraction of correctly matched events among all selected events, regardless of whether they could be matched or not.

The BDT algorithm is exploited to enrich the event sample in events that have correct jet-to-parton matching by reducing the remainder, i.e. the sum of incorrectly matched and unmatched events. Using the preselection, the BDT algorithm is trained on the simulated $t\bar{t}$ signal sample with $m_{\text{top}} = 172.5$ GeV. Many variables were studied and only those with a separation$^5$ larger than 0.1% are used in the training. The 13 variables chosen for the final training are given in Table 2. For all input variables to the BDT algorithm, good agreement between the MC predictions and the data is found, as shown in Fig. 1e, f for the examples of the likelihood of the chosen permutation and the opening angle $\Delta R$ of the two untagged jets associated with the $W$ boson decay. These two variables also have the largest separation for the correctly matched events and the remainder. The corresponding distributions for the two event classes are shown in Fig. 2a, b. These figures show a clear separation of the correctly matched events and the remainder. Half the simulation sample is used to train the algorithm and the other half to assess its performance. The significant difference between the distributions of the output value $r_{BDT}$ of the BDT classifier between the two classes of events in Fig. 2c shows their efficient separation by the BDT algorithm. In addition, reasonable agreement is found for the $r_{BDT}$ distributions in simulation and data in Fig. 2d agree within the experimental uncertainties. The above findings justify the application of the BDT approach to the data.

The full $m_{\text{top}}$ analysis detailed in Sect. 8 is performed, except for the evaluation of the small method and pile-up uncertainties described in Sect. 8, for several minimum

\footnote{The chosen definition of the separation is given in Eq. (1) of the TMVA manual [79].}
Fig. 1 Distributions for the events passing the preselection. The data are shown together with the signal-plus-background prediction, normalized to the number of events observed in the data. The hatched area is the uncertainty in the prediction as described in the text. The rightmost bin contains all entries with values above the lower edge of this bin, similarly the leftmost bin contains all entries with values below the upper edge of this bin. a shows the transverse momentum of the lepton, b shows the average transverse momentum of the jets, c shows the transverse momentum of the hadronically decaying top quark, d shows the transverse momentum of the \( t\bar{t} \) system, e shows the logarithm of the event likelihood of the best permutation and f shows the distance \( \Delta R \) of the two untagged jets \( q_1 \) and \( q_2 \) from the hadronically decaying \( W \) boson.
requirements on $r_{\text{BDT}}$ in the range of $[-0.10, 0.05]$ in steps of 0.05 to find the point with smallest total uncertainty. The total uncertainty in $m_{\text{top}}$ together with the various classes of uncertainty sources as a function of $r_{\text{BDT}}$ evaluated in the BDT optimization are shown in Fig. 3. The minimum requirement $r_{\text{BDT}} = -0.05$ provides the smallest total uncertainty in $m_{\text{top}}$. The resulting numbers of events for this BDT selection are given in Table 1. Compared with the preselection, $\epsilon_{\text{cm}}$ is increased from 0.71 to 0.82, albeit at the expense of a significant reduction in the number of selected events. The purity $\pi_{\text{cm}}$ is increased from 0.28 to 0.41. In addition, the intrinsic resolution in $m_{\text{top}}$ of the remaining event sample is improved, i.e. the statistical uncertainty in $m_{\text{top}}$ in Fig. 3 is almost constant as a function of $r_{\text{BDT}}$; in particular, it does not scale with the square root of the number of events retained. For the signal sample with $m_{\text{top}} = 172.5$ GeV, the template fit functions for the standard selection and the BDT selection, together with their ratios, are shown in Fig. 12 in Appendix A. The shape of the signal modelling uncertainty derives from a sum of contributions with different shapes. The curves from the signal Monte Carlo generator and colour reconnection uncertainties decrease, the one from the underlying event uncertainty is flat, the one from the initial- and final-state QCD radiation has a valley similar to the sum of all contributions, and finally the one from the hadronization uncertainty rises.

Some distributions of the observed event kinematics after the BDT selection are shown in Fig. 4. Good agreement between the MC predictions and the data is found, as seen for the preselection in Fig. 1. The examples shown are the observed $W$ boson transverse mass for the semi-leptonically decaying top quark in Fig. 4a and the three observables of the $m_{\text{top}}$ analysis (within the ranges of the template fit) in Fig. 4b–d. The sharp edge observed at 30 GeV in Fig. 4a originates from the different selection requirements for the $W$ boson transverse mass in the electron+jets and muon+jets final states.

### 7 Template fit

This analysis uses a three-dimensional template fit technique which determines $m_{\text{top}}$ together with the jet energy scale factors JSF and bJSF. The aim of the multi-dimensional fit to the data is to measure $m_{\text{top}}$ and, at the same time, to absorb the mean differences between the jet energy scales observed in data and MC simulated events into jet energy scale factors. By using JSF and bJSF, most of the uncertainties in $m_{\text{top}}$ induced by JES and bJES uncertainties are transformed into additional statistical components caused by the higher dimensionality of the fit. This method reduces the total uncertainty in $m_{\text{top}}$ only for sufficiently large data samples. In this case, the sum in quadrature of the additional statistical uncertainty in $m_{\text{top}}$ due to the JSF (or bJSF) fit and the residual JES-induced (or bJES-induced) systematic uncertainty is smaller than the original JES-induced (or bJES-induced) uncertainty in $m_{\text{top}}$. This situation was already realized for the $\sqrt{s} = 7$ TeV data analysis [9] and is even more advantageous for the much larger data sample of the $\sqrt{s} = 8$ TeV data analysis. Since JSF and bJSF are global factors, they do not completely absorb the JES and bJES uncertainties which have $p_T$- and $\eta$-dependent components.

For simultaneously determining $m_{\text{top}}$, JSF and bJSF, templates are constructed from the MC samples. Templates of $m_{\text{reco}}$ are constructed with several input $m_{\text{top}}$ values used in the range 167.5–177.5 GeV and for the sample at $m_{\text{top}} = 172.5$ GeV also with independent input values for JSF and bJSF in the range 0.96–1.04 in steps of 0.02. Statistically independent MC samples are used for different input values of $m_{\text{top}}$. The templates with different values of JSF and bJSF are constructed by scaling the energies of the jets appropriately. In this procedure, JSF is applied to all jets, while bJSF is solely applied to $b$-jets according to the generated quark flavour. The scaling is performed after the various correction steps of the jet calibration but before the event selection. This procedure results in different events passing the BDT selection from one energy scale variation to another. However, many events are in all samples, resulting in a large statistical correlation of the samples with different jet scale factors. Similarly, templates of $m_{\text{reco}}$ and $R_{\text{reco}}$ are constructed with the above listed input values of $m_{\text{top}}$, JSF and bJSF.

Independent signal templates are derived for the three observables for all $m_{\text{top}}$-dependent samples, consisting of the $\ell\ell$ signal events and single-top-quark production events. This procedure is adopted because single-top-quark produc-

<table>
<thead>
<tr>
<th>Separation (%)</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>31</td>
<td>Logarithm of the event likelihood of the best permutation, $\ln L$</td>
</tr>
<tr>
<td>13</td>
<td>$\Delta R$ of the two untagged jets $q_1$ and $q_2$ from the hadronically decaying $W$ boson, $\Delta R(q, q)$</td>
</tr>
<tr>
<td>5.0</td>
<td>$p_T$ of the hadronically decaying $W$ boson</td>
</tr>
<tr>
<td>4.3</td>
<td>$p_T$ of the hadronically decaying top quark</td>
</tr>
<tr>
<td>4.2</td>
<td>Relative event probability of the best permutation</td>
</tr>
<tr>
<td>2.0</td>
<td>$p_T$ of the reconstructed $\ell\ell$ system</td>
</tr>
<tr>
<td>1.7</td>
<td>$p_T$ of the semi-leptonically decaying top quark</td>
</tr>
<tr>
<td>1.2</td>
<td>Transverse mass of the leptonically decaying $W$ boson</td>
</tr>
<tr>
<td>0.3</td>
<td>$p_T$ of the leptonically decaying $W$ boson</td>
</tr>
<tr>
<td>0.3</td>
<td>Number of jets</td>
</tr>
<tr>
<td>0.2</td>
<td>$\Delta R$ of the reconstructed $b$-tagged jets</td>
</tr>
<tr>
<td>0.2</td>
<td>$p_T$ of the leptonically decaying $W$ boson</td>
</tr>
<tr>
<td>0.1</td>
<td>Missing transverse momentum</td>
</tr>
</tbody>
</table>

Table 2 The input variables to the BDT algorithm sorted by their separation.
Fig. 2 Input and results of the BDT training on \( \bar{t}t \) signal events for the preselection. a shows the logarithm of the event likelihood of the best permutation (\( \ln L \)) for the correctly matched events and the remainder. Similarly, b shows the distribution of the \( \Delta R \) between the two untagged jets assigned to the \( W \) boson decay. c shows the distribution of the BDT output (\( r_{\text{BDT}} \)) for the two classes of events for both the training (histograms) and test samples (points with statistical uncertainties). The compatibility in terms of the \( \chi^2 \) probability is also listed. The distributions peaking at around \( r_{\text{BDT}} = 0.1 \) are for the correctly matched events, the ones to the left are for incorrectly or unmatched events. The ratio figure shows the difference between the number of events in the training and test samples divided by the statistical uncertainty in this difference. Finally, d shows the comparison of the \( r_{\text{BDT}} \) distributions observed in data and MC simulation. The hatched area includes the uncertainties as detailed in the text. The uncertainty bars correspond to the statistical uncertainties in the data.

...function, while both the \( m_{\text{reco}} \) and the \( R_{\text{bq}}^{\text{reco}} \) distributions are fitted to the sum of two Gaussian functions.

In Fig. 5a–c, the sensitivity of \( m_{\text{reco}} \) to the fit parameters \( m_{\text{top}} \), JSF and bJSF is shown by the superposition of the signal templates and their fits for three input values per varied parameter. In a similar way, the sensitivity of \( m_{\text{reco}} \) to JSF is shown in Fig. 5d. The dependences of \( m_{\text{reco}} \) on the input values of \( m_{\text{top}} \) and bJSF are negligible and are not shown.

...
Consequently, to increase the size of the simulation sample, the fit is performed on the sum of the $m^\text{rec}_W$ distributions of the samples with different input top quark masses. Finally, the sensitivity of $R^\text{reco}_b$ to the input values of $m^\text{top}_\text{rec}$ and bJSF is shown in Fig. 5e, f. The dependence of $R^\text{reco}_b$ on JSF (not shown) is much weaker than the dependence on bJSF.

For the signal, the parameters of the fitting functions for $m^\text{rec}_\text{top}$ depend linearly on $m^\text{rec}_\text{top}$, JSF and bJSF. The parameters of the fitting functions for $m^\text{rec}_W$ depend linearly on JSF. Finally, the parameters of the fitting functions for $R^\text{reco}_b$ depend linearly on $m^\text{rec}_\text{top}$, JSF and bJSF. For the background, the dependences of the parameters of the fitting functions are identical to those for the signal, except that they do not depend on $m^\text{rec}_\text{top}$ and that those for $R^\text{reco}_b$ do not depend on JSF.

Signal and background probability density functions $P^\text{sig}_\text{top}$ and $P^\text{bkg}_\text{top}$ for the $m^\text{rec}_\text{top}$, $m^\text{rec}_W$ and $R^\text{reco}_b$ distributions are used in an unbinned likelihood fit to the data for all events, $i = 1, \ldots, N$. The likelihood function maximized is

$$L_{\text{shape}}(m^\text{rec}_\text{top}, \text{JSF}, \text{bJSF}, f^\text{bkg}) = \prod_{i=1}^{N} P^\text{top}(m^\text{rec}_\text{top}, | m^\text{rec}_\text{top}, \text{JSF}, \text{bJSF}, f^\text{bkg}) \times P^W(m^\text{rec}_W, | \text{JSF}, f^\text{bkg}) \times P^\text{bkg}(R^\text{reco}_b, | m^\text{rec}_\text{top}, \text{JSF}, \text{bJSF}, f^\text{bkg}),$$

with

$$P^\text{top}(m^\text{rec}_\text{top}, | m^\text{rec}_\text{top}, \text{JSF}, \text{bJSF}, f^\text{bkg}) = (1 - f^\text{bkg}) \cdot P^\text{sig}_\text{top}(m^\text{rec}_\text{top}, | m^\text{rec}_\text{top}, \text{JSF}, \text{bJSF}) + f^\text{bkg} \cdot P^\text{bkg}_\text{top}(m^\text{rec}_\text{top}, | \text{JSF}, \text{bJSF}),$$

$$P^W(m^\text{rec}_W, | \text{JSF}, f^\text{bkg}) = (1 - f^\text{bkg}) \cdot P^\text{sig}_W(m^\text{rec}_\text{top}, | \text{JSF}) + f^\text{bkg} \cdot P^\text{bkg}_W(m^\text{rec}_\text{top}, | \text{JSF}),$$

and

$$P^\text{bkg}(R^\text{reco}_b, | m^\text{rec}_\text{top}, \text{JSF}, \text{bJSF}, f^\text{bkg}) = (1 - f^\text{bkg}) \cdot P^\text{sig}_\text{bkg}(R^\text{reco}_b, | m^\text{rec}_\text{top}, \text{JSF}, \text{bJSF}) + f^\text{bkg} \cdot P^\text{bkg}_\text{bkg}(R^\text{reco}_b, | \text{bJSF}),$$

where the fraction of background events is denoted by $f^\text{bkg}$. The parameters determined by the fit are $m^\text{rec}_\text{top}$, JSF and bJSF, while $f^\text{bkg}$ is fixed to its expectation shown in Table 1. It was verified that the correlations between $m^\text{rec}_\text{top}$, $m^\text{rec}_W$ and $R^\text{reco}_b$ of $\rho(m^\text{rec}_\text{top}, m^\text{rec}_W) = 0.05$, $\rho(m^\text{rec}_\text{top}, R^\text{reco}_b) = 0.18$, and $\rho(m^\text{rec}_W, R^\text{reco}_b) = -0.13$, are small enough that formulating the likelihood in Eq. (1) as a product of three one-dimensional likelihoods does not bias the result.

