Search for charginos and neutralinos in final states with two boosted hadronically decaying bosons and missing transverse momentum in pp collisions at $\sqrt{s} = 13$ TeV with the ATLAS detector

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Search for charginos and neutralinos in final states with two boosted hadronically decaying bosons and missing transverse momentum in \( pp \) collisions at \( \sqrt{s} = 13 \) TeV with the ATLAS detector

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A search for charginos and neutralinos at the Large Hadron Collider using fully hadronic final states and missing transverse momentum is reported. Pair-produced charginos or neutralinos are explored, each decaying into a high-\( p_T \) Standard Model weak boson. Fully hadronic final states are studied to exploit the advantage of the large branching ratio, and the efficient rejection of backgrounds by identifying the high-\( p_T \) bosons using large-radius jets and jet substructure information. An integrated luminosity of 139 fb\(^{-1}\) of proton-proton collision data collected by the ATLAS detector at a center-of-mass energy of 13 TeV is used. No significant excess is found beyond the Standard Model expectation. Exclusion limits at the 95% confidence level are set on wino or higgsino production with various assumptions about the decay branching ratios and the type of lightest supersymmetric particle. A wino (higgsino) mass up to 1060 (900) GeV is excluded when the lightest supersymmetry particle mass is below 400 (240) GeV and the mass splitting is larger than 400 (450) GeV. The sensitivity to high-mass winos and higgsinos is significantly extended relative to previous LHC searches using other final states.

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I. INTRODUCTION

Supersymmetry (SUSY) [1–6] is a theoretical framework that extends the Standard Model (SM) by introducing new particles (“superpartners”) that have the same quantum numbers as the SM particles except for their spins. In the Minimal Supersymmetric Standard Model (MSSM) [7,8], the bino (\( \tilde{B} \)), wino (\( \tilde{W} \)) and higgsino (\( \tilde{H} \)) are the superpartners of the U(1)\(_Y\) and SU(2) gauge fields and the Higgs field, respectively. These are collectively referred to as “electroweakinos” and form the chargino (\( \tilde{\chi}^\pm_1, \tilde{\chi}^\pm_2 \)) and neutralino (\( \tilde{\chi}_1^0, \tilde{\chi}_2^0, \tilde{\chi}_3^0, \tilde{\chi}_4^0 \)) mass eigenstates through mixing, with the subscripts indicating increasing mass. The lightest neutralino (\( \tilde{\chi}_1^0 \)) is often considered to be the lightest SUSY particle (LSP), since it is then a viable candidate for weakly interacting massive particle dark matter [9,10] when R-parity conservation is assumed [11]. Depending on the signal model, the superpartner of the graviton (gravitino, \( \tilde{G} \)) and the axion (axino, \( \tilde{a} \)) are alternatively considered to be the LSP and dark matter candidate in this search.

Electroweakinos with masses of the order of 0.1–1 TeV are motivated by various phenomenological arguments: (1) the mass of the neutralino LSP dark matter candidate is constrained to be less than a few TeV by the observed relic density [12,13]; (2) the higgsino mass is also motivated to be of the same order as the Z boson mass by naturalness arguments [14–17]; (3) the MSSM parameter space explaining the discrepancy between the measured muon anomalous magnetic moment [18] and its SM predictions [19] tends to include electroweakinos with masses from 200 GeV to 1 TeV [20–22].

This search targets the pair production of electroweakinos (\( \tilde{\chi}_\text{heavy} \)), where each of them decays into a lighter one (\( \tilde{\chi}_\text{light} \)) and an on-shell \( W, Z \) or SM Higgs boson (\( h \)). A mass splitting \( \Delta m(\tilde{\chi}_\text{heavy}, \tilde{\chi}_\text{light}) \) greater than 400 GeV is considered in the search. The \( \tilde{\chi}_\text{heavy} \) can be either wino- or higgsinolike, and \( \tilde{\chi}_\text{light} \) can be a bino-, wino-, higgsinolike chargino/neutralino, gravitino, or axino as discussed more in Sec. II. Cases where both \( \tilde{\chi}_\text{heavy} \) and \( \tilde{\chi}_\text{light} \) are wino- or higgsinolike are not considered as they lead to very small \( \Delta m(\tilde{\chi}_\text{heavy}, \tilde{\chi}_\text{light}) \). The \( \tilde{\chi}_\text{light} \) is either the LSP or an electroweakino nearly degenerate with it, leading to missing transverse momentum (\( \vec{p}_T^{\text{miss}} \)) with magnitude \( E_T^{\text{miss}} \) in the decay signature.\(^1\)

\(^1\)In the regime of large mass splitting, the effect of chargino/neutralino mixing is highly suppressed so that the gauge eigenstates (e.g., bino) and the mass eigenstates (e.g., bino-like \( \tilde{\chi}_1^0 \)) can be regarded as almost identical. Therefore, this paper does not make the distinction and “electroweakinos” are defined to represent both unless explicitly stated otherwise.
The analysis focuses on the hadronic decay modes of the $W$, $Z$, and $h$ bosons, namely $W \rightarrow q\bar{q}$, $Z \rightarrow q\bar{q}/b\bar{b}$ and $h \rightarrow b\bar{b}$, where $q$ ($\bar{q}$) represents light-flavor (anti)quarks $u$, $d$, $s$, $c$ ($\bar{u}$, $\bar{d}$, $\bar{s}$, $\bar{c}$). Two fully hadronic final states are considered: the $qqqq$ final state which involves two $W/Z$ bosons decaying into two light-flavor (anti)quarks, and the $bbqq$ final state where a $W/Z$ boson decays into two light-flavor (anti)quarks and a $Z/h$ boson decays into $b\bar{b}$, as illustrated by the diagrams in Fig. 1. While the ATLAS and CMS experiments have typically searched for pair production of electroweakinos using leptonic decay modes [23–36], the fully hadronic final states are used here to take advantage of the larger $W$, $Z$, and $h$ hadronic branching ratios, and thereby provide sensitivity to the production of heavier electroweakinos, despite their smaller production cross sections. Final states with four $b$ quarks are not considered in this search; however, they are targeted by dedicated searches [37,38] complementing the sensitivity.

The multijet background is highly suppressed by requiring large $E_T^{miss}$, and the dominant backgrounds in the analysis are $Z(\rightarrow \nu\bar{\nu}) +$ jets, $W(\rightarrow \ell\nu) +$ jets, and diboson production. These can be effectively suppressed when targeting large mass splittings between the produced electroweakinos and the LSP by selecting high-$p_T$ kinematics and explicitly reconstructing the two boosted SM bosons. The “boson tagging” technique developed by the ATLAS and CMS experiments [39–42] is employed, where a single large-radius jet is used to capture the two collimated energetic jets from each boosted SM boson decay. Analysis of the jet substructure helps to identify the hadronic decays of $W$, $Z$, and $h$. The introduction of this technique significantly improves upon the previously fully hadronic final-state analysis in ATLAS targeting the $bbqq$

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{fig1}
\caption{Diagrams for the targeted signatures and final states.}
\end{figure}

In this paper the symbols $q$ ($b$) represent both (bottom) quarks and (bottom) antiquarks unless explicitly stated otherwise, since they are not distinguished in the search. In addition, charm quarks and antiquarks are treated as light-flavor quarks and antiquarks in the analysis.

The contributions from signals with two $h$ bosons are included in the signal models although not targeted. Likewise, all the decays of $W$, $Z$, and $h$ are taken into account for the signals.

The analysis uses proton-proton collision data collected by the ATLAS detector in the years 2015–2018 at a center-of-mass energy of $\sqrt{s} = 13$ TeV, corresponding to an integrated luminosity of $139$ fb$^{-1}$. The results are interpreted in terms of various models with different electroweakino types for ($\tilde{\chi}_\text{heavy}$, $\tilde{\chi}_\text{light}$) and their branching ratio assumptions. While each model predicts different electroweakino branching ratios into $W$, $Z$, or $h$, the search combines the dedicated event selections for each decay to achieve only a small model dependency.

II. TARGET PHYSICS SCENARIOS AND THE SIGNAL MODELS

Three physics scenarios are considered in the analysis:

(i) a baseline MSSM scenario where bino, wino and higgsino are considered as $\tilde{\chi}_\text{heavy}$ or $\tilde{\chi}_\text{light}$;

(ii) a scenario with a gravitino LSP and light higgsinos inspired by the general gauge mediation (GGM) [43–47] models and naturalness;

(iii) a scenario with an axino LSP assuming the SM extension with a QCD axion and light higgsinos driven by naturalness.

The signal models considered in the analysis, derived from each physics scenario, are described in the following subsections. Each model is labeled as $(A, B)$, where $A$ and $B$ represent the dominant component of $\tilde{\chi}_\text{heavy}$ and $\tilde{\chi}_\text{light}$, respectively. All the SUSY particles other than $\tilde{\chi}_\text{heavy}$ and $\tilde{\chi}_\text{light}$ are assumed to be decoupled in mass [48,49]. The production modes, final states, and the branching ratio assumptions for $\tilde{\chi}_\text{heavy}$ are summarized in Table I.

The winolike states form a doublet consisting of one chargino and one neutralino, while the higgsino-like triplet includes an additional neutralino. The mass degeneracy within these wino/higgsino multiplets is dictated by the extent of mixing with the other electroweakino states, which is characterized by $\Delta m(\tilde{\chi}_\text{heavy}, \tilde{\chi}_\text{light})$. With $\Delta m(\tilde{\chi}_\text{heavy}, \tilde{\chi}_\text{light}) > 400$ GeV, the mass splittings within
The (\( \tilde{W}, \tilde{B} \)) and \( (\tilde{H}, \tilde{G}) \) models are used to optimize the selection, and the rest are considered in the interpretation. The (\( \tilde{W}, \tilde{B} \)) simplified models \((\tilde{W}, \tilde{B})\)-SIM discussed in Sec. IV B 2 are also interpreted in order to allow comparisons with the ATLAS electroweakino search results [23–25,29,68].

### Table I

<table>
<thead>
<tr>
<th>Model</th>
<th>Production</th>
<th>Final states</th>
<th>SRs simultaneously fitted</th>
<th>Branching ratio</th>
</tr>
</thead>
<tbody>
<tr>
<td>( (\tilde{W}, \tilde{B}) )</td>
<td>( \tilde{\chi}^{±}_1 \tilde{\chi}^0_1, \tilde{\chi}^{±}_1 \tilde{\chi}^0_2 )</td>
<td>WW, WZ, Wh</td>
<td>4Q-VV, 2B2Q-WZ, 2B2Q-Wh</td>
<td>( B(\tilde{\chi}^+_1 \rightarrow W\tilde{\chi}^0_1) = 1 )</td>
</tr>
<tr>
<td>( (\tilde{H}, \tilde{B}) )</td>
<td>( \tilde{\chi}^{±}_1 \tilde{\chi}^0_1, \tilde{\chi}^{±}_2 \tilde{\chi}^0_3 )</td>
<td>WW, WZ, Wh, ZZ, Zh, hh</td>
<td>4Q-VV, 2B2Q-VZ, 2B2Q-Vh</td>
<td>( B(\tilde{\chi}^+_1 \rightarrow W\tilde{\chi}^0_1) = 1 )</td>
</tr>
<tr>
<td>( (\tilde{W}, \tilde{H}) )</td>
<td>( \tilde{\chi}^{±}_1 \tilde{\chi}^0_1, \tilde{\chi}^{±}_1 \tilde{\chi}^0_2, \tilde{\chi}^{±}_2 \tilde{\chi}^0_3 )</td>
<td>WW, WZ, Wh, ZZ, Zh, hh</td>
<td>4Q-VV, 2B2Q-VZ, 2B2Q-Vh</td>
<td>( B(\tilde{\chi}^+_1 \rightarrow W\tilde{\chi}^0_1) = 1 )</td>
</tr>
<tr>
<td>( (\tilde{H}, \tilde{W}) )</td>
<td>( \tilde{\chi}^{±}_1 \tilde{\chi}^0_1, \tilde{\chi}^{±}_1 \tilde{\chi}^0_2, \tilde{\chi}^{±}_2 \tilde{\chi}^0_3 )</td>
<td>ZZ, Zh, hh</td>
<td>4Q-VV, 2B2Q-VZ, 2B2Q-Vh</td>
<td>Determined from ( (M_2, \mu, \tan \beta) )</td>
</tr>
<tr>
<td>( (\tilde{H}, \tilde{G}) )</td>
<td>( \tilde{\chi}^{±}_1 \tilde{\chi}^0_1, \tilde{\chi}^{±}_1 \tilde{\chi}^0_2, \tilde{\chi}^{±}_2 \tilde{\chi}^0_3 )</td>
<td>ZZ, Zh, hh</td>
<td>4Q-VV, 2B2Q-VZ, 2B2Q-Vh</td>
<td>Determined from ( (M_2, \mu, \tan \beta) )</td>
</tr>
<tr>
<td>( (\tilde{H}, \tilde{a}) )</td>
<td>( \tilde{\chi}^{±}_1 \tilde{\chi}^0_1, \tilde{\chi}^{±}_1 \tilde{\chi}^0_2, \tilde{\chi}^{±}_2 \tilde{\chi}^0_3 )</td>
<td>ZZ, Zh, hh</td>
<td>4Q-VV, 2B2Q-VZ, 2B2Q-Vh</td>
<td>( B(\tilde{\chi}^+_1 \rightarrow Z\tilde{\chi}^0_1) = 1 )</td>
</tr>
</tbody>
</table>

The (\( \tilde{W}, \tilde{H} \)), \( (\tilde{H}, \tilde{B}) \), and \( (\tilde{H}, \tilde{W}) \) hierarchies are typically predicted by the MSSM parameter space that explains the muon \( g - 2 \) anomaly with loop contributions including a wino and/or higgsino.\(^5\) The \( (\tilde{H}, \tilde{B}) \) hierarchy is additionally motivated when the mass of a binolike LSP is half of the \( Z \) or \( h \) boson mass, where the LSP dark matter can annihilate via the \( Z/h \) resonance (“\( Z/h \)-funnel” dark matter). This is a special case of well-tempered neutralino dark matter where a large higgsino-bino mass splitting is favored in order to realize the observed relic density [50–58].

