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Adaptive Multiscale Molecular Dynamics of Macromolecular Fluids

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Until now, adaptive atomistic–coarse-grain (A/CG) molecular dynamics simulations have had very limited applicability because the on-the-fly CG → A transformation is problematic for all but those molecules whose CG representation consists of a single particle. Here, we solve this problem by combining a transitional healing region with a rotational dynamics of rigid atomistic fragments in the CG region. Error control is obtained by analysis of the A → CG energy flow. We illustrate the method with adaptive multiscale simulations of liquid hexane and of a dilute polymer solution in a theta solvent.

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Multiscale molecular dynamics (MMD) holds great promise for the modeling of the wide variety of newly discovered phenomena that display an inherent multiscale character [1–5]. Examples include membrane fusion, ion diffusion in polymer electrolytes, signal transduction between proteins, nanostructure formation on surfaces, flexible protein-ligand docking, and phase transitions in organic crystals. MMD would complement experiments by interpreting and linking the mesoscale phenomena to the underlying fundamental atomic motions and is thus expected to have an important impact on research fields ranging from polymer physics and surface science to biophysics and drug discovery.

Apart from the expected physical insight from its applications, MMD also raises various statistical mechanics issues by itself that are very exciting to address. For example, what does it mean to simulate a system partly in atomistic detail and partly at a CG level; how should particles adapt their resolution when they diffuse between an atomistic region (AR) and a coarse-grain region (CGR), and what ensemble does such a hybrid simulation sample? These and many other questions have been addressed by us and others with detailed MMD studies of toy models during the last five years [6–12].

Although these efforts have led to several MMD approaches as well as a wealth of understanding, until now none of these hybrid methods have been shown to work for realistic soft matter systems, due to a fundamental difficulty related to the reverse mapping of a CG model to its atomistic representation. That is, the current approach of using an intermediate healing region (HR) to smoothly (re-) insert the chemical details into CG particles that leave the CGR and enter the AR unfortunately only works in practice for simple systems with spherical CG molecules, such as methane [7] and water [13]. MMD of molecules that are represented by several bonded CG particles requires an unwrokably large HR or additional reverse mapping techniques. Clearly this reverse mapping problem has held back MMD of soft matter systems but also further study of the statistical mechanics implications of MMD at higher levels of coarse graining.

In this Letter, we present a hybrid molecular dynamics method that implements the adaptive A/CG coupling for general molecular systems in an efficient manner. We solve the reverse mapping problem by combining the healing region approach with an auxiliary rotational dynamics of atomistic fragments in the HR and CGR. The rotational dynamics maintains near-optimal orientations of the fragments with respect to their CG molecular frame which preconditions reverse mapping taking place in the HR. This dynamical preconditioning is distinct from other recent reverse mapping methods in which restrained optimization or simulated annealing calculations reoptimize the atomistic degrees of freedom [14–16]. This would be too computationally demanding here. Rather, the rotational dynamics is analogous to the rotamer library approach used in the protein community to restore atomistic structure [17]. Hereafter we show that our novel MMD algorithm has some appealing properties, such as conservation of momentum and error control through conservation of a total energy function despite the continuously fluctuating number of degrees of freedom and the nonequilibrium dynamics in the HR.

Prerequisites for a MMD simulation include an atomistic and a CG model of the system, a mapping between groups of atoms and the CG particles, and a choice for the spatial partitioning of the system into high- and low-resolution regions. The atomistic and CG models should be parametrized to represent the same thermodynamic state (e.g., temperature and pressure), such that the molecules have the same average chemical potential in either representation [18]. In the AR and HR, the inactive CG positions are updated from the center of mass positions of the corresponding atom groups. In the CGR, the inactive...
atom groups are frozen and treated as rigid bodies that follow the CG particles and rotate according to an auxiliary rotational dynamics.

For the rotation of the frozen fragments in the CGR, we make use of an SO(3) integrator which is the velocity Verlet algorithm for rotational dynamics [19]. Given an initial angular velocity \( \omega_0 \) and angular acceleration \( \alpha_0 \), the dynamics occurs in a 4-step loop with a time step \( \tau \):

1. \( \omega'_n = \omega_{n-1} + \tau \alpha_{n-1} \)
2. \( R_n = \exp(\tau J(\omega'_n)) \)
3. \( I_n \alpha_n - t_n + \left( \omega'_n + \frac{\tau}{2} \alpha_n \right) \times I_n \left( \omega'_n + \frac{\tau}{2} \alpha_n \right) = 0 \)
4. \( \omega_n = \omega'_n + \frac{\tau}{2} \alpha_n \).