Pseudo-experiments are used to verify the internal consistency of the fitting procedure and to obtain the expected statistical uncertainty for the data. For each set of parameter values, 500 pseudo-experiments are performed, each corresponding to the integrated luminosity of the data. To retain the correlation of the three observables for the three-dimensional fit, individual events are used. Because this exceeds the number of available MC events, results are corrected for oversampling [80]. The results of pseudo-experiments for different input values of $m^\text{rec}_\text{top}$ are obtained from statistically independent samples, while the results for different JSF and bJSF are obtained from statistically correlated samples as explained above. For each fitted quantity and each variation of input parameters, the residual, i.e. the difference between the input value and the value obtained by the fit, is compatible with zero. The three expected statistical uncertainties are

$$\sigma_{\text{stat}}(m^\text{rec}_\text{top}) = 0.389 \pm 0.004 \text{ GeV},$$

$$\sigma_{\text{stat}}(\text{JSF}) = 0.00115 \pm 0.00001,$$

and

$$\sigma_{\text{stat}}(\text{bJSF}) = 0.0046 \pm 0.0001,$$

where the values quoted are the mean and RMS of the distribution of the statistical uncertainties in the fitted quantities from pseudo-experiments. The widths of the pull distributions are below unity for $m^\text{rec}_\text{top}$ and the two jet scale factors, which results in an overestimation of the uncertainty in $m^\text{rec}_\text{top}$ of up to 7%. Since this leads to a conservative estimate of the uncertainty in $m^\text{rec}_\text{top}$, no attempts to mitigate this feature are made.
Fig. 4 Distributions for the events passing the BDT selection. The data are shown, together with the signal-plus-background prediction normalized to the number of events observed in the data. The hatched area is the uncertainty in the prediction described in the text. The rightmost bin contains all entries with values above the lower edge of this bin, similarly the leftmost bin contains all entries with values below the upper edge of this bin. a shows the $W$ boson transverse mass for the semi-leptonic top quark decay. The remaining figures show the three observables used for the determination of $m_{\text{top}}$, where b shows the reconstructed top quark mass $m_{\text{top}}^\text{reco}$, c shows the reconstructed invariant mass of the $W$ boson $m_{W}^\text{reco}$ and d shows the reconstructed ratio of jet transverse momenta $R_{\text{bq}}^\text{reco}$. The three distributions are shown within the ranges of the template fit.

8 Uncertainties affecting the $m_{\text{top}}$ determination

This section focuses on the treatment of uncertainty sources of a systematic nature. The same systematic uncertainty sources as in Ref. [9] are investigated. If possible, the corresponding uncertainty in $m_{\text{top}}$ is evaluated by varying the respective quantities by $\pm 1 \sigma$ from their default values, constructing the corresponding event sample and measuring the average $m_{\text{top}}$ change relative to the result from the nominal MC sample with 500 pseudo-experiments each, drawn from the full MC sample. In the absence of a $\pm 1 \sigma$ variation, e.g. for the evaluation of the uncertainty induced by the choice of signal MC generator, the full observed difference is assigned as a symmetric systematic uncertainty and further treated as a variation equivalent to a $\pm 1 \sigma$ variation. Whenever a $\pm 1 \sigma$ variation can be performed, half the observed difference between the $+1 \sigma$ and $-1 \sigma$ variation in $m_{\text{top}}$ is assigned as an uncertainty if the $m_{\text{top}}$ values obtained from
Fig. 5 Template parameterizations for signal events, composed of $t\bar{t}$ and single-top-quark production events. a–c show the sensitivity of $m_{\text{reco}}^{\text{top}}$ to $m_{\text{top}}$, JSF and bJSF, d shows the sensitivity of $m_{\text{reco}}^{W}$ to JSF and e, f show the sensitivity of $R_{bq}$ to $m_{\text{top}}$ and bJSF. Each template is overlaid with the corresponding probability density function from the combined fit to all templates described in the text. The ratios shown are calculated relative to the probability density function of the central sample with $m_{\text{top}} = 172.5$ GeV, JSF = 1 and bJSF = 1.
the variations lie on opposite sides of the nominal result. If they lie on the same side, the maximum observed difference is taken as a symmetric systematic uncertainty. Since the systematic uncertainties are derived from simulation or data samples with limited numbers of events, all systematic uncertainties have a corresponding statistical uncertainty, which is calculated taking into account the statistical correlation of the considered samples, as explained in Sect. 8.5. The statistical uncertainty in the total systematic uncertainty is dominated by the limited sizes of the simulation samples. The resulting systematic uncertainties are given in Table 3 independent of their statistical significance. Further information is given in Tables 8, 9, 10, 11 and 12 in Appendix A. This approach follows the suggestion in Ref. [81] and relies on the fact that, given a large enough number of considered uncertainty sources, statistical fluctuations average out. The uncertainty sources are designed to be uncorrelated with each other, and thus the total uncertainty is taken as the sum in quadrature of uncertainties from all sources. The individual uncertainties are compared in Table 3 for three cases: the standard selection for the $\sqrt{s} = 7$ TeV [9] and 8 TeV data and the BDT selection for $\sqrt{s} = 8$ TeV data. Many uncertainties in $m_{\text{top}}$ obtained with the standard selection at the two centre-of-mass energies agree within their statistical uncertainties such that the resulting total systematic uncertainties are almost identical. Consequently, repeating the $\sqrt{s} = 7$ TeV analysis on $\sqrt{s} = 8$ TeV data would have only improved the statistical precision. The picture changes when comparing the uncertainties in $\sqrt{s} = 8$ TeV data for the standard selection and the BDT selection. In general, the experimental uncertainties change only slightly, with the largest reduction observed for the JES uncertainty. In contrast, a large improvement comes from the reduced uncertainties in the modelling of the $t\bar{t}$ signal processes as shown in Table 3. This, together with the improved intrinsic resolution in $m_{\text{top}}$, more than compensates for the small loss in precision caused by the increased statistical uncertainty. The individual sources of systematic

<table>
<thead>
<tr>
<th>Event selection</th>
<th>$\sqrt{s} = 7$ TeV</th>
<th>$\sqrt{s} = 8$ TeV</th>
<th>BDT</th>
</tr>
</thead>
<tbody>
<tr>
<td>$m_{\text{top}}$ result [GeV]</td>
<td>172.33</td>
<td>171.90</td>
<td>172.08</td>
</tr>
<tr>
<td>Statistics</td>
<td>0.75</td>
<td>0.38</td>
<td>0.39</td>
</tr>
<tr>
<td>$-\text{Stat. comp. (n}_{\text{top}}$</td>
<td>0.23</td>
<td>0.12</td>
<td>0.11</td>
</tr>
<tr>
<td>$-\text{Stat. comp. (JSF)}$</td>
<td>0.25</td>
<td>0.11</td>
<td>0.11</td>
</tr>
<tr>
<td>$-\text{Stat. comp. (bJSF)}$</td>
<td>0.67</td>
<td>0.34</td>
<td>0.35</td>
</tr>
<tr>
<td>Method</td>
<td>0.11 ± 0.10</td>
<td>0.04 ± 0.11</td>
<td>0.13 ± 0.11</td>
</tr>
<tr>
<td>Signal Monte Carlo generator</td>
<td>0.22 ± 0.21</td>
<td>0.50 ± 0.17</td>
<td>0.16 ± 0.17</td>
</tr>
<tr>
<td>Hadronization</td>
<td>0.18 ± 0.12</td>
<td>0.05 ± 0.10</td>
<td>0.15 ± 0.10</td>
</tr>
<tr>
<td>Initial- and final-state QCD radiation</td>
<td>0.32 ± 0.06</td>
<td>0.28 ± 0.11</td>
<td>0.08 ± 0.11</td>
</tr>
<tr>
<td>Underlying event</td>
<td>0.15 ± 0.07</td>
<td>0.08 ± 0.15</td>
<td>0.08 ± 0.15</td>
</tr>
<tr>
<td>Colour reconnection</td>
<td>0.11 ± 0.07</td>
<td>0.37 ± 0.15</td>
<td>0.19 ± 0.15</td>
</tr>
<tr>
<td>Parton distribution function</td>
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<td>0.08 ± 0.00</td>
<td>0.09 ± 0.00</td>
</tr>
<tr>
<td>Background normalization</td>
<td>0.10 ± 0.00</td>
<td>0.04 ± 0.00</td>
<td>0.08 ± 0.00</td>
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<tr>
<td>W+jets shape</td>
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<td>0.11 ± 0.00</td>
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<tr>
<td>Fake leptons shape</td>
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<td>0</td>
</tr>
<tr>
<td>Jet energy scale</td>
<td>0.58 ± 0.11</td>
<td>0.63 ± 0.02</td>
<td>0.54 ± 0.02</td>
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<tr>
<td>Relative b-to-light-jet energy scale</td>
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<td>0.05 ± 0.01</td>
<td>0.03 ± 0.01</td>
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<tr>
<td>Jet energy resolution</td>
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<td>0.23 ± 0.03</td>
<td>0.20 ± 0.04</td>
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<td>Jet reconstruction efficiency</td>
<td>0.12 ± 0.00</td>
<td>0.04 ± 0.01</td>
<td>0.02 ± 0.01</td>
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<tr>
<td>Jet vertex fraction</td>
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<td>0.09 ± 0.01</td>
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<tr>
<td>$b$-tagging</td>
<td>0.50 ± 0.00</td>
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<td>Leptons</td>
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<td>0.16 ± 0.01</td>
</tr>
<tr>
<td>Missing transverse momentum</td>
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<td>0.05 ± 0.01</td>
</tr>
<tr>
<td>Pile-up</td>
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<td>0.15 ± 0.01</td>
</tr>
<tr>
<td>Total systematic uncertainty</td>
<td>1.04 ± 0.08</td>
<td>1.07 ± 0.10</td>
<td>0.82 ± 0.06</td>
</tr>
<tr>
<td>Total</td>
<td>1.28 ± 0.08</td>
<td>1.13 ± 0.10</td>
<td>0.91 ± 0.06</td>
</tr>
</tbody>
</table>

Table 3: Systematic uncertainties in $m_{\text{top}}$. The measured values of $m_{\text{top}}$ are given together with the statistical and systematic uncertainties in GeV for the standard and the BDT event selections. For comparison, the result in the $t\bar{t} \rightarrow$ lepton + jets channel at $\sqrt{s} = 7$ TeV from Ref. [9] is also listed. For each systematic uncertainty listed, the first value corresponds to the uncertainty in $m_{\text{top}}$, and the second to the statistical precision in this uncertainty. An integer value of zero means that the corresponding uncertainty is negligible and therefore not evaluated. Statistical uncertainties quoted as 0.00 are smaller than 0.005. The statistical uncertainty in the total systematic uncertainty is calculated from uncertainty propagation. The last line refers to the sum in quadrature of the statistical and systematic uncertainties.

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6 In the limit of many small systematic uncertainties with large statistical uncertainties, this procedure on average leads to an overestimate of the total systematic uncertainty.
uncertainties and the evaluation of their effect on $m_{\text{top}}$ are described in the following.

8.1 Statistics and method calibration

Uncertainties related to statistical effects and the method calibration are discussed here.

Statistical: The quoted statistical uncertainty consists of three parts: a purely statistical component in $m_{\text{top}}$ and the contributions stemming from the simultaneous determination of JSF and $b$JSF. The purely statistical component in $m_{\text{top}}$ is obtained from a one-dimensional template method exploiting only the $m_{\text{top}}^{\text{reco}}$ observable, while fixing the values of JSF and $b$JSF to the results of the three-dimensional analysis. The contribution to the statistical uncertainty in the fitted parameters due to the simultaneous fit of $m_{\text{top}}$ and JSF is estimated as the difference in quadrature between the statistical uncertainty in a two-dimensional fit to $m_{\text{top}}^{\text{reco}}$ and $m_{W}^{\text{reco}}$ while fixing the value of $b$JSF and the one-dimensional fit to the data described above. Analogously, the contribution of the statistical uncertainty due to the simultaneous fit of $m_{\text{top}}$ together with JSF and $b$JSF is defined as the difference in quadrature between the statistical uncertainties obtained in the three-dimensional and the two-dimensional fits to the data. This separation allows a comparison of the statistical sensitivities of the $m_{\text{top}}$ estimator used in this analysis, to those of analyses exploiting a different number of observables in the fit. In addition, the sensitivity of the estimators to the global jet energy scale factors can be compared directly. These uncertainties are treated as uncorrelated uncertainties in $m_{\text{top}}$ combinations. Together with the systematic uncertainty in the residual jet energy scale uncertainties discussed below, they directly replace the uncertainty in $m_{\text{top}}$ from the jet energy scale variations present without the in situ determination.

Method: The residual difference between fitted and generated $m_{\text{top}}$ when analysing a template from a MC sample reflects the potential bias of the method. Consequently, the largest observed fitted $m_{\text{top}}$ residual and the largest observed statistical uncertainty in this quantity, in any of the five signal samples with different assumed values of $m_{\text{top}}$, is assigned as the method calibration uncertainty and its corresponding statistical uncertainty, respectively. This also covers effects from limited numbers of simulated events in the templates and potential deficiencies in the template parameterizations.

8.2 Modelling of signal processes

The modelling of $t\bar{t} \rightarrow$ lepton + jets events incorporates a number of processes that have to be accurately described, resulting in systematic effects, ranging from the $t\bar{t}$ production to the hadronization of the showered objects.

