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ABSTRACT

The distribution and kinematics of the circumstellar medium (CSM) around a supernova remnant (SNR) tell us useful information about the explosion of its natal supernova (SN). Kepler’s SNR, the remnant of SN1604, is widely regarded to be of Type Ia origin. Its shock is moving through a dense, asymmetric CSM. The presence of this dense gas suggests that its parent progenitor system consisted of a white dwarf and an asymptotic giant branch (AGB) star. In this paper, we analyze a new and long observation with the reflection grating spectrometers (RGS) on board the XMM-Newton satellite, spatially resolving the remnant emission in the cross-dispersion direction. We find that the CSM component is blue-shifted with velocities in the general range 0–500 km s\(^{-1}\). We also derive information on the central bar structure and find that the northwest half is blue-shifted, while the southeast half is red-shifted. Our result is consistent with a picture proposed by previous studies, in which a “runaway” AGB star moved to the north-northwest and toward us in the line of sight, although it is acceptable for both single-degenerate and core-degenerate scenarios for the progenitor system.

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1. INTRODUCTION

Kepler’s supernova remnant (SNR) is the remnant of SN 1604 (Baade 1943), the last naked-eye Galactic supernova and named after Johannes Kepler, who wrote a monograph on the appearance and the brightness evolution of this new star. Kepler’s SNR is one of the best studied SNRs across the electromagnetic spectrum (see Vink 2017, for a review). Like the similarly aged SN 1572/Tycho’s SNR (see Decourchelle 2017, for a review), Kepler’s SNR is identified as the remnant of a Type Ia supernova (Kimugasa & Tsunemi 1999; Reynolds et al. 2007; Badenes et al. 2006). Unlike the remnant of SN 1572, Kepler’s SNR is not spherically symmetric (Lopez et al. 2011). The probable reason is that the progenitor system for SN 1604 was a runaway system, and the SNR is interacting with a bow-shock shaped shell concentrated toward the northwest, created by the interaction of a stellar wind from the moving progenitor system with the local, tenuous interstellar medium. The evidence for this was first reported by van den Bergh & Kamper (1977); Bandiera & van den Bergh (1991), who found that the optical emission from dense knots has an overall proper motion of \( \sim 200 \text{ km s}^{-1} \) out of the Galactic plane, whereas narrow-line H\( \alpha \) emission shows blueshifts of around 180 km s\(^{-1}\) (Blair et al. 1991).

The SNR distance was long uncertain, but recent estimates based on the kinematics and the historical light curve suggest a distance of \( \approx 5 \pm 1 \text{ kpc} \) (Vink 2017; Ruiz-Lapuente 2017; Sankrit et al. 2016), implying a height above the Galactic plane of \( \approx 594 d_5 \text{ pc} \) — with \( d_5 \) the distance in units of 5 kpc. The velocity of the progenitor system resulted in a density that is highest in the northwestern region, where the SNR blast wave has indeed slowed down considerably (Vink 2008; Katsuda et al. 2008).

The presence of nitrogen-rich material was initially interpreted as due to the wind of a massive star (Bandiera 1987; Borkowski et al. 1992). But the over-abundance of iron-rich ejecta, and lack of oxygen-rich ejecta as seen in the X-ray band (Kimugasa & Tsunemi 1999; Reynolds et al. 2007) clearly suggest a Type Ia origin. There are two main scenarios for the progenitor systems for Type Ia supernova explosions. One is the single degenerate (SD) scenario, for which the binary progenitor system consists of a C+O white dwarf (WD) and a non-degenerate star, for example an asymptotic giant branch (AGB) star (Whelan & Iben 1973; Nomoto 1982; Han & Podsiadlowski 2004). Due to a mass transfer, the mass of the WD is increased to near the Chandrasekhar mass \( (\sim 1.4 M_\odot) \), which results in high density core, initiating a thermonuclear explosion. The other scenario is the double degenerate (DD) scenario. According to this scenario the progenitor system consists of a WD-WD binary. The explosion is initiated when the WDs merge due to orbital energy loss caused by gravitational wave emission (Iben & Tutukov 1984; Webbink 1984). A third scenario that is sometimes discussed is the so-called core degenerate (CD) scenario, which is somewhat intermediate between the SD and DD scenarios. It involves the merger of a WD and an AGB core in a WD-AGB binary system (Livio & Riess 2003; Ilkov & Soker 2012; Kashi & Soker 2011).

The presence of a dense shell at \( \sim 600 \text{ pc} \) above the Galactic plane, which is not only rich in nitrogen, but also silicate-rich dust grains (Douvion et al. 2001; Williams et al. 2012), suggests that the SN 1604 progenitor system consisted of a “runaway” system containing a WD and an AGB
star. This model was explored by 2D (Velázquez et al. 2006; Chiotellis et al. 2012; Burkey et al. 2013) and a 3D (Toledo-Roy et al. 2014) hydrodynamical simulations. Silicate-rich dust is typically produced by relatively massive AGB stars (\( \gtrsim 4 M_\odot \), e.g. Karakas 2010). However, the core of the AGB donor star is expected to survive the Type Ia explosion, which is at odds with the lack of bright stars near the explosion centre in Kepler’s SNR (Kerzendorf et al. 2014; Ruiz-Lapuente et al. 2018). This puts Kepler’s SNR in a similar situation as other Type Ia SNRs: Tycho’s SNR, SNR 0509-675, and SN 1006 (Kerzendorf et al. 2013; Schaefer & Pagnotta 2012; González Hernández et al. 2012), namely favouring a DD-scenario progenitor, if it were not for the CSM structure and composition. More recently, Chiotellis et al. (2020) simulated Kepler’s SNR assuming a CD scenario, in which the short-lived double degenerate system merges while still situated within the planetary nebula created by the AGB star. This scenario also explains the “ears” in the north-west and south-east of the remnant, but also retains the bowshock shaped region due to proper motion of the progenitor system (Tsebrenko & Soker 2013; Chiotellis et al. 2021).

