Measurement of the inclusive jet cross-sections in proton-proton collisions at $\sqrt{s}=8$ TeV with the ATLAS detector

The ATLAS Collaboration

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Measurement of the inclusive jet cross-sections in proton-proton collisions at $\sqrt{s} = 8$ TeV with the ATLAS detector

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ABSTRACT: Inclusive jet production cross-sections are measured in proton-proton collisions at a centre-of-mass energy of $\sqrt{s} = 8$ TeV recorded by the ATLAS experiment at the Large Hadron Collider at CERN. The total integrated luminosity of the analysed data set amounts to 20.2 fb$^{-1}$. Double-differential cross-sections are measured for jets defined by the anti-$k_t$ jet clustering algorithm with radius parameters of $R = 0.4$ and $R = 0.6$ and are presented as a function of the jet transverse momentum, in the range between 70 GeV and 2.5 TeV and in six bins of the absolute jet rapidity, between 0 and 3.0. The measured cross-sections are compared to predictions of quantum chromodynamics, calculated at next-to-leading order in perturbation theory, and corrected for non-perturbative and electroweak effects. The level of agreement with predictions, using a selection of different parton distribution functions for the proton, is quantified. Tensions between the data and the theory predictions are observed.

KEYWORDS: Hadron-Hadron scattering (experiments), Jet physics

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1 Introduction

The Large Hadron Collider (LHC) [1] at CERN, colliding protons on protons, provides a unique opportunity to explore the production of hadronic jets in the TeV energy range. In Quantum Chromodynamics (QCD), jet production can be interpreted as the fragmentation of quarks and gluons produced in a short-distance scattering process. The inclusive jet production cross-section ($p + p \rightarrow \text{jet} + X$) gives valuable information about the strong coupling constant ($\alpha_s$) and the structure of the proton. It is also among the processes directly testing the experimentally accessible space-time distances.

Next-to-leading-order (NLO) perturbative QCD calculations [2, 3] give quantitative predictions of the jet production cross-sections. Progress in next-to-next-to-leading-order (NNLO) QCD calculations has been made over the past several years [4–9]. After the completion of the first calculations of some sub-processes [10, 11], the complete NNLO QCD inclusive jet cross-section calculation was published recently [12].

As fixed-order QCD calculations only make predictions for the quarks and gluons associated with the short-distance scattering process, corrections for the fragmentation of these partons to particles need to be applied. The measurements can also be compared to Monte Carlo event generator predictions that directly simulate the particles entering the detector. These event generators can be based on calculations with leading-order (LO) or NLO accuracy for the description of the short-distance scattering process as well as additional QCD radiation, hadronisation and multiple parton interactions [13].

Inclusive jet production cross-sections have been measured in proton-antiproton collisions at the Tevatron collider at various centre-of-mass energies. The latest and most precise measurements at $\sqrt{s} = 1.96$ TeV can be found in refs. [14, 15]. At the LHC, the ALICE, ATLAS and CMS collaborations have measured inclusive cross-sections in proton-proton collisions at centre-of-mass energies of $\sqrt{s} = 2.76$ TeV [16–18] and $\sqrt{s} = 7$ TeV [19–23], and recently the CMS Collaboration has also measured them at $\sqrt{s} = 8$ TeV [24] and $\sqrt{s} = 13$ TeV [25].

This paper presents the measurement of the inclusive jet cross-sections in proton-proton collisions at a centre-of-mass energy of $\sqrt{s} = 8$ TeV using data collected by the ATLAS experiment in 2012 corresponding to an integrated luminosity of 20.2 fb\(^{-1}\). The cross-sections are measured double-differentially and presented as a function of the jet transverse momentum, $p_T$, in six equal-width bins of the absolute jet rapidity, $|y|$. Jets are reconstructed using the anti-$k_t$ jet clustering algorithm [26] with radius parameters of $R = 0.4$ and $R = 0.6$. The measurement is performed for two jet radius parameters, since the uncertainties in the theoretical predictions are different. The kinematic region of $70 \text{GeV} \leq p_T \leq 2.5 \text{TeV}$ and $|y| < 3$ is covered.

The measurements explore a higher centre-of-mass energy than the previous ATLAS measurements and are also more precise due to the higher integrated luminosity and the better knowledge of the jet energy measurement uncertainties. Fixed-order NLO QCD predictions calculated for a suite of proton parton distribution function (PDF) sets, corrected for non-perturbative (hadronisation and underlying event) and electroweak effects, are quantitatively compared to the measurement results, unfolded for detector effects. The
results are also compared to the predictions of a Monte Carlo event generator based on
the NLO QCD calculation for the short-distance scattering process matched with parton
showers, followed by hadronisation. The measurement is performed with two different
jet radius parameters to test the sensitivity to perturbative (higher-order corrections and
parton shower) and non-perturbative effects.

The outline of the paper is as follows. A brief description of the ATLAS detector is
given in section 2. The inclusive jet production cross-section is defined in section 4. Section 3
gives an overview of the data set and Monte Carlo simulations used. The details of
the experimental measurement are presented in the next sections. Section 5 describes the
event and jet selection for the measurement. The jet energy calibration and the uncertain-
ties associated with the jet energy measurements are outlined in section 6. The procedure
to unfold the detector effects is detailed in section 7 and the propagation of the systematic
uncertainties in the measurements is explained in section 8. The theoretical predictions
are described in section 9. The results together with a quantitative comparison of the
measurements to the theory predictions are presented in section 10.

2 ATLAS detector

The ATLAS experiment [27] at the LHC is a multipurpose particle detector with a forward-
backward symmetric cylindrical geometry and a near 4π coverage in solid angle. It consists
of an inner tracking detector surrounded by a thin superconducting solenoid providing a 2 T
axial magnetic field, electromagnetic and hadron calorimeters, and a muon spectrometer.
The inner tracking detector covers the pseudorapidity range |η| < 2.5 and is made of silicon
pixel, silicon microstrip, and transition-radiation tracking detectors. Lead/liquid-argon
(LAr) sampling calorimeters provide electromagnetic (EM) energy measurements with high
granularity. A hadron (steel/scintillator-tile) calorimeter covers the central pseudorapidity
range (|η| < 1.7). The endcap and forward regions are instrumented with LAr calorimeters
for EM and hadronic energy measurements up to |η| = 4.9. The muon spectrometer
surrounds the calorimeters and is based on three large air-core toroid superconducting
magnets with eight coils each. Its bending power ranges between 2.0 and 6.0 T m for most
of the detector.

A three-level trigger system is used to select events. The first-level trigger is imple-
mented in hardware and uses a subset of the detector information to reduce the accepted
event rate to at most 75 kHz. This is followed by two software-based trigger levels that
together reduce the accepted event rate to 400 Hz on average depending on the data-taking
conditions during 2012.

The relevant systems used to select events with jets are the minimum-bias trigger
scintillators (MBTS), located in front of the endcap cryostats covering 2.1 < |η| < 3.8, as
well as calorimeter-based jet triggers covering |η| < 3.2 for central jets [28].

1ATLAS uses a right-handed coordinate system with its origin at the nominal interaction point (IP)in
the centre of the detector and the z-axis along the beam pipe. The x-axis points from the IP to the centre
of the LHC ring, and the y-axis points upwards. Cylindrical coordinates (r, φ) are used in the transverse
plane, φ being the azimuthal angle around the z-axis. The pseudorapidity is defined in terms of the polar
angle θ as η = −ln tan(θ/2). Angular distance is measured in units of ∆R = \sqrt{(Δφ)^2 + (Δη)^2}, where y is
the jet rapidity.
3 Data set and Monte Carlo simulations

The measurement uses proton-proton collision data at a centre-of-mass energy of $\sqrt{s} = 8\text{ TeV}$ collected by the ATLAS detector during the data-taking period of the LHC in 2012. The LHC beams were operated with proton bunches organised in “bunch trains”, with bunch-crossing intervals (or bunch spacing) of 50 ns.

The absolute luminosity measurement is derived from beam-separation scans performed in November 2012 and corresponds to $20.2\pm 2\text{ fb}^{-1}$ with an uncertainty of 1.9%. The uncertainty in the luminosity is determined following the technique described in refs. [29]. The average number of interactions per bunch crossing, $\langle \mu \rangle$, was $10 \leq \langle \mu \rangle \leq 36$. All data events considered in this analysis have good detector status and data quality.

For the simulation of the detector response to scattered particles in proton-proton collisions, events are generated with the Pythia 8 [30] (v8.160) Monte Carlo event generator. It uses LO QCD matrix elements for $2 \rightarrow 2$ processes, along with a leading-logarithmic (LL) $p_T$-ordered parton shower [31] including photon radiation, underlying-event simulation with multiple parton interactions [32], and hadronisation with the Lund string model [33]. The MC event generator’s parameter values are set according to the AU2 underlying event tune [34] and the CT10 PDF set [35] is used.

