All-sky search for continuous gravitational waves from isolated neutron stars in the early O3 LIGO data

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All-sky search for continuous gravitational waves from isolated neutron stars in the early O3 LIGO data

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We report on an all-sky search for continuous gravitational waves in the frequency band 20–2000 Hz and with a frequency time derivative in the range of [−1.0, +0.1] × 10⁻⁸ Hz/s. Such a signal could be produced by a nearby, spinning and slightly nonaxisymmetric isolated neutron star in our Galaxy. This search uses the LIGO data from the first six months of Advanced LIGO’s and Advanced Virgo’s third observational run, O3. No periodic gravitational wave signals are observed, and 95% confidence-level (C.L.) frequentist upper limits are placed on their strengths. The lowest upper limits on worst-case (linearly polarized) strain amplitude h₀ are ~1.7 × 10⁻²⁵ near 200 Hz. For a circularly polarized source (most favorable orientation), the lowest upper limits are ~6.3 × 10⁻²⁶. These strict frequentist upper limits refer to all sky locations and the entire range of frequency derivative values. For a population-averaged ensemble of sky locations and stellar orientations, the lowest 95% C.L. upper limits on the strain amplitude are ~1.4 × 10⁻²⁵. These upper limits improve upon our previously published all-sky results, with the greatest improvement (factor of ~2) seen at higher frequencies, in part because quantum squeezing has dramatically improved the detector noise level relative to the second observational run, O2. These limits are the most constraining to date over most of the parameter space searched.

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I. INTRODUCTION

We report the results of an all-sky search for continuous, nearly monochromatic gravitational waves from rapidly rotating isolated neutron stars using the first six months of data from the third observing run (O3) of the Advanced Laser Interferometer Gravitational wave Observatory (Advanced LIGO [1,2]). This first search of the early O3 data uses the powerFlux hierarchical search program [3–8] with loose-coherence follow-up [9,10] of outliers and covers a broad band of frequencies (20–2000 Hz) and frequency derivatives (|−1.0, +0.1| × 10⁻⁸ Hz/s). Although more than 1.4 × 10⁵ search outliers are found in the initial stage of analysis, successive follow-up stages failed to confirm an astrophysical signal. Hence the primary results from this analysis are the upper limits on strain amplitude presented in Sec. IVA.

All-sky searches for continuous gravitational waves from isolated neutron stars have been carried out in Advanced LIGO and Virgo data previously [7,8,11–18]. The results presented here are the most sensitive to date in strain amplitude for a broadband, all-sky search with high allowed spin-down magnitudes, with improvement factors ranging from ~1.2 at signal frequencies of ~100 Hz to ~2 at the higher frequencies. The improvement with respect to similar, previous analyses of O2 data [12,13] is greater at higher frequencies, in part because of the improved detector noise (~3 db) achieved with quantum squeezing [19] and in part because longer Fourier transform coherence times are used here (for frequencies up to 1475 Hz) than in the O2 analyses.

Our primary targets in this analysis are fast-spinning, nonaxisymmetric neutron stars in the Milky Way. Given the immense pressure on its nuclear matter, one expects a neutron star to assume a highly spherical shape in the limit of no rotation and, with rotation, to form an axisymmetric oblate spheroid. A number of physical processes can disrupt the symmetry, however, to produce quadrupolar gravitational waves from the stellar rotation. Those processes include crustal distortions from cooling or accretion, buried magnetic field energy and excitation of r-modes. Comprehensive reviews of continuous gravitational wave emission mechanisms from neutron stars can be found in [20,21].

This article is organized as follows: Sec. II describes the dataset used, including steps taken to mitigate extremely loud and relatively frequent instrumental glitches seen in the O3 LIGO data, a phenomenon not seen in previous LIGO observing runs. Section III briefly describes the powerFlux and loose-coherence algorithm used in this and previous searches. Section IV presents the results of the analysis. Section V concludes with a discussion of the results and prospects for future searches.

*Full author list given at the end of the article.
II. DATASETS USED

Advanced LIGO consists of two detectors, one in Hanford, Washington (designated H1), and the other in Livingston, Louisiana (designated L1), separated by a 3000-km baseline [1]. Each site hosts one, 4-km-long interferometer inside a vacuum envelope with the primary interferometer optics suspended by a cascaded, quadruple suspension system in order to isolate them from external disturbances. The interferometer mirrors act as test masses, and the passage of a gravitational wave induces a differential-arm length change that is proportional to the gravitational-wave strain amplitude.

Advanced LIGO’s first observing run (O1) occurred between September 12, 2015 and January 19, 2016 and led to the discovery on September 14, 2015 of gravitational waves from binary black hole (BBH) coalescences [22]. The O2 observing run began November 30, 2016 and ended August 25, 2017 and included the first detection of a binary neutron star (BNS) merger [23]. The O3 run began April 1, 2019 and ended March 27, 2020, for which the first six months (April 1, 2019 to October 1, 2019), prior to a 1-month commissioning break, is designated as the O3a epoch. The analysis presented here is based primarily on the O3a dataset, with data from the remainder of the run (O3b epoch) used only for following up on promising signal candidates. From the O1, O2 and O3a datasets, the LIGO Scientific Collaboration and Virgo Collaboration have reported a total of 50 compact binary coalescences [24–26], primarily BBH events, with two binary neutron star (BNS) detections [23,27] and one potential binary neutron star / black hole detection [28].

The Virgo interferometer [29] observed during August 2017 near the end of the O2 run and throughout the O3 run. The Virgo data have not been used in this analysis, however, because of an unattractive tradeoff in computational cost for sensitivity gain, given the interferometer’s higher noise level during the O3 run.

Prior to searching the O3a data for continuous wave (CW) signals, the quality of the data was assessed and steps taken to mitigate the effects of instrumental artifacts. As in previous Advanced LIGO observing runs [30], instrumental “lines” (sharp peaks in fine-resolution run-averaged H1 and L1 spectra) are marked, and where possible, their instrumental or environmental sources identified [31]. The resulting database of artifacts proved helpful in eliminating spurious signal candidates emerging from the search. In general, the line multiplicity for H1 O3a data was similar to that observed in the O2 run, while the line multiplicity for L1 O3a data was substantially reduced.

