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DOI
10.1103/PhysRevC.95.024605

Publication date
2017

Document Version
Final published version

Published in
Physical Review C

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Citation for published version (APA):
https://doi.org/10.1103/PhysRevC.95.024605

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Search for two-neutrino double electron capture of $^{124}$Xe with XENON100

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I. INTRODUCTION

Double electron capture is a rare nuclear decay where a nucleus captures two electrons from the atomic shell

$$A, Z + 2e^- \rightarrow (A, Z - 2) + (2\nu_e).$$

The two-neutrino mode (2$\nu$EC) is allowed in the standard model, while the existence of the lepton number-violating

$\nu$EC
neutrinoless double electron capture (0ν2EC) would prove the Majorana nature of the neutrino. In 0ν2EC, there is the possibility of a resonant enhancement of the decay rate for decays to excited atomic or nuclear states [1–4]. Due to low isotopic abundances and longer half-lives [5,6], experimental searches for 0ν2EC are generally not competitive with those for neutrinoless double-β decay (0ν2β) to constrain the effective neutrino mass $m_{\nu\nu}$ and the neutrino mass hierarchy [7]. The largest uncertainty in the conversion of the half-life of 0ν2β or 0ν2EC to $m_{\nu\nu}$ is introduced by the calculation of nuclear matrix elements. Although the matrix elements for the two-neutrino and neutrinoless modes of the double electron capture differ, they are based on the same nuclear structure models. A measurement of the 2ν2EC half-life would help to test the accuracy of these models.

So far, 2ν2EC has only been observed for $^{130}$Ba in geochemical experiments [8,9]. In addition, there is an indication for 2ν2EC of $^{78}$Kr from a low-background proportional counter [10]. In natural xenon the isotopes $^{124}$Xe ($Q = 2864$ keV [11], abundance 0.095% [12]) and $^{126}$Xe ($Q = 919$ keV [11], abundance 0.089% [12]) can decay via 2ν2EC. However, any signal will be dominated by $^{124}$Xe due to the $Q$ dependence of the phase space [13]. In the case of $^{124}$Xe, the theoretically calculated branching ratio that the two electrons are captured from the K shell (2ν2K) is 76.7% [14]. Filling the vacancies of the daughter atom $^{124}$Te leads to the emission of x rays and Auger electrons with a total energy of approximately 64 keV. There is a wide spread in the predicted half-lives of 2ν2EC for $^{124}$Xe, from $\sim 10^{29}$ yr to $10^{24}$ yr due to different nuclear matrix element calculations [15–20]. Previous searches for 2ν2K of $^{124}$Xe have been carried out using a low-background proportional counter with enriched xenon [14,21] and large-scale liquid xenon detectors [22,23]. The current best experimental limit on the half-life, $T_{1/2} > 4.7 \times 10^{24}$ yr (90% confidence level) is set by the XMASS experiment [23].

A limit of $T_{1/2} > 1.66 \times 10^{21}$ yr (90% confidence level) was derived from previously published XENON100 data [22]. However, the available data were not well suited for a signal search due to the coarse binning. The limit was calculated from the average background rate for the energy region below $\sim 10$ keV [24], outside the expected 2ν2K signal region, and the assumed isotopic abundance of $^{124}$Xe did not match the real situation. Here, we improve on this study by using the 224.6 live days of XENON100 data and additional insight into the experimental details.