A signal model is defined for each of the four hierarchies with a set of assumptions described below. The mass spectra, corresponding mass eigenstates, and the decays considered are illustrated for each model in Fig. 2. A \( W \) boson is generated when a chargino decays into a neutralino or vice versa; a \( Z \) or \( h \) boson is emitted when a chargino decays into a chargino, or a neutralino decays into a neutralino.

The production modes considered in each model are shown in Table I. Processes involving chargino-chargino or chargino-neutralino pair production are taken into account in the wino production models: \( (\tilde{W}, \tilde{B}) \) and \( (\tilde{W}, \tilde{H}) \); and

---

\(^4\)A mass splitting of 1 GeV is used to avoid potential technical issues when setting it exactly to zero. This choice is arbitrary and has no impact on the analysis.

\(^5\)In this case, smuons and muon sneutrinos need to be only mildly decoupled in mass.
neutralino-neutralino production is additionally included for the higgsino production models: \( \tilde{H}, \tilde{B} \) and \( \tilde{W}, \tilde{B} \). It should be noted that neutralino pairs can only be produced via a \( t \)-channel exchange of squarks, which is prohibited when squarks are assumed to be decoupled.

The branching ratios of \( \tilde{\chi}_{\text{heavy}} \) are treated as follows. In the \( \tilde{W}, \tilde{B} \) and \( \tilde{H}, \tilde{B} \) models, the produced chargino \( \tilde{\chi}^\pm_1 \) decays with 100% probability into the bino LSP \( \tilde{\chi}^0_1 \) and a \( W \) boson. Meanwhile, the produced neutralino(s) can decay either into \( Z \) or into \( h \). Given the complicated model dependency, the branching ratio of the second lightest neutralino \( \tilde{\chi}^0_2 \) is treated as a free parameter, and \( B(\tilde{\chi}^0_2 \rightarrow Z\tilde{\chi}^0_1) = 1 - B(\tilde{\chi}^0_2 \rightarrow h\tilde{\chi}^0_1) \) is scanned over 0, 25, 50, 75, and 100% in both models. For the \( \tilde{H}, \tilde{B} \) model, the branching ratios of the heavy neutral higgsino \( \tilde{\chi}^0_2 \) are fixed relative to those of the light neutral higgsino \( \tilde{\chi}^0_1 \) via

\[
\begin{align*}
&\text{(i)} \quad B(\tilde{\chi}^0_2 \rightarrow Z\tilde{\chi}^0_1) + B(\tilde{\chi}^0_2 \rightarrow Z\tilde{\chi}^0_2) = 1, \\
&\text{(ii)} \quad B(\tilde{\chi}^0_2 \rightarrow h\tilde{\chi}^0_1) + B(\tilde{\chi}^0_2 \rightarrow h\tilde{\chi}^0_2) = 1.
\end{align*}
\]

These provide a good approximation when \( \Delta m(\tilde{\chi}_{\text{heavy}}, \tilde{\chi}_{\text{light}}) \) is significantly larger than \( m_h \) [59].

In \( \tilde{W}, \tilde{H} \) and \( \tilde{H}, \tilde{W} \) models, however, the branching ratios of the produced chargino and neutralino(s) are largely dictated by the three MSSM parameters: the wino mass parameter \( M_2 \), the higgsino mass parameter \( \mu \), and the ratio of vacuum expectation values of the two Higgs fields, \( \tan\beta \). For a given set of \( (M_2, \mu, \tan\beta) \), the branching ratios are coherently used according to SOFTSUSY 4.1.7 [60,61], with all the SUSY mass parameters except for \( M_2 \) and \( \mu \) being set as decoupled. The signal models are tested using various combinations of \( (M_2, \mu, \tan\beta) \) where \( M_2 \in [0, 1.2] \) TeV, \( \mu \in [-1.2, 1.2] \) TeV, and \( \tan\beta = 2, 5, 10, 30 \) are considered.

The vast majority of the previous electroweakino searches at the LHC have targeted the simplified \( \tilde{W}, \tilde{B} \) model, where only a specific production channel and decay mode are considered (detailed in Sec. IV B 2). For \( \tilde{\chi}^\pm_1 \tilde{\chi}^0_1 \) production with decays into \( WW \), \( m(\tilde{\chi}^\pm_1) \) < 400 GeV is excluded for \( m(\tilde{\chi}^0_1) < 200 \) GeV [23,31]. For \( \tilde{\chi}^\pm_1 \tilde{\chi}^0_2 \) production, \( m(\tilde{\chi}^\pm_1/\tilde{\chi}^0_2) < 640 \) GeV is excluded for \( m(\tilde{\chi}^0_1) < 300 \) GeV when \( \tilde{\chi}^0_2 \) is assumed to decay into \( Z \) and \( \tilde{\chi}^0_1 \) with 100% probability [24–26,32,33]. Alternatively, \( m(\tilde{\chi}^\pm_1/\tilde{\chi}^0_2) < 740 \) GeV is excluded for \( m(\tilde{\chi}^0_1) < 250 \) GeV [27–29,34–36] when the \( \tilde{\chi}^0_2 \) decays solely into \( h \) and \( \tilde{\chi}^0_1 \).

B. GGM/naturalness-driven gravitino LSP model: \( \tilde{H}, \tilde{G} \)

GGM, a class of SUSY-breaking scenarios characterized by a messenger sector to which only SM gauge bosons can couple, typically predicts a nearly massless gravitino \( \tilde{G} \) as the LSP. Motivated also by the naturalness argument, the production of a relatively light higgsino triplet \( (\tilde{\chi}^\pm_1, \tilde{\chi}^0_1, \tilde{\chi}^0_2) \) decaying into a gravitino LSP has been explored at ATLAS [30,37] and CMS [33], as illustrated in Fig. 3(a). All of the four production modes are considered together: \( \tilde{\chi}^\pm_1 \tilde{\chi}^\pm_1, \tilde{\chi}^\pm_1 \tilde{\chi}^0_2, \tilde{\chi}^0_1 \tilde{\chi}^\pm_1, \tilde{\chi}^0_1 \tilde{\chi}^0_2 \). A moderately small higgsino-gravitino coupling is considered in this analysis, where the produced heavy higgsinos \( \tilde{\chi}^\pm_1/\tilde{\chi}^0_2 \) always decay into a gravitino via...
the lightest neutral higgsino (χ$_0^0$), while the χ$_1^0$ still has a short enough lifetime to be regarded as decaying promptly. In this model, the χ$_1^0$ decays into a gravitino and either a Z or h boson, where the branching ratio $B(χ_1^0 → ZG)(=1 − B(χ_1^0 → hG))$ is treated as a free parameter and scanned in the limit setting. The previous searches have excluded masses of χ$_1^0$ lighter than 650–880 GeV depending on the branching ratio [30,33,37].

C. Naturalness-driven axino LSP model: ($H, ̄a$)

While the QCD Lagrangian generally allows for CP violation, the absence of such observation suggests a highly unnatural tuning of the parameters in the theory, referred to as the “strong CP problem.” The Peccei-Quinn mechanism aims to solve this problem by introducing an additional chiral U(1) symmetry [62]. Through its spontaneous symmetry breaking, the CP-violating term vanishes dynamically, leaving a Nambu-Goldstone boson known as the axion [63,64]. In the SUSY extension, the axino is introduced as the superpartner of the axion. A model symmetry breaking, the chiral U(1) symmetry [62]. Through its spontaneous symmetry breaking, the CP-violating term vanishes dynamically, leaving a Nambu-Goldstone boson known as the axion [63,64]. In the SUSY extension, the axino is introduced as the superpartner of the axion. A model including a light higgsino triplet (χ$_1^+$, χ$_0^0$, χ$_1^-$) decaying into an axino LSP [65] is proposed in the spirit of pursuing naturalness as well as axion/axino dark matter [66,67] under R-parity conservation.

A diagram of the model is shown in Fig. 3(b). Higgsinos are produced by each of the four modes: $χ_{1/2}^0, χ_{3/2}^0, χ_{1/2}^±, χ_{3/2}^±$. The produced heavier higgsinos ($χ_1^±, χ_2^±, χ_3^±$) are assumed to always decay into the axino via the lightest natural higgsino (χ$_1^0$). This is typically valid when the wino and bino are reasonably decoupled so as to maintain approximate mass degeneracy of the higgsino triplet, and when the conventionally motivated range of the axion coupling constant is assumed [65]. A prompt χ$_1^0$ decay into an axino and a Z or h boson is considered in the search. The value of the branching ratio $B(χ_1^0 → Za)(=1 − B(χ_1^0 → h̄a))$ is scanned over 10, 50, 75, and 90% in the interpretation. The model is similar to ($H, ̄G$), except that the LSP can be massive.

III. ATLAS DETECTOR

The ATLAS experiment [69,70] is a multipurpose detector with a forward-backward symmetric cylindrical geometry and nearly 4π coverage in solid angle.8 It consists of an inner tracking detector surrounded by a thin superconducting solenoid providing a 2-T axial magnetic field, electromagnetic and hadron calorimeters, and a muon spectrometer.

The inner detector (ID) consists of pixel and microstrip silicon detectors covering the pseudorapidity range $|η| < 2.5$ and a transition radiation tracker covering $|η| < 2.0$. Outside the ID, a lead/liquid-argon (LAr) electromagnetic calorimeter (ECAL) and a steel/scintillator-tile hadronic calorimeter cover the $|η| < 3.2$ and $|η| < 1.7$ ranges, respectively. In the forward regions, a copper/LAr end-cap calorimeter extends the coverage of hadronic measurements to $1.7 < |η| < 3.2$, while copper/LAr and tungsten/LAr forward calorimeters are employed for electromagnetic and hadronic measurements in the $3.1 < |η| < 4.9$ region. The muon spectrometer (MS) surrounds the calorimeters and comprises three layers of trigger and high-precision tracking chambers spanning $|η| < 2.4$ and $|η| < 2.7$, respectively. A magnetic field is provided by a system of three superconducting air-core toroidal magnets with eight coils each. The field integral of the toroids ranges between 2.0 and 6.0 Tm across most of the detector.

Events of interest are selected and collected by the ATLAS trigger system [71], consisting of a hardware-based first-level trigger (L1) and a software-based high-level trigger (HLT). The L1 trigger is designed to accept events from the 40-MHz bunch crossings at a rate below 100 kHz, and the HLT reduces this to about 1 kHz, the rate at which events are recorded to disk. An extensive software suite [72] is used for real and simulated data reconstruction and analysis, for operation and in the trigger and data acquisition systems of the experiment.

IV. DATA AND MONTE CARLO SIMULATION

A. Data sample

The data events used in the analysis are from proton-proton collisions at $\sqrt{s} = 13$ TeV, recorded during stable beam conditions at the LHC during 2015–2018. The collected dataset corresponds to an integrated luminosity of 139 fb$^{-1}$ after applying the data quality criteria [73]. The primary dataset was collected by triggers targeting large missing transverse momentum [74]. Events were accepted when the $E_T^{miss}$ calculated at trigger level was greater than 70–110 GeV, with the threshold rising with the increased instantaneous luminosity during the data-taking period. The efficiency reaches approximately 100% for events reconstructed offline with $E_T^{miss} > 200$ GeV, which is generally required in the search. Auxiliary data samples used to validate the background estimation were selected using triggers requiring at least one isolated electron, muon or photon [75,76]. The thresholds were $p_T = 24(26)$ GeV for electrons, $p_T = 20(26)$ GeV for muons, and $p_T = 120(140)$ GeV for photons in data taken in 2015 (2016–2018).

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8 ATLAS uses a right-handed coordinate system with its origin at the nominal interaction point (IP) in the center of the detector and the z axis along the beam pipe. The x axis points from the IP to the center of the LHC ring, and the y axis points upwards. Cylindrical coordinates (r, φ) are used in the transverse plane, φ being the azimuthal angle around the z axis. The pseudorapidity is defined in terms of the polar angle θ as $η = −\ln \tan(θ/2)$. Angular distance is measured in units of $ΔR = \sqrt{(Δη)^2 + (Δφ)^2}$. 
B. Monte Carlo simulation

Monte Carlo (MC) simulations are used to estimate the SM backgrounds and the signals contributing to the analysis regions. All of the generated events were propagated through the ATLAS detector simulation [77] based on GEANT4 [78]. Multiple proton-proton collisions in the same and neighboring bunch crossings (pileup) were modeled by overlaying the hard-scatter events with minimum-bias events simulated by PYTHIA 8.186 [79] with a set of tuned parameters called the A3 tune [80] and NNPDF2.3LO parton distribution function (PDF) set [81].

The simulated events are processed with the same trigger and reconstruction algorithms as the data. The lepton and photon trigger efficiencies in the simulation are corrected to match those in data using scale factors that depend on the \( p_T \) and \( \eta \) of the leptons and photons, as derived from control samples [75,76].

1. Standard Model backgrounds

Events with a leptonically decaying \( W \) or \( Z \) boson associated with hadron jets were simulated using the SHERPA 2.2.1 [82] generator. The matrix elements were calculated for up to two partons at next-to-leading-order (NLO) accuracy and up to four jets at leading-order (LO) accuracy using the Comix [83] and openloops [84,85] generators. The NLO matrix elements for a given jet multiplicity were matched to the parton shower using a color-exact variant of the MC@NLO algorithm [86]. Different jet multiplicities were then merged into an inclusive sample using an improved Catani-Krauss-Kuhn-Webber (CKKW) matching procedure [87,88] which is extended to NLO accuracy using the MEPS@NLO prescription [89]. The NNPDF3.0NNLO PDF sets [90] were used. Prompt single-photon production, denoted by \( \gamma + \text{jets} \), was simulated using the same configuration except that the generator version is SHERPA 2.2.2. The photons must be isolated according to a smooth-cone isolation criterion [91].