For a better understanding of the supernova explosion and interaction with the CSM, we need to explore in more detail the kinematics. In X-rays, kinematic studies have concentrated either on the proper motions (Vink 2008; Katsuda et al. 2008), rather than on the line of sight motions (Kasuga et al. 2018). Recently, a study was published combining the proper motions of individual bright X-ray knots, with Doppler measurements obtained from Chandra ACIS-S data (Sato & Hughes 2017) and HETGS data (Millard et al. 2020). However, the dispersion angle of the HETGS does not allow to study the Doppler shifts and Doppler broadening from the SNR in its entirety.

Here we explore the data of Kepler’s SNR obtained with the Reflection Grating Spectrometers (RGS) (den Herder et al. 2001) on board the XMM-Newton satellite (Jansen et al. 2001). The spectra are suitable for decomposing detailed line features in the lower X-ray energy band, including CSM emission lines. A detailed analysis of the RGS data for Kepler’s SNR was carried out by Katsuda et al. (2015). Here we follow-up on this study, by using deeper RGS observations. Apart from obtaining a better view of the net Doppler shifts of both the ejecta and CSM components, the Doppler broadening provides additional information on both the kinematics and thermal + turbulent Doppler broadening, which yields constraints on the ion temperature.

This paper is structured as follows. Section 2 describes the observation information and data reduction process. Section 3 explains the details of our analysis including the process of dividing regions and fitting models. Finally, section 4 discusses our results concerning mainly to the kinematics of CSM.

2. OBSERVATIONS

Table 1 shows a list of RGS observations of Kepler’s SNR. Because the difference of the roll angle is too large to allow the observations to be merged and the cross-dispersion directions do not correspond to the same portions of Kepler’s SNR, we only use the longest observation 0842550101 in this paper. This observation shows almost no background flares in its light curve, so the full exposure is available for science. We also use a blank-sky observation 0051940401 as the detector background for our analysis due to the brightness and extent of the source. All observation data are screened by cifbuild and odfingest commands in the SAS 18.0.0 package (Gabriel et al. 2004). In order to divide the analysis regions and create spectral response files, we use the ACIS-S image in the 470–860 eV (14.4–26.4 Å) band obtained with the Chandra satellite (Garmire et al. 2003) in 2006 (Obs.
Table 1. RGS observation table

<table>
<thead>
<tr>
<th>Target</th>
<th>Obs. ID</th>
<th>Time</th>
<th>Position</th>
<th>Roll angle</th>
<th>Exposure</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
<td>(RA,dec)</td>
<td>(deg)</td>
<td>(ksec)</td>
</tr>
<tr>
<td>Kepler’s SNR</td>
<td>0084100101</td>
<td>Mar. 2001</td>
<td>(262.67499, -21.491667)</td>
<td>94.71</td>
<td>31.7</td>
</tr>
<tr>
<td>Kepler’s SNR</td>
<td>0853790101</td>
<td>Mar. 2020</td>
<td>(262.67499, -21.491667)</td>
<td>94.68</td>
<td>37.0</td>
</tr>
<tr>
<td>Kepler’s SNR (This Work)</td>
<td>0842550101</td>
<td>Mar. 2020</td>
<td>(262.65359, -21.500305)</td>
<td>92.67</td>
<td>132.0</td>
</tr>
<tr>
<td>Background (This Work)</td>
<td>0051940401</td>
<td>Mar. 2001</td>
<td>(277.10040, -11.826722)</td>
<td>92.36</td>
<td>9.8</td>
</tr>
</tbody>
</table>

Note—The roll angle is the averaged value of those of both RGS detectors because they are \( \sim 0.15 \) degree different from each other.

ID: 6714–6718 and 7366), which we reprocessed using the chandra_repro command and merged using merge_obs from the CIAO 4.9 package (Fruscione et al. 2006).

3. SPECTRAL ANALYSIS AND RESULTS

3.1. Regions and reprocessing

For spatially resolved spectroscopy, we divide the field of view along the dispersion angle of the RGS. The events detected along the dispersion angle contain a mix of positional information and incident photon energy. The extraction regions perpendicular to the dispersion axis contain information from several, independent strips covering the SNR. Figure 1 (a) shows the 6 strips of our analysis, where we consider various geometric features of the SNR and the \( \sim 5 \) arcsec angular resolution of the XMM-Newton telescopes (Jansen et al. 2001). We identify each strip by name and classify them into 3 groups. Strip N*s include the northern bright rim of the remnant. The central bar structure lies in strip C*s, but strip CS also has an edge structure in the western half. The strip S represents the dark southern structure. Note that the effects of vignetting by the XMM-Newton telescopes is less than 5%, given that the diameter of Kepler’s SNR is \( \sim 4 \) arcmin. Therefore we ignore vignetting in our analysis.

To reprocess the XMM-Newton observation, we use the rgsproc command in SAS. For extracting events in each strip, we consider the slight difference of the pointing center of the two RGS detectors, which cannot be ignored for such a source distribution as complicated as that of Kepler’s SNR. Figure 1 (b) shows the strip division on the RGS raw images after accounting for the pointing shift. We extract events in the energy band 470–860 eV, which includes the CSM-indicator line emission (N Ly\( \alpha \)), CSM-dominated lines (O He\( \alpha \) & O Ly\( \alpha \)), and ejecta-dominated lines (Fe-L lines). Note that we exclude the Ne and Mg lines because their energy band could include more complicated ejecta components (see Figure 2 in Katsuda et al. 2015). We sum up the spectra in the 1st order from each RGS detector. We exclude some bad spectral bins with extremely poor photon statistics, due to bad CCD pixels of the RGS detectors.