The stable particles from the generated events are passed through the ATLAS detector simulation [36] based on the Geant4 software toolkit [37] and are reconstructed using the same version of the ATLAS software as used to process the data. Effects from multiple proton-proton interactions in the same and neighbouring bunch crossings (pile-up) are included by overlaying inclusive proton-proton collision events (minimum bias), which consist of single-, double- and non-diffractive collisions generated by the Pythia 8 event generator using the A2 tune [34] based on the MSTW2008 LO PDF set [38]. The Monte Carlo events are weighted such that the distribution of the generated mean number of proton-proton collisions per bunch crossing matches that of the corresponding data-taking period. The particles from additional interactions are added before the signal digitisation and reconstruction steps of the detector simulation, but are not considered a signal and are therefore not used in the definition of the cross-section measurement defined in section 4.

For the evaluation of non-perturbative effects, the Pythia 8 [30] (v8.186) and Herwig++ [39] (v2.7.1) [40] event generators are also employed as described in section 9.3. The latter also uses LO matrix elements for the $2 \rightarrow 2$ short-distance process together with a LL angle-ordered parton shower [41]. It implements an underlying-event simulation based on an eikonal model [42] and the hadronisation process based on the cluster model [43].

The Powheg [44–46] method provides MC event generation based on an NLO QCD calculation matched to LL parton showers using the Powheg Box 1.0 package [47]. In this simulation the CT10 PDF set [35] is used. The simulation of parton showers, the hadronisation and the underlying event is based on Pythia 8 [30] using the AU2 tune [34]. These predictions are referred to as the Powheg predictions in the following.

The renormalisation and factorisation scales for the fixed-order NLO prediction are set to the transverse momentum of each of the outgoing partons of the $2 \rightarrow 2$ process, $p_T^{\text{Born}}$. 
In addition to the hard scatter, Powheg also generates the hardest partonic emission in the event using the LO $2 \to 3$ matrix element or parton showers. The radiative emissions in the parton showers are limited by the matching scale $\mu_M$ provided by Powheg.

4 Inclusive jet cross-section definition

Jets are identified with the anti-$k_t$ [26] clustering algorithm using the four-momentum recombination scheme, implemented in the FastJet [48] library, using two values of the jet radius parameter, $R = 0.4$ and $R = 0.6$. Throughout this paper, the jet cross-section measurements refer to jets built from stable particles defined by having a proper mean decay length of $c\tau > 10$ mm. Muons and neutrinos from decaying hadrons are included in this definition. More information about the particle definition can be found in ref. [49]. These jets are called “particle-level” jets in the following.

The inclusive jet double-differential cross-section, $d^2\sigma/dp_T^2dy$, is measured as a function of the jet transverse momentum $p_T$ in bins of rapidity $y$. In this context, “inclusive” cross-section means that all reconstructed jets in accepted events contribute to the measurement in the bins corresponding to their $p_T$ and $y$ values.

The kinematic range of the measurement is $70 \text{ GeV} \leq p_T \leq 2.5 \text{ TeV}$ and $|y| < 3$.

5 Event and jet selection

A set of single-jet triggers with various $p_T$ thresholds are used to preselect events to be recorded. The highest threshold trigger accepts all events passing the threshold. To keep the trigger rate to an acceptable level, the triggers with lower $p_T$ thresholds are only read out for a fraction of all events.

A $p_T$-dependent trigger strategy is adopted in order to optimise the statistical power of the measurement. Trigger efficiencies are studied using the trigger decisions in samples selected by lower-threshold jet triggers. The efficiency of the lowest $p_T$ jet trigger is determined with an independent trigger based on the MBTS scintillators. For each measurement bin, the trigger is chosen such that the highest effective luminosity (i.e. the lowest prescale factor) is obtained and the trigger is fully efficient. This procedure is performed separately for each of the jet radius parameters and for each jet rapidity bin.

At least one reconstructed vertex with at least two associated well-reconstructed tracks is required. Jet quality criteria are applied to reject jets from beam-gas events, beam-halo events, cosmic-ray muons and calorimeter noise bursts following the procedure described in ref. [50].

In the 2012 data set the central hadron calorimeter had a few modules turned off for certain long time periods or suffered from power-supply trips that made them non-operational for a few minutes. The energy deposited in these modules is estimated using the energy depositions in the neighbouring modules [50]. This correction overestimates the true deposited energy. Therefore, events where a jet with $p_T \geq 40 \text{ GeV}$ points to such a calorimeter region are rejected both in data and simulation.
6 Jet energy calibration and resolution

6.1 Jet reconstruction

Jets are defined with the anti-$k_t$ clustering algorithm with the jet radius parameters $R = 0.4$ and $R = 0.6$. The input objects for the jet algorithm are three-dimensional topological clusters (topoclusters) \cite{51, 52} built from the energy deposits in calorimeter cells. A local cluster weighting calibration (LCW) based on the topology of the calorimeter energy deposits is then applied to each topocluster to improve the energy resolution for hadrons impinging on the calorimeter \cite{51, 52}. The four-momentum of the LCW-scale jet is defined as the sum of four-momenta of the locally calibrated clusters in the calorimeter treating each cluster as a four-momentum with zero mass.

6.2 Jet energy calibration

Jets are calibrated using the procedure described in refs. \cite{50, 51}. The jet energy is corrected for the effect of multiple proton-proton interactions (pile-up) both in collision data and in simulated events. Further corrections depending on the jet energy and the jet pseudorapidity ($\eta$) are applied to achieve a calibration that matches the energy of jets composed of stable particles in simulated events. Fluctuations in the particle content of jets and in hadronic calorimeter showers are reduced with the help of observables characterising internal jet properties. These corrections are applied sequentially (Global Sequential Calibration). Differences between data and Monte Carlo simulation are evaluated using in situ techniques exploiting the $p_T$ balance of a jet and a well-measured object such as a photon ($\gamma$+jet balance), a $Z$ boson ($Z$+jet balance) or a system of jets (multijet balance). These processes are used to calibrate the jet energy in the central detector region, while the $p_T$ balance in dijet events is used to achieve an intercalibration of jets in the forward region with respect to central jets (dijet balance).

The calibration procedure that establishes the jet energy scale (JES) and the associated systematic uncertainty is given in more detail in the following:

Pile-up correction. Jets are corrected for the contributions from additional proton-proton interactions within the same (in-time) or nearby (out-of-time) bunch crossings \cite{53}. First, for each event a correction based on the jet area and the median $p_T$ density $\rho$ \cite{54, 55} is calculated. The jet area is a measure of the susceptibility of the jet to pile-up and is determined for each jet. The density, $\rho$, is a measure of the pile-up activity in the event. Subsequently, an average offset subtraction is performed based on the number of additional interactions and reconstructed vertices ($N_{PV}$) in the event. It is derived by comparing reconstructed calorimeter jets, with the jet-area correction applied, to particle jets in simulated inclusive jet events. The correction for contributions from additional proton-proton interactions can also remove part of the soft physics contributions, e.g. the contribution from the underlying event. This contribution is restored on average by the MC-based jet energy scale correction discussed below. The impact of pile-up subtraction on the jet energy resolution is corrected for in the unfolding step (see section 7).
Jet energy scale. The energy and the direction of jets are corrected for instrumental effects (non-compensating response of the calorimeter, energy losses in dead material, and out-of-cone effects) and the jet energy scale is restored on average to that of the particles entering the calorimeter using an inclusive jet Monte Carlo simulation [56]. These corrections are derived in bins of energy and the pseudorapidity of the jet.

Global sequential correction. The topology of the calorimeter energy deposits and of the tracks associated with jets can be exploited to correct for fluctuations in the jet’s particle content [51, 57]. The measured mean jet energy depends on quantities such as the number of tracks, the radial extent of the jets as measured from the tracks in the jets, the longitudinal and lateral extent of the hadronic shower in the calorimeter and the hits in the muon detector associated with the jet. A correction of the jet energy based on these quantities can therefore improve the jet resolution and reduce the dependence on jet fragmentation effects. The correction is constructed from a MC sample based on one generator such that the jet energy scale correction is unchanged for the inclusive jet sample, but the jet energy resolution is improved and the sensitivity to jet fragmentation effects such as differences between quark- or gluon-induced jets is moderated. The dependence of this correction on the MC generator is treated as uncertainty.

Correction for difference between data and Monte Carlo simulation. A residual calibration is applied to correct for remaining differences between the jet energy response in data and simulation. This correction is derived insitu by comparing the results of $\gamma+\text{jet}$, $Z+\text{jet}$, dijet and multijet $p_T$-balance techniques [56, 58, 59]. The level of agreement between the jet energy response in the Monte Carlo simulation and the one in the data is evaluated by exploiting the $p_T$ balance between a photon or a $Z$ boson and a jet. In the $p_T$ range above about 800 GeV, which cannot be reached by $\gamma+\text{jet}$ events, the recoil system of low-$p_T$ jets in events with more than two jets is used (multijet balance).

This correction is applied to the central detector region. The relative response in all detector regions is equalised using an intercalibration method that uses the $p_T$ balance in dijet events where one jet is central and one jet is in the forward region of the detector ($\eta$-intercalibration).

In the region above $p_T = 1.7$ TeV, where the insitu techniques do not have sufficient statistical precision, the uncertainty in the jet energy measurement is derived from single-hadron response measurements [60, 61].

6.3 Jet energy scale uncertainties

The jet calibration corrections are combined following the procedure described in ref. [56]. The systematic and statistical uncertainties of each of the above mentioned corrections contribute to the total JES uncertainty as independent systematic components.

