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WASP-4b Arrived Early for the TESS Mission


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ABSTRACT

The Transiting Exoplanet Survey Satellite (TESS) recently observed 18 transits of the hot Jupiter WASP-4b. The sequence of transits occurred 81.6 ± 11.7 seconds earlier than had been predicted, based on data stretching back to 2007. This is unlikely to be the result of a clock error, because TESS observations of other hot Jupiters (WASP-6b, 18b, and 46b) are compatible with a constant period, ruling out an 81.6-second offset at the 6.4σ level. The 1.3-day orbital period of WASP-4b appears to be decreasing at a rate of \( \dot{P} = -12.6 \pm 1.2 \) milliseconds per year. The apparent period change might be caused by tidal orbital decay or apsidal precession, although both interpretations have shortcomings. The gravitational influence of a third body is another possibility, though at present there is minimal evidence for such a body. Further observations are needed to confirm and understand the timing variation.

Keywords: planet-star interactions — planets and satellites: individual (WASP-4b, WASP-5b, WASP-6b, WASP-12b, WASP-18b, WASP-46b) — binaries: close

1. INTRODUCTION

Although the Transiting Exoplanet Survey Satellite (TESS, Ricker et al. 2015) is designed to detect new planets, it is also precisely monitoring most of the planets that have been discovered by ground-based transit surveys over the last two decades. One application of the new TESS data is to search for timing anomalies in previously known hot Jupiter systems. Long-term monitoring of hot Jupiter transit and occultation times should eventually reveal variations caused by three different phenomena.

First, the orbits of most hot Jupiters should shrink because of tidal orbital decay (Counselman 1973; Hut 1980; Levrard et al. 2009; Matsumura et al. 2010). Directly measuring the rate of decay might lead to an improved understanding of how friction dissipates the energy of tidal disturbances (a problem reviewed by Mazeh 2008 and Ogilvie 2014). Second, if hot Jupiter orbits are appreciably eccentric, then long-term timing studies should reveal rotation of the orbital ellipse within the orbital plane (“apsidal precession”). If this effect were observed, it could yield a measure of the planet’s Love number, which would constrain the planet’s interior structure (Ragozzine & Wolf 2009). The most convincing direct evidence yet found for either orbital decay or apsidal precession of a hot Jupiter is the case of WASP-12b, which has a transit period that has decreased by about 30 millisecond-
onds per year over the last decade (Maciejewski et al. 2016; Patra et al. 2017).

The final effect of interest that can produce period changes in hot Jupiter systems is gravitational acceleration caused by massive outer companions (e.g., Agol et al. 2005, Section 4). Prototypes include WASP-53 and WASP-81, systems in which the inner hot Jupiters are periodically perturbed by eccentric brown dwarf companions with semimajor axes of a few astronomical units (Triaud et al. 2017).

Here, we present evidence for a timing anomaly in the WASP-4 system. The hot Jupiter WASP-4b orbits a G7V star every 1.34 days, corresponding to an orbital distance of 5.5 stellar radii (Wilson et al. 2008; Huitson et al. 2017). It is a good target to search for departures from a constant period, because transits have been observed since 2007. The orbital eccentricity is less than 0.018 (2σ), based on the work of Knutson et al. (2014), who combined the available transit times, occultation times, and Doppler data. The sky projection of the stellar obliquity is also compatible with zero, within about 10 degrees (Triaud et al. 2010; Sanchis-Ojeda et al. 2011).

In what follows, § 2 presents the new TESS observations, and § 3 describes our timing analysis. We tried fitting the data with three models: a constant period; a steadily shrinking period; and a slightly eccentric, precessing orbit. A constant period can be ruled out. We cannot distinguish between the possibilities of a decaying orbit, a precessing orbit, and the unmodeled possibility of an orbit being gravitationally perturbed by an outer companion. Any of the three scenarios would have interesting implications (§ 4), and more data are required for a definitive ruling (§ 5). Appendix A considers the possibility that the WASP-4 timing anomaly is due to an error in timestamps in the TESS data products. We found this possibility to be unlikely because none of the other hot Jupiters we examined show a timing offset with the same amplitude as was seen for WASP-4.

2. NEW TRANSITS AND SYSTEM PARAMETERS

2.1. Observations

WASP-4 was observed by TESS with Camera 2 from August 23 to September 20, 2018, within the second “sector” of science operations. The star is designated as TIC 402026209 in the TESS Input Catalog (Stassun et al. 2018). The pixel data for an 11 × 11 array surrounding WASP-4 were averaged into 2-minute stacks by the onboard computer. The data were downlinked via the Deep Space Network\(^1\), and the spacecraft timestamps were calibrated against the ground-station clocks. The spacecraft clock times were then transformed by the Payload Operations Center into the Temps Dynamique Barycentrique (TDB) reference system. The images were then reduced to lightcurves by the Science Processing Operations Center (SPOC) at NASA Ames (Jenkins et al. 2016). During this processing, the SPOC used the known spacecraft trajectory to compute the barycentric time corrections on a target by target basis, and expressed the timestamps as Barycentric TESS Julian Dates (BTTJD), which is simply the Barycentric Julian Date minus 2,457,000. Lightcurves that were flagged by the SPOC pipeline as crossing a transit detection threshold were then vetted and released by the MIT TESS Science Office to the Mikulski Archive for Space Telescopes on November 29, 2018 (Ricker & Vanderspek 2018).

We began our analysis with the Presearch Data Conditioning (PDC) lightcurve, which has had non-astrophysical variability removed through the methods discussed by Smith et al. (2017a) and Smith et al. (2017b). We then processed the lightcurve as follows. First, we removed all points with non-zero quality flags. This removed data that might have been adversely affected by “momentum dumps,” the firing of thrusters and resetting of reaction wheels\(^2\) that took place every 2.5 days during sector 2. The data during these events were assigned quality flags corresponding to “Action Wheel Desaturation Event” and “Manual Exclude” (Tenenbaum & Jenkins 2018, Table 28). For WASP-4, these flags were simultaneously set for 54 distinct cadences, and there were 10 momentum dumps, averaging about 10 minutes of flagged data per dump. Out of caution, we clipped out an additional 10 minutes before and after every momentum dump. We also removed the data within the first and last hours of both orbits, because of correlated red noise that appears during those time ranges.

All told, we removed 8% of the original data points, and were left with 18,165 measurements of the relative flux of WASP-4. We normalized the data by dividing out the median flux. We converted the timestamps from BTJD\(^2\) into BJD\(^2\) by adding the appropriate 2,457,000 day offset (Tenenbaum & Jenkins 2018). Many of these and subsequent processing steps were performed using astrobase (Bhatti et al. 2018). We did not “flatten” the lightcurves, as is often done with splines, polynomials, or Gaussian processes. Instead, we modeled the out-of-transit flux variations simultaneously with the transit parameters, as described below.

2.2. Measuring the transit times

Using the cleaned PDC lightcurve, we applied the Box Least Squares algorithm (Kovács et al. 2002) to estimate the orbital period, transit duration, and a reference epoch using the TESS data alone. Based on the results, we isolated the data within 4 transit durations of each transit midpoint. To find the transit parameters that best fit the data, we first fitted a line to the out-of-transit flux measurements surrounding each transit, and divided it out. We then created a phase-folded lightcurve from all 18 transits and fitted a standard transit model using the analytic formulae given by Mandel & Agol (2002) and implemented by Kreidberg (2015, BATMAN). We assumed the orbit to be circular, consistent with the limits from radial velocities and occultation timing (Beerrer et al.