Samples of \( \tilde{t}\tilde{t} \) and single-top-quark \( (t+X) \) events were generated with POWHEGBOX v2 [92–95] at NLO with the NNPDF3.0NLO PDF sets. The top-quark mass was set to 172.5 GeV. For the \( \tilde{t}\tilde{t} \) generation, the \( h_{damp} \) parameter, which controls the \( p_T \) of the first additional emission beyond the Born configuration in POWHEG, was set to 1.5 times the top-quark mass. This is to regulate the high-\( p_T \) emission recoiling against the \( \tilde{t}\tilde{t} \) system so as to reproduce the data [96]. The parton shower, fragmentation, and underlying event were simulated using PYTHIA 8.230 with the NNPDF2.3LO PDF set and the A14 tune [97]. The decays of bottom and charm hadrons were performed by EvtGen1.6.0 [98]. The diagram removal scheme [99] was employed to account for the interference between \( \tilde{t}\tilde{t} \) and single-top \( Wt \) production.

Events containing \( \tilde{t}\tilde{t} \) with additional heavy particles, such as \( \tilde{t}\tilde{t} + W/Z/h, \tilde{t}\tilde{t} + WW, \tilde{t}\tilde{t} + t\bar{t}t, \) and \( \tilde{t}\tilde{t} + Wt \), are collectively referred to as \( \tilde{t}\tilde{t} + X \) in this paper. The \( \tilde{t}\tilde{t} + W/Z \) events were modeled by MadGraph5_aMC@NLO2.3.3 [100] at NLO accuracy with the NNPDF3.0NLO PDF set [90] while \( \tilde{t} + h \) events were modeled by POWHEGBOX 2.2. Both were interfaced with PYTHIA 8.230 for parton showering. The \( \tilde{t}\tilde{t} + h \) events were generated using the same setup as for \( \tilde{t}\tilde{t} \) described above, with the \( h \) mass set to 125 GeV. The \( \tilde{t}\tilde{t} + WW, \tilde{t}\tilde{t} + t\bar{t}t, \) and \( \tilde{t}\tilde{t} + Wt \) events were generated with MadGraph5_aMC@NLO2.2.2, interfaced to PYTHIA 8.210 using the A14 tune and the NNPDF2.3LO PDF set. The decays of bottom and charm hadrons were simulated using EvtGen 1.2.0.

Diboson production, including \( WW, WZ \) and \( ZZ \), is collectively denoted here by \( VV \). Events with semileptonic \( VV \) decays (\( \ell\nu\nu, \ell\ell\nu \) and \( \ell\ell\nu\nu \)) were simulated with SHERPA 2.2.1 using matrix elements with up to one additional parton at NLO accuracy in QCD and up to three additional parton emissions at LO accuracy. Events with fully leptonic \( VV \) decays were simulated with SHERPA 2.2.1 (\( ZZ \rightarrow \nu\nu\nu\nu \)) or SHERPA 2.2.2 (\( \ell\ell\ell\ell, \ell\ell\ell\nu, \ell\ell\nu\nu, \) and \( \ell\ell\nu\nu \)) where all the processes at orders of \( (\alpha_s^N, \alpha_s^N) \) and \( (\alpha_s^N, \alpha_s^N) \) are taken into account, including the off-shell contributions and those mediated by Higgs bosons. The NNPDF3.0NNLO PDF set is used.

The production of \( Wh \) and \( Zh \) (collectively denoted by \( Vh \)) was modeled by POWHEGBOX 2.2 interfaced with PYTHIA 8.186. The \( h \) mass was set to 125 GeV. The NNPDF3 PDF set and the AZNLO tune were used.

Triboson production, including \( WWWW, WWZ, WZZ \) and \( ZZZ \), are collectively denoted by \( VVV \). The \( V(\rightarrow \ell\ell/\ell\nu/\nu\nu)(\rightarrow \nu\nu) \) processes were generated using MadGraph5.aMC@NLO2.6.6 at LO, interfaced to PYTHIA 8.243 for modeling of parton showers and hadronization using the A14 tune. The NNPDF3.0LO PDF set was used.

Theoretical cross sections are used to normalize the generated background samples. The \( \tilde{t}\tilde{t} \) sample is normalized to the cross section predicted at NNLO in QCD, including the resummation of next-to-next-to-leading-logarithmic (NNLL) soft-gluon terms calculated using \( \text{top++} 2.0 \) [101–107]. The cross sections of single-top-quark \( t \)- and \( s \)-channel production are calculated using the HATHOR 2.1 program [108,109], while the \( Wt \)-channel calculation followed the prescriptions from Refs. [110,111]. The \( VV \) and \( \tilde{t}\tilde{t} + W/Z \) samples are normalized to the cross sections calculated at NLO [112–114]. The cross sections for the \( V + \text{jets} \) and \( \gamma + \text{jets} \) samples are calculated at NNLO [115]. The remaining samples, including the production of \( Vh \), \( \gamma VV \), \( \tilde{t}\tilde{t} + WW \), \( t\bar{t}W \), \( t\bar{t}Z \), \( \tilde{t}\tilde{t} + h \), \( t\bar{t}t \), and \( t\bar{t}t\tilde{t} \), are normalized to the cross sections calculated at LO by the generators.

2. Signals

The \( (\tilde{W}, \tilde{B}), (\tilde{H}, \tilde{B}), (W, \tilde{H}), (H, \tilde{W}) \), and \( (\tilde{H}, \tilde{a}) \) models discussed in Sec. II were simulated by combining the “simplified model” signals in which a fixed production mode and decay chain are considered. Six sets of simplified
model samples, derived as variants of the \((\tilde{W}, \tilde{B})\) and \((\tilde{H}, \tilde{B})\) models, were generated to cover the different final states:

(i) wino pair production, with each decaying into a bino LSP (referred to as \((\tilde{W}, \tilde{B})\) simplified models, or \((\tilde{W}, \tilde{B})\)-SIM):

\[
\begin{align*}
\text{C1C1-WW: } & \tilde{\chi}_1^+ \tilde{\chi}_1^- \rightarrow WW\tilde{\chi}_1^0 (B(\tilde{\chi}_1^+ \rightarrow W_1^0) = 100\%) \\
\text{C1N2-WZ: } & \tilde{\chi}_1^+ \tilde{\chi}_2^0 \rightarrow WZ\tilde{\chi}_1^0 (B(\tilde{\chi}_1^+ \rightarrow Z_1^0) = 100\%) \\
\text{C1N2-Wh: } & \tilde{\chi}_1^+ \tilde{\chi}_2^0 \rightarrow Wh\tilde{\chi}_1^0 (B(\tilde{\chi}_1^+ \rightarrow h_1^0) = 100\%).
\end{align*}
\]

(ii) neutral higgsino pair production, with each decaying into a bino LSP (denoted by \((\tilde{H}, \tilde{B})\)-SIM):

\[
\begin{align*}
\text{N2N3-ZZ: } & \tilde{\chi}_2^0 \tilde{\chi}_2^0 \rightarrow ZZ\tilde{\chi}_1^0 (B(\tilde{\chi}_2^0 \rightarrow Z_2^0) = 100\%) \\
\text{N2N3-Zh: } & \tilde{\chi}_2^0 \tilde{\chi}_3^0 \rightarrow Zh\tilde{\chi}_1^0 (B(\tilde{\chi}_3^0 \rightarrow h_1^0) = 100\%) \\
\text{N2N3-hh: } & \tilde{\chi}_2^0 \tilde{\chi}_2^0 \rightarrow hh\tilde{\chi}_1^0 (B(\tilde{\chi}_3^0 \rightarrow h_1^0) = 100\%).
\end{align*}
\]

The symbols C1, N2 and N3 in the model names represent \(\tilde{\chi}_1^+, \tilde{\chi}_2^0\) and \(\tilde{\chi}_3^0\), respectively. These samples are used to model event kinematics for each final state; the \((\tilde{W}, \tilde{B})\)-SIM samples are used for events containing \(WW, WZ\) or \(Wh\), while \((\tilde{H}, \tilde{B})\)-SIM samples are employed to model events with \(ZZ, Zh\) or \(hh\). The events are reweighted to account for the production cross section and the \(\tilde{\chi}\) branching ratios considered in the model. The underlying assumption for the method is that the event kinematics depend only on \(m(\tilde{\chi}_\text{light})\) and \(m(\tilde{\chi}_\text{heavy})\), and not on the production mode, type of LSP, or other MSSM variables such as \(\tan\beta\). This is validated in the phase space considered in the analysis by using generator-level samples.

The \((\tilde{W}, \tilde{B})\)-SIM models are also considered in the limit interpretation in order to allow comparisons with previous ATLAS searches, as these models were the most commonly studied \([23,25-29,31-36]\). For the \((\tilde{H}, \tilde{G})\) model, a dedicated sample was generated with all of the production modes \(\tilde{\chi}_1^+ \tilde{\chi}_1^-\), \(\tilde{\chi}_2^0 \tilde{\chi}_1^0\), \(\tilde{\chi}_1^+ \tilde{\chi}_2^0\) included.

The \((\tilde{W}, \tilde{B})\)-SIM and \((\tilde{H}, \tilde{G})\) signal samples were simulated using LO matrix elements with up to two extra partons in MadGraph5_aMC@NLO2.6.2. The events were subsequently interfaced to PYTHIA 8.230 \([116]\) together with the A14 tune and NNPDF2.3LO PDF set for simulation of parton showering and hadronization. For \((\tilde{H}, \tilde{B})\)-SIM, MadGraph5_aMC@NLO2.6.7 and PYTHIA 8.244 were used. The mass of the SM Higgs boson was set to 125 GeV.

Decays of the produced electroweakinos are simulated using PYTHIA. As the performance of the boosted \(W/Z\) boson tagging is known to be sensitive to the boson polarization \([39]\), \(W/Z\) bosons from the electroweakino decays were carefully modeled either by using Madspin 2.7.3 \([117,118]\) or by reweighting the helicity angle distribution such that the overall cross section remains unchanged. The \(W/Z\) bosons are typically longitudinally polarized when \(\Delta m(\tilde{\chi}_{\text{heavy}}, \tilde{\chi}_{\text{light}}) > 400\) GeV is considered. The decays of bottom and charm hadrons were performed by EvtGen 1.2.0.

The signal cross sections are computed at NLO in the strong coupling constant, adding the resummation of soft-gluon emission at next-to-leading-logarithm (NLL) accuracy \([119-124]\). The PDF4LHC15_MC PDF set is used following the recommendations in Ref. \([125]\). Assuming a mass of 800 GeV, the calculated cross section for winolike (higgsinolike) chargino pair production is 2.21 \((0.63)\) fb, and 4.76 \((1.12)\) fb for winolike (higgsinolike) chargino-neutralino production. For neutral higgsino pair production, the corresponding cross section is 0.59 fb.

V. EVENT RECONSTRUCTION

The primary reconstructed objects used in the analysis are large-radius (large-\(R\)) jets, denoted by \(J\). These are reconstructed from locally calibrated topo-clusters \([126]\) using the anti-\(k_t\) algorithm \([127]\) implemented in the Fastjet package \([128]\) with a radius parameter \(R = 1.0\). A trimming algorithm \([129]\) is applied to mitigate the effects of pileup and soft radiation. The constituents of each jet are reclustered with the \(k_t\) algorithm \([130]\) into \(R = 0.2\) subjets, and the subjets are removed if \(p_T^{\text{subj}} / p_T^{\text{jet}} < 0.05\), where \(p_T^{\text{subj}}\) and \(p_T^{\text{jet}}\) are the transverse momenta of the subjet and the large-\(R\) jet, respectively. The jet mass, \(m_J\), is calculated according to the combined mass prescription \([131]\) in order to achieve the best mass resolution, which is given by the weighted sum of masses computed using only the calorimeter information and with tracking information included. The \(p_T\) and mass scales are calibrated using simulation, followed by an in situ calibration \([132]\) to correct for residual differences between
data and MC simulation. Large-$R$ jets used in the analysis are selected with $p_T > 200$ GeV, $|\eta| < 2.0$, and $m_j > 40$ GeV.

Track jets are used to identify large-$R$-jet subjets that contain $b$ hadrons. They are reconstructed from ID tracks by using the anti-$k_t$ algorithm with a sliding radius parameter $R = 30$ GeV/$p_T$ truncated at 0.02 and 0.4 [133]. The MV2c10 $b$-tagging algorithm [134] is applied to track jets satisfying $p_T > 20$ GeV and $|\eta| < 2.5$. This algorithm is a multivariate discriminator that utilizes track impact parameters, the presence of secondary vertices, and the trajectories of $b$- and $c$ hadrons inside the jet. A working point is chosen such that $b$ jets from simulated $t\bar{t}$ events are identified with 85% efficiency, with rejection factors of 3 against $c$ jets and 33 against jets originating from other light-flavor quarks or gluons [134]. Efficiency correction factors are applied to simulated samples to account for the efficiency difference observed between MC and data events in dedicated measurement regions in which $t\bar{t}$ samples [134,135] are used for $b$ jets and mistagged $c$ jets, and $Z + j$ jets samples are used for the light-flavor mistagged jets [136].

The $b$-jet multiplicity of each large-$R$ jet is defined by the number of $b$-tagged track jets it contains. A $b$-tagged track jet is contained in a large-$R$ jet if the two jet axes have an angular separation $\Delta R < 1.0$.