The insitu techniques are based on various processes leading to jets with different fragmentation patterns. Differences in the calorimeter response to jets initiated by quarks
or gluons in the short-distance processes lead to an additional uncertainty. Limited knowledge of the exact flavour composition of the analysed data sample is also considered as an uncertainty. An estimation of flavour composition based on the Pythia and the Powheg + Pythia Monte Carlo simulations is used in order to reduce this uncertainty.

A systematic uncertainty needs to be assigned to the correction, based on the muon hits behind the jet, that corrects jets with large energy deposition behind the calorimeter (punch-through).

In total, 66 independent systematic components uncorrelated among each other and fully correlated across $p_T$ and $\eta$, constitute the full JES uncertainty in the configuration with the most detailed description of correlations [56]. A simplification is performed in this standard configuration: the $\eta$-intercalibration statistical uncertainty being treated as one uncertainty component fully correlated between the jet rapidity and $p_T$ bins for which the $\eta$-intercalibration was performed. However, at the level of precision achieved in this analysis a detailed description of the statistical uncertainties of the $\eta$-intercalibration calibration procedure is important. For this reason, in this measurement, the total statistical uncertainty of the $\eta$-intercalibration in the standard configuration is replaced by 240 (250) uncertainty components for jets with $R = 0.4$ ($R = 0.6$), propagated from the various bins of the insitu $\eta$-intercalibration analysis [58].

The total uncertainty in the JES is below 1% for $100 \text{GeV} < p_T < 1500 \text{GeV}$ in the central detector region ($|\eta| \leq 0.8$) rising both towards lower and higher $p_T$ and larger $|\eta|$ [56].

### 6.4 Jet energy resolution and uncertainties

The fractional uncertainty in the jet $p_T$ resolution (JER) is derived using the same insitu techniques as used to determine the JES uncertainty from the width of the ratio of the $p_T$ of a jet to the $p_T$ of a well-measured particle such as a photon or a $Z$ boson [59]. In addition, the balance between the jet transverse momenta in events with two jets at high $p_T$ can be used ($\eta$-intercalibration) [58]. This method allows measurement of the JER at high jet rapidities and in a wide range of transverse momenta. The results from individual methods are combined similarly to those for the JES [56]. This JER evaluation includes a correction for physics effects such as radiation of extra jets which can also alter the $p_T$ ratio width. This correction is obtained from a Monte Carlo simulation.

The JER uncertainty has in total 11 systematic uncertainty components. Nine systematic components are obtained by combining the systematic uncertainties associated with the insitu methods. The last two are the uncertainty due to the electronic and pile-up noise measured in inclusive proton-proton collisions and the absolute JER difference between data and MC simulation as determined with the insitu methods. The latter is non-zero only for low-$p_T$ jets in forward rapidity regions. In the rest of the phase-space region the JER in MC simulation is better than in data and this uncertainty is eliminated by smearing the jet $p_T$ in simulation such that the resulting resolution matches closely the one in data. Each JER systematic component describes an uncertainty that is fully correlated in jet $p_T$ and pseudorapidity. The 11 JER components are treated independently from each other.
6.5 Jet angular resolution and uncertainties

The jet angular resolution (JAR) is estimated from comparisons of the polar angles of a reconstructed jet and the matched particle-level jet using the Monte Carlo simulation. This estimate is cross-checked by comparing the standard jets using calorimeter energy deposits as inputs to the ones using tracks in the inner detector [50, 51]. A relative uncertainty of 10% is assigned to the JAR to account for possible differences between data and MC simulation.

7 Unfolding of detector effects

The reconstructed jet spectra in data are unfolded to correct for detector inefficiencies and resolution effects to obtain the inclusive jet cross-section that refers to the stable particles entering the detector. The detector unfolding is based on Monte Carlo simulation and is performed in three consecutive steps, namely, a correction for the matching impurity at reconstruction level, the unfolding for resolution effects and a correction for the matching inefficiency at particle level, as explained below. In order to account for migrations from lower $p_T$ into the region of interest, this study is performed in a wider $p_T$ range than the one for the final result.

The unfolding of the detector resolution in jet $p_T$ is based on a modified Bayesian technique, the Iterative Dynamically Stabilised (IDS) method [62]. This unfolding method uses a transfer matrix describing the migrations of jets across the $p_T$ bins, between the particle level and the reconstruction level. A minimal number of iterations in the IDS unfolding method is chosen such that the residual bias, evaluated through a data-driven closure test (see below), is within a tolerance of 1% in the bins with less than 10% statistical uncertainty. In this measurement this is achieved after one iteration.

The transfer matrix used in the unfolding is derived by matching a particle level jet with a reconstructed jet in Monte Carlo simulations, when both are closer to each other than to any other jet and lie within a radius of $\Delta R = 0.3$.

The matching purity, $\mathcal{P}$, is defined as the ratio of the number of matched reconstructed jets to the total number of reconstructed jets. The matching efficiency, $\mathcal{E}$, is defined as the ratio of the number of matched particle jets to the total number of particle jets. If jets migrate to other rapidity bins, they are considered together with the jets that are completely unmatched. In this way the migrations across rapidity bins are effectively taken into account by bin-to-bin corrections.

The final result is given by

$$\mathcal{N}_i^{\text{part}} = \sum_j \mathcal{N}_j^{\text{reco}} \cdot \mathcal{P}_j \cdot A_{ij} / \mathcal{E}_i,$$

(7.1)

where $i$ and $j$ are the bin indices of the jets at particle- and reconstructed-levels and $\mathcal{N}_i^{\text{part}}$ and $\mathcal{N}_j^{\text{reco}}$ are the number of particle-level and reconstructed jets in a given bin. The symbol $A$ denotes the unfolding matrix obtained by the IDS method from the transfer matrix. The element $A_{ij}$ describes the probability for a reconstructed jet in $p_T$ bin $j$ to originate from particle-level $p_T$ bin $i$. 


The precision of the unfolding technique is assessed using a data-driven closure test \cite{20, 62}. The particle-level $p_T$ spectrum in the MC simulation is reweighted such that the reweighted reconstructed spectrum and the data agree. The reconstructed spectrum in this reweighted MC simulation is then unfolded using the same procedure as for the data. The ratio of the unfolded spectrum to the reweighted particle-level spectrum provides an estimate of the unfolding bias. The residual bias is taken into account as a systematic uncertainty. After one IDS iteration, this uncertainty is of the order of a few per mille in the whole phase-space region, except for the very high $p_T$ bins in each of the rapidity bins, where it grows to a few percent (up to 15\% in certain cases).

The statistical and systematic uncertainties are evaluated by repeating the unfolding as explained in section 8.

8 Propagation of the statistical and systematic uncertainties

The statistical uncertainties are propagated through the unfolding procedure using an ensemble of pseudo-experiments. For each pseudo-experiment in the ensemble, a weight fluctuated according to a Poisson distribution with a mean value equal to one is applied to each event in data and simulation. This procedure takes into account the correlation between jets produced in the same event. The unfolding is performed for each pseudo-experiment. An ensemble of 10000 pseudo-experiments is used to calculate a covariance matrix for the cross-section in each jet rapidity bin. The total statistical uncertainty is obtained from the covariance matrix, where bin-to-bin correlations are also encoded. The separate contributions from the data and from the MC statistics are obtained from the same procedure by fluctuating only either the data or the simulated events. Furthermore, an overall covariance matrix is constructed to describe the full statistical covariance among all analysis bins.

To propagate the JES uncertainties to the measurement, the jet $p_T$ is scaled up and down by one standard deviation of each of the components (see section 6) in the MC simulation. The resulting $p_T$ spectra are unfolded for detector effects using the nominal unfolding matrix. The difference between the nominal unfolded cross-section and the one with the jet $p_T$ scaled up and down is taken as a systematic uncertainty.

The uncertainty in the JER is the second largest individual source of systematic uncertainty. The effect of each of the 11 JER systematic uncertainty components is evaluated by smearing the energy of the reconstructed jets in the MC simulation such that the resolution is degraded by the size of each uncertainty component. A new transfer matrix is constructed using the smeared jets and is used to unfold the data spectra. The difference of the cross-sections unfolded with the jet-energy-smeared transfer matrix and the nominal transfer matrix is taken as a systematic uncertainty. The JER uncertainty is applied symmetrically as an upward and downward variation.

The JAR is propagated to the cross-section in the same way as for the JER.

The uncertainty associated with the residual model dependence in the unfolding procedure is described in section 7. The systematic uncertainties propagated through the
unfolding are evaluated using a set of pseudo-experiments for each component, as in the evaluation of the statistical uncertainties.

The use of pseudo-experiments for the evaluation of the systematic uncertainties allows an evaluation of the statistical fluctuations. The statistical fluctuations of the systematic uncertainties are reduced using a smoothing procedure. For each component, the $p_T$ bins are combined until the propagated uncertainty value in the bin has a Poisson statistical significance larger than two standard deviations. A Gaussian kernel smoothing [50] is used to restore the original fine bins.

An uncertainty for the jet cleaning procedure described in section 5 is estimated from the relative difference between the efficiencies obtained from the distributions with and without the jet quality cut in data and simulation.

The uncertainty in the luminosity measurement of 1.9% [29] is propagated as being correlated across all measurement bins.