3.2. Fitting results

We fit the spectra using the Xspec 12.9.1 software package (Arnaud 1996) with AtomDB 3.0.8 (Foster et al. 2012). Because un-binned spectra are used, we optimise the emission models using the W-statistic, which is a modification of the C-statistic (Kaastra 2017) that Xspec automatically
Figure 1. (a) Analysis strips on the Chandra ACIS-S image of Kepler’s SNR in linear scale. The blue and red represent the CSM band (470–600 eV) and the ejecta (Fe-L: 700–860 eV), respectively. Notice that the O Lyα line is not included in both of them. The yellow, cyan, and white color mean distinction of the proposal value and the actual values of both RGS detectors. The squares and vertical lines represent their pointing position and cross dispersion axes, respectively. The green horizontal lines represent dividing positions of each strips and the yellow values are their cross dispersion angle on the proposal axis, whose roll angle is shown in Table 1. (b) Strips on the both RGS images. Both color scales are linear in order to emphasize the spacial distribution of the brightness.
Figure 2. Fitting Results in the northern strips. Blue lines are \textit{vpshock} components representing CSM, and red lines are \textit{vnei} of ejecta. Magenta lines are the PL component. Green lines are the sum of them, and lower panels show the residual of our fitting, which we calculate the values of \((\text{data-model})/\text{error}\) in W-statistics (Kaastra 2017).
adopts when including background data. The fitting model consists of two optically thin thermal emission models, \texttt{vpshock} for the CSM component, with the initial value of the ionization timescale $n_e t$ is set to 0, and \texttt{vnei} for the ejecta component (Borkowski et al. 2001). Because the detector response created by \texttt{rgsrmmgen} command in \textsc{sas} is for a point source, we convolve the response with the spatial emission profile along each dispersion region, by employing the \texttt{rgsrmsmooth} command in the \textsc{Heasoft 6.21} package (Blackburn 1995). As input images, we use \textit{Chandra} images for each emission component: 460–600 eV for the CSM and 700–860 eV for the ejecta component (Figure 1 (a)). For the CSM component we adopt solar abundances, except for nitrogen, which is allowed to be optimised. For the ejecta component we use pure metal abundances, following the previous study of Katsuda et al. (2015).

Each of these two components are Doppler shifted using the \texttt{vashift} model, to account for bulk velocities along the line-of-sight directions. The red-shift parameters of the \texttt{vpshock} and \texttt{vnei} models are set to be 0, because non-zero redshifts include cosmological effects that affect the model normalisation parameters. Both components are also each broadened with the \texttt{gsmooth} model, to account for both the thermal Doppler broadening and the spread in plasma velocities along the line-of-sight in each strip. Note that the interpretation of the ionization time scale in the fitting models between \texttt{vpshock} and \texttt{vnei} is different. In the \texttt{vpshock} model there is a linear distribution of ionisation ages ($n_e t$), whereas the \texttt{vnei} model assumes a single ionisation age for the entire plasma (Borkowski et al. 2001).

Concerning the element abundances, we assume that N emission originates solely from the CSM component, so we allow only the N abundance to be free for the CSM component; the other abundances are set to their solar values (Wilms et al. 2000). The N abundance of the ejecta component is fixed to 0. Because we assume the pure-metal ejecta, we set abundance ratios to H for the intermediate mass elements (Si, S, Ar, and Ca) to be fixed to $10^5$, the iron-group elements (Fe and Ni) to be free near $10^5$, and treated O, Ne, and Mg abundances as free parameters. Note that the K-shell emission lines of the intermediate mass elements are outside the RGS spectral band. We also include a Power Law component (PL) for the synchrotron radiation, which is thought to be the dominant component of the non-thermal continuum emission in this energy band (Nagayoshi et al. 2021). The PL photon index is defined as $\Gamma$, where the differential number of photons goes as $N(E) \propto E^{-\Gamma}$ as a function of energy $E$. In this paper, $\Gamma$ is fixed to 2.64, the best-fit value in Katsuda et al. (2015), which is also broadly consistent with the results of other studies (2.2–2.6 in Bamba et al. 2005, 2.60 in Park et al. 2013, and 2.63$\pm 0.04$ in Nagayoshi et al. 2021). Finally, the interstellar absorption is modelled with the \texttt{tbabs} model (Wilms et al. 2000), and is applied to all model components. Because there is some discrepancy in published values for the absorption column density $N_H$ toward Kepler’s SNR (for example, $N_H = 5.2 \times 10^{21} \text{ cm}^{-2}$ in Reynolds et al. 2007 and $6.4 \times 10^{21} \text{ cm}^{-2}$ in Katsuda et al. 2015), we set $N_H$ to be a free parameter. In summary, our fitting model is $\texttt{tbabs* (vashift*gsmooth*vpshock + vashift*gsmooth*vnei + PL)}$.

Figure 2 shows our fitted results for each extracted strip. The lower panels show the (data-model)/error value, i.e. the fitting residuals, which in general show no obvious feature except for strip CS. These results indicate that our fitting model well-reproduces the observational data, with a relatively simple model in which the CSM and ejecta emission is each represented with a single non-equilibrium ionisation emission model. Note that, as a check, we also fitted the entire RGS energy band (0.4–2.5 keV). The main results in the strips with more compact emission features
(NC, NS, and CN) are consistent with the results for the narrower energy band (Table 2). Fits for the other strips are unreliable especially in the narrow energy band we focus here, which may be due to the complicated structure of them for such a 1-D detector.

3.3. Strip CS

![Figure 3.](image)

**Figure 3.** (a) Yellow dashed line represents the division boundary between the west and east halves of the remnant. (b) Fitting results in the strip CS with the improved model. Dashed lines represent the components from west half and dots do east. Other legends are same as Figure 2.