\(^1\) deepspace.jpl.nasa.gov

\(^2\) The spacecraft pointing and momentum dumps are described in the data release notes: archive.stsci.edu/missions/tess/doc/tess_drn/tess_sector_02_drn02_v01.pdf
Figure 1. TESS observations of WASP-4b. On the left, black points are TESS flux measurements, with a vertical offset applied. Blue curves are best-fit models. The numbers printed next to each lightcurve are the approximate transit times expressed in BJD minus 2,457,000. The right side shows the residuals.
Figure 2. Phase-folded lightcurve of WASP-4b. Gray points are TESS flux measurements, with median 1σ uncertainty shown in the lower right. Yellow points are binned measurements. The bottom panel shows the residuals. The fit to the phase-folded transit (blue line) is used when measuring mid-transit times of individual transits (see § 2.2).

2011; Knutson et al. 2014; Bonomo et al. 2017). The free parameters were the reference epoch, the planet to star radius ratio \( R_p/R_\star \), the orbital distance to stellar radius ratio \( a/R_\star \), the inclination \( i \), two quadratic limb-darkening coefficients \( u_{\text{linear}}, u_{\text{quad}} \), and the orbital period \( P \).

We sampled the posterior probability distribution for all the parameters using the algorithm proposed by Goodman & Weare (2010) and implemented by Foreman-Mackey et al. (2013, emcee). Table 1 gives the results, which are in reasonable agreement with the parameters reported by e.g., Southworth et al. (2009) and Huittson et al. (2017). Figure 2 shows the phase-folded lightcurve.

To measure the transit times, we returned to the ‘cleaned’ PDC time series and fitted the data within four transit durations of each transit separately. We used four free parameters: the time of mid-transit \( t_{\text{tra}} \), the planet-to-star radius ratio, and the slope and intercept of a linear trend to account for any slow variations unrelated to the transit. We fixed the remaining parameters at the values that had been determined from the phase-folded TESS lightcurve. The uncertainty in each photometric data point was set equal to the root-mean-square (rms) level of the out-of-transit data.

To verify that the measured uncertainties are estimated accurately, we computed the \( \chi^2 \) value for a linear ephemeris fit to the measured TESS mid-transit times. We found that \( \chi^2 = 9.2 \), with \( n = 16 \) degrees of freedom. The variance of the \( \chi^2 \) distribution is \( 2n \), so we would expect \( \chi^2 = 16 \pm 5.7 \). Visually inspecting the residuals showed that the error variance had been overestimated, so we multiplied the measured TESS errors by a factor \( f = 0.76 \), forcing a reduced \( \chi^2 \) of unity. This lowered the mean uncertainty of the transit midtimes from 29.8 to 22.6 seconds. We verified that omitting this step did not appreciably alter any of our conclusions.

Figure 1 shows the lightcurve of each individual transit, the best-fit models, and the residuals. Table 2 reports the mid-transit times and their uncertainties. After binning the residuals to 1-hour windows, the lightcurves have an rms scatter of 586 ppm. The pre-launch TESS noise model\(^3\) (Winn 2013, Sullivan et al. 2015 Section 6.4) would have predicted an error budget consisting of the following terms added in quadrature: 410 ppm from photon-counting noise, 202 ppm from detector read noise, and 673 ppm from the zodiacal background light. The level of background light appears to have been overestimated in the model.

2.3. Star and planet parameters

We calculated the stellar and planetary parameters in the following way. We computed the star’s spectral energy distribution based on the Gaia DR2 parallax (after making the small correction advocated by Stassun & Torres 2018) and the broadband magnitudes from the available all-sky catalogs: \( G \) from Gaia DR2, \( B_T \) and \( V_T \) from Tycho-2, \( BVgr \) from APASS, \( JHK_\text{S} \) from 2MASS, and the WISE 1–4 passbands, thus spanning the wavelength range 0.4–22 \( \mu \)m. We adopted the effective temperature from the work by Doyle et al. (2013), who determined the spectroscopic parameters of WASP-4 using high-signal-to-noise observations with the High Accuracy Radial-velocity Planet Searcher (HARPS). Then, we determined the stellar radius through the combination of the bolometric luminosity and the effective temperature, using the Stefan-Boltzmann law. To determine the stellar mass, we first computed the mean stellar density based on the value of \( a/R_\star \), that gave the best fit to the phase-folded

\(^3\) github.com/lgbouma/tnm, commit be06f09
TESS lightcurve (for the relevant equation, see Seager & Mallén-Ornelas 2003 or Winn 2010). The mass was calculated from the radius and density, and the orbital distance was also calculated from the radius and $a/R_\star$. The planetary radius was calculated as the product of $R_e$ and $R_\text{p}/R_\star$. Finally, the planet mass was calculated based on the stellar mass, the radial-velocity amplitude observed by Triaud et al. (2010), and the orbital inclination.

Table 1 gives the resulting parameters, which we adopted for the remaining analysis. The uncertainties in our derived stellar and planetary parameters are propagated according to standard analytic formulae, under the assumption that the variables are uncorrelated and normally distributed. Our system parameters are in agreement with those of previous investigators, but have the benefit of incorporating the Gaia parallax (Wilson et al. 2008; Gillon et al. 2009a; Winn et al. 2009; Southworth 2011; Petrucci et al. 2013; Huitson et al. 2017). By comparing the star’s luminosity and spectroscopic parameters with the outputs of the Yonsei-Yale stellar-evolutionary models, we found that WASP-4 is a main-sequence star with an age of approximately 7 Gyr (Demarque et al. 2004).

### 3. TIMING ANALYSIS

#### 3.1. Pre-TESS timing measurements

Table 2 gives the transit times we used in our analysis. We included data from peer-reviewed literature for which the analysis was based on observations of a single transit, and for which the midpoint was allowed to be a free parameter.

### Table 1. Selected system parameters of WASP-4b

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
<th>68% Confidence Interval</th>
<th>Comment</th>
</tr>
</thead>
<tbody>
<tr>
<td>$R_p/R_\star$</td>
<td>0.15201</td>
<td>+0.00040, −0.00033</td>
<td>A</td>
</tr>
<tr>
<td>$i$ [deg]</td>
<td>89.06</td>
<td>+0.65, −0.84</td>
<td>A</td>
</tr>
<tr>
<td>$a/R_\star$</td>
<td>5.451</td>
<td>+0.023, −0.052</td>
<td>A</td>
</tr>
<tr>
<td>$M_\text{sin}e$</td>
<td>0.382</td>
<td>—</td>
<td>A</td>
</tr>
<tr>
<td>$M_\text{quad}$</td>
<td>0.210</td>
<td>—</td>
<td>A</td>
</tr>
<tr>
<td>$K$ [m s$^{-1}$]</td>
<td>241.1</td>
<td>+2.8, −3.1</td>
<td>B</td>
</tr>
<tr>
<td><strong>Stellar parameters:</strong></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$T_\text{eff}$ [K]</td>
<td>5400</td>
<td>±90</td>
<td>C</td>
</tr>
<tr>
<td>$\log g_\star$ [cgs]</td>
<td>4.47</td>
<td>±0.11</td>
<td>C</td>
</tr>
<tr>
<td>$[\text{Fe/H}]$</td>
<td>−0.07</td>
<td>±0.19</td>
<td>C</td>
</tr>
<tr>
<td>$R_\text{bol}$ [erg cm$^{-2}$ s$^{-1}$]</td>
<td>$2.802 \times 10^{-10}$</td>
<td>±0.076 $\times 10^{-10}$</td>
<td>D</td>
</tr>
<tr>
<td>$A_V$ [mag]</td>
<td>0.03</td>
<td>+0.02, −0.01</td>
<td>D</td>
</tr>
<tr>
<td>$\pi$ [mas]</td>
<td>3.7145</td>
<td>0.0517</td>
<td>F</td>
</tr>
<tr>
<td>$R_\star$ [R$_\odot$]</td>
<td>0.893</td>
<td>±0.034</td>
<td>E</td>
</tr>
<tr>
<td>$\rho_\star$ [g cm$^{-3}$]</td>
<td>1.711</td>
<td>+0.022, −0.048</td>
<td>E</td>
</tr>
<tr>
<td>$M_\star$ [M$_\odot$]</td>
<td>0.864</td>
<td>+0.084, −0.090</td>
<td>E</td>
</tr>
<tr>
<td>$T$ magnitude</td>
<td>11.778</td>
<td>±0.018</td>
<td>G</td>
</tr>
<tr>
<td><strong>Planetary parameters:</strong></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$a$ [AU]</td>
<td>0.0226</td>
<td>+0.0007, −0.0008</td>
<td>E</td>
</tr>
<tr>
<td>$M_\text{p}$ [M$_\oplus$]</td>
<td>1.186</td>
<td>+0.090, −0.098</td>
<td>E</td>
</tr>
<tr>
<td>$R_\text{p}$ [R$_\oplus$]</td>
<td>1.321</td>
<td>±0.039</td>
<td>E</td>
</tr>
</tbody>
</table>