## II. THE XENON100 EXPERIMENT

Located at the Laboratori Nazionali del Gran Sasso (LNGS), the XENON100 experiment [25] utilizes a dual-phase xenon time-projection chamber (TPC) in order to search for dark matter particles in form of weakly interacting massive particles (WIMPs). The TPC contains 62 kg of liquid xenon (LXe) in a cylindrical (30.5 cm in height and diameter) volume equipped with 178 radio pure photomultiplier tubes (PMTs) placed in the gaseous phase on top and immersed in the LXe at the bottom. The TPC is fully surrounded by an active LXe veto viewed by 64 additional PMTs. If a particle deposits its energy in the LXe, it creates excited atoms and ions leading to the formation of excimers. The de-excitation of these excimers causes prompt scintillation light (S1). A fraction of the electrons generated by the ionization process are drifted towards the gas phase by an applied electric field of 530 V/cm. At the liquid-gas interface they are extracted and accelerated by a strong field of 12 kV/cm. This induces a secondary scintillation signal (S2) which is proportional to the number of generated electrons. Three-dimensional event vertex reconstruction is achieved by obtaining the interaction depth from the time difference of the two signals and by deriving the $(x,y)$ position from the hit pattern of the S2 signal on the top PMT array. A background-optimized fiducial volume can thus be selected, with a strongly reduced background from external γ radiation. A detailed description of the detector can be found in Ref. [25].

## III. DATA ANALYSIS

Data for the 2ν2K search consist of 224.6 live days collected between February 28, 2011, and March 31, 2012, using a fiducial target mass of 34 kg. This data set has also been analyzed for different purposes in Refs. [24,26–29]. The detector was filled with a mixture of natural xenon and xenon depleted in $^{136}$Xe and $^{124}$Xe, leading to a $^{124}$Xe abundance of $\eta = (8.40 \pm 0.07) \times 10^{-4}$. This corresponds to an absolute amount of about 29 g of $^{124}$Xe in the fiducial volume.

The energy calibration uses the S1 and S2 signals from an Americium-Beryllium ($^{241}$AmBe) calibration measurement. We employ γ lines from neutron-activated xenon isotopes at 40 and 320 keV ($^{128}$Xe), 80 keV ($^{131}$Xe), 164 keV ($^{131m}$Xe), and 236 keV ($^{129m}$Xe). The energy $E$ was obtained by a linear combination of the S1 and S2 signals measured in photoelectrons (PE), exploiting their anticorrelation [30,31]

\[ E = W \left( \frac{S_1}{g_1} + \frac{S_2}{g_2} \right), \]

(2)

$W$ is the mean energy required to produce a photon or electron and $g_1$ and $g_2$ are detector-specific gain factors. When fixing $W$ to 13.7 eV [31], the best-fit values of the gain factors are $g_1 = (5.07 \pm 0.03) \times 10^{-2}$ PE/photon and $g_2 = (10.13 \pm 0.07)$ PE/electron. Although the S1 and S2 signals depend on particle type and vary nonlinearly with energy, the combined signal provides a common, linear energy scale for both x rays and Auger electrons at the relevant energies. The energy resolution $\sigma$ was derived from the same γ lines and is given by

\[ \sigma(E) = a \sqrt{E} + b E, \]

(3)

with $a = (0.405 \pm 0.010) \sqrt{\text{keV}}$ and $b = 0.0261 \pm 0.0008$.

Selection cuts were applied in order to ensure data quality and consistency. Every valid event was required to have exactly one S1 and one corresponding S2. In order to avoid dark count contributions, the S1 had to be detected by at least two PMTs. Further cuts address the removal of noisy events using the information on the signal width (S1 and S2) and on the signal distribution between the top and bottom PMT arrays.

Events which have a coincident signal in the veto were not considered as this indicates multiple scattering induced by external radiation. The acceptance of each selection cut was
with an average rate of \(5\) kHz. Apart from this peak, the background is nearly constant.

For bound-bound x rays and electrons for a single signal, we calculated the energies and emission probabilities. The total acceptance of events that passed all selection cuts but the one of interest. Therefore, the expected signal is the sum energy. The RELAX code assumes that the final atom returns to neutrality by filling all remaining vacancies with electrons from the continuum which leads to the shell binding energies independent of the ionization of the atom. Therefore, the total emitted energy equals the binding energy of the \(K\) shell of the neutral atom \(E_K = 31.8\) keV [35]. In 2ν2K the total emitted energy is given by the double-electron hole energy (64.457 ± 0.012) keV [36] which is very close to two times the \(K\)-shell binding energy. However, the energies of a small fraction of the emitted quanta are below the xenon excitation threshold of 13.7 eV. According to RELAX, and under the assumption that the quanta emitted in 2ν2K are similar to those generated by two single \(K\)-shell vacancies, this leads to an average energy loss of 0.13 keV. Therefore, the 2ν2K peak is expected to be centered at 64.33 keV. To estimate the energy resolution of the signal peak, we take the average energy and number of x rays and electrons emitted per vacancy as shown in Table I but neglect the contribution from free-bound x rays. Again, assuming the same de-excitation spectrum as for two single \(K\) captures, we arrive at an energy resolution \(\sigma_{\text{sig}}\) of