Steps 1 and 4 are the velocity half-steps. In step 2 the operator \( J \) is used to transform the angular velocity into a skew symmetric matrix which is then scaled by the time step \( \tau \). This scaled matrix [which is technically an element of the Lie algebra so(3) corresponding to the Lie group SO(3)] represents the vector in the tangent space of SO(3) along which we should step. However, since SO(3) is a curved manifold, we must apply the exponential map to this vector to obtain a rotation matrix \( R_n \) which is used to update the atom positions relative to their centers of mass. In step 3, first the moment of inertia tensor \( I_n \) is updated and then the forces are evaluated to obtain the torque \( t_n \). With the new moment of inertia tensor and the new torque the angular acceleration is computed using Newton’s root finding method to be consistent with the angular velocity.

The rotational dynamics is governed by a potential energy function \( V^{\text{rot}} \) that consists of a subset of the atomistic force field, such as the bond and bend and dispersion potentials between atoms that span neighboring CG particles [20]. These interactions produce the torques \( t_n \) on the frozen atomic fragments causing them to rotate and follow the orientation of the moving (CG) molecules. The total potential energy of the mixed A/CG dynamics plus rotational dynamics is

\[
E = T^A + T^{CG} + T^{rot} + V^{A/CG}_{\text{intra}} + V^{A/CG}_{\text{inter}} + V^{\text{rot}} + \Delta T^{A/CG} + \Delta U^{A/CG}_{\text{intra}} + \Delta U^{A/CG}_{\text{inter}}.
\]

Here, the first three terms are the atomistic kinetic energy (from the AR and HR), the CG kinetic energy (from the CGR), and the kinetic energy of the rotating fragments (in the CGR). The A/CG potential energy is separated into \( V^{A/CG}_{\text{intra}} \) due to the intra-CG bead atomistic interactions, and \( V^{A/CG}_{\text{inter}} \) due to the A and CG interactions that span different CG beads. The latter interactions between each pair of beads \( \alpha \) and \( \beta \) are composed of the CG pair potentials \( \Phi_{\alpha\beta}^{CG} \) mixed with the pair potentials between atoms \( i \) (belonging to bead \( \alpha \)) and atoms \( j \) (belonging to bead \( \beta \)):

\[
V^{A/CG}_{\text{inter}} = \sum_{\alpha\beta} \left( \lambda_{\alpha\beta} \Phi_{\alpha\beta}^{CG} + (1 - \lambda_{\alpha\beta}) \sum_{j,\beta} \Phi_{ij}^A \right).
\]

Here, \( \lambda \) is a scaling function that switches smoothly from zero to one for particles in the HR [7]. The intra-CG bead atomistic interactions are not scaled, which would otherwise require introduction of fractional degrees of freedom and complicated thermostats to avoid the molecules from disintegrating in the HR [10,21]. The last three terms are bookkeeping terms that allow us to recover the total energy as a conserved quantity. A derivation of the adaptive coupling is found in the supplementary information [22].

The bookkeeping terms for the kinetic energy and the intra-CG bead potential energy collect the surplus energy of the atomistic degrees of freedom that is removed from the system when the atoms are frozen and replaced by a CG bead upon leaving the HR. Vice versa, when a CG bead enters the HR and the atomistic dynamics takes over, the surplus energy is released from \( \Delta T^{A/CG} \) and \( \Delta U^{A/CG}_{\text{intra}} \). The inter-CG bead interactions are gradually replaced in the HR, so that the bookkeeping of the instantaneous surplus energy takes the form

\[
\Delta U^{A/CG}_{\text{inter}} = \sum_{\alpha} \int dr \sum_{\beta > \alpha} \frac{\partial \lambda_{\alpha\beta}}{\partial r} \left( \Phi_{\alpha\beta}^{CG} - \sum_{j,\beta} \Phi_{ij}^A \right).
\]

with \( r \) the position of the CG particle [23]. It is important to note that Eq. (3) not only provides an efficient means to recover the total energy as a conserved quantity, but also that its derivatives \( -\nabla \Delta U^{A/CG}_{\text{inter}} \) exactly cancel the \( \partial \lambda / \partial r \) terms included in the thermodynamic forces, \( -\nabla V \), which would otherwise cause a particle flux across the HR and impair total momentum conservation. Note also that this total energy does not resemble a physical observable because the bookkeeping terms continuously reset the reference for the energy scale. This is in a sense analogous to the Nose-Hoover “potential energy” of the thermostat, which is added to book-keep the energy flow between the system and the thermostat and to recover the energy as conserved quantity [24].