An uncertainty in the beam energy of 0.1% [63] is considered when comparing data with the theory prediction at a fixed beam energy. The induced uncertainty at the cross-section level is evaluated by comparing the theory predictions at the nominal and shifted beam energies. It amounts for 0.2% at low $p_T$ and 1% at high $p_T$ in the central region and rises up to 3% at highest $p_T$ and high rapidity. This uncertainty is similar for jets with $R = 0.4$ and $R = 0.6$.

The individual systematic uncertainty sources are treated as uncorrelated with each other for the quantitative comparison of the data and the theory prediction. When shown in figures the individual uncertainties are added in quadrature to obtain the total systematic uncertainty. The shape of the systematic uncertainties follows a log-normal distribution, as in the analysis of inclusive jet production at 7 TeV [19]. The systematic uncertainties in the inclusive jet cross-section measurement are shown in figure 1 for representative rapidity regions for anti-$k_T$ jets with $R = 0.4$ and $R = 0.6$. In the central (forward) region the total uncertainty is about 5% (10%) at medium $p_T$ of 300–600 GeV. The uncertainty increases towards both lower and higher $p_T$ reaching to 15% at low $p_T$ and 50% at high $p_T$. The JES and JER uncertainties for jets with different sizes are rather similar at the jet level. However, at the cross-section level differences occur due to the different slopes of the distributions.

The dominant systematic uncertainty source for the measurement of the inclusive jet cross-sections is related to the jet energy measurement. The jet energy scale uncertainty is larger than the jet energy resolution uncertainty.

9 Theoretical predictions

9.1 Next-to-leading-order QCD calculation

The NLOJet++ [64] (v4.1.3) software program is used to calculate the NLO QCD predictions for the $2 \rightarrow 2$ processes for the inclusive jet cross-sections. The renormalisation and factorisation scales are set to the $p_T$ of the leading jet in the event, i.e. $\mu_R = \mu_F = p_{T,\text{jet,max}}$. For fast and flexible calculations with various PDFs as well as different renormalisation and factorisation scales, the APPLGRID software [65] is interfaced with NLOJet++. 
Figure 1. Relative systematic uncertainty for the inclusive jet cross-section as a function of the jet transverse momentum $p_{T,jet}$. The total systematic uncertainty is shown by the black line. The individual uncertainties are shown in colours: the jet energy scale (red), jet energy resolution (yellow) and the other uncertainties (JAR, jet selection, luminosity and unfolding bias) added in quadrature. The results are shown for the (a,b) first and (c,d) last jet rapidity bins and for anti-$k_t$ jets with (a,c) $R = 0.4$ and (b,d) $R = 0.6$. The statistical uncertainty is shown by the vertical error bar on each point.

The inclusive jet cross-sections are presented for the CT14 [66], MMHT2014 [67], NNPDF3.0 [68], HERAPDF2.0 [69] PDF sets provided by the LHAPDF6 [70] library. The value for the strong coupling constant $\alpha_s$ is taken from the corresponding PDF set.
Three sources of uncertainty in the NLO QCD calculation are considered: the PDFs, the choice of renormalisation and factorisation scales, and the value of $\alpha_s$. The PDF uncertainty is defined at 68% confidence level (CL) and is evaluated following the prescriptions given for each PDF set, as recommended by the PDF4LHC group for PDF-sensitive analyses [71]. The scale uncertainty is evaluated by varying the renormalisation and factorisation scales by a factor of two with respect to the original choice in the calculation. The envelope of the cross-sections with all possible combinations of the scale variations, except the ones when the two scales are varied in opposite directions, is considered as a systematic uncertainty. An alternative scale choice, $\mu_R = \mu_F = p_T^\text{jet}$, the $p_T$ of each individual jet that enters the cross-section calculation, is also considered. This scale choice is proposed in ref. [72]. The difference with respect to the prediction obtained for the $p_T^\text{jet,max}$ scale choice is treated as an additional uncertainty. The uncertainty from $\alpha_s$ is evaluated by calculating the cross-sections using two PDF sets determined with two different values of $\alpha_s$ and then scaling the cross-section difference corresponding to an $\alpha_s$ uncertainty $\Delta \alpha_s = 0.0015$ as recommended in ref. [71].

The uncertainties in the NLO QCD cross-section predictions obtained with the CT14 PDF set are shown in figure 2 for representative phase-space regions. The renormalisation and factorisation scale uncertainty is the dominant uncertainty in most phase-space regions, rising from around 5–10% at low $p_T$ in the central rapidity bin to about 50% in the highest $p_T$ bins in the most forward rapidity region. This uncertainty is asymmetric and it is larger for anti-$k_t$ jets with $R = 0.6$ than for jets with $R = 0.4$. The alternative scale choice, $p_T^\text{jet}$, leads to a similar inclusive jet cross-section at the highest jet $p_T$, but gives an increasingly higher cross-section when the jet $p_T$ decreases. For $p_T = 70$ GeV this difference is about 10%. The PDF uncertainties vary from 5% to 50% depending on the jet $p_T$ and rapidity. The $\alpha_s$ uncertainty is about 3% and is rather constant in the considered phase-space regions.

9.2 Electroweak corrections

The NLO QCD predictions are corrected for electroweak effects derived using an NLO calculation in the electroweak coupling ($\alpha$) and based on a LO QCD calculation [73]. The CTEQ6L1 PDF set is used [74]. This calculation includes tree-level effects on the cross-section of $O(\alpha S, \alpha^2)$ as well as effects of loops of weak interactions at $O(\alpha_s^2)$. Effects of photon or $W=Z$ radiation are not included in the corrections. Real $W/Z$ radiation may affect the cross-section by a few percent at $p_T \sim 1$ TeV [75].

The correction factors were derived in the phase space considered for the measurement presented here and are provided by the authors of ref. [73] through a private communication. No uncertainty associated with these corrections is presently estimated.

Figure 3 shows the electroweak corrections for jets with $R = 0.4$ and $R = 0.6$. The correction reaches more than 10% for the highest $p_T$ in the lowest rapidity bin, but decreases rapidly as the rapidity increases. It is less than 3% for jets with $|y| > 1$.

9.3 Non-perturbative corrections

In order to compare the fixed-order NLO QCD calculations to the measured inclusive jet cross-sections, corrections for non-perturbative (NP) effects need to be applied. Each
Figure 2. Relative NLO QCD uncertainties for the inclusive jet cross-section calculated for the CT14 PDF set in the (a,b) central and (c,d) forward region for anti-$k_t$ jets with (a,c) $R = 0.4$ and (b,d) $R = 0.6$. Shown are the uncertainties due to the renormalisation and factorisation scales, the $s$, the PDF and the total uncertainty. The default scale choice $p_{\text{jet,max}}^T$ is used.

The corrections are derived using LO Monte Carlo event generators complemented by the leading-logarithmic parton shower by evaluating the bin-wise ratio of the cross-section with and without the hadronisation and the underlying event processes.
The MC event generators are run twice, once with the hadronisation and underlying event switched on and again with these two processes switched off. The inclusive jet cross-sections are built either from the stable particles or from the last partons in the event record, i.e. the partons after the parton showers finished and before the hadronisation process starts. These partons are the ones that are used in the Lund string model and the cluster fragmentation model to form the final-state hadrons. The bin-by-bin ratios of the inclusive jet cross-sections are taken as an estimate for the non-perturbative corrections.

The nominal correction is obtained from the Pythia 8 event generator [30] with the AU2 tune using the CT10 PDF [35], i.e. the same configuration as used to correct the data for detector effects (see section 3). The uncertainty is estimated as the envelope of the corrections obtained from a series of alternative Monte Carlo event generator configurations as shown in table 1.

The correction factors are shown in figure 4 in representative rapidity bins for anti-\(k_T\) jets with \(R = 0.4\) and \(R = 0.6\) as a function of the jet \(p_T\).

The nominal correction increases the cross-section by 4\% (15\%) for \(p_T = 70 \text{ GeV}\) for anti-\(k_T\) jets with \(R = 0.4\) (\(R = 0.6\)). The large differences between the two jet sizes result from the different interplay of hadronisation and underlying-event effects. While for anti-\(k_T\) jets with \(R = 0.4\) the contribution from the hadronisation tends to cancel with the one from the underlying event, for anti-\(k_T\) jets with \(R = 0.6\) the effect from the underlying event becomes dominant. At large \(p_T\) the non-perturbative correction factor is close to 1. There is only a small dependence of the non-perturbative corrections on the jet rapidity.
<table>
<thead>
<tr>
<th>Generator</th>
<th>Tune</th>
<th>PDF</th>
</tr>
</thead>
<tbody>
<tr>
<td>Pythia 8</td>
<td>4C [78]</td>
<td>CTEQ6L [74]</td>
</tr>
<tr>
<td></td>
<td>Monash [76]</td>
<td>NNPDF2.3L [79, 80]</td>
</tr>
<tr>
<td></td>
<td>AU2 [34]</td>
<td>CT10 [35]</td>
</tr>
<tr>
<td></td>
<td>AU2 [34]</td>
<td>CTEQ6L [74]</td>
</tr>
<tr>
<td></td>
<td>A14 [77]</td>
<td>NNPDF2.3L [79, 80]</td>
</tr>
<tr>
<td></td>
<td>A14 [77]</td>
<td>MRSTW2008lo** [81]</td>
</tr>
<tr>
<td></td>
<td>A14 [77]</td>
<td>CTEQ6L [74]</td>
</tr>
<tr>
<td>Herwig++</td>
<td>UE-EE-5 [82, 83]</td>
<td>CTEQ6L [74]</td>
</tr>
<tr>
<td></td>
<td>UE-EE-5 [82, 83]</td>
<td>MRSTW2008lo** [81]</td>
</tr>
<tr>
<td></td>
<td>UE-EE-4 [82, 83]</td>
<td>CTEQ6L [74]</td>
</tr>
</tbody>
</table>

Table 1. Summary of Monte Carlo generator configurations used for the evaluation of the non-perturbative corrections. The name of the generator and the soft physics model tune as well as the PDF set used when deriving the tune is specified.