Thanks to the restrictive event-selection requirements, the contribution of non-$t\bar{t}$ processes, comprising the single-top-quark process and the various background processes, is very low. The systematic uncertainty in $m_{\text{top}}$ from the uncertainty in the single-top-quark normalization is estimated from the corresponding uncertainty in the theoretical cross-section given in Sect. 3. The resulting systematic uncertainty is small compared with the systematic uncertainty in the $t\bar{t}$ production and is consequently neglected. For the modelling of the signal processes, the consequence of including single-top-quark variations in the uncertainty evaluation was investigated for various uncertainty sources and found to be negligible. Therefore, the single-top-quark variations are not included in the determination of the signal event uncertainties.

Signal Monte Carlo generator: The full observed difference in fitted $m_{\text{top}}$ between the event samples produced with the POWHEG-BOX and MC@NLO [82,83] programs is quoted as a systematic uncertainty. For the renormalization and factorization scales the POWHEG-BOX sample uses the function given in Sect. 3, while the MC@NLO sample uses $\mu_{R,F} = \sqrt{m_{\text{top}}^{2} + 0.5(p_{T,j}^{2} + p_{T,W}^{2})}$. Both samples are generated with a top quark mass of $m_{\text{top}} = 172.5$ GeV with the CT10 PDFs in the matrix-element calculation and use the HERWIG and JIMMY programs with the ATLAS AUET2 tune [47].

Hadronization: To cover the choice of parton shower and hadronization models, samples produced with the POWHEG-BOX program are showered with either the PYTHIA6 program using the P2011C tune or the HERWIG and JIMMY programs using the ATLAS AUET2 tune. This includes different approaches in shower modelling, such as using a $p_T$-ordered parton showering in the PYTHIA program or angular-ordered parton showering in the HERWIG program, the different parton shower matching scales, as well as fragmentation functions and hadronization models, such as choosing the Lund string model [84,85] implemented in the PYTHIA program or the cluster fragmentation model [86] used in the HERWIG program. The full observed difference between the samples is quoted as a systematic uncertainty.

As shown in Fig. 1, the distributions of transverse momenta in data are slightly softer than those in the POWHEG+PYTHIA MC simulation samples. Similarly to what was observed in the $t\bar{t} \rightarrow$ dilepton channel for the $p_{T,\ell\ell}$ distribution, in the $t\bar{t} \rightarrow$ lepton + jets channel the POWHEG+HERWIG sample is much closer to the data for several distributions of transverse momenta. The $p_{T,\text{had}}$ distribution is much better described by the POWHEG+HERWIG sample as was also observed in Ref. [78]. In addition, but to a lesser extent, the MC@NLO sample used to assess the signal Monte Carlo generator uncertainty and the samples to assess the initial- and final-state QCD radiation uncertainty...
discussed next also lead to a softer distribution in simulation. Given this, the observed difference in the $p_T,\text{had}$ distribution is covered by a combination of the signal-modelling uncertainties given in Table 3.

Despite the fact that the JES and bJES are estimated independently using dijet and other non-$t\bar{t}$ samples [63], some double-counting of hadronization-uncertainty-induced uncertainties in the JES and $m_{\text{top}}$ cannot be excluded. This was investigated closely for the ATLAS top quark mass measurement in the $t\bar{t} \rightarrow \text{lepton} + \text{jets}$ channel at $\sqrt{s} = 7$ TeV. The results in Ref. [87] revealed that the amount of double-counting of JES and hadronization effects for the $t\bar{t} \rightarrow \text{lepton} + \text{jets}$ channel is small.

**Initial- and final-state QCD radiation (ISR/FSR):** ISR/FSR leads to a higher jet multiplicity and different jet energies than the hard process, which affects the distributions of the three observables. The uncertainties due to ISR/FSR modelling are estimated with samples generated with the Powheg-Box program interfaced to the Pythia6 program for which the parameters of the generation are varied to span the ranges compatible with the results of measurements of $t\bar{t}$ production in association with jets [88–90]. This uncertainty is evaluated by comparing two dedicated samples that differ in several parameters, namely the QCD scale $\Lambda_{\text{QCD}}$, the transverse momentum scale for space-like parton-shower evolution $Q^2_{\text{max}}$, the $h_{\text{damp}}$ parameter [91] and the P2012 RADLO and RADHi tunes [30]. In Ref. [90], it was shown that a number of final-state distributions are better accounted for by the Powheg+Pythia samples with $h_{\text{damp}} = m_{\text{top}}$. Therefore, these samples are used for evaluating this uncertainty, taking half the observed difference between the up variation and the down variation sample. Because the parameterizations for the template fit to data are obtained from Powheg+Pythia samples using $h_{\text{damp}} = \infty$, it was verified that, considering the method uncertainty quoted in Table 3, applying the same functions to the $h_{\text{damp}} = m_{\text{top}}$ samples leads to a result compatible with the input top quark mass.

**Underlying event:** To reduce statistical fluctuations in the evaluation of this systematic uncertainty, the difference in underlying-event modelling is assessed by comparing a pair of Powheg-Box samples based on the same partonic events generated with the CT10 PDFs. A sample with the P2012 tune is compared with a sample with the P2012 MPIHI tune [30], with both tunes using the same CTEQ6L1 PDFs [92] for parton showering and hadronization. The Perugia 2012 MPIHI tune provides more semi-hard multiple parton interactions and is used for this comparison with identical colour reconnection parameters in both tunes. The full observed difference is assigned as a systematic uncertainty.

**Colour reconnection:** This systematic uncertainty is estimated using a pair of samples with the same partonic events as for the underlying-event uncertainty evaluation but with the P2012 tune and the P2012 LOCR tune [30] for parton showering and hadronization. The full observed difference is assigned as a systematic uncertainty.

**Parton distribution function (PDF):** The PDF systematic uncertainty is the sum in quadrature of three contributions. These are the sum in quadrature of the differences in fitted $m_{\text{top}}$ for the 26 eigenvector variations of the CT10 PDF and two differences in $m_{\text{top}}$ obtained from reweighting the central CT10 PDF set to the MSTW2008 PDF [39] and the NNPDF2.3 PDF [42].

8.3 Modelling of background processes

Uncertainties in the modelling of the background processes are taken into account by variations of the corresponding normalizations and shapes of the distributions.

**Background normalization:** The normalizations are varied for the data-driven background estimates according to their uncertainties. For the negligible contribution from diboson production, no normalization uncertainty is evaluated.

**Background shape:** For the $W+$jets background, the shape uncertainty is evaluated from the variation of the heavy-flavour fractions. The corresponding uncertainty is small. Given the very small contribution from $Z+$jets, diboson and NP/fake-lepton backgrounds, no shape uncertainty is evaluated for these background sources.

8.4 Detector modelling

The level of understanding of the detector response and of the particle interactions therein is reflected in numerous systematic uncertainties.

**Jet energy scale (JES):** The JES is measured with a relative precision of about 1% to 4%, typically falling with increasing jet $p_T$ and rising with increasing jet $|\eta|$ [93,94]. The total JES uncertainty consists of more than 60 subcomponents originating from the various steps in the jet calibration. The number of these nuisance parameters is reduced with a matrix diagonalization of the full JES covariance matrix including all nuisance parameters for a given category of the JES uncertainty components.

The analyses of $\sqrt{s} = 7$ TeV and $\sqrt{s} = 8$ TeV data make use of the EM+JES and LCW+GSC [93] jet calibrations, respectively. The two calibrations feature different sets of nuisance parameters, and the LCW+GSC calibration generally has smaller uncertainties than the EM+JES calibration. While the pile-up correction for the jet calibration for $\sqrt{s} = 7$ TeV data only depends on the number of primary vertices ($n_{\text{vtx}}$) and the mean number of interactions per bunch crossing ($\langle \mu \rangle$), a pile-up subtraction method based on jet area is introduced for the $\sqrt{s} = 8$ TeV data. Terms to account
for uncertainties in the pile-up estimation are added. They depend on the jet $p_T$ and the local transverse momentum density. In addition, the punch-through uncertainty, i.e. an uncertainty for jets that penetrate through to the muon spectrometer, is added. The final reduced number of nuisance parameters for the $\sqrt{s} = 8$ TeV analysis is 25. The JES-uncertainty-induced uncertainty in $m_{\text{top}}$ is the dominant systematic uncertainty for all results shown in Table 3. When only a one-dimensional fit to $m_{\text{top}}^{\text{reco}}$ or a two-dimensional fit to $m_{\text{top}}^{\text{reco}}$ and $m_{\text{W}}^{\text{reco}}$ is done, this uncertainty is 0.99 GeV or 0.74 GeV, respectively.

Relative $b$-to-light-jet energy scale (bJES): The bJES uncertainty is an additional uncertainty for the remaining differences between $b$-jets and light-jets after the global JES is applied, and therefore the corresponding uncertainty is uncorrelated with the JES uncertainty. An additional uncertainty of 0.2% to 1.2% is assigned to $b$-jets, with the lowest uncertainty for $b$-jets with high transverse momenta [63].

Due to the determination of bJSF, the bJES uncertainty leads to a very small contribution to the uncertainty in $m_{\text{top}}$. However, performing only a two-dimensional fit to $m_{\text{top}}^{\text{reco}}$ and $m_{\text{W}}^{\text{reco}}$ would result in an uncertainty of 0.47 GeV from this source.

Jet energy resolution (JER): The JER uncertainty is determined following an eigenvector decomposition strategy similar to the JES systematic uncertainties [93,94]. The 11 components take into account various effects evaluated from simulation-to-data comparisons including calorimeter noise terms in the forward region. The corresponding uncertainty in $m_{\text{top}}$ is the sum in quadrature of the components of the eigenvector decomposition.

Jet reconstruction efficiency (JRE): This uncertainty is evaluated by randomly removing 0.23% of the jets with $p_T < 30$ GeV from the simulated events prior to the event selection to reflect the precision with which the data-to-simulation JRE ratio is known [62]. The fitted $m_{\text{top}}$ difference between the varied sample and the nominal sample is taken as a systematic uncertainty.

Jet vertex fraction (JVF): When summing the scalar $p_T$ of all tracks in a jet, the JVF is the fraction contributed by tracks originating at the primary vertex. The uncertainty in $m_{\text{top}}$ is evaluated by varying the requirement on the JVF within its uncertainty [65].

$b$-tagging: Mismodelling of the $b$-tagging efficiency and mistag rate is accounted for by the application of jet-specific scale factors to simulated events [66]. These scale factors depend on jet $p_T$, jet $\eta$ and the underlying quark flavour. The ones used in this analysis are derived from dijet and $t\bar{t} \rightarrow$ dilepton [66] events. They are the same as those used for the measurement of $m_{\text{top}}$ in the $t\bar{t} \rightarrow$ dilepton channel [14].

Similarly to the JES uncertainties, the $b$-tagging uncertainties are estimated by using an eigenvector approach, based on the $b$-tagging calibration analysis [66–68]. They include the uncertainties in the $b$-tagging, $c/\tau$-tagging and mistagging scale factors. This uncertainty in $m_{\text{top}}$ is derived by varying the scale factors within their uncertainties and adding the resulting fitted differences in quadrature. In this procedure, uncertainties that are considered both in the $b$-tagging calibration and as separate sources in the $m_{\text{top}}$ analysis are taken into account simultaneously by applying the corresponding varied $b$-tagging scale factors together with the varied sample when assessing the corresponding uncertainty in $m_{\text{top}}$. The final uncertainty is the sum in quadrature of these independent components. Compared with the result from $\sqrt{s} = 7$ TeV data, this uncertainty is reduced by about one third for both the standard and BDT event selections in accordance with the improvements made in the calibrations of the $b$-tagging algorithm [66,67].

Leptons: The lepton uncertainties are related to the electron energy or muon momentum scale and resolution, as well as trigger, isolation and identification efficiencies. These are measured very precisely in high-purity $J/\psi \rightarrow \ell^+\ell^-$ and $Z \rightarrow \ell^+\ell^-$ data [57,58,95]. For each component, the corresponding uncertainty is propagated to the $E_{\text{T}}^{\text{miss}}$ as well.

Missing transverse momentum: The remaining contribution to the missing-transverse-momentum uncertainty stems from the uncertainties in calorimeter-cell energies associated with low-$p_T$ jets (7 GeV $< p_T < 20$ GeV) without any corresponding reconstructed physics object or from pile-up interactions. They are accounted for as described in Ref. [69].

The corresponding uncertainty in $m_{\text{top}}$ is small.

Pile-up: Besides the component treated in the JES uncertainty, the residual dependence of the fitted $m_{\text{top}}$ on the amount of pile-up activity and a possible mismodelling of pile-up in MC simulation is determined. For this, the $m_{\text{top}}$ dependence in bins of $n_{\text{vtx}}$ and $\mu$ is determined for data and MC simulated events. Within the statistical uncertainties, the slopes of the linear dependences of $m_{\text{top}}$ observed in data and predicted by the MC simulation are compatible. The same is true for JSF and bJSF. The final effect on the measurement is assessed by a convolution of the linear dependence with the respective $n_{\text{vtx}}$ and $\mu$ distributions observed for data and MC simulated events. The maximum of the $n_{\text{vtx}}$ and $\mu$ effects is assigned as an uncertainty due to pile-up. The pile-up conditions differ between the $\sqrt{s} = 7$ and 8 TeV data. For the BDT selection of $\sqrt{s} = 8$ TeV data used here, the average of the mean number of inelastic $pp$ interactions per bunch crossing is $\langle \mu \rangle = 20.3$ and the average number of reconstructed primary vertices is about $n_{\text{vtx}} = 9.4$, to be compared
with $\langle \mu \rangle = 8.8$ and $n_{\text{vtx}} = 7.0$ for $\sqrt{s} = 7$ TeV data [65]. The corresponding uncertainty is somewhat larger than for $\sqrt{s} = 7$ TeV data but still small.