Two types of boosted boson tagging are employed for the preselected large-$R$ jets to identify the SM boson decays: $W_{qq}(Z_{qq})$-tagging targeting $W(Z) \rightarrow qq$, and $Z_{bb}(h_{bb})$-tagging targeting $Z(h) \rightarrow bb$. The $W_{qq}(Z_{qq})$ tagging utilizes cuts on $m_j$, the energy correlation function $D_2$, and the track multiplicity $n_{\text{track}}$ [39,137]. In order to maintain orthogonality with the $Z_{bb}(h_{bb})$ tagging, the $b$-jet multiplicity of the large-$R$ jet is required to be less than two. The $D_2$ variable is defined as a ratio of three-point to two-point energy correlation functions [138,139] based on the energies and pairwise angular separations of particles within a jet, and $n_{\text{track}}$ is the number of tracks matched to the large-$R$ jet by ghost association [140] before trimming is applied. While the upper bound on $n_{\text{track}}$ is fixed, the cut values applied to $m_j$ and $D_2$ are shifted smoothly as a function of $p_T$ to maximize the rejection for typical single-parton initiated jets, maintaining a constant efficiency for signal jets that contain the decay products of $W(Z) \rightarrow qq$. The selections are optimized separately for targeting $W$ and $Z$, and $V_{qq}$ tagging is defined by a selection satisfying either the $W_{qq}$ or $Z_{qq}$ tagging. The cut values applied to $m_j$ and $D_2$ are the same as for the “50% efficiency $W/Z$ tagger” in Ref. [137]; however, a loosened $n_{\text{track}}$ cut, from $\leq 26$ to $\leq 32(34)$ for the $W_{qq}(Z_{qq})$ tagging, is applied to achieve the optimum sensitivity for the analysis and better modeling in MC simulation. The efficiency correction factors are rederived according to this refinement, using a methodology similar to that described in Ref. [137]. A correction factor of 0.85–1.05 is typically obtained. The performance of the $W_{qq}$- and $Z_{qq}$-tagging is summarized in Figs. 4(a) and 4(b). For a sample of preselected large-$R$ jets ($p_T > 200$ GeV, $|\eta| < 2.0$, $m_j > 40$ GeV), the tagging efficiency is about 50% for the signal jets originating from electroweakino decays, while the background rejection is typically about 10 (40) at $p_T = 200(1000)$ GeV per jet in $Z(\rightarrow \nu\nu) + j$ events.

The $Z_{bb}(h_{bb})$ tagging is applied to large-$R$ jets containing exactly two $b$ jets (denoted by $J_{bb}$) by applying a jet mass window cut that selects the peak consistent with $Z(h)$ bosons. The jet mass is corrected by adding the momentum of the highest-$p_T$ muon identified inside the large-$R$ jet in order to improve the resolution of the mass peak. The $Z_{bb}(h_{bb})$ tagging requires the jet mass to satisfy $70(100)$ GeV for $m_j < 100(135)$ GeV. The performance of the $Z_{bb}$-and $h_{bb}$-tagging is summarized in Figs. 4(c) and 4(d).

The analysis also uses reconstructed electrons and muons (collectively referred to as “leptons”), as well as photons and small-radius (small-$R$) jets, for kinematic selection, validation of the background estimation, and the $E_T^{\text{miss}}$ computation. Electron candidates are reconstructed from energy clusters that are consistent with electromagnetic showers in the ECAL and are matched to tracks in the ID, which are calibrated in situ using $Z \rightarrow ee$ samples [141]. Muon candidates in the detector are typically reconstructed by matching tracks in the MS to tracks in the ID, and they are calibrated in situ using $Z \rightarrow \mu\mu$ and $J/\psi \rightarrow \mu\mu$ samples [142]. Small-$R$ jet candidates are reconstructed from particle-flow objects [143] calibrated at the electromagnetic scale using the anti-$k_t$ algorithm with a radius parameter of $R = 0.4$. After subtracting the expected energy contribution from pileup using the jet area technique [144], the jet energy scale and resolution are corrected to particle level using MC simulation as well as by in situ calibration using $Z + j$, $\gamma + j$, and multijet events [145]. Photon candidates are reconstructed either as electromagnetic clusters with no matching ID track or as $e^+e^-$ pairs from photon conversions in the ID material [141].

Reconstructed electrons, muons, small-$R$ jets, and photons are subject to two sets of identification criteria: the looser “baseline” criteria and the tighter “signal” criteria. The baseline objects are used for the $E_T^{\text{miss}}$ computation, event cleaning, and the overlap removal procedure that resolves ambiguities between reconstructed objects as described below. Baseline electrons are required to have $p_T > 4.5$ GeV and $|\eta| < 2.47$, and meet the Loose criteria of the likelihood-based identification [141]. Baseline muons are required to have $p_T > 3$ GeV and $|\eta| < 2.7$, and to meet the Medium identification criteria defined in Ref. [142]. To suppress the contributions from pileup, baseline leptons are represented by a “tight” selection, which combines loose and medium requirements, to reduce the background from unresolved prompt photons and $J/\psi$ events in the dilepton search mode.

The corresponding efficiency for the nominal working point (50% efficiency $W/Z$ tagger in Ref. [137]) is 35–40% for this particular set of preselected jets.

9The corresponding efficiency for the nominal working point (50% efficiency $W/Z$ tagger in Ref. [137]) is 35–40% for this particular set of preselected jets.
jets must have 
order. Any electron sharing an ID track with a muon or 
the baseline leptons, photons, and jets in the following 
multiple objects, an overlap removal procedure is applied to 
other electrons is removed, such that only the highest-$p_T$

electron is kept when multiple electrons share the same ID 
track. Photons around the remaining electrons and muons are 
removed if they are separated by $\Delta R < 0.4$. Next, small-
R jets are removed if they are separated from a remaining electron or photon, or are $\Delta R < 0.4$ from a muon and the jet has fewer than three associated tracks with $p_T > 500$ MeV. Leptons (photons) are removed if they are separated from a remaining small-R jet by $\Delta R < \min(0.4, 0.04 + 10 \text{ GeV}/p_T)$. Finally, large-
R jets are removed if they are separated by $\Delta R < 1.0$ from any remaining electrons.

The missing transverse momentum, with magnitude $E_T^{miss}$, is calculated as the negative vectorial sum of the transverse momenta of all baseline leptons, photons and small-R jets calibrated to their respective energy scales, and an additional

---

10The transverse impact parameter, $d_0$, is defined as the distance of closest approach in the transverse plane between a track and the beam line. The longitudinal impact parameter, $z_0$, corresponds to the $z$-coordinate distance between the point along the track at which the transverse impact parameter is defined and the primary vertex.
“soft term” constructed from tracks originating from the primary vertex but not associated with any of the baseline objects [146].

Signal objects are defined by applying additional stringent criteria in event selections to ensure a high selection purity. Signal leptons and photons are used only for validating the background estimation. Signal electrons and muons must satisfy $p_T > 10$ GeV. Additionally, the Tight identification criteria are imposed for signal electrons. To reduce the contribution from nonprompt decays of heavy-flavor hadrons, the significance of the transverse impact parameter is required to satisfy $|d_0/\sigma(d_0)| < 5(3)$ for signal electrons (muons). An isolation selection is imposed to further suppress the residual misidentified leptons originating from jets. The Tight (HighPtCaloOnly) working point defined in Ref. [141] is used for signal electrons with $p_T < 200$ GeV ($p_T > 200$ GeV), and the Tight working point defined in Ref. [142] is applied for signal muons. Signal small-$R$ jets are selected within $|\eta| < 2.8$, and those with $p_T < 120$ GeV and $|\eta| < 2.5$ must satisfy the Tight quality criteria of the track-based jet vertex tagger [144,147] in order to suppress jets originating from pileup. Signal photons are defined as baseline photons with $p_T > 200$ GeV.

VI. EVENT SELECTION

A. Common preselection

As described below, a common preselection is used when defining the signal regions (SRs), as well as the control regions (CRs) and validation regions (VRs) used for background estimation.

After the trigger requirement discussed in Sec. IV.A, both the data and MC events are required to have at least one reconstructed vertex that is associated with two or more tracks with $p_T > 500$ MeV. The primary vertex of each event is selected as the vertex with the largest $\sum p_T^2$ of associated tracks [148].

A set of event cleaning criteria are applied to ensure the quality of the measurements as well as to veto noncollision backgrounds. Events with baseline muons consistent with cosmic muons ($|z_0| > 1$ mm or $|d_0| > 0.2$ mm) are removed. To avoid pathological $E_T^{\text{miss}}$ reconstruction, events are also vetoed if any baseline jet points to a module of the tile hadronic calorimeter that was not operational during the data taking, or if any baseline muon suffers from a poor momentum measurement [$\sigma(q/p)/(q/p) > 0.4$ where $q/p$ is the measured charge divided by momentum and $\sigma(q/p)$ is its uncertainty]. Track jets can overlap due to their $p_T$-dependent variable radius. To avoid the ambiguous cases of concentric jets, events with a track jet overlapping with another track jet are removed. An overlap is defined by $\Delta R < R_{\text{min}}$ where $\Delta R$ is the angular distance between a given pair of track jets and $R_{\text{min}}$ is the smaller of their radii.

Beam-induced background is one of the major noncollision backgrounds. Particles (typically muons) generated by interactions between the beam and the upstream collimators may directly hit the detector material. Particular care is needed for this background since it can cause high-energy jetlike signatures and, correspondingly, large spurious $E_T^{\text{miss}}$ [149]. Events with baseline jets failing the Loose cleaning [150] are removed. Further cleaning is applied to events with no baseline leptons and photons by requiring consistency between the $E_T^{\text{miss}}$ and the alternative $E_T^{\text{miss,track}}$, which is computed using only the good-quality ID tracks associated with the primary vertex. While those events satisfy $E_T^{\text{miss}} > 200$ GeV due to the trigger requirements, $E_T^{\text{miss,track}} > 75$ GeV and $\Delta\phi(E_T^{\text{miss}}, E_T^{\text{miss,track}}) < 2.0$ are required in the cleaning procedure.

Finally, events are required to contain at least two large-$R$ jets. Events with three or more large-$R$ jets are not vetoed in the analysis, in order to be as inclusive as possible in model coverage; however, the applied event selection is always based on the two highest-$p_T$ large-$R$ jets.

B. Signal region selection

After the preselection, events with no baseline leptons are selected. Two orthogonal signal region categories, 4Q and 2B2Q, based on the absence or presence of a large-$R$ jet containing exactly two $b$-tagged track jets ($J_{bb}$) are defined in order to target the $qqqq$ and $bbqq$ final states, respectively.

Boson tagging is required for the two leading large-$R$ jets. The two leading large-$R$ jets must pass the $V_{qq}$ tagging ($n(V_{qq}) = 2$) in SR-4Q. On the other hand, SR-2B2Q requires $J_{bb}$ to satisfy the $Z_{bb}$ or $h_{bb}$ tagging, while the other jet (denoted by $J_{qq}$) must satisfy the $V_{qq}$-tagging criteria. Multiple SRs are defined in each SR category to target the different final states of the signal processes.

<table>
<thead>
<tr>
<th>$n(W_{qq})$</th>
<th>$n(Z_{qq})$</th>
<th>$n(V_{qq})$</th>
<th>$n(Z_{bb})$</th>
<th>$n(h_{bb})$</th>
</tr>
</thead>
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<td>4Q-WW</td>
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<td>= 2</td>
<td>= 0</td>
<td>= 0</td>
</tr>
<tr>
<td>4Q-WZ</td>
<td>$\geq 1$</td>
<td>= 2</td>
<td>= 0</td>
<td>= 0</td>
</tr>
<tr>
<td>4Q-ZZ</td>
<td>= 2</td>
<td>= 2</td>
<td>= 0</td>
<td>= 0</td>
</tr>
<tr>
<td>4Q-VV</td>
<td>= 2</td>
<td>= 2</td>
<td>= 0</td>
<td>= 0</td>
</tr>
<tr>
<td>2B2Q-WZ</td>
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<td>= 1</td>
<td>= 1</td>
<td>= 0</td>
</tr>
<tr>
<td>2B2Q-ZZ</td>
<td>= 1</td>
<td>= 1</td>
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<td>= 0</td>
</tr>
<tr>
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</tr>
<tr>
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</tr>
</tbody>
</table>
The WW (ZZ) region in SR-4Q requires both leading large-R jets to pass the $W_{qq}$- or $Z_{qq}$-tagging, while the WZ region is defined to contain events with at least one $W_{qq}$-tagged jet and at least one $Z_{qq}$-tagged jet. The inclusive bin VV, the logical union of WW, WZ, and ZZ, is designed to cover the signals that can have various $\tilde{\chi}$ branching ratios into W relative to Z. Similarly, the 2B2Q category accommodates the WZZZZ/WhZh region, which varies by $W_{qq}$- versus $Z_{qq}$- tagging or $Z_{bb}$- versus $h_{bb}$- tagging. The VZ (Vh) region serves as the inclusive SR defined by the logical union of WZ and ZZ (Wh and Zh). The SR segmentation is summarized in Table II and illustrated schematically in Fig. 5. In total, four and six SRs are defined in SR-4Q and SR-2B2Q, respectively. SR-4QXX, SR-2B2QXZ, and SR-2B2QXh (where X = W/Z/V) are mutually orthogonal, and are statistically combined according to the models considered in Table I.