\[
\sigma_{\text{sig}} = \sqrt{2(n_1\sigma_1^2 + n_2\sigma_2^2)},
\]

where \(n_1 = 0.96\) and \(n_2 = 11.7\) are the average number of x rays and Auger electrons and \(\sigma_1 = \sigma(25.9\) keV) and \(\sigma_2 = (0.57\) keV) correspond to their respective energy resolution from Eq. (3). This leads to \(\sigma_{\text{sig}} = (4.10 \pm 0.27)\) keV compared to \(\sigma(64.33\) keV) = (4.93 \pm 0.27) keV for a single energy deposition.

The statistical analysis for the signal search uses the BAYESIAN ANALYSIS TOOLKIT [37]. The spectrum with a 1-keV binning was fit in the energy range 10–135 keV with a signal + background model \(f_{\text{sig}}(E)\) and a background-only model \(f_{\text{bkg}}(E)\)

\[
f_{\text{sig}}(E) = \frac{\Gamma \eta t N_A}{\sqrt{2\pi \sigma_{\text{sig}} M_{\text{Xe}}}} \exp\left(\frac{-(E - \mu_{\text{sig}})^2}{2\sigma_{\text{sig}}^2}\right) + f_{\text{bkg}}(E),
\]

\[
f_{\text{bkg}}(E) = a_{\text{bkg}} E + c_{\text{bkg}}.
\]

\(E\) is the energy, \(\Gamma\) is the decay rate, \(\epsilon\) is the signal acceptance, \(\eta\) is the abundance of \(^{124}\)Xe, \(m_t\) is the exposure, \(N_A\) is Avogadro’s constant, \(M_{\text{Xe}}\) is the molar mass of xenon, \(\mu_{\text{sig}}\) is the mean energy, and \(\sigma_{\text{sig}}\) is the width of the signal peak. The parameters \(a_{\text{bkg}}\) and \(c_{\text{bkg}}\) represent the slope and constant term of the background spectrum, respectively. The binned likelihood of the fit assumes independent Poisson fluctuations of the bin entries and is defined as

\[
L = \prod_{i=1}^{N_{\text{bin}}} \frac{\lambda_i^n_i e^{-\lambda_i}}{n_i!},
\]

where \(N_{\text{bin}}\) is the total number of bins. \(\lambda_i\) is the expected number of events, and \(n_i\) is the observed number of events in the \(i\)th bin. Systematic uncertainties were included in the fit by Gaussian priors and are summarized in Table II. The uncertainty on the cut acceptance \(\epsilon\) is only statistical. For the natural abundance \(\eta\), the uncertainty was calculated from the individual uncertainties on the amounts and abundances of the deployed xenon batches. The uncertainty on the exposure \(m_t\) accounts for the uncertainty in the determination of the fiducial volume due to the limited spatial resolution. Regarding the peak position \(\mu_{\text{sig}}\) and width \(\sigma_{\text{sig}}\), we

![FIG. 1. Spectrum of remaining events after all cuts. The peak at 164 keV originates from \(^{131}\)Xe. The red shaded area indicates the ±3σ region around the expected 2ν2K peak of \(^{125}\)Xe.](image)

**TABLE I.** Average energies and average number of emitted quanta per \(K\)-shell vacancy in Tc, as calculated with the RELAX code [34].