**Note:** (A) From phase-folded TESS lightcurve (§2.2). Orbital periods are in Table 4. The limb darkening parameters were allowed to float around the Claret (2017) prediction, but were unconstrained. (B) Triaud et al. (2010). (C) From HARPS spectra (Doyle et al. 2013). (D) Stassun et al. (2017). (E) This work, see §2.3. (F) Gaia Collaboration et al. (2018). (G) Stassun et al. (2018).

We also required that the time system be clearly documented. Many of the times were previously compiled by Hoyer et al. (2013). We confirmed that the times in that paper were in agreement with the original sources and that barycentric corrections had been performed when needed.

The earliest epoch is from EulerCam on the 1.2-m Euler telescope (Wilson et al. 2008). The second epoch is based on $z$-band photometry acquired by Gillon et al. (2009b) at
Figure 4. Timing residuals and best-fit models for WASP-4b. The vertical axis shows the observed times minus the calculated times assuming a constant period for transits (top) and occultations (bottom). In the upper panel, darker points correspond to more precise data. The constant-period model (gray line) is a poor description of the data. Models with a decreasing period (blue) or an eccentric, precessing orbit (orange) provide better fits. The binned TESS point (red square) is the weighted average of 18 TESS transits and is for display purposes only. The models were fitted to all of the individual transit times.

We also compiled the available occultation times, which are given in Table 3. The tabulated values have been corrected for the light-travel time across the diameter of the orbit by subtracting $2a/c = 22.8$ seconds from the observed time. Be'er et al. (2011) detected an occultation from the ground in the $K_s$ band, and gave a time in HJD, without specifying the time standard. We assumed the standard was UTC, and performed the appropriate corrections to convert to BJD$_{TDB}$. We verified that none of our conclusions would be changed if this assumption was mistaken. Finally, Zhou et al. (2015) observed an occultation with the Anglo-Australian Telescope. They did not report the observed midpoint, but they did report a result for $e \cos \omega$ based upon the observed midpoint. We calculated the implied midpoint using the formula (e.g., Winn 2010)

$$t_{occ}(E) = t_0 + P E + \frac{P}{2} \left( 1 + \frac{4}{\pi} e \cos \omega \right),$$

for $E$ the transit number, $t_0$ the reference epoch, $e$ the eccentricity, and $\omega$ the argument of pericenter. In total, there are four available occultation times.

3.2. Analysis

First, we performed a weighted least-squares fit of a constant-period model (a “linear ephemeris”) to the pre-TESS data, and used it to extrapolate to the epochs of the TESS observations. The residuals of the best fitting model are shown in Figure 3. The transits observed by TESS occurred earlier than expected. Because the TESS mission is...
still in an early stage, we were concerned about a possible offset in the TESS timestamps due to an error with the TESS clock or the data processing pipeline. Appendix A describes some tests that convinced us that a simple offset is unlikely. Assuming that the observed timing variation is astrophysical, we proceeded by exploring three models for the timing data in a manner identical to the study by Patra et al. (2017).

The first model assumes a constant orbital period on a circular orbit:

\[ t_{\text{tra}}(E) = t_0 + P_E E, \]
\[ t_{\text{occ}}(E) = t_0 + \frac{P}{2} + P_E E, \]

where \( E \) is the epoch number. We defined the epoch numbers such that \( E = 0 \) is near the weighted average of the observed times. This helps to reduce the covariance between the

The second model assumes the period is changing at a steady rate:

\[ t_{\text{tra}}(E) = t_0 + P_E E + \frac{1}{2} \frac{\partial P}{\partial E} E^2, \]
\[ t_{\text{occ}}(E) = t_0 + \frac{P}{2} + P_E E + \frac{1}{2} \frac{\partial P}{\partial E} E^2. \]

The three free parameters are the reference epoch \( t_0 \), the period at the reference epoch, and the period derivative, \( \frac{\partial P}{\partial E} \).

The third model assumes the planet has a slightly eccentric orbit, and that the line of apsides is rotating (Giménez & Bastero 1995):

\[ t_{\text{tra}}(E) = t_0 + P_E E - \frac{P_a}{\pi} \cos \omega, \]
\[ t_{\text{occ}}(E) = t_0 + \frac{P}{2} + P_E E + \frac{P_a}{\pi} \cos \omega, \]

where \( P_s \) is the sidereal period, \( e \) is the eccentricity, \( P_a \) is the anomalistic period, and \( \omega \) is the argument of pericenter. In this model the angular velocity of the line of apsides \( \frac{d\omega}{dE} \) is constant,

\[ \omega(E) = \omega_0 + \frac{d\omega}{dE} E, \]

and the sidereal and anomalistic periods are connected through the equation

\[ P_s = P_a \left( 1 - \frac{1}{2\pi} \frac{d\omega}{dE} \right). \]

The sidereal period is the duration required to return to the same orientation with respect to the stars; the slightly longer anomalistic period is the duration required to reach a fixed longitude with respect to the rotating line of apsides. The five free parameters of this model are \( (t_0, P_s, e, \omega_0, \frac{d\omega}{dE}) \), denoting the reference epoch, the sidereal period, the eccentricity, the argument of pericenter at the reference epoch, and the angular velocity of the line of apsides.

We fitted each model by assuming a Gaussian likelihood and sampling over the posterior probability distributions.

The prior for the quadratic model allowed the period derivative to have any sign. We considered two possible priors for the precession model: the first is a wide prior that allows nonphysical values of the planetary Love number (Equation 18). The second prior requires that the planetary Love number is less than that of a sphere of constant density.

Figure 4 shows the residuals with respect to the constant-period model. The best-fitting constant-period model has \( \chi^2 = 174 \) and 61 degrees of freedom. The best-fitting quadratic model has \( \chi^2 = 62.6 \) and 60 degrees of freedom. The best-fitting precession model under the wide prior has \( \chi^2 = 64.3 \) and 58 degrees of freedom. Under the physical prior, the best-fit is slightly worse, with \( \chi^2 = 64.8 \). The precession and quadratic models both provide much better fits than the constant-period model. The difference in \( \chi^2 \) between the linear and quadratic models corresponds to \( p \approx 10^{-26} \).

The quadratic model provides a marginally better fit to the data than the precession model. It is favored by \( \Delta \chi^2 = 1.7 \), and has two fewer free parameters. A useful heuristic for model comparison is the Bayesian Information Criterion,

\[ \text{BIC} = \chi^2 + k \log n, \]

where \( k \) is the number of free parameters, and \( n \) is the number of data points. In this case, \( n = 62 \). The difference in the BIC between the precession and decay models is \( \Delta \text{BIC} = \text{BIC}_{\text{prec}} - \text{BIC}_{\text{quad}}\approx 10 \), assuming a wide prior for the precession model. This corresponds to a Bayes factor of \( 1.1 \times 10^4 \). Likewise, the Akaike Information Criterion favors the constant-period-derivative model by \( \Delta \text{AIC} = 5.8 \). Differences of this magnitude are traditionally deemed “strong evidence” that one model is a better description of the data than the other (Kass & Raftery 1995), although we prefer to reserve judgment until more data can be obtained.