As shown in Figure 2, we found that the line shape of the O Lyα in CS is not well reproduced by the model explained above. This strip obviously includes both the central bar-like structure and the western side of the main shell (Figure 1). We therefore applied another model particularly for the CS strip, where the RGS spectrum is fitted with a model assuming the superposition of two spatially-distinct components. Specifically we use the combination of \( \text{vpshock} \) for CSM at the center, \( \text{vpshock} \) for CSM at the rim, \( \text{vnei} \) for ejecta at the center, and \( \text{vnei} \) for ejecta at the rim. The Doppler parameters (the line-of-sight velocity and the line width) are set to be independent parameters, but the other parameters are forced to be the same. We set the normalization parameters to be coupled between the western and the central parts. This procedure also requires that the response matrix take into account the spatial differences corresponding to the central bar and western part of the shell. To accomplish this, we split the image of Kepler’s SNR (Figure 3 (a)) into two, one for the western and one for the eastern half. We use the western-half image for the spatial-part of the detector response of the outer rim component and the eastern-half image for the central bar detector response (cf., Katsuda et al. (2013)). Figure 3 (b) shows the model fitting results for this more elaborate, two-spatial-component model. Compared to the previous result (Figure 2), the residuals near the peak of the O Lyα emission are considerably reduced. The fits are much better with the \( \text{W-stat} \)
Figure 4. Results of the free parameters of our fitting with $1\sigma$ confidential level. The horizontal axis is the cross-dispersion angle in the unit of arcsec, which is shown in Figure 1. (a) Line-of-sight velocity. The positive values mean red-shifted, i.e., moving away from us. The blue points show CSM parameters and red show ejecta ones. The filled square points represent components in the outer rim and outlined triangle points do in the central bar. The black solid line means 0 km s$^{-1}$. For the strip CS, we distinguish the plots from the west and east halves. (b) Same but line width $\sigma$ converted at 1 keV. (c) Electron temperature $kT_e$ of vphock and vnei models. (d) Same but ionization parameter $n_e t$.

(d.o.f) values improved from 1641.43 (1131) to 1323.61 (1127), and with the F-test probability is much lower than 0.01 based on the chi-square values. The best-fit parameter table (Table 2) and plots (Figure 4) include these additional analyses.
Table 2. Best-fit parameters

<table>
<thead>
<tr>
<th>Region</th>
<th>NN</th>
<th>NC</th>
<th>NS</th>
<th>CN</th>
<th>CS-E</th>
<th>CS-W</th>
<th>S</th>
</tr>
</thead>
<tbody>
<tr>
<td>CSM</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>velocity (km s(^{-1}))</td>
<td>(-136^{+44}_{-109})</td>
<td>(-192^{+29}_{-29})</td>
<td>(-419^{+38}_{-41})</td>
<td>(-562^{+36}_{-56})</td>
<td>(738^{+75}_{-60})</td>
<td>(-539^{+280}_{-290})</td>
<td>(-86^{+135}_{-160})</td>
</tr>
<tr>
<td>line width (\sigma) (eV @ 1 keV)</td>
<td>(6.3^{+0.1}_{-0.4})</td>
<td>(1.4^{+0.2}_{-0.2})</td>
<td>(3.6^{+0.2}_{-0.2})</td>
<td>(2.1^{+0.3}_{-0.2})</td>
<td>(2.3^{+0.3}_{-0.3})</td>
<td>(5.2^{+0.6}_{-0.6})</td>
<td>(7.9^{+0.7}_{-0.6})</td>
</tr>
<tr>
<td>(kT_e) (keV)</td>
<td>(0.85^{+0.10}_{-0.09})</td>
<td>(0.51^{+0.07}_{-0.05})</td>
<td>(0.58^{+0.06}_{-0.04})</td>
<td>(0.66^{+0.10}_{-0.04})</td>
<td>(0.90^{+0.11}_{-0.22})</td>
<td>(0.91^{+0.28}_{-0.17})</td>
<td>(0.91^{+0.28}_{-0.17})</td>
</tr>
<tr>
<td>(n_e t) (10(^{10}) cm(^{-3}) s)</td>
<td>(5.5^{+1.0}_{-0.8})</td>
<td>(12.9^{+2.5}_{-2.8})</td>
<td>(11.2^{+1.7}_{-2.0})</td>
<td>(7.8^{+1.7}_{-1.5})</td>
<td>(3.9^{+0.8}_{-0.4})</td>
<td>(2.5^{+0.7}_{-0.5})</td>
<td>(2.5^{+0.7}_{-0.5})</td>
</tr>
<tr>
<td>other elements (solar)</td>
<td>(1.51^{+0.18}_{-0.11})</td>
<td>(2.04^{+0.19}_{-0.16})</td>
<td>(1.77^{+0.16}_{-0.16})</td>
<td>(1.41^{+0.14}_{-0.14})</td>
<td>(1.54^{+0.11}_{-0.10})</td>
<td>(0.77^{+0.23}_{-0.23})</td>
<td>(0.77^{+0.23}_{-0.23})</td>
</tr>
<tr>
<td>Ejecta</td>
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<td></td>
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<td></td>
<td></td>
</tr>
<tr>
<td>velocity (km s(^{-1}))</td>
<td>(702^{+33}_{-34})</td>
<td>(532^{+53}_{-47})</td>
<td>(578^{+75}_{-38})</td>
<td>(1805^{+104}_{-63})</td>
<td>(2531^{+280}_{-289})</td>
<td>(-321^{+361}_{-323})</td>
<td>(615^{+61}_{-59})</td>
</tr>
<tr>
<td>line width (\sigma) (eV @ 1 keV)</td>
<td>(9.6^{+0.1}_{-0.1})</td>
<td>(13.9^{+0.3}_{-0.2})</td>
<td>(14.8^{+0.4}_{-0.4})</td>
<td>(12.1^{+0.4}_{-0.4})</td>
<td>(10.6^{+0.7}_{-0.6})</td>
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<td>(kT_e) (keV)</td>
<td>(0.74^{+0.05}_{-0.03})</td>
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<td>(0.56^{+0.04}_{-0.04})</td>
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<td>(n_e t) (10(^{10}) cm(^{-3}) s)</td>
<td>(2.4^{+0.1}_{-0.1})</td>
<td>(2.6^{+0.3}_{-0.2})</td>
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<td>(18.4^{+6.3}_{-3.3})</td>
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<td>1</td>
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<td>1</td>
<td>1</td>
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<tr>
<td>N (solar)</td>
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<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>O,Ne,Mg (10(^3) solar)</td>
<td>&lt; 1.8 &amp; 3.9^{+0.7}<em>{-0.4} \leq 1.3 &amp; 1.5^{+0.5}</em>{-0.6} \leq 0.3 &amp; &lt; 0.3 &amp; &lt; 0.3</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Si,S,Ar,Ca (10(^3) solar)</td>
<td>100</td>
<td>100</td>
<td>100</td>
<td>100</td>
<td>100</td>
<td>100</td>
<td>100</td>
</tr>
<tr>
<td>Fe,Ni (10(^3) solar)</td>
<td>117^{+42}_{-8}</td>
<td>128^{+25}_{-25}</td>
<td>77^{+21}_{-15}</td>
<td>66^{+17}_{-11}</td>
<td>68^{+19}_{-21}</td>
<td>44^{+3}_{-5}</td>
<td></td>
</tr>
<tr>
<td>(n_H) (10(^{21}) cm(^{-2}))</td>
<td>(5.7^{+0.2}_{-0.2})</td>
<td>(5.6^{+0.2}_{-0.2})</td>
<td>(5.5^{+0.2}_{-0.3})</td>
<td>(5.4^{+0.2}_{-0.3})</td>
<td>(5.8^{+0.2}_{-0.1})</td>
<td>(5.3^{+0.1}_{-0.2})</td>
<td>(5.3^{+0.1}_{-0.2})</td>
</tr>
<tr>
<td>W-stat</td>
<td>1681.47</td>
<td>1602.46</td>
<td>1584.98</td>
<td>1410.52</td>
<td>1323.61</td>
<td>1233.72</td>
<td>1233.72</td>
</tr>
<tr>
<td>d.o.f.</td>
<td>1131</td>
<td>1131</td>
<td>1131</td>
<td>1131</td>
<td>1127</td>
<td>1131</td>
<td>1131</td>
</tr>
<tr>
<td>W-stat/d.o.f.</td>
<td>1.487</td>
<td>1.417</td>
<td>1.401</td>
<td>1.247</td>
<td>1.174</td>
<td>1.091</td>
<td>1.091</td>
</tr>
</tbody>
</table>