<table>
<thead>
<tr>
<th>Energy per quantum (eV)</th>
<th>Number of quanta</th>
</tr>
</thead>
<tbody>
<tr>
<td>Bound-bound x rays</td>
<td>25950</td>
</tr>
<tr>
<td>Bound-bound electrons</td>
<td>572</td>
</tr>
<tr>
<td>Free-bound x rays</td>
<td>14</td>
</tr>
</tbody>
</table>
included the uncertainties derived from the fits to the energy calibration and resolution. In addition, we added systematic uncertainties of 0.2% and 3% for the peak position and energy resolution, respectively, which were determined from the RELAX calculation. Uniform priors were chosen for the remaining free parameters of the fit, \( \Gamma, a_{\text{bkg}}, \) and \( c_{\text{bkg}}. \) All fit parameters were constrained to physically allowed positive values. The significance of a possible signal was evaluated by calculating the Bayes factor \([38]\),

\[
B = \frac{P(f_{\text{bkg}} \mid D)}{P(f_{\text{sig}} \mid D)}, \tag{8}
\]

where \( P(f \mid D) \) is the posterior probability of the model \( f \) and \( D \) is the data.

IV. RESULTS

The best fits to the spectrum with \( f_{\text{sig}} \) and \( f_{\text{bkg}} \) are shown in Fig. 2 and the obtained values can be found in Table III. The \( p \) values of the signal + background and background-only fits, calculated as described in Ref. [39], are 0.92 and 0.89, respectively. These values show that the data are well described by both fit models. Since the Bayes factor is

\[
B = 1.2, \tag{9}
\]

and thus favors the background-only model, we calculate a lower limit on the half-life. The 90% credibility limit \( \Gamma_{\text{lim}} \) on the decay rate is defined as the 90% quantile of the marginalized posterior probability distribution shown in Fig. 3. This leads to a 90% credibility limit on the half-life \( T_{1/2} \) of

\[
T_{1/2} > \frac{\ln(2)}{\Gamma_{\text{lim}}} = 6.5 \times 10^{20} \text{ yr}. \tag{10}
\]

The influence of the nuisance parameters on the limit was evaluated by fixing all parameters shown in Table II to their mean values, which weakens the limit by 0.5%. While the binning has only a moderate influence (~15%), decreasing the fit range can worsen the half-life limit by up to a factor of \(~2\). The latter comes from the anticorrelation of the parameters \( \Gamma \) and \( c_{\text{bkg}} \) in Eq. (5). We have checked our result with the Feldman-Cousins procedure [40] using the approach of a simple counting experiment with known background. The number of observed events was derived from the \( \pm 3\sigma \) region of the expected 2ν2K peak, while the number of background events was calculated from the regions left and right of the peak. This gives a lower half-life limit of \( 7.3 \times 10^{20} \) yr

![FIG. 2. Best fit to the data with the signal + background model \( f_{\text{sig}} \) (blue solid line) and the background-only model \( f_{\text{bkg}} \) (red dashed line). The shaded areas indicate the 68% uncertainty bands.](image)

![FIG. 3. Marginalized posterior probability distribution for the decay rate \( \Gamma \). The vertical line indicates the 90% quantile from which the lower half-life limit was derived.](image)
TABLE IV. Current experimental limits (at 90% confidence level) on the half-life of two-neutrino double $\nu K$ capture ($2\nu$2K) of $^{124}$Xe. Our work supersedes the limit by Mei et al. [22], which was based on publicly available XENON100 data.

<table>
<thead>
<tr>
<th>Reference</th>
<th>$T_{1/2}$ ($10^{21}$ yr)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Abe et al. (XMASS) [23]</td>
<td>&gt;4.7</td>
</tr>
<tr>
<td>Gavriluk et al. [14]</td>
<td>&gt;2.0</td>
</tr>
<tr>
<td>Mei et al. [22]</td>
<td>&gt;1.66</td>
</tr>
<tr>
<td>This work</td>
<td>&gt;0.65</td>
</tr>
</tbody>
</table>

(90% confidence level), which confirms the result of the full Bayesian analysis.