Finally, a series of background rejection cuts are applied to further suppress the main SM backgrounds at this stage: $Z(\rightarrow \nu\nu) +$ jets, $W(\rightarrow \ell\nu) +$ jets, and $t\bar{t}$. To reject backgrounds including top quarks, the $b$ jets that do not originate from boosted boson candidates are vetoed. This is done by requiring $n_b^{\text{unmatched}} = 0$, where $n_b^{\text{unmatched}}$ denotes the number of $b$-tagged track jets that are not matched with any of the two leading large-R jets by the $\Delta R < 1.0$ criterion. For the 4Q category, the total number of $b$-tagged track jets in the events ($n_{b,jet}$) must be less than two in order to further suppress the $t\bar{t}$ background. The effective mass variable, $m_{\text{eff}}$, defined as the scalar sum of the $p_T$ of the two leading large-R jets and $E_T^{\text{miss}}$, is used to select events with hard kinematics together with $E_T^{\text{miss}}$. Selections of $E_T^{\text{miss}} > 300(200)$ GeV and $m_{\text{eff}} > 1300(1000)$ GeV are applied in the 4Q (2B2Q) regions. Event shape information is also useful in distinguishing the signals from the backgrounds. Signal events have a relatively spherical shape, where the jets tend to be isolated from $E_T^{\text{miss}}$, indicating that the heavy electroweakinos are produced nearly at rest. Background events, meanwhile, have a higher chance of containing a jet aligned with a W/Z boson, due to boosted top decays in $t\bar{t}$ events or the emission of collinear radiation in $Z +$ jets and $W +$ jets events. The minimum azimuthal angle separation between $E_T^{\text{miss}}$ and any signal small-R jets must satisfy $\Delta \phi(E_T^{\text{miss}}; j) > 1.0$ for both SR categories. The use of small-R jets is motivated by the need to effectively identify low-$p_T^{}$ jets and it also provides better resolution in terms of jet alignment with $E_T^{\text{miss}}$. In 2B2Q, the transverse mass variable $m_T^{2B2Q}$ [151, 152] is also used, constructed by assigning each of the two leading large-R jets to the visible particle legs. A selection of $m_T^{2B2Q} > 250$ GeV is found to effectively suppress the SM backgrounds, particularly $t\bar{t}$ which exhibits a kinematic cutoff at $m_{T^2} \sim 200$ GeV, driven by the top-quark mass constraint.\textsuperscript{11}

The cut values of the kinematic selection are equivalent within the SR-4Q and SR-2B2Q categories. The selection criteria that define the SR-4Q, SR-2B2Q-Wh, and SR-2B2Q-Vh regions are obtained by optimizing the sensitivity to the ($\tilde{W},\tilde{B}$) model with $(m(\tilde{\chi}_1^\pm), m(\tilde{\chi}_1^0)) \approx (800, 100)$ GeV, while those for SR-2B2Q-WZ, SR-2B2Q-ZZ, and SR-2B2Q-VZ are determined by optimizing the sensitivity to the ($\tilde{H},\tilde{G}$) model with $m_{\tilde{\chi}} \approx 800$ GeV. The discovery significance is used as the metric of sensitivity. The obtained cuts are also found to be nearly optimal for the other signal models.

The acceptance times efficiency for signal events ranges from 1 to 4% depending on $\Delta m(\tilde{\chi}_{\text{heavy}}, \tilde{\chi}_{\text{light}})$ and the SR. For example, it is about 1–2% (1.5%) in SR-4Q-VV (SR-2B2Q-Vh) for the C1N2-WZ (C1N2-Wh) signals with $\Delta m(\tilde{\chi}_{\text{heavy}}, \tilde{\chi}_{\text{light}}) = 600$ GeV, and 3–4% (2–3%) with $\Delta m(\tilde{\chi}_{\text{heavy}}, \tilde{\chi}_{\text{light}}) = 1$ TeV.\textsuperscript{11}

\textsuperscript{11}The hypothetical missing-particle mass is set to 100 GeV and this offset is subtracted from the calculated $m_{T^2}$, although the dependency on the choice of missing-particle mass is very small.
The fake boson jets are typically caused by two collimated $\nu\nu$ W=Z → $\nu\nu$ jets. The same selection is applied to the SR (VR) and CR in the same category except for the $V_{qq}$ tagging and some kinematic selections that are explicitly indicated in parentheses. The trigger selection and event cleaning described in Sec. V are also applied. VRTTX is a validation region used to validate the $\bar{t}t + X$ modeling as described in Sec. VII A. $p_T(W)$ is the vector sum of the $p_T$ of the lepton and $E_T^{miss}$ in the 1L regions. In the 1L (1Y) regions, $E_T^{miss}$ is replaced by $p_T(\gamma)$ when calculating the kinematic variables $m_{eff}$, $\Delta\phi(E_T^{miss},j)$ and $m_{T2}$. Details are given in Sec. VII B.

### VII. BACKGROUND ESTIMATION

The main SM background process in the SRs is $Z(\to \nu\nu) +$ jets (∼50%), followed by $W(\to \ell\nu) +$ jets (15–20%), and $VV$ (10–20%). The rest consists of $VVV$ events in SR-4Q (5–10%), or $\bar{t}t$, single-top and $\bar{t}t + X$ events in SR-2B2Q (10–20%).

The estimation strategy varies between the “reducible” and “irreducible” backgrounds. The irreducible backgrounds in this search are due to SM events including at least two hadronic $W/Z/h$ decays and large $E_T^{miss}$ from high-$p_T$ neutrinos. These consist of $VVV$ and $\bar{t}t + X$, and are estimated using MC simulation. The contributions from fully hadronic $VV$ and $\bar{t}t$ are negligible due to the stringent $E_T^{miss}$ requirement.

The reducible backgrounds are all that remain, including the dominant $Z(\to \nu\nu) +$ jets production. These backgrounds are characterized by the presence of at least one large-$R$ jet that originates from a process other than a $W/Z \to qq$ decay and is referred to as a “fake boson jet.” The fake boson jets are typically caused by two collimated high-$p_T$ initial-state radiation (ISR) jets that are clustered together as a single large-$R$ jet. A partly data-driven method is used to estimate the reducible backgrounds; a control region (CROL) is defined in the phase space adjacent to a SR, where the MC sample is normalized to the CR data.

The SR expectation is obtained using the normalized MC sample, assuming the modeling of the SR/CROL yield ratio (“0L transfer factor”) is reliable. This assumption is tested in a number of VRs in data. A CROL is defined for each 4Q and 2B2Q category by reversing the $V_{qq}$-tagging requirement on one of the two leading large-$R$ jets in the SR, and is denoted by CROL-4Q and CROL-2B2Q, respectively. The multijet and noncollision background contributions are found to be negligible using the data-driven methods or from the estimation in a similar phase space carried out in Ref. [153].

The following subsections discuss the methodology and results of the irreducible and reducible background estimations.

#### A. Irreducible background estimation

The $VVV$ ($\bar{t}t + X$) events account for at most 10% of the total background in SR-4Q (SR-2B2Q), and are negligible in SR-2B2Q (SR-4Q). Given their minor contribution, these backgrounds are estimated directly from the MC predictions and assigned conservative uncertainties.

The dominant $\bar{t}t + X$ component in SR-2B2Q is $\bar{t}t(\to bqqbqq) + Z(\to \nu\nu)$. To validate the MC modeling, a dedicated validation region VRTTX is defined in a three-lepton region populated by $\bar{t}t(\to b\ell\nu bqq) + Z(\to \ell\ell\ell)$. The selections are summarized in Table III. Exactly three baseline and signal leptons are required, with the leading

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**TABLE III.** Summary of selections for the SRs, CRs, and VRs. $n(V_{qq}) (n(V_{qq}))$ represents the number of large-$R$ jets passing (failing) the $V_{qq}$ tagging of the two highest-$p_T$ large-$R$ jets. The same selection is applied to the SR (VR) and CR in the same category except for the $V_{qq}$ tagging and some kinematic selections that are explicitly indicated in parentheses. The trigger selection and event cleaning described in Sec. V are also applied. VRTTX is a validation region used to validate the $\bar{t}t + X$ modeling as described in Sec. VII A. $p_T(W)$ is the vector sum of the $p_T$ of the lepton and $E_T^{miss}$ in the 1L regions. In the 1L (1Y) regions, $E_T^{miss}$ is replaced by $p_T(\gamma)$ when calculating the kinematic variables $m_{eff}$, $\Delta\phi(E_T^{miss},j)$ and $m_{T2}$. Details are given in Sec. VII B.

<table>
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<th>Selections</th>
<th>4Q</th>
<th>2B2Q</th>
<th>4Q</th>
<th>2B2Q</th>
<th>4Q</th>
<th>2B2Q</th>
<th>VRTTX</th>
</tr>
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<td>≤2</td>
<td>≥2</td>
<td>≤2</td>
<td>≥2</td>
<td>≤2</td>
<td>=1</td>
</tr>
<tr>
<td>$n_\nu$</td>
<td>=1</td>
<td>≥1</td>
<td>=1</td>
<td>≥1</td>
<td>=1</td>
<td>≥1</td>
<td>=1</td>
</tr>
<tr>
<td>$p_T(\ell)$</td>
<td>≥30</td>
<td>≥30</td>
<td>≥30</td>
<td>≥30</td>
<td>≥30</td>
<td>≥30</td>
<td>≥30</td>
</tr>
<tr>
<td>$m_{eff}$</td>
<td>≥1300</td>
<td>≥1300</td>
<td>&gt;1000</td>
<td>&gt;900</td>
<td>&gt;900</td>
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<td>&gt;900</td>
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<tr>
<td>$m_{T2}$</td>
<td>≥250</td>
<td>≥250</td>
<td>≥250</td>
<td>≥250</td>
<td>≥250</td>
<td>≥250</td>
<td>≥250</td>
</tr>
</tbody>
</table>
lepton of $p_T > 30$ GeV firing the single-lepton trigger. At least one large-$R$ jet is required in the event, and it must contain exactly two $b$-tagged track jets. No further kinematic cuts are applied, in order to maintain a sufficient data sample size in the region. The $t\bar{t} + X$ purity in this region is about 70%. Sixty-eight data events are observed in VRTTX, while 46.5 events are predicted by MC simulation (31.5 from $t\bar{t} + X$, 12.1 from $VV$, and 2.9 from the others).

A 70% uncertainty is therefore assigned to the $t\bar{t} + X$ normalization to fully cover the observed discrepancy; this has only a small impact on the total background estimation, given the minor contribution in the SRs.

The $VVV$ contribution to SR-4Q is mainly from $VV(qqqq) + Z(\rightarrow \ell\nu\ell)$ processes. The $VVV$ process has only recently been observed at the LHC [154,155]. As the data sample size in that phase-space region is insufficient and loosening the selection leads to poor $VVV$ purity, no control or validation regions were designed and this background is estimated directly from the MC prediction. A 50% uncertainty is therefore assigned for the normalization based on the precision of the $WWZ$ production cross-section measurement performed by the CMS experiment [155].

**B. Reducible background estimation**

The CR0L-4Q is defined by the same selection as SR-4Q-VVV except that one of the two leading large-$R$ jets must fail the $V_{qq}$-tagging, and the CR0L-2B2Q is constructed as the logical union of SR-2B2Q-VZ and SR-2B2Q-Vh with the $J_{qq}$ failing the $V_{qq}$ tagging. For the reducible backgrounds, the extrapolation from a CR0L to the SR is mainly characterized by the $V_{qq}$-tagging response for a fake boson jet. In order to maintain a sufficient data sample size and to suppress signal contamination, the $m_{\text{eff}}$ selection and the $J_{bb}$ mass window cut for CR0L-2B2Q are loosened relative to the SR, from $m_{\text{eff}} > 1000$ GeV to $m_{\text{eff}} > 900$ GeV and from $70 < m(J_{bb}) < 135$ GeV to $70 < m(J_{bb}) < 150$ GeV. The signal contamination in CR0L-4Q and CR0L-2B2Q is evaluated using the $(\tilde{W}, \tilde{B})$-SIM and $(\tilde{H}, \tilde{G})$ samples. While a contribution of up to 15% (24%) of the expected backgrounds in CR0L-4Q (CR0L-2B2Q) can be caused by the nonexcluded signals, the introduced bias in the estimate is still smaller than the total uncertainty in the SRs and VRs, and therefore has only a small impact on the final sensitivity. The selections are summarized in Table III, and the relation with the SR is illustrated in Fig. 6.

One advantage of this CR0L definition is that all physics processes contributing to the background ($Z +$ jets, $W +$ jets, $t\bar{t}$, etc.) have comparable 0L transfer factors. This is because the fake boson jets have similar origins and kinematics, and therefore the same boson tagging efficiency, confirmed by the simulation. Consequently, they can be treated as a single combined component with a common normalization factor assigned to correct their normalizations at once. The normalization is performed in 4Q and 2B2Q separately with an independent normalization factor, based on the “background-only fits” described in Sec. IX A.

Good MC modeling of the 0L transfer factor is essential for the estimation. Data events with exactly one lepton or one photon are utilized for the validation. This is motivated by the fact that in these regions the main backgrounds, $Z(\rightarrow \ell\nu\ell)$ + jets in SR/CR0L, $W(\rightarrow \ell\nu)$ + jets in the one-lepton region and $\gamma +$ jets in the one-photon region, have similar ISR jet kinematics and, relative to the minor backgrounds, contribute similarly to the respective regions when a compatible kinematic phase space is chosen. The one-lepton (one-photon) regions corresponding to CR0L and the SR are constructed, denoted by CR1L(1Y) and VR1L(1Y), respectively. The level of data-vs-MC agreement in the ratio VR1L(1Y)/CR1L(1Y) [“1L(1Y) transfer factor”] is validated as a proxy for the MC modeling of the 0L transfer factor.

The selections applied for VR(CR)1L and VR(CR)1Y are listed in Table III. The VR(CR)1L is defined by requiring exactly one baseline lepton and a signal lepton with $p_T > 30$ GeV that fires the single-lepton trigger. In addition, $E_{\text{miss}}^{\text{pass}} > 50$ GeV is required to suppress contributions from
FIG. 7. Comparison between the observed data and the postfit SM background prediction in VR1L and VR1Y. The background predictions are obtained using the background-only fit described in Sec. IX A. “Top” includes \( t \bar{t}, t^+X, \) and \( t \bar{t}^+X \) production. The total systematic uncertainty of the background prediction is shown by the hatched band. The bottom panel shows the statistical significance of the discrepancy between the observed number of events and the SM expectation, following the prescription described in Ref. [158].