The nominal correction is larger than the correction from other MC configurations. The corrections based on Pythia 8 with the Monash [76] or the A14 [77] tunes give correction factors that are closer to 1. The corrections based on Herwig++ give corrections that are much lower than the one based on Pythia 8. The correction based on Herwig++ is $-10\%$ (1%) for $p_T = 70\,\text{GeV}$ for anti-$k_t$ jets with $R = 0.4$ ($R = 0.6$).

9.4 NLO QCD matched with parton showers and hadronisation

The measured inclusive jet cross-section can be directly compared to predictions based on the Powheg Monte Carlo generator where an NLO QCD calculation for the hard scattering $2 \rightarrow 2$ process is matched to parton showers, hadronisation and underlying event.

A procedure to estimate the effect of the matching of the hard scattering and the parton shower is not yet well established. Therefore, no uncertainties are shown for the Powheg predictions. The Powheg prediction’s uncertainty due to PDF is expected to be similar to that in fixed-order NLO calculations, whereas the uncertainty due to $\alpha_s$ is expected to be larger, and the uncertainty due to the renormalisation and factorisation scales smaller.

The simulation using a matched parton shower has a more coherent treatment of the effect of parton showers and hadronisation than the approach using a fixed-order NLO QCD calculation corrected for non-perturbative effects. However, ambiguities in the matching procedure and the tuning of the parton shower parameters based on processes simulated only at leading order by Pythia 8 may introduce additional theoretical uncertainties. Therefore, quantitative comparisons using theoretical uncertainties based on Powheg are not performed in this paper.
Figure 4. Non-perturbative correction factors as a function of jet $p_T$ for (a,b) the most central and (c,d) most forward region, for jets defined by the anti-$k_t$ algorithm with (a,c) $R = 0.4$ and (b,d) $R = 0.6$. The corrections are derived using Pythia 8 and Herwig++ with several soft physics tunes. The envelope of all MC configuration variations is shown as a band.

10 Results

10.1 Qualitative comparisons of data to NLO QCD calculations

The measured double-differential inclusive jet cross-sections are shown in figure 5 and figure 6 as a function of the jet $p_T$ for anti-$k_t$ jets with $R = 0.4$ and $R = 0.6$ for each jet rapidity bin. The cross-section covers 11 orders of magnitude in the central rapidity region and 9 orders of magnitude in the forward region. Jet transverse momenta above $p_T = 2$ TeV...
are observed. In the most forward region the jet $p_T$ reaches about 500 GeV. Tabulated values of all observed results, with full details of uncertainties and their correlations, are also provided in the Durham HEP database [84].

The measurement is compared to an NLO QCD prediction using the MMHT2014 PDF set [67] based on NLOJet++ corrected for non-perturbative and electroweak effects. The shaded band shows the total theory uncertainty as explained in section 9.1. This theory prediction describes the gross features in the data.

The ratio of NLO QCD calculations to data corrected for non-perturbative and electroweak effects for various PDF sets is shown in figure 7 and figure 8 for anti-$k_T$ jets $R = 0.4$ and $R = 0.6$, respectively. At low $p_T$ the level of agreement is very sensitive to
\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{inclusive-jet-cross-section.png}
\caption{Inclusive jet cross-section as a function of jet $p_T$ in bins of jet rapidity. The results are shown for jets identified using the anti-$k_t$ algorithm with $R = 0.6$. For better visibility the cross-sections are multiplied by the factors indicated in the legend. The data are compared to the NLO QCD prediction with the MMHT2014 PDF set corrected for non-perturbative and electroweak effects. The error bars indicate the statistical uncertainty and the systematic uncertainty in the measurement added in quadrature. The statistical uncertainty is shown separately by the inner vertical line.}
\end{figure}

non-perturbative effects. When using Pythia 8 as the nominal non-perturbative correction, the NLO QCD prediction is typically about 10–20% above the data at low $p_T$, whereas the NLO QCD prediction corrected with Herwig++ follows the data well for anti-$k_t$ jets with $R = 0.4$, while it is 5–10% below the data for anti-$k_t$ jets with $R = 0.6$.

The comparison is also influenced by the nominal choice of renormalisation and factorisation scales in the NLO QCD calculation. Setting the scale to $p_{T,jet}^{\text{max}}$ instead of $p_{T,jet}^{\text{jet,max}}$ (see section 9.1) leads to an NLO QCD prediction that is at low jet $p_T$ higher than the prediction using the $p_{T,jet}^{\text{jet,max}}$ scale (about 8% at $p_T = 100$ GeV for all pseudorapidity regions). With this scale setting the deviation from the data at low $p_T$ is larger.
Figure 7. Ratio of the inclusive jet cross-section predicted by NLO QCD corrected for non-perturbative and electroweak effects to the cross-section in data as a function of the jet $p_T$ in each jet rapidity bin. Shown are the predictions for various PDF sets for anti-$k_t$ jets with $R = 0.4$. The points are offset in jet $p_T$ for better visibility. The error bars indicate the total theory uncertainty. The grey band shows the total uncertainty in the measurement.

The recent calculation of NNLO QCD inclusive jet cross-sections at $\sqrt{s} = 7$ TeV is higher than in NLO QCD at low jet $p_T$ for all jet rapidity regions [12]. For instance, for $p_T = 100$ GeV the increase from NLO to NNLO is about 10%. For both the NNLO and the NLO QCD calculations the $p_T^{\text{jet}, \text{max}}$ scale is used. Therefore, it is expected that the NNLO QCD prediction at $\sqrt{s} = 8$ TeV would deviate from the data more strongly than the NLO QCD calculation. This deviation might need to be accommodated by an adjustment of the PDFs.

Towards higher $p_T$ the NLO QCD predictions get closer to the data while for $p_T > 1$ TeV they rise with respect to the data. For the highest $p_T$ at central rapidities they are typically up to 10–20% higher than data. The behaviour of the CT14, NNPDF3.0 and MMHT2014 PDF sets is similar. The NLO QCD predictions based on the HERAPDF2.0, however, are significantly lower than data in the region $300 < p_T < 1000$ GeV.

In the most forward region, $|y| > 2$, all PDF sets give predictions close to the data at low $p_T$ for anti-$k_t$ jets with $R = 0.4$ and $R = 0.6$. However, towards higher $p_T$ and in particular for $p_T > 400$ GeV the CT14, NNPDF3.0 and MMHT2014 PDF sets give predictions much higher than the data. The prediction for the HERAPDF2.0 is lower than for the other PDF sets and also falls below the data. In this region, both the experimental and the theoretical uncertainties become large.

Overall, the NLO QCD prediction based on the CT14 PDF set gives the best qualitative agreement, while HERAPDF2.0 gives the worst agreement over a wide jet $p_T$ range.
Figure 8. Ratio of the inclusive jet cross-section predicted by NLO QCD corrected for non-perturbative and electroweak effects to the cross-section in data as a function of the jet $p_T$ in each jet rapidity bin. Shown are the predictions for various PDF sets for anti-$k_t$ jets with $R = 0.6$. The points are offset in jet $p_T$ for better visibility. The error bars indicate the total theory uncertainty. The grey band shows the total uncertainty in the measurement.

However, the central values from the HERAPDF2.0 PDF set are more consistent with the data in the forward region at high $p_T$. This indicates that this measurement has sensitivity to constrain PDFs.

10.2 Quantitative comparison of data to NLO QCD calculations

A quantitative comparison of the NLO QCD predictions, corrected for non-perturbative and electroweak effects, to the measurement is performed using the method described in ref. [85]. The $\chi^2$ value and the corresponding observed $p$-value, $P_{\text{obs}}$, are computed taking into account the asymmetries and the correlations of the experimental and theoretical uncertainties. The individual experimental and theoretical uncertainty components are assumed to be uncorrelated among one another and fully correlated across the $p_T$ and $y$ bins. The correlation of the statistical uncertainties across $p_T$ and rapidity bins are taken into account using covariance matrices derived from 10000 pseudo-experiments obtained by fluctuating the data and the MC simulation (see section 7).

For the theoretical prediction, the uncertainties related to the scale variations, the alternative scale choice, the PDF eigenvectors, the non-perturbative corrections and the strong coupling constant are treated as separate uncertainty components. In the case of the NNPDF3.0 PDF set, the replicas are used to evaluate a covariance matrix, from which the eigenvectors are then determined.