8.5 Statistical precision of systematic uncertainties

The systematic uncertainties quoted in Table 3 carry statistical uncertainties themselves. In view of a combination with other measurements, the statistical precision $\sigma$ from a comparison of two samples (1 and 2) is determined for each uncertainty source based on the statistical correlation $\rho_{12}$ of the underlying samples using $\sigma^2 = \sigma_1^2 + \sigma_2^2 - 2 \rho_{12} \sigma_1 \sigma_2$. The statistical correlation is expressed as a function of the fraction of shared events of both samples $\rho_{12} = \sqrt{N_{12}/N_1 \cdot N_{12}/N_2} = N_{12} / \sqrt{N_1 \cdot N_2}$, with $N_1$ and $N_2$ being the unweighted numbers of events in the two samples and $N_{12}$ being the unweighted number of events present in both samples. The size of the MC sample at $m_{\text{top}} = 172.5$ GeV results in a statistical precision in $m_{\text{top}}$ of about 0.1 GeV. Most estimations are based on the same sample with only a change in a single parameter, such as lepton energy scale uncertainties. This leads to a high correlation of the central $m_{\text{top}}$ values and a correspondingly low statistical uncertainty in their difference. Others, which do not share the same generated events or exhibit other significant differences, have a lower correlation, and the corresponding statistical uncertainty is higher, such as in the case of the signal-modelling uncertainty. The statistical uncertainty in the total systematic uncertainty is calculated from the individual statistical uncertainties by the propagation of uncertainties.

9 Results

For the BDT selection, the likelihood fit to the data results in

$$m_{\text{top}} = 172.08 \pm 0.39 \text{ (stat) GeV},$$
$$\text{JSF} = 1.005 \pm 0.001 \text{ (stat), and}$$
$$\text{bJSF} = 1.008 \pm 0.005 \text{ (stat).}$$

The statistical uncertainties are taken from the parabolic approximation of the likelihood profiles. The expected statistical uncertainties, calculated in Sect. 7, are compatible with those. The correlation matrices of the three variables with $i = 0, 1$ and 2 corresponding to $m_{\text{top}}, \text{JSF}$ and $\text{bJSF}$ are

$$\rho_{\text{Stat}} = \begin{pmatrix} 1 & -0.27 & -0.92 \\ -0.27 & 1 & -0.02 \\ -0.92 & -0.02 & 1 \end{pmatrix} \quad \text{and}$$
$$\rho_{\text{Syst}} = \begin{pmatrix} 1 & -0.30 & -0.39 \\ -0.30 & 1 & -0.42 \\ -0.39 & -0.42 & 1 \end{pmatrix}.$$

The upper matrix corresponds to the correlations for statistical uncertainties only, while the lower matrix is obtained by additionally taking into account all systematic uncertainties.

Figure 6 shows the $m_{\text{top}}$, $m_W$, and $R_{\text{top}}$ distributions in the data with statistical uncertainties together with the corresponding fitted probability density functions for the background alone and for the sum of signal and background. The uncertainty band attached to the fit to data is obtained in the following way. At each point in $m_{\text{top}}$, $m_W$, and $R_{\text{top}}$, the band contains 68% of all fit function values obtained by randomly varying $m_{\text{top}}$, JSF and bJSF within their total uncertainties and taking into account their correlations. The waist in the uncertainty band is caused by the usage of normalized probability density functions. The band visualises the variations of the three template fit functions caused by all the uncertainties in $m_{\text{top}}$ listed in Table 3. The total uncertainty in all three fitted parameters is dominated by their systematic uncertainty. Therefore, the band shown is much wider than the band that would be obtained by fitting to the distributions with statistical uncertainties only.

The measured value of $m_{\text{top}}$ in the $t\bar{t} \rightarrow \text{lepton} + \text{jets}$ channel at $\sqrt{s} = 8$ TeV is

$$m_{\text{top}} = 172.08 \pm 0.39 \text{ (stat) } \pm 0.82 \text{ (syst) GeV}$$

with a total uncertainty of 0.91 GeV. The statistical precision of the systematic uncertainty is 0.06 GeV. This result corresponds to a 19% improvement on the result obtained using the standard selection on the same data. Compared with the result in the $t\bar{t} \rightarrow \text{lepton} + \text{jets}$ channel at $\sqrt{s} = 7$ TeV, the improvement is 29%. On top of the smaller statistical uncertainty, the increased precision is mainly driven by smaller theory modelling uncertainties achieved by the BDT selection. The larger number of events in the $\sqrt{s} = 8$ TeV dataset is effectively traded for lower systematic uncertainties, resulting in a significant gain in total precision. The new ATLAS result in the $t\bar{t} \rightarrow \text{lepton} + \text{jets}$ channel is more precise than the result from the CDF experiment, but less precise than the CMS and D0 results, measured in the same channel, as shown in Fig. 14b in Appendix B.

10 Combination with previous ATLAS results

This section presents the combination of the six $m_{\text{top}}$ results of the ATLAS analyses in the $t\bar{t} \rightarrow \text{dilepton, } t\bar{t} \rightarrow \text{lepton} + \text{jets and } t\bar{t} \rightarrow \text{all jets channels at centre-of-mass energies of } \sqrt{s} = 7$ and 8 TeV. The treatment of the results that are input to the combinations are described, followed by a detailed explanation of the evaluation of the estimator correlations for the various sources of systematic uncertainty. The compatibilities of the measured $m_{\text{top}}$ values are investigated using a pairwise $\chi^2$ for all pairs of measurements.
Fig. 6 Results of the likelihood fit to the data. The figures show the data distributions of the three observables with statistical uncertainties together with the fitted probability density function for the background alone (barely visible at the bottom of the figure) and for the sum of signal and background. The uncertainty band corresponds to the one standard deviation total uncertainty in the fit function. It is based on the total uncertainty in the three fitted parameters as explained in the text. 

(a) Reconstructed top quark mass

(b) Reconstructed W boson mass

(c) Reconstructed ratio of jet transverse momenta

and by evaluating the compatibility of selected combinations. Finally, the six results are combined, displaying the effect of individual results on the combined result.

10.1 Inputs to the combination and categorization of uncertainties

The measured values of the individual analyses and their statistical and systematic uncertainties are given in Table 4. For each result, the evaluated systematic uncertainties are shown together with their statistical uncertainties. The statistical uncertainties in the total systematic uncertainties and the total uncertainties are obtained from the propagation of uncertainties.\(^7\)

\(^7\) For the previous results in the \(t \bar{t} \rightarrow \text{dilepton} and t \bar{t} \rightarrow \text{lepton + jets} channels, the values quoted for the statistical uncertainties in the total systematic uncertainties differ from the ones in the original publications, where just the sum in quadrature of the statistical uncertainties in the individual systematic uncertainties was used.

For the combinations to follow, the combined uncertainties for the previous results, namely \(t \bar{t} \rightarrow \text{dilepton} and t \bar{t} \rightarrow \text{lepton + jets at } \sqrt{s} = 7 \text{ TeV from Ref. [9], } t \bar{t} \rightarrow \text{all jets at } \sqrt{s} = 7 \text{ TeV from Ref. [96], } t \bar{t} \rightarrow \text{dilepton at } \sqrt{s} = 8 \text{ TeV from Ref. [14] and } t \bar{t} \rightarrow \text{all jets at } \sqrt{s} = 8 \text{ TeV from Ref. [74], were all re-evaluated. In all cases, the numbers agree to within 0.01 GeV with the original publications, which in any case is the rounding precision due to the precision of some of the inputs. On top of this, the results listed in Table 4 differ in some aspects from the original publications as explained below."

The combination follows the approach developed for the combination of \(\sqrt{s} = 7 \text{ TeV analyses in Ref. [9], including the evaluation of the correlations given in Sect. 10.2 below. The treatment of uncertainty categories for the } t \bar{t} \rightarrow \text{dilepton and } t \bar{t} \rightarrow \text{lepton + jets measurements at } \sqrt{s} = 7 \text{ TeV exactly follows Ref. [9]. The uncertainty categorizations for the } t \bar{t} \rightarrow \text{all jets measurements at } \sqrt{s} = 7 \text{ and } 8 \text{ TeV from Refs. [74, 96] closely follow this categorization but have }\)
Table 4 The six measured values of $m_{\text{top}}$ ($i = 0, \ldots, 5$) and their statistical and systematic uncertainty sources $k$, numbered as given in the first column. For the individual measurements, the systematic uncertainty in $m_{\text{top}}$ and its associated statistical uncertainty are given for each source of uncertainty. The last line refers to the sum in quadrature of the statistical and systematic uncertainties. The statistical uncertainties in the total systematic uncertainties and in the total uncertainties are calculated from the propagation of uncertainties. Systematic uncertainties listed as 0 are not evaluated, while an empty cell indicates an uncertainty not applicable to the corresponding measurement. Statistical uncertainties quoted as 0.00 are smaller than 0.005

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some extra, analysis-specific sources of uncertainty, as shown in Table 4. In addition, the $t\bar{t} \to$ all jets result at $\sqrt{s} = 8$ TeV from Ref. [74] is based on a different treatment of the PDF-uncertainty-induced uncertainty in $m_{\text{top}}$. To allow the evaluation of the estimator correlations also for this uncertainty in $m_{\text{top}}$, for this combination, the respective uncertainty is newly evaluated according to the prescription given in Sect. 8.

For the $t\bar{t} \to$ all jets result at $\sqrt{s} = 7$ TeV the statistical precisions in the systematic uncertainties were not evaluated in Ref. [9] but were calculated for this combination. For the $t\bar{t} \to$ all jets result at $\sqrt{s} = 8$ TeV in Ref. [74], for some of the sources, the statistical uncertainty in the systematic uncertainty was not evaluated, such that the quoted statistical uncertainty in the total systematic uncertainty is a lower limit.

For the mapping of uncertainty categories for data taken at different centre-of-mass energies, the choice of Ref. [14] is employed. The most complex cases are the uncertainties involving eigenvector decompositions, such as the JES and $b$-tagging scale factor uncertainties, and the uncertainty categories that do not apply to all input measurements. The JES-uncertainty-induced uncertainty in $m_{\text{top}}$ is obtained from a number of JES subcomponents. Some JES subcomponents have an equivalent at the other centre-of-mass energy and others do not. As in Ref. [14], the JES subcomponents without an equivalent at the other centre-of-mass energy are treated as independent, resulting in vanishing estimator correlations for that part of the covariance matrix. For the remaining subcomponents, the estimator correlations are partly positive and partly negative. As an example, for the flavour part of the JES-uncertainty-induced uncertainty in $m_{\text{top}}$, the two most precise results, the $t\bar{t} \to$ dilepton and $t\bar{t} \to$ lepton + jets measurements at $\sqrt{s} = 8$ TeV, are negatively correlated. Consequently, for this pair, the resulting estimator correlation for the total JES-induced uncertainty in $m_{\text{top}}$ is also negative. At the quoted precision, the two assumptions about the equivalence of the JES subcomponents between the datasets at the two centre-of-mass energies, i.e. the weak and strong correlation scenarios described in Table 10 in Appendix A, leave the combined value and uncertainty unchanged.

Following Ref. [14], the $\sqrt{s} = 7$ and 8 TeV measurements are treated as uncorrelated for the nuisance parameters of the $b$-tagging, $c/\tau$-tagging, mistagging and JER uncertainties. In Ref. [14] it was shown that a correlated treatment of the flavour-tagging nuisance parameters results in an insignificant change in the combination. For the statistical, method calibration, MC-based background shape at $\sqrt{s} = 7$ and 8 TeV, and the pile-up uncertainties in $m_{\text{top}}$, the measurements are assumed to be uncorrelated. Details of the evaluation of the correlations for all remaining systematic uncertainties are discussed below.

10.2 Mathematical framework and evaluation of estimator correlations

All combinations are performed using the best linear unbiased estimate (BLUE) method [97,98] in a C++ implementation described in Ref. [99]. The BLUE method uses a linear combination of the inputs to combine measurements. The coefficients (BLUE weights) are determined via the minimization of the variance of the combined result. They can be used to construct measures for the importance of a given single measurement in the combination [98]. For any combination, the measured values $x_i$, the list of uncertainties $\sigma_{ik}$ and the correlations $\rho_{ijk}$ of the estimators $(i, j)$ for each source of uncertainty $(k)$ have to be provided. For all uncertainties, a Gaussian probability distribution function is assumed. For the uncertainties in $m_{\text{top}}$ for which the measurements are correlated, when using $\pm \sigma_1$ variations of a systematic effect, e.g. when changing the bJES by $\pm \sigma_1$, there are two possibilities. When simultaneously applying a variation for a systematic uncertainty, e.g. $+ \sigma_1$ for the bJES, to a pair $(i, j)$ of measurements, e.g. the $t\bar{t} \to$ lepton + jets and $t\bar{t} \to$ dilepton measurements at $\sqrt{s} = 8$ TeV, both analyses can result in a larger or smaller $m_{\text{top}}$ value than the one obtained for the nominal case (full correlation, $\rho_{ijk} = +1$), or one analysis can result in a larger and the other in a smaller value (full anti-correlation, $\rho_{ijk} = -1$). Consequently, an uncertainty from a source only consisting of a single variation, such as the bJES-uncertainty-induced uncertainty or the uncertainty related to the choice of MC generator for signal events, results in a correlation of $\rho_{ijk} = \pm 1$. The estimator correlations for composite uncertainties are evaluated by calculating the correlation from the subcomponents. As an example, for the $t\bar{t} \to$ lepton + jets result at $\sqrt{s} = 8$ TeV, the subcomponents of the JES uncertainty are shown in Table 10 in Appendix A. For any pair of measurements $(i, j)$, this evaluation is done by adding the covariance terms of the subcomponents $k$ with $\rho_{ijk} = \pm 1$ and dividing by the total uncertainties for that source. The resulting estimator correlation is

$$\rho_{ij} = \frac{\sum_{k=1}^{N_{\text{comp}}} \rho_{ijk} \sigma_{ik} \sigma_{jk}}{\sigma_i \sigma_j}.$$

The quantity $\sigma_i^2 = \sum_{k=1}^{N_{\text{comp}}} \sigma_{ik}^2$ is the sum of the single subcomponent variances in analysis $i$. This procedure is applied to all uncertainty sources that consist of more than one subcomponent to reduce the large list of uncertainty subcomponents per estimator of $\mathcal{O}(100)$ to a suitable number of uncertainty sources, i.e. to those given in Table 4. Since the full
covariance matrix is independent of how the subsets are chosen, this does not affect the combination.