Note—Notice that the definition of the ionization timescale \(n_e t\) is different in both \(v_p\) and \(v_{\text{nei}}\) models. Almost all parameters except for velocity and line width in the strip CS are linked between the east- and west-halves.
Figure 5. A schematic view of the kinematics of CSM in Kepler’s SNR from diagonally above. The blue or red color surrounded by green line represents the Doppler shift of CSM. Darker color means a larger shifted component. We also add a bow-shock generated by the “runaway” AGB star. The green image is the X-ray image of CSM (same as Figure 1) and colored arrows also mean the Doppler shift at each position.

4. DISCUSSION

The modelling results give us insight in both the velocity structure and composition of the CSM and the ejecta component. Figures 4 (a) and (b) show the Doppler velocities and widths for both these components. For the velocity structure it is important to remember that for a perfectly spherical expanding shell, no net Doppler shift is expected. So any Doppler shift is either due to an overall Doppler shift for the system, which for Kepler is expected to be $230\pm50 \text{ km s}^{-1}$ (Minkowski 1959), or due to deviations from spherical symmetry. At the edges of the expanding shell, all motions are in the plane of the sky, and deviations from spherical symmetry should not play a role — except for cases where the emission comes from a wider region, or if there is some contamination due to the instrumental point spread function.

Doppler widths can have several causes: i) the bulk velocity of the expanding shell, ii) motions from unresolved knots or turbulence, and iii) thermal Doppler shifts. For a spherically expanding shell, the bulk velocity broadening is largest in the center where the line-of-sight motions have maximum approaching and receding components toward the observer. At the edges of the SNR the bulk motion is in the plane of the sky, and hence bulk velocity broadening should be minimal. However, turbulent motions and thermal Doppler broadening should to first order not be dependent on the projected location on the sky.

In particular, thermal Doppler broadening received some attention, as collisionless shocks likely heat the different plasma components to different temperatures, instead of equipartition of temperatures
In the most extreme case the temperatures are given by

\[ kT_i = \frac{3}{16} m_i V_S^2, \]

with \( T_i \) the temperature of a given species \( i \), \( m_i \) the species’ particle mass, and \( V_S \) the shock velocity. Post-shock Coulomb interactions, may then equilibrate the temperatures further downstream of the shock, proportional to \( n_e t \).

Below we will discuss separately the velocity structure and composition of the CSM and ejecta components.