Another type of artifact observed in the O3a data for both H1 and L1 was relatively frequent and contained loud “glitches” (short, high-amplitude instrumental transients) with most of their spectral power lying below ∼500 Hz. Although loud glitches have been observed in previous runs, their frequency in O3a was dramatically higher. At present, investigations of the source of these glitches remain inconclusive. An effort to identify and mitigate them during the October 2019 commissioning break (between the O3a and O3b epochs) did not succeed. Unlike in previous LIGO data runs, the sheer spectral power in the glitches increased the effective broadband noise floor of the data below ∼500 Hz quite substantially, as seen in run-averaged spectra computed from 1800s and 7200s discrete Fourier transforms known as “SFTs” (for “short Fourier transforms”). Most CW searches based on summing strain spectral power from SFTs, including the powerFlux program used here, apply weightings that disfavor SFTs with high noise. Because the average time interval between loud glitches in O3a data is comparable to or smaller than the coherence time of the SFTs; however, inverse noise weighting of SFTs proved much less effective than in previous runs, especially for the 7200s SFTs.

To mitigate the effects of these glitches on O3a CW searches for signals below 475 Hz, a simple glitch-gating algorithm was applied [32,33] to excise the transients from the data. For each 1/16-second for which a whitened version of the H1 and L1 strain data channels had excess rms power in the 25–50 Hz or 70–110 Hz bands, the strain channel was set to zero. To reduce artifacts from discontinuous data, a 1/4-second half-Hann-window ramping from unity to zero was multiplied against the data stream prior to each zeroed interval, and a 1/4-second half-Hann window ramping from zero back to unity was multiplied at the end of zeroed intervals. This gating can be considered to be inverse-Tukey-windowed. Although the Tukey windowing mitigates severe spectral artifacts, the resulting spectra still suffer visible spectral leakage very near loud instrumental lines, such as from 60-Hz power mains and “violin modes” (near 500 Hz) due to ambient vibrations of the silica fibers from which LIGO mirrors are suspended. All gated intervals longer than 30 seconds are excluded from analysis, as are 7200s SFTs containing total gate durations longer than 120 seconds. Altogether, the applied gating leads in this analysis to losses of about 1% and 11% of the H1 and L1 observation times during the O3a epoch for search frequencies below 475 Hz. Details of the gating, including validation that low-frequency CW “hardware injections” (simulated signals imposed on interferometer mirrors during data taking, see Sec. III E) are recovered with higher signal-to-noise ratio (SNR) in gated data than in the original, ungated data can be found in a technical report [32].

As discussed in Sec. III, the powerFlux program searches many narrow frequency bands, where the SFT coherence time chosen depends on frequency. In general, longer coherence times give improved sensitivity, but incur larger computational costs from the need to search more finely in parameter space. In addition, efficiency loss from spectral
leakage due to Doppler modulations from the Earth’s motion increases at higher frequency, especially for sources near the ecliptic plane. Given these tradeoffs, the same coherence-time choices made for the O1 analysis [8] are chosen here, as shown in Table I. The SFTs are created from the C01 calibrated strain data [34], using Hann windowing and 50% overlap. Upper limits on the calibration uncertainties over the 20–2000 Hz band in the O3a epoch are estimated to be <7% in magnitude and <4 deg in phase (68% confidence interval).

### III. ANALYSIS METHOD

This search uses the PowerFlux program [3,5,7,8] with loose-coherence follow-up of outliers [9,10]. In brief, strain power is summed over many SFTs after correcting for Doppler modulations, for a large bank of templates based on sky location, frequency, frequency derivative and stellar orientation. The maximum strain powers detected over the entire sky and for all frequency derivatives in each orientation, which determines the polarization, is parametrized by the inclination angle $\iota$ of its spin axis relative to the detector line-of-sight and by the angle $\psi$ of the axis projection on the plane of the sky. The linear polarization case ($\iota = \pi/2$) is the most unfavorable because the gravitational wave flux impinging on the detectors is smallest for an intrinsic strain amplitude $h_0$, possessing 8 times less incident strain power than for circularly polarized waves ($\iota = 0, \pi$).

The strain signal model $h(t)$ for a periodic source is assumed to be the following function of time $t$:

$$
    h(t) = h_0 \left( F_+ (t, \alpha_0, \delta_0, \psi) \frac{1 + \cos^2(\iota)}{2} \cos(\Phi(t)) + F_\times (t, \alpha_0, \delta_0, \psi) \cos(\iota) \sin(\Phi(t)) \right),
$$

where $h_0$ is the intrinsic strain amplitude, $\Phi(t)$ is the signal phase, $F_+$ and $F_\times$ characterize the detector responses to signals with “+” and “×” quadrupolar polarizations [3], and the sky location is described by right ascension $\alpha_0$ and declination $\delta_0$.

In a rotating triaxial ellipsoid model for a star at distance $r$ spinning at frequency $f_{\text{rot}}$ about its (approximate) symmetry axis ($z$), the amplitude $h_0$ can be expressed as

$$
    h_0 = \frac{4\pi^2 G e I_{zz} f_{GW}^2}{c^3 r}
$$

$$
    = \left[ 1.1 \times 10^{-24} \right] \left[ \frac{e}{10^{-6}} \right] \left[ \frac{I_{zz}}{I_0} \right] \left[ \frac{f_{GW}}{1 \text{ kHz}} \right] \left[ \frac{1 \text{ kpc}}{r} \right],
$$

where $I_0 = 10^{38}$ kg · m$^2$ ($10^{45}$ g · cm$^2$) is a nominal neutron star moment of inertia $I_{zz}$ about $z$, and the gravitational radiation is emitted at frequency $f_{GW} = 2f_{\text{rot}}$.

### TABLE I. Information on the short Fourier transforms (SFTs) used in the search. All SFTs are Hann-windowed with 50% overlap. The numbers of gated SFTs used below 475 Hz are affected by live time loss from avoiding data stretches with high rates of gated glitches, with a larger effect seen for L1 data.

<table>
<thead>
<tr>
<th>Frequency bin</th>
<th>20–475 Hz</th>
<th>475–1475 Hz</th>
<th>1475–2000 Hz</th>
</tr>
</thead>
<tbody>
<tr>
<td>Coherence time</td>
<td>Gated C01</td>
<td>Ungated C01</td>
<td>Ungated C01</td>
</tr>
<tr>
<td>H1: 2287</td>
<td>7200s</td>
<td>3600s</td>
<td>1800s</td>
</tr>
<tr>
<td>H1: 5535</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>H1: 11735</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>L1: 2247</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>L1: 5973</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>L1: 12574</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

### TABLE II. Information on the band-specific parameters for the initial search (stage 0) and outlier follow-up stages. The number of spin-down steps and the spin-down step size refer to the templates used in the stage-0 search. The tolerances refer to the consistency requirements between H1 and L1 outliers used to define candidates selected for stage-1 follow-up. Other search parameters relevant to all search bands are described in the text.