To complete the implementation of the rotational dynamics within the hybrid A/CG MD, two technical aspects require special attention. First, the CG dynamics must be back-coupled to the rotational dynamics to maintain stability and energy conservation. CG bond vibration (see panel B in Fig. 1), which would pump energy into the rotational dynamics in the absence of backcoupling, is removed from the torque evaluation by renormalizing the CG bond to its equilibrium distance; in this manner the CG dynamics is not perturbed by the stiff atomistic bonds. On the other hand, a rotational CG motion, for example, due to intramolecular bending (panel C in Fig. 1), cannot be removed from the torque evaluation as this would defeat the purpose of orienting the fragments. Here the proper backcoupling is added which causes torque on the CG particles (see panel C in Fig. 1) [25]. Second, the rotational dynamics
is gradually replaced by the atomistic interactions in the HR, simply by adding the forces from torques to the atomistic MD forces, after scaling by $C^2$ and removing the fragment center of mass translational component.

We illustrate our novel adaptive MMD algorithm with two examples. Our first example is liquid hexane in which the different resolution regions are 2D slabs. The system was initialized from a CG isothermal-isobaric simulation (303 K and 1 atm) to obtain 1900 equilibrated hexane molecules in a rectangular box with initial dimensions $60 \times 60 \times 120 \text{ Å}$. At the CG level hexane molecules consist of two beads connected with a harmonic spring; dispersion is modeled using a 9-6 Lennard-Jones pair potential [26]. Atomistic (frozen) $\text{C}_3\text{H}_7$ fragments were positioned over each CG bead, after which the rotational dynamics energy function was minimized. To drive the rotational dynamics, a subset of the atomistic force field was employed consisting of the atomistic bond between CG beads and the WCA repulsive potential between the hydrogen atoms attached to the carbon atoms involved in this bond [27]. The AR is selected to be a 2D slab with a thickness of 24 Å centered on an immobilized dummy atom. The atomistic molecules are fully flexible using the CHARMM force field without electrostatics [28]. Short, 50 ps, $NVT$ MMD simulations were performed to further equilibrate the atomistic degrees of freedom in the AR and HR, followed by several MMD simulations in which we varied the HR width between 1 and 6 Å. Figure 2 shows the total energy of Eq. (1) (offset for comparison) during the first 100 ps of each simulation. Excellent stability of $E$ is observed with a 3 Å HR width or greater. The irregular curve shows the erratic result obtained from MMD without the rotational dynamics.

Our second example is the swelling of a $\text{C}_{450}\text{H}_{902}$ (150 CG beads) polyethylene chain in a theta solvent of liquid hexane. The system was prepared by immersing a densely coiled polymer chain, taken from a 10 ns CG simulation of the chain in vacuum, in a cubic box containing 1900 hexane molecules. The CG force field is identical to the hexane slab system. The solvent was equilibrated with the chain fixed, after which atomistic fragments were introduced as above. To study swelling (due to the penetration of solvent molecules) at different resolutions, a spherical AR with a radius of 10 Å was centered at the 75th CG bead of the polymer and a 5 Å HR was used. The MMD
shows how the number of solvent carbon atoms within the CW VIDI grant. The algorithm applicable to general soft matter systems. This allows us to choose an optimal time step and HR information on the derivation of the adaptive coupling. The torque on the CG particles effectively stiffens the CG dynamics which is thus parametrized to minimize disturbances to the CG dynamics.

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[18] However, our method also works if the two models do not match, in which case molecules will flow from one region to the other until a new (unphysical) equilibrium is reached with different densities in the AR and CGR.
[23] To be precise, since \( \lambda \) is in practice defined by the interacting particle (\( \alpha \) or \( \beta \)) that has the greatest CG character, here \( r \) is the position of that particle determining the value of \( \lambda \). See Ref. [7] for details.
[25] The torque on the CG particles effectively stiffens the CG bend potential which is thus parametrized to minimize disturbances to the CG dynamics.