For the three analyses, the evaluated shifts in $m_{\text{top}}$ per uncertainty subcomponent are referred to as $\Delta m_{\text{dilepton}}^{\ell+\text{jets}}$, $\Delta m_{\text{top}}^{\ell+\text{jets}}$, and $\Delta m_{\text{top}}^{\text{all jets}}$. They are shown in Fig. 7 for the various uncertainty subcomponents in selected pairs of analyses. The pairs using the results from $\sqrt{s} = 8$ TeV data are shown in Fig. 7a–c, while Fig. 7d is for the two analyses in the $\bar{t} \ell \rightarrow \text{lepton} + \text{jets}$ channel at the two centre-of-mass energies. Each point represents the observed shifts for a systematic uncertainty or a subcomponent of a systematic uncertainty together with a cross, indicating the corresponding statistical precision in the systematic uncertainty in the two results. The solid points indicate the fully correlated cases, and the open points indicate the anti-correlated ones.

For many significant sources of uncertainty in Fig. 7a, the $t\bar{t} \rightarrow \text{lepton} + \text{jets}$ and $\bar{t}t \rightarrow \text{dilepton}$ measurements are anti-correlated. As shown in Ref. [9], this is caused by the in situ determination of the JSF and bJSF in the three-dimensional $t\bar{t} \rightarrow \text{lepton} + \text{jets}$ analysis. In contrast, for most sources of uncertainty, a positive estimator correlation is observed for the $t\bar{t} \rightarrow \text{dilepton}$ and $\bar{t}t \rightarrow \text{lepton} + \text{jets}$ measurements at $\sqrt{s} = 8$ TeV, shown in Fig. 7b. The prominent

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Fig. 7 The pairwise shifts in $m_{\text{top}}$ when simultaneously varying a pair of measurements for a systematic uncertainty or a subcomponent of a systematic uncertainty. a, b show the correlations of the $t\bar{t} \rightarrow \text{dilepton}$ measurement at $\sqrt{s} = 8$ TeV with the two other measurements at the same centre-of-mass energy for all sources of uncertainty for which the estimators are correlated. c shows the correlations of the present measurement with the $t\bar{t} \rightarrow \text{all jets}$ measurement at $\sqrt{s} = 8$ TeV, while d shows the correlations of the present measurement with the $t\bar{t} \rightarrow \text{lepton} + \text{jets}$ measurement at $\sqrt{s} = 7$ TeV. The crosses indicate the statistical uncertainty in the systematic uncertainties. The solid points indicate the fully correlated cases, and the open points indicate the anti-correlated ones.
Table 5 The pairwise correlations $\rho_{ij,k}$ of the six measurements $i,j = 0, \ldots, 5$ of $m_{\text{top}}$ for each source of systematic uncertainty $k = 0, \ldots, 22$, along with the total estimator correlations and the compatibility of the measurements using $\chi^2_{ij}$ from Eq. (2). The indices $i$ and $j$ are 0 for $t\bar{t} \rightarrow$ dilepton at $\sqrt{s} = 7$ TeV, 1 for $t\bar{t} \rightarrow$ lepton + jets at $\sqrt{s} = 7$ TeV, 2 for $t\bar{t} \rightarrow$ all jets at $\sqrt{s} = 7$ TeV, 3 for $t\bar{t} \rightarrow$ dilepton at $\sqrt{s} = 8$ TeV, 4 for $t\bar{t} \rightarrow$ lepton + jets at $\sqrt{s} = 8$ TeV, and 5 for $t\bar{t} \rightarrow$ all jets at $\sqrt{s} = 8$ TeV. The correspondence of the indices $k = 0, \ldots, 22$ and the sources of systematic uncertainty are given in Table 4. Correlations that are assigned, or cannot be evaluated because one uncertainty in the covariance term is zero at the quoted precision, are given as integer values, while evaluated correlations are shown as real values.

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exception is the hadronization-uncertainty-induced uncertainty in $m_{\text{top}}$, i.e. the single largest uncertainty in the $t\bar{t} \rightarrow$ all jets measurement at $\sqrt{s} = 8$ TeV, for which the two measurements are anti-correlated. On the contrary, the $t\bar{t} \rightarrow$ lepton + jets and $tt \rightarrow$ all jets measurements at $\sqrt{s} = 8$ TeV, shown in Fig. 7c, are positively correlated for this uncertainty. Finally, the $t\bar{t} \rightarrow$ lepton + jets measurements at the two centre-of-mass energies in Fig. 7d show a rather low correlation. The correlations per source of uncertainty and the total estimator correlations are summarized in Table 5.

The improvement in the combination obtained by the use of evaluated correlations compared with using estimator correlations assigned solely by physics assessments (here referred to as assigned correlations) is quantified using an example. Using the choices of assigned correlations from Ref. [11] for the ATLAS results in the $t\bar{t} \rightarrow$ dilepton and $t\bar{t} \rightarrow$ lepton + jets channels at $\sqrt{s} = 7$ TeV listed in Table 4 gives a combined value of $m_{\text{top}} = 172.91 \pm 0.50$ (stat) $\pm 1.05$ (syst) GeV compared with $m_{\text{top}} = 172.99 \pm 0.48$ (stat) $\pm 0.78$ (syst) GeV. The significant improvement in the precision of the combination demonstrates the particular importance of evaluating the correlations.

For the combinations presented in this paper, most estimator correlations could be evaluated. The most prominent exception is for the $b$-tagging uncertainty, where the $t\bar{t} \rightarrow$ all jets measurement at $\sqrt{s} = 8$ TeV is based on a different $b$-tagging algorithm and calibration than the $t\bar{t} \rightarrow$ dilepton and $t\bar{t} \rightarrow$ lepton + jets measurements at $\sqrt{s} = 8$ TeV.
was verified that assignments of the estimator correlations of $\rho_{5k} \in [-1, 1]$, with $i = 3, 4$ and $k = 17$, yield insignificant differences in the full combination. Estimator correlations of $\rho_{5} = 1$ are assigned for this case, as this choice gives the largest uncertainty in the combination. A similar situation arises for the data-driven all-jets background uncertainty in the two $t\bar{t}$ → all jets measurements, where the method used for the background estimate is similar but not identical for the two measurements. Consequently, the conservative ad hoc assignment of $\rho_{25k} = 1$ was also made for this source $k = 11$.

10.3 Compatibility of the inputs and selected combinations

Before any combination is performed, the compatibility of the input results is verified. For each pair of results, their compatibility is expressed by the ratio of the squared difference between the pair of measured values and the uncertainty in this difference [98] as

$$\chi^2_{ij} = \frac{(x_i - x_j)^2}{\sigma_i^2 + \sigma_j^2 - 2\rho_{ij}\sigma_i\sigma_j}.$$  (2)

The corresponding values are given in Table 5. Analysing the $\chi^2_{ij}$ values reveals good $\chi^2$ probabilities, with the smallest $\chi^2$ probability being $P(\chi^2, 1) = 15\%$. The largest sum of $\chi^2_{ij}$ values far is observed for the $t\bar{t}$ → all jets result at $\sqrt{s} = 7$ TeV.

The dependences of the combined values and their uncertainties on the total correlation for pairwise combinations of results are analysed. The dependences for pairs of the three results from $\sqrt{s} = 8$ TeV data are shown in Fig. 8. The largest information gain is achieved by combining the $t\bar{t}$ → dilepton and $t\bar{t}$ → lepton + jets results at $\sqrt{s} = 8$ TeV, shown in Fig. 8a, b, which are anti-correlated, i.e. $\rho = -0.19$.

Based on Tables 4 and 5, selected combinations are analysed, yielding the results given in Table 6 and shown in Fig. 9. The BLUE weights and the pulls\(^9\) of the results are given in Table 7.

To investigate the difference in precision of combined results obtained from $\sqrt{s} = 7$ and 8 TeV results, two independent combinations of the three results per centre-of-mass energy are performed. For each decay channel, the results at $\sqrt{s} = 8$ TeV are significantly more precise than those at $\sqrt{s} = 7$ TeV. In addition, the two most precise results per centre-of-mass energy are significantly less correlated at $\sqrt{s} = 8$ TeV than at $\sqrt{s} = 7$ TeV. Consequently, the size of the uncertainty of the combined result at $\sqrt{s} = 8$ TeV ($m_{8\text{TeV}})$ is 39% smaller than the one obtained from the results at $\sqrt{s} = 7$ TeV ($m_{7\text{TeV}}$). As shown in Fig. 13a, b in Appendix B, for both centre-of-mass energies, the combination is dominated by the results in the $t\bar{t}$ → dilepton and $t\bar{t}$ → lepton + jets channels.

To investigate whether the measured $m_{\text{top}}$ depends on the $t\bar{t}$ decay mode, a combination of the six results is performed in which the results in the three $t\bar{t}$ decay channels are treated as determining potentially different masses, namely $m_{\text{top}}^{\text{dilepton}}$, $m_{\text{top}}^{\ell+\text{jets}}$, and $m_{\text{top}}^{\text{all jets}}$. In such a combination, results obtained in one decay channel influence the combined result in another decay channel by means of their estimator correlation. Therefore, for each observable, e.g. $m_{\text{top}}^{\text{dilepton}}$, by construction the sum of weights of the results in the corresponding decay channel equals unity, while for each of the other decay channels the sum of weights of the results equals zero [100]. The combination yields compatible results for the three masses listed in Table 6. Consequently, the data do not show any sign of a decay-channel-dependent $m_{\text{top}}$. The correlation matrix of the three observables 0, 1 and 2 corresponding to $m_{\text{top}}^{\text{dilepton}}$, $m_{\text{top}}^{\ell+\text{jets}}$ and $m_{\text{top}}^{\text{all jets}}$ is

$$\rho_{\text{m}_{\text{top}}} = \begin{pmatrix} 1 & -0.14 & 0.43 \\ -0.14 & 1 & -0.05 \\ 0.43 & -0.05 & 1 \end{pmatrix},$$

and the smallest $\chi^2$ probability of any pair of combined results for determining the same $m_{\text{top}}$ is $P(\chi^2, 1) = 11\%$. As shown in Fig. 13c–e in Appendix B, for the combination of the three observables, the results based on $\sqrt{s} = 7$ TeV data lead to significant improvements on their more precise counterparts obtained from $\sqrt{s} = 8$ TeV data, apart from the $t\bar{t}$ → dilepton channel.

Given that no dependence of $m_{\text{top}}$ on the centre-of-mass energy or the $t\bar{t}$ decay channel is expected, the above examples of combinations are merely additional investigations of the compatibility of the input results. The compatibility combinations are summarized in Fig. 9 and listed in Table 6. For all combinations, the values quoted in Fig. 9 are the combined value, the statistical uncertainty, the systematic uncertainty, the total uncertainty and the statistical uncertainty in the total uncertainty.

10.4 The combined result of $m_{\text{top}}$

The use of the statistical uncertainties in the systematic uncertainties has two main advantages. Firstly, it allows a determination of the uncertainties in the evaluation of the total correlations of the estimators, avoiding the need to perform ad hoc variations. Secondly, it enables the monitoring of the evolution of the combined result in relation to the precision in its uncertainty while including results, thereby evaluating

\(^9\) Using the individual results $x_i \pm \sigma_i$ and the combined result $x \pm \sigma_x$, the pull of result $i$ is calculated as $(x_i - x) / \sqrt{\sigma_i^2 - \sigma_x^2}$ and should be Gaussian distributed with mean zero and width unity. The pull is a measure of the likeness of the $x_i$ measured in data.
Fig. 8  The combined values (left) and uncertainties (right) of the combination of pairs of individual results at \(\sqrt{s} = 8\) TeV, shown as functions of the total correlation \(\rho\) (solid lines). The combination of the \(t\bar{t} \to\) dilepton and \(t\bar{t} \to\) lepton + jets results is shown in the top row. The middle row is for the combination of the \(t\bar{t} \to\) dilepton and \(t\bar{t} \to\) all jets results. Finally, the combination of the \(t\bar{t} \to\) lepton + jets and \(t\bar{t} \to\) all jets results is shown in the bottom row. For comparison, the corresponding values for the input results are also shown (dashed lines).
Table 6 The results for selected combinations based on the six results at \( \sqrt{s} = 7 \) and 8 TeV. The left two columns of results show the combination of the three results at \( \sqrt{s} = 7 \) TeV \( (m_{\text{7TeV}}^{\text{top}}) \) or at \( \sqrt{s} = 8 \) TeV \( (m_{\text{8TeV}}^{\text{top}}) \), both combinations neglecting the results at the respective other centre-of-mass energy. The middle three columns show the combination of the six results as if pairs of measurements would determine a decay-specific top quark mass, namely \( m_{\text{dilepton}}^{\text{top}}, m_{\text{ℓ+jets}}^{\text{top}} \) and \( m_{\text{all jets}}^{\text{top}} \). Finally, shown on the right is the combination of the three most important results in the combination denoted by \( m_{\text{top}}^{(3)} \) and the combination of all results, i.e. the ATLAS result for \( m_{\text{top}} \) shown in Fig. 10. For each combination, the uncertainty is given for each source of uncertainty. Uncertainties quoted as 0.00 are smaller than 0.005, while empty cells indicate uncertainties that do not apply to the respective combination. Finally, the total systematic uncertainty and the sum in quadrature of the statistical and systematic uncertainties are given. Both are quoted including the precision at which the respective uncertainty is known.