<table>
<thead>
<tr>
<th>Frequency bin</th>
<th>20–475 Hz</th>
<th>475–1475 Hz</th>
<th>1475–2000 Hz</th>
</tr>
</thead>
<tbody>
<tr>
<td>Number of spin-down templates</td>
<td>66</td>
<td>34</td>
<td>18</td>
</tr>
<tr>
<td>Spin-down step size (Hz/s)</td>
<td>$1.692 \times 10^{-10}$</td>
<td>$3.333 \times 10^{-10}$</td>
<td>$6.667 \times 10^{-10}$</td>
</tr>
<tr>
<td>H1/L1 frequency mismatch tolerance (mHz)</td>
<td>2.5</td>
<td>2.5</td>
<td>2.5</td>
</tr>
<tr>
<td>H1/L1 spin-down mismatch tolerance (Hz/s)</td>
<td>$3.0 \times 10^{-10}$</td>
<td>$3.0 \times 10^{-10}$</td>
<td>$3.0 \times 10^{-10}$</td>
</tr>
</tbody>
</table>
The equatorial ellipticity $\epsilon$ is a convenient, dimensionless measure of stellar nonaxisymmetry,

$$\epsilon \equiv \frac{I_{xx} - I_{yy}}{I_{zz}}.$$  \hfill (4)

The phase evolution of the signal is given in the reference frame of the Solar System barycenter (SSB) by the second-order approximation,

$$\Phi(t) = 2\pi (f_{\text{source}} \cdot (t - t_0) + f^{(1)} \cdot (t - t_0)^2 / 2) + \phi,$$  \hfill (5)

where $f_{\text{source}}$ is the SSB source frequency, $f^{(1)}$ is the first frequency derivative (which, when negative, is termed the spin-down), $t$ is the SSB time, and the initial phase $\phi$ is computed relative to reference time $t_0$. When expressed as a function of the local time of ground-based detectors, Eq. (5) acquires sky-position-dependent Doppler shift terms.

We search a frequency band 20–2000 Hz and a frequency derivative $\dot{f}$ range of $[-1 \times 10^{-8}, +1 \times 10^{-9}]$ Hz/s. Figure 1 shows this parameter space coverage together with those of previous all-sky searches of the LIGO O2 data using different methods. Most natural sources are expected to have a negative first frequency derivative, as the energy lost in gravitational or electromagnetic waves would make the source spin more slowly. A small number of isolated pulsars in globular clusters exhibit slight apparent spin-up, believed to arise from acceleration in the Earth’s direction; known apparent spin-up values have magnitudes too small to prevent source detection with the zero-spin-down templates used in this search, given a strong enough signal. The frequency derivative can also be positive when the source is affected by a strong slowly varying Doppler shift, such as due to a long-period orbit with a companion. A more exotic source of spin-up is gravitational wave superradiance from a boson cloud in the vicinity of an isolated black hole[35].

All known isolated pulsars spin down more slowly than the maximum value of $|\dot{f}|_{\text{max}}$ used here, and as seen in the results section, the equatorial ellipticity required for higher $|\dot{f}|_{\text{max}}$ is improbably high for a source losing rotational energy primarily via gravitational radiation at low frequencies. More plausible is a source with spin-down dominated by electromagnetic radiation energy loss, but for which detectable gravitational radiation is also emitted.

FIG. 1. Comparison in frequency and spin-down for this search with those of previous all-sky searches of LIGO O2 data. The shaded rectangle with vertical bars shows the 20–2000 Hz and $-10^{-8}$–$10^{-9}$ Hz/s range for this O3a search. The slightly larger rectangle with horizontal bars shows the region searched in the O2 data with the Frequency Hough method [12,13]. The smaller rectangle with crossed diagonal bars shows the region searched by the distributed-computing project Einstein@Home [14]. The solid line at zero spin-down depicts the specialized O2 search for low-ellipticity millisecond pulsars using the Falcon method [15–17] (the thickness of the line overstates the coverage in spin-down range). The dotted curves indicate contours of constant equatorial ellipticity $\epsilon = (10^{-8}, 10^{-7}, 10^{-6}, 10^{-5}$ and $10^{-4})$ for a star with stellar spin-down dominated by gravitational wave emission.
One measure of gravitational wave detectability of known pulsars is the “spin-down strain limit” defined by equating inferred rotational kinetic energy loss to gravitational wave energy emission. For the frequency band searched here, such limits range from as high as $O(10^{-24})$ for energetic, low-frequency young stars, such as the Crab and Vela pulsars, down to below $10^{-27}$ for high-frequency millisecond pulsars [36], where the highest such limit at high frequencies is $O(10^{-26})$.

### B. Methodology

The powerflux pipeline has a hierarchical structure that permits systematic follow-up of loud outliers from the initial stage. The later stages improve intrinsic strain sensitivity by increasing effective coherence time while dramatically reducing the parameter space volume over which the follow-up is pursued. The pipeline uses loose coherence [9] with stages of improving refinement via steadily increasing effective coherence times. Any outliers that survive all stages of the search pipeline are examined manually for contamination from known instrumental artifacts and for evidence of contamination from a previously unknown single-interferometer artifact. Those for which no artifacts are found are subjected to further follow-up described below.

In the pipeline’s initial stage, the main powerflux algorithm [3–8] establishes upper limits and produces lists of outliers. The program sets strict frequentist upper limits on detected strain power in circular and linear polarizations that apply everywhere on the sky except for small regions near the ecliptic poles, where signals with small Doppler modulations can be masked by stationary instrumental spectral lines. The procedure defining these excluded regions is described in [5] and applies to less than 0.2% of the sky over the entire run, where the precise shapes of the regions near the poles depend on assumed signal frequency and spin-down. Initial outliers are defined by a joint H1-L1 signal-to-noise ratio (SNR) greater than a threshold of 7, with consistency among corresponding H1, L1 and joint H1-L1 outliers (criteria described in Sec. III D). These outliers are then followed up with a loose-coherence detection pipeline [5,9,10], which is used to reject or confirm the outliers.