In the quadratic model, the period derivative is

\[ \dot{P} = -(4.00 \pm 0.38) \times 10^{-10} = -12.6 \pm 1.2 \text{ ms yr}^{-1}. \]

For comparison, the best-fitting period derivative of WASP-12b is \( \dot{P} = -29 \pm 3 \text{ ms yr}^{-1} \) (Maciejewski et al. 2016; Patra et al. 2017). If both planets are truly falling onto their stars, then WASP-4b is falling at about half the rate of WASP-12b.

In the precession model, the best-fit eccentricity is

\[ e = (1.92^{+0.93}_{-0.76}) \times 10^{-3}. \]

The longitude of periastron advances by \( \dot{\omega} = 13.6^{+4.7}_{-3.6} \) degrees yr\(^{-1}\), and the precession period is \( 27^{+19}_{-10} \) years. All of the best-fitting parameters (the medians of the posterior distributions) and the 68% credible intervals are reported in Table 4.

### 3.3. Possible systematic errors

To assess the overall robustness of our results, we considered a few possible systematic effects in the timing dataset.

**Suspect pre-TESS light curves**—Some of the pre-TESS light curves have incomplete phase coverage: a handful of the
transit times in Table 2 are from lightcurves with gaps. A separate issue is the effect of spot-crossing anomalies on transit timings. To address these concerns, we repeated the model-fitting described above, but omitted epochs -827, -804, -537, and -208 because of gaps in their coverage. We also omitted epochs -526 and -561 because of visible spot anomalies during the transits. (All epoch numbers are as in Table 2.) The resulting best-fit transit timing model parameters were all within 1σ of the values quoted in Table 4. The uncertainties, goodness-of-fit statistics, and model comparison statistics did not appreciably change.

Spot-crossing events in TESS data—To explore the effect of possible spot-crossing events on the TESS transit time measurements, we performed a separate test. We injected triangular spot-anomalies with amplitude 0.03% and duration 30 minutes at random phases into each transit. The amplitude was chosen to be larger than the spot-crossing anomalies observed by Southworth et al. (2009) and Sanchis-Ojeda et al. (2011), and the duration was chosen to be comparable to those of previously observed events. Spots of these amplitudes resemble the possible anomalies present in transits “1360.54” and “1372.58” of Figure 1.

With spots injected, we repeated our measurement of the transit times. On average, the measured transit times did not change after injecting spots, because the flux deviations are equally likely to occur in the first and second halves of the transit. For individual transits, there were no cases for which the timing deviation was larger than one minute. The largest shifts occur when the spot anomaly occurs during transit ingress or egress, in which case the measured mid-time is shifted either late or early by between 30 and 50 seconds.

The TESS observations could therefore be skewed early if there were spot-crossing events during every egress. Two arguments rule out this possibility. (1) The lightcurve residuals do not show evidence for these events. (2) The stellar rotation period is between 20 and 40 days, and the sky-projected stellar obliquity is less than 10 degrees (Trijau et al. 2010; Sanchis-Ojeda et al. 2011; Hoyer et al. 2013). Since the planet orbits every 1.3 days, requiring that spot anomalies always occur during egress would be equivalent to requiring a stellar spot distribution that is exquisitely (and thus implausibly) distributed to match the planet egress times.

Detrending choices in pre-TESS data—There is a final concern that is difficult to address. We collected the mid-transit time values derived by different authors, who used heterogeneous methods to fit and detrend their lightcurves. We have also assumed that these authors have correctly documented the time systems in which the data are reported. Further, though many choices in transit-fitting (e.g., parametrization of limb-darkening and eccentricity) do not affect transit mid-time measurements, different detrending approaches can asymmetrically warp transits and shift mid-transit times. The magnitude of this systematic effect is hard to quantify, but the situation is fairly clear from Figure 4. Many independent authors provided transit measurements shortly after WASP-4b’s discovery, and the data are consistent with each other. Huitson et al. (2017) provided the most important data from epochs 0-1000. If their data were systematically affected by detrending choices or time-system confusion at the level of several times their reported uncertainties, then it is possible that the orbital period is constant despite the evidence in the TESS data. For this reason, we paid careful attention to the Huitson et al. (2017) data set, and corresponded with the authors to confirm that their results are not affected by systematic effects of the required amplitude.

None of the concerns mentioned in this subsection seem likely to explain the observed timing variations. We proceed by considering possible astrophysical explanations.

4. INTERPRETATION

4.1. Orbital decay

If the timing variation is caused entirely by orbital decay, then the best-fit model parameters yield a characteristic decay timescale of

$$\frac{P}{dP/dt} = 9.2 \text{Myr.}$$

For comparison, the corresponding time for WASP-12b is 3.2 Myr (Patra et al. 2017).

If WASP-4 really is undergoing rapid orbital decay, then how many of the other known hot Jupiters should have orbits that are decaying at detectable (or nearly detectable) rates? Figure 5 compares some key properties of WASP-4 with those of a larger ensemble of hot Jupiters. The middle panel displays two parameters that strongly affect the expected orbital decay timescale, $PM_{\text{eq}}/M_p$ and $a/R_\star$. WASP-4 has one of the shortest theoretical timescales for orbital decay. Figure 5 shows about 20 hot Jupiters (including WASP-12) for which the theoretical timescale is shorter. In almost all of those cases, though, the planet was discovered more recently than WASP-4 and a decade-long baseline of observations is not yet available. A separate consideration not shown in Figure 5 is that the hot Jupiter host stars have a variety of different structures, from being fully convective to nearly fully radiative, which may lead to widely divergent tidal dissipation timescales.

In the simple “constant phase lag” model for tidal interaction (Zahn 1977), the rate of dissipation can be parametrized by a modified quality factor, $Q' = 3Q/(2k_\ast)$. Here, $Q_\ast$ is the ratio between the energy stored in the equilibrium deformation of the star and the energy lost to heat per tidal period (e.g., Goldreich & Soter 1966). A larger $Q_\ast$ implies less efficient tidal dissipation. The dimensionless number $k_\ast$ is the stellar Love number, which is smaller when the star’s density distribution is more centrally concentrated. In this model, once the planet’s spin and orbit are synchronized, then the semi-major axis and eccentricity evolve as (Appendix B of

4 For stars, $k_\ast \sim \mathcal{O}(10^{-2})$, so it is important to explicitly distinguish $Q'$ from $Q_\ast$ (e.g., Schwarzschild 1958).
Figure 5. WASP-4b in the context of other hot Jupiters. Most of the data in these plots are from Bonomo et al. (2017), who measured the eccentricities using radial velocities. The colored symbols highlight WASP-4, WASP-12 (which also shows evidence for a decreasing period), and the hot Jupiters analyzed in Appendix A. **Top:** Key parameters relevant to eccentricity damping. Solid squares represent planets with a securely detected nonzero eccentricity. Circles represent planets whose orbits are consistent with circular. Lines of constant damping timescale are drawn based on Equation 14 and assuming $Q'_p = 10^5$. WASP-4b has one of the shortest eccentricity damping times. **Middle:** Key parameters relevant to orbital decay. Lines of constant decay timescale are drawn based on Equation 15, assuming $Q'_\star = 10^7$. WASP-4b has a relatively short orbital decay timescale, although it is not as extreme a case in this regard as it is for eccentricity damping. **Bottom:** A Hertzsprung-Russell diagram for hot Jupiter hosts. WASP-4 appears to be on the main sequence.
The orbital period evolves as
\[
\frac{1}{\tau_c} = \frac{|e|}{e} = \frac{63\pi}{2Q_p^5} \left( \frac{R_p}{a} \right) \left( \frac{M_*}{M_p} \right) \left( \frac{1}{P} \right)
\]
(14)
\[
\frac{1}{\tau_a} = \frac{|a|}{a} = \frac{9\pi}{Q_e^5} \left( \frac{R_*}{a} \right) \left( \frac{M_*}{M_p} \right) \left( \frac{1}{P} \right).
\]
(15)