Table 2 shows the evaluated $P_{\text{obs}}$ for the NLO QCD predictions corrected for non-perturbative and electroweak effects for each rapidity bin considered individually. In this...
Table 2. Observed $P_{\text{obs}}$ values evaluated for the NLO QCD predictions corrected for non-perturbative and electroweak effects and the measured inclusive jet cross-section of anti-$k_T$ jets with $R = 0.4$ and $R = 0.6$. Only measurements with $p_T > 100$ GeV are included. The predictions are evaluated for various PDF sets. The default scale choice $p_T^{\text{jet,max}}$ is used.

<table>
<thead>
<tr>
<th>Rapidity ranges</th>
<th>$p_T &gt; 70$ GeV</th>
<th>$100 &lt; p_T &lt; 900$ GeV</th>
<th>$100 &lt; p_T &lt; 400$ GeV</th>
</tr>
</thead>
<tbody>
<tr>
<td>Anti-$k_T$ jets</td>
<td>$R = 0.4$</td>
<td>$R = 0.6$</td>
<td>$R = 0.6$</td>
</tr>
<tr>
<td>$</td>
<td>y</td>
<td>&lt; 0.5$</td>
<td>44%</td>
</tr>
<tr>
<td>$0.5 \leq</td>
<td>y</td>
<td>&lt; 1.0$</td>
<td>43%</td>
</tr>
<tr>
<td>$1.0 \leq</td>
<td>y</td>
<td>&lt; 1.5$</td>
<td>44%</td>
</tr>
<tr>
<td>$1.5 \leq</td>
<td>y</td>
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<td>3.7%</td>
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<td>$2.0 \leq</td>
<td>y</td>
<td>&lt; 2.5$</td>
<td>92%</td>
</tr>
<tr>
<td>$2.5 \leq</td>
<td>y</td>
<td>&lt; 3.0$</td>
<td>4.5%</td>
</tr>
</tbody>
</table>

In addition to the quantitative comparisons of the theory and data cross-sections in individual jet rapidity bins, all data points can be considered together. Table 3 shows the $\chi^2$ values for each PDF set, $R$ value and scale choice, when using all the $|y|$ bins together. Various $p_T$ ranges are tested. All the corresponding $P_{\text{obs}}$ values are much smaller than $10^{-3}$. If the statistical uncertainty of the $\eta$-intercalibration were treated as a single component (see section 6), the $\chi^2$ values computed in table 3 would be strongly enhanced (by even more than 200 units for some configurations).
Further quantitative comparisons using all the $|y|$ bins together were performed in more restricted $p_T$ ranges (70 < $p_T$ < 100 GeV, 100 < $p_T$ < 240 GeV, 240 < $p_T$ < 408 GeV, 408 < $p_T$ < 642 GeV, 642 < $p_T$ < 952 GeV and $p_T$ > 952 GeV), for the CT14 PDF set. While good agreement is observed in the range 70 < $p_T$ < 100 GeV, for both jet radii $R$ values, the $P_{\text{obs}}$ values for the other ranges are small (often below 0.1%). For the same five restricted $p_T$ ranges above 100 GeV, considering this time pairs of consecutive $|y|$ bins, good agreement between data and theory is observed in most cases. Good agreement is also observed when considering pairs of one central and one forward (i.e. first-last) $|y|$ bins. These tests show that the source of the low $P_{\text{obs}}$ values discussed above is not localised in a single rapidity bin, nor due to some possible tension between the central and the forward regions.

Since the difference between the non-perturbative corrections with two Monte Carlo generators is taken as a systematic uncertainty, the result of the quantitative comparison has little sensitivity to which correction is chosen as the nominal one. Even using the correction that brings the fixed-order NLO QCD to the Powheg prediction, i.e. including an additional correction for parton shower effects, does not alter the $P_{\text{obs}}$ values. It is therefore expected that an explicit correction of parton shower effects as suggested in

<table>
<thead>
<tr>
<th>$\chi^2$/ndf</th>
<th>$p_T^{\text{jet, max}}$</th>
<th>$p_T^{\text{jet}}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$p_T &gt; 70$ GeV</td>
<td></td>
<td></td>
</tr>
<tr>
<td>CT14</td>
<td>349/171 398/171</td>
<td>340/171 392/171</td>
</tr>
<tr>
<td>HERAPDF2.0</td>
<td>415/171 424/171</td>
<td>405/171 418/171</td>
</tr>
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<td>350/171 393/171</td>
</tr>
<tr>
<td>MMHT2014</td>
<td>356/171 400/171</td>
<td>354/171 399/171</td>
</tr>
<tr>
<td>$p_T &gt; 100$ GeV</td>
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</tr>
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<td>CT14</td>
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</tr>
<tr>
<td>HERAPDF2.0</td>
<td>385/159 374/159</td>
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</tr>
<tr>
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<td>333/159 356/159</td>
<td>331/159 356/159</td>
</tr>
<tr>
<td>MMHT2014</td>
<td>335/159 364/159</td>
<td>333/159 362/159</td>
</tr>
<tr>
<td>$100 &lt; p_T &lt; 900$ GeV</td>
<td></td>
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</tr>
<tr>
<td>CT14</td>
<td>272/134 306/134</td>
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</tr>
<tr>
<td>HERAPDF2.0</td>
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<td>340/134 326/134</td>
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<tr>
<td>$100 &lt; p_T &lt; 400$ GeV</td>
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<td>141/72 170/72</td>
</tr>
<tr>
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<td>119/72 141/72</td>
<td>115/72 139/72</td>
</tr>
<tr>
<td>MMHT2014</td>
<td>132/72 143/72</td>
<td>122/72 140/72</td>
</tr>
</tbody>
</table>

**Table 3.** Summary of $\chi^2$/ndf obtained from the comparison of the inclusive jet cross-section and the NLO QCD prediction for various PDF sets and scale choices for anti-$k_t$ jets with $R = 0.4$ and $R = 0.6$, for several $p_T$ cuts, using all $|y|$ bins. All the corresponding $p$-values are $\ll 10^{-3}$. 
ref. [86] has a similar effect. The quantitative comparison is also not very sensitive to the choice of nominal renormalisation and factorisation scales in the NLO calculations.

A set of $\chi^2$ values were also evaluated for the ABM11 PDF set [87], for $R = 0.4$ and $R = 0.6$, for the $p_T^{jet,\text{max}}$ and $p_T^{jet}$ scale choices, in the full $p_T$ range, for individual $|y|$ bins, as well as all the $|y|$ bins together. In this case, tension between data and the theory prediction is observed even in individual $|y|$ bins, with $P_{\text{obs}}$ values below $10^{-3}$ for both $|y| < 0.5$ and $0.5 \leq |y| < 1.0$. When using all the $|y|$ bins together, the $\chi^2$ is significantly larger than for other PDF sets, by up to 152–232 units compared to the results obtained for CT14.

### 10.3 Quantitative comparison of data to NLO QCD calculations with alternative correlation scenarios

Considering all data points together requires a good understanding of the correlations of the experimental and theoretical systematic uncertainties in jet $p_T$ and rapidity. In the ATLAS JES uncertainty correlation model [50, 51, 56] the correlations of most uncertainties in the jet energy measurement are generally well known.

Where this is not the case, alternative correlation scenarios are provided alongside the default scenario: the “weaker” correlation scenario proposed in ref. [56] was tested, and found to yield $\chi^2$ reductions by up to about 12 units for some phase-space regions.

Correlations of the uncertainties that are based on simple comparisons between two options (two-point systematic uncertainties), e.g. systematic uncertainties due to differences between the fragmentation models in Pythia [30] and Herwig++ [39], are not well defined and therefore different levels of correlations can in principle be used. Concerning the theoretical prediction, the correlations are not well defined for the uncertainty related to the scale variations, the uncertainty related to the alternative scale choice and the uncertainty due to the non-perturbative corrections. For this reason, this analysis investigated in detail the impact of alternative correlation scenarios for the largest sources of two-point experimental uncertainties, as well as for the theoretical uncertainties.

The impact of fully decorrelating (in both $p_T$ and $|y|$) any of those two-point systematic uncertainties was checked. Potentially important effects are observed when fully decorrelating the uncertainty due to the response difference between quark- and gluon-induced jets (JES Flavour Response), the jet fragmentation uncertainty in the multijet balance (JES MJB Fragmentation) and the uncertainty in the density of pile-up activity in a given event ($\rho$) (JES Pile-up Rho topology) (see ref. [56] for more details). However, even if the exact correlations are not known, one must keep in mind that this potential $\chi^2$ reduction is far too optimistic, since some non-negligible level of correlation, in both $p_T$ and $|y|$, is expected for these uncertainties. This motivated some tests using more realistic decorrelation models for these uncertainties. These experimental systematic uncertainties are split into sub-components whose size varies with jet rapidity and $p_T$. While the sub-components are independent of each other, each of them is fully correlated between different phase-space regions and their sum in quadrature equals the original uncertainty. A series of 18 different splitting options into two or three sub-components, with various smooth $p_T$ and $|y|$ dependences, were studied for both $R = 0.4$ and $R = 0.6$, using the CT14 PDF set and the
\( p_T^{\text{jet,max}} \) scale choice. While many of these decorrelation options have little impact on the \( \chi^2 \), some of them induce a \( \chi^2 \) reduction by up to 33 units. When applying various splitting options (the ones yielding the largest \( \chi^2 \) reductions when splitting one single component) to the JES Flavour Response, JES MJB Fragmentation and JES Pile-up Rho topology uncertainties simultaneously, the \( \chi^2 \) is reduced by up to 51 units compared to the nominal JES configuration. For all these variations of the correlations, the corresponding \( P_{\text{obs}} \) values are \( \ll 10^{-3} \).