The power calculation of the data can be expressed as a bilinear form of the input matrix $\{a_{i,j}\}$ constructed from the SFT coefficients with indices representing time and frequency,

$$P[f] = \sum_{t_1, t_2, D_i, D_j} a^{(D_i)}_{1, f} a^{(D_j)}_{2, f} K^{(D_i, D_j)}_{t_1, t_2, f}.$$  

In this expression $\Delta f(t)$ is the detector-frame frequency drift due to the effects from both Doppler shifts and the first frequency derivative. The sum is taken over all times $t$ corresponding to the midpoints of the SFT time intervals. The kernel $K^{(D_i, D_j)}_{t_1, t_2, f}$ includes the contribution of time-dependent SFT noise weights, antenna response, signal polarization parameters, and relative phase terms [9,10] for detectors $D_{i,j} (= H1, L1)$. Separate power sums are computed for H1, L1 and combined H1-L1 data.

<p>| TABLE III. powerflux outlier follow-up parameters. Stage 1 and higher use a loose-coherence algorithm for demodulation. The sky (both right ascension $\alpha$ and declination $\delta$) and frequency refinement parameters are relative to values used in the stage 0 powerflux search. |
| --- | --- | --- | --- | --- | --- |</p>
<table>
<thead>
<tr>
<th>Stage</th>
<th>Instrument sum</th>
<th>Phase coherence $\delta$ rad</th>
<th>Spin-down step Hz/s</th>
<th>Sky refinement $\alpha \times \delta_0$</th>
<th>Frequency refinement</th>
<th>SNR increase %</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>Initial/upper limit incoherent</td>
<td>NA</td>
<td>$1.692 \times 10^{-10}$</td>
<td>1</td>
<td>$1/2$</td>
<td>...</td>
</tr>
<tr>
<td>1</td>
<td>Incoherent</td>
<td>$\pi/2$</td>
<td>$1.0 \times 10^{-10}$</td>
<td>$1/4 \times 1/4$</td>
<td>$1/8$</td>
<td>20</td>
</tr>
<tr>
<td>2</td>
<td>Coherent</td>
<td>$\pi/2$</td>
<td>$5.0 \times 10^{-11}$</td>
<td>$1/4 \times 1/4$</td>
<td>$1/8$</td>
<td>10</td>
</tr>
<tr>
<td>0</td>
<td>Initial/upper limit incoherent</td>
<td>NA</td>
<td>$1.692 \times 10^{-10}$</td>
<td>1</td>
<td>$1/2$</td>
<td>...</td>
</tr>
<tr>
<td>1</td>
<td>Incoherent</td>
<td>$\pi/2$</td>
<td>$1.692 \times 10^{-10}$</td>
<td>$1/4 \times 1/4$</td>
<td>$1/8$</td>
<td>20</td>
</tr>
<tr>
<td>2</td>
<td>Coherent</td>
<td>$\pi/2$</td>
<td>$5.0 \times 10^{-11}$</td>
<td>$1/4 \times 1/4$</td>
<td>$1/8$</td>
<td>10</td>
</tr>
<tr>
<td>0</td>
<td>Initial/upper limit incoherent</td>
<td>NA</td>
<td>$3.33 \times 10^{-10}$</td>
<td>1</td>
<td>$1/2$</td>
<td>...</td>
</tr>
<tr>
<td>1</td>
<td>Incoherent</td>
<td>$\pi/2$</td>
<td>$3.33 \times 10^{-10}$</td>
<td>$1/4 \times 1/4$</td>
<td>$1/8$</td>
<td>15</td>
</tr>
<tr>
<td>2</td>
<td>Coherent</td>
<td>$\pi/2$</td>
<td>$5.0 \times 10^{-11}$</td>
<td>$1/4 \times 1/4$</td>
<td>$1/8$</td>
<td>10</td>
</tr>
<tr>
<td>0</td>
<td>Initial/upper limit incoherent</td>
<td>NA</td>
<td>$6.67 \times 10^{-10}$</td>
<td>1</td>
<td>$1/2$</td>
<td>...</td>
</tr>
<tr>
<td>1</td>
<td>Incoherent</td>
<td>$\pi/2$</td>
<td>$3.33 \times 10^{-10}$</td>
<td>$1/4 \times 1/4$</td>
<td>$1/8$</td>
<td>15</td>
</tr>
<tr>
<td>2</td>
<td>Coherent</td>
<td>$\pi/2$</td>
<td>$5.0 \times 10^{-11}$</td>
<td>$1/4 \times 1/4$</td>
<td>$1/8$</td>
<td>10</td>
</tr>
</tbody>
</table>
The fast first-stage (stage 0) PowerFlux algorithm uses a kernel with diagonal terms only (including separate single-detector contributions $D_i = D_j$). The second stage (stage 1) increases effective coherence time while still allowing for controlled deviation in phase [9] via kernels that increase effective coherence length by inclusion of limited single-detector, off diagonal terms. The third stage (stage 2) maintains the stage-1 effective coherence time, but adds SFT coefficients from H1 and L1 data coherently ($D_i \neq D_j$) to improve SNR and parameter resolution.

The effective coherence length is captured in a parameter $\delta$ [9], which describes the degree of phase drift allowed between SFTs. A value of $\delta = 0$ corresponds to a fully coherent case, and $\delta = \pi$ corresponds to incoherent power sums.

Depending on the terms used, the data from different interferometers can be combined incoherently (such as in stages 0 and 1, see Table III) or coherently (as used in stage 2). The coherent combination is more computationally expensive but improves parameter estimation.

C. Upper limits determination

The 95% confidence-level (C.L.) upper limits presented in Sec. IV are reported in terms of the worst-case value of $h_0$ (linear polarization) and for the most sensitive case of circular polarization.

These upper limits, produced in stage 0, are based on the overall noise level and largest outlier in strain found for every template in each narrow subband in the first stage of the pipeline. Subbands are analyzed by separate instances of PowerFlux [5].

To allow robust analysis of the entire spectrum, including regions with severe spectral artifacts, a universal statistic algorithm [7,37] is used for establishing upper limits. The algorithm is derived from the Markov inequality and shares its independence from the underlying noise distribution. It produces upper limits less than 5% above optimal in case of Gaussian noise. In non-Gaussian bands, it can report values larger than what would be obtained if the true underlying distribution were known, but the upper limits are always at least 95% valid. Figure 2 shows results of a high-statistics “software injections” simulation run performed as described in [5]. Correctly established upper limits lie above the dashed diagonal lines (defining equality between upper limit obtained and true injection strain) in each panel, corresponding to four selected subbands [SFT coherence times]: 20–60 Hz [7200s], 60–475 Hz [7200s], 475–1475 Hz [3600s] and 1475–2000 Hz [1800s]. Performance for the 7200s-SFT upper limits is demonstrated in Fig. 2.
20–60 Hz and 60–475 Hz bands are shown separately because of the proliferation of spectral line artifacts below 60 Hz, primarily in the H1 data. The breakpoint frequencies of 475 Hz and 1475 Hz for decreasing SFT coherence time (Table I) are those used in the O1 power-flux search [7,8], marking the starts of bands disturbed by first and third violin mode harmonics. Additional band-specific parameters for the initial stage of the search are listed in Table II.