4.1. The circumstellar medium component

4.1.1. Doppler velocity structure

Focusing on CSM velocity parameters at the edge of the remnant, the line-of-sight velocity is fit in the narrow range between 0–500 km s\(^{-1}\) toward us. These results can be generally explained by the bulk motion of the whole remnant. From an observation of some bright optical knots, the radial velocity of the remnant is estimated to be blue-shifted with a velocity of 230±50 km s\(^{-1}\) (Minkowski 1959). Combining the observation of the tangential velocity, Bandiera & van den Bergh (1991) estimated the 3-Dimensional kinematics of the remnant as it moves towards the northwest and in our direction along the line-of-sight with a space velocity of 278±12 km s\(^{-1}\). Previous studies attributed the overall blue-shifts and proper motions to be caused by the stellar wind from a “runaway” star with a large system motion (Bandiera 1987; Borkowski et al. 1992). Original binary system could be like the Mira’s binary, whose velocity is ∼100 km s\(^{-1}\) and who has a bow-shock in the infrared and ultraviolet band (cf., Martin et al. 2007). Such “runaway” massive stars are still found even 600 pc above the galactic plane like Kepler’s position (e.g., Martin 2006).

In the central region, we can see a red-shifted feature in the north-west structure (strip CN) and a blue-shifted structure in the south-east (the east half of strip CS). These results are consistent with the previous optical observation of the H\(\alpha\) lines from CSM knots in this vicinity (Blair et al. 1991). Blair et al. (1991) compared the centroid energy of the broad H\(\alpha\) lines and estimated the difference as ∼20 Å between these CSM knots in the area we are discussing (see Table 3 in Blair et al. 1991). The line widths in these regions are narrower than that in the edge (Figure 4 (b)). These results are explainable by a dense and torus-like CSM, which Burkey et al. (2013) indicated using a hydrodynamical simulation. Such a torus-like CSM is explained by the SD scenario of type Ia SN (Hachisu et al. 2008), and is also found in other SNe and SNRs like SN2012dn (Nagao et al. 2017, 2018) and N103B (Yamaguchi et al. 2021), for example.

Figure 5 shows our interpretation of the velocity structure of the shocked CSM. This figure shows that the bipolar CSM to the north and south with a central dense torus (Burkey et al. 2013) is moving towards the northwest and in our direction. The angle to us out of the sky plane is estimated as ∼35 degree (Bandiera & van den Bergh 1991). Such movement is because of the “runaway” AGB star, which generates a bow-shock in the direction of motion (Borkowski et al. 1992). The blue-shift of the CSM is expected to follow this motion of the bow-shock. Note that the radial velocity is anti-correlated with the density of ISM, for example the northern, bright region moves more slowly (Katsuda et al. 2008). The central torus is along the axis of the motion of the AGB star.

Borkowski et al. (1992); Velázquez et al. (2006); Chiotellis et al. (2012) did 2D-simulations considering a “runaway” AGB star with an isotropic CSM, and Burkey et al. (2013) assumed an anisotropic
CSM in a static system. Combining these ideas, Toledo-Roy et al. (2014) carried out 3D-simulations with both assumptions and succeeded in generating the northern bright structure and the central bar of this remnant, that was visible in its X-ray emission (see Figure 10 in Toledo-Roy et al. (2014)). Future simulations concentrating on the line-of-sight velocity of the CSM could test the validity of this assumption. On the other hand, especially based on the CD scenario, Chiotellis et al. (2020) generated Kepler’s characteristic “ears” (Tsebrenko & Soker 2013) with the northern brightness by the PNe-like CSM formed just before the explosion of a WD with a “runaway” AGB star. Our observed velocity structure in the central region suggest the ears may be a torus-like structure.

Remarkably, the line width of the CSM component peaks in the outer two regions, where we expect the broadening effects of the shell velocities to be minimal. For the northern edge we measured $\sigma = 3.6$ eV at 1 keV. If we interpret the broadening as being purely due to unequilibration of temperatures, the implied shock velocity is $V_s = \sqrt{16/3}\sigma_v \approx 2500$ km s$^{-1}$, which is consistent with the slower proper motions in that region. For the southern part we have $7.9 \pm 0.7$ eV at 1 keV, corresponding to $V_s \approx 5400$ km s$^{-1}$, which is somewhat higher than inferred from the measured proper motion for the southern part of the remnant, $4500d_5$ km s$^{-1}$ (Vink 2008; Katsuda et al. 2008). Note that the line width provides an upper limit to the shock velocity. The relation between ion temperature and velocity dispersion is $kT_i = m_i\sigma_v^2$. So our measurement for the southern part implies for oxygen, $kT_O \approx 900$ keV.

However, it is remarkable that for the more central strips — where we expect bulk motions to contribute more — that the line broadening is much lower, which either requires slower shocks, whether interpreted as bulk motions or thermal broadening, and/or stronger equilibration of ion-electron temperatures. This region is dominated by the bar-like feature in the SNR.

4.1.2. Nitrogen abundance

We confirm the existence of Nitrogen from the CSM components in all strips (Table 2). Our result of the N abundance of CSM is generally 1–2 solar, where Katsuda et al. (2015) indicated $2.91^{+0.36}_{-0.32}$ solar in the whole of the remnant and $6.08^{+3.17}_{-2.75}$ solar in the southern region (see Table 2 in Katsuda et al. 2015). They analyzed the wide-band spectra combined with the old RGS data (Obs. ID 0084100101 in Table 1) and CCD data above 2 keV using the X-Ray Imaging Spectrometer on board Suzaku (Koyama et al. 2007). Nagayoshi et al. (2021) re-analyzed the same datasets by using same fitting models as Katsuda et al. (2015) and their result of N abundance was also smaller than previous one, $1.93^{+0.17}_{-0.15}$ solar (see the appendix and Table 4 in Nagayoshi et al. 2021). They pointed out the reason was the difference of the version of AtomDB used. Nagayoshi et al. (2021) used the latest version AtomDB 3.0.9, whereas Katsuda et al. (2015) used the old version AtomDB 2.0.2. Our work uses AtomDB 3.0.8 and the new, deep RGS data and supports the result from Nagayoshi et al. (2021).