The orbital period evolves as
\[
\dot{P} = -\frac{27\pi}{2Q_e^5} \left( \frac{M_*}{M_p} \right) \left( \frac{R_*}{a} \right)^5.
\]
(16)

The modified quality factor of WASP-4 corresponding to the observed value of \( \dot{P} \) is
\[
Q'_e = (2.9 \pm 0.3) \times 10^4.
\]
(17)

This is about an order of magnitude lower than the value that was inferred for WASP-12b. It is also smaller than most theoreticians would have expected. The \( Q'_\text{Jup} \) value of Jupiter is estimated to be \( \approx 1.4 \times 10^5 \), based on the observed motions of the Galilean moons (Lainey et al. 2009). For stars, studies of the binary eccentricity distribution have been interpreted with tidal models, giving \( Q'_e \approx 10^5 - 10^7 \) (e.g., Meibom & Mathieu 2005; Belczynski et al. 2008; Geller et al. 2013; Mil- liman et al. 2014). Population studies of hot Jupiter systems have also been undertaken, generally finding \( Q'_e \approx 10^5 - 10^8 \) using different models (Jackson et al. 2009; Hansen 2010; Geller et al. 2013; Penev et al. 2012, 2018; Collier Cameron & Jardine 2018). For instance, motivated by the rapid rotation of some hot Jupiter hosts (Pont 2009; Ciceri et al. 2016a; Penev et al. 2016), Penev et al. (2018) modeled the evolution of hot Jupiter systems under the influence of a magnetized wind and a constant phase-lag tide. For WASP-4, their method gave \( Q'_e \approx (1.2^{+1.9}_{-1.0}) \times 10^6 \), which would correspond to \( \dot{P} \approx -30 \) microseconds per year. This strongly disagrees with the the period change that we have observed.

Essick & Weinberg (2016) studied the problem of the orbital decay of hot Jupiters using a theory in which gravity modes are excited at the base of the stellar convective zone, propagate inward through the radiative core and break near the stellar core, leading to energy dissipation. They predicted the stellar quality factors in hot Jupiter systems to vary from \( Q'_e \approx 10^5 - 10^6 \). From their Equation 26, the prediction for WASP-4 is \( Q'_e \approx 7 \times 10^5 \), which is an order of magnitude larger than implied by the observed period change.

The applicability of the Essick & Weinberg (2016) model depends on the evolutionary state of the star. Weinberg et al. (2017) showed that more rapid dissipation — enough to account for the period change of WASP-12b — could exist in stars that have begun evolving into red giants. The bottom panel of Figure 5 shows a Hertzsprung-Russell diagram of hot Jupiters hosts, including WASP-4. On the y-axis is \( G = g - \mu \), for \( g \) the apparent Gaia-band magnitude, and \( \mu \) the distance modulus reported by Gaia Collaboration et al. (2018). The x-axis is the effective temperature from Bonomo et al. (2017), which for WASP-4 agrees within 1σ of that from Table 1. Inspecting the HR diagram, WASP-4 shows little evidence of being evolved, in agreement with our analysis from § 2.3.

To summarize, if the observed period change is caused entirely by tidal orbital decay, then the constant-phase-lag tidal model implies a stellar tidal dissipation rate that is higher than expected by at least an order of magnitude. It might be possible that we are observing at a special time, shortly after the planet’s inward migration, or when the planet is near resonance with a stellar oscillation mode. Tidal dissipation rates might also be increased if the star is just turning off the main sequence. Another hypothesis, recently advanced by Millholland & Laughlin (2018) for the case of WASP-12b, is that an exterior planet could be trapping WASP-4b’s spin vector in a high-obliquity state, leading to rapid dissipation through planetary obliquity tides.

4.2. Apsidal precession

If instead the observed timing variation is just a small portion of an apsidal precession cycle, then the orbital eccentricity is a few times \( 10^{-3} \), and the full precession period is about 27 years. Ragozzine & Wolf (2009) calculated apsidal precession periods for hot Jupiters, finding them to range between about 10 and 100 years. They highlighted that for many hot Jupiters, including WASP-4b, the theoretical precession rate is dominated by the non-Keplerian force due to the planet’s tidal bulge. Precession from general relativity, the planet’s rotational bulge, and the star’s rotational and tidal bulges contribute at the 10% level at most. Thus, a measurement of the precession rate can be used to determine the planet’s Love number. From their Equation 14, the implied Love number for WASP-4b is

\[
k_{2,p} = 1.59^{+0.70}_{-0.47} \quad \text{(wide prior),}
\]
\[
k_{2,p} = 1.20^{+0.20}_{-0.26} \quad \text{([k_{2,p} \sim \mathcal{U}(0.015, 1.5)],}
\]
(19)
Regardless of the detailed model assumptions, the main physical problem with the apsidal precession hypothesis is to explain why the eccentricity would be as large as $\sim 10^{-3}$ despite rapid tidal circularization. For WASP-4, Equation 14 gives $\tau_e = 0.29(q_4/10^3)$ Myr. The star is several billion years old, so unless the planet arrived very recently, any initial eccentricity should have been lowered well below $\sim 10^{-3}$. The top panel of Figure 5 compares the expected eccentricity damping time of WASP-4b with that of other transiting giant planets. WASP-4b has one of the shortest known eccentricity damping times.

**Neighboring companion**—One way to maintain a significant eccentricity is through the gravitational perturbations from another planet. Mardling (2007) considered the long-term tidal evolution of hot Jupiters with companions. The companion in their model is coplanar, and can have a mass down to an Earth-mass; the main requirement is that both the hot Jupiter and the outer companion start on eccentric orbits. They found that although the early phases of the two-planet eccentricity evolution occur quickly, the final phase of the joint eccentricity evolution towards circularity would occur on timescales several orders of magnitude longer than the circularization time of an isolated hot Jupiter (see their Figures 4 and 5).

A separate way a neighboring companion could excite the hot Jupiter’s eccentricity is through the Kozai-Lidov mechanism (Lidov 1962; Kozai 1962). In this case, the orbital plane of the outer companion, “c”, would need to be inclined relative to that of the hot Jupiter, “b”, by at least $\sin^{-1} \sqrt{2/5} \approx 39^\circ$. For the Kozai-Lidov mechanism to operate at maximum efficiency, we need (Bailey & Goodman 2019, Equation 20)

$$M_c > 7.5 M_\oplus \times \left( \frac{a_c}{a_b} \right)^{3/2},$$

where $a_b$ is the semi-major axis of WASP-4b, $M_c$ is the mass of the hypothetical WASP-4c, and $a_c$ is WASP-4c’s semi-major axis. Owing to our imprecise measurement, in Equation 20 we have assumed WASP-4b’s Love number is $k_{2,b} \approx 0.6$, similar to Jupiter. For the RV signal of the companion to remain undetected, it would need to be in the residual $(O-C)_{RV} = 15.2 \text{ms}^{-1}$ reported by Triaud et al. (2010). Again following Bailey & Goodman (2019), this implies

$$M_c < (O-C)_{RV} \left( \frac{M_c a_b}{M_\oplus G} \right)^{1/2} \left( \frac{a_c}{a_b} \right)^{1/2} f^{-1/2},$$

$$M_c < 23.7 M_\oplus \times \left( \frac{a_c}{a_b} \right)^{1/2} f^{-1/2}, \tag{21}$$

for $f(e_c, \omega_c, i_c) \propto \sin^2 i_c$ a geometric prefactor that depends on the argument of periastron $\omega_c$ and inclination $i_c$ of the exterior companion (Bailey & Goodman 2019 Equation 23). Since WASP-4b is transiting, $f$ can be arbitrarily small, and both of the preceding limits can be satisfied.