For the theoretical uncertainties, in addition to the 18 options discussed above, 3 other splitting options based on the ones discussed in ref. [88] were tested. These additional options consist in splitting a given uncertainty component into six sub-components. Many of these decorrelation options have little impact on the \( \chi^2 \), but some of them induce a \( \chi^2 \) reduction by up to 60 units. Still, all the corresponding \( P_{\text{obs}} \) values are \( \ll 10^{-3} \). When applying various splitting options (the ones yielding the largest \( \chi^2 \) reductions when splitting one single component) to the scale variations, the alternative scale choice and the non-perturbative corrections uncertainties simultaneously, the \( \chi^2 \) is reduced by up to 87 units compared to the nominal configuration, but the corresponding \( P_{\text{obs}} \) values are still \( \ll 10^{-3} \).

The various splitting options yielding the largest \( \chi^2 \) reductions when splitting either the experimental or the theoretical uncertainties were applied to both the experimental (JES Flavour Response, the JES MJB Fragmentation, JES Pile-up Rho topology) and theoretical uncertainties (the scale variations, the alternative scale choice and the non-perturbative corrections uncertainties) simultaneously. In this case the \( \chi^2 \) evaluated for CT14 is reduced by up to 96 units compared to the nominal configuration, but the corresponding \( P_{\text{obs}} \) values are still below \( 10^{-3} \). Similar reductions of the \( \chi^2 \) values are observed for NNPDF3.0.

In summary, all the tested JES uncertainty decorrelation scenarios that could be judged as justifiable from the performance point of view yield small \( P_{\text{obs}} \) values. The same is true when using similar decorrelation scenarios for the theoretical uncertainties. When decorrelating the JES uncertainty components and the theoretical uncertainties simultaneously, values of \( \chi^2/\text{ndf} \) down to 256/159 are obtained. Furthermore, it should be noted that for the experimental and theoretical systematic uncertainties that are based on simple comparisons between two options (e.g. the renormalisation and factorisation scale uncertainties), even the notion of a standard deviation (i.e. the size of the uncertainty itself) in different phase-space regions is not well defined. Since, in addition to the correlations, the phase-space dependence of the size of the uncertainties is a key ingredient in the \( \chi^2 \) evaluation, this second aspect may also explain part of the observed tension between the measurement and the theory.

10.4 Comparisons with NLO QCD calculation including parton showers and fragmentation

The comparisons of the Powheg predictions with the measurement for jets with \( R = 0.4 \) and \( R = 0.6 \) are shown in figure 9 and figure 10 as a function of the jet \( p_T \) in bins of the jet rapidity. The measurements are also compared to the NLO QCD prediction
Figure 9. Ratio of the inclusive jet cross-section predicted by the Powheg Monte Carlo event generator with respect to the cross-section in data as a function of the jet $p_T$ in each jet rapidity bin for anti-$k_t$ jets with $R = 0.4$. Only the nominal values of this ratio are indicated. Also shown is the prediction by NLO QCD corrected for non-perturbative effects, where the error bars indicate the total theory uncertainty. Electroweak corrections are applied for both theory predictions and the CT10 PDF set is used. The points are offset in jet $p_T$ for better visibility. The grey band shows the total uncertainty in the measurement.

using the CT10 PDF set and corrected for non-perturbative effects with the same MC generator configuration as was used for Powheg. Electroweak corrections are also applied in both cases.

For anti-$k_t$ jets with $R = 0.4$ the Powheg prediction is lower than the one from fixed-order NLO QCD corrected for non-perturbative effects. This difference increases towards high-$p_T$ and decreases with jet rapidity. In the most forward rapidity region the two predictions are similar. For anti-$k_t$ jets with $R = 0.6$ the Powheg prediction is higher than the fixed-order NLO QCD prediction at low $p_T$ and lower at high $p_T$. In the most forward rapidity region the two predictions are similar.

The ratio of the Powheg prediction to data is less dependent on the jet radius than the same ratio using the fixed-order NLO QCD prediction corrected for non-perturbative effects. The theory to data ratio for anti-$k_t$ jets with $R = 0.6$ and the same ratio for anti-$k_t$ jets with $R = 0.4$ is unity within 5% for all jet $p_T$ and rapidities while the fixed-order calculation shows deviations of up to 15% for low $p_T$ jets in the central region. This indicates the importance of parton shower effects in correctly describing the jet radius dependence.
Figure 10. Ratio of the inclusive jet cross-section predicted by the Powheg Monte Carlo event generator with respect to the cross-section in data as a function of the jet $p_T$ in each jet rapidity bin for anti-$k_t$ jets with $R = 0.6$. Only the nominal values of this ratio are indicated. Also shown is the prediction by NLO QCD corrected for non-perturbative effects, where the error bars indicate the total theory uncertainty. Electroweak corrections are applied for both theory predictions and the CT10 PDF set is used. The points are offset in jet $p_T$ for better visibility. The grey band shows the total uncertainty in the measurement.

11 Conclusion

The double-differential inclusive jet cross-sections in proton-proton collisions at $\sqrt{s} = 8$ TeV are measured for jets reconstructed with the anti-$k_t$ algorithm with jet radius parameter values of $R = 0.4$ and $R = 0.6$ in the kinematic region of the jet transverse momentum from $p_T = 70$ GeV to about 2.5 TeV and jet rapidities $|y| < 3$. The measurement is based on the data collected with the ATLAS detector during LHC operation in 2012, corresponding to an integrated luminosity of 20.2 fb$^{-1}$. The cross-sections are measured double-differentially in the jet transverse momentum and rapidity.

The dominant systematic uncertainty arises from the jet energy calibration. Compared to previous jet cross-section measurements a significant reduction of the uncertainties is achieved.

The publication of all observed results, including uncertainties and correlations, in the Durham HEP database allows further quantitative comparisons of data and theory. A quantitative comparison of the measurement to fixed-order NLO QCD calculations, corrected for non-perturbative and electroweak effects, shows overall fair agreement (with $p$-values in the percent range) when considering jet cross-sections in individual jet rapidity bins treated independently. Some tension between data and theory is observed in the central rapidity region for anti-$k_t$ jets with $R = 0.6$. Strong tension between data and
theory is observed when considering data points from all jet transverse momentum and rapidity regions, with a full treatment of the correlations. This tension can be reduced, but not completely resolved, using alternative correlation scenarios for the experimental and theoretical two-point systematic uncertainties. The remaining tension could be due either to the breakdown of the assumptions that need to be made in the treatment of two-point systematic uncertainty components, or to an incomplete theoretical description, such as missing higher-order corrections.

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We honour the memory of our colleague Hrachya Hakobyan, who made a large contribution to this work, but died before its completion.

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A Quantitative comparison of data to NLO QCD calculations with alternate correlation scenarios

Alternative correlation scenarios for experimental and theoretical uncertainties

In order to test in a realistic way the sensitivity of the results to the correlations for two-point systematic uncertainties, 18 different options for splitting into sub-components (see table 4) were studied for experimental and theoretical uncertainties. The options 1–12 (13–18) correspond to a splitting into two (three) sub-components, of which one (two) are explicitly listed in table 4. An extra (complementary) sub-component completes them, such that the sum in quadrature of all the sub-components in each splitting option equals the original uncertainty. These sub-components are defined as fractions of the original uncertainty. The actual fractions are functions with various $p_T$ and $|y|$ dependences. They depend only on $p_T$ for options 1–6, only on $|y|$ for options 7–8 and on both $p_T$ and $|y|$ for the other options. The functions used for the splitting are defined using the linear function $L(x, \min, \max) = (x - \min)/(\max - \min)$, for $x$ in the range $[\min, \max]$. This function is set to $L(x, \min, \max) = 0$ for $x < \min$ and to $L(x, \min, \max) = 1$ for $x > \max$ respectively. For options 2, 4, 6, 11 and 12, the factor 0.5 included for the listed component induces a reduction of its size, hence the enhancement of the complementary component.

Three additional splitting options (19–21), based on the ones discussed in ref. [88], were tested for the theoretical uncertainties. These options consist in splitting a given uncertainty component into six sub-components, with the following $p_T$ and $y$ dependencies indicated in eq. (A.1):

$$
f_1(p_T, y) = C(p_T, y) \cdot c_1 / \log (M(y)/p_T),$$
$$f_2(p_T, y) = C(p_T, y) \cdot c_2 \cdot y^2 / \log (M(y)/p_T),$$
$$f_3(p_T, y) = C(p_T, y) \cdot c_3,$$
$$f_4(p_T, y) = C(p_T, y) \cdot c_4 \cdot y^2,$$
$$f_5(p_T, y) = C(p_T, y) \cdot c_5 \cdot \log (15p_T/M(y)),$$
$$f_6(p_T, y) = C(p_T, y) \cdot c_6 \cdot y^2 \cdot \log (15p_T/M(y)), $$

where $M(y) = \sqrt{s} \cdot e^{-y}$. The coefficients ($c_1$–$c_6$) are (4.56, 1.24, 5.36, 0.536, 1.07, 0.214) for option 19, (9.62, 2.89, 8.42, 0.842, 1.68, 0.336) for option 20 and (5.0, 1.5, 5.7, 0.57, 1.15, 0.24) for option 21 respectively. The normalisation coefficient $C(p_T, y)$ is adjusted in each bin, such that the sum in quadrature of the 6 components is equal to the original uncertainty that is split.