FIG. 8. \( m_{\text{eff}} \) distributions in VR1L-4Q/VR1Y-4Q and \( m_{T^2} \) distributions in VR1L-2B2Q/VR1Y-2B2Q. The postfit SM background expectation using the background-only fit is shown in a histogram stack. “Top” includes \( \ell \ell, t^+X, \) and \( \ell \bar{\ell}^+X \) production. The hatched bands indicate the combined statistical and systematic uncertainty of the background. The bottom panels show the ratio of the observed data to the background expectation. The selection criterion for the variable shown by each plot is removed, while the arrow indicates the cut value used to define the region.
QCD multijet events with poorly measured $E_T^{\text{miss}}$. The VR (CR1)Y requires exactly one baseline and signal photon to fire the single-photon trigger, and vetoes events with at least one baseline lepton. For both VR(CR1)L and VR(CR1)Y, at least two large-$R$ jets are required, and the events are separated into the 4Q and 2B2Q categories, based on the absence or presence of $J_{bb}$, respectively. A b-jet veto strategy similar to that for the SRs and the CR0L bins is applied: $n_{b-jet}^{\text{unmatched}} = 0$ in all the regions, $n_{b-jet} \leq 1$ in the 4Q regions. A stricter veto of $n_{b-jet} = 0$ is applied in CR(VR)1L-4Q to suppress the large single-top contribution relative to the other 4Q regions.

The kinematic selection in the IL (1Y) regions is applied with $E_T^{\text{miss}}$ replaced by $p_T(W) (p_T(\gamma))$ in the variables. This is to ensure that compatible phase spaces are probed for $Z(\rightarrow \nu \nu)$ + jets in SR/CR0L, $W(\rightarrow \ell \nu)$ + jets in VR1L/CR1L, and $\gamma$ + jets in VR1Y/CR1Y, since $E_T^{\text{miss}}$ in $Z(\rightarrow \nu \nu)$ + jets events typically represents the $p_T$ of the $Z$ boson. The $p_T(W)$ variable is defined as the vector sum of the $p_T$ of the lepton and $E_T^{\text{miss}}$ in the IL regions. The $E_T^{\text{miss}}$, $p_T(W)$, and $p_T(\gamma)$ are collectively denoted by $p_T(V)$.

Table IV. Number of observed data events and the postfit SM background prediction in the VR1L (1Y) bins and the corresponding CR1L (1Y) bins. Negligibly small contributions are indicated by "dots." Within each CR the reducible backgrounds have the same relative uncertainty in their expected yield because a common normalization factor is assigned to all of them in the fit.

The min $\Delta \phi(E_T^{\text{miss}}, j)$ variable, as well as those analogously derived from $p_T(W)$ and $p_T(\gamma)$, are collectively denoted by min $\Delta \phi(V, j)$. The cuts in $p_T(V)$ and $m_{\text{eff}}$ are moderately loosened relative to the SRs to ensure a data size sample sufficient for the validation. For 2B2Q regions, the $J_{bb}$ mass window cut for the $Z_{bb}/h_{bb}$ tagging is loosened to $70 < m_j < 150$ GeV to match CR0L-2B2Q, further increasing the data sample size. The contributions from events containing fake leptons and fake photons are estimated by data-driven methods [156,157] and are found to be negligible.

The same estimation procedure used to estimate the backgrounds in the SRs is employed to predict the background in the VRs. A background-only fit, described in Sec. IX A, is performed, where the sum of the reducible backgrounds in MC samples is normalized to the data in each CR1L (CR1Y). The modeling of the transfer factor is examined using the level of agreement between the data and the postfit background expectation in the corresponding VR1L (VR1Y). Four sets of fits are performed in the 1L-4Q, 1L-2B2Q, 1Y-4Q, and 1Y-2B2Q categories separately. Including all the systematic uncertainties discussed in Sec. VIII, the observed data event yields and the postfit background expectations in the VRs are summarized in Table IV, and compared graphically in Fig. 7. The distributions of $m_{\text{eff}}$ in VR1L(1Y)-4Q and $m_{\text{eff}}$ in VR1L(1Y)-2B2Q are shown in Fig. 8. The data agree reasonably well with the estimated backgrounds across the VRs. The largest disagreement is found in VR1L-4Q, corresponding to a statistical significance of 1.8 $\sigma$.

### VIII. SYSTEMATIC UNCERTAINTIES

Uncertainties in the expected signal and background yields account for the statistical uncertainties of the MC samples, the experimental systematic uncertainties associated with the detector measurements and reconstruction, and the theoretical systematic uncertainties in the MC simulation modeling. For the signals and irreducible backgrounds, the uncertainties are assigned directly to the event yields. For the reducible backgrounds, however, they are assigned to the SR(VR)/CR ratio ("transfer factor," TF) as a consequence of the normalization performed in the CRs. The reducible backgrounds are also subject to uncertainties due to the limited data sample size in the CRs. Each systematic uncertainty is treated as fully correlated across the analysis regions but not across physics processes, unless explicitly stated otherwise. A summary of the background prediction uncertainties is shown in Fig. 9. The postfit values are quoted after a background-only fit described in Sec. IX. The MC statistical uncertainties give the largest contribution to the systematic uncertainty, mainly from the limited size of the $Z(\rightarrow \nu \nu)$ + jets background sample used for the extrapolation. However, this is not a limiting factor for the analysis sensitivity since the total uncertainty in the SRs is dominated by the statistical uncertainty due to the low number of data events in the SRs.

<table>
<thead>
<tr>
<th>Region</th>
<th>CR1L-4Q</th>
<th>VR1L-4Q</th>
<th>CR1L-2B2Q</th>
<th>VR1L-2B2Q</th>
</tr>
</thead>
<tbody>
<tr>
<td>Observed</td>
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<td>13</td>
<td>96</td>
<td>5</td>
</tr>
<tr>
<td>Post-fit</td>
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</tr>
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<tr>
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<tr>
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</tr>
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<table>
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<tr>
<td>Observed</td>
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<td>127</td>
<td>14</td>
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<tr>
<td>Post-fit</td>
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<td>$127 \pm 11$</td>
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Details of the experimental and theoretical systematic uncertainties are described in the following subsections.

A. Experimental uncertainties

The first class of experimental uncertainties is related to the reconstruction and identification efficiencies for large-R jets, small-R jets, leptons and photons considered in the analysis. These are assigned as uncertainties in the efficiency correction factors applied to the MC samples, which correct for discrepancies between the efficiency predicted by MC simulation and the efficiency in data, as measured using dedicated control samples.

<table>
<thead>
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<th>SR-4Q-WZ</th>
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<tr>
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<td>2</td>
<td>3</td>
<td>1</td>
<td>3</td>
</tr>
<tr>
<td>Postfit</td>
<td>129 ± 11</td>
<td>83 ± 9</td>
<td>1.9 ± 0.4</td>
<td>3.4 ± 0.7</td>
<td>1.9 ± 0.5</td>
<td>3.9 ± 0.8</td>
</tr>
<tr>
<td>W + jets</td>
<td>24.2 ± 2.2</td>
<td>16.6 ± 2.0</td>
<td>0.37 ± 0.08</td>
<td>0.60 ± 0.13</td>
<td>0.26 ± 0.07</td>
<td>0.69 ± 0.15</td>
</tr>
<tr>
<td>Z + jets</td>
<td>78 ± 7</td>
<td>44 ± 5</td>
<td>1.0 ± 0.21</td>
<td>1.8 ± 0.4</td>
<td>1.26 ± 0.32</td>
<td>2.1 ± 0.4</td>
</tr>
<tr>
<td>VV</td>
<td>21.5 ± 1.9</td>
<td>7.1 ± 0.9</td>
<td>0.35 ± 0.11</td>
<td>0.73 ± 0.24</td>
<td>0.26 ± 0.09</td>
<td>0.79 ± 0.25</td>
</tr>
<tr>
<td>VVV</td>
<td>0.9 ± 0.4</td>
<td>0.10 ± 0.05</td>
<td>0.17 ± 0.09</td>
<td>0.19 ± 0.10</td>
<td>0.11 ± 0.07</td>
<td>0.23 ± 0.12</td>
</tr>
<tr>
<td>$t\bar{t}$</td>
<td>1.38 ± 0.12</td>
<td>7.8 ± 0.9</td>
<td>0.039 ± 0.009</td>
<td>0.060 ± 0.018</td>
<td>0.025 ± 0.010</td>
<td>0.063 ± 0.018</td>
</tr>
<tr>
<td>$t + X$</td>
<td>1.32 ± 0.12</td>
<td>2.87 ± 0.34</td>
<td>0.015 ± 0.006</td>
<td>0.039 ± 0.016</td>
<td>0.012 ± 0.005</td>
<td>0.039 ± 0.016</td>
</tr>
<tr>
<td>$t\bar{t} + X$</td>
<td>1.3 ± 0.9</td>
<td>3.7 ± 2.6</td>
<td>...</td>
<td>...</td>
<td>...</td>
<td>...</td>
</tr>
<tr>
<td>Other</td>
<td>&lt; 0.1</td>
<td>0.95 ± 0.11</td>
<td>&lt; 0.001</td>
<td>&lt; 0.001</td>
<td>&lt; 0.001</td>
<td>&lt; 0.001</td>
</tr>
</tbody>
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</thead>
<tbody>
<tr>
<td>Observed</td>
<td>2</td>
<td>0</td>
<td>2</td>
<td>1</td>
<td>2</td>
<td>1</td>
</tr>
<tr>
<td>Postfit</td>
<td>1.6 ± 0.4</td>
<td>1.9 ± 0.7</td>
<td>1.7 ± 0.5</td>
<td>1.6 ± 0.5</td>
<td>2.2 ± 0.6</td>
<td>2.5 ± 0.8</td>
</tr>
<tr>
<td>W + jets</td>
<td>0.11 ± 0.06</td>
<td>0.24 ± 0.09</td>
<td>0.23 ± 0.08</td>
<td>0.26 ± 0.10</td>
<td>0.26 ± 0.09</td>
<td>0.26 ± 0.09</td>
</tr>
<tr>
<td>Z + jets</td>
<td>0.84 ± 0.27</td>
<td>1.3 ± 0.5</td>
<td>0.78 ± 0.23</td>
<td>0.66 ± 0.24</td>
<td>1.15 ± 0.33</td>
<td>1.4 ± 0.5</td>
</tr>
<tr>
<td>VV</td>
<td>0.33 ± 0.11</td>
<td>0.09 ± 0.03</td>
<td>0.32 ± 0.10</td>
<td>0.085 ± 0.032</td>
<td>0.37 ± 0.11</td>
<td>0.085 ± 0.030</td>
</tr>
<tr>
<td>VVV</td>
<td>0.047 ± 0.027</td>
<td>&lt; 0.01</td>
<td>0.051 ± 0.032</td>
<td>0.011 ± 0.007</td>
<td>0.06 ± 0.04</td>
<td>0.011 ± 0.007</td>
</tr>
<tr>
<td>$t\bar{t}$</td>
<td>0.016 ± 0.006</td>
<td>0.13 ± 0.04</td>
<td>0.064 ± 0.019</td>
<td>0.40 ± 0.16</td>
<td>0.072 ± 0.021</td>
<td>0.46 ± 0.18</td>
</tr>
<tr>
<td>$t + X$</td>
<td>0.11 ± 0.05</td>
<td>0.07 ± 0.04</td>
<td>0.11 ± 0.05</td>
<td>0.041 ± 0.022</td>
<td>0.11 ± 0.05</td>
<td>0.10 ± 0.05</td>
</tr>
<tr>
<td>$t\bar{t} + X$</td>
<td>0.10 ± 0.08</td>
<td>0.07 ± 0.10</td>
<td>0.14 ± 0.12</td>
<td>0.08 ± 0.09</td>
<td>0.18 ± 0.14</td>
<td>0.10 ± 0.11</td>
</tr>
<tr>
<td>Other</td>
<td>&lt; 0.01</td>
<td>0.03 ± 0.01</td>
<td>&lt; 0.01</td>
<td>0.024 ± 0.008</td>
<td>&lt; 0.01</td>
<td>0.037 ± 0.011</td>
</tr>
</tbody>
</table>
FIG. 10. Summary of the observed data and predicted SM background in all SRs. The background prediction in SR-4Q (SR-2B2Q) is obtained by a background-only fit to CR0L-4Q (CR0L-2B2Q). The total systematic uncertainty in the background prediction is shown by the hatched area. Distributions of a few representative signals are overlaid. For the \((\tilde{W}, \tilde{B})\)-SIM models, the label (900, 100) GeV indicates \((m_{\tilde{\chi}_1^{\pm}}, m_{\tilde{\chi}_1^0})\). The bottom panel shows the statistical significance of the discrepancy between the observed number of events and the SM expectation, following the prescription described in Ref. [158].

FIG. 11. (a) \(m_{\text{eff}}\) distribution in SR-4Q-VV. (b), (c) \(m_{T_2}\) distributions in SR-2B2Q-VZ and SR-2B2Q-Vh. The postfit SM background expectation using the background-only fit is shown in a histogram stack. Distributions of a few representative signals are overlaid. The bottom panels show the ratio of the observed data to the background prediction. The selection criterion for the variable shown by each plot is removed, while the arrow indicates the cut value used to define the region. For the \((\tilde{W}, \tilde{B})\)-SIM models, the labels (700, 100) GeV and (900, 100) GeV indicate \((m_{\tilde{\chi}_1^{\pm}}, m_{\tilde{\chi}_1^0})\).
The uncertainty in $W_{qq}(Z_{qq})$ tagging contributes the most to this class of efficiency uncertainties. It originates from the MC modeling uncertainty in the jet substructure variable distributions ($m_1$, $D_2$, and $R_{	ext{tag}}$), as well as the precision of the efficiency determination in data. The MC modeling uncertainty is evaluated by comparing samples from different MC generator configurations [137]. The $W_{qq}$-tagging efficiency in data is measured using $t\bar{t}$ for signal jets (large-$R$ jets that contain the $W \rightarrow q q$ decays) and QCD multijet/$\gamma +$ jets for background jets, following the prescription described in Ref. [137].

The total uncertainty of the $W_{qq}$-tagging efficiency correction factor ranges from 12 to 23% for signal jets, and from 7 to 15% for background jets, depending on the $p_T$. The same efficiency correction factors are applied to the $Z_{qq}$-tagging selection, with a simulation-based additional uncertainty of 4–5% to account for differences between W and Z bosons.