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<td>0.04</td>
<td>0.03</td>
<td>0.04</td>
<td>0.00</td>
<td>0.03</td>
<td>0.02</td>
</tr>
<tr>
<td>W/Z+Jets shape</td>
<td>0.15</td>
<td>0.05</td>
<td>0.01</td>
<td>0.12</td>
<td>0.00</td>
<td>0.07</td>
<td>0.06</td>
</tr>
<tr>
<td>Fake leptons shape</td>
<td>0.03</td>
<td>0.03</td>
<td>0.07</td>
<td>0.02</td>
<td>0.00</td>
<td>0.03</td>
<td>0.03</td>
</tr>
<tr>
<td>Data-driven all-jets background</td>
<td>0.04</td>
<td>0.02</td>
<td>0.01</td>
<td>0.01</td>
<td>0.22</td>
<td>0.03</td>
<td>0.03</td>
</tr>
<tr>
<td>Jet energy scale</td>
<td>0.40</td>
<td>0.27</td>
<td>0.53</td>
<td>0.34</td>
<td>0.51</td>
<td>0.21</td>
<td>0.22</td>
</tr>
<tr>
<td>Relative b-to-light-jet energy scale</td>
<td>0.35</td>
<td>0.19</td>
<td>0.32</td>
<td>0.01</td>
<td>0.41</td>
<td>0.15</td>
<td>0.17</td>
</tr>
<tr>
<td>Jet energy resolution</td>
<td>0.04</td>
<td>0.10</td>
<td>0.09</td>
<td>0.16</td>
<td>0.07</td>
<td>0.10</td>
<td>0.09</td>
</tr>
<tr>
<td>Jet reconstruction efficiency</td>
<td>0.09</td>
<td>0.01</td>
<td>0.01</td>
<td>0.05</td>
<td>0.00</td>
<td>0.03</td>
<td>0.03</td>
</tr>
<tr>
<td>Jet vertex fraction</td>
<td>0.00</td>
<td>0.05</td>
<td>0.02</td>
<td>0.07</td>
<td>0.02</td>
<td>0.05</td>
<td>0.05</td>
</tr>
<tr>
<td>b-tagging</td>
<td>0.24</td>
<td>0.18</td>
<td>0.05</td>
<td>0.30</td>
<td>0.09</td>
<td>0.17</td>
<td>0.17</td>
</tr>
<tr>
<td>Leptons</td>
<td>0.04</td>
<td>0.10</td>
<td>0.14</td>
<td>0.11</td>
<td>0.01</td>
<td>0.09</td>
<td>0.08</td>
</tr>
<tr>
<td>Missing transverse momentum</td>
<td>0.08</td>
<td>0.03</td>
<td>0.01</td>
<td>0.07</td>
<td>0.01</td>
<td>0.04</td>
<td>0.04</td>
</tr>
<tr>
<td>Pile-up</td>
<td>0.01</td>
<td>0.07</td>
<td>0.05</td>
<td>0.10</td>
<td>0.01</td>
<td>0.06</td>
<td>0.06</td>
</tr>
<tr>
<td>All-jets trigger</td>
<td>0.00</td>
<td>0.01</td>
<td>0.00</td>
<td>0.00</td>
<td>0.06</td>
<td>0.01</td>
<td>0.01</td>
</tr>
<tr>
<td>Fast vs. full simulation</td>
<td>0.03</td>
<td>0.01</td>
<td>0.01</td>
<td>0.07</td>
<td>0.01</td>
<td>0.04</td>
<td>0.04</td>
</tr>
<tr>
<td>Total systematic uncertainty</td>
<td>0.76 ± 0.04</td>
<td>0.48 ± 0.04</td>
<td>0.74 ± 0.04</td>
<td>0.61 ± 0.04</td>
<td>0.80 ± 0.05</td>
<td>0.42 ± 0.04</td>
<td>0.41 ± 0.03</td>
</tr>
<tr>
<td>Total</td>
<td>0.89 ± 0.04</td>
<td>0.54 ± 0.04</td>
<td>0.84 ± 0.04</td>
<td>0.71 ± 0.04</td>
<td>0.98 ± 0.05</td>
<td>0.50 ± 0.04</td>
<td>0.48 ± 0.03</td>
</tr>
</tbody>
</table>
their influence on the combination. The significance of the individual results in the combination is shown in Fig. 10. The individual results are shown in Fig. 10a. Their combination is displayed in Fig. 10b where, following Ref. [98], starting from the most precise result, i.e. the $t\bar{t} \rightarrow$ dilepton measurement at $\sqrt{s} = 8$ TeV, results are added to the combination one at a time according to their importance, and the combined result is reported. Each following line of this figure shows the combined result when adding the result listed to the input of $m_{\text{top}}^\text{(3)}$. The values quoted are the combined value, the statistical uncertainty, the systematic uncertainty, the total uncertainty and the uncertainty in the combination.

The changes in statistical uncertainties in the combined value and its uncertainty due to variations of the input systematic uncertainties within their uncertainties are evaluated for two cases, namely for $m_{\text{top}}^\text{(3)}$ and for the combination of all results. Following Ref. [14], the distributions of the combined values and uncertainties are calculated from 500 combinations, where for each combination, the sizes of the uncertainties as well as the correlations are newly evaluated. Due to the re-evaluation of the correlation, the resulting distributions

![Compatibility evaluations](image_url)
are not Gaussian and are also not exactly centred around the combined value and the combined uncertainty. For $m_{\text{top}}^{(3)}$, the root mean square of the distribution of the combined value is 0.03 GeV, and that of the distribution of its uncertainty is 0.04 GeV. The corresponding values for the new ATLAS combination are 0.07 GeV and 0.03 GeV, respectively.

The full breakdown of uncertainties for the new combined ATLAS result for $m_{\text{top}}$ is reported in the last column of Table 6. The combined result is

$$m_{\text{top}} = 172.69 \pm 0.25 \text{ (stat)} \pm 0.41 \text{ (syst) GeV}$$

with a total uncertainty of $0.48 \pm 0.03$ GeV, where the quoted uncertainty in this uncertainty is statistical. This means that the uncertainty in this combined result is only known to this precision, which, given its size, is fully adequate.

The $\chi^2$ probability of $m_{\text{top}}^{(3)}$ is 78%. Driven by the larger pulls of the remaining three results listed in Table 7, the $\chi^2$ probability of 64% for the new ATLAS combination of $m_{\text{top}}$ is lower but still good. The new ATLAS combined result of $m_{\text{top}}$ provides a 44% improvement relative to the most precise single input result, which is the $t \bar{t} \rightarrow$ dilepton analysis at $\sqrt{s} = 8$ TeV. With a relative precision of 0.28%, it improves on the previous combination in Ref. [14] by 31% and supersedes it. As shown in Appendix B, the new ATLAS combined result of $m_{\text{top}}$ is more precise than the results from the CDF and D0 experiments, and has a precision similar to the CMS combined result.

In Fig. 11, the 68% and 95% confidence-level contours of the indirect determination of $m_W$ and $m_{\text{top}}$ from the global electroweak fit in Ref. [2] are compared with the corresponding confidence-level contours of the direct ATLAS measurements of the two masses. The top quark mass used in this figure was obtained above, while the $W$ boson mass is taken from Ref. [101]. The electroweak fit uses as input the LHC combined result of the Higgs boson mass of $m_H = 125.09 \pm 0.24$ GeV from Ref. [102]. There is good agreement between the direct ATLAS mass measurements and their indirect determinations by the electroweak fit.

11 Conclusion

The top quark mass is measured via a three-dimensional template method in the $t \bar{t} \rightarrow$ lepton + jets channel and combined with previous ATLAS $m_{\text{top}}$ measurements at the LHC.
For the $t\bar{t} \rightarrow$ lepton + jets analysis from $\sqrt{s} = 8$ TeV proton–proton collision data with an integrated luminosity of about 20.2 fb$^{-1}$, the event selection of the corresponding $\sqrt{s} = 7$ TeV analysis is refined. An optimization employing a BDT selection to efficiently suppress less-well-reconstructed events results in a significant reduction in total uncertainty, driven by a significant decrease in theory-modelling-induced uncertainties. With this approach, the measured value of $m_{\text{top}}$ is

$$m_{\text{top}} = 172.08 \pm 0.39 \text{(stat)} \pm 0.82 \text{(syst)} \text{ GeV}$$

with a total uncertainty of $0.91 \pm 0.06$ GeV, where the quoted uncertainty in the total uncertainty is statistical. The precision is limited by systematic uncertainties, mostly by uncertainties in the calibration of the jet energy scale, $b$-tagging and the Monte Carlo modelling of signal events. This result is more precise than the CMS and D0 results, measured in the same framework of RIVET (http://rivet.hepforge.org/). This information is taken from the ATLAS Data Access Policy, which is a public document that can be downloaded from http://opendata.cern.ch/record/413 [opendata.cern.ch].]

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Data Availability Statement This manuscript has no associated data or the data will not be deposited. [Authors’ comment: All ATLAS scientific output is published in journals, and preliminary results are made available in Conference Notes. All are openly available, without restriction on use by external parties beyond copyright law and the standard conditions agreed by CERN. Data associated with journal publications are also made available: tables and data from plots (e.g. cross section values, likelihood profiles, selection efficiencies, cross section limits, ...) are stored in appropriate repositories such as HEPDATA (http://hepdata.cedar.ac.uk/). ATLAS also strives to make additional material related to the paper available that allows a reinterpretation of the data in the context of new theoretical models. For example, an extended encapsulation of the analysis is often provided for measurements in the framework of RIVET (http://rivet.hepforge.org/). This information is taken from the ATLAS Data Access Policy, which is a public document that can be downloaded from http://opendata.cern.ch/record/413 [opendata.cern.ch].]

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Appendix A: Results from the BDT optimization and individual sources of systematic uncertainty

This appendix has additional details of the measurement of $m_{\text{top}}$ in the $t\bar{t} \rightarrow \text{lepton} + \text{jets}$ channel from $\sqrt{s} = 8$ TeV data discussed in the main text.

In Fig. 12, the template fit functions of the three observables are compared for the standard and the BDT event selection. The distributions of $m_{\text{top}}^{\text{reco}}$ and $m_{W}^{\text{reco}}$ are narrower for the BDT event selection, which means the resolution in the two masses is improved compared with what is observed for the standard selection. The $R_{bq}^{\text{reco}}$ distribution is slightly shifted to lower values for the BDT event selection, but the difference is small.

(a) Reconstructed top quark mass

(b) Reconstructed $W$ boson mass

(c) Reconstructed ratio of jet transverse momenta

Fig. 12 Comparison of the template fit functions of the three observables for the standard event selection (solid line) and the BDT event selection (dashed line). The ratios (standard/BDT) of the pairs of functions are also shown. a shows the reconstructed top quark mass $m_{\text{top}}^{\text{reco}}$, b shows the reconstructed $W$ boson mass $m_{W}^{\text{reco}}$ and c shows the reconstructed jet-$p_T$ ratio $R_{bq}^{\text{reco}}$. 
Table 8  The individual components of the uncertainty sources considered for the $t\bar{t} \rightarrow$ lepton + jets analysis at $\sqrt{s} = 8$ TeV for the sources of uncertainty not documented in Tables 9, 10, 11 and 12. The uncertainties together with their statistical precisions are listed in boldface and given with 0.01 GeV precision. The uncertainty per source is calculated as the sum in quadrature of the subcomponents. Uncertainties quoted as 0.00 (0.000) are smaller than 0.005 (0.0005).