D. Outlier follow-up

A follow-up search for detection is carried out for high-SNR outliers found in stage 0. The outliers are subject to an initial coincidence test. For each outlier with SNR > 7 in the combined H1 and L1 data, we require there to be outliers in the individual detector data of the same small sky patch, approximately square with a side length $\sim 30$ mrad $\times \left( \frac{100 \text{ Hz}}{\text{frequency}} \right)$ that have SNR > 5 and match the parameters of the combined-detector outlier within 2.5 mHz in frequency and $3 \times 10^{-10}$ Hz/s in spin-down.

The combined-detector SNR is additionally required to be above both single-detector SNRs, in order to suppress single-detector instrumental artifacts, except for unusually loud outliers (combined, H1 and L1 SNRs all greater than 20).

The identified outliers using combined data are then passed to the follow-up stage using a loose-coherence algorithm [9] with progressively improved determination of frequency, spin-down, and sky location.

As the initial stage 0 sums only powers, it does not use the relative phase between interferometers, which results in some degeneracy among sky position, frequency, and spin-down. The first loose-coherence follow-up stage (1) demands greater temporal coherence (smaller $\delta$) within each interferometer, which should boost the SNR of viable outliers, but combines H1 and L1 power sums incoherently. The subsequent stage (2) uses combined H1 and L1 data coherently, providing tighter bounds on outlier location.

Testing of the stages 0–2 pipeline is performed for frequency bands searched via software injections using

![Diagram](image-url)

FIG. 3. Injection (software simulations) recovery efficiencies in the 20–60 Hz, 60–475 Hz, 475–1475 Hz and 1475–2000 Hz frequency bands are shown in the upper left, upper right, lower left and lower right panels, respectively, for stages 0, 1 and 2 of the search. The injected strain divided by the 95% C.L. upper limit in its band (without injection) is shown on the horizontal axis. The percentage of surviving injections is shown on the vertical axis, with a horizontal dashed line drawn at the 95% level. The vertical dashed line marks a relative strain of unity. Ideally, the recovery efficiencies should lie to the left of the vertical line or above the horizontal line. One observes, however, that the ideal recovery efficiency is significantly degraded below 60 Hz, where large instrumental artifacts in the H1 data and only modest expected Doppler modulations make clean signal recovery more challenging. Most of the degradation stems from the band below 27 Hz for which H1 line contamination is severe and for which the H1 noise floor is substantially higher than the L1 noise floor.
the same follow-up procedure. The recovery criteria also require that an outlier close to the true injection location (within 2.5 mHz in frequency, 3 \times 10^{-10} Hz/s in spin-down and 28.5 rad-Hz/f in sky location) be found and successfully pass through all stages of the detection pipeline.

Injection recovery efficiencies from simulations covering the major subbands (20–475 Hz, 475–1475 Hz, 1475–2000 Hz) are shown in Fig. 3 for stages 0, 1 and 2, which confirm that 95% signal recovery is comparable to the 95% upper limit in all bands, as desired, except for the region below 60 Hz for which spectral line artifacts heavily contaminate the H1 dataset. Injections in vetoed frequency bands (see Sec. IV B and Table VI) are not included in these graphs.

As in previous PowerFlux analyses with loose-coherence follow-up [7,8], only a mild influence from parameter mismatch is expected, as the parameters are chosen to accommodate the worst few percent of injections. The follow-up procedure establishes very wide margins for outlier follow-up. For example, when transitioning from the semicoherent stage 0 to the loose-coherence stage 1 below 475 Hz, the effective coherence length increases by a factor of 4. The average true signal SNR should then increase by more than 40%. But the threshold used in follow-up is only 15%–20%, depending on frequency, which accommodates unfavorable noise conditions, template mismatch, and detector artifacts.

Although a similar prior analysis [7,8] of O1 data used additional stages (3, 4) of loose coherence, we choose after stage 2 to inspect candidates manually. The small number not found to be contaminated by obvious instrumental artifacts are followed up in the full O3 dataset by a search similar to the powerFlux O3a stage 1, but using much finer spin-down stepping of 1 \times 10^{-11} Hz/s, and refinement factors of 1/4 for both sky (right ascension and declination each) and frequency stepping, to exploit the improved SNR and parameter resolution possible in the nearly doubled observation span. Any outlier surviving this full-O3 follow-up is explored via a more sensitive method, implemented in PyFstat [38,39] which uses Markov chain Monte Carlo (MCMC) techniques [40,41] to explore small regions of parameter space in successive stages of increasing coherence times.

The full-O3 powerFlux follow-up search uses nearly 11 months of data (compared to the 6-month O3a period), leading to an expected increase in SNR by a factor of approximately \sqrt{11/6} = 1.35, with an additional \sim 40% increase from the use of stage-1 loose coherence, leading to a nominal expectation of SNR gain of a factor of \sim 1.9. Software simulations of signals with amplitudes as weak as 1/3 of the upper limit in a given band, however, reveal large fluctuations above and below this expectation for all search bands. These simulations suggest applying a conservative (negligible efficiency loss) threshold on the SNR increase of only 20%, which is nonetheless effective in suppressing most noise artifacts.