A comparison of the current experimental half-life limits is shown in Table IV. Since our analysis is more accurate it supersedes the previous limit given in Ref. [22] which made use of the publicly available XENON100 data. The larger mass of the XMASS experiment (835 kg) results in better self-shielding capabilities and consequently a lower background, and thus makes the experiment more sensitive to $2\nu$2K.

The successor of XENON100, the XENON1T experiment [41], is based on the same detector technology but with an increased total target mass of 2 t and a reduced background. It is currently in the commissioning phase. The sensitivity of XENON1T for $2\nu$2K of $^{124}$Xe was investigated using the expected background spectrum in a 1-t fiducial volume [41]. We assumed the same energy resolution as in XENON100. This assumption is conservative as the energy resolution is related to the light yield, which is expected to be about a factor of two higher in XENON1T [41]. We used the Bayesian approach for a simple counting experiment with known background to estimate the sensitivity on the half-life in XENON1T. The likelihood is defined as

$$L = \left( N_{\text{sig}} + N_{\text{bkg}} \right)^{N_{\text{obs}}} e^{-(N_{\text{bkg}}+N_{\text{sig}})} \frac{N_{\text{obs}}!}{N_{\text{bkg}}! N_{\text{sig}}!},$$

where $N_{\text{obs}} = N_{\text{bkg}}$ is the expected number of counts in the ±3σ region around the $2\nu$2K peak, and $N_{\text{sig}}$ is the number of signal counts. The first is a function of lifetime with an expected value of 4.82 counts per day. For the latter a uniform prior was chosen. The limit on the half-life $T_{1/2}$ was calculated as

$$T_{1/2} > \frac{\ln(2) \eta_{\text{nat}} m t}{M_{\text{Xe}} N_{\text{lim}}},$$

where $\eta_{\text{nat}} = 9.52 \times 10^{-4}$ is the natural abundance of $^{124}$Xe and $N_{\text{lim}}$ is the 90% quantile of the posterior distribution for $N_{\text{sig}}$. The 90% credibility limit on the half-life as a function of measurement time is shown in Fig. 4 for a 1-t fiducial target. With only five live days of XENON1T, we expect to reach a sensitivity exceeding the current best experimental limit. With an exposure of 2 t yr we expect to reach a half-life limit of $6.1 \times 10^{22}$ yr.

V. CONCLUSIONS

We have conducted a search for $2\nu$2K of $^{124}$Xe using 7636 kg d of XENON100 data. No significant signal was observed leading to a lower 90% credibility limit on the half-life of $6.5 \times 10^{20}$ yr. This result supersedes the previous limit of $>1.66 \times 10^{21}$ yr [22] from an external analysis of published XENON100 data. We have shown that the XENON1T experiment is expected to probe half-lives up to a value of $6.1 \times 10^{22}$ yr after an exposure of 2 t yr. Since the XENON1T detector was also designed to measure higher energy signals more accurately than XENON100 it offers the possibility to study neutrinoless double-electron capture as well as electron capture with positron emission or double-positron decay where the main part of the observable energy is above 1 MeV [42]. Moreover, future multiton target experiments such as XMASS [23], LZ [22], XENONnT [41], and DARWIN [43] will have the sensitivity to investigate the parameter space even further.

ACKNOWLEDGMENTS

We thank Dieter Frekers and Jouni Suhonen for useful discussion. We gratefully acknowledge support from the National Science Foundation, Swiss National Science Foundation, Deutsche Forschungsgemeinschaft, Max Planck Gesellschaft, Foundation for Fundamental Research on Matter, Weizmann Institute of Science, I-CORE, Initial Training Network Invisibles (Marie Curie Actions, PITNGA-2011-289442), Fundacao para a Ciencia e a Tecnologia, Region des Pays de la Loire, Knut and Alice Wallenberg Foundation, and Istituto Nazionale di Fisica Nucleare. We are grateful to Laboratori Nazionali del Gran Sasso for hosting and supporting the XENON project.


[33] A. C. Thompson and D. Vaughan, editors, X-ray Data Booklet, 2nd ed. (Lawrence Berkeley National Laboratory, University of California, 2001).