![Figure 6. Radial velocities of WASP-4 (top), and residuals from the best-fit Keplerian model (bottom). The lower panel shows the best-fit linear trend inferred from the RV data (black line, 1σ errors in gray), and the trend that would be needed to produce the period decrease seen in transits (purple dotted line). Since both the RV and transit timing datasets are sparse after 2013, a distant massive companion on an eccentric orbit might still explain the observations.](image)

**Fluctuations in the gravitational potential from convection**—An independent mechanism to pump the eccentricity invokes the gravitational fluctuations from stellar convection (Phinney 1992, Section 7). From equation 7.33 of that work, the mean-squared eccentricity of the orbit is

$$\langle e^2 \rangle = \frac{2 \langle E_e \rangle}{\mu \nu^2 a^2} = 6.8 \times 10^{-5} \left( \frac{L_{\text{conv}}^2 M_{\text{conv}}^2}{\mu \nu^2 a^2} \right)^{1/3}, \tag{22}$$

where $L$ is the stellar luminosity, $R_{\text{conv}}$ and $M_{\text{conv}}$ are the width and mass of the convective region, $\mu$ is the reduced mass, $n$ is the orbital frequency, and $a$ is the semi-major axis. For the luminosity, reduced mass, and semi-major axis, we used values from Table 1, combined with the Stefan-Boltzmann law and standard definitions. To estimate the width and mass of the convective region we ran the MESA code for a star with mass and metallicity matched to WASP-4, and the input physics detailed in the MIST isochrones project (Paxton et al. 2011, 2013, 2015; Dotter 2016; Choi et al. 2016). We identified the tachocline boundary using the mixing types specified in the resulting radial profiles, and found $R_{\text{conv}} \approx 0.33 R_\odot$ and $M_{\text{conv}} \approx 9 \times 10^{-4} M_\odot$. For WASP-4, this implies $\langle e^2 \rangle^{1/2} \leq 10^{-3}$. Hence, this mechanism does not seem capable of producing the required eccentricity of $\sim 10^{-3}$.

### 4.3. Timing variation due to line of sight acceleration

An acceleration of the center of mass of the system towards our line of sight could cause a decrease in the apparent orbital
period. The period derivative would be

$$\dot{P} = \frac{\dot{v}_r P}{c},$$

(23)

where $\dot{v}_r$ is the time derivative of the radial velocity.

Knutson et al. (2014), combining radial-velocity data from their own program with those of Wilson et al. (2008), Pont et al. (2011), and Husnoo et al. (2012), found evidence for long-term trend in WASP-4, with low statistical significance:

$$\dot{v}_r = -0.0099^{+0.0052}_{-0.0054} \text{ m/s day}^{-1}.$$  

(24)

This acceleration translates to an expected $\dot{P} = -(4.4 \pm 2.4) \times 10^{-11}$. The period decrease from the observed RV trend is an order of magnitude smaller than the observed $\dot{P}$ from transit times, $(4.0 \pm 0.4) \times 10^{-10}$ (Table 4).

Nonetheless, it is intriguing that the host star shows a weakly significant acceleration, and with the correct sign needed to explain the transit timing variations. Given the potential importance of the radial velocities for interpreting this system, we performed an independent analysis, as follows.

First, we collected the usable RV measurements from CORALIE, HARPS, and HIRES. We included the CORALIE measurements from Wilson et al. (2008) and Triaud et al. (2010), using the homogeneous radial velocities calculated by the latter authors. We included the HARPS values reported by Pont et al. (2011), which are identical to those from Husnoo et al. (2012). We omitted the HARPS data points taken over three nights by Triaud et al. (2010) for Rossiter-McLaughlin observations because they were calculated using a different pipeline than the longer-baseline Pont et al. HARPS measurements, and necessary inclusion of an extra offset term would nullify their statistical value. Finally, we included the five HIRES measurements taken over many years by Knutson et al. (2014).

We then fitted a single Keplerian orbit, plus instrument offsets, jitters, and a long-term trend (Fulton et al. 2018, radvel). We set Gaussian priors on the period and time of inferior conjunction using the values from Table 4, and fixed the eccentricity to zero, consistent with results from Beemer et al. (2011), Knutson et al. (2014) and Bonomo et al. (2017). The remaining free parameters were the velocity semi-amplitude, the instrument zero-points, the instrument jitters (an additive white noise term for each instrument), linear ($\dot{v}_i$), and optionally second-order ($\ddot{v}_i$) acceleration terms.

We found that the best-fitting model with both linear and quadratic radial velocity terms was marginally preferred (by $\Delta \text{BIC} = 5.8$) over the best-fitting model with only a linear term. Regardless, for consistency with Knutson et al. (2014), who fixed the quadratic component of the long-term trend to zero, in Figure 6 we show best-fitting models for the linear-trend case. The best-fit value for the line of sight acceleration,

$$\dot{v}_r = -0.0077^{+0.0052}_{-0.0047} \text{ m/s day}^{-1},$$

(25)

is within 1σ of the value reported by Knutson et al. (2014). (Note that the CORALIE data used in our and their analyses differ, as we included additional measurements reported by Triaud et al. 2010). The implied period derivative is still therefore about an order of magnitude smaller than our observed $\dot{P}$ from transit timing.

To summarize, only about one tenth of the observed period decrease can be explained through a constant acceleration of the WASP-4 system’s center of mass. However, given the limited amount and uneven time coverage of the existing radial-velocity data (Figure 6), it remains possible that the center of mass has a more complex motion, perhaps due to a companion on an eccentric orbit (e.g., WASP-53 or WASP-81, Triaud et al. 2017). It would be useful to gather more radial-velocity data to confirm or refute this possibility.

### 4.4. Applegate effect

A separate candidate explanation for the timing deviations is the Applegate (1992) effect. Some eclipsing binaries exhibit period modulations with amplitudes of $\lesssim 0.05$ days over timescales of decades (e.g., Söderhjelm 1980; Hall 1989). The Applegate mechanism explains these modulations by positing that the internal structure of a magnetically active star changes shape via cyclic exchange of angular momentum between the inner and outer zones of the star. This model could also apply to a hot Jupiter orbiting a star with a convective zone. The changing gravitational quadrupole of the star would cause the orbit of the planet to precess on the timescale of the stellar activity cycle. An essential difference between this process and apsidal precession is that Applegate timing variations need not be strictly periodic (e.g., Söderhjelm 1980, Figure 12). This mechanism would also produce transit and occultation timing deviations of the same sign, while for apsidal precession they would have opposite signs. For WASP-4, Watson & Marsh (2010) estimated that the Applegate effect could produce timing deviations of up to 15 seconds, depending on the modulation period of the stellar dynamo. If this analysis is accurate, then the Applegate mechanism cannot explain the majority of our observed 82 second variation.

### 4.5. Other possible explanations

There are two other small effects worth noting. The first is the Shkolovskii (1970) effect due to the star’s proper motion, which leads to an apparent period change of $P\mu^2 d/c$, which is only $6 \times 10^{-13}$ for the case of WASP-4. The second effect, described by Rafikov (2009), comes from the star’s on-sky motion altering our viewing angle, and leads to an observed apsidal precession. The corresponding period change is $\dot{P} \sim (P\mu)^3/2\pi$, which is on the order of $10^{-21}$ for WASP-4, too small to be of any consequence.