<table>
<thead>
<tr>
<th>Uncertainty</th>
<th>$\Delta m_{\text{top}}^{\text{up}}$ [GeV]</th>
<th>$\Delta m_{\text{top}}^{\text{down}}$ [GeV]</th>
<th>$\Delta m_{\text{top}}$ [GeV]</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Signal Monte Carlo generator</strong></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Powheg-Box - MC@NLO (Herwig)</td>
<td></td>
<td></td>
<td>$0.16 \pm 0.17$</td>
</tr>
<tr>
<td><strong>Hadronization</strong></td>
<td></td>
<td></td>
<td>$-0.161 \pm 0.168$</td>
</tr>
<tr>
<td>Powheg+Pythia - Powhig+Herwig</td>
<td></td>
<td></td>
<td>$+0.146 \pm 0.098$</td>
</tr>
<tr>
<td><strong>Initial- and final-state QCD radiation</strong></td>
<td></td>
<td></td>
<td>$0.08 \pm 0.11$</td>
</tr>
<tr>
<td>Less I/FSR - more I/FSR</td>
<td>$+0.086$</td>
<td>$-0.075$</td>
<td>$+0.080 \pm 0.111$</td>
</tr>
<tr>
<td>Underlying event</td>
<td></td>
<td></td>
<td>$0.08 \pm 0.15$</td>
</tr>
<tr>
<td>P2012 - P2012 M0Hi</td>
<td></td>
<td></td>
<td>$-0.080 \pm 0.153$</td>
</tr>
<tr>
<td><strong>Colour reconnection</strong></td>
<td></td>
<td></td>
<td>$0.19 \pm 0.15$</td>
</tr>
<tr>
<td>P2012 - P2012 LOCR</td>
<td></td>
<td></td>
<td>$+0.191 \pm 0.154$</td>
</tr>
<tr>
<td><strong>Background normalization</strong></td>
<td></td>
<td></td>
<td>$0.08 \pm 0.00$</td>
</tr>
<tr>
<td>Z+jets norm.</td>
<td>$+0.007$</td>
<td>$-0.015$</td>
<td>$+0.011 \pm 0.000$</td>
</tr>
<tr>
<td>W+jets norm.</td>
<td>$-0.017$</td>
<td>$-0.061$</td>
<td>$-0.061 \pm 0.000$</td>
</tr>
<tr>
<td>Fake lepton norm.</td>
<td></td>
<td></td>
<td>$+0.046 \pm 0.000$</td>
</tr>
<tr>
<td>W/Z+jets shape</td>
<td></td>
<td></td>
<td>$0.11 \pm 0.00$</td>
</tr>
<tr>
<td>W+jets HF0</td>
<td>$-0.001$</td>
<td>$-0.070$</td>
<td>$-0.070 \pm 0.000$</td>
</tr>
<tr>
<td>W+jets HF1</td>
<td>$-0.005$</td>
<td>$-0.087$</td>
<td>$-0.087 \pm 0.000$</td>
</tr>
<tr>
<td><strong>Jet reconstruction efficiency</strong></td>
<td></td>
<td></td>
<td>$0.02 \pm 0.01$</td>
</tr>
<tr>
<td>Nominal - 0.23% drop</td>
<td></td>
<td></td>
<td>$+0.022 \pm 0.013$</td>
</tr>
<tr>
<td><strong>Jet vertex fraction</strong></td>
<td></td>
<td></td>
<td>$0.09 \pm 0.01$</td>
</tr>
<tr>
<td>Leptons</td>
<td></td>
<td></td>
<td>$0.095 \pm 0.009$</td>
</tr>
<tr>
<td>Electron energy scale</td>
<td>$+0.025$</td>
<td>$-0.006$</td>
<td>$+0.016 \pm 0.006$</td>
</tr>
<tr>
<td>Electron energy resolution</td>
<td>$-0.152$</td>
<td>$-0.145$</td>
<td>$-0.152 \pm 0.013$</td>
</tr>
<tr>
<td>Muon resolution (muon spectrometer)</td>
<td></td>
<td></td>
<td>$+0.027 \pm 0.000$</td>
</tr>
<tr>
<td>Muon resolution (inner detector)</td>
<td></td>
<td></td>
<td>$+0.023 \pm 0.000$</td>
</tr>
<tr>
<td>Muon scale</td>
<td>$-0.013$</td>
<td>$+0.015$</td>
<td>$-0.014 \pm 0.000$</td>
</tr>
<tr>
<td>Lepton trigger SF</td>
<td>$-0.005$</td>
<td>$-0.003$</td>
<td>$-0.005 \pm 0.001$</td>
</tr>
<tr>
<td>Lepton identification SF</td>
<td>$+0.005$</td>
<td>$-0.011$</td>
<td>$+0.008 \pm 0.001$</td>
</tr>
<tr>
<td>Lepton reconstruction SF</td>
<td>$+0.003$</td>
<td>$-0.008$</td>
<td>$+0.005 \pm 0.000$</td>
</tr>
<tr>
<td><strong>Missing transverse momentum ($E_T^{\text{miss}}$)</strong></td>
<td></td>
<td></td>
<td>$0.05 \pm 0.01$</td>
</tr>
<tr>
<td>$E_T^{\text{miss}}$ (resolution soft term)</td>
<td>$+0.003$</td>
<td>$+0.012$</td>
<td>$+0.012 \pm 0.018$</td>
</tr>
<tr>
<td>$E_T^{\text{miss}}$ (scale soft term)</td>
<td>$+0.054$</td>
<td>$-0.039$</td>
<td>$+0.047 \pm 0.009$</td>
</tr>
</tbody>
</table>

For the BDT selection, a number of systematic uncertainties listed in Table 3 are calculated by performing pseudo-experiments for more than one systematic variation. The individual components are given in Tables 8, 9, 10, 11 and 12 below. Whenever the uncertainty is obtained from just a pair of samples, the shift $\Delta m_{\text{top}}$ is listed together with the definition of the difference evaluated indicating the direction of the shift. For the other cases, the shift in $m_{\text{top}}$ is quoted relative to the value measured in the central sample for the upward variation ($\Delta m_{\text{top}}^{\text{up}}$), the downward variation ($\Delta m_{\text{top}}^{\text{down}}$) and the final shift assigned to this uncertainty component ($\Delta m_{\text{top}}$). For most of the cases the signs of $\Delta m_{\text{top}}^{\text{up}}$ and $\Delta m_{\text{top}}^{\text{down}}$ are different, indicating that $m_{\text{top}}$ from the central sample is surrounded by the values from the two variations. In this case $|\Delta m_{\text{top}}|$ is $0.5(|\Delta m_{\text{top}}^{\text{up}}| - |\Delta m_{\text{top}}^{\text{down}}|)$, otherwise it is the maximum of $|\Delta m_{\text{top}}^{\text{up}}|$ and $|\Delta m_{\text{top}}^{\text{down}}|$. In both cases, the sign of $\Delta m_{\text{top}}$ is the one from $\Delta m_{\text{top}}^{\text{up}}$.

Appendix B: Additional information about the various combinations

This appendix gives additional information about the various combinations discussed in the main text. For all combinations the values quoted are the combined value, the statistical uncertainty, the systematic uncertainty, the total uncertainty.
Table 9 The individual components of the PDF uncertainty considered for the $t\bar{t} \rightarrow$ lepton + jets analysis at $\sqrt{s} = 8$ TeV, the resulting PDF-uncertainty-induced shifts in $m_{top}$ and the final uncertainty in $m_{top}$. The components [31,39,42] together with their statistical precisions are listed in boldface. The total uncertainty in the CT10 variations is calculated as the sum in quadrature of the CT10 subcomponents. The total uncertainty is given with 0.01 GeV precision. Uncertainties quoted as 0.00 (0.000) are smaller than 0.005 (0.0005). The term nuisance parameter is denoted by NuP. The last line refers to the sum in quadrature of the PDF subcomponents.

<table>
<thead>
<tr>
<th>PDF uncertainty components</th>
<th>$\Delta m_{top}$ [GeV]</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>CT10 variations</strong></td>
<td></td>
</tr>
<tr>
<td>CT10 NuP2 - NuP1</td>
<td>$0.09 \pm 0.00$</td>
</tr>
<tr>
<td>CT10 NuP4 - NuP3</td>
<td>$-0.001 \pm 0.000$</td>
</tr>
<tr>
<td>CT10 NuP6 - NuP5</td>
<td>$+0.000 \pm 0.000$</td>
</tr>
<tr>
<td>CT10 NuP8 - NuP7</td>
<td>$+0.015 \pm 0.000$</td>
</tr>
<tr>
<td>CT10 NuP10 - NuP9</td>
<td>$+0.004 \pm 0.000$</td>
</tr>
<tr>
<td>CT10 NuP12 - NuP11</td>
<td>$+0.002 \pm 0.000$</td>
</tr>
<tr>
<td>CT10 NuP14 - NuP13</td>
<td>$-0.026 \pm 0.001$</td>
</tr>
<tr>
<td>CT10 NuP16 - NuP15</td>
<td>$-0.004 \pm 0.000$</td>
</tr>
<tr>
<td>CT10 NuP18 - NuP17</td>
<td>$-0.015 \pm 0.001$</td>
</tr>
<tr>
<td>CT10 NuP20 - NuP19</td>
<td>$+0.013 \pm 0.001$</td>
</tr>
<tr>
<td>CT10 NuP22 - NuP21</td>
<td>$+0.006 \pm 0.001$</td>
</tr>
<tr>
<td>CT10 NuP24 - NuP23</td>
<td>$+0.063 \pm 0.001$</td>
</tr>
<tr>
<td>CT10 NuP26 - NuP25</td>
<td>$+0.000 \pm 0.001$</td>
</tr>
<tr>
<td>CT10 NuP28 - NuP27</td>
<td>$+0.009 \pm 0.000$</td>
</tr>
<tr>
<td>CT10 NuP30 - NuP29</td>
<td>$-0.004 \pm 0.000$</td>
</tr>
<tr>
<td>CT10 NuP32 - NuP31</td>
<td>$+0.007 \pm 0.001$</td>
</tr>
<tr>
<td>CT10 NuP34 - NuP33</td>
<td>$+0.019 \pm 0.002$</td>
</tr>
<tr>
<td>CT10 NuP36 - NuP35</td>
<td>$-0.011 \pm 0.001$</td>
</tr>
<tr>
<td>CT10 NuP38 - NuP37</td>
<td>$-0.001 \pm 0.000$</td>
</tr>
<tr>
<td>CT10 NuP40 - NuP39</td>
<td>$-0.001 \pm 0.001$</td>
</tr>
<tr>
<td>CT10 NuP42 - NuP41</td>
<td>$-0.005 \pm 0.001$</td>
</tr>
<tr>
<td>CT10 NuP44 - NuP43</td>
<td>$-0.003 \pm 0.000$</td>
</tr>
<tr>
<td>CT10 NuP46 - NuP45</td>
<td>$-0.002 \pm 0.000$</td>
</tr>
<tr>
<td>CT10 NuP48 - NuP47</td>
<td>$+0.027 \pm 0.000$</td>
</tr>
<tr>
<td>CT10 NuP50 - NuP49</td>
<td>$+0.002 \pm 0.000$</td>
</tr>
<tr>
<td>CT10 NuP52 - NuP51</td>
<td>$-0.003 \pm 0.001$</td>
</tr>
<tr>
<td><strong>NNPDF - CT10</strong></td>
<td>$-0.034 \pm 0.001$</td>
</tr>
<tr>
<td><strong>MSTW - CT10</strong></td>
<td>$-0.024 \pm 0.002$</td>
</tr>
<tr>
<td><strong>Total</strong></td>
<td>$0.09 \pm 0.00$</td>
</tr>
</tbody>
</table>

and the uncertainty in the total uncertainty, which is statistical.

Figure 13a, b shows the independent combinations per centre-of-mass energy. For both centre-of-mass energies, the combination is dominated by the results in the $t\bar{t} \rightarrow$ dilepton and $t\bar{t} \rightarrow$ lepton + jets channels. Using only those in the combinations yields combined results of $m_{top}^{8\text{TeV}} = 172.99 \pm 0.48$ (stat) $\pm 0.78$ (syst) GeV with an uncertainty of $0.91 \pm 0.05$ GeV at $\sqrt{s} = 7$ TeV and $m_{top}^{8\text{TeV}} = 172.56 \pm 0.28$ (stat) $\pm 0.48$ (syst) GeV with an uncertainty of $0.56 \pm 0.04$ GeV at $\sqrt{s} = 8$ TeV. At both centre-of-mass energies, the difference between the combined uncertainties of the partial and full combination is much smaller than the respective statistical precision in the total systematic uncertainties. This statistical precision is obtained from varying each systematic uncertainty within its statistical precision and repeating the combination, as explained in the main text.

Figure 13c–e shows the dependent combinations per $t\bar{t}$ decay channel. The combined result of $m_{top}^{\text{dilepton}}$ based only on the $t\bar{t} \rightarrow$ dilepton measurement from $\sqrt{s} = 8$ TeV data and the measurements in the other decay channels is $m_{top}^{\text{dilepton}} = 172.94 \pm 0.41$ (stat) $\pm 0.73$ (syst) GeV with an uncertainty of $0.84 \pm 0.05$ GeV. As a consequence of the influence of the measurements in the other decay channels discussed in the main text, this result does not coincide with the $t\bar{t} \rightarrow$ dilepton result at $\sqrt{s} = 8$ TeV.

In Fig. 14, the most precise ATLAS results of $m_{top}$ per decay channel and the new ATLAS combined value of $m_{top}$ are compared with the respective results from the CDF, D0 and CMS experiments.
The individual components of the JES uncertainty considered for the \( \bar{t}t \) \to lepton + jets analysis at \( \sqrt{s} = 8 \) TeV, the resulting JES- and bJES-uncertainty-induced shifts in \( m_{\text{top}} \) and the final uncertainty in \( m_{\text{top}} \). The components [63] together with their statistical precisions are listed in boldface and, wherever applicable, calculated as the sum in quadrature of the respective subcomponents. A shift listed as ‘0’ means that the corresponding variation resulted in an unchanged event sample. Uncertainties quoted as 0.00 (0.000) are smaller than 0.005 (0.0005).

In the rightmost column, the mapping to the uncertainty components used for \( \sqrt{s} = 7 \) TeV data is given for the weak and the strong correlation scenarios. The ‘+’ sign indicates corresponding components at the two centre-of-mass energies for the weak and strong scenario, while the ‘(+)’ sign indicates components that only correspond for the strong scenario. Finally, mentioning a name indicates that the mapped sources carry different names at \( \sqrt{s} = 7 \) and 8 TeV. The uncertainty components and the total uncertainty are given with 0.01 GeV precision. The term nuisance parameter is denoted by NuP. The last line refers to the sum in quadrature of the JES components.