When studying the correlations of the uncertainty related to the scale variations, this uncertainty is first split into three independent sub-components, matching the variation factors of the (renormalisation; factorisation) scales, for the “Up” and “Down” components, as follows: (Up (0.5; 0.5), Down (2; 2)), (Up (0.5; 1), Down (2; 1)) and (Up (1; 0.5),

\footnote{A 7th component is described in ref. [88], corresponding to the uncertainty associated with the non-perturbative correction. The present analysis does not include this 7th component in these splitting options, since the non-perturbative uncertainty is treated differently in our study.}
The sub-component(s) definition(s), completed by complementary splitting either the experimental or the theoretical uncertainties.

These three sub-components are then further decorrelated using one of the 21 splitting options discussed above.

For some component(s) the “Up” and the “Down” variations have the same sign. These matching options allow minimisation of the phase space reduction equals the original uncertainty.

An extra (complementary) sub-component is defined in the table, as fractions of the original uncertainty. An extra (complementary) sub-component two (first 12 options) or three (last 6 options) sub-components. One or two sub-components are defined in the table, as fractions of the original uncertainty. An extra (complementary) sub-component.

Table 4. Summary of the 18 options for splitting the two-point systematic uncertainties into two (first 12 options) or three (last 6 options) sub-components. One or two sub-components are defined in the table, as fractions of the original uncertainty. An extra (complementary) sub-component.

<table>
<thead>
<tr>
<th>Splitting option</th>
<th>Sub-component(s) definition(s), completed by complementary splitting</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>$L(\ln(p_T[TeV]), \ln(0.1), \ln(2.5))$ - uncertainty</td>
</tr>
<tr>
<td>2</td>
<td>$L(\ln(p_T[TeV]), \ln(0.1), \ln(2.5)) \cdot 0.5$ - uncertainty</td>
</tr>
<tr>
<td>3</td>
<td>$L(p_T[TeV], 0.1, 2.5)$ - uncertainty</td>
</tr>
<tr>
<td>4</td>
<td>$L(p_T[TeV], 0.1, 2.5) \cdot 0.5$ - uncertainty</td>
</tr>
<tr>
<td>5</td>
<td>$L((\ln(p_T[TeV]))^2, (\ln(0.1))^2, (\ln(2.5))^2)$ - uncertainty</td>
</tr>
<tr>
<td>6</td>
<td>$L((\ln(p_T[TeV]))^2, (\ln(0.1))^2, (\ln(2.5))^2) \cdot 0.5$ - uncertainty</td>
</tr>
<tr>
<td>7</td>
<td>$L(</td>
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<td>8</td>
<td>$L(</td>
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<tr>
<td>9</td>
<td>$L(\ln(p_T[TeV]), \ln(0.1), \ln(2.5)) \cdot L(</td>
</tr>
<tr>
<td>10</td>
<td>$L(\ln(p_T[TeV]), \ln(0.1), \ln(2.5)) \cdot \sqrt{1 - L(</td>
</tr>
<tr>
<td>11</td>
<td>$L(\ln(p_T[TeV]), \ln(0.1), \ln(2.5)) \cdot L(</td>
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<td>12</td>
<td>$L(\ln(p_T[TeV]), \ln(0.1), \ln(2.5)) \cdot \sqrt{1 - L(</td>
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<td>17</td>
<td>$L(\ln(p_T[TeV]), \ln(0.1), \ln(2.5)) \cdot \sqrt{1 - L(</td>
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<tr>
<td>18</td>
<td>$L(\ln(p_T[TeV]), \ln(0.1), \ln(2.5)) \cdot \sqrt{1 - L(</td>
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</tbody>
</table>

Down (1; 2) respectively. These matching options allow minimisation of the phase space where for some component(s) the “Up” and the “Down” variations have the same sign. These three sub-components are then further decorrelated using one of the 21 splitting options discussed above.

Tables 5 and 6 show the $\chi^2$ obtained when applying various splitting options to both the experimental (JES Flavour Response, the JES MJB Fragmentation, JES Pile-up Rho

3The splitting options shown here are restricted to the ones yielding the largest $\chi^2$ reductions when splitting either the experimental or the theoretical uncertainties.
### Table 5

Summary of $\chi^2$/ndf obtained from the comparison of the inclusive jet cross-section and the NLO QCD prediction for the CT14 and the NNPDF3.0 PDF sets and the $p_{T,jet,\max}$ scale choice for anti-$k_t$ jets with $R = 0.4$, for $p_T > 100$ GeV and various de-correlation options (see text) of the JES Flavour Response, the JES MJB Fragmentation, JES Pile-up Rho topology, the uncertainty related to the scale variations, the uncertainty related to the alternative scale choice and the uncertainty related to the non-perturbative corrections. All the $p$-values corresponding to the $\chi^2$/ndf in the table are $\ll 10^{-3}$.

<table>
<thead>
<tr>
<th>Splitting options for $R = 0.4$</th>
<th>CT14</th>
<th>NNPDF3.0</th>
</tr>
</thead>
<tbody>
<tr>
<td>JES Flavour Response Opt 7</td>
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<tr>
<td>JES MJB Fragmentation Opt 17</td>
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<tr>
<td>JES Pile-up Rho topology Opt 18</td>
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<tr>
<td>Scale variations Opt 17</td>
<td></td>
<td></td>
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<tr>
<td>Alternative scale choice Opt 7</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Non-perturbative corrections Opt 7</td>
<td>268/159</td>
<td>257/159</td>
</tr>
<tr>
<td>JES Flavour Response Opt 7</td>
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<tr>
<td>JES MJB Fragmentation Opt 17</td>
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<td>JES Pile-up Rho topology Opt 18</td>
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<tr>
<td>Scale variations Opt 20</td>
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<tr>
<td>Alternative scale choice Opt 17</td>
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<tr>
<td>Non-perturbative corrections Opt 17</td>
<td>261/159</td>
<td>260/159</td>
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### Table 6

Summary of $\chi^2$/ndf obtained from the comparison of the inclusive jet cross-section and the NLO QCD prediction for the CT14 and the NNPDF3.0 PDF sets and the $p_{T,jet,\max}$ scale choice for anti-$k_t$ jets with $R = 0.4$, for $p_T > 100$ GeV and various de-correlation options (see text) of the JES Flavour Response, the JES MJB Fragmentation, JES Pile-up Rho topology, the uncertainty related to the scale variations, the uncertainty related to the alternative scale choice and the uncertainty related to the non-perturbative corrections. All the $p$-values corresponding to the $\chi^2$/ndf in the table are $\ll 10^{-3}$.

<table>
<thead>
<tr>
<th>Splitting options for $R = 0.6$</th>
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<th>NNPDF3.0</th>
</tr>
</thead>
<tbody>
<tr>
<td>JES Flavour Response Opt 14</td>
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<tr>
<td>JES MJB Fragmentation Opt 17</td>
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<td>JES Pile-up Rho topology Opt 16</td>
<td></td>
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<tr>
<td>Scale variations Opt 17</td>
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<tr>
<td>Alternative scale choice Opt 16</td>
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<tr>
<td>Non-perturbative corrections Opt 18</td>
<td>266/159</td>
<td>258/159</td>
</tr>
<tr>
<td>JES Flavour Response Opt 7</td>
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<tr>
<td>JES MJB Fragmentation Opt 17</td>
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<td>JES Pile-up Rho topology Opt 16</td>
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<td>Alternative scale choice Opt 16</td>
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<tr>
<td>Non-perturbative corrections Opt 18</td>
<td>264/159</td>
<td>256/159</td>
</tr>
</tbody>
</table>

(topology) and theoretical uncertainties (the scale variations, the alternative scale choice and the non-perturbative corrections uncertainties) simultaneously. Results are shown for both the CT14 and the NNPDF3.0 pdf sets.
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[27] ATLAS collaboration, The ATLAS Experiment at the CERN Large Hadron Collider, 2008 JINST 3 S08003 [nSPIRE].


[84] A complete set of tables with the full results are available at the Durham HepData repository, https://hepdata.net.


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<table>
<thead>
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<th>Page</th>
<th>Institution</th>
<th>Location</th>
</tr>
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<td>56</td>
<td>SUPA - School of Physics and Astronomy, University of Glasgow, Glasgow, U.K.</td>
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<td>57</td>
<td>II Physikalisches Institut, Georg-August-Universität, Göttingen, Germany</td>
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<td>58</td>
<td>Laboratoire de Physique Subatomique et de Cosmologie, Université Grenoble-Alpes, CNRS/IN2P3, Grenoble, France</td>
<td>Grenoble, France</td>
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<td>60</td>
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