### TABLE IV

<table>
<thead>
<tr>
<th>Label</th>
<th>Frequency Hz</th>
<th>Spindown nHz/s</th>
<th>RA\text{12000} degrees</th>
<th>DEC\text{12000} degrees</th>
<th>h\text{true}</th>
<th>UL sig bin UL ctrl bins</th>
<th>Detected?</th>
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</thead>
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<tr>
<td>Inj0</td>
<td>265.575086</td>
<td>\sim 4.15 \times 10^{-3}</td>
<td>71.55193</td>
<td>\sim 56.21749</td>
<td>6.12 \times 10^{-26}</td>
<td>1.8 \times 10^{-25}</td>
<td>Yes</td>
</tr>
<tr>
<td>Inj1</td>
<td>848.937350</td>
<td>\sim 3.00 \times 10^{-1}</td>
<td>37.39385</td>
<td>\sim 29.45246</td>
<td>5.47 \times 10^{-25}</td>
<td>8.1 \times 10^{-25}</td>
<td>Yes</td>
</tr>
<tr>
<td>Inj2</td>
<td>575.163506</td>
<td>\sim 1.37 \times 10^{-4}</td>
<td>215.25617</td>
<td>3.44399</td>
<td>7.59 \times 10^{-26}</td>
<td>2.7 \times 10^{-25}</td>
<td>No</td>
</tr>
<tr>
<td>Inj3</td>
<td>108.857159</td>
<td>\sim 1.46 \times 10^{-8}</td>
<td>178.37257</td>
<td>\sim 33.4366</td>
<td>1.30 \times 10^{-25}</td>
<td>1.9 \times 10^{-25}</td>
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<tr>
<td>Inj4</td>
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<td>\sim 2.54 \times 10^{-11}</td>
<td>279.98768</td>
<td>\sim 12.4666</td>
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<td>4.9 \times 10^{-25}</td>
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</tr>
<tr>
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<td>\sim 83.83914</td>
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<td>1.8 \times 10^{-25}</td>
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</tr>
<tr>
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<td>198.88558</td>
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<td>3.1 \times 10^{-25}</td>
<td>Yes</td>
</tr>
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<td>\sim 8.50 \times 10^{-2}</td>
<td>221.55565</td>
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<td>1.9 \times 10^{-24}</td>
<td>No</td>
</tr>
<tr>
<td>Inj11</td>
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<td>\sim 58.27209</td>
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<td>9.4 \times 10^{-25}</td>
<td>No</td>
</tr>
<tr>
<td>Inj12</td>
<td>37.805210</td>
<td>\sim 6.25 \times 10^{0}</td>
<td>331.85267</td>
<td>\sim 16.97288</td>
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<td>4.8 \times 10^{-25}</td>
<td>No</td>
</tr>
<tr>
<td>Inj14</td>
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<td>\sim 1.00 \times 10^{-3}</td>
<td>300.80284</td>
<td>\sim 14.32394</td>
<td>1.83 \times 10^{-24}</td>
<td>2.1 \times 10^{-24}</td>
<td>Yes</td>
</tr>
</tbody>
</table>

\text{a} True spin-down value outside of nominal search range. Injection is recovered when search range is extended for this band.
The final follow-up method applied to any survivors of the full-O3 loose-coherence check uses the PYTHON-based PyFstat [38,39] software infrastructure to combine a MCMC approach [40,41] with semicoherent summing of the well known $F$-statistic detection statistic [42]. In this approach, the parameter space near to those values from a stage-2 outlier is sampled randomly according to a certain probability density function determined by the $F$-statistic likelihood function. We closely follow an implementation [41] applied to a recent analysis of O2 data to follow up on outliers emerging from several prior O2 continuous wave searches.

Briefly, the O3a observation time is divided into $N_{\text{seg}}$ segments, for each of which the $F$-statistic is computed over a coherence time approximately equal to the observation time divided by $N_{\text{seg}}$. For each point sampled in parameter space, the sum of the $F$-statistic values is computed to form a total detection statistic. This procedure is repeated, decreasing the number of segments (increasing the coherence time), using the resulting MCMC-maximized $F$-statistic sum as the seed for the next stage, with a consequent reduction in parameter space volume searched. For this O3a analysis we choose five successive stages of follow-up with decreasing values of $N_{\text{seg}} = 500$ (coherence time of 0.36 day), 250, 55, 5 and 1. A random sample of 600 off-source sky locations having the same declination as the putative signal direction, but separated by more than 90 deg from that direction, is used to determine a nonsignal expectation for the background distributions in the same frequency band [41]. A Bayes factor $B_{\text{SN}}$ is computed from the change in $F$-statistic values for a nominal signal compared to the empirical background distribution in the last stage ($N_{\text{seg}} = 5$ to $N_{\text{seg}} = 1$).

E. Hardware injections

During the O3 run 18 hardware injections were used to simulate particular CW signals, as part of detector response validation, including long-term phase fidelity. The injections were imposed via radiation pressure from auxiliary lasers [43]. For reference, Table IV lists the key source parameters for the 14 injections relevant to this analysis (labeled Inj0-Inj12 and Inj14), namely those that simulate isolated neutron stars with nominal frequencies between 20 and 2000 Hz. In general, the injection amplitudes used in
FIG. 5. Ranges (kpc) of the power-flux search for neutron stars spinning down solely due to gravitational radiation ("gravitars") under different assumptions. The three sets of three curves (purple, green dotted, yellow-green diamonds) that generally rise with frequency are the ranges for which the O3a circular-polarization, O3a population-averaged and O2 population-averaged Frequency Hough [12,13] upper limits apply for three different assumed equatorial ellipticities of $\epsilon = 10^{-4}$, $10^{-6}$ and $10^{-8}$. In each case, the curve stops at the frequency at which the implied spindown magnitude at the corresponding range exceeds the maximum range allowed by the maximum spindown magnitude ($10^{-8}$ Hz/s) used in these analyses. The three black curves (solid, dashed, dot-dashed) that peak below 100 Hz represent the maximum possible ranges for which the O3a circular-polarization limits apply under the assumption that the maximum spindown magnitude is $\left(10^{-8}, 10^{-10}, 10^{-12}\right)$ Hz/s. Searching for high spindown magnitudes simultaneously probes higher ellipticities and larger regions of the galaxy, reaching well beyond the galactic center ($\sim 8.5$ kpc) at high ellipticities and low frequencies. More realistically, a neutron star’s spin-down may be dominated by electromagnetic radiation, in which case searching for high spindown magnitude achieves a shorter search range, but enables detection of stars that would not be detected under the gravitar assumption. (color online).

TABLE V. Counts of outliers surviving different stages of the hierarchical follow-up for four frequency bands. Survivors from stage-2 follow-up are broken down into the categories of hardware injections, visible artifacts identified via strain histograms and candidates for loose-coherence follow-up in the full-O3 data. Only one cluster of O3a outliers (near 1663.6 Hz) survives the full-O3 fine-grained follow-up, leading to a cluster of 21 full-O3 outliers. Additional follow-up of these weak candidates, which appear in a visibly disturbed band of L1 data, was carried out using the MCMC Pyrstat follow-up procedure described in section III D. The Pyrstat follow-up confirmed these 21 outliers to be uninteresting.
the O3 run are substantially lower than those used in previous observing runs. For this reason, some injections with identical source parameters, except for stronger signal amplitudes, were detected with high SNR in the O2 run, but are not detected in this analysis, although they can be found with targeted matched-filter analyses.