The uncertainty in the $Z_{bb}(h_{bb})$ tagging is obtained from the $b$-tagging efficiency uncertainty and the $J_{bb}$ mass distribution’s shape uncertainty. For the $b$-tagging uncertainty, 1–10%, 15–50%, and 50–100% uncertainties are assigned to the MC correction factor for $b$ jets, $c$-jet mistagging, and light-flavor jet mistagging, respectively, driven by theoretical uncertainties in the MC-simulated efficiency and the precision of the efficiency measurement in data. The $J_{bb}$ mass scale uncertainty is estimated using the $R_{\text{fit}}$ method [132], and a relative scale uncertainty of 2–8% is assigned depending on $p_T$ and $m_J$. A 20% relative uncertainty is assigned for the $J_{bb}$ mass resolution based on the variation in the simulation [159].

Other efficiency uncertainties related to triggering, identification, reconstruction, and isolation requirements of electrons [75,141], muons [142] and photons [75], and the jet vertex tagger selection for small-$R$ jets, are found to be negligible.

The second class of experimental uncertainties is related to the energy (or momentum) determination for the reconstructed objects, namely large-$R$ jets [132], small-$R$ jets [145], electrons [141], muons [160] and photons [141]. These typically come from the precision of simulation-based and in situ calibrations of the energy (or momentum) scale and resolution. These per-object uncertainties are propagated through the $E_{\text{miss}}$ calculation, with additional uncertainties accounting for the scale and resolution of the soft term [146].

Additionally, an uncertainty in the integrated luminosity used to normalize the MC samples is considered. A 1.7% uncertainty is quoted for the combined 2015–2018 integrated luminosity obtained primarily using the LUCID-2 detector [161]. Finally, a pileup modeling uncertainty is assigned to account for the discrepancy between the predicted and measured inelastic cross sections [162].

### B. Theoretical uncertainties

Theoretical uncertainties in the main reducible backgrounds ($W/Z +$ jets, $\gamma +$ jets, and $VV$ production) are estimated with varied generator parameters. Uncertainties due to the choice of QCD renormalization and factorization scales are evaluated by varying them up and down by a factor of 2 relative to their nominal values [163]. For $W/Z +$ jets, the uncertainties related to the choice of CKKW merging scale are also considered. These are assessed by shifting the merging scale to 15 or 30 GeV from the default scale of 20 GeV. For the $t\bar{t}$ background, the nominal POWHEG+PYTHIA 8 sample is compared with two alternative samples: one from MadGraph5_aMC@NLO to estimate the hard-scatter modeling uncertainty, and the other from POWHEGBOX interfaced to HERWIG 7.0.4 [164] and H7UE set of tuned parameters [164] to assess the uncertainty due to the choice of parton shower scheme and hadronization model. Variations in the $t\bar{t}$ initial- and final-state radiation modeling, and renormalization and factorization scales, are also considered following the prescription described in Ref. [165]. Uncertainties related to the choice of NNPDF3.0NNLO PDF sets are assigned to the $W/Z +$ jets, $\gamma +$ jets, $VV$, $t\bar{t}$ and single-top backgrounds. These are derived by taking the envelope of the eigenvector variations from 100 propagated uncertainties.

For the reducible background estimation, an additional uncertainty is assigned for the modeling of the relative background composition. This is because different physics processes ($Z +$ jets, $W +$ jets, $t\bar{t}$, etc.) are considered as a background for the signal regions and there are a number of assumptions concerning the relative contributions of each background. These uncertainties are evaluated by comparing samples from different MC generator configurations and by varying the scale and resolution parameters used to generate the signal events.

### TABLE VI. Left to right: 95% C.L. upper limits on the visible cross section ($\langle \sigma \rangle_{\text{obs}}^{95}$), $\sigma_{\text{obs}}^{95}$ ($\sigma_{\text{exp}}^{95}$) shows the 95% C.L. upper limit on the number of signal events, given the observed number (expected number and $\pm \sigma$ excursions) of background events. The last two columns indicate the $\text{CL}_{b}$ value and the discovery $p$ value ($p(s = 0)$) with the corresponding Gaussian significance ($\sigma$). $\text{CL}_{b}$ provides a measure of compatibility of the observed data with the 95% C.L. signal strength hypothesis relative to fluctuations of the background, and $p(s = 0)$ measures compatibility of the observed data with the background-only (zero signal strength) hypothesis relative to fluctuations of the background. Larger values indicate greater relative compatibility. $p(s = 0)$ is not calculated in signal regions with a deficit with respect to the nominal background prediction.

<table>
<thead>
<tr>
<th>Signal region</th>
<th>$\langle \sigma \rangle_{\text{obs}}^{95}$ (fb)</th>
<th>$\sigma_{\text{obs}}^{95}$</th>
<th>$\sigma_{\text{exp}}^{95}$ ($\pm \sigma$)</th>
<th>$\text{CL}_{b}$</th>
<th>$p(s = 0)$ (Z)</th>
</tr>
</thead>
<tbody>
<tr>
<td>SR-4Q-WW</td>
<td>0.032 4.5</td>
<td>$4.2^{+1.8}_{-1.0}$</td>
<td>0.55 0.44 (0.15)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>SR-4Q-WZ</td>
<td>0.036 5.0</td>
<td>$5.1^{+1.3}_{-1.0}$</td>
<td>0.46 ...</td>
<td></td>
<td></td>
</tr>
<tr>
<td>SR-4Q-ZZ</td>
<td>0.025 3.6</td>
<td>$4.1^{+1.8}_{-1.0}$</td>
<td>0.30 ...</td>
<td></td>
<td></td>
</tr>
<tr>
<td>SR-4Q-VV</td>
<td>0.034 4.7</td>
<td>$5.3^{+2.3}_{-1.5}$</td>
<td>0.38 ...</td>
<td></td>
<td></td>
</tr>
<tr>
<td>SR-2B2Q-WZ</td>
<td>0.033 4.7</td>
<td>$4.0^{+1.7}_{-1.0}$</td>
<td>0.66 0.33 (0.44)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>SR-2B2Q-Wh</td>
<td>0.022 3.1</td>
<td>$3.9^{+1.1}_{-0.7}$</td>
<td>0.28 ...</td>
<td></td>
<td></td>
</tr>
<tr>
<td>SR-2B2Q-ZZ</td>
<td>0.033 4.5</td>
<td>$4.1^{+1.7}_{-0.9}$</td>
<td>0.63 0.37 (0.32)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>SR-2B2Q-Zh</td>
<td>0.026 3.6</td>
<td>$3.9^{+1.4}_{-0.7}$</td>
<td>0.38 ...</td>
<td></td>
<td></td>
</tr>
<tr>
<td>SR-2B2Q-VZ</td>
<td>0.032 4.4</td>
<td>$4.4^{+1.8}_{-1.0}$</td>
<td>0.50 ...</td>
<td></td>
<td></td>
</tr>
<tr>
<td>SR-2B2Q-Vh</td>
<td>0.026 3.6</td>
<td>$4.4^{+1.7}_{-1.0}$</td>
<td>0.24 ...</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Disc-SR-2B2Q</td>
<td>0.034 4.8</td>
<td>$5.6^{+2.4}_{-1.6}$</td>
<td>0.30 ...</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Disc-SR-Incl</td>
<td>0.042 5.9</td>
<td>$7.2^{+3.2}_{-2.0}$</td>
<td>0.27 ...</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
single component in the fits, and therefore its composition is predicted solely by the simulation. While the estimation is insensitive to the composition at first order since the TFs of those physics processes are similar, the residual TF difference can cause a bias in the estimation when the composition is significantly mismodeled by the simulation. The impact of the potential composition mismodeling is evaluated by the variation in the combined TF when shifting the normalization of each physics process up and down by a factor of 2. An uncertainty of about 2–8% is assigned in the 4Q category, while 7–10% is assigned for those in the 2B2Q category.

For the irreducible backgrounds, cross-section uncertainties are assigned to account for their normalization. A 50% uncertainty is quoted for VVVVV production based on the cross-section measurement by the CMS experiment [155], while a 70% normalization uncertainty is assigned to $t\bar{t} + X$ based on the data/MC discrepancy observed in VRTTX, as discussed in Sec. VII.A.

The uncertainty in the signal yields consists of the cross-section uncertainty and the shape uncertainties. The cross-section uncertainty ranges from 6 to 20% for the production of electroweakinos with masses between 400 GeV and 1 TeV, driven mainly by the PDF uncertainty [125]. The shape uncertainties comprise uncertainties in the choice of renormalization/factorization scales and parton shower modeling, affecting the signal acceptance by 5–10%.

IX. RESULTS

A. Statistical analysis

Final background estimates are obtained by performing a profile log-likelihood fit [166] simultaneously in all CRs and

![Exclusion limits for the ($W$, $\tilde{B}$) and ($\tilde{H}$, $\tilde{B}$) models shown as a function of the wino/higgsino chargino mass $m(\tilde{\chi}^±_1)$ and the bino LSP mass $m(\tilde{\chi}^0_1)$. The (a) expected and (b) observed limits for various $B(\tilde{\chi}^0_2 \rightarrow Z\tilde{\chi}^0_1)$ hypotheses are overlaid. The outer and inner bundles correspond to the limits for the ($W$, $\tilde{B}$) and ($\tilde{H}$, $\tilde{B}$) models, respectively. The limits set on the ($\tilde{H}$, $\tilde{B}$) models are highly consistent and thus the contour lines are highly overlapped. Expected (dashed) and observed (solid red) 95% C.L. exclusion limits are shown for the (c) ($W$, $\tilde{B}$) and (d) ($\tilde{H}$, $\tilde{B}$) models with a representative branching ratio $B(\tilde{\chi}^0_2 \rightarrow Z\tilde{\chi}^0_1) = 50%$.](image)
described in Sec. II A, where the mass of binolike LSP (\( \tilde{\chi}_1^0 \)) is (a) half of the Z boson mass (42.6 GeV) or (b) half of the h boson mass (62.5 GeV). The areas surrounded by the green bands or dashed lines represent the excluded range of \( \beta \tan \beta \). The overlaid red solid (blue dashed) line indicates for \( \mu > 0 (\mu < 0) \) the \( \tilde{\chi}_1^0 \) mass that reproduces the observed dark matter relic density (\( \Omega h^2 = 0.12 \)) as function of \( \tan \beta \) [55]; below (above) these lines the predicted dark matter relic density is too small (too large).

\[ \begin{align*}
\tilde{\chi}_1^0 & = m_Z/2 \text{ (Z-funnel)} \\
\tilde{\chi}_1^0 & = m_h/2 \text{ (h-funnel)}
\end{align*} \]

FIG. 13. Expected (dashed green lines) and observed (green band) 95% C.L exclusion limits on the Z/h-funnel dark matter model described in Sec. II A, where the mass of binolike LSP (\( \tilde{\chi}_1^0 \)) is (a) half of the Z boson mass (42.6 GeV) or (b) half of the h boson mass (62.5 GeV). The areas surrounded by the green bands or dashed lines represent the excluded range of \( \beta \tan \beta \). The overlaid red solid (blue dashed) line indicates for \( \mu > 0 (\mu < 0) \) the \( \tilde{\chi}_1^0 \) mass that reproduces the observed dark matter relic density (\( \Omega h^2 = 0.12 \)) as function of \( \tan \beta \) [55]; below (above) these lines the predicted dark matter relic density is too small (too large).

\[ \begin{align*}
\tilde{\chi}_1^0 & = m_Z/2 \text{ (Z-funnel)} \\
\tilde{\chi}_1^0 & = m_h/2 \text{ (h-funnel)}
\end{align*} \]

FIG. 14. 95% C.L. exclusion limits for the \((\tilde{W}, \tilde{H})\) and \((\tilde{H}, \tilde{W})\) models. The limits are projected onto a two-dimensional plane either as a function of the wino/higgsino mass parameters \((M_2, \mu)\) (top figures), or of the physical electroweakino masses \((m(\tilde{\chi}_2^0), m(\tilde{\chi}_1^0))\) representing \((m(\tilde{\chi}_{\text{heavy}}), m(\tilde{\chi}_{\text{light}})))\) (bottom figures). For the limits shown on the \((M_2, \mu)\) plane, the excluded regions are indicated by the area inside the contours. The round excluded area in the top part corresponds to the excluded parameter space in the \((\tilde{W}, \tilde{H})\) model \((M_2 > |\mu|)\), while the two small areas at the bottom are that in the \((\tilde{H}, \tilde{W})\) model \((M_2 < |\mu|)\).
SRs relevant to a given interpretation. The HistFitter [167] framework is employed. Systematic uncertainties are treated as Gaussian-distributed nuisance parameters in the likelihood, while the statistical uncertainties of the MC samples are treated as Poisson-distributed nuisance parameters.

Three types of fit configurations are used to derive the results.

(i) A “background-only fit” is performed considering only the CRs and assuming no contribution from signals. The normalization of the total reducible background is allowed to float and is constrained by the fit using the data in the CRs. The normalization factors and nuisance parameters are adjusted by maximizing the likelihood. Three independent sets of fits are performed in the 0L, 1L, and 1Y categories, respectively. The 4Q and 2B2Q regions in each category are fitted simultaneously, but with independent normalization factors assigned in 4Q and 2B2Q. The normalization factors obtained from the fits range from 0.7 to 1.3.

(ii) A “discovery fit” performs the hypothesis test for a generic beyond-the-SM (BSM) signal, setting upper limits on the number of events and visible cross section for the signal. The fit uses only a single SR and the associated CR0L bin(s), constraining the backgrounds following the same method as in the background-only fit. Any contribution from signals is allowed only in the SR, and the signal-strength parameter is defined to be strictly positive.

(iii) An “exclusion fit” is performed to set the exclusion limit for a given signal model. The SRs and the corresponding CR0L bins are fit simultaneously to determine the reducible background normalization factors and constrain the systematic uncertainties. The signal contamination in CR0L is also taken into account according to the model predictions.