### 5. CALL FOR ADDITIONAL OBSERVATIONS

A primary purpose of this work has been to call attention to the timing anomaly of WASP-4 that has been sighted by TESS, and alert observers to the need for follow-up transit timing, occultation timing, and radial-velocity monitoring. There is no unique interpretation of the current data, and two of the possibilities — orbital decay and apsidal precession
— would be of great interest to confirm. Detection of orbital decay would lead to an unusually direct determination of a stellar dissipation rate. Detection of apsidal precession would give a rare constraint on the interior density distribution of an exoplanet. The third possibility — a massive outer companion — would be the least exotic option, but nonetheless a valuable discovery.

If TESS is extended beyond its primary mission, it will likely observe additional transits of WASP-4b in the early 2020s. High-precision transit observations with larger telescopes would also be useful. In order to decide between orbital decay and apsidal precession, occultation measurements in both the near term and also in the mid-2020s will be needed (Figure 7). More radial-velocity data would help in the search for additional bodies that could be causing dynamical perturbations, or an overall acceleration of the host star. The transit duration variations are expected to be of order 10 seconds (Pál & Kocsis 2008), and so may remain out of reach.

TESS will also be monitoring the other known hot Jupiters, which will reveal whether the timing anomalies seen in WASP-12 and now WASP-4 are commonplace, and may shed some light on the circumstances in which they arise. Other wide-field photometric surveys, such as the Next Generation Transit Survey (Wheatley et al. 2018), HATPI (hatpi.org) and PLATO (Rauer et al. 2014) will also extend the time baseline of transit timing for a large number of systems.

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**Facility:** TESS (Ricker et al. 2015), Gaia (Gaia Collaboration et al. 2016, 2018), Tycho-2 (Høg et al. 2000), 2MASS (Skrutskie et al. 2006), APASS (Henden et al. 2012), WISE (Wright et al. 2010).

**Software:** astrobase (Bhatti et al. 2018), astropy (Collaboration et al. 2018), astroquery (Ginsburg et al. 2018), BATMAN (Kreidberg 2015), corner (Foreman-Mackey et al. 2013), emcee (Foreman-Mackey et al. 2013), IPython (Pérez & Granger 2007), matplotlib (Hunter 2007), MESA ( Paxton et al. 2011, 2013, 2015) numpy (McKinney 2010), pandas (McKinney 2010), radvel (Fulton et al. 2018), scikit-learn (Pedregosa et al. 2011), scipy (Jones et al. 2001).

Table 2 continued

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<td>1</td>
<td>Nikolov et al. (2012)</td>
</tr>
<tr>
<td>2455069.82676</td>
<td>0.00031</td>
<td>-549</td>
<td>1</td>
<td>Nikolov et al. (2012)</td>
</tr>
<tr>
<td>2455073.84108</td>
<td>0.00029</td>
<td>-546</td>
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<td>Nikolov et al. (2012)</td>
</tr>
<tr>
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<td>Nikolov et al. (2012)</td>
</tr>
<tr>
<td>2455073.84111</td>
<td>0.00023</td>
<td>-546</td>
<td>1</td>
<td>Nikolov et al. (2012)</td>
</tr>
</tbody>
</table>

Note—\( \Delta t_{\text{adj}} \) is the measured transit midtime, and \( \sigma_{\Delta t} \) is its 1σ uncertainty. \( \sigma_{\Delta t} \) was evaluated from the sampled posteriors by taking the maximum of the difference between the 84th percentile minus the median, and the median minus the 16th percentile. The resulting error variances then appeared to have been overestimated, so we lowered the uncertainties as described in § 2.2. The “Reference” column refers to the work describing the original observations. The “H137” column is 1 if the mid-time value was taken from Hoyer et al. (2013). Otherwise, the mid-time came from the column listed in “Reference”. The Hoyer et al. 2013 BJD\(_{\text{TDB}} \) times are equal to BJD\(_{\text{TDB}} \) for our purposes (Urban & Seidelmann 2012). We omitted the timing measurements from Southworth et al. (2009), since there were technical problems with the computer clock at the time of observation (Nikolov et al. 2012). The two Baxter et al. (in prep) times were obtained from Spitzer/IRAC transit light curves in the 3.6\( \mu \)m and 4.5\( \mu \)m channels.
Early Arrival of WASP-4b

Table 3. WASP-4b occultation times, uncertainties, and references.

<table>
<thead>
<tr>
<th>$t_{\text{occ}}$ [BJD$_{\text{TDB}}$]</th>
<th>$\sigma_{t_{\text{occ}}}$ [days]</th>
<th>Epoch</th>
<th>Reference</th>
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</thead>
<tbody>
<tr>
<td>2455102.61210</td>
<td>0.00074</td>
<td>-511</td>
<td>Cáceres et al. (2011)$^a$</td>
</tr>
<tr>
<td>2455172.20159</td>
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<td>-459</td>
<td>Beerer et al. (2011)</td>
</tr>
<tr>
<td>2455174.87780</td>
<td>0.00087</td>
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<td>Beerer et al. (2011)</td>
</tr>
<tr>
<td>2456907.88714</td>
<td>0.00290</td>
<td>838</td>
<td>Zhou et al. (2015)$^b$</td>
</tr>
</tbody>
</table>

NOTE—$t_{\text{occ}}$ is the measured occultation midtime, minus the $2a/e = 22.8$ second light travel time; $\sigma_{t_{\text{occ}}}$ is the 1σ uncertainty on the occultation time.

$^a$ Cáceres et al. (2011) reported this time in “HJD”, with an unspecified time standard. We assumed the time was originally in HJD$_{\text{UTC}}$, and converted to BJD$_{\text{TDB}}$ for the tabulated time.

$^b$ Zhou et al. (2015) fixed the epoch, and let $e \cos \omega$ float. Using the reported dates of observation, we converted their $e \cos \omega$ values into an occultation time using Equation 1 of the text.

Table 4. Best-fit transit timing model parameters.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Median Value (Unc.)$^a$</th>
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</thead>
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<tr>
<td>Constant period</td>
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</tr>
<tr>
<td>$t_0$ [BJD$_{\text{TDB}}$]</td>
<td>2455804.515752(+19)(-19)</td>
</tr>
<tr>
<td>$P$ [days]</td>
<td>1.338231466(+23)(-22)</td>
</tr>
<tr>
<td>Constant period derivative</td>
<td></td>
</tr>
<tr>
<td>$t_0$ [BJD$_{\text{TDB}}$]</td>
<td>2455804.515918(+24)(-24)</td>
</tr>
<tr>
<td>$P$ [days]</td>
<td>1.338231679(+31)(-31)</td>
</tr>
<tr>
<td>$dP/dt$</td>
<td>$-4.00(+37)(-38) \times 10^{-10}$</td>
</tr>
<tr>
<td>Apsidal precession (wide prior)</td>
<td></td>
</tr>
<tr>
<td>$t_0$ [BJD$_{\text{TDB}}$]</td>
<td>2455804.51530(+25)(-31)</td>
</tr>
<tr>
<td>$P_s$ [days]</td>
<td>1.33823127(+10)(-48)</td>
</tr>
<tr>
<td>$e$</td>
<td>$1.92^{+1.93}_{-0.96} \times 10^{-3}$</td>
</tr>
<tr>
<td>$\omega_0$ [rad]</td>
<td>$2.40(+38)(-34)$</td>
</tr>
<tr>
<td>$d\omega/dE$ [rad epoch$^{-1}$]</td>
<td>$8.70^{+0.131}_{-0.195} \times 10^{-4}$</td>
</tr>
</tbody>
</table>