<table>
<thead>
<tr>
<th>JES uncertainty components</th>
<th>( \Delta m_{\text{top}}^{\text{up}} ) [GeV]</th>
<th>( \Delta m_{\text{top}}^{\text{dw}} ) [GeV]</th>
<th>( \Delta m_{\text{top}} ) [GeV]</th>
<th>Map to ( \sqrt{s} = 7 ) TeV</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Statistical (total)</strong></td>
<td></td>
<td></td>
<td></td>
<td>0.17 ± 0.01</td>
</tr>
<tr>
<td>Statistical NuP1</td>
<td>−0.159</td>
<td>+0.151</td>
<td>−0.155</td>
<td>(+)</td>
</tr>
<tr>
<td>Statistical NuP2</td>
<td>−0.008</td>
<td>+0.048</td>
<td>−0.028</td>
<td>(+)</td>
</tr>
<tr>
<td>Statistical NuP3</td>
<td>+0.063</td>
<td>−0.035</td>
<td>+0.049</td>
<td>(+)</td>
</tr>
<tr>
<td>Statistical NuP4</td>
<td>+0.020</td>
<td>+0.022</td>
<td>+0.022</td>
<td>(+)</td>
</tr>
<tr>
<td>( \eta ) inter-calibration (stat.)</td>
<td>−0.062</td>
<td>+0.020</td>
<td>−0.041</td>
<td>(+)</td>
</tr>
<tr>
<td><strong>Modelling (total)</strong></td>
<td></td>
<td></td>
<td></td>
<td>0.38 ± 0.02</td>
</tr>
<tr>
<td>Modelling NuP1</td>
<td>−0.372</td>
<td>+0.389</td>
<td>−0.380</td>
<td>(+)</td>
</tr>
<tr>
<td>Modelling NuP2</td>
<td>+0.029</td>
<td>−0.000</td>
<td>+0.014</td>
<td>(+)</td>
</tr>
<tr>
<td>Modelling NuP3</td>
<td>+0.010</td>
<td>+0.005</td>
<td>+0.010</td>
<td>(+)</td>
</tr>
<tr>
<td>Modelling NuP4</td>
<td>+0.034</td>
<td>−0.026</td>
<td>+0.030</td>
<td>(+)</td>
</tr>
<tr>
<td>( \eta ) inter-calibration (model)</td>
<td>+0.056</td>
<td>−0.038</td>
<td>+0.047</td>
<td>(+)</td>
</tr>
<tr>
<td><strong>Detector (total)</strong></td>
<td></td>
<td></td>
<td></td>
<td>0.11 ± 0.01</td>
</tr>
<tr>
<td>Detector NuP1</td>
<td>+0.116</td>
<td>−0.103</td>
<td>+0.110</td>
<td>(+)</td>
</tr>
<tr>
<td>Detector NuP2</td>
<td>−0.015</td>
<td>+0.017</td>
<td>−0.016</td>
<td>(+)</td>
</tr>
<tr>
<td>Detector NuP3</td>
<td>+0.015</td>
<td>−0.014</td>
<td>+0.015</td>
<td>(+)</td>
</tr>
<tr>
<td><strong>Mixed (total)</strong></td>
<td></td>
<td></td>
<td></td>
<td>0.09 ± 0.01</td>
</tr>
<tr>
<td>Mixed NuP1</td>
<td>−0.004</td>
<td>−0.029</td>
<td>−0.029</td>
<td>(+)</td>
</tr>
<tr>
<td>Mixed NuP2</td>
<td>+0.053</td>
<td>−0.054</td>
<td>+0.054</td>
<td>(+)</td>
</tr>
<tr>
<td>Mixed NuP3</td>
<td>−0.044</td>
<td>+0.061</td>
<td>−0.052</td>
<td>(+)</td>
</tr>
<tr>
<td>Mixed NuP4</td>
<td>+0.039</td>
<td>−0.016</td>
<td>+0.028</td>
<td>(+)</td>
</tr>
<tr>
<td><strong>Single particle high-( p_T )</strong></td>
<td>0</td>
<td>+0.005</td>
<td>+0.005</td>
<td>(+)</td>
</tr>
<tr>
<td><strong>Pile-up (total)</strong></td>
<td></td>
<td></td>
<td></td>
<td>0.01 ± 0.00</td>
</tr>
<tr>
<td>Pile-up: offset (( \mu ))</td>
<td>+0.041</td>
<td>−0.040</td>
<td>+0.041</td>
<td>(+)</td>
</tr>
<tr>
<td>Pile-up: offset (( n_{\text{ch}} ))</td>
<td>+0.065</td>
<td>−0.083</td>
<td>+0.074</td>
<td>(+)</td>
</tr>
<tr>
<td>Pile-up: ( p_T )</td>
<td>+0.042</td>
<td>+0.040</td>
<td>+0.042</td>
<td>(+)</td>
</tr>
<tr>
<td>Pile-up: ( \rho )</td>
<td>−0.173</td>
<td>+0.141</td>
<td>−0.157</td>
<td>(+)</td>
</tr>
<tr>
<td><strong>Punch-through</strong></td>
<td></td>
<td></td>
<td></td>
<td>0.02 ± 0.01</td>
</tr>
<tr>
<td>Punch-through</td>
<td>+0.013</td>
<td>+0.017</td>
<td>+0.017</td>
<td>(+)</td>
</tr>
<tr>
<td><strong>Flavour (total)</strong></td>
<td></td>
<td></td>
<td></td>
<td>0.24 ± 0.02</td>
</tr>
<tr>
<td>Flavour composition</td>
<td>+0.079</td>
<td>−0.119</td>
<td>+0.099</td>
<td>(+)</td>
</tr>
<tr>
<td>Flavour response</td>
<td>+0.220</td>
<td>−0.211</td>
<td>+0.215</td>
<td>(+)</td>
</tr>
<tr>
<td><strong>bJES</strong></td>
<td></td>
<td></td>
<td></td>
<td>0.03 ± 0.01</td>
</tr>
<tr>
<td>bJES</td>
<td>+0.006</td>
<td>−0.047</td>
<td>+0.026</td>
<td>(+)</td>
</tr>
<tr>
<td><strong>Total (without bJES)</strong></td>
<td></td>
<td></td>
<td></td>
<td>0.54 ± 0.02</td>
</tr>
</tbody>
</table>
The sum in quadrature of the nuisance parameter $0.005 (0.0005)$. The term \( m_{\text{top}} \) are smaller than 0.01 GeV precision. The uncertainty components are quoted as the difference from the nominal sample. The total uncertainty is calculated as the sum in quadrature of the subcomponents and given with 0.01 GeV precision. The term nuisance parameter is denoted by \( \text{NuP} \).

<table>
<thead>
<tr>
<th>JER uncertainty components</th>
<th>( \Delta m_{\text{top}} ) [GeV]</th>
<th>( \Delta m_{\text{top}}^{\text{up}} ) [GeV]</th>
<th>( \Delta m_{\text{top}}^{\text{down}} ) [GeV]</th>
</tr>
</thead>
<tbody>
<tr>
<td>JER data versus simulation difference</td>
<td>-0.034</td>
<td>0.055</td>
<td></td>
</tr>
<tr>
<td>JER noise forward region</td>
<td>+0.032</td>
<td>0.013</td>
<td></td>
</tr>
<tr>
<td>JER NuP1 (only down var.)</td>
<td>-0.111</td>
<td>0.052</td>
<td></td>
</tr>
<tr>
<td>JER NuP2</td>
<td>-0.034</td>
<td>0.055</td>
<td></td>
</tr>
<tr>
<td>JER NuP3</td>
<td>+0.025</td>
<td>-0.084</td>
<td></td>
</tr>
<tr>
<td>JER NuP4</td>
<td>-0.074</td>
<td>0.090</td>
<td></td>
</tr>
<tr>
<td>JER NuP5</td>
<td>+0.078</td>
<td>0.016</td>
<td></td>
</tr>
<tr>
<td>JER NuP6</td>
<td>-0.041</td>
<td>0.017</td>
<td></td>
</tr>
<tr>
<td>JER NuP7</td>
<td>-0.039</td>
<td>0.076</td>
<td></td>
</tr>
<tr>
<td>JER NuP8</td>
<td>-0.053</td>
<td>0.013</td>
<td></td>
</tr>
<tr>
<td>JER NuP9 (only up var.)</td>
<td>+0.036</td>
<td>0.018</td>
<td></td>
</tr>
<tr>
<td>Total</td>
<td>0.20</td>
<td>0.04</td>
<td></td>
</tr>
</tbody>
</table>

**Table 12** The individual components of the JER uncertainty considered for the \( t\bar{t} \rightarrow \text{lepton} + \text{jets} \) analysis at \( \sqrt{s} = 8 \text{ TeV} \), the resulting JER-uncertainty-induced shifts in \( m_{\text{top}} \) and the final uncertainty in \( m_{\text{top}} \). The data versus simulation difference and noise forward region components are quoted as the difference from the nominal sample. The total uncertainty is calculated as the sum in quadrature of the subcomponents and given with 0.01 GeV precision. The term nuisance parameter is denoted by \( \text{NuP} \).

<table>
<thead>
<tr>
<th>Flavour-tagging uncertainty components</th>
<th>( \Delta m_{\text{top}} ) [GeV]</th>
<th>( \Delta m_{\text{top}}^{\text{up}} ) [GeV]</th>
<th>( \Delta m_{\text{top}}^{\text{down}} ) [GeV]</th>
</tr>
</thead>
<tbody>
<tr>
<td>b-tagging scale factor variations</td>
<td>0.31</td>
<td>0.00</td>
<td></td>
</tr>
<tr>
<td>b-tagging NuP1</td>
<td>+0.050</td>
<td>-0.062</td>
<td></td>
</tr>
<tr>
<td>b-tagging NuP2</td>
<td>-0.230</td>
<td>+0.143</td>
<td></td>
</tr>
<tr>
<td>b-tagging NuP3</td>
<td>-0.090</td>
<td>+0.005</td>
<td></td>
</tr>
<tr>
<td>b-tagging NuP4</td>
<td>+0.090</td>
<td>-0.175</td>
<td></td>
</tr>
<tr>
<td>b-tagging NuP5</td>
<td>-0.230</td>
<td>+0.148</td>
<td></td>
</tr>
<tr>
<td>b-tagging NuP6</td>
<td>+0.023</td>
<td>-0.105</td>
<td></td>
</tr>
<tr>
<td>c/( \tau )-tagging scale factor variations</td>
<td>0.15</td>
<td>0.00</td>
<td></td>
</tr>
<tr>
<td>c/( \tau )-tagging NuP1</td>
<td>+0.098</td>
<td>-0.102</td>
<td></td>
</tr>
<tr>
<td>c/( \tau )-tagging NuP2</td>
<td>-0.057</td>
<td>-0.026</td>
<td></td>
</tr>
<tr>
<td>c/( \tau )-tagging NuP3</td>
<td>+0.046</td>
<td>-0.125</td>
<td></td>
</tr>
<tr>
<td>c/( \tau )-tagging NuP4</td>
<td>-0.057</td>
<td>-0.023</td>
<td></td>
</tr>
<tr>
<td>Mistagging scale factor variations</td>
<td>0.16</td>
<td>0.00</td>
<td></td>
</tr>
<tr>
<td>Mistagging NuP1</td>
<td>-0.005</td>
<td>+0.003</td>
<td></td>
</tr>
<tr>
<td>Mistagging NuP2</td>
<td>-0.042</td>
<td>-0.039</td>
<td></td>
</tr>
<tr>
<td>Mistagging NuP3</td>
<td>-0.038</td>
<td>-0.036</td>
<td></td>
</tr>
<tr>
<td>Mistagging NuP4</td>
<td>-0.032</td>
<td>-0.040</td>
<td></td>
</tr>
<tr>
<td>Mistagging NuP5</td>
<td>-0.037</td>
<td>-0.044</td>
<td></td>
</tr>
<tr>
<td>Mistagging NuP6</td>
<td>-0.036</td>
<td>-0.045</td>
<td></td>
</tr>
<tr>
<td>Mistagging NuP7</td>
<td>-0.034</td>
<td>-0.040</td>
<td></td>
</tr>
<tr>
<td>Mistagging NuP8</td>
<td>-0.041</td>
<td>-0.040</td>
<td></td>
</tr>
<tr>
<td>Mistagging NuP9</td>
<td>-0.029</td>
<td>-0.045</td>
<td></td>
</tr>
<tr>
<td>Mistagging NuP10</td>
<td>-0.073</td>
<td>-0.001</td>
<td></td>
</tr>
<tr>
<td>Mistagging NuP11</td>
<td>-0.026</td>
<td>-0.055</td>
<td></td>
</tr>
<tr>
<td>Mistagging NuP12</td>
<td>+0.007</td>
<td>-0.095</td>
<td></td>
</tr>
<tr>
<td>Total</td>
<td>0.38</td>
<td>0.00</td>
<td></td>
</tr>
</tbody>
</table>
Fig. 13 Selected combinations of the six ATLAS measurements of $m_{\text{top}}$ according to importance. The figures show the combined result when successively adding results to the most precise one of a given category. Each line of this figure shows the combined result when adding the result listed to the combination, indicated by a ‘+’. The values quoted are the combined value, the statistical uncertainty, the systematic uncertainty, the total uncertainty and the uncertainty in the total uncertainty, which is statistical. a and b refer to the independent combinations of the three measurements per centre-of-mass energy resulting in uncorrelated results $m_{\text{top}}^{7\text{ TeV}}$ and $m_{\text{top}}^{8\text{ TeV}}$. c–e refer to the combination of the three correlated observables from pairs of measurements per $t\bar{t}$ decay channel, resulting in $m_{\text{top}}^{\text{dilepton}}$, $m_{\text{top}}^{\ell+\text{jets}}$ and $m_{\text{top}}^{\text{all jets}}$. 
Fig. 14 The most precise result of $m_{\text{top}}$ per experiment in the different $t\bar{t}$ decay channels and $m_{\text{top}}$ from the latest combinations performed by the individual experiments. 

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94. ATLAS Collaboration, Data-driven determination of the energy scale and resolution of jets reconstructed in the ATLAS calorimeters using dijet and multijet events at $\sqrt{s} = 8$ TeV. ATLAS-CONF-2015-017 (2015). https://cds.cern.ch/record/2008678
99. R. Nisius, A ROOT class to combine a number of correlated estimates of one or more observables using the Best Linear Unbiased Estimate method (2015). http://blue.hepforge.org/Bluemanual.pdf

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