For each injection in Table IV, the column labeled “UL sig bin” gives the 95% UL (upper limit) for the corresponding band. Ideally, that value should exceed the true injected amplitude $h_0$ for at least 95% of the injections. In this case, that statement holds for all 14 injections. The column labeled “UL ctrl bins” shows the average 95% UL for the six nearest neighboring frequency subbands as a rough guide to the expected value in the absence of an injection (or true signal).

The last column states whether or not the injection survives all stages of loose-coherence follow-up. As hoped, all five injections with a true $h_0$ amplitude above the expected background estimation of the UL do survive these follow-up stages, as do two additional injections with somewhat smaller amplitudes.

### IV. SEARCH RESULTS

Carrying out the stage-0 analysis described above leads to a set of all-sky upper limits (95% C.L.) on strain.
amplitude for worst-case, linear polarization (relative stellar spin orientation) and for best-case, circular polarization. That analysis also leads to an initial set of outliers for follow-up with later analysis stages. Whether or not a particular narrow frequency band contains an outlier, the upper limits obtained remain valid. As shown in Table IV, hardware injections were reliably recovered when their injected strain was at least 0.7 times the recorded upper limit.

FIG. 6. Shaded regions (yellow) overlaid on the run-averaged spectra (inverse-noise weighted) from the H1 (magenta) and L1 (blue) O3a datasets indicate vetoed bands for which outlier follow-up is impeded by artifacts. The widest affected bands correspond to test-mass “violin modes” (ambient vibrations of the silica fibers from which LIGO mirrors are suspended) near multiples of 500 Hz. Top panel: Full 20–2000 Hz band. Bottom panel: Magnification of example 1900–2000 Hz band, for which line artifacts are dominated by the 4th harmonics of violin modes. (color online).
limit (and in one case as low as 0.34 times the upper limit). The upper limits obtained from stage-0 analysis are presented in section IVA, along with corresponding astrophysical sensitivities. Section IVB presents the results of outlier follow-up.

A. Upper limits and sensitivity

Figure 4 shows the upper limits obtained in this search as three curves, along with results from other all-sky searches in the O2 dataset [12–17]. The upper (blue) curve shows the upper limits for a worst-case (linear) polarization. The lowest (red) curve shows upper limits for an optimally oriented source (circular polarization). Both curves represent strict frequentist upper limits on these worst-case and best-case orientations with respect to location on the sky, spin-down and frequency within each narrow search band. For sensitivity comparisons with the previous O2 results, the intermediate (green) curve represents approximate population-averaged upper limits (over random sky locations and polarizations) and is derived from the circular polarization curve with a simple scale factor (2.3), based on injection studies in test bands.

Each linear-polarization or circular-polarization point in the search is considered in a maximum over the sky, except for a small excluded portion of the sky near the ecliptic poles, which is highly susceptible to detector artifacts due to stationary frequency evolution produced by the combination of frequency derivative and Doppler shifts [5].

The O3a results presented here improve upon the previous O2 results in strain sensitivity with factors ranging from ∼1.2 at signal frequencies of ∼100 Hz to ∼2.0 at higher frequencies below the 1475-Hz breakpoint. The improvements at high frequencies come in part from the improved detector noise achieved with quantum squeezing [19] and in part from using longer Fourier transform coherence times than were used in the similar O2 analyses. At frequencies below ∼40 Hz, the O2 data was badly contaminated by instrumental lines [30], leading to poorer upper limits, and in some bands, precluding reliable upper limits using the method of [13]. The dramatically improved sensitivities obtained for low frequencies in this analysis come in part from mitigation of many spectral lines between the O2 and O3 runs, especially in the L1 interferometer, and in part from the use here of the “universal statistic” described in section III C.

One can recast these upper limits on source amplitude as lower limits on the range at which neutron stars with assumed equatorial ellipticity can reside. Figure 5 shows the ranges (kpc) of this search (circular-polarization and population-averaged) vs. frequency for assumed equatorial ellipticity values $\epsilon = 10^{-4}$, $10^{-6}$ and $10^{-8}$ and under the assumption that the total stellar spin-down magnitude does not exceed the $10^{-8}$ Hz/s maximum used in this search. The population-averaged ranges from prior O2 searches of comparable parameter space coverage [12,13] are also shown for these ellipticities. One sees a gain in range with respect to O2 analyses over the full frequency band, with the greatest improvements seen at highest frequencies, as expected. The number of accessible neutron stars is expected to rise at least quadratically as the range extends out into the plane of the galaxy and approaches the denser regions near its center, at a distance of ∼8.5 kpc, enhancing the detection probabilities from these range gains.

For reference, Fig. 5 also shows this search’s implied maximum ranges vs. frequency for a “gravitar” (star with spin-down dominated by gravitational radiation) for maximum spin-down magnitudes of $10^{-8}$, $10^{-10}$ and $10^{-12}$ Hz/s. If a neutron star’s spin-down has major contributions from electromagnetic radiation, the range to which this search is sensitive for fixed $\epsilon$ may be reduced by the choice of maximum spin-down permitted. Conversely, searching for spin-down magnitudes much higher than expected for a gravitar of given $\epsilon$ could allow detection of a star with more realistic emission contributions.

TABLE VII. Parameters of the outliers surviving stage-2 follow-up, but discarded after visual inspection of a strain histogram confirmed instrumental contamination. Each outlier listed is the loudest after clustering in frequency, spin-down and sky location. Figure 7 shows a strain histogram example.