The nitrogen abundance of 1–2 solar translates into an N/O mass ratio of $\approx 0.15–0.3$ for the solar abundance values of Wilms et al. (2000) that we use here. Associating this ratio with the surface abundance ratio in AGB stars as calculated by Karakas & Lugaro (2016) (their Figure 2), the required mass of an AGB star is less than $4 M_\odot$ because the N/O rapidly gets larger than 1 for heavier stars. On the other hand, the presence of silicate dust requires a C/O ratio smaller than 1 (see the discussion in Vink 2017), which is because a carbon excess will result in CO molecule formation instead of silicate dust formation, and this requires an AGB star with $M > 4 M_\odot$ in the models of Karakas & Lugaro (2016). We have here an apparent contradiction. However, note that the N/O and C/O ratios differ considerably between the initial and final thermal pulses. So the
question is whether most of the material encountered by the SNR blastwave so far corresponds to
the first or the final thermal pulses. Another concern is that the models of Karakas & Lugardo (2016)
are for the evolution of single stars, whereas the progenitor system of SN1604 must have been a
binary system. In particular, the CD scenario prescribes a common-envelope phase in the progenitor
evolution, which may result in different relations for the N/O and C/O ratios as a function of the
initial mass of the AGB star. Notice that in the strip S, the N abundance is lower than 1 solar.
Considering the small equivalent width of the N line (Figure 2) and the wide line width (Figure 4
(b)), we may observe the mixture of CSM and ISM there.

4.2. The ejecta component

4.2.1. The Doppler velocity structure

Table 2 also includes the results for the Doppler shifts and Doppler widths for the ejecta component.
For the RGS this component is mainly associated with the Fe-L line emission. In contrast to the
CSM, the ejecta velocity parameters imply that the ejecta are receding from the observer. This is in
qualitative agreement with the analysis of radial velocities of bright Si ejecta knots in Kepler’s SNR
from Sato & Hughes (2017) and Millard et al. (2020), who found several knots moving with high
velocity, approaching 10,000 km s$^{-1}$. However, the velocities reported here are much less than this.
This may reflect the different nature of the features under study. The compact knots seen by Chandra
are isolated and their lack of deceleration may be due to their motion through low density gaps in
the CSM (see discussion in Sato & Hughes 2017). The results reported here pertain to large sections
of the SNR, which include a mix of ejecta velocities, both from the front and backside of the shell
and likely include material encountering more typical, higher density regions of the CSM. Apart from
the NS and CS strip, the Doppler velocities are below 1000 km s$^{-1}$. The highest velocity measured is
$\approx 2500$ km s$^{-1}$ for the east component of the CS strip, which corresponds to the central bar. Given
that the shell is approximately moving at 75% of the shock velocity expected for a high Mach number
shock, we expect shell velocities of roughly 1500–3500 km s$^{-1}$ based on the overall proper motion
measurements (Katsuda et al. 2008; Vink 2008), in agreement with the highest Doppler velocity
report here. The redshift means that the central bar is on average moving away from us, implying
that it is located on the far side of the SNR.

For the central bar, Kasuga et al. (2018) found diffuse Fe-K structures whose centroid energy is
lower than that of the neutral Fe line at 6.4 keV, especially in the east half of the strip CS. The
energy shifts imply a velocity of $\sim 2000$ km s$^{-1}$, consistent with this work. In contrast, the RGS
result shows that the Fe-L ejecta in the western half of the strip CS is the only blue-shifted feature.
This is in agreement with previous studies concerning the Si ejecta knots (Sato & Hughes 2017) and
Fe-K bulk structure (Kasuga et al. 2018), which found higher centroid energies in this location. In
fact, Sato et al. (2020) found a large structure of Fe ejecta that moves towards us (see Figure 12 in
Sato et al. 2020). It may be surprising to find an overall redshift for the ejecta component, whereas
the CSM component appears to be blueshifted. One possible explanation is that a higher density
of the CSM on the near-side of the SNR may trigger an earlier response of the reverse shock, and
result in general in slower expansion of the ejecta, whereas at the far-side the ejecta is moving faster,
resulting in a net redshift. The contrast in densities on the near- and far-side could be the result of
the overall angle of the bow-shock shaped structure created by the stellar wind from the progenitor
system, which is tilted toward us, given the reported overall blueshifts of the CSM. But an additional
geometrical axis to be considered is that of a possible bipolar wind from the progenitor system, whose axis may not be aligned with the overall direction of the progenitor motion.

There may be additional factors at play. For example, Reynoso & Goss (1999) found extended HI emission—which is thought to be an indicator of ISM—at the back side of this SNR. We should, however, be cautious as the nature of the RGS only allows us to resolve only one spatial direction (north to south), which leaves us with uncertainty about the other direction (east to west). In the future, X-ray calorimeters (Kelley et al. 2016) enable us to observe with 2-Dimensional angular resolution using the Resolve detector (Ishisaki et al. 2018) on board the XRISM (Tashiro et al. 2018), the X-IFU (Barret et al. 2018) on the Athena+ (Nandra et al. 2013), and the LXM on the Lynx satellite (Bandler et al. 2019). Such detectors will help us to analyze the line-of-sight kinematics of not only the CSM components but also ejecta in detail without the current limitation on spatially-resolved spectroscopy.

The line broadening of the ejecta component is substantially larger than for the CSM component: ≈ 9.6–15.6 eV at 1 keV, corresponding to \( \sigma_v \approx 2850–4650 \text{ km s}^{-1} \). Here the expectation is satisfied that the line broadening should be largest in the central regions where the line of sight speeds are maximised for an expanding spherical shell. So very likely, the width provides constraints on the expansion velocity of the ejecta shell. The proper motions indicate shock velocities of 2000–4500 km s\(^{-1}\), and the maximum plasma velocities are expected to have a similar range (c.f., models in Chevalier 1982). The values of \( \sigma_v \) are also larger than the velocity shifts, indicating that indeed we have a more or less complete shell, but may have emission differences between the back and front sides of the shell. There is also very likely additional thermal line broadening. The line width at the outer strips provides reasonable upper limits to the thermal broadening of ≈ 10 eV, corresponding to <3000 km s\(^{-1}\). This upper limit provides an upper limit to the Fe temperature of \( kT_{\text{Fe}} \lesssim 5300 \text{ keV} \). This limit corresponds to a reverse shock velocity of \( V_s \approx 6900 \text{ km s}^{-1} \) and the equilibration of the ion temperatures in principle even allows for higher shock velocities. This velocity is also higher than that inferred from the proper motions of the forward shock. But it should be remembered that the shock velocity is a combination of the free expansion velocity of the ejecta and the velocity of the reverse shock in the observed frame: \( V_s = R/t - dR_s/dt \). If \( dR_s/dt < 0 \) — i.e., the reverse shock moves toward the center, which is reasonably for at those parts of the shell that encountered a high density environment, given that the overall ejecta mass is \( \sim 1M_\odot \) (see Figure 2 in Ferreira & de Jager 2008) — the reverse shock velocity may be larger than the forward shock.

The large broadening indeed provides an hint for this, but given the uncertainties about the different line-broadening mechanisms, the large line width at the outer strips does not provide sufficient proof for this. For example, Sato & Hughes (2017) found both red- and blue-shifted bright knots throughout the remnant covering a velocity range of -8000 to +10000 km s\(^{-1}\). Comparing our result with Figure 2 in Sato & Hughes (2017), we find some high-velocity compact knots in strips with large line width.

### 4.2.2. The ejecta abundances

As for the elemental abundance of ejecta, we assumed a pure-metal plasma, with the Si abundance set to \( 10^5 \) solar. Our fits indicate that the abundance ratio Fe/Si is \( \sim 1 \), whereas the O/Si abundance is ratio is generally \( \sim 0.03 \). But for some strips we only could obtain an upper limit (Table 2). The lack of the O ejecta is consistent with the previous with Chandra (Reynolds et al. 2007). The number ratio of O/Fe is lower than 0.6 at most. Such low ratio is cannot be explained by the core-collapsed progenitor and supports that the origin of Kepler’s SNR is type Ia SN (Iwamoto et al. 1999).
4.3. The electron temperature and ionization timescale

Figure 4 (c) and (d) show the electron temperature parameter $kT_e$ and ionization parameter $n_e t$. The results for the CSM show that the northern bright rim generally has low-$kT_e$ and high-$n_e t$ and the southern region has high-$kT_e$ and low-$n_e t$. Sun & Chen (2019) also found that $kT_e$ and $n_e t$ show anti-correlation in Kepler’s SNR by tessellated mapping of Chandra ACIS data (see Figure 7 in Sun & Chen 2019). They interpreted such high-$kT_e$ and low-$n_e t$ regions as newly shocked CSM, and low-$kT_e$ and high-$n_e t$ for the Si- or S-rich ejecta. Although such features might be real, the coupling effect of fitting parameter of $kT_e$ and $n_e t$ could also lead such results. We found the results for the ejecta have the inverse feature to the CSM. We should discuss this by using wide-band spectra with 2-Dimensional spatial resolution in future.

As a whole, the range of $n_e t$ values ($2.5 \times 10^{10} - 13 \times 10^{10}$ cm$^{-3}$ s) for the CSM component suggests typical densities of $n_e \approx 2–10$ cm$^{-3}$, assuming an age of $t = 416$ yr, which is the maximum age of the plasma given the age of the SNR. In reality, $t$ is likely to be smaller, as much of the plasma will have been heated more recently. So the electron densities are likely larger. Note, however, that this estimate may be skewed toward the denser parts of the plasma, which have higher emissivities. The $n_e t$ is smallest in the southern region, consistent with the fainter thermal X-ray emission from that region, as well as the larger shock velocities, which implies less deceleration and lower densities.

The variation in electron temperature is relatively limited: $kT_e \approx 0.5–0.9$ keV. This is inconsistent with the measured shock velocities of $V_s \approx 2000–4500$ km s$^{-1}$ assuming complete electron-ion equilibration, which would lead to $kT_e \approx 5–25$ keV. Clearly, the plasma cannot be fully temperature equilibrated.

5. CONCLUSIONS

In this paper, we reveal the line-of-sight kinematics of the CSM in Kepler’s SNR, using a new long observation by the RGS detectors on board the XMM-Newton satellite using the cross-dispersion direction to spatially resolve the remnant in 1D. At the edge of the remnant, we find the CSM is blue-shifted with a velocity of 0–500 km s$^{-1}$. Our result is consistent with a “runaway” AGB star as the progenitor of the remnant moving in 3D towards the northwest and in our direction along the line-of-sight (Bandiera 1987; Borkowski et al. 1992). In addition, we also derive information on the kinematics at the central bar, and find that the northwestern half is blue-shifted and southeastern half is red-shifted. This is consistent with the optical observation of broad H$\alpha$ line (Blair et al. 1991) and the torus-like shape of CSM distribution (Burkey et al. 2013). These results are explainable by both the SD and CD scenarios of the progenitor system. Future simulations considering the observed line-of-sight velocity in the X-ray band and observation by calorimeters with 2D spatial resolution could help further discussion about the kinematics of CSM around SNRs.
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Software: SAS 18.0.0 (Gabriel et al. 2004), CIAO 4.9 (Fruscione et al. 2006), Xspec 12.9.1 (Arnaud 1996), HEASoft 6.21 (Blackburn 1995)

REFERENCES


—. 2017, Supernova 1604, Kepler’s Supernova, and its Remnant, ed. A. W. Alsabti & P. Murdin, 139