![Exclusion limits for (\tilde{W}, \tilde{B})-SIM as a function of the produced wino mass m(\tilde{\chi}_1^0) and the bino LSP mass m(\tilde{\chi}_1^0). Expected (dashed) and observed (solid) 95% C.L. exclusion limits on (\tilde{W}, \tilde{B}) simplified models are shown for (a) C1C1-WW, (b) C1N2-WZ, and (c) C1N2-Wh. The limits from the previous ATLAS searches on C1C1-WW[23], C1N2-WZ[24], and C1N2-Wh[29] are shown by the shaded areas.](image-url)
For each discovery or exclusion fit, the compatibility of the observed data with the background-only or signal-plus-background hypotheses is quantified by calculating a one-sided \( p \)-value with the profile likelihood ratio used as a test statistic [166]. The upper limits and exclusion are derived using the \( CL_s \) prescription [168] where the 95% confidence level (C.L.) exclusion is defined by \( CL_s < 0.05 \).

**B. Signal region yields**

The observed data yields in each SR and CR0L together with their SM background expectations are summarized in Table V and shown in Fig. 10. No significant excess is found in any of the SRs. The distributions of \( m_{\text{eff}} \) in SR-4Q-VV and \( m_{T2} \) in SR-2B2Q-VZ and SR-2B2Q-Vh are shown in Fig. 11 with some representative signal samples overlaid to illustrate the sensitivity.

**C. Model-independent upper limits**

A discovery fit is performed for each SR to derive the expected and observed 95% C.L. upper limits on the number of BSM signal events \( S_{\text{exp}}^{95} \) and \( S_{\text{obs}}^{95} \) as well as the one-sided \( p \)-value \( (p_0) \) of the background-only hypothesis. Pseudoexperiments with toy MC are used for the calculation. An upper limit on the cross section, \( \langle \epsilon \sigma \rangle_{\text{obs}} \) where \( \epsilon \) represents the efficiency times acceptance of the SR for the given signal, is obtained by dividing \( S_{\text{exp}}^{95} \) by the integrated luminosity. The upper limits and the \( p_0 \) value associated with each SR are summarized in Table VI. Two additional “discovery SRs” are defined in order to set model-independent upper limits in the inclusive phase space. First, Disc-SR-2B2Q is defined as the logical union of SR-2B2Q-VZ and SR-2B2Q-Vh, and then the inclusive discovery signal region Disc-SR-Incl is defined as the logical union of SR-4Q-VV and Disc-SR-2B2Q. When evaluating Disc-SR-Incl, both CR0L-4Q and CR0L-2B2Q are included in the simultaneous fit and each has its own floating normalization factor for the reducible backgrounds.

**D. Model-dependent exclusion limits**

The results are also interpreted in the context of the specific signal models discussed in Sec. II. An exclusion fit is performed for each point in the model space, and a \( CL_s \) value is assigned based on the hypothesis test. The expected and observed 95% C.L. exclusion regions correspond to values of \( CL_s < 0.05 \). Given the large number of models tested, an asymptotic approximation [166] is employed in the \( CL_s \) calculation instead of the full calculation using pseudoexperiments. The validity is checked and the \( CL_s \) values of the two methods typically agree within 5%, and maximally within 10%.

The SRs participating in the simultaneous fit vary with the signal model being tested, as summarized in Table I. CR0L-4Q (CR0L-2B2Q) is included in the fit when at least one SR-4Q (SR-2B2Q) bin is used in deriving the limit, while both of the CR0L bins are included when the SR bins from both SR-4Q and SR-2B2Q participate in the fit.

1. **Exclusion limits on \((W, \tilde{B}), (\tilde{H}, \tilde{B}), (W, \tilde{H}), \) and \((\tilde{H}, \tilde{W})\) models**

The exclusion limits on the \((W, \tilde{B})\) and \((\tilde{H}, \tilde{B})\) models are summarized in Fig. 12. As discussed in Sec. II A, different \( B(\tilde{\chi}_0^0 \to Z \tilde{\chi}_0^0) \) hypotheses are examined, and these are shown to result in very similar limits in Figs. 12(a) and 12(b). The expected and observed limits for a representative slice \( B(\tilde{\chi}_0^0 \to Z \tilde{\chi}_0^0) = 50\% \) are shown in Figs. 12(c) and 12(d), for \((W, \tilde{B})\) and \((\tilde{H}, \tilde{B})\) models respectively.

The \((\tilde{H}, \tilde{B})\) limits are also interpreted for the \(Z/\tilde{h}\)-funnel dark matter model described in Sec. II A. The exclusion limits are shown in Fig. 13, overlaid with theoretical predictions of higgsino masses (\(m_{\tilde{\chi}}\)) reproducing the observed dark matter relic density (\(\Omega h^2 = 0.12\)) [55]. While the relic density depends drastically on \(\tan \beta\), the exclusion limits obtained by the search are assumed to be constant along \(\tan \beta\) since they do not change when varying \(B(\tilde{\chi}_0^0 \to Z \tilde{\chi}_0^0)\), and are interpreted from the exclusion limits for the \(B(\tilde{\chi}_0^0 \to Z \tilde{\chi}_0^0) = 50\% \) hypothesis in Fig. 12(d). For the \(h\)-funnel case, where \(m(\tilde{\chi}_0^0) = m_h/2\), the excluded regions are \(\tan \beta > 8.5\) for \(\mu > 0\) and \(5.5 < \tan \beta < 7\) for \(\mu < 0\).

The exclusion limits set on the \((W, \tilde{H})\) and \((\tilde{H}, \tilde{W})\) models are evaluated in a three-dimensional model space defined by \((M_2, \mu, \tan \beta)\). For each model point, the mass spectra and the branching ratios are determined using the...
prescription described in Sec. II A. Figure 14(a) shows the expected limit and observed limit as a function of \((M_2, \mu)\) with a fixed \(\tan \beta = 10\). Figure 14(b) shows that varying \(\tan \beta\) or the sign of \(\mu\) (sign(\(\mu\))) has very little effect on the sensitivity. The limits are also interpreted as a function of the physical electroweakino masses so that they can be directly compared with the other models. For a given set of \(\langle \tan \beta, \text{sign}(\mu)\rangle\), a pair of \((M_2, |\mu|)\) can be projected one to one to \((m(\tilde{\chi}^0_\pm), m(\tilde{\chi}^0_0))\) when all the other MSSM parameters are fixed. Figure 14(c) and Figure 14(d) show the limits for the \((\tilde{W}, \tilde{H})\) model \((M_2 > |\mu|)\) and \((\tilde{H}, \tilde{W})\) model \((M_2 < |\mu|)\), respectively, assuming \(\tan \beta = 10\) and \(\mu > 0\).

The mass exclusion limits are shown to be highly stable with respect to the internal variations within each model. The limits for \((\tilde{W}, \tilde{B})\) and \((\tilde{W}, \tilde{H})\) (or for \((\tilde{H}, \tilde{B})\) and \((\tilde{H}, \tilde{W})\)) are also very similar, despite the branching ratios of \(\tilde{\chi}\) being substantially different between the models. This model dependency is small mostly due to the statistical combination of SR-4Q and SR-2B2Q, and the inclusive SR bins (SR-4Q-VV, SR-2B2Q-VZ, and SR-2B2Q-Vh), which are designed to be agnostic with regard to the difference between \(W\) and \(Z\) bosons.

To summarize, a wino mass between 400 and 1060 GeV is excluded for the wino production models for \(m(\tilde{\chi}^0_1) < 400\) GeV; and a higgsino mass between 450 and 900 GeV is excluded for the higgsino production models for \(m(\tilde{\chi}^0_1) < 240\) GeV.

2. Exclusion limits on \((\tilde{W}, \tilde{B})\)-SIM

The exclusion limits for the \((\tilde{W}, \tilde{B})\) simplified models (C1C1-WW, C1N2-WZ, and C1N2-Wh) are also derived, in order to directly compare the search sensitivity with the previous ATLAS analyses. Figure 15 shows the obtained exclusion as a function of the produced wino mass \(m(\tilde{\chi}^0_1/\tilde{\chi}^0_1)\) and the bino LSP mass \(m(\tilde{\chi}^0_1)\). For C1C1-WW, \(m(\tilde{\chi}^0_1/\tilde{\chi}^0_1)\) between 630 and 760 GeV is excluded for \(m(\tilde{\chi}^0_1) < 80\) GeV. For C1N2-WZ (C1N2-Wh), \(m(\tilde{\chi}^0_1/\tilde{\chi}^0_1)\) between 440 and 960 GeV (400 and 1060 GeV) is excluded for \(m(\tilde{\chi}^0_1) < 300\) GeV (420 GeV).\(^{13}\)

The sensitivity to high-mass winos is significantly improved relative to ATLAS searches using the other final states and the same dataset. For example, the expected limits on C1N2-WZ (C1N2-Wh) are typically extended by about 300 (140) GeV in \(m(\tilde{\chi}^0_1/\tilde{\chi}^0_1)\), corresponding to exclusion of signals with a 7.5 (2.4) times smaller production cross section than in the search using final states with three leptons [24] (one lepton and two \(b\) jets [29]). This result also sets the most stringent limit on the model to date from the LHC experiments.

3. Exclusion limits on \((\tilde{H}, \tilde{G})\) model

The exclusion for the \((\tilde{H}, \tilde{G})\) model is presented in Fig. 16, as the function of the mass of the lightest higgsino, \(m(\tilde{\chi}^0_1)\), and the branching ratio \(B(\tilde{\chi}^0_1 \rightarrow Z \tilde{G})\). For \(B(\tilde{\chi}^0_1 \rightarrow Z \tilde{G}) = 100\% (50\%)\), \(m(\tilde{\chi}^0_1)\) between 450 (500) and 940 (850) GeV is excluded, while the exclusion reaches \(B(\tilde{\chi}^0_1 \rightarrow Z \tilde{G}) \sim 20\%\) for \(m(\tilde{\chi}^0_1) \sim 600\) GeV. This complements the sensitivity achieved by previous ATLAS searches using four-lepton final states to target signals with decays

\(^{13}\) The obtained limits are generally weaker than those set on the \((\tilde{W}, \tilde{B})\) model shown in Sec. IX D 1. This is because only one production mode is considered in these simplified models, while multiple production modes are included in the signals in the \((\tilde{W}, \tilde{B})\) model.
into ZZ [30] and final states with three or more $b$ jets to target signals with decays into $hh$ [37].

4. Exclusion limits on $(\tilde{H}, \tilde{a})$ model

Lastly, Fig. 17 shows the exclusion limits on the $(\tilde{H}, \tilde{a})$ model as the function of the mass of the axino, $m(\tilde{a})$, and the lightest higgsino, $m(\tilde{h}^0)$. Similarly to the $(\tilde{H}, \tilde{G})$ model, different branching ratio hypotheses of $B(\tilde{H}^0_1 \rightarrow Z\tilde{a})(=1 - B(\tilde{H}^0_1 \rightarrow h\tilde{a}))$ are tested. For $B(\tilde{H}^0_1 \rightarrow Z\tilde{a}) = 100\%$, a higgsino mass between 450 and 940 GeV is excluded when the axino mass is less than 300 GeV. The sensitivity decreases with decreasing $B(\tilde{H}^0_1 \rightarrow Z\tilde{a})$. For $B(\tilde{H}^0_1 \rightarrow Z\tilde{a}) = 50\%$, the observed limit excludes higgsino masses of 500–850 GeV when the axino mass is less than 210 GeV.

X. CONCLUSION

A search for electroweakino pair production using final states consisting of $E_T^{\text{miss}}$ and two boosted hadronically decaying heavy SM bosons ($W$, $Z$, or $h$) is reported. Signatures with large mass splitting between the produced electroweakino and the lightest SUSY particle are targeted.

The use of fully hadronic final states takes advantage of the large SM boson branching ratios, while the backgrounds are efficiently suppressed by reconstructing the $W$, $Z$, and $h$ bosons using boosted boson-tagging techniques. Using 139 fb$^{-1}$ of proton-proton collision data at $\sqrt{s} = 13$ TeV recorded by the ATLAS detector at the LHC, this strategy provides unprecedented sensitivity to the production of heavy electroweakinos.

No excess over the SM background prediction is observed, and 95% C.L. exclusion limits are set for signal models in various $R$-parity conserving scenarios. For wino pair production with direct decays into a bino or higgsino LSP, wino masses between 400 and 1060 GeV are excluded when the LSP mass is below 400 GeV and the mass splitting is larger than 400 GeV. For higgsino pair production with direct decays into a bino or wino LSP, higgsino masses between 450 and 900 GeV are excluded when the LSP mass is below 240 GeV and the mass splitting is larger than 450 GeV. The limits are also examined for various wino (higgsino) branching ratio assumptions, by directly scanning over relevant branching ratios (for the bino LSP models) or over the MSSM parameters that dictate them ($M_2$, $\mu$, and $\tan\beta$ for the wino/higgsino LSP models). The results are shown to be highly consistent for the variations.

The results are also interpreted in the context of simplified models of wino production with decays into a bino LSP, which are more conventionally explored in electroweakino searches at the LHC. For chargino pair production, with each decaying into a $W$ boson and an LSP, a chargino mass between 630 and 760 GeV is excluded for a LSP mass below 80 GeV. For chargino-neutralino pair production involving decays into $WZ$ ($Wh$) and two LSPs, a wino mass between 440 (400) and 960 (1060) GeV is excluded for a LSP mass below 300 (420) GeV. These extend significantly beyond the exclusion limits set by the previous searches at the LHC using different final states.

Finally, exclusion limits are set on higgsino production with decays into a massless gravitino LSP or a massless/massive axino LSP, motivated by the GGM or new physics models involving the axion, respectively. A higgsino mass between 450 (500) and 940 (850) GeV is excluded for the gravitino LSP model with $B(\tilde{H}^0_1 \rightarrow Z\tilde{G}) = 100\%$ (50\%), and a mass between 450 (500) and 940 (850) GeV is excluded for the axino LSP model with $B(\tilde{H}^0_1 \rightarrow Z\tilde{G}) = 100\%$ (50\%) when the axino LSP mass is below 300 (210) GeV.

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