<table>
<thead>
<tr>
<th>$f$ (Hz)</th>
<th>$df/dt$ (nHz/s)</th>
<th>R.A. (radians)</th>
<th>Dec. (radians)</th>
</tr>
</thead>
<tbody>
<tr>
<td>32.5982</td>
<td>0.442</td>
<td>4.225</td>
<td>0.342</td>
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<tr>
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<td>1838.6522</td>
<td>−7.700</td>
<td>1.039</td>
<td>−0.808</td>
</tr>
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</table>
**B. Outliers**

Outliers seen in the stage-0 search are followed up with loose-coherence stages of increasing effective coherence time, as described in section III D, with the SNR expected to increase for true signals. Table V shows the counts of outliers seen at each stage for major sub-bands. In the presence of Gaussian noise and no signal, one expects the outlier counts to decrease monotonically with increasing stage as SNR increases are required for each advancement. For particular sub-bands, however, one can see count increases from at least two contributions, both associated with the finer sampling of parameter space in successive stages. 1) Hardware injections (section III E) from a simulated signal naturally satisfy the SNR increase requirements demanded of a signal; and 2) stationary line artifacts of finite bandwidth can be compatible with signal templates having limited Doppler modulation or having partial cancellation between seasonal modulation and assumed frequency derivative for a certain region of the sky [3].

In the extreme, the number of outliers produced by a particular instrumental artifact can be so large as to make systematic follow-up impracticable and pointless. Table VI shows particular frequency bands (about 13% of the original search band) for which no outlier follow-up is attempted for the initial or later stages because of instrumental artifacts that lead to such an unmanageable flood of initial or later-stage outliers. The table includes the stage for which the vetos are applied in order to reduce artifact-induced outlier counts. Artifacts include loud mechanical resonances, such as higher harmonics of violin modes, and especially loud hardware injections. The widest bands excluded lie in the regions of test-mass violin modes and their higher harmonics. Figure 6 shows these vetoed regions over the full search band, with a magnification of an example 100-Hz band (1900–2000 Hz) that includes a “forest” of 4th harmonics of violin modes from both interferometers. For the narrow search bands affected by loud hardware injections, only outliers within 1.0 radian of the injection’s sky location are excluded, except for the top 20 (highest SNR), which are followed up to verify successful injection recovery.

Nearly all outliers that survived all stages of the loose-coherence follow-up correspond to hardware injections (see Table IV) or lie in highly disturbed bands, for which contamination of the putative signal by an instrumental spectral line is apparent. To identify these contaminations, we construct “strain histograms” in which the summed power over the observation period from a simulation of the nominal signal candidate is superposed on a background estimate of the noise estimated via interpolation between neighboring frequency bands. Except for signal templates with high-magnitude spin-downs, the histograms typically display at least one “horn” (narrow peak) from an epoch.

---

**FIG. 7.** Example of a “strain histogram” graph used in vetoing outliers surviving stage-2 follow-up for which instrumental contamination is apparent. The solid curves show the O3a-run-averaged H1 (red) and L1 (blue) amplitude spectral densities in a narrow band containing an artifact at 1740.39 Hz. The dotted curves show histograms of expected strain excess from H1 (black) and L1 (magenta) signal templates added to smooth backgrounds interpolated from neighboring frequency bands. In this depiction, the strain amplitude of the signal template has been magnified to make its structure clear. The large excess power in the L1 data, not seen in the H1 data, despite comparable strain sensitivities and comparable sidereal-averaged antenna pattern sensitivities to any point in the sky, excludes an astrophysical source for the L1 artifact. The fact that the artifact aligns in frequency with the putative signal’s template peak in power confirms contamination of the outlier from an instrumental source. (color online).
We have performed the most sensitive all-sky search to date for continuous gravitational waves in the range 20–2000 Hz while probing spin-down magnitudes as high as $10^{-8}$ Hz/s, using the powerflux search program with loose coherence. The overall improvements in strain sensitivity come primarily from the improved noise floors of the Advanced LIGO interferometers over previous LIGO datasets. Improvements in strain sensitivity over our previous O2 results range from a factor of 1.2 at $\sim$100 Hz to $\sim$2 at $\sim$2000 Hz, with still larger improvements at the lowest frequencies for which spectral line artifacts degraded O2 results.

No credible gravitational wave signals are observed, allowing upper limits to be placed on possible source signal amplitudes. Fig. 4 shows the strain amplitude upper limits obtained. The lowest upper limits on worst-case (linearly polarized) strain amplitude $h_0$ are $\sim 1.7 \times 10^{-25}$ near 200 Hz. For a circularly polarized source (most favorable orientation), the smallest upper limits are $\sim 6.3 \times 10^{-26}$. These upper limits refer to all sky locations and the entire range of frequency derivative values. For a population-averaged ensemble of sky locations and stellar orientations, the lowest 95% CL upper limits on the strain amplitude are $\sim 1.4 \times 10^{-25}$.

At the highest frequencies ($\sim$2000 Hz) we are sensitive to neutron stars with an equatorial ellipticity $\epsilon$ as small as $4 \times 10^{-7}$ and as far away as 6 kpc for favorable spin orientations (see Fig. 5). For a higher ellipticity $\epsilon = 10^{-6}$ and favorable spin orientations, we are sensitive to neutron stars beyond the galactic center. The maximum ellipticity that a conventional neutron star can theoretically support is at least $1 \times 10^{-5}$ according to [44,45]. Our results are sensitive to such maximally deformed pulsars above 100 Hz pulsar rotation frequency (200 Hz gravitational-wave frequency) within 3 kpc. Outliers from initial stages of each search method are followed up systematically, but no candidates from any search survived scrutiny.

A recent, similar all-sky search of the LIGO O2 data [15–17], over the same frequency range (20–2000 Hz), but severely restricted in spin-down range ($|\dot{f}| < 3 \times 10^{-12}$ Hz/s), achieved better strain sensitivity (improvements ranging from $\sim$30% lower at 500 Hz to $\sim$15% lower at 1500 Hz) by using loose coherence with an effective coherence time of 12 hours in its initial search stage, at a substantially higher computational cost than that of this analysis. A similar approach [18], but further restricting the search frequency range to 171–172 Hz, also achieved a higher sensitivity $h_0 \sim 1.07 \times 10^{-25}$ at 95% confidence. Figure 5 illustrates the potential gain in ellipticity and range sensitivity from searching for high-spin-down magnitudes. A recent deep search of the O2 data using the distributed-computing project Einstein@Home [14] over the frequency band 20–585.15 Hz and spindown magnitude up to $2.6 \times 10^{-9}$ Hz/s achieved similar sensitivity to this search over the common search parameter space, quoting 90% CL upper limits slightly lower than the 95% CL values presented here. Figure 4 shows the strain upper limits achieved in this O3a
search and in the previous O2 searches, and Fig. 1 shows a comparison of their parameter space coverages.

As the LIGO, Virgo and KAGRA gravitational wave detectors improve their strain sensitivities in the coming decade [46], searches will probe still smaller neutron star deformations and explore further out into the galaxy.

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