$^a$ The numbers in parenthesis give the 68% confidence interval for the final two digits, where appropriate.
REFERENCES

Bhatti, W., Bouma, L. G., & Wallace, J. 2018, astrobase
Ginsburg, A., Sipocz, B., Madhura Parikh, et al. 2018, Astropy/Astroquery: V0.3.7 Release
Goodman, J., & Weare, J. 2010, Communications in Applied Mathematics and Computational Science, 5, 65
Hall, D. S. 1989, Space Science Reviews, 50, 219
Hunter, J. D. 2007, Computing in Science & Engineering, 9, 90
Hut, P. 1980, Astronomy and Astrophysics, 92, 167
Jones, E., Oliphant, T., Peterson, P., et al. 2001, Open source scientific tools for Python
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Lidov, M. L. 1962, Planetary and Space Science, 9, 719
Ni, D. 2018, Astronomy & Astrophysics, 613, A32
Pérez, F., & Granger, B. E. 2007, Computing in Science and Engineering, 9, 21
Phinney, E. S. 1992, Philosophical Transactions of the Royal Society of London Series A, 341, 39
Schwarzschild, M. 1958, Structure and evolution of the stars (Princeton Univesity Press), Ch. 18
Shkolniiiskii, I. S. 1970, Soviet Astronomy, 13, 562
Söderhjelm, S. 1980, *Astronomy and Astrophysics*, 89, 100
APPENDIX

A. VERIFYING THE TESS TIMESTAMPS USING OTHER HOT JUPITERS

An obvious concern that one might have about the WASP-4b timing anomaly is that there might be a systematic offset between the TESS time system and the time system in which the previous observations have been reported. There is a precedent for this type of error: data from the Kepler mission was afflicted by a systematic timing error that was corrected only late in the mission (Thompson et al. 2013, Section 3.4).

If the observed timing delay in WASP-4b were caused by a systematic global offset between the TESS time system and the BJD<sub>TDB</sub> reference, we would expect that it would be apparent in other hot Jupiter systems, too. It would also be apparent in eclipsing binary observations and any other periodic phenomena that have been observed over a long time baseline. Here we examine only hot Jupiters because of our greater familiarity with the data.

We repeated all the data reduction and analysis steps described in this paper for other hot Jupiters observed by TESS for which timing data exists spanning many years. First, we checked which hot Jupiters were observed over the first three TESS sectors using a combination of tessmaps<sup>5</sup> and TEPCat (Southworth 2011). We recalculated the barycentric corrections using the Eastman et al. (2010) code, and found values that agreed with the lightcurve headers to within about 1 second. We then selected hot Jupiters for which there were at least five distinct epochs reported in the peer-reviewed literature. We required that each observation be of a single transit, that the midpoint be fit as a free parameter, and that the time system be clearly documented.

<sup>5</sup> github.com/lgbouma/tessmaps, commit 569bbc2
Our final hot Jupiter sample included WASP-4b, 5b, 6b, 18b, and 46b. The collected and measured times are given in Tables 5, 6, 7, and 8 for each.

We determined the best-fitting constant-period ephemeris based on the pre-TESS data. Then we used the parameters and uncertainties in the best-fitting model to calculate the predicted transit times during the TESS observation period, as well as the uncertainty in the predicted times. The uncertainties are 11, 94, 18, 42, and 59 seconds for WASP-4b, 5b, 6b, 18b, and 46b, respectively. By comparing the observed and predicted times, Figure 8 shows that WASP-4b is the only hot Jupiter that transited significantly earlier than expected.

To use these results to place a quantitative limit on any global clock offset, for each hot Jupiter we considered the model

$$t_{\text{tra}}(E) = t_0 + PE + t_{\text{offset}},$$  \hspace{1cm} (A1)

for $t_{\text{offset}}$ a systematic constant offset between the reported timestamps and the true BJD\textsubscript{TDB} reference. Our priors were

$$t_0 \sim \mathcal{N}[t'_0, \sigma_{t'_0}],$$  \hspace{1cm} (A2)

$$P \sim \mathcal{N}[P', \sigma_{P'}],$$  \hspace{1cm} (A3)

$$t_{\text{offset}} \sim \mathcal{U}[-20\sigma_{t'_0}, 20\sigma_{t'_0}],$$  \hspace{1cm} (A4)

where $\mathcal{N}$ and $\mathcal{U}$ denote a normal and uniform distribution, $(t'_0, P')$ are the best-fit reference time and period using only the pre-TESS transit times, and $(\sigma_{t'_0}, \sigma_{P'})$ are the corresponding uncertainties.

For each planet, we asked: what fraction of the posterior for $t_{\text{offset}}$ is consistent with an offset worse than 81.6 seconds? For WASP-4b, the answer is unsurprisingly 50%. For WASP-6b, the most constraining object, about 1 sample in 2 million is consistent with such a timing offset (4.9$\sigma$). For WASP-18b, 1 in 103 samples would be consistent with this timing offset (2.3$\sigma$), and in WASP-46b, the limit is 1 in 49 samples (2.0$\sigma$). For WASP-5b, the predicted time is too imprecise to rule out timing offsets at the necessary amplitude. Multiplying the three independent probabilities for WASP-6b, 18b, and 46b, we can rule out $t_{\text{offset}} < -81.6$ seconds at 6.4$\sigma$, or about 1 part in 11 billion.

### Table 5. WASP-5b transit times, uncertainties, and references.

<table>
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<th>$t_{\text{tra}}$ [BJD\textsubscript{TDB}]</th>
<th>$\sigma_{t_{\text{tra}}}$ [days]</th>
<th>Epoch</th>
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</tr>
</thead>
<tbody>
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</tr>
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<td>2454387.02275</td>
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<td>2455079.10830</td>
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Table 5 (continued)

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<th>(t_{\text{tr}}) [BJD(_{\text{TDB}})]</th>
<th>(\sigma_{t_{\text{tr}}}) [days]</th>
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<th>Reference</th>
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NOTE—\(t_{\text{tr}}\) is the measured transit midtime, and \(\sigma_{t_{\text{tr}}}\) is its 1\(\sigma\) uncertainty. The “Reference” column refers to the work describing the original observations. All the literature times except for the two Moyano et al. (2017) times are from the homogeneous Hoyer et al. (2012) analysis.

Table 6. WASP-6b transit times, uncertainties, and references.

<table>
<thead>
<tr>
<th>(t_{\text{tr}}) [BJD(_{\text{TDB}})]</th>
<th>(\sigma_{t_{\text{tr}}}) [days]</th>
<th>Epoch</th>
<th>Reference</th>
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NOTE—\(t_{\text{tr}}\) is the measured transit midtime, and \(\sigma_{t_{\text{tr}}}\) is its 1\(\sigma\) uncertainty. The “Reference” column refers to the work describing the original observations.

Table 7. WASP-18b transit times, uncertainties, and references.

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<th>(t_{\text{tr}}) [BJD(_{\text{TDB}})]</th>
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Table 7 continued
### Table 7 (continued)

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**NOTE:** $t_{\text{tr}}$ is the measured transit midtime, and $\sigma_{t_{\text{tr}}}$ is its 1σ uncertainty. The “Reference” column refers to the work describing the original observations. All the literature times are from the homogeneous Wilkins et al. (2017) analysis.

### Table 8 (continued)

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**NOTE:** $t_{\text{tr}}$ is the measured transit midtime, and $\sigma_{t_{\text{tr}}}$ is its 1σ uncertainty. The “Reference” column refers to the work describing the original observations. All the literature times are from the homogeneous Petrucci et al. (2018) analysis. 14 of the lightcurves were acquired by ETD observers (see Petrucci et